

ST3131 Assignment

```
rm(list = ls())
library(car)
library(MASS)
library(LambertW)

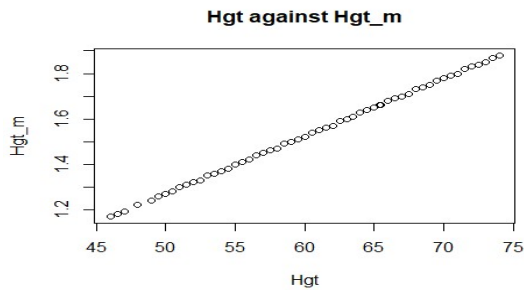
setwd("C:/Users/user/Desktop/ST3131")
data <- read.csv("FEV.csv")
data[[5]] <- as.factor(data[[5]])
data[[6]] <- as.factor(data[[6]])
attach(data)
model1 <- lm(FEV ~ Age + Sex + Smoke + Hgt + Hgt_m, data = data)
summary(model1)

##
## Call:
## lm(formula = FEV ~ Age + Sex + Smoke + Hgt + Hgt_m, data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.41306 -0.25696  0.00108  0.26249  1.89828
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -4.436160   0.222961 -19.897  < 2e-16 ***
## Age          0.065435   0.009477   6.904 1.21e-11 ***
## Sex1         0.160431   0.033255   4.824 1.75e-06 ***
## Smoke1       -0.082226   0.059267  -1.387  0.1658
## Hgt          0.312051   0.142227   2.194  0.0286 *
## Hgt_m        -8.197478   5.605713  -1.462  0.1441
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.4117 on 648 degrees of freedom
## Multiple R-squared:  0.7762, Adjusted R-squared:  0.7744
## F-statistic: 449.4 on 5 and 648 DF,  p-value: < 2.2e-16

anova(model1)

## Analysis of Variance Table
##
## Response: FEV
##           Df Sum Sq Mean Sq  F value    Pr(>F)
## Age         1 280.893  280.893 1657.0034 < 2.2e-16 ***
## Sex         1  17.040   17.040  100.5212 < 2.2e-16 ***
## Smoke       1   1.144    1.144   6.7503 0.009586 **
## Hgt         1  81.478   81.478  480.6441 < 2.2e-16 ***
## Hgt_m       1   0.363    0.363   2.1384 0.144132
## Residuals 648 109.848    0.170
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
plot(Hgt,Hgt_m, main = "Hgt against Hgt_m")
```



From the above plot, we can see that the variables Hgt is nearly linearly dependent on Hgt_M. Since this gives rise to the possibility of multicollinearity, and from anova table of model1, I know that Hgt_m has a larger p-value than Hgt, I will remove Hgt_m since it is not as significant as Hgt.

Additionally, since logically we can see that certain regressors will affect another, we will introduce certain interaction terms in the model. For now, the interaction terms that will be introduced will be (Smoke * Age), (Sex * Smoke), (Sex * Hgt), (Age * Hgt). (Smoke * Hgt) will be excluded since it makes the least sense to me. Just because someone is tall does not mean that the person is more likely to smoke.

Lastly, I will also add in quadratic terms as I want to maximise the fit for now.

```
model2 <- lm(FEV ~ Age + Sex + Smoke + Hgt + Smoke * Age + Sex * Smoke +
Age * Hgt + Sex * Hgt + I(Age ** 2) + I(Hgt ** 2), data = data)
summary(model2)
```

```
##
## Call:
## lm(formula = FEV ~ Age + Sex + Smoke + Hgt + Smoke * Age + Sex *
##      Smoke + Age * Hgt + Sex * Hgt + I(Age^2) + I(Hgt^2), data = data)
##
## Residuals:
```

