

# A Sweet Introduction to the Mathematical Analysis of Time-Resolved Spectra and Complex Kinetic Mechanisms: The Chameleon Reaction Revisited

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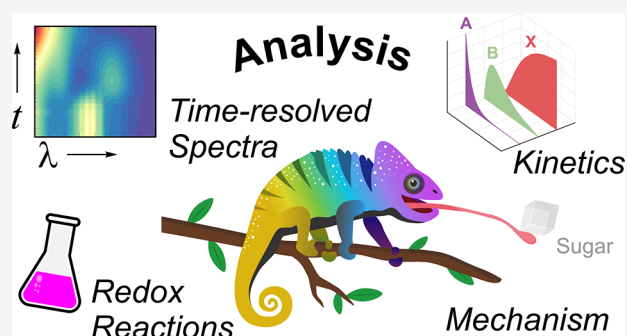
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**ABSTRACT:** We present a detailed yet easy-to-follow discussion of the mathematical treatment of time-resolved spectroscopic data in a model-based approach. This is accompanied and complemented by an example of a colorful and pedagogically rich chemical reaction: the permanganate oxidation of sugars in basic aqueous media (often known as the chameleon reaction). Our *sweet* approach allows both students and lecturers to tackle the problem of a model-based analysis of time-resolved data in a simple manner and one step at the time, while also exercising programming and data analysis skills—fundamental for present and future chemists of all levels.

**KEYWORDS:** Upper-Division Undergraduate, Graduate Education/Research, Physical Chemistry, Computer-Based Learning, Problem Solving/Decision Making, Kinetics, Mathematics/Symbolic Mathematics, Mechanisms of Reactions, Oxidation/Reduction, Spectroscopy



## INTRODUCTION

Understanding the rates and mechanisms of chemical reactions is a matter of central importance in chemistry, biochemistry, and other fields. Chemists can monitor the twists and turns of the reactant on its way to the product, and the kinetic or rate constants of each step using time-resolved spectroscopy. Careful analysis of a series of spectra collected at different reaction times ultimately provides the spectroscopic signatures and rate constants of the proposed intermediates, confirming the mechanistic picture. Armed with this knowledge, for instance, the reaction conditions can be optimized to avoid side reactions and optimize product yield—as is commonly done in industry or in the lab.

The treatment of time-resolved spectra in the context of ultrafast spectroscopy has been described in vast detail by van Stokkum et al., who popularized the method of global and target analysis.<sup>1</sup> Other authors have published alternative data analysis implementations, including lifetime density analysis,<sup>2</sup> and multivariate curve resolution by alternating least-squares (MCR-ALS).<sup>3–6</sup> A recent review by Vauthey et al. in the context of ultrafast transient UV–vis and fluorescence upconversion spectroscopy summarizes these methods in detail.<sup>7</sup>

Apart from specific details intrinsic to the treatment of ultrafast transient spectra, these analysis methods are general and independent of the time scale of the studied processes, motivating us to introduce it to chemistry students at any stage

of their education. In the typical undergraduate chemistry curriculum, most emphasis is typically given to first- and second-order kinetics.<sup>8</sup> More complex cases are often neglected or treated at an approximate level (e.g., by using the steady-state approximation), and approximate kinetic equations are often derived for certain limiting cases. A more advanced treatment involves numerical integration of the complex systems of ordinary differential equations (ODEs) that arise in chemical kinetics.<sup>9–11</sup> These systems, however, are often *stiff*,<sup>12</sup> which can lead to numerically inaccurate solutions. An exhaustive description of numerical methods to solve systems of ODEs can be found elsewhere.<sup>13,14</sup>

In our previous work,<sup>15,16</sup> we established an analogy between viral spread during a pandemic and chemical kinetics, using it to introduce more complex reaction mechanisms and abstract concepts—such as the collision cross section. Other authors also developed analogies with chemical kinetics concepts,<sup>17–20</sup> and illustrated their power in helping the students master the fundamentals. Some of us have also applied complex kinetic schemes to model, for example,

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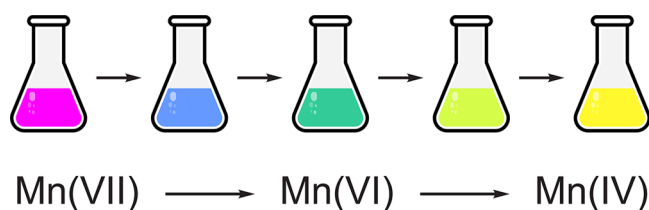
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electron transfer processes in surface-anchored molecular catalysts and photosensitizers for water splitting<sup>21,22</sup> or proton-coupled electron transfer processes in tungsten carbon-yls, where a dimerization takes place after the initial event,<sup>23</sup> and compared different strategies for the analysis of time-resolved data of protein nonequilibrium dynamics.<sup>24</sup>

Herein, we present a combined theoretical and practical treatment of more complex reaction mechanisms, exemplified by the oxidation of a carbohydrate in the presence of  $\text{KMnO}_4$ —often called the chemical *chameleon* reaction. This colorful reaction can be readily monitored by UV–vis absorption spectroscopy, and performed using inexpensive and readily available chemicals (Figure 1).



**Figure 1.** Sequence of color changes and oxidation states of Mn observed during the chemical chameleon reaction.

We have chosen the chemical chameleon reaction because of its simplicity, the availability of the required reagents, and the captivating color changes that take place—a fact that we will use to our advantage when discussing the UV–vis spectra. The chemical chameleon reaction is a widely performed demonstrative experiment in introductory chemistry laboratories, and can be used to teach fundamental concepts of redox chemistry.<sup>25–30</sup> In this reaction, a carbohydrate is oxidized by the permanganate ion in an alkaline aqueous medium. The rapid color changes are evidence of the different oxidation states of manganese—going from pink-violet  $\text{Mn(VII)}$ , to green  $\text{Mn(VI)}$ , and finally to yellow  $\text{Mn(IV)}$ , as seen in Figure 1.

