

INTRODUCTION

---

Message Passing Programming

# MPI Users' Guide in FORTRAN

INTRODUCTION TO MESSAGE PASSING PROGRAMMING

# MPI User Guide in FORTRAN

---

Dr Peter S. Pacheco  
Department of Mathematics  
University of San Francisco  
San Francisco, CA 94117  
March 26, 1995

Woo Chat Ming  
Computer Centre  
University of Hong Kong  
Hong Kong  
March 17, 1997

---

<b>1. INTRODUCTION .....</b>	<b>2</b>
<b>2. GREETINGS ! .....</b>	<b>3</b>
2.1 GENERAL MPI PROGRAMS .....	4
2.2 FINDING OUT ABOUT THE REST OF THE WORLD .....	5
2.3 MESSAGE : DATA + ENVELOPE .....	6
2.4 MPI_SEND AND MPI_RECV .....	7
<b>3. AN APPLICATION .....</b>	<b>9</b>
3.1 SERIAL PROGRAM .....	9
3.2 PARALLELIZING THE TRAPEZOID RULE .....	10
3.3 I/O ON PARALLEL PROCESSORS .....	14
<b>4. COLLECTIVE COMMUNICATION .....</b>	<b>17</b>
4.1 TREE-STRUCTURED COMMUNICATION .....	17
4.2 BROADCAST .....	19
4.3 REDUCE .....	20
4.4 OTHER COLLECTIVE COMMUNICATION FUNCTIONS .....	22
<b>5. GROUPING DATA FOR COMMUNICATION .....</b>	<b>24</b>
5.1 THE COUNT PARAMETER .....	24
5.2 DERIVED TYPES AND MPI_TYPE_STRUCT .....	25
5.3 OTHER DERIVED DATATYPE CONSTRUCTORS .....	28
5.4 PACK/UNPACK .....	29
5.5 DECIDING WHICH METHOD TO USE .....	31
<b>6. COMMUNICATORS AND TOPOLOGIES .....</b>	<b>34</b>
6.1 FOX'S ALGORITHM .....	34
6.2 COMMUNICATORS .....	35
6.3 WORKING WITH GROUPS, CONTEXTS, AND COMMUNICATORS .....	37
6.4 MPI_COMM_SPLIT .....	40
6.5 TOPOLOGIES .....	41
6.6 MPI_CART_SUB .....	44
6.7 IMPLEMENTATION OF FOX'S ALGORITHM .....	44
<b>7. WHERE TO GO FROM HERE .....</b>	<b>48</b>
7.1 WHAT WE HAVEN'T DISCUSSED .....	48
7.2 IMPLEMENTATIONS OF MPI .....	49
7.3 MORE INFORMATION ON MPI .....	49
7.4 THE FUTURE OF MPI .....	50
<b>8. COMPILING AND RUNNING MPI PROGRAMS .....</b>	<b>51</b>
<b>9. REFERENCE .....</b>	<b>52</b>

---

# 1. Introduction

**T**he Message-Passing Interface or MPI is a library of functions and macros that can be used in C, FORTRAN, and C++ programs. As its name implies, MPI is intended for use in programs that exploit the existence of multiple processors by message-passing.

MPI was developed in 1993-1994 by a group of researchers from industry, government, and academia. As such, it is one of the first standards for programming parallel processors, and it is the first that is based on message-passing.

In 1995, *A User's Guide to MPI* has been written by Dr Peter S. Pacheco. This is a brief tutorial introduction to some of the more important features of the MPI for C programmers. It is a nicely written documentation and users in our university find it very concise and easy to read.

However, many users of parallel computer are in the scientific and engineers community and most of them use FORTRAN as their primary computer language. Most of them don't use C language proficiently. This situation occurs very frequently in Hong Kong. As a result, the "*A User's Guide to MPI*" is translated to this guide in Fortran to address for the need of scientific programmers.

**Acknowledgments.** I gratefully acknowledge Dr Peter S. Pacheco for the use of C version of the user guide on which this guide is based. I would also gratefully thank to the Computer Centre of the University of Hong Kong for their human resource support of this work. And I also thank to all the research institution which supported the original work by Dr Pacheco.

---

## 2. Greetings !

The first program that most of us saw was the “Hello, world!” program in most of introductory programming books. It simply prints the message “Hello, world!”. A variant that makes some use of multiple processes is to have each process send a greeting to another process.

In MPI, the process involved in the execution of a parallel program are identified by a sequence of non-negative integers. If there are  $p$  processes executing a program, they will have ranks 0, 1,...,  $p-1$ . The following program has each process other than 0 send a message to process 0, and process 0 prints out the messages it received.

```
program greetings
include 'mpif.h'

integer my_rank
integer p
integer source
integer dest
integer tag
character*100 message
character*10 digit_string
integer size
integer status(MPI_STATUS_SIZE)
integer ierr
call MPI_Init(ierr)
call MPI_Comm_rank(MPI_COMM_WORLD, my_rank, ierr)
call MPI_Comm_size(MPI_COMM_WORLD, p, ierr)
if (my_rank .NE. 0) then
  1write(digit_string,FMT="(I3)") my_rank
  message = 'Greetings from process '
+  2// trim(digit_string) // ' !'
  dest = 0
  tag = 0
  call MPI_Send(message, len_trim(message)3,
+  MPI_CHARACTER, dest, tag, MPI_COMM_WORLD, ierr)
else
  do source = 1, p-1
    tag = 0
    call MPI_Recv(message, 100, MPI_CHARACTER,
```

---

<sup>1</sup> This line changes the binary format (integer) `my_rank` to string format `digit_string`.

<sup>2</sup> `//` is concatenation operator which combines two strings to form a third, composite string. E.g. `'This ' // 'is ' // 'a ' // 'dog.'` is equal to the string `'This is a dog.'`

<sup>3</sup> `LEN_TRIM(STRING)` returns the length of the character argument without counting trailing blank.

```

+         source, tag, MPI_COMM_WORLD, status, ierr)
        write(6,FMT="(A)") message
    enddo
endif

call MPI_Finalize(ierr)
end program greetings

```

The details of compiling and executing this program is in chapter 8.

When the program is compiled and run with two processes, the output should be

```
Greetings from process 1!
```

If it's run with four processes, the output should be

```
Greetings from process 1!
Greetings from process 2!
Greetings from process 3!
```

Although the details of what happens when the program is executed vary from machine to machine, the essentials are the same on all machines. Provided we run one process on each processor.

1. The user issues a directive to the operating system which has the effect of placing a copy of the executable program on each processor.
2. Each processor begins execution of its copy of the executable.
3. Different processes can execute different statements by branching within the program. Typically the branching will be based on process ranks.

So the **Greetings** program uses the *Single Program Multiple Data* or *SPMD* paradigm. That is, we obtain the *effect* of different programs running on different processors by taking branches within a single program on the basis of process rank : the statements executed by process 0 are different from those executed by the other processes, even though all processes are running the same program. This is the most commonly used method for writing MIMD programs, and we'll use it exclusively in this Guide.

## 2.1 General MPI Programs

Every MPI program must contain the preprocessor directive

```
include 'mpif.h'
```

This file, `mpif.h`, contains the definitions, macros and function prototypes necessary for compiling an MPI program.

Before any other MPI functions can be called, the function `MPI_Init` must be called, and it should only be called once. Fortran MPI routines have an `IERROR` argument - this contains the error code. After a program has finished using MPI library, it must call `MPI_Finalize`. This cleans up any “unfinished business” left by MPI - e.g. pending receives that were never completed. So a typical MPI program has the following layout.

```
.  
.   
.   
include 'mpif.h'  
.   
.   
call MPI_Init(ierr)  
.   
.   
call MPI_Finalize(ierr)  
.   
.   
end program
```

## 2.2 Finding out About the Rest of the World

MPI provides the function `MPI_Comm_rank`, which returns the rank of a process in its second in its second argument, Its syntax is

```
CALL MPI_COMM_RANK(COMM, RANK, IERROR)  
INTEGER COMM, RANK, IERROR
```

The first argument is a *communicator*. Essentially a communicator is a collection of processes that can send message to each other. For basic programs, the only communicator needed is `MPI_COMM_WORLD`. It is predefined in MPI and consists of all the processes running when program execution begins.

Many of the constructs in our programs also depend on the number of processes executing the program. So MPI provides the functions `MPI_Comm_size` for determining this. Its first argument is a communicator. It returns the number of processes in a communicator in its second argument. Its syntax is

```
CALL MPI_COMM_SIZE(COMM, P, IERROR)  
INTEGER COMM, P, IERROR
```

## 2.3 Message : Data + Envelope

The actual message-passing in our program is carried out by the MPI functions `MPI_Send` and `MPI_Recv`. The first command sends a message to a designated process. The second receives a message from a process. These are the most basic message-passing commands in MPI. In order for the message to be successfully communicated the system must append some information to the data that the application program wishes to transmit. This additional information forms the *envelope* of the message. In MPI it contains the following information.

1. The rank of the receiver.
2. The rank of the sender.
3. A tag.
4. A communicator.

These items can be used by the receiver to distinguish among incoming messages. The *source* argument can be used to distinguish messages received from different processes. The *tag* is a user-specified integer that can be used to distinguish messages received from a single process. For example, suppose process *A* is sending two messages to process *B*; both messages contain a single real number. One of the real numbers is to be used in a calculation, while the other is to be printed. In order to determine which is which, *A* can use different tags for the two messages. If *B* uses the same two tags in the corresponding receives, when it receives the messages, it will “know” what to do with them. MPI guarantees that the integers 0-32767 can be used as tags. Most implementations allow much larger values.

As we noted above, a communicator is basically a collection of processes that can send messages to each other. When two processes are communicating using `MPI_Send` and `MPI_Recv`, its importance arises when separate modules of a program have been written independently of each other. For example, suppose we wish to solve a system of differential equations, and, in the course of solving the system, we need to solve a system of linear equations. Rather than writing the linear system solver from scratch, we might want to use a *library* of functions for solving linear systems that was written by someone else and that has been highly optimized for the system we’re using. How do we avoid confusing the messages we send from process *A* to process *B* with those sent by the library functions? Before the advent of communicators, we would probably have to partition the set of valid tags, setting aside some of them for exclusive use by the library functions. This is tedious and it will cause problems if we try to run our program on another system: the other system’s linear solver may not (probably won’t) require the same set of tags. With the advent of communicators, we simply create a communicator that can be used exclusively by the linear solver, and pass it as an argument in calls to the solver. We’ll discuss the details of this later. For now, we can get away with using the predefined communicator `MPI_COMM_WORLD`. It consists of all the processes running the program when execution begins.



## 2.4 MPI\_Send and MPI\_Recv

To summarize, let's detail the syntax of `MPI_Send` and `MPI_Recv`.

```
MPI_SEND( MESSAGE, COUNT, DATATYPE, DEST, TAG, COMM, IERROR)
<TYPE> MESSAGE( *)
INTEGER COUNT, DATATYPE, DEST, TAG, COMM, IERROR

MPI_RECV( MESSAGE, COUNT, DATATYPE, SOURCE, TAG,
COMM, STATUS, IERROR)
<TYPE> MESSAGE( *)
INTEGER COUNT, DATATYPE, DEST, TAG, COMM
INTEGER STATUS(MPI_STATUS_SIZE), IERROR
```

Most MPI functions stores an integer error code in the argument `ierror`. However, we will ignore these return values in most cases.

The contents of the message are stored in a block of memory referenced by the argument **message**. The next two arguments, **count** and **datatype**, allow the system to identify the end of the message : it contains a sequence of **count** values, each having *MPI* type **datatype**. This type is not a Fortran type, although most of the predefined types correspond Fortran types. The predefined MPI types and the corresponding FORTRAN types (if they exist) are listed in the following table.