	Min	1Q	Median	3Q	Max
	-1.49590	-0.22845	0.01279	0.23456	1.67474

```
##
## Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	4.558e-01	2.314e+00	0.197	0.84390
Age	-3.560e-01	1.416e-01	-2.514	0.01219 *
Sex1	-8.601e-01	3.916e-01	-2.197	0.02841 *
Smoke1	4.995e-01	3.328e-01	1.501	0.13387
Hgt	1.542e-02	9.359e-02	0.165	0.86920
I(Age^2)	-2.903e-03	2.997e-03	-0.969	0.33313
I(Hgt^2)	2.959e-05	9.539e-04	0.031	0.97526
Age:Smoke1	-4.914e-02	2.525e-02	-1.946	0.05210 .
Sex1:Smoke1	6.187e-02	1.109e-01	0.558	0.57706
Age:Hgt	7.937e-03	2.976e-03	2.667	0.00784 **
Sex1:Hgt	1.585e-02	6.530e-03	2.427	0.01551 *

```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 0.3903 on 643 degrees of freedom
## Multiple R-squared:  0.8004, Adjusted R-squared:  0.7973
## F-statistic: 257.9 on 10 and 643 DF,  p-value: < 2.2e-16

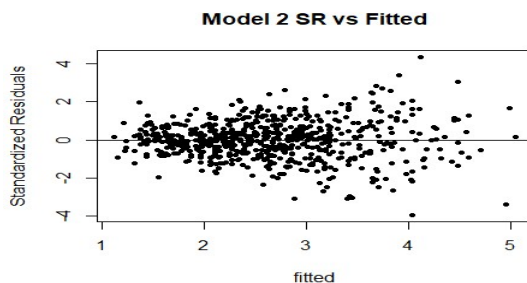
anova(model12)

## Analysis of Variance Table
##
## Response: FEV
##
```

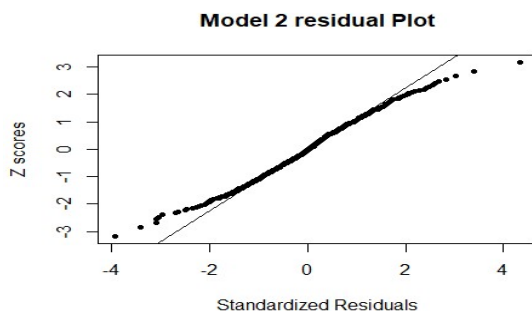
	Df	Sum Sq	Mean Sq	F value	Pr(>F)	
Age	1	280.893	280.893	1843.9343	< 2.2e-16	***
Sex	1	17.040	17.040	111.8613	< 2.2e-16	***
Smoke	1	1.144	1.144	7.5119	0.006300	**
Hgt	1	81.478	81.478	534.8669	< 2.2e-16	***
I(Age^2)	1	4.129	4.129	27.1043	2.597e-07	***
I(Hgt^2)	1	5.144	5.144	33.7680	9.774e-09	***
Age:Smoke	1	0.520	0.520	3.4148	0.065075	.
Sex:Smoke	1	0.408	0.408	2.6798	0.102117	
Age:Hgt	1	1.162	1.162	7.6268	0.005915	**
Sex:Hgt	1	0.897	0.897	5.8886	0.015513	*
Residuals	643	97.950	0.152			

```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
plot(model12$fitted.values,rstandard(model12), xlab="fitted", ylab= "Standardized Residuals",
main = "Model 2 SR vs Fitted", pch = 20)
abline(h = 0)
```