The chameleon reaction can be easily monitored with the naked eye, and a series of UV–vis absorption spectra can be recorded for more quantitative spectrokinetic analysis. The time-dependent absorption spectra obtained from such experiments can be interpreted and fitted to a mechanistic model to further the students' understanding of key concepts in chemical kinetics and inorganic chemistry. The students will learn to carefully analyze and interpret time-dependent spectroscopic data, allowing them to extract rate constants and the spectroscopic signatures of the proposed intermediates in a complex reaction mechanism. The methods presented herein are general and can be adapted to specific mechanisms and to the study of other chemical reactions (by changing the kinetic/mechanistic model). Moreover, and as mentioned above, this approach can be adapted to all time scales—ranging from slow to ultrafast—and to other spectroscopic techniques—such as IR or NMR. Thanks to this, the students can even connect with the latest developments in ultrafast spectroscopy, obtaining tools to analyze the fastest chemical events by making analogies with slower reactions that can be monitored even with the naked eye.

## THEORETICAL BACKGROUND

In this section, we present a detailed mathematical treatment of chemical kinetics and spectrokinetic modeling, including

advanced concepts of linear algebra and differential equations (some of which are explained to a greater extent in the [Supporting Information \(SI\)](#)). This is provided herein in a tutorial manner to allow the interested reader to gain a deep understanding of the methods and the equations behind the analysis of time-resolved spectra.

### Initial Considerations

We start from a chemical reaction in which species A and B react through a series of steps, yielding a product, P. The overall reaction is eq 1:



The reaction rate ( $r$ ) is related to the rate of disappearance/formation of the reactants/products, as follows (eq 2):

$$r = -\frac{1}{a} \frac{d[A]}{dt} = -\frac{1}{b} \frac{d[B]}{dt} = \frac{1}{p} \frac{d[P]}{dt} \quad (2)$$

Let us assume that the reaction described in eq 1 follows from two consecutive elementary steps:



An *elementary reaction* or *elementary step* is a simple chemical equation describing the interaction that takes place at the molecular level, in a particular step of a reaction mechanism. These elementary steps may contain intermediate species which do not appear directly in the overall stoichiometric eq (eq 1)—for example, species X in eq 3. For an elementary reaction, we can write a *rate law*, which relates the concentrations of the reactants and the reaction rate. For the first elementary step, we have

$$-\frac{1}{a} \frac{d[A]}{dt} = -\frac{1}{b} \frac{d[B]}{dt} = k_1[A]^\alpha[B]^\beta \quad (4)$$

and for the second elementary step:

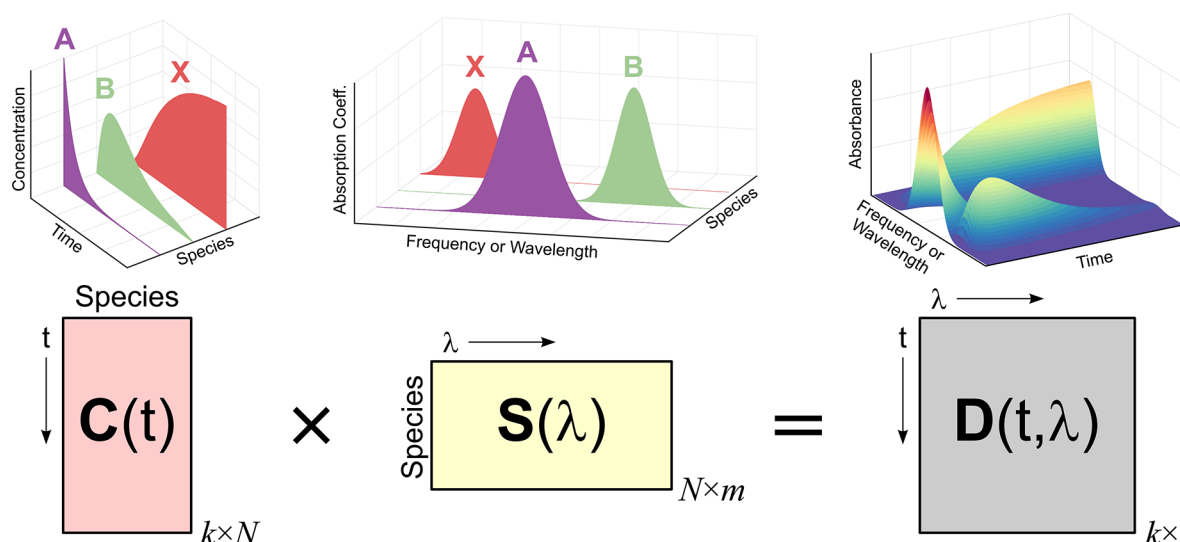
$$-\frac{1}{x} \frac{d[X]}{dt} = \frac{1}{p} \frac{d[P]}{dt} = k_2[X]^\chi \quad (5)$$

where the brackets denote concentrations of the species, and the exponents are experimentally determined coefficients (often integers), relating to the *order* of the reaction in terms of a given reactant. These exponents ( $\alpha$ ,  $\beta$ ,  $\chi$ ) may or may not be the same of the balancing coefficients ( $a$ ,  $b$ ,  $x$ ). The total order of the reaction is the sum of the reaction orders of all reactants.<sup>31</sup> The *rate constants* ( $k_1$ ,  $k_2$ ) are the proportionality constants relating the concentrations of the reactants with the rate. Its units depend on the rate law.

The rate laws can be integrated to yield the analytical time dependence of the concentration of each participating species. For simple and uncoupled reaction steps this is a trivial matter, and is often done in introductory chemical kinetics courses.<sup>8,32</sup>

A more complex case arises whenever there are several coupled elementary steps. For example, let us now consider an equilibrium followed by an irreversible reaction (e.g., a decomposition reaction, eq 6):





**Figure 2.** Visual representation of eq 12: Under the assumption of bilinearity, the product of a matrix containing the concentration profiles  $[C(t)]$  and a matrix with the spectra of each species  $[S(\lambda)]$ , yields the time-resolved absorption spectra,  $D(t, \lambda)$ .

In this case, the time dependence of the concentrations can no longer be derived based on a single differential equation (as in eq 4–5). Instead, we must solve a system of three coupled ordinary differential equations (eq 7) with three unknowns ( $[A]_t$ ,  $[B]_t$ , and  $[C]_t$  where the subscript  $t$  refers to the concentration at any time):

$$\begin{cases} \frac{d[A]_t}{dt} = -k_1[A]_t + k_{-1}[B]_t & 7a \\ \frac{d[B]_t}{dt} = +k_1[A]_t - k_{-1}[B]_t - k_2[B]_t & 7b \\ \frac{d[X]_t}{dt} = +k_2[B]_t & 7c \end{cases}$$

We will focus on mechanisms in which all stoichiometric coefficients are equal to 1, for which an analytical solution exists and is discussed next. More complex kinetic models have been discussed elsewhere.<sup>15,33,34</sup>

### Generalized Matrix Kinetics for First Order Reaction Systems

The problem of solving systems of coupled first-order reactions with matrix methods has been previously treated in detail in this *Journal* by Berberan-Santos and Martinho,<sup>33</sup> and by others.<sup>11,35</sup> We shall restate some of the concepts and methods in this paper so the reader can have a complete picture.