MPI datatype	FORTTRAN datatype
MPI_INTEGER	INTEGER
MPI_REAL	REAL
MPI_DOUBLE_PRECISION	DOUBLE PRECISION
MPI_COMPLEX	COMPLEX
MPI_LOGICAL	LOGICAL
MPI_CHARACTER	CHARACTER(1)
MPI_BYTE	
MPI_PACKED	

The last two types, `MPI_BYTE` and `MPI_PACKED`, don't correspond to standard Fortran types. The `MPI_BYTE` type can be used if you wish to force the system to perform no

conversion between different data representations ( e.g. on a heterogeneous network of workstations using different representations of data). We'll discuss the type `MPI_PACKED` later.

Note that the amount of space allocated for the receiving buffer does not have to match the exact amount of space in the message being received. For example, when our program is run, the size of the message that process 1 sends, `len_trim(message)`, is 28 characters, but process 0 receives the message in a buffer that has storage for 100 characters. This makes sense. In general, the receiving process may not know the exact size of the message being sent. So MPI allows a message to be received as long as there is sufficient storage allocated. If there isn't sufficient storage, an overflow error occurs [4].

The arguments `dest` and `source` are, respectively, the ranks of the receiving and the sending processes. MPI allows `source` to be "wildcard". There is a predefined constant `MPI_ANY_SOURCE` that can be used if a process is ready to receive a message from *any* sending process rather than a particular sending process. There is *not* a wildcard for `dest`.

As we noted earlier, MPI has two mechanisms specifically designed for "partitioning the message space" : tags and communicators. The arguments `tag` and `comm` are, respectively, the tag and communicator. The `tag` is an integer, and for now, our only communicator is `MPI_COMM_WORLD`, which, as we noted earlier is predefined on all MPI systems and consists of all the processes running when execution of the program begins. There is a wildcard, `MPI_ANY_TAG`, that `MPI_Recv` can use for the tag. There is *no* wildcard for the communicator. In other words, in order for process *A* to send a message to process *B*, the argument `comm` that *A* uses in `MPI_Send` must be identical to the argument that *B* uses in `MPI_Recv`.

The last argument of `MPI_Recv`, `status`, returns information on the data that was actually received. It references a array with two elements - one for the source and one for the tags. So if, for example, the `source` of the receive was `MPI_ANY_SOURCE`, then `status` will contain the rank of the process that sent the message.

## 3. An Application

Now that we know how to send message with MPI, let's write a program that uses message-passing to calculate a definite integral with the trapezoid rule.

### 3.1 Serial program

Recall that the trapezoid rule estimates  $\int_a^b f(x)dx$  by dividing the interval  $[a,b]$  into  $n$  segments of equal and calculating the following sum.

$$h[f(x_0)/2 + f(x_n)/2 + \sum_{i=1}^{n-1} f(x_i)].$$

Here,  $h = (b - a)/n$ , and  $x_i = a + ih$ ,  $i = 0, \dots, n$ .

By putting  $f(x)$  into a subprogram, we can write a *serial* program for calculating an integral using the trapezoid rule.

```
C serial.f -- calculate definite integral using trapezoidal
C             rule.
C
C The function f(x) is hardwired.
C Input: a, b, n.
C Output: estimate of integral from a to b of f(x)
C         using n trapezoids.

      PROGRAM serial
      IMPLICIT NONE4
      real integral
      real a
      real b
```

---

<sup>4</sup> In Fortran, if you omit to declare a variable it will not normally lead to an error when it is first used; instead it will be implicitly declared to be an integer if the first letter of its name lies in the range I-N, and will be implicitly declared to be a real variable otherwise. *This is extremely dangerous, and must be avoided at all cost.*

Fortunately, Fortran 90 provides the means to avoid this problem by instructing the compiler that all variables *must* be declared before use, and that implicit declaration is not to be allowed. This is achieved by including the statement

```
IMPLICIT NONE
```

as the first statement after the initial PROGRAM, SUBROUTINE or FUNCTION statement.

*It is extremely important that this statement appears at the beginning of every program in order that implicit declarations of variables are forbidden.* There are a great many stories, some apocryphal and some true, about major catastrophes in Fortran programs that would never have happened had implicit declaration not masked a programming error.

```

integer n
real h
real x
integer i

real f
external f

print *, 'Enter a, b, and n'
read *, a, b, n

h = (b-a)/n
integral = (f(a) + f(b))/2.0
x = a
do i = 1, n-1
    x = x + h
    integral = integral + f(x)
enddo
integral = integral*h

print *, 'With n =', n, ' trapezoids, our estimate'
print *, 'of the integral from ', a, ' to ', b, ' = ',
+integral
end

C*****
real function f(x)
IMPLICIT NONE
real x
C Calculate f(x).

f = x*x
return
end
C*****

```

## 3.2 Parallelizing the Trapezoid Rule

One approach to parallelizing this program is to simply split the interval  $[a,b]$  up among the processes, and each process can estimate the integral of  $f(x)$  over its subinterval. In order to estimate the total integral, the processes' local calculations are added.

Suppose there are  $p$  processes and  $n$  trapezoids, and, in order to simplify the discussion, also suppose that  $n$  is evenly divisible by  $p$ . Then it is natural for the first process to calculate the area of the first  $n/p$  trapezoids, the second process to calculate the area of the next  $n/p$ , etc. So process  $q$  will estimate the integral over the interval

$$\left[ a + q \frac{nh}{p}, a + (q+1) \frac{nh}{p} \right]$$

Thus each process needs the following information.

- The number of processes,  $p$ .
- Its rank.
- The entire interval of integration,  $[a, b]$ .
- The number of subintervals,  $n$ .

Recall that the first two items can be found by calling the MPI functions `MPI_Comm_size` and `MPI_Comm_Rank`. The latter two items should probably be input by the user. But this can raise some difficult problems. So for our first attempt at calculating the integral, let's "hardwire" these values by simply setting their values with assignment statements.

A straightforward approach to summing the processes' individual calculations is to have each process send its *local* calculation to process 0 and have process 0 do the final addition.

With these assumptions we can write a parallel trapezoid rule program.

```
c  trap.f -- Parallel Trapezoidal Rule, first version
c
c  Input: None.
c  Output: Estimate of the integral from a to b of f(x)
c          using the trapezoidal rule and n trapezoids.
c
c  Algorithm:
c    1. Each process calculates "its" interval of
c       integration.
c    2. Each process estimates the integral of f(x)
c       over its interval using the trapezoidal rule.
c    3a. Each process != 0 sends its integral to 0.
c    3b. Process 0 sums the calculations received from
c        the individual processes and prints the result.
c
c  Note: f(x), a, b, and n are all hardwired.
c
c
c      program trapezoidal
c
c      IMPLICIT NONE
c      include 'mpif.h'
c
c      integer my_rank ! My process rank.
c      integer p       ! The number of processes.
```

```

real      a          ! Left endpoint.
real      b          ! Right endpoint.
integer   n          ! Number of trapezoids.
real      h          ! Trapezoid base length.
real      local_a    ! Left endpoint for my process.
real      local_b    ! Right endpoint my process.
integer   local_n    ! Number of trapezoids for my
                    ! calculation.
real      integral   ! Integral over my interval.
real      total      ! Total integral.
integer   source     ! Process sending integral.
integer   dest       ! All messages go to 0.
integer   tag
integer   status(MPI_STATUS_SIZE)
integer   ierr

real      Trap

data a, b, n, dest, tag /0.0, 1.0, 1024, 0, 50/

C  Let the system do what it needs to start up MPI.
  call MPI_INIT(ierr)

C  Get my process rank.
  call MPI_COMM_RANK(MPI_COMM_WORLD, my_rank, ierr)

C  Find out how many processes are being used.
  call MPI_COMM_SIZE(MPI_COMM_WORLD, p, ierr)

  h = (b-a)/n          ! h is the same for all processes.
  local_n = n/p        ! So is the number of trapezoids.

C  Length of each process' interval of integration = local_n*h.
C  So my interval starts at :
  local_a = a + my_rank*local_n*h
  local_b = local_a + local_n*h
  integral = Trap(local_a, local_b, local_n, h)

C  Add up the integrals calculated by each process.
  if (my_rank .EQ. 0) then
    total = integral
    do source = 1, p-1
      call MPI_RECV(integral, 1, MPI_REAL, source, tag,
+               MPI_COMM_WORLD, status, ierr)
      total = total + integral
    enddo
  else
    call MPI_SEND(integral, 1, MPI_REAL, dest,
+               tag, MPI_COMM_WORLD, ierr)
  endif

```

```

C  Print the result.
    if (my_rank .EQ. 0) then
        write(6,200) n
200        format(' ', 'With n = ',I4,' trapezoids, our estimate')
        write(6,300) a, b, total
300        format(' ', 'of the integral from ',f6.2,' to ',f6.2,
+           ' = ',f11.5)
    endif

C      Shut down MPI.
    call MPI_FINALIZE(ierr)
    end program trapezoidal

real function Trap(local_a, local_b, local_n, h)
IMPLICIT NONE
real    local_a
real    local_b
integer local_n
real    h
real    integral    ! Store result in integral.
real    x
real    i

real    f

integral = (f(local_a) + f(local_b))/2.0
x = local_a
do i = 1, local_n - 1
    x = x + h
    integral = integral + f(x)
enddo
integral = integral*h
Trap = integral
return
end

real function f(x)
IMPLICIT NONE
real x

f = x*x
end

```

Observe that this program also uses the SPMD paradigm. Even though process 0 executes an essentially different set of commands from the remaining processes, it still runs the same program. The different commands are executed by branching based on the process rank.

### 3.3 I/O on Parallel Processors

One obvious problem with our program is its lack of generality : the data,  $a$ ,  $b$ , and  $n$ , are hardwired. The user should be able to enter these values during execution. Let's look more carefully at the problem of I/O on parallel machines.

In our **greetings** and **trapezoid** programs we assumed that process 0 could write to standard output ( the terminal screen). Most parallel processors provide this much I/O. In fact, most parallel processors allow all processors to both read from standard input and write to standard output. However difficulties arise when several processes are simultaneously trying to execute I/O functions. In order to understand this, let's look at an example.

Suppose we modify the **trapezoid** program so that each process attempts to read the values  $a$ ,  $b$ , and  $n$  by adding the statement

```
read *, a , b, n
```

Suppose also that we run the program with two processes and the user types in

```
0 1 1024
```

What happens ? Do both processes get the data ? Does only one ? Or, even worse, does (say) process 0 get the 0 and 1, while process 1 gets the 1024 ? If all the processes get the data, what happens when we write a program, where we want process 0 gets the data, what happens to the others ? Is it even reasonable to have multiple processes reading data from a single terminal ?

On the other hand, what happens if several processes attempt to simultaneously write data to the terminal screen. Does the data from process 0 get printed first, then the data from process 1, etc ? Or does the data appear in some random order ? Or, even worse, does the data from the different processes get all mixed up - say, half a line from 0, two characters from 1, 3 characters from 0, two lines from 2, etc ?

The standard I/O commands available in Fortran (and most other languages) don't provide simple solutions to these problems, and I/O continues to be the subject of considerable research in the parallel processing community. So let's look at some not so simple solutions to these problems.