```
qqnorm(rstandard(model12),datax = TRUE, ylab = "Standardized Residuals", xlab = "Z scores",
main = "Model 2 residual Plot", pch = 20)
qqline(rstandard(model12),datax = TRUE)
```



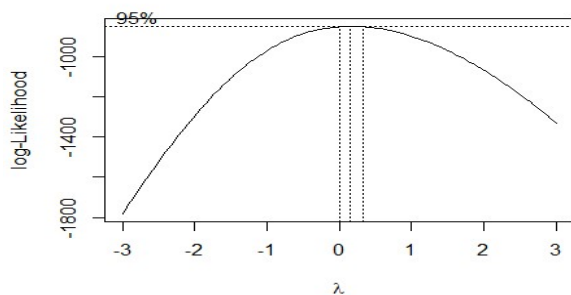
From the summary, even though Sex * Smoke still has quite a high p-value, I will just leave it in the model for now since the R² is somewhat strong, at 0.8. Next up, I will proceed to test the adequacy of the model, using the residual plot and the residual vs fitted plot.

From the fitted values vs residual plot, we can see that the constant variance assumption is violated and the points are ranging from close to -4 to 4, which is not very ideal.

From the residual plots, we can see that the normality assumption is also violated since we can see a trend whereby the right and left tail deviates from the straight line. Hence, I will attempt to do some transformation to make the variance more constant. For the transformation, I will do a boxcox transformation.

```
boxcox(model12, lambda = seq(-3,3, by = 0.5), optimize = TRUE, plotit = TRUE)
```

```
## Warning: In lm.fit(x, y, offset = offset, singular.ok = singular.ok, ...):  
## extra argument 'optimize' will be disregarded
```



From the boxcox diagram, I will take 0 to transform my response since it is easier to interpret as compared to 0.2. As such, my response will be transformed to log(FEV).

```
model13 <- lm(log(FEV) ~ Age + Sex + Smoke + Hgt + Smoke * Age + Sex * Smoke + Age * Hgt + Sex * Hgt + I(Age ** 2) + I(Hgt ** 2), data = data)  
summary(model13)
```

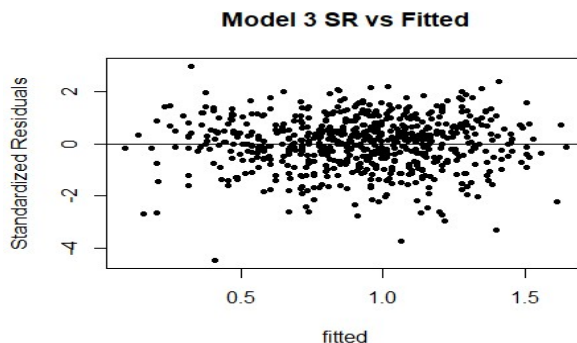
```
##  
## Call:  
## lm(formula = log(FEV) ~ Age + Sex + Smoke + Hgt + Smoke * Age +  
##      Sex * Smoke + Age * Hgt + Sex * Hgt + I(Age^2) + I(Hgt^2),  
##      data = data)  
##  
## Residuals:  
##      Min       1Q   Median       3Q      Max   
## -0.64357 -0.08702  0.01360  0.09503  0.42723   
##  
## Coefficients:  
##              Estimate Std. Error t value Pr(>|t|)      
## (Intercept) -3.5833218   0.8615887  -4.159 3.63e-05 ***  
## Age          -0.0643388   0.0527379  -1.220  0.2229      
## Sex1         -0.1003664   0.1458068  -0.688  0.4915      
## Smoke1        0.1251306   0.1239266   1.010  0.3130    
```

```
## Hgt          0.1126094  0.0348499   3.231   0.0013 **
## I(Age^2)     -0.0010640  0.0011161  -0.953   0.3408
## I(Hgt^2)     -0.0007350  0.0003552  -2.069   0.0389 *
## Age:Smoke1   -0.0129784  0.0094032  -1.380   0.1680
## Sex1:Smoke1  0.0095665  0.0412876   0.232   0.8168
## Age:Hgt      0.0018119  0.0011081   1.635   0.1025
## Sex1:Hgt     0.0022023  0.0024315   0.906   0.3654
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1453 on 643 degrees of freedom
## Multiple R-squared:  0.8127, Adjusted R-squared:  0.8097
## F-statistic: 278.9 on 10 and 643 DF, p-value: < 2.2e-16
```

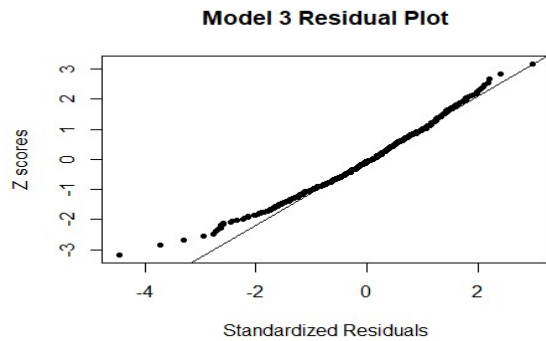
```
anova(model3)
```