We start by designating a *species concentration vector*,  $C(t) = [A(t) \ B(t) \ X(t)]^T$ . This way, eq 7 can be expressed in matrix form as

$$\frac{d}{dt} \begin{pmatrix} [A]_t \\ [B]_t \\ [X]_t \end{pmatrix} = \begin{pmatrix} -k_1 & k_{-1} & 0 \\ k_1 & -k_{-1} - k_2 & 0 \\ 0 & k_2 & 0 \end{pmatrix} \begin{pmatrix} [A]_t \\ [B]_t \\ [X]_t \end{pmatrix} \quad (8)$$

More generally, for any first-order system:

$$\frac{d}{dt} C(t) = K \cdot C(t) \quad (9)$$

where  $K$  is an  $N \times N$  matrix (for a system with  $N$  species), often called the *transition* or *rate matrix*, and contains all the kinetic information about the model.

Since in eq 9 we have written  $C(t)$  as a column vector, the off-diagonal elements of  $K$ ,  $\{K\}_{ij}$  ( $i \neq j$ ), represent the net interconversion rates of species  $j$  in the kinetic equation of species  $i$ . For a system of  $N$  species obeying mass conservation, the sum of the elements of each column in  $K$  must be equal to zero. In this manner, the diagonal elements can be simply defined as the negative of the sum of all other elements in the column (eq 10).

$$\{K\}_{ii} = - \sum_{i=1, i \neq j}^N \{K\}_{ij} \quad (10)$$

The definition in eq 10 follows from the intuitive concept that every chemical species is changing only because of interconversion to/from other species.<sup>36</sup> An analytical solution to eq 8 is given by<sup>33</sup>

$$C(t) = \expm(Kt) \cdot C(0) \quad (11)$$

where  $C(0)$  is a vector containing the initial (known) concentrations of each species, and the term  $\expm(Kt)$  corresponds to a matrix exponential. Note the similarity between eq 11 and the more familiar scalar case. A discussion about the matrix exponential and a detailed description about the solution of a system of coupled first-order reactions with matrix methods are given in the SI, section 3.

### From Kinetics to Spectral Changes

Until now, we have focused in the kinetic (concentration) profiles of the different species involved in a reaction. We often monitor the spectral changes associated with the kinetic evolution of the system under study, leading us to the present description of time-resolved spectra. Under the assumption that the spectral properties of the involved species are time-independent, and that the kinetic profiles are independent of the detection channel—an assumption called *bilinearity* between the concentration and spectra—we can write an array of time-dependent spectra,  $D(t, \lambda)$ , as the product of a

species concentration matrix,  $C(t)$ , and a spectral matrix,  $S(\lambda)$ , eq 12 (graphically illustrated in Figure 2):<sup>7</sup>

$$D(t, \lambda) = C(t) \cdot S(\lambda) \quad (12)$$

From the definitions given above,  $C(t)$  is a  $k \times N$  matrix where every row corresponds to one sampled time point and every column to a different species. Similarly,  $S(\lambda)$  is an  $N \times m$  matrix where every row corresponds to a species and every column represents a spectral channel (i.e., wavelength or frequency). This leads to  $D(t, \lambda)$ , which is a matrix of time-resolved spectra containing  $k$  time points (rows) and  $m$  spectroscopic channels (columns).

As nicely explained by Vauthey and co-workers,<sup>7</sup> the assumed bilinearity of the time-dependent spectra can break down if either the assumption of classical kinetics (i.e., well-defined species and intermediates) or the assumption of time-invariant spectra of these species do not hold.

For example, in ultrafast transient experiments, solvent relaxation and fast population kinetics can compete with each other. In this scenario, no clear intermediates can be defined and thus no time-invariant species-associated spectral features can be described. Some examples of these scenarios are nicely discussed in ref 7, and are especially evident when studying solvation in ionic liquids.<sup>37,38</sup>

### The Inverse Problem: From Spectral Changes to Kinetic Profiles and Mechanisms

If we know the concentration profiles and species-associated spectra of a system, calculation of the time-resolved spectra that would be observed becomes a trivial matter, and could be done merely by using eq 12.

In practice, however, we wish to solve the *inverse* problem: we want to obtain the concentration profiles and species-associated spectra for the system under study, given a reasonable kinetic or spectral model.

To begin our discussion on the inverse problem, we start by characterizing a real experimental data set with noise ( $D_e$ ) in a manner analogous to eq 12. We calculate a parameter-dependent concentration matrix using a given kinetic model,  $C(t; \beta)$  (where  $\beta$  is the kinetic parameters), and obtain the best possible guess for a spectral matrix,  $\hat{S}(\lambda)$ —for which the circumflex indicates this is not an exact solution but an *estimated* one.<sup>7</sup> In this manner, we can define  $D_{\text{fit}}$  as

$$D_{\text{fit}}(t, \lambda; \beta) = C(t; \beta) \cdot \hat{S}(\lambda) \quad (13)$$

To calculate  $\hat{S}(\lambda)$ , we can take advantage of a mathematical tool called the Moore–Penrose pseudoinverse, explained in more detail in the SI, section 4.

We can use the Moore–Penrose pseudoinverse of  $C(t; \beta)$ , denoted  $C^+$ , to calculate  $\hat{S}(\lambda)$ , thus solving the problem from eq 13. It can be shown that this leads to the linear least-squares fit whenever an exact solution does not exist (i.e.,  $A$  is singular or rectangular).<sup>39</sup> We then arrive at the following equation (a full derivation is given in the SI, section 4):

$$C^+ D_e = C^+ C \cdot \hat{S} \quad \text{and hence} \quad \hat{S} = C^+ D_e \quad (14)$$

where the variables have been omitted for clarity, and  $D_e$  is the experimental data set. It can be shown that the calculated data set for a chosen set of parameters ( $\beta$ ) is<sup>40</sup>

$$D_{\text{fit}}(t, \lambda; \beta) = C(t; \beta) \cdot [C^+(t; \beta) \cdot D_e(t, \lambda)] \quad (15)$$

Variation of  $\beta$  would allow—using a least-squares minimization routine—to obtain the best-fitting reconstruction of the

experimental time-resolved spectra,  $D_{\text{opt}}(t, \lambda; \beta_{\text{opt}})$ , which minimizes the square of the norm of the residuals,  $\|D_{\text{fit}}(t, \lambda; \beta) - D_e(t, \lambda)\|^2$ .