Thus far, we have assumed that process 0 can at least write to standard output. We will also assume that it can read from standard input. In most cases, we will only assume that process 0 can do I/O. It should be noted that this is a very weak assumption, since, as we noted most parallel



machines allow multiple processes to carry out I/O.<sup>5</sup> You might want to ask your local expert whether there are any restrictions on which processes can do I/O.<sup>6</sup>

If only process 0 can do I/O, then we need for process 0 to send the user input to the other processes. This is readily accomplished with a short I/O function that uses `MPI_Send` and `MPI_Recv`.

```
C *****
C  Function Get_data
C    Reads in the user input a, b, and n.
C    Input arguments:
C      1.  integer my_rank:  rank of current process.
C      2.  integer p:  number of processes.
C    Output parameters:
C      1.  real a:  left endpoint a.
C      2.  real b:  right endpoint b.
C      3.  integer n:  number of trapezoids.
C    Algorithm:
C      1.  Process 0 prompts user for input and
C          reads in the values.
C      2.  Process 0 sends input values to other
C          processes.
C
C      subroutine Get_data(a, b, n, my_rank, p)
C      IMPLICIT NONE
C      real a
C      real b
C      integer n
C      integer my_rank
C      integer p
C      INCLUDE 'mpif.h'
C
C      integer source
C      integer dest
C      integer tag
C      integer status(MPI_STATUS_SIZE)
C      integer ierr
C      data source /0/
C
C      if (my_rank ==7 0) then
C        print *, 'Enter a, b and n'
```

---

<sup>5</sup> The MPI function `MPI_Attr_get` can determine the rank of a process that can carry out the usual I/O functions. See [4]. But it is not important in our SP2.

<sup>6</sup> In our SP2, this is controlled by the environment variable `MP_STDINMODE`. By default, all processes receive the same input data from the keyboard ( or standard input ). See [8] for detail.

<sup>7</sup> `==` means exactly the same as `.EQ.`

```

C      read *, a, b, n
C
      do dest = 1 , p-1
        tag = 0
        call MPI_SEND(a, 1, MPI_REAL , dest, tag,
+          MPI_COMM_WORLD, ierr )
        tag = 1
        call MPI_SEND(b, 1, MPI_REAL , dest, tag,
+          MPI_COMM_WORLD, ierr )
        tag = 2
        call MPI_SEND(n, 1, MPI_INTEGER, dest,
+          tag, MPI_COMM_WORLD, ierr )
      enddo
    else
      tag = 0
      call MPI_RECV(a, 1, MPI_REAL , source, tag,
+        MPI_COMM_WORLD, status, ierr )
      tag = 1
      call MPI_RECV(b, 1, MPI_REAL , source, tag,
+        MPI_COMM_WORLD, status, ierr )
      tag = 2
      call MPI_RECV(n, 1, MPI_INTEGER, source, tag,
+        MPI_COMM_WORLD, status, ierr )
    endif
    return
  end
C
C
C
*****

```

## 4. Collective Communication

There are probably a few things in the trapezoid rule program that we can improve on. For example, there is the I/O issue. There are also a couple of problems we haven't discussed yet. Let's look at what happens when the program is run with eight processes.

All the processes begin executing the program ( more or less ) simultaneously. However, after carrying out the basic set-up tasks ( calls to `MPI_Init`, `MPI_Comm_size`, and `MPI_Comm_rank`), processes 1-7 are idle while process 0 collects the input data. We don't want to have idle processes, but in view of our restrictions on which processes can read input data, the higher rank processes must continue to wait while 0 sends the input data to the lower rank processes. This isn't just an I/O issue. Notice that there is a similar inefficiency at the end of the program, when process 0 does all the work of collecting and adding the local integrals.

Of course, this is highly undesirable : the main point of parallel processing is to get multiple processes to collaborate on solving a problem. If one of the processes is doing most of the work, we might as well use a conventional, single-processor machine.

### 4.1 Tree-Structured Communication

Let's try to improve our code. We'll begin by focusing on the distribution of the input data. How can we divide the work more evenly among the processes ? A natural solution is to imagine that we have a tree of processes, with 0 at the root.

During the first stage of data distribution, 0 sends the data to (say) 4. During the next stage, 0 sends the data to 2, while 4 sends it to 6. During the last stage, 0 sends to 1, while 2 sends to 3, 4 sends to 5, and 6 sends to 7. (see figure 4.1) So we have reduced our input distribution loop from 7 stages to 3 stages. More generally, if we have  $p$  processes, this procedure allows us to distribute the input data in  $\lceil \log_2(p) \rceil$  stages, rather than  $p-1$  stages, which, if  $p$  is large, is a huge savings.

---

<sup>8</sup> The notation  $\lceil x \rceil$  denotes the smallest whole number greater than or equal to  $x$ .

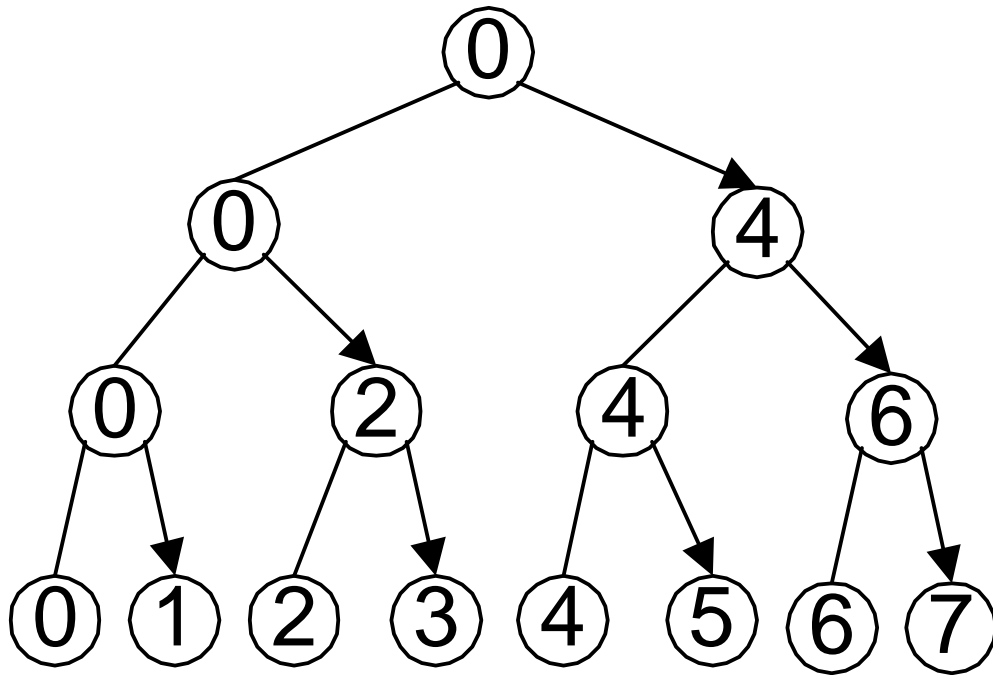


Figure 1 Processors configured as a tree

In order to modify the `Get_data` function to use a tree-structured distribution scheme, we need to introduce a loop with  $\lceil \log_2(p) \rceil$  stages. In order to implement the loop, each process needs to calculate at each stage.

- whether it receives, and, if so, the source ; and
- whether it sends, and, if so, the destination.

As you can probably guess, these calculations can be a bit complicated, especially since there is no canonical choice of ordering. In our example, we chose :

0 sends to 4.

0 sends to 2, 4 sends to 6.

0 sends to 1, 2 sends to 3, 4 sends to 5, 6 sends to 7.

We might also have chosen ( for example ) :

0 sends to 1.

0 sends to 2, 1 sends to 3.

0 sends to 4, 1 sends to 5, 2 sends to 6, 3 sends to 7.

Indeed, unless we know something about the underlying topology of our machine, we can't really decide which scheme is better.

So ideally we would prefer to use a function that has been specifically tailored to the machine we're using so that we won't have to worry about all these tedious details, and we won't have to modify our code every time we change machines. As you may have guess, MPI provides such a function.

## 4.2 Broadcast

A communication pattern that involves all the processes in a communicator is a *collective communication*. As a consequence, a collective communication usually involves more than two processes. A *broadcast* is a collective communication in which a single process sends the same data to every process. In MPI the function for broadcasting data is `MPI_Bcast` :

```
MPI_BCAST( BUFFER, COUNT, DATATYPE, ROOT, COMM, IERROR )
<type> BUFFER(*)
INTEGER COUNT, DATA, ROOT, COMM, IERROR
```

It simply sends a copy of the data in `BUFFER` on process `ROOT` to each process in the communicator `COMM`. It should be called by all the processes in the communicator with the same arguments for `ROOT` and `COMM`. Hence a broadcast message cannot be received with `MPI_Recv`. The parameters `COUNT` and `DATATYPE` have the same function that they have in `MPI_Send` and `MPI_Recv` : they specify the extent of the message. However, unlike the point-to-point functions, MPI insists that in collective communication `COUNT` and `DATATYPE` be the same on all the processes in the communicator [4]. The reason for this is that in some collective operations (see below), a single process will receive data from many other processes, and in order for a program to determine how much data has been received, it would need an entire *array* of return statuses.

We can rewrite the `Get_data` function using `MPI_Bcast` as follows.

```
subroutine Get_data2(a, b, n, my_rank)
  real a
  real b
  integer n
  integer my_rank
  integer ierr
  include 'mpif.h'
C
C
  if (my_rank .EQ. 0) then
```

```

        print *, 'Enter a, b, and n'
        read *, a, b, n
        endif
C
        call MPI_BCAST(a, 1, MPI_REAL , 0, MPI_COMM_WORLD, ierr )
        call MPI_BCAST(b, 1, MPI_REAL , 0, MPI_COMM_WORLD, ierr )
        call MPI_BCAST(n, 1, MPI_INTEGER, 0, MPI_COMM_WORLD, ierr )
        end subroutine Get_data2
C
C
C
*****

```

Certainly this version of Get\_data is much more compact and readily comprehensible than the original, and if MPI\_Bcast has been optimized for your system, it will also be a good deal faster.

## 4.3 Reduce

In the trapezoid rule program after the input phase, every processor executes essentially the same commands until the final summation phase. So unless our function  $f(x)$  is fairly complicated ( i.e., it requires considerably more work to evaluate over certain parts of  $[a,b]$ ), this part of the program distributes the work equally among the processors. As we have already noted, this is not the case with the final summation phase, when, once again, process 0 gets a disproportionate amount of the work. However, you have probably already noticed that by reversing the arrows in figure 4.1, we can use the same idea we used in section 4.1. That is, we can distribute the work of calculating the sum among the processors as follows.

1.     (a) 1 sends to 0, 3 sends to 2, 5 sends to 4, 7 sends to 6.  
       (b) 0 adds its integral to that of 1, 2 adds its integral to that of 3, etc.
2.     (a) 2 sends to 0, 6 sends to 4.  
       (b) 0 adds, 4 adds.
3.     (a) 4 sends to 0.  
       (b) 0 adds.

Of course, we run into the same question that occurred when we were writing our own broadcast : is this tree structure making optimal use of the topology of our machine ? Once again, we have to answer that this depends on the machine. So, as before, we should let MPI do the work, by using an optimized function.

The “global sum” that we wish to calculate is an example of a general class of collective communication operations called *reduction operations*. In a global reduction operation, all the

processes ( in a communicator ) contribute data which is combined using a binary operation. Typical binary operations are addition, max, min, logical and, etc. The MPI function for performing a reduction operation is

```
MPI_Reduce(OPERAND, RESULT, COUNT, DATATYPE, OP, ROOT, COMM,
IERROR)
<type> OPERAND(*), RESULT(*)
INTEGER COUNT, DATATYPE, OP, ROOT, COMM, IERROR
```

MPI\_Reduce combines the operands stored in OPERAND using operation OP and stores the result in RESULT on process ROOT. Both OPERAND and RESULT refer to COUNT memory locations with type DATATYPE. MPI\_Reduce must be called by all processes in the communicator COMM, and COUNT, DATATYPE, and OP must be the same on each process.