```
## Analysis of Variance Table
##
## Response: log(FEV)
##          Df Sum Sq Mean Sq  F value    Pr(>F)
## Age         1  43.192   43.192  2045.0700 < 2.2e-16 ***
## Sex         1   1.568    1.568   74.2639 < 2.2e-16 ***
## Smoke       1   0.262    0.262   12.3828 0.0004639 ***
## Hgt         1  13.740   13.740  650.5752 < 2.2e-16 ***
## I(Age^2)    1   0.007    0.007    0.3501 0.5542517
## I(Hgt^2)    1   0.010    0.010    0.4812 0.4881399
## Age:Smoke   1   0.041    0.041    1.9592 0.1620779
## Sex:Smoke   1   0.011    0.011    0.5250 0.4689785
## Age:Hgt     1   0.059    0.059    2.7918 0.0952344 .
## Sex:Hgt     1   0.017    0.017    0.8204 0.3654153
## Residuals 643  13.580    0.021
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
plot(model3$fitted.values,rstandard(model3), xlab="fitted", ylab= "Standardized Residuals", main = "Model 3 SR vs Fitted", pch = 20)
abline(h = 0)
```



```
qqnorm(rstandard(model3),datax = TRUE, ylab = "Standardized Residuals", xlab = "Z scores", main = "Model 3 Residual Plot", pch = 20)
qqline(rstandard(model3),datax = TRUE)
```



```
vif(model3)
```

##	Age	Sex	Smoke	Hgt	I(Age^2)	I(Hgt^2)
##	750.355261	164.456604	42.568344	1221.537411	155.003704	1865.808259
##	Age:Smoke	Sex:Smoke	Age:Hgt	Sex:Hgt		
##	46.285015	2.015118	1961.201395	179.709062		

From Model3 SR vs fitted plot, it appears that the variance is acceptable as there is no obvious non-constant variance and now there is only one point that is less than -4. However, the VIF values are not acceptable since they are in the hundreds and even thousands. As such, I will conduct unit length scaling to reduce VIF.

#scaled regressors - have smaller VIF values compared to unscaled regressors

```
age_new <- (Age - mean(Age)) / sqrt(var(Age)*142)
hgt_new <- (Hgt - mean(Hgt)) / sqrt(var(Hgt)*142)

model4 <- lm(log(FEV) ~ age_new + Sex + Smoke + hgt_new + Smoke * age_new
+ Sex * Smoke + age_new * hgt_new + Sex * hgt_new + I(age_new ** 2) + I(hgt_new ** 2), data = data)
summary(model4)
```

```
##
## Call:
## lm(formula = log(FEV) ~ age_new + Sex + Smoke + hgt_new + Smoke *
##   age_new + Sex * Smoke + age_new * hgt_new + Sex * hgt_new +
##   I(age_new^2) + I(hgt_new^2), data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.64357 -0.08702  0.01360  0.09503  0.42723
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   0.910684   0.010160  89.635 < 2e-16 ***
## age_new       0.890967   0.146186   6.095 1.89e-09 ***
## Sex1          0.034291   0.013000   2.638  0.00855 **
## Smoke1       -0.003760   0.038808  -0.097  0.92284
## hgt_new       2.768092   0.180379  15.346 < 2e-16 ***
## I(age_new^2)  -1.318409   1.382910  -0.953  0.34077
```