Note that this procedure is general and independent of the functional form of  $C(t)$ , which allows for the implementation of kinetic schemes of arbitrary complexity toward the analysis of time-resolved spectra. Also important is to note that the dependence on  $\beta$  is nonlinear, and hence  $\beta_{\text{opt}}$  must be found iteratively.<sup>41</sup> An in-depth discussion of the algorithms for solving nonlinear least-squares problems with separable variables, particularly applied to the analysis of time-resolved spectra has been presented by van Stokkum et al. in ref 42.

We have included in the Supporting Information a set of fully functional MATLAB code, with a detailed description of both the code and the above procedure. We consider a generalized network of coupled first-order reactions as well as an arbitrary kinetic model defined by a system of ODEs. Simulation and fitting routines are also provided and discussed in detail.

## EXPERIMENTAL SECTION

### Chemicals and Solvents

All chemicals and reagents were used as received from their suppliers. The solutions were prepared in doubly distilled water. Stock solutions of  $\text{KMnO}_4$  in water were freshly prepared to avoid degradation upon storage. Information regarding safety precautions of used chemicals can be consulted in the SI, section 1.

### UV–Visible Spectrokinetic Measurements

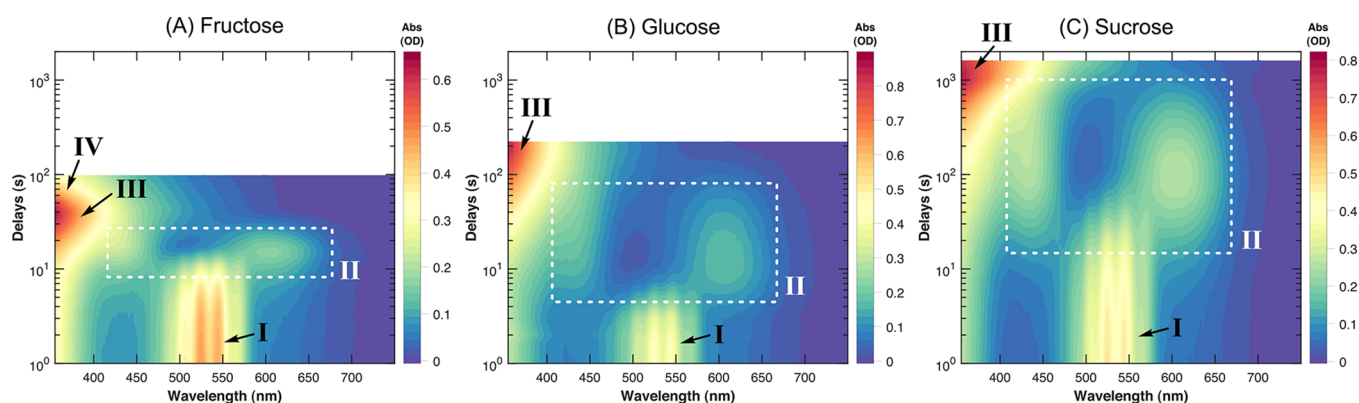
To acquire UV–vis absorption spectra of the reaction mixtures, a  $1 \times 1$  cm path length quartz cuvette, equipped with a small magnetic stir bar was coupled to a fiber optics spectrometer (Ocean Optics USB4000, with a DH-2000-BAL fiber-coupled tungsten/deuterium lamp). Optical filters before the sample cuvette were used to adapt the light intensity to the dynamic range of the detector.

Absorption spectra were recorded before and after the addition of 10  $\mu\text{L}$  of a 700 mM (7  $\mu\text{mol}$ ) aqueous stock solution of the corresponding sugar (*D*-glucose, *D*-fructose, or sucrose) to a freshly prepared reaction mixture containing 1.4 mL of dd- $\text{H}_2\text{O}$ , 500  $\mu\text{L}$  of 400 mM NaOH (200  $\mu\text{mol}$ ), and 1 mL of 0.5 mM  $\text{KMnO}_4$  (0.5  $\mu\text{mol}$ ). The cuvette was constantly stirred to minimize the mixing time. The initial concentrations of the sugar, NaOH and  $\text{KMnO}_4$  were equal to 2.4, 68.7, and 0.2 mM, respectively. Doubly distilled water was used to record the intensity background (blank spectrum). All measurements were run using the OceanView 2.0 software (Ocean Insight).

The reaction was monitored until formation of the yellow/brown  $\text{MnO}_2$  species was complete and no further color changes were evident to the naked eye. All reactions were complete within 10–30 min, depending strongly on the identity of the sugar and the starting concentrations of the reagents. The initial concentrations chosen above lead to a pseudo-first-order behavior of the bimolecular steps involving the sugar and the Mn species. This allows us to treat the data—to a very good approximation—with the first order kinetic models discussed herein, for a simplified pedagogical approach.

A video file which illustrates in real time the color and spectral changes observed during a typical experimental run is included in the SI.





**Figure 3.** Spectral changes observed during kinetic runs of the oxidation of fructose (A), glucose (B), and sucrose (C) with basic  $\text{KMnO}_4$ . All data sets are plotted from 1 to 2000 s in a logarithmic time axis for easier comparison. Roman numerals identify the main spectrokinetic features evident from the contour plots, see text for discussion.

## Data Analysis

All calculations were performed in MATLAB R2021b using homemade scripts, which build upon our previous examples of modeling arbitrary chemical kinetics.<sup>15</sup> We have adopted a data analysis strategy based in the concepts discussed in the [Theoretical Background](#) section of this paper. Further details on the implementation of the code are given in the [Supporting Information](#), with a detailed explanation and potential changes to the code to adapt it to a general kinetic model.