The argument OP can take on one of the following predefined values.

Operation Name	Meaning
<b>MPI_MAX</b>	Maximum
<b>MPI_MIN</b>	Minimum
<b>MPI_SUM</b>	Sum
<b>MPI_PROD</b>	Product
<b>MPI_LAND</b>	Logical And
<b>MPI_BAND</b>	Bitwise And
<b>MPI_LOR</b>	Logical Or
<b>MPI_BOR</b>	Bitwise Or
<b>MPI_LXOR</b>	Logical Exclusive Or
<b>MPI_BXOR</b>	Bitwise Exclusive Or
<b>MPI_MAXLOC</b>	Maximum and Location of Maximum
<b>MPI_MINLOC</b>	Minimum and Location of Minimum

It is also possible to define additional operations. For details see [4].

As an example, let's rewrite the last few lines of the trapezoid rule program.

C Add up the integrals calculated by each process.

```

    MPI_Reduce( INTEGRAL, TOTAL, 1, MPI_REAL, MPI_SUM, 0,
+             MPI_COMM_WORLD, ierr)
C Print the result.

```

Note that each processor calls MPI\_Reduce with the same arguments. In particular, even though total only has significance on process 0, each process must supply an argument.

## 4.4 Other Collective Communication Functions

MPI supplies many other collective communication functions. We briefly enumerate some of these here. For full details, see [4].

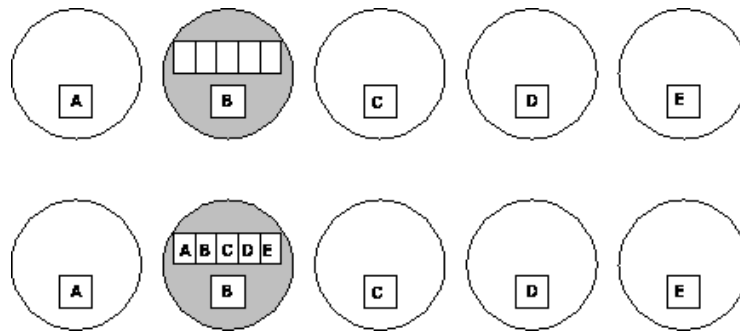
- MPI\_Barrier( COMM, IERROR)  
 INTEGER COMM, IERROR

MPI\_Barrier provides a mechanism for synchronizing all the processes in the communicator comm. Each process blocks (i.e., pauses) until every process in comm has called MPI\_Barrier.

```

MPI_Gather( SEND_BUF, SEND_COUNT, SEND_TYPE, RECV_BUF, RECV_COUNT,
RECV_TYPE, ROOT, COMM, IERROR )
<type>SEND_BUF(*), RECV_BUF(*)
INTEGER SEND_COUNT, SEND_TYPE, RECV_COUNT, RECV_TYPE, ROOT, COMM, IERROR

```



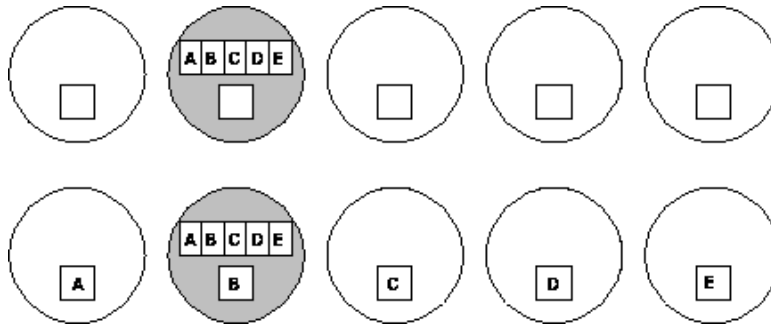
Each process in comm sends the contents of send\_buf to process with rank root. The process root concatenates the received data in process rank order in recv\_buf. That is, the data from process 0 is followed by the data from process 1, which is followed by the data from process 2, etc. The recv arguments are significant only on the process with rank root. The argument recv\_count indicates the number of items received from each process - not the total number received.

```

MPI_Scatter( SEND_BUF, SEND_COUNT, SEND_TYPE, RECV_BUF, RECV_COUNT,
RECV_TYPE, ROOT, COMM, IERROR )
<type>SEND_BUF(*), RECV_BUF(*)
INTEGER SEND_COUNT, SEND_TYPE, RECV_COUNT, RECV_TYPE, ROOT, COMM, IERROR

```





The process with rank root distributes the contents of send\_buf among the processes. The contents of send\_buf are split into p segments each consisting of send\_count items. The first segment goes to process 0, the second to process 1, etc. The send arguments are significant only on process root.

```
MPI_Allgather(SEND_BUF, SEND_COUNT, SEND_TYPE, RECV_BUF,
RECV_COUNT, RECV_TYPE, ROOT, COMM, IERROR )
<type>SEND_BUF(*), RECV_BUF(*)
INTEGER SEND_COUNT,SEND_TYPE,RECV_COUNT, RECV_TYPE,ROOT,COMM,IERROR
```

MPI\_Allgather gathers the contents of each send\_buf on each process. Its effect is the same as if there were a sequence of p calls to MPI\_Gather, each of which has a different process acting as root.

```
MPI_Allreduce(OPERAND, RESULT, COUNT, DATATYPE, OP, COMM, IERROR )
<type>OPERAND(*), RESULT(*)
INTEGER COUNT, DATATYPE, OP ,COMM,IERROR
```

MPI\_Allreduce stores the result of the reduce operation OP in each process' result buffer.

## 5. Grouping Data for Communication

With current generation machines sending a message is an expensive operation. So as a rule of thumb, the fewer messages sent, the better the overall performance of the program. However, in each of our trapezoid rule programs, when we distributed the input data, we sent  $a$ ,  $b$  and  $n$  in separate messages - whether we used `MPI_Send` and `MPI_Recv` or `MPI_Bcast`. So we should be able to improve the performance of the program by sending the three input values in a single message. MPI provides three mechanisms for grouping individual data items into a single message : the count parameter to the various communication routines, derived datatypes, and `MPI_Pack` / `MPI_Unpack`. We examine each of these options in turn.

### 5.1 The Count Parameter

Recall that `MPI_Send`, `MPI_Recv`, `MPI_Bcast`, and `MPI_Reduce` all have a count and a **datatype** argument. These two parameters allow the user to group data items having the same basic type into a single message. In order to use this, the grouped data items must be stored in *contiguous* memory locations. Since Fortran guarantees that array elements are stored in contiguous memory locations, if we wish to send the elements of an array, or a subset of an array, we can do so in a single message. In fact, we've already done this in section 2, when we sent an array of `character`.

As another example, suppose we wish to send the second half of a vector containing 100 real numbers from process 0 to process 1.

```
      real vector(100)
      integer status(MPI_STATUS_SIZE)
      integer p, my_rank, ierr
      integer i
      .
      .
      .
      if (my_rank == 0) then
C        Initialize vector and send.
          tag = 47
          count = 50
          dest = 1
          call MPI_SEND(vector(51), count, MPI_REAL, dest, tag,
+                      MPI_COMM_WORLD, ierr)
      else
          tag = 47
          count = 50
          source = 0
```

```

        call MPI_RECV(vector(51), count, MPI_REAL, source, tag,
+                      MPI_COMM_WORLD, status, ierr)

    endif

```

Unfortunately, this doesn't help us with the trapezoid rule program. The data we wish to distribute to the other processes, *a*, *b*, and *n*, are stored in an array. So even if we declared them one after the other in our program,

```

real a
real b
integer n

```

Fortran does *not* guarantee that they are stored in contiguous memory locations. One might be tempted to store *n* as a float and put the three values in an array, but this would be poor programming style and it wouldn't address the fundamental issue. In order to solve the problem we need to use one of MPI's other facilities for grouping data.

## 5.2 Derived Types and MPI\_Type\_struct

It might seem that another option would be to store *a*, *b*, and *n* in a derived type<sup>9</sup> with three members - two reals and an integer - and try to use the *datatype* argument to `MPI_Bcast`. The difficulty here is that the type of *datatype* is `MPI_Datatype`, which is an actual type itself - not the same thing as a user-defined type in Fortran 90. For example, suppose we included the type definition

```

type INDATA_TYPE
    real a
    real b
    integer n
end type

```

and the variable definition

```

type (INDATA_TYPE) indata

```

Now if we call `MPI_Bcast`

```

    call MPI_Bcast(indata, 1, INDATA_TYPE, 0, MPI_COMM_WORLD,
+                  ierr)

```

---

<sup>9</sup> Type definition is available in FORTRAN 90. We may access individual variables in the derived type using the operator `%`. E.g., `indata%a = 1.0`

the program will fail. The detail depend on the implementation of MPI that you're using. The problem here is that MPI is a *pre-existing* library of functions. That is, the MPI functions were written without knowledge of the datatypes that you define in your program. In particular, none of the MPI functions “knows” about INDATA\_TYPE.

MPI provides a partial solution to this problem, by allowing the user to build MPI datatypes at execution time. In order to build an MPI datatype, one essentially specifies the layout of the data in the type - the member types and their relative locations in memory. Such a type is called a *MPI derived data type*. In order to see how this works, let's write a function that will build a MPI derived type.

```

MODULE GLOBAL10
  type INDATA_TYPE
    real a
    real b
    integer n
  end type INDATA_TYPE
END MODULE GLOBAL

subroutine Build_derived_type(indata, mesg_mpi_t)
use GLOBAL11
INCLUDE      'mpif.h'
IMPLICIT NONE

type(INDATA_TYPE)    indata
integer              mesg_mpi_t

integer              ierr

integer              block_lengths(3)
integer              displacements(3)
integer              address(4)
integer              typelist(3)

```

C Build a derived datatype consisting of two real and an integer.

C First specify the types.

```

  typelist(1) = MPI_REAL
  typelist(2) = MPI_REAL
  typelist(3) = MPI_INTEGER

```

C Specify the number of elements of each type.

---

<sup>10</sup> MODULE is a new kind of Fortran 90 program unit. Any program unit may use the variables and type definition in a module by the “USE” statement. This feature is intended to replace “common block” in Fortran 77 which is very inconvenient.

<sup>11</sup> Supra.

```

    block_lengths(1) = 1
    block_lengths(2) = 1
    block_lengths(3) = 1

C   Calculate the displacements of the members relative to indata.
    call MPI_Address(indata, address(1), ierr)
    call MPI_Address(indata%a, address(2), ierr)
    call MPI_Address(indata%b, address(3), ierr)
    call MPI_Address(indata%n, address(4), ierr)
    displacements(1) = address(2) - address(1)
    displacements(2) = address(3) - address(1)
    displacements(3) = address(4) - address(1)

C   Build the derived datatype
    call MPI_TYPE_STRUCT(3, block_lengths, displacements,
+       typelist, mesg_mpi_t, ierr)

C   Commit it -- tell system we'll be using it for communication.
    call MPI_TYPE_COMMIT(mesg_mpi_t, ierr)
    return
end

```

The first three statements specify the types of the members of the MPI derived type, and the next three specifies the number of elements of each type. The next four calculate the addresses of the three members of `indata`. The next three statements use the calculated addresses to determine the *displacements* of the three members relative to the address of the first - which is given displacement 0. With this information, we know the types, sizes and relative locations of the members of a variable having Fortran 90 type `INDATA_TYPE`, and hence we can define a derived data type that corresponds to the Fortran type. This is done by calling the functions `MPI_Type_struct` and `MPI_Type_commit`.