```
## I(hgt_new^2)      -3.394948    1.640610    -2.069    0.03891 *
## age_new:Smoke1    -0.456841    0.330995    -1.380    0.16800
## Sex1:Smoke1       0.009566    0.041288     0.232    0.81684
## age_new:hgt_new   4.334717    2.650975     1.635    0.10251
## Sex1:hgt_new      0.149681    0.165259     0.906    0.36542
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1453 on 643 degrees of freedom
## Multiple R-squared:  0.8127, Adjusted R-squared:  0.8097
## F-statistic: 278.9 on 10 and 643 DF, p-value: < 2.2e-16
```

```
anova(model4)
```

```
## Analysis of Variance Table
```

```
##
```

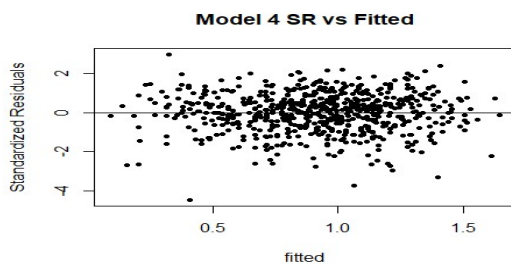
```
## Response: log(FEV)
```

```
##              Df Sum Sq Mean Sq  F value    Pr(>F)
## age_new        1 43.192   43.192 2045.0700 < 2.2e-16 ***
## Sex            1  1.568    1.568   74.2639 < 2.2e-16 ***
## Smoke          1  0.262    0.262   12.3828 0.0004639 ***
## hgt_new        1 13.740   13.740  650.5752 < 2.2e-16 ***
## I(age_new^2)    1  0.007    0.007    0.3501 0.5542517
## I(hgt_new^2)    1  0.010    0.010    0.4812 0.4881399
## age_new:Smoke   1  0.041    0.041    1.9592 0.1620779
## Sex:Smoke       1  0.011    0.011    0.5250 0.4689785
## age_new:hgt_new 1  0.059    0.059    2.7918 0.0952344 .
## Sex:hgt_new     1  0.017    0.017    0.8204 0.3654153
## Residuals      643 13.580    0.021
```

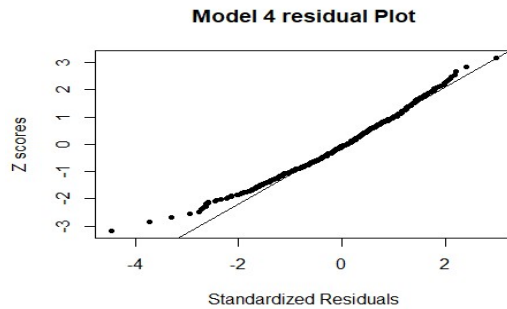
```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
plot(model4$fitted.values,rstandard(model4), xlab="fitted", ylab= "Standardized Residuals", main = "Model 4 SR vs Fitted", pch = 20)
abline(h = 0)
```



```
qqnorm(rstandard(model4),datax = TRUE, ylab = "Standardized Residuals", xlab = "Z scores", main = "Model 4 residual Plot", pch = 20)
qqline(rstandard(model4),datax = TRUE)
```



```
vif(model4)
```

	age_new	Sex	Smoke	hgt_new	I(age_new^2)
age_new	4.653080	1.307371	4.174384	7.084445	6.160395
Sex					
Smoke					
hgt_new					
I(age_new^2)					
age_new:Smoke	6.207006	4.628144	2.015118	12.849294	3.794035
Sex:Smoke					
age_new:hgt_new					
Sex:hgt_new					

After the scaling, it is evident that the VIF values have decreased tremendously. However, there is still one VIF value belonging to age_new * hgt_new that is too large (above 10). Hence, I will remove the regressor from the model.