## RESULTS AND DISCUSSION

### Interpreting the Spectral Changes During the Chameleon Reaction

Contour maps of the time-dependent UV–vis absorption spectra recorded after adding the corresponding sugar to the basic  $\text{KMnO}_4$  solution are shown in [Figure 3](#). As is evident from the time scale of these plots, the overall reaction rates decrease in the order: fructose  $\gg$  glucose  $>$  sucrose. In the following we will examine the data in more detail.

We begin our dissection of the time-resolved spectra by discussing the main features evident in the contour maps ([Figure 3](#)). As indicated by Roman numerals I–III in the corresponding subplots of this figure, at least three main spectrokinetic features can be observed in all three sugars, and a fourth feature clearly appears in the fructose data set, the sugar with the fastest overall reaction rate.

While these spectrokinetic features suggest the presence of at least three or four intermediates, a more quantitative criterion is needed before considering a mechanism. The number of (spectrally) observable species will ultimately determine the number of components ( $N$ ) needed to build our concentration and species matrices. An over- or underestimation in the number of components can result in spurious or physically meaningless analysis, despite a potentially good fit.

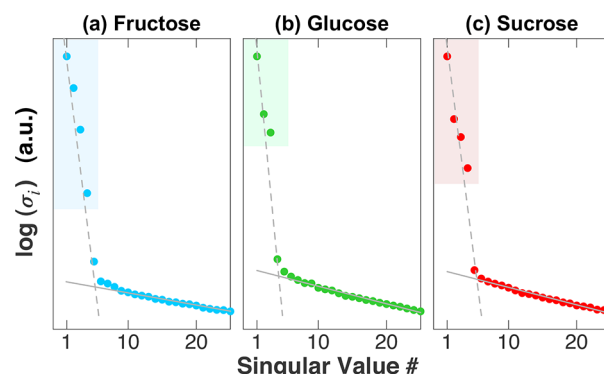
The singular value decomposition (SVD) of the array of time-resolved spectra provides a preliminary estimation on the number of spectrally observable components.

This mathematical decomposition expresses a real matrix ( $\mathbf{D}$ ) as the product of a diagonal matrix ( $\mathbf{\Sigma}$ ) and two real orthogonal matrices,  $\mathbf{U}$  and  $\mathbf{V}$  as follows:

$$\mathbf{D} = \mathbf{U}\mathbf{\Sigma}\mathbf{V}^T \quad (16)$$

where the columns of  $\mathbf{U}$  and  $\mathbf{V}$  are known, respectively, as the left- and right-singular vectors, and are related to the time ( $\mathbf{U}$ ) and spectral ( $\mathbf{V}$ ) components. The diagonal elements of  $\mathbf{\Sigma}$  are known as the *singular values* of  $\mathbf{D}$  (denoted as  $\sigma_i$ ). Choosing the decomposition as to sort the singular values in descending order, this factorization is unique up to a unitary transformation. SVD constitutes a generalization of the eigenvalue decomposition (diagonalization), the former being also applicable to rectangular matrices.

Whenever [eq 12](#) holds, the magnitude of the singular values gives an estimate on the number of components. For a noise-free data set, the number of nonzero  $\sigma_i$  is equal to  $N$ . In the presence of noise, there exists a cutoff point between significant  $\sigma_i$  and the noise level. This is illustrated in [Figure 4](#) for our three data sets. We observe that the first three/four



**Figure 4.** Relative magnitudes of the first 25 singular values of the fructose (A), glucose (B), and sucrose (C) data sets. Lines to guide the eye show the noise level (solid lines) and significant/non-noise singular values (dashed lines), the latter highlighted by colored boxes.

$\sigma_i$ 's are significantly higher than the rest (the vertical axis in [Figure 4](#) is logarithmic), and that the magnitude of the following  $\sigma_i$ 's decays roughly in an exponential manner with the index  $i$  (evidenced by a straight line in [Figure 4](#)).<sup>1</sup> This plot is often called a screeplot (see ref 43 for more details).

Having estimated the number of components, we then move on to a discussion of plausible reaction mechanisms, to ultimately fit a kinetic model to our data and to elucidate the spectra of the individual species.

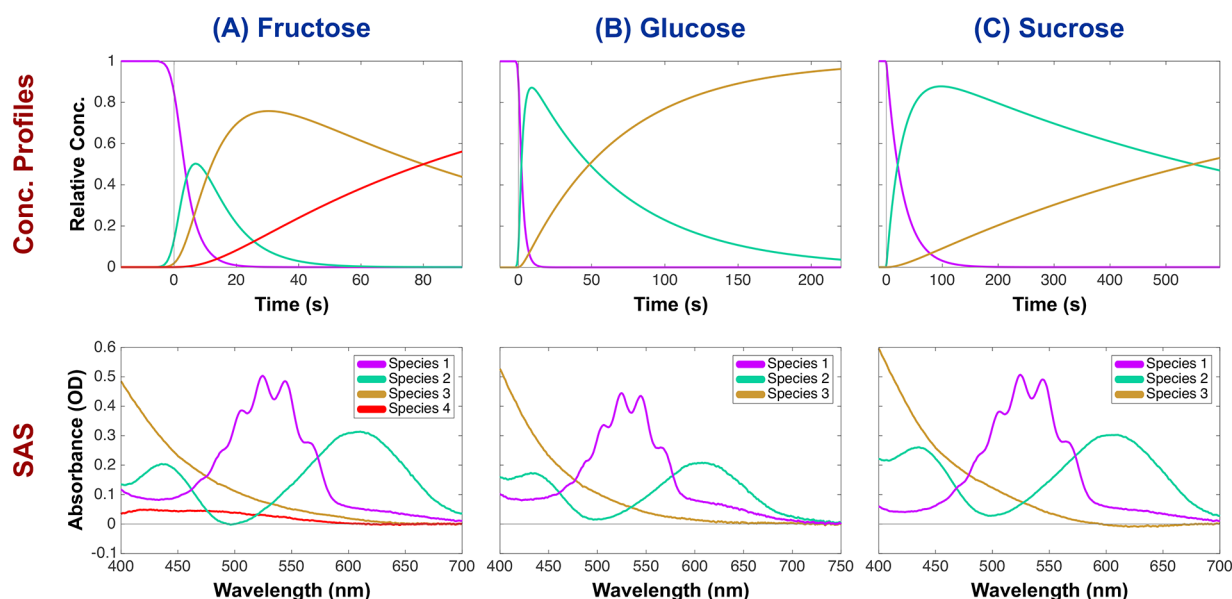
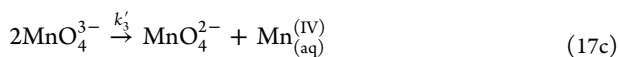
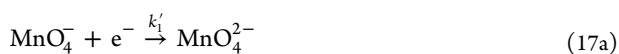


Figure 5. Concentration profiles (top row) and species-associated spectra (SAS, bottom row) obtained from the fits of the experimental data sets.