The newly created MPI datatype can be used in any of the MPI communication functions. In order to use it, we simply use the starting address of a variable of type `INDATA_TYPE` as the first argument, and the derived type in the datatype argument. For example, we could rewrite the `Get_data` function as follows.

```

subroutine Get_data3(indata, my_rank)
use global
type(INDATA_TYPE) indata
integer my_rank
integer mesg_mpi_t
integer ierr
include 'mpif.h'

if (my_rank == 0) then
    print *, 'Enter a, b, and n'
    read *, indata%a, indata%b, indata%n
endif

```

```

    call Build_derived_type(indata, mesg_mpi_t)
    call MPI_BCAST(indata, 1, mesg_mpi_t, 0, MPI_COMM_WORLD,
+ierr )
    return
end

```

To summarize, then, we can build general MPI derived datatypes by calling `MPI_Type_struct`. The syntax is

```

    call MPI_TYPE_STRUCT(count, array_of_block_lengths,
+array_of_displacements, array_of_types, newtype, ierror)
    integer count, array_of_block_lengths(*),
    integer array_of_displacements(*) , array_of_types(*)
    integer array_of_types(*), newtype, ierror

```

The argument `count` is the number of elements in the derived type. It is also the size of the three arrays, `array_of_block_lengths`, `array_of_displacements`, and `array_of_types`. The array `array_of_block_lengths` contains the number of entries in each element of the type. So if an element of the type is an array of  $m$  values, then the corresponding entry in `array_of_block_lengths` is  $m$ . The array `array_of_displacements` contains the displacement of each element from the beginning of the message, and the array `array_of_types` contains the MPI datatype of each entry. The argument `newtype` returns a pointer to the MPI datatype created by the call to `MPI_Type_struct`.

Note also that `newtype` and the entries in `array_of_types` all have type `MPI_Datatype`. So `MPI_Type_struct` can be called recursively to build more complex derived datatypes.

## 5.3 Other Derived Datatype Constructors

`MPI_Type_struct` is the most general datatype constructor in MPI, and as a consequence, the user must provide a *complete* description of each element of the type. If the data to be transmitted consists of a subset of the entries in an array, we shouldn't need to provide such detailed information, since all the elements have the same basic type. MPI provides three derived datatype constructors for dealing with this situation: `MPI_Type_Contiguous`, `MPI_Type_vector` and `MPI_Type_indexed`. The first constructor builds a derived type whose elements are contiguous entries in an array. The second builds a type whose elements are equally spaced entries of an array, and the third builds a type whose elements are arbitrary entries of an array. Note that before any derived type can be used in communication it must be *committed* with a call to `MPI_Type_commit`.

Details of the syntax of the additional type constructors follow.

```

MPI_Type_contiguous(count, oldtype, newtype, ierror)

```

```
integer count, oldtype, newtype, ierror
```

**MPI\_Type\_contiguous** creates a derived datatype consisting of **count** elements of type **oldtype**. The elements belong to contiguous memory locations.

```
MPI_Type_vector(count, block_length, stride,
+element_type, newtype, ierror)
integer count, blocklength, stride oldtype, newtype, ierror
```

**MPI\_Type\_vector** creates a derived type consisting of **count** elements. Each element contains **block\_length** entries of type **element\_type**. **Stride** is the number of elements of type **element\_type** between successive elements of **new\_type**.

```
MPI_Type_indexed(count, array_of_block_lengths,
+array_of_displacements, element_type, newtype, ierror
integer count, array_of_block_lengths(*),
+array_of_displacements, element_type, newtype, ierror
```

**MPI\_Type\_indexed** creates a derived type consisting of **count** elements. The *i*th element (*i* = 1, ..., **count**), consists of **array\_of\_block\_lengths[i]** entries of type **element\_type**, and it is displaced **array\_of\_displacements[i]** units of type **element\_type** from the beginning of **newtype**.

## 5.4 Pack/Unpack

An alternative approach to grouping data is provided by the MPI functions **MPI\_Pack** and **MPI\_Unpack**. **MPI\_Pack** allows one to explicitly store noncontiguous data in contiguous memory locations, and **MPI\_Unpack** can be used to copy data from a contiguous buffer into noncontiguous memory locations. In order to see how they are used, let's rewrite **Get\_data** one last time.

```
subroutine Get_data4(a, b, n, my_rank)
real a
real b
integer n
integer my_rank
C
INCLUDE 'mpif.h'
integer ierr
character buffer(100)
integer position
C in the buffer
C
if (my_rank .EQ. 0) then
print *, 'Enter a, b, and n'
read *, a, b, n
```

```

C
C  Now pack the data into buffer.  Position = 0
C  says start at beginning of buffer.
C      position = 0
C
C  Position is in/out
C      call MPI_PACK(a, 1, MPI_REAL , buffer, 100,
C          +          position, MPI_COMM_WORLD, ierr )
C  Position has been incremented: it now refer-
C  ences the first free location in buffer.
C
C      call MPI_PACK(b, 1, MPI_REAL , buffer, 100,
C          +          position, MPI_COMM_WORLD, ierr )
C  Position has been incremented again.
C
C      call MPI_PACK(n, 1, MPI_INTEGER, buffer, 100,
C          +          position, MPI_COMM_WORLD, ierr )
C  Position has been incremented again.
C
C  Now broadcast contents of buffer
C      call MPI_BCAST(buffer, 100, MPI_PACKED, 0,
C          +          MPI_COMM_WORLD, ierr )
C      else
C          call MPI_BCAST(buffer, 100, MPI_PACKED, 0,
C          +          MPI_COMM_WORLD, ierr )
C
C  Now unpack the contents of buffer
C      position = 0
C      call MPI_UNPACK(buffer, 100, position, a, 1,
C          +          MPI_REAL , MPI_COMM_WORLD, ierr )
C  Once again position has been incremented:
C  it now references the beginning of b.
C
C      call MPI_UNPACK(buffer, 100, position, b, 1,
C          +          MPI_REAL , MPI_COMM_WORLD, ierr )
C      call MPI_UNPACK(buffer, 100, position, n, 1,
C          +          MPI_INTEGER, MPI_COMM_WORLD, ierr )
C      endif
C      return
C      end
C

```

In this version of `Get_data` process 0 uses `MPI_Pack` to copy `a` to `buffer` and then append `b` and `n`. After the broadcast of `buffer`, the remaining processes use `MPI_Unpack` to successively extract `a`, `b`, and `n` from `buffer`. Note that the datatype for the calls to `MPI_Bcast` is `MPI_PACKED`.

The syntax of `MPI_Pack` is



```

MPI_Pack( pack_data, in_count, datatype, buffer, size,
+position_ptr, comm, ierror)
<type> pack_data(*), buffer(*)
integer in_count, datatype, size, position_ptr, comm, ierror

```

The parameter **pack\_data** references the data to be buffered. It should consist of **in\_count** elements, each having type **datatype**. The parameter **position\_ptr** is an *in/out* parameter. On input, the data referenced by **pack\_data** is copied into memory starting at address **buffer + position\_ptr**. On return, **position\_ptr** references the first location in **buffer** *after* the data that was copied. The parameter **size** contains the size *in bytes* of the memory referenced by **buffer**, and **comm** is the communicator that will be using **buffer**.

The syntax of **MPI\_Unpack** is

```

MPI_Unpack(buffer, size, position_ptr, unpack_data,
+count, datatype, comm, ierror)
<type> inbuf(*), outbuf(*)
integer insize, position, outcount, datatype, comm, ierror

```

The parameter **buffer** references the data to be unpacked. It consists of **size** bytes. The parameter **position\_ptr** is once again an *in/out* parameter. When **MPI\_Unpack** is called, the data starting at address **buffer + position\_ptr** is copied into the memory referenced by **unpack\_data**. On return, **position\_ptr** references the first location in **buffer** after the data that was just copied. **MPI\_Unpack** will copy **count** elements having type **datatype** into **unpack\_data**. The communicator associated with **buffer** is **comm**.

## 5.5 Deciding Which Method to Use

If the data to be sent is stored in consecutive entries of an array, then one should simply use the **count** and **datatype** arguments to the communication function(s). This approach involves no additional overhead in the form of calls to derived datatype creation functions or calls to **MPI\_Pack/MPI\_Unpack**.

If there are a large number of elements that are not in contiguous memory locations, then building a derived type will probably involve less overhead than a large number of calls to **MPI\_Pack/MPI\_Unpack**.

If the data all have the same type and are stored at regular intervals in memory (e.g., a column of a matrix), then it will almost certainly be much easier and faster to use a derived datatype than it will be to use **MPI\_Pack/MPI\_Unpack**. Furthermore, if the data all have the same type, but are stored in irregularly spaced locations in memory, it will still probably be easier and more efficient to create a derived type using **MPI\_Type\_indexed**. Finally, if the data are heterogeneous and one is repeatedly sending the same collection of data (e.g., row number, column number, matrix entry), then it will be better to use a derived type, since the overhead of creating the derived type

is incurred only once, while the overhead of calling `MPI_Pack/MPI_Unpack` must be incurred every time the data is communicated.

This leaves the case where one is sending heterogeneous data only once, or very few times. In this case, it may be a good idea to collect some information on the cost of derived type creation and packing/unpacking the data. For example, on an nCUBE 2 running the MPICH implementation of MPI, it takes about 12 milliseconds to create the derived type used in `Get_data3`, while it only takes about 2 milliseconds to pack or unpack the data in `Get_data4`. Of course, the saving isn't as great as it seems because of the asymmetry in the pack/unpack procedure. That is, while process 0 packs the data, the other processes are idle, and the entire function won't complete until both the pack and unpack are executed. So the cost ratio is probably more like 3:1 than 6:1.

There are also a couple of situations in which the use of `MPI_Pack` and `MPI_Unpack` is preferred. Note first that it may be possible to avoid the use of *system* buffering with pack, since the data is explicitly stored in a user-defined buffer. The system can exploit this by noting that the message datatype is `MPI_PACKED`. Also note that the user can send "variable-length" messages by packing the number of elements at the beginning of the buffer. For example, suppose we want to send rows of a sparse matrix. If we have stored a row as a pair of arrays --- one containing the column subscripts, and one containing the corresponding matrix entries --- we could send a row from process 0 to process 1 as follows.

```

PROGRAM SpaRow
INCLUDE 'mpif.h'
integer HUGE
parameter (HUGE = 100)
integer p
integer my_rank
real entries(10)
integer column_subscripts(10)
integer nonzeroes
integer position
integer row_number
character buffer *100
integer status(MPI_STATUS_SIZE)
integer ierr
integer i
data nonzeroes /10/
C
call MPI_INIT( ierr)
call MPI_COMM_SIZE(MPI_COMM_WORLD, p, ierr )
call MPI_COMM_RANK(MPI_COMM_WORLD, my_rank, ierr )
C
if (my_rank .EQ. 0) then
C Get the number of nonzeros in the row.
C Initialize entries and column_subscripts
do i = 1, nonzeroes
entries(i) = 2*i
column_subscripts(i) = 3*i

```

```

        enddo
C
C  Now pack the data and send
        position = 1
        call MPI_PACK( nonzeroes, 1, MPI_INTEGER, buffer, HUGE,
+           position, MPI_COMM_WORLD, ierr )
        call MPI_PACK( row_number, 1, MPI_INTEGER, buffer, HUGE,
+           position, MPI_COMM_WORLD, ierr )
        call MPI_PACK( entries, nonzeroes, MPI_REAL , buffer,
+           HUGE, position, MPI_COMM_WORLD, ierr )
        call MPI_PACK( column_subscripts, nonzeroes, MPI_INTEGER,
+           buffer, HUGE, position, MPI_COMM_WORLD, ierr )
        call MPI_SEND( buffer, position, MPI_PACKED, 1, 0,
+           MPI_COMM_WORLD, ierr )
        else
            call MPI_RECV( buffer, HUGE, MPI_PACKED, 0, 0,
+           MPI_COMM_WORLD, status, ierr )
            position = 1
            call MPI_UNPACK( buffer, HUGE, position, nonzeroes,
+           1, MPI_INTEGER, MPI_COMM_WORLD, ierr )
            call MPI_UNPACK( buffer, HUGE, position, row_number,
+           1, MPI_INTEGER, MPI_COMM_WORLD, ierr )
            call MPI_UNPACK( buffer, HUGE, position, entries,
+           nonzeroes, MPI_REAL , MPI_COMM_WORLD, ierr )
            call MPI_UNPACK( buffer, HUGE, position,
+           column_subscripts,
+           nonzeroes, MPI_INTEGER, MPI_COMM_WORLD, ierr )
            do i = 1, nonzeroes
                print *, entries(i), column_subscripts(i)
            enddo
        endif
C
        call MPI_FINALIZE(ierr)
    end

```

## 6. Communicators and Topologies

The use of communicators and topologies makes MPI different from most other message-passing systems. Recollect that, loosely speaking, a communicator is a collection of processes that can send messages to each other. A topology is a structure imposed on the processes in a communicator that allows the processes to be addressed in different ways. In order to illustrate these ideas, we will develop code to implement Fox's algorithm for multiplying two square matrices.