### Proposing a Reaction Mechanism

Permanganate is an important oxidant in many organic and inorganic redox transformations.<sup>44</sup> Among the organic substrates that can be oxidized by permanganate, we will focus our attention on carbohydrates (sugars). Several mechanisms have been proposed for both acidic,<sup>45</sup> and basic aqueous media,<sup>46,47</sup> which are complex and depend on the concentration of both reactants, and the pH of the medium.<sup>44,46,48–52</sup> An in-depth examination of such mechanisms is outside the scope of this work. The interested reader can find more details in ref 44.

The first mechanism we will discuss is shown in eqs 17:<sup>53</sup>



The first step (eq 17a) represents the initial reduction of permanganate [Mn(VII)] to manganate [ $\text{MnO}_4^{2-}$ , Mn(VI)], followed by the generation of the hypomanganate ( $\text{MnO}_4^{3-}$ ) anion [eq 17b, Mn(V)], which disproportionates to give  $\text{MnO}_4^{2-}$  [Mn(VI)] and  $\text{Mn}_{(\text{aq})}^{(\text{IV})}$  as products (eq 17c). The last step (eq 17d) represents the precipitation of a soluble Mn(IV) species to form a colloidal suspension of  $\text{MnO}_2$ , as reported in literature.<sup>54</sup> This mechanism would lead to the following ODEs:

$$\frac{d[\text{MnO}_4^-]_t}{dt} = -k'_1[\text{MnO}_4^-]_t \quad 18\text{a}$$

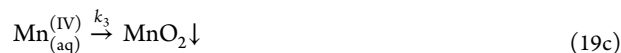
$$\frac{d[\text{MnO}_4^{2-}]_t}{dt} = +k'_1[\text{MnO}_4^-]_t - k'_2[\text{MnO}_4^{2-}]_t \quad 18\text{b}$$

$$\frac{d[\text{MnO}_4^{3-}]_t}{dt} = +k'_2[\text{MnO}_4^{2-}]_t - k'_3[\text{MnO}_4^{3-}]_t^2 \quad 18\text{c}$$

$$\frac{d[\text{Mn}_{(\text{aq})}^{(\text{IV})}]_t}{dt} = +k'_3[\text{MnO}_4^{3-}]_t^2 - k'_4[\text{Mn}_{(\text{aq})}^{(\text{IV})}]_t \quad 18\text{d}$$

$$\frac{d[\text{MnO}_2]_t}{dt} = +k'_4[\text{Mn}_{(\text{aq})}^{(\text{IV})}]_t \quad 18\text{e}$$

The  $\text{MnO}_4^{3-}$  species is highly unstable in basic media.<sup>46,55–57</sup> Hence, we can consider an alternative mechanism in which the  $\text{MnO}_4^{2-}$  species undergoes a two-electron reduction instead, leading directly to the soluble Mn(IV) species, which then precipitates as before (eq 19):



This mechanism leads to following ODE system:

$$\begin{cases} \frac{d[\text{MnO}_4^-]_t}{dt} = -k_1[\text{MnO}_4^-]_t & 20a \\ \frac{d[\text{MnO}_4^{2-}]_t}{dt} = +k_1[\text{MnO}_4^-]_t - k_2[\text{MnO}_4^{2-}]_t & 20b \\ \frac{d[\text{Mn}_{(aq)}^{(IV)}]_t}{dt} = +k_2[\text{MnO}_4^{2-}]_t - k_3[\text{Mn}_{(aq)}^{(IV)}]_t & 20c \\ \frac{d[\text{MnO}_2]_t}{dt} = +k_3[\text{Mn}_{(aq)}^{(IV)}]_t & 20d \end{cases}$$

The main difference between eq 18 and eq 20 is the absence of second-order concentration terms (e.g.,  $[\text{MnO}_4^{3-}]^2$  in eq 18c,d). Considering the pedagogical aim of our present paper, and the aforementioned instability of the  $\text{MnO}_4^{3-}$  species, we shall focus our attention on the second mechanism (eqs 19–20). Further details about this mechanism are discussed in the SI, section 13.

Defining the concentration vector as  $\mathbf{C}(t) = ([\text{MnO}_4^-]_t, [\text{MnO}_4^{2-}]_t, [\text{Mn}_{(aq)}^{(IV)}]_t, [\text{MnO}_2]_t)^T$ , the rate matrix becomes

$$\mathbf{K}_{M2} = \begin{pmatrix} -k_1 & 0 & 0 & 0 \\ +k_1 & -k_2 & 0 & 0 \\ 0 & +k_2 & -k_3 & 0 \\ 0 & 0 & +k_3 & 0 \end{pmatrix} \quad (21)$$

In the following section, we discuss the results of analyzing our data with this kinetic model.

### Species Associated Spectra and Kinetic Profiles

The ultimate goal of the analysis of time-resolved spectra is the determination of the rate constants and species-associated spectra (SAS) that describe the system in a physically meaningful way. In agreement with our discussion in the context of SVD (Figure 4), we have fitted the glucose data set with three components, since we believe that our detection window did not allow us to observe the last step of the mechanism (eq 19c). The sucrose data set was also fit with three components, as this gave the best results. The fructose data set was fit to a model with four components. This shows that the number of significant  $\sigma_k$ 's is not an absolute criterion as to the number of observable components.

In Figure 5 and Table 1, we show the results of fitting all three data sets (fructose, glucose, and sucrose) with the model described in eq 19 and eq 21. More detailed plots can be found in Figures S6–S8.

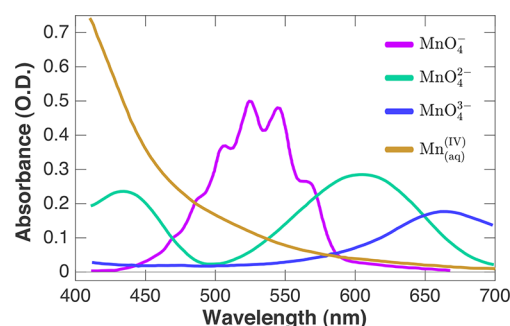
The SAS obtained for all data sets can be compared with the reported spectra of the different manganese-oxy species with oxidation states of manganese ranging from VII to IV (Figure 6).

A very important modification to the model was introduced to make the concentration of the initial species (Species 1, corresponding to  $\text{MnO}_4^-$ ) nonzero at negative reaction times. We set it to 1 as this would then lead to relative concentrations for all species. This is done to take into account that  $\text{MnO}_4^-$  is already in the reaction mixture, and its concentration is expected to decrease only after the addition of the sugar—hence starting the reaction. Furthermore, to correctly fit the fructose data set, a non-negativity penalty of the SAS was introduced (further details are given in the SI).

**Table 1. Kinetic Parameters of the Permanganate Oxidation of Sugars in Basic Aqueous Medium at Room Temperature**

parameter	(units)	fructose	glucose	sucrose
$t_0$	(s)	5.72	2.21	3.57
$\Delta^a$	(s)	4.96	1.02	2.17
$k_1$	(s <sup>-1</sup> ) <sup>b</sup>	$2.33 \times 10^{-1}$	$3.11 \times 10^{-1}$	$3.46 \times 10^{-2}$
$k_2$	(s <sup>-1</sup> ) <sup>b</sup>	$9.86 \times 10^{-2}$	$1.54 \times 10^{-2}$	$1.33 \times 10^{-3}$
$k_3$	(s <sup>-1</sup> ) <sup>b</sup>	$1.29 \times 10^{-2}$		

<sup>a</sup>Full-width at half-maximum of the Gaussian IRF used to convolve the kinetic response. <sup>b</sup>The kinetics of the system are being approximated by a pseudo-first-order mechanism, and as such, the rates shown herein are observed rates and will depend on concentration. See discussion of the kinetic model in the SI, section 13.



**Figure 6.** UV-vis spectra of the manganese species in oxidation states VII–IV. Spectra from a 0.2 mM solution in a 1 cm cuvette at 20 °C. Digitalized and adapted with permission from ref 56. Copyright 1985 American Chemical Society.

When treating time-resolved difference spectra, this needs to be considered more carefully, since species-associated difference spectra (SADS) can also have negative contributions (see the SI for an extended discussion).<sup>7</sup>

The fructose data set required the inclusion of the non-negative SAS penalty function and very careful selection of the initial parameters to converge to a physically meaningful solution, yet the quality of the fit (especially at early times) is not optimal. We believe that improper mixing and fast dynamics contribute to a non-Gaussian instrument response function (IRF), evidenced by the larger residuals appearing at early times (Figure S6). The concept of instrument response function is introduced and discussed in detail in the SI, section 9. This case serves to exemplify that a reasonable fit does not necessarily imply that a given model/mechanism accurately describes the physical phenomenon under study, and careful examination of the residuals (which should be structureless) can reveal any inconsistencies.

The SAS of the fourth component (Figure 5A; which corresponds to precipitated  $\text{MnO}_2$  nanoparticles) shows a very broad, weak, and featureless band. We believe that, since the formation of  $\text{MnO}_2$  nanoparticles is an uncontrolled process under our experimental conditions, the size of these nanoparticles (and hence their absorption spectra) will change over time.<sup>58–60</sup> This last observation would then help explain why the model does not fit the data to the same degree as with the other sugars.

The sucrose data set, on the other hand, was truncated at  $t < 600$  s for the fit, since precipitation of  $\text{MnO}_2$  and degradation of  $\text{MnO}_4^-$  by other side reactions not considered here can play a significant role and alter the kinetics at longer times.

As shown in Table 1, the extracted rate constants obey, in general, the relationship  $k_1 > k_2 > k_3$ , indicating that the successive electron transfer steps are slower in nature, as is expected when the manganate ions lose their oxidizing power (driving force). Furthermore,  $k_2$  decreases in the order fructose > glucose > sucrose, becoming roughly an order of magnitude slower every time.

These results are all in agreement with the qualitative observations about the overall speed of the reaction. The initial electron transfer rates are similar for glucose and fructose, but significantly slower for sucrose. This observation can be explained by considering that sucrose is a dimer of glucose and fructose, linked through the anomeric carbon. Hence, sucrose is the only nonreducing sugar, since it has no open chain form. This makes the latter significantly more difficult to oxidize, and thus slows down the reaction. Further mechanistic details can be found elsewhere.<sup>44</sup>

The SAS obtained from the fits to all three data sets using the kinetic model from eq 18 almost quantitatively match the reported spectra of the Mn-oxo species (Figure 6), confirming their identities in the kinetic model and validating the proposed reaction mechanism.

As shown in Figure 3 and Figures 5 and 6, and in agreement with our previous discussion about the mechanism, the  $\text{MnO}_4^{3-}$  species was not detected in our experiments. This is evidenced both by the lack of additional kinetic features at ca. 660 nm, and by the absence of any significant absorption bands beyond 700 nm in all data sets.

The shapes of the SAS and the reported spectra (Figure 6) can be discussed during elementary inorganic and general chemistry courses in the context of the analysis of electronic (UV–vis) absorption spectra. In this manner, students and lecturers can correlate the observed spectra and the position of the bands with the oxidation states and electronic configurations of the metal center in each species (i.e., in the context of ligand field theory, see chapter 8 of ref 61).