### 6.1 Fox's Algorithm

We assume that the factor matrices  $A = (a_{ij})$  and  $B = (b_{ij})$  have order  $n$ . We also assume that the number of processes,  $p$ , is a perfect square, whose square root evenly divides  $n$ . Say  $p = q^2$ , and  $\bar{n} = n/q$ . In Fox's algorithm the factor matrices are partitioned among the processes in a *block checkerboard* fashion. So we view our processes as a virtual two-dimensional  $q \times q$  grid, and each process is assigned an  $\bar{n} \times \bar{n}$  submatrix of each of the factor matrices. More formally, we have a mapping

$$\phi: \{0, 1, \dots, p-1\} \rightarrow \{(s, t): 0 \leq s, t \leq q-1\}$$

that is both one-to-one and onto. This defines our grid of processes: process  $i$  belongs to the row and column given by  $\phi(i)$ . Further, the process with rank  $\phi^{-1}(s, t)$  is assigned the submatrices

$$A_{st} = \begin{pmatrix} a_{s\bar{n}, t\bar{n}} & \dots & a_{s\bar{n}, (t+1)\bar{n}-1} \\ \dots & & \dots \\ a_{(s+1)\bar{n}-1, t\bar{n}} & \dots & a_{(s+1)\bar{n}-1, (t+1)\bar{n}-1} \end{pmatrix},$$

and

$$B_{st} = \begin{pmatrix} b_{s\bar{n}, t\bar{n}} & \dots & b_{s\bar{n}, (t+1)\bar{n}-1} \\ \dots & & \dots \\ b_{(s+1)\bar{n}-1, t\bar{n}} & \dots & b_{(s+1)\bar{n}-1, (t+1)\bar{n}-1} \end{pmatrix}.$$

For example, if  $p = 9$ ,  $\phi(x) = (x/3, x \bmod 3)$ , and  $n = 6$ , then  $A$  would be partitioned as follows.

Process 0	Process 1	Process 2
-----------	-----------	-----------

$A_{00} = \begin{pmatrix} a_{00} & a_{01} \\ a_{10} & a_{11} \end{pmatrix}$	$A_{01} = \begin{pmatrix} a_{02} & a_{03} \\ a_{12} & a_{13} \end{pmatrix}$	$A_{02} = \begin{pmatrix} a_{04} & a_{05} \\ a_{14} & a_{15} \end{pmatrix}$
Process 3 $A_{10} = \begin{pmatrix} a_{20} & a_{21} \\ a_{30} & a_{31} \end{pmatrix}$	Process 4 $A_{11} = \begin{pmatrix} a_{22} & a_{23} \\ a_{32} & a_{33} \end{pmatrix}$	Process 5 $A_{12} = \begin{pmatrix} a_{24} & a_{25} \\ a_{34} & a_{35} \end{pmatrix}$
Process 6 $A_{20} = \begin{pmatrix} a_{40} & a_{41} \\ a_{50} & a_{51} \end{pmatrix}$	Process 7 $A_{21} = \begin{pmatrix} a_{42} & a_{43} \\ a_{52} & a_{53} \end{pmatrix}$	Process 8 $A_{22} = \begin{pmatrix} a_{44} & a_{45} \\ a_{54} & a_{55} \end{pmatrix}$

In Fox's algorithm, the block submatrices,  $A_{rs}$  and  $B_{st}$ ,  $s = 0, 1, \dots, q - 1$ , are multiplied and accumulated on process  $\phi^{-1}(r, t)$ . The basic algorithm is:

```

do step = 0, q - 1
  1. Choose a submatrix of A from each row of processes.
  2. In each row of processes broadcast the submatrix
     chosen in that row to the other processes in that row.
  3. On each process, multiply the newly received submatrix
     of A by the submatrix of B currently residing on the
     process.
  4. On each process, send the submatrix of B to the
     process directly above. (On processes in the first row,
     send the submatrix to the last row.)
enddo

```

The submatrix chosen in the  $r^{\text{th}}$  row is  $A_{r,u}$ , where

$$u = (r + \text{step}) \bmod q.$$

## 6.2 Communicators

If we try to implement Fox's algorithm, it becomes apparent that our work will be greatly facilitated if we can treat certain subsets of processes as a communication universe --- at least on a temporary basis. For example, in the pseudo-code

```

2. In each row of processes broadcast the submatrix chosen in
   that row to the other processes in that row.

```

it would be useful to treat each row of processes as a communication universe, while in the statement

4. On each process, send the submatrix of B to the process directly above. (On processes in the first row, send the submatrix to the last row.)

it would be useful to treat each column of processes as a communication universe.

The mechanism that MPI provides for treating a subset of processes as a “communication” universe is the *communicator*. Up to now, we’ve been loosely defining a communicator as a collection of processes that can send messages to each other. However, now that we want to construct our own communicators, we will need a more careful discussion.

In MPI, there are two types of communicators: *intra-communicators* and *inter-communicators*.

Intra-communicators are essentially a collection of processes that can send messages to each other *and* engage in collective communication operations. For example, `MPI_COMM_WORLD` is an intra-communicator, and we would like for each row and each column of processes in Fox’s algorithm to form an intra-communicator. Inter-communicators, as the name implies, are used for sending messages between processes belonging to *disjoint* intra-communicators. For example, an inter-communicator would be useful in an environment that allowed one to dynamically create processes: a newly created set of processes that formed an intra-communicator could be linked to the original set of processes (e.g., `MPI_COMM_WORLD`) by an inter-communicator. We will only discuss intra-communicators. The interested reader is referred to [4] for details on the use of inter-communicators.

A minimal (intra-)communicator is composed of

- a *Group*, and
- a *Context*.

A group is an ordered collection of processes. If a group consists of  $p$  processes, each process in the group is assigned a unique *rank*, which is just a nonnegative integer in the range  $0, 1, \dots, p-1$ . A context can be thought of as a system-defined tag that is attached to a group. So two processes that belong to the same group and that use the same context can communicate. This pairing of a group with a context is the most basic form of a communicator. Other data can be associated to a communicator. In particular, a structure or topology can be imposed on the processes in a communicator, allowing a more natural addressing scheme. We’ll discuss topologies in section 6.5.

## 6.3 Working with Groups, Contexts, and Communicators

To illustrate the basics of working with communicators, let's create a communicator whose underlying group consists of the processes in the first row of our virtual grid. Suppose that `MPI_COMM_WORLD` consists of  $p$  processes, where  $q^2 = p$ . Let's also suppose that  $\phi(x) = (x/q, x \bmod q)$ . So the first row of processes consists of the processes with ranks 0, 1, ...,  $q - 1$ . (Here, the ranks are in `MPI_COMM_WORLD`.) In order to create the group of our new communicator, we can execute the following code.

```
PROGRAM ComCrt
  INCLUDE 'mpif.h'
  IMPLICIT NONE
  integer, parameter12 :: MAX_PROCS = 100
  integer          p
  real             p_real
  integer          q
  integer          my_rank
  integer          MPI_GROUP_WORLD
  integer          first_row_group
  integer          first_row_comm
  integer          process_ranks(0:MAX_PROCS-1)
  integer          proc
  integer          test
  integer          sum
  integer          my_rank_in_first_row
  integer          ierr

C
C
  test = 0
  call MPI_INIT( ierr )
  call MPI_COMM_SIZE(MPI_COMM_WORLD, p, ierr )
  call MPI_COMM_RANK(MPI_COMM_WORLD, my_rank, ierr )

C
  p_real = p
  q = sqrt(p_real)

C
C Make a list of the processes in the new communicator.
  do proc = 0, q-1
    process_ranks(proc) = proc
  enddo

C
C Get the group underlying MPI_COMM_WORLD
  call MPI_COMM_GROUP(MPI_COMM_WORLD, MPI_GROUP_WORLD, ierr )

C
```

---

<sup>12</sup> An integer with the attribute “parameter” means it is a integer symbolic constant and cannot be changed at run time.

```

C  Create the new group
    call MPI_GROUP_INCL(MPI_GROUP_WORLD, q, process_ranks,
+                        first_row_group, ierr)
C
C  Create the new communicator
    call MPI_COMM_CREATE(MPI_COMM_WORLD, first_row_group,
+                        first_row_comm, ierr)
C

```

This code proceeds in a fairly straightforward fashion to build the new communicator. First it creates a list of the processes to be assigned to the new communicator. Then it creates a group consisting of these processes. This required two commands: first get the group associated with `MPI_COMM_WORLD`, since this is the group from which the processes in the new group will be taken; then create the group with `MPI_Group_incl`. Finally, the actual communicator is created with a call to `MPI_Comm_create`. The call to `MPI_Comm_create` implicitly associates a context with the new group. The result is the communicator `first_row_comm`. Now the processes in `first_row_comm` can perform collective communication operations. For example, process 0 (in `first_row_group`) can broadcast `A00` to the other processes in `first_row_group`.

```

integer my_rank_in_first_row
real, allocatable13, dimension( :, : )14 ::15 A_00

if (my_rank < q) then
    call MPI_COMM_RANK(first_row_comm,
+                      my_rank_in_first_row, ierr)
    ! Allocate space for A_00, order n_bar.
    allocate (A_00(n_bar,n_bar))16
    if (my_rank_in_first_row == 0) then
        ! initialize A_00
    endif
    call MPI_BCAST( A_00, n_bar*n_bar, MPI_INTEGER, 0,
+                  first_row_comm, ierr)
endif

```

---

<sup>13</sup> Allocatable is an attribute of a variable. It means that the array can be dynamically allocated at run time.

<sup>14</sup> "dimension(:, :)" means the array is two dimensional and the size of the two dimension is unknown at compile time. The array have to be allocated at run time.

<sup>15</sup> :: is a separator between variable attributes and variable names.

<sup>16</sup> The function "Allocate " allocates memory space for an allocatable array.



Groups and communicators are *opaque objects*. From a practical standpoint, this means that the details of their internal representation depend on the particular implementation of MPI, and, as a consequence, they cannot be directly accessed by the user. Rather the user accesses a *handle* that references the opaque object, and the opaque objects are manipulated by special MPI functions, for example, `MPI_Comm_create`, `MPI_Group_incl`, and `MPI_Comm_group`.

Contexts are not explicitly used in any MPI functions. Rather they are implicitly associated with groups when communicators are created. The syntax of the commands we used to create `first_row_comm` is fairly self-explanatory. The first command

```
MPI_Comm_group(comm, group, ierror)
integer comm, group, ierror
```

simply returns the group underlying the communicator `comm`.

The second command

```
MPI_Group_incl(old_group, new_group_size,
+ranks_in_old_group, new_group, ierror)
integer old_group, new_group_size,
integer ranks_in_old_group(*), new_group, ierror
```

creates a new group from a list of processes in the existing group `old_group`. The number of processes in the new group is `new_group_size`, and the processes to be included are listed in `ranks_in_old_group`. Process 0 in `new_group` has rank `ranks_in_old_group(0)` in `old_group`, process 1 in `new_group` has rank `ranks_in_old_group(1)` in `old_group`, etc.

The final command

```
MPI_Comm_create(old_comm, new_group, new_comm, ierror)
integer old_comm, new_group, new_comm, ierror
```

associates a context with the group `new_group` and creates the communicator `new_comm`. All of the processes in `new_group` belong to the group underlying `old_comm`.

There is an extremely important distinction between the first two functions and the third. `MPI_Comm_group` and `MPI_Group_incl`, are both *local* operations. That is, there is *no* communication among processes involved in their execution. However, `MPI_Comm_create` *is* a collective operation. *All* the processes in `old_comm` must call `MPI_Comm_create` with the same arguments. The *Standard* [4] gives three reasons for this:

1. It allows the implementation to layer `MPI_Comm_create` on top of regular collective communications.
2. It provides additional safety.
3. It permits implementations to avoid communication related to context creation.

Note that since `MPI_Comm_create` is collective, it will behave, in terms of the data transmitted, as if it synchronizes. In particular, if several communicators are being created, they must be created in the same order on all the processes.

## 6.4 MPI\_Comm\_split

In our matrix multiplication program we need to create multiple communicators --- one for each row of processes and one for each column. This would be an extremely tedious process if  $p$  were large and we had to create each communicator using the three functions discussed in the previous section. Fortunately, MPI provides a function, `MPI_Comm_split` that can create several communicators simultaneously. As an example of its use, we'll create one communicator for each row of processes.

```
integer my_row_comm
integer my_row

C my_rank is rank in MPI_COMM_WORLD.
C q*q = p
  my_row = my_rank/q
  call MPI_COMM_SPLIT(MPI_COMM_WORLD, my_row, my_rank,
+      my_row_comm, ierr)
```

The single call to `MPI_Comm_split` creates  $q$  new communicators, all of them having the same name, `my_row_comm`. For example, if  $p = 9$ , the group underlying `my_row_comm` will consist of the processes 0, 1, and 2 on processes 0, 1, and 2. On processes 3, 4, and 5, the group underlying `my_row_comm` will consist of the processes 3, 4, and 5, and on processes 6, 7, and 8 it will consist of processes 6, 7, and 8.

The syntax of `MPI_Comm_split` is

```
MPI_COMM_SPLIT(old_comm, split_key, rank_key,
+      new_comm, ierror)
integer old_comm, split_key, rank_key, new_comm, ierror
```

It creates a new communicator for each value of `split_key`. Processes with the same value of `split_key` form a new group. The rank in the new group is determined by the value of `rank_key`. If process  $A$  and process  $B$  call `MPI_Comm_split` with the same value of `split_key`, and the `rank_key` argument passed by process  $A$  is less than that passed by process  $B$ , then the rank of  $A$  in the group underlying `new_comm` will be less than the rank of process  $B$ . If they call the function with the same value of `rank_key`, the system will arbitrarily assign one of the processes a lower rank.

`MPI_Comm_split` is a collective call, and it must be called by all the processes in `old_comm`. The function can be used even if the user doesn't wish to assign every process to a new

communicator. This can be accomplished by passing the predefined constant `MPI_UNDEFINED` as the `split_key` argument. Processes doing this will have the predefined value `MPI_COMM_NULL` returned in `new_comm`.

## 6.5 Topologies

Recollect that it is possible to associate additional information --- information beyond the group and context --- with a communicator. This additional information is said to be *cached* with the communicator, and one of the most important pieces of information that can be cached with a communicator is a topology. In MPI, a *topology* is just a mechanism for associating different addressing schemes with the processes belonging to a group. Note that MPI topologies are *virtual* topologies --- there may be no simple relation between the process structure defined by a virtual topology, and the actual underlying physical structure of the parallel machine.

There are essentially two types of virtual topologies that can be created in MPI --- a *cartesian* or *grid* topology and a *graph* topology. Conceptually, the former is subsumed by the latter. However, because of the importance of grids in applications, there is a separate collection of functions in MPI whose purpose is the manipulation of virtual grids.

In Fox's algorithm we wish to identify the processes in `MPI_COMM_WORLD` with the coordinates of a square grid, and each row and each column of the grid needs to form its own communicator. Let's look at one method for building this structure.

We begin by associating a square grid structure with `MPI_COMM_WORLD`. In order to do this we need to specify the following information.

1. The number of dimensions in the grid. We have 2.
2. The size of each dimension. In our case, this is just the number of rows and the number of columns. We have  $q$  rows and  $q$  columns.
3. The periodicity of each dimension. In our case, this information specifies whether the first entry in each row or column is "adjacent" to the last entry in that row or column, respectively. Since we want a "circular" shift of the submatrices in each column, we want the second dimension to be periodic. It's unimportant whether the first dimension is periodic.
4. Finally, MPI gives the user the option of allowing the system to optimize the mapping of the grid of processes to the underlying physical processors by possibly reordering the processes in the group underlying the communicator. Since we don't need to preserve the ordering of the processes in `MPI_COMM_WORLD`, we should allow the system to reorder.

Having made all these decisions, we simply execute the following code.

```
integer      grid_comm
integer      dim_sizes(0:1)
```

```

logical      wrap_around(0:1)
logical      reorder17 = .TRUE.

dim_sizes(0) = q
dim_sizes(1) = q
wrap_around(0) = .TRUE.
wrap_around(1) = .TRUE.
call MPI_CART_CREATE(MPI_COMM_WORLD, 2, dim_sizes,
+      wrap_around, reorder, grid_comm, ierr)

```

After executing this code, the communicator `grid_comm` will contain all the processes in `MPI_COMM_WORLD` (possibly reordered), and it will have a two-dimensional cartesian coordinate system associated. In order for a process to determine its coordinates, it simply calls the function `MPI_Cart_coords` :

```

integer      coordinates(0:1)
integer      my_grid_rank

call MPI_COMM_RANK(grid_comm, my_grid_rank, ierr)
call MPI_CART_COORDS(grid_comm, my_grid_rank, 2,
+      coordinates, ierr)

```

Notice that we needed to call `MPI_Comm_rank` in order to get the process rank in `grid_comm`. This was necessary because in our call to `MPI_Cart_create` we set the `reorder` flag to `.TRUE.` , and hence the original process ranking in `MPI_COMM_WORLD` may have been changed in `grid_comm`.

The “inverse” to `MPI_Cart_coords` is `MPI_Cart_rank`.

```

call MPI_CART_RANK(grid_comm, coordinates, grid_rank,
+      ierr)
integer grid_comm, coordinates(*), grid_rank, ierr

```

Given the coordinates of a process, `MPI_Cart_rank` returns the rank of the process in its third parameter `process_rank`.

The syntax of `MPI_Cart_create` is

```

call MPI_CART_CREATE(old_comm, number_of_dims, dim_sizes,
+      periods, reorder, cart_comm, ierror)
integer old_comm, number_of_dims, dim_sizes(*)
logical periods(*), reorder
integer cart_comm, ierror

```

---

<sup>17</sup> This syntax initialize the variable.

**MPI\_Cart\_create** creates a new communicator, **cart\_comm** by caching a cartesian topology with **old\_comm**. Information on the structure of the cartesian topology is contained in the parameters **number\_of\_dims**, **dim\_sizes**, and **periods**. The first of these, **number\_of\_dims**, contains the number of dimensions in the cartesian coordinate system. The next two, **dim\_sizes** and **periods**, are arrays with order equal to **number\_of\_dims**. The array **dim\_sizes** specifies the order of each dimension, and **periods** specifies whether each dimension is circular or linear.

The processes in **cart\_comm** are ranked in *row-major* order. That is, the first row consists of processes 0, 1, ..., **dim\_sizes**(0)-1, the second row consists of processes **dim\_sizes**(0), **dim\_sizes**(0)+1, ..., 2\***dim\_sizes**(0)-1, etc. Thus it may be advantageous to change the relative ranking of the processes in **old\_comm**. For example, suppose the *physical* topology is a 3 x 3 grid, and the processes (numbers) in **old\_comm** are assigned to the processors (grid squares) as follows.

3	4	5
0	1	2
6	7	8

Clearly, the performance of Fox's algorithm would be improved if we re-numbered the processes. However, since the user doesn't know what the exact mapping of processes to processors is, we must let the system do it by setting the **reorder** parameter to **.TRUE.** .

Since **MPI\_Cart\_create** constructs a new communicator, it is a collective operation.

The syntax of the address information functions is

```

MPI_Cart_rank(comm, coordinates, rank, ierror)
integer comm, coordinates(*), rank, ierror

MPI_Cart_coords(comm, rank, number_of_dims, coordinates,
+ ierror)
integer comm, rank, number_of_dims, coordinates(*), ierror

```

**MPI\_Cart\_rank** returns the rank in the cartesian communicator **comm** of the process with cartesian coordinates **coordinates**. So **coordinates** is an array with order equal to the number of dimensions in the cartesian topology associated with **comm**. **MPI\_Cart\_coords** is the inverse to **MPI\_Cart\_rank**: it returns the coordinates of the process with rank **rank** in the cartesian communicator **comm**. Note that both of these functions are local.

## 6.6 MPI\_Cart\_sub

We can also partition a grid into grids of lower dimension. For example, we can create a communicator for each row of the grid as follows.

```
logical varying_coords(0:1)
integer row_comm

varying_coords(0) = .FALSE.
varying_coords(1) = .TRUE.
call MPI_CART_SUB(grid_comm, varying_coords, row_comm, ierr)
```

The call to `MPI_Cart_sub` creates `q` new communicators. The `varying_coords` argument is an array of boolean. It specifies whether each dimension “belongs” to the new communicator. Since we’re creating communicators for the rows of the grid, each new communicator consists of the processes obtained by fixing the row coordinate and letting the column coordinate *vary*. Hence we assigned `varying_coords(0)` the value `.FALSE.` --- the first coordinate doesn’t vary --- and we assigned `varying_coords(1)` the value `.TRUE.` --- the second coordinate varies. On each process, the new communicator is returned in `row_comm`. In order to create the communicators for the columns, we simply reverse the assignments to the entries in `varying_coords`.

```
integer col_comm

varying_coords(0) = .TRUE.
varying_coords(1) = .FALSE.
call MPI_CART_SUB(grid_comm, varying_coords, row_comm, ierr)
```

Note the similarity of `MPI_Cart_sub` to `MPI_Comm_split`. They perform similar functions -- they both partition a communicator into a collection of new communicators. However, `MPI_Cart_sub` can only be used with a communicator that has an associated cartesian topology, and the new communicators can only be created by fixing (or varying) one or more dimensions of the old communicators. Also note that `MPI_Cart_sub` is, like `MPI_Comm_split`, a collective operation.