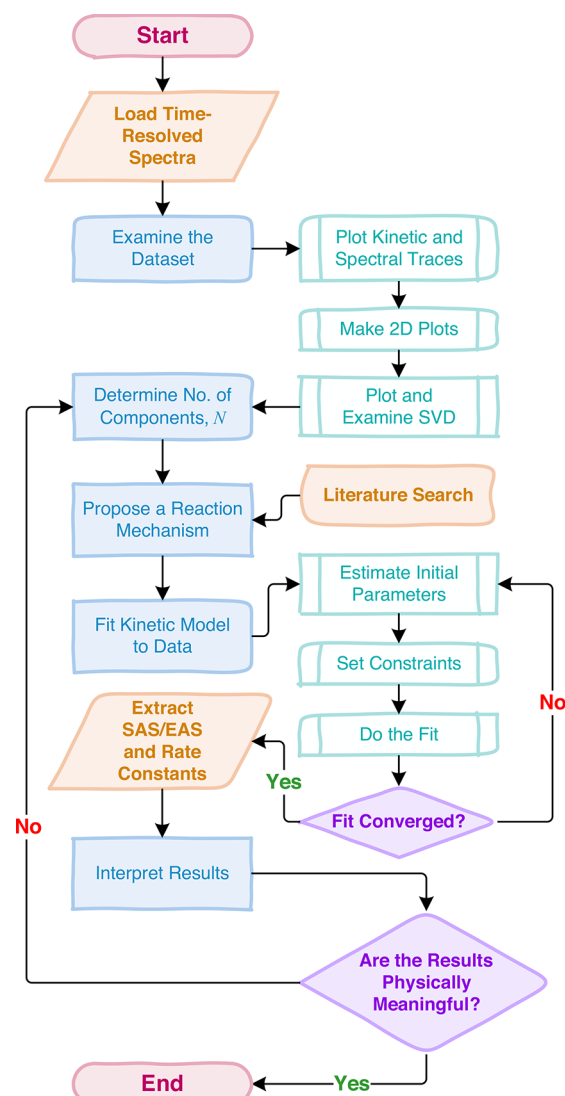
### Pedagogical Approach to This Paper: A Flowchart to Analyze Time-Resolved Spectroscopic Data

To summarize the data analysis strategies presented in this paper, we introduce the flowchart shown in Scheme 1. This scheme illustrates step-by-step the processes and subprocesses involved in each stage of data analysis of a time-resolved spectral data set following a model-based strategy. We believe that the use of a flowchart can ease the explanation of every step in a lecture, and also serve as reference for students and lecturers, to be used in both teaching and research laboratories.

The flowchart can be explained as follows: The data is first loaded and examined into a suitable data processing software (e.g., MATLAB). The kinetic and spectral traces, as well as the contour (2D) and SVD plots are done in order to determine the  $N$  components and the approximate time scales of the spectral changes. After a literature research, a kinetic model/mechanism can be proposed and fitted to the data until convergence is achieved (typically meaning that the norm of the residuals is below a certain threshold value).

A careful analysis of the extracted SAS/EAS<sup>62</sup> and rate constants will then lead to the question of whether these results are physically meaningful—for instance, by checking the magnitude of the rate constants, the shape of the SAS/EAS, and their relationship with the expected intermediates according to the proposed kinetic model and/or literature information). If the results are not satisfactory, new starting

**Scheme 1. Flow Chart Summarizing a Model-Based Data Analysis Strategy for Time-Resolved Spectra**



conditions or a new mechanism/kinetic model must be tested, repeating the process over again.

The information presented in this manuscript can be used by lecturers to explain the theory behind generalized matrix kinetics for first-order reaction systems (complementary to the approach discussed by Berberan-Santos and Martinho),<sup>33</sup> the correlation between kinetics and spectral changes, and how to propose and test reaction mechanisms (e.g., estimation of the number of components from SVD, simulation of time-resolved data, among others).

Our approach is versatile, and the topics discussed in this paper can be presented in several ways. For example, the lecturer can use this article in a traditional lecture as a part of a kinetics course, and then ask the students to analyze the provided data sets using our flowchart, paving the way for discussion about the possible mechanisms. As an alternative, the chemical chameleon reaction can also be implemented as a hands-on experiment, allowing the students to analyze and process their own data, collected by using inexpensive chemicals and equipment that is readily available in most chemistry laboratories. With a larger class, the effects of other variables such as pH, temperature, and concentration can be



used to test and discuss the results and their impact in the kinetics and involved chemical mechanisms. The lecturer can then ask the students to provide enough evidence to support their own proposed mechanisms and discuss the outcome, the goodness of the fit, and the limitations of the used kinetic models.

The vast amount of information available in literature regarding time-resolved analysis can be overwhelming for an upper-division undergraduate or for graduate students beginning their research. Our manuscript can be used for a first, solid approach to the treatment of time-resolved data and kinetic analysis. These students can perform the chemical chameleon reaction on their own and then analyze the data themselves by following the step-by-step flowchart; while getting deeper knowledge about the theory behind such analysis in a facile way. The present work can also be used by senior researchers as a first activity assigned to new students, allowing them to gain experience in the collection of time-resolved data and its analysis.

## CONCLUSIONS

Herein we present a *sweet* introduction to the treatment of time-resolved data, exemplified by the permanganate oxidation of sugars in aqueous basic media. The mathematical aspects of a model-based data analysis strategy under the assumptions of classical kinetics and bilinearity between concentrations and spectra are discussed in detail, presented in a pedagogical manner, and summarized in a flowchart. Example code files provide a fully functional implementation of the described methods, while giving the readers the option to simulate and model their own data in a simple manner. We believe that a basic knowledge of programming and data processing strategies is essential for chemists, as they can significantly facilitate the analysis of data collected on a day-to-day basis—especially true in the physical and analytical chemistry subdisciplines.

Our mechanistic discussion of this reaction bridges important concepts among the organic, inorganic, physical, and analytical branches of chemistry—illustrating how a complex reaction can be analyzed from several perspectives to gain a deeper insight. At the same time, our work provides an easy to follow treatment of the complex aspects at the interface between spectroscopy and kinetics, essential for mechanistic understanding and modeling of complex chemical systems in all time scales.

## ASSOCIATED CONTENT

### Supporting Information

The Supporting Information is available at <https://pubs.acs.org/doi/10.1021/acs.jchemed.2c00104>.

Additional discussions pertaining to the Theoretical Background: a summary of the generalized matrix kinetics method, the Moore–Penrose pseudoinverse and eigenvalue/eigenvector methods, the instrument response function and convolution. A detailed explanation of all MATLAB code files, an in-depth discussion of our implementation, a discussion of the kinetic model, IRF convolution, and the analogy with transient absorption spectroscopy, as well as additional figures (detailed fit results and residuals, convolution examples and other kinetics examples) (PDF)

MATLAB source code files containing the routines to simulate and fit the spectrokinetic data sets using a model-based strategy (ZIP)

Fructose, glucose, and sucrose time-resolved spectral data sets (ZIP)

Video of an experimental run of the chameleon reaction with glucose, illustrating the real-time color changes easily observable by naked eye and corresponding absorption spectra (MP4)

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### Notes

The authors declare no competing financial interest.

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