## 6.7 Implementation of Fox's Algorithm

To complete our discussion, let’s write the code to implement Fox’s algorithm. First, we’ll write a function that creates the various communicators and associated information. Since this requires a large number of variables, and we’ll be using this information in other functions, we’ll put it into a Fortran 90 derived type to facilitate passing it among the various functions.

Notice that since each of our communicators has an associated topology, we constructed them using the topology construction functions --- `MPI_Cart_create` and `MPI_Cart_sub` --- rather

than the more general communicator construction functions `MPI_Comm_create` and `MPI_Comm_split`.

```

program myfox
include 'mpif.h'
IMPLICIT NONE
type GRID_INFO_TYPE
    integer p          ! Total number of processes.
    integer comm        ! Communicator for the entire grid.
    integer row_comm    ! Communicator for my row.
    integer col_comm    ! Communicator for my col.
    integer q          ! Order of grid.
    integer my_row      ! My row number.
    integer my_col      ! My column number.
    integer my_rank     ! My rank in the grid communicator.
end type GRID_INFO_TYPE

TYPE (GRID_INFO_TYPE) :: grid_info
integer my_rank, ierr
real, allocatable, dimension(:, :) :: A,B,C
integer n, n_bar

call MPI_INIT(ierr)
call Setup_grid(grid_info)

call MPI_Comm_rank(MPI_COMM_WORLD, my_rank, ierr)
if (my_rank == 0) then
    print *, 'What is the order of the matrices?'
    read *, n
endif

call MPI_BCAST(n,1,MPI_INTEGER, 0, MPI_COMM_WORLD,ierr)
n_bar = n/(grid_info%q)
! Allocate local storage for local matrix.
allocate( A(n_bar,n_bar) )
allocate( B(n_bar,n_bar) )
allocate( C(n_bar,n_bar) )

A = 1.018
B = 2.0
call Fox(n,grid_info,A,B,C,n_bar)
print *, C

contains19
subroutine Setup_grid(grid)

```

---

<sup>18</sup> This is Fortran 90 array syntax. It assigns every element of array A to be 1.0 .

<sup>19</sup> In Fortran 90, it is permissible to include a procedure as an integral part of a program unit. The program unit can invoke the internal procedure. This inclusion is done by the statement “contains”.

```

TYPE (GRID_INFO_TYPE), intent(inout)20 :: grid

integer old_rank
integer dimensions(0:1)
logical periods(0:1)
integer coordinates(0:1)
logical varying_coords(0:1)
integer ierr

! Set up Global Grid Information.
call MPI_Comm_size(MPI_COMM_WORLD, grid%p, ierr)
call MPI_Comm_rank(MPI_COMM_WORLD, old_rank, ierr )
grid%q = int(sqrt(dble(grid%p)))
dimensions(0) = grid%q
dimensions(1) = grid%q
periods(0) = .TRUE.
periods(1) = .TRUE.
call MPI_Cart_create(MPI_COMM_WORLD, 2,
+   dimensions, periods, .TRUE. , grid%comm, ierr)
call MPI_Comm_rank (grid%comm, grid%my_rank, ierr )
call MPI_Cart_coords(grid%comm, grid%my_rank, 2,
+   coordinates, ierr )
grid%my_row = coordinates(0)
grid%my_col = coordinates(1)

! Set up row and column communicators.
varying_coords(0) = .FALSE.
varying_coords(1) = .TRUE.
call MPI_Cart_sub(grid%comm,varying_coords,
+   grid%row_comm,ierr)
varying_coords(0) = .TRUE.
varying_coords(1) = .FALSE.
call MPI_Cart_sub(grid%comm,varying_coords,
+   grid%col_comm,ierr)
end subroutine Setup_grid

subroutine Fox(n,grid,local_A,local_B,local_C,n_bar)
integer, intent(in) :: n, n_bar
TYPE(GRID_INFO_TYPE), intent(in) :: grid
real, intent(in) , dimension(:,:) :: local_A, local_B
real, intent(out), dimension ([:,]) :: local_C

real temp_A( SIZE(A,DIM=1),SIZE(A,DIM=2) )
integer step, source, dest, request
integer status(MPI_STATUS_SIZE), bcast_root

local_C = 0.0
source = mod( (grid%my_row + 1), grid%q )

```

---

<sup>20</sup> intent(inout) is an attribute of dummy argument. It informs the compiler that this dummy argument may be used for read and write inside the subroutine.



```

dest    = mod( (grid%my_row + grid%q -1), (grid%q) )
temp_A = 0.0

do step = 0, grid%q -1
    bcast_root = mod( (grid%my_row + step), (grid%q) )
    if (bcast_root == grid%my_col) then
        call MPI_BCAST(local_A,n_bar*n_bar,MPI_REAL,
+             bcast_root, grid%row_comm, ierr)
        call sgemm('N','N',n_bar,n_bar,n_bar,1.0,
+ local_A,n_bar,local_B,n_bar,1.0,local_C,n_bar)
    else
        call MPI_BCAST(temp_A,n_bar*n_bar,MPI_REAL,
+             bcast_root, grid%row_comm, ierr)
        call sgemm('N','N',n_bar,n_bar,n_bar,1.0,
+             temp_A,n_bar,local_B,n_bar,1.0,local_C,n_bar)
    endif
    call MPI_Send(local_B,n_bar*n_bar,MPI_REAL,dest, 0,
+             grid%col_comm, ierr)
    call MPI_Recv(local_B,n_bar*n_bar,MPI_REAL,source,0,
+             grid%col_comm, status, ierr )

enddo
end subroutine Fox

end program myfox

```

## 7. Where To Go From Here

### 7.1 What We Haven't Discussed

MPI is a large library. The Standard [4] is over 200 pages long and it defines more than 125 functions. As a consequence, this *Guide* has covered only a small fraction of MPI, and many readers will fail to find a discussion of functions that they would find very useful in their applications. So we briefly list some of the more important ideas in MPI that we have not discussed here.

1. **Communication Modes.** We have used only the *standard* communication mode for *send*. This means that it is up to the system to decide whether the message is buffered. MPI provides three other communication modes: *buffered*, *synchronous*, and *ready*. In buffered mode, the user explicitly controls the buffering of outgoing messages. In synchronous mode, a send will not complete until a matching receive is posted. In ready mode, a send may be started only if a matching receive has already been posted. MPI provides three additional send functions for these modes.
2. **Nonblocking Communication.** We have used only *blocking* sends and receives (MPI\_Send and MPI\_Recv.) For the send, this means that the call won't return until the message data and envelope have been buffered or sent --- i.e., until the memory referenced in the call to MPI\_Send is available for re-use. For the receive, this means that the call won't return until the data has been received into the memory referenced in the call to MPI\_Recv. Many applications can improve their performance by using *nonblocking* communication. This means that the calls to send/receive may return before the operation completes. For example, if the machine has a separate communication processor, a non-blocking send could simply notify the communication processor that it should begin composing and sending the message. MPI provides nonblocking sends in each of the four modes and a nonblocking receive. It also provides various utility functions for determining the completion status of a non-blocking operation.
3. **Inter-communicators.** Recollect that MPI provides two types of communicators: intra-communicators and inter-communicators. Inter-communicators can be used for point-to-point communications between processes belonging to distinct intra-communicators.

There are many other functions available to users of MPI. If we haven't discussed a facility you need, please consult the *Standard* [4] to determine whether it is part of MPI.

## 7.2 Implementations of MPI

If you don't have an implementation of MPI, there are three versions that are freely available by anonymous ftp from the following sites.

- Argonne National Lab/Mississippi State University. The address is `info.mcs.anl.gov`, and the directory is `pub/mpi`.
- Edinburgh University. The address is `ftp.epcc.ed.ac.uk`, and the directory is `pub/chimp/release`.
- Ohio Supercomputer Center. The address is `tbag.osc.edu`, and the directory is `pub/lam`.

All of these run on networks of UNIX workstations. The Argonne/Mississippi State and Edinburgh versions also run on various parallel processors. Check the “README” files to see if your machine(s) are supported.

## 7.3 More Information on MPI

There is an MPI FAQ available by anonymous ftp at

- Mississippi State University. The address is `ftp.erc.msstate.edu`, and the file is `pub/mpi/faq`.

There are also numerous web pages devoted to MPI. A few of these are

- <http://www.epm.ornl.gov/~walker/mpi>. The Oak Ridge National Lab MPI web page.
- <http://www.erc.msstate.edu/mpi>. The Mississippi State MPI web page.
- <http://www.mcs.anl.gov/mpi>. The Argonne MPI web page.

Each of these sites contains a wealth of information about MPI. Of particular note, the Mississippi State page contains a bibliography of papers on MPI, and the Argonne page contains a collection of test MPI programs.

The *MPI Standard* [4] is currently available from each of the sites above. This is, of course, the definitive statement of what MPI is. So if you're not clear on something, this is the final arbiter. It also contains a large number of nice examples of uses of the various MPI functions. So it is considerably more than just a reference. Currently, several members of the MPI Forum are working on an annotated version of the MPI standard [5].

The book [2] is a tutorial introduction to MPI. It provides numerous complete examples of MPI programs.

The book [6] contains a tutorial introduction to MPI (on which this guide is based). It also contains a more general introduction to parallel processing and the programming of message-passing machines.

The Usenet newsgroup, `comp.parallel.mpi`, provides information on updates to all of these documents and software.

## 7.4 The Future of MPI

As it is currently defined, MPI fails to specify two critical concepts: I/O and the creation/destruction of processes. Work has already been started on the development of both I/O facilities and dynamic process creation. Information on the former can be obtained from <http://lovelace.nas.nasa.gov/MPI-IO/mpi-io.html>, and information on the latter can be found on the Argonne MPI web page. Significant developments are invariably posted to `comp.parallel.mpi`.

## 8. Compiling and Running MPI Programs

This section is intended to give the outline of how to compile and run a program in the IBM SP2.

MPI program written in Fortran or Fortran 90 can be compiled using the following command :

```
mpif77 program.f
```

By default, the program will be running on 4 processors of the SP2. The program can be invoked by the name of executable

```
a.out
```

The number of processes is controled by the environment variable MP\_PROCS. The web page <http://www.hku.hk/cc/sp2/technical/setenv.html> has manuals for setting the environment variable.

## 9. Reference

- [1] Geoffrey Fox, et al., *Solving Problems on Concurrent Processors*, Englewood Cliffs, NJ, Prentice--Hall, 1988.
- [2] William Gropp, Ewing Lusk, and Anthony Skjellum, *Using MPI: Portable Parallel Programming with the Message-Passing Interface*, Cambridge, MA, MIT Press, 1994.
- [3] Brian W. Kernighan and Dennis M. Ritchie, *The C Programming Language*, 2nd ed., Englewood Cliffs, NJ, Prentice--Hall, 1988.
- [4] Message Passing Interface Forum, *MPI: A Message-Passing Interface Standard*, International Journal of Supercomputer Applications, vol 8, nos 3/4, 1994. Also available as Technical Report CS-94-230, Computer Science Dept., University of Tennessee, Knoxville, TN, 1994.
- [5] Steve Otto, et al., *MPI Annotated Reference Manual*, Cambridge, MA, MIT Press, to appear.
- [6] Peter S. Pacheco, *Programming Parallel with MPI*, San Francisco, CA, Morgan Kaufmann. 1997.
- [7] Peter S. Pacheco, *A User's Guide to MPI*, 1995.