```
model5 <- lm(log(FEV) ~ age_new + Sex + Smoke + hgt_new + Smoke * age_new
+ Sex * Smoke + Sex * hgt_new + I(age_new ** 2) + I(hgt_new ** 2), data =
data)
summary(model5)
```

```
##
## Call:
## lm(formula = log(FEV) ~ age_new + Sex + Smoke + hgt_new + Smoke *
##   age_new + Sex * Smoke + Sex * hgt_new + I(age_new^2) + I(hgt_new^
##   2),
##   data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.63865 -0.08616  0.01331  0.09575  0.43123
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   0.906677   0.009873  91.836 < 2e-16 ***
## age_new       0.868455   0.145725   5.960 4.17e-09 ***
## Sex1          0.034563   0.013016   2.655 0.00812 **
## Smoke1       -0.002629   0.038852  -0.068 0.94607
## hgt_new       2.747201   0.180160  15.249 < 2e-16 ***
## I(age_new^2)   0.436501   0.873245   0.500 0.61734
## I(hgt_new^2)  -1.164072   0.912335  -1.276 0.20244
## age_new:Smoke1 -0.509199   0.329870  -1.544 0.12317
## Sex1:Smoke1    0.017854   0.041028   0.435 0.66359
## Sex1:hgt_new   0.159978   0.165354   0.967 0.33366
```



```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1455 on 644 degrees of freedom
## Multiple R-squared:  0.8119, Adjusted R-squared:  0.8092
## F-statistic: 308.8 on 9 and 644 DF,  p-value: < 2.2e-16
```

```
anova(model5)
```

```
## Analysis of Variance Table
```

```
##
```

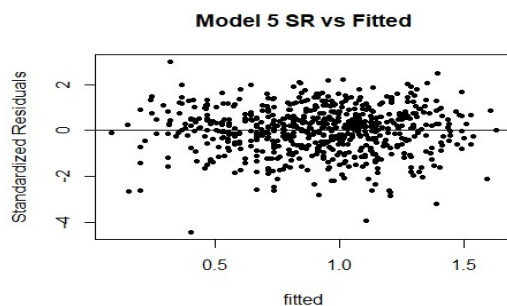
```
## Response: log(FEV)
```

```
##          Df Sum Sq Mean Sq    F value    Pr(>F)
## age_new    1  43.192   43.192  2039.7689 < 2.2e-16 ***
## Sex        1   1.568    1.568   74.0714 < 2.2e-16 ***
## Smoke      1   0.262    0.262   12.3507 0.0004717 ***
## hgt_new    1  13.740   13.740  648.8888 < 2.2e-16 ***
## I(age_new^2) 1   0.007    0.007    0.3492 0.5547651
## I(hgt_new^2) 1   0.010    0.010    0.4799 0.4887036
## age_new:Smoke 1   0.041    0.041    1.9542 0.1626214
## Sex:Smoke    1   0.011    0.011    0.5236 0.4695545
## Sex:hgt_new  1   0.020    0.020    0.9360 0.3336622
## Residuals   644  13.637    0.021
```

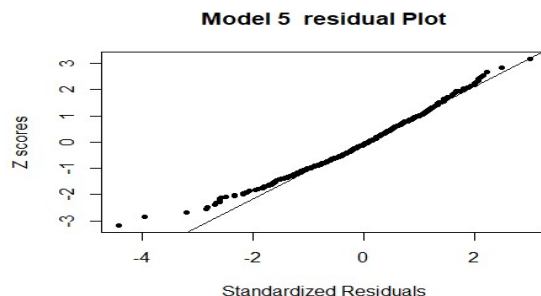
```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
plot(model5$fitted.values,rstandard(model5), xlab="fitted", ylab= "Standardized Residuals", main = "Model 5 SR vs Fitted", pch = 20)
abline(h = 0)
```



```
qqnorm(rstandard(model5),datax = TRUE, ylab = "Standardized Residuals", xlab = "Z scores", main = "Model 5 residual Plot", pch = 20)
qqline(rstandard(model5),datax = TRUE)
```



```
vif(model5)
```

	age_new	Sex	Smoke	hgt_new	I(age_new^2)
##	4.611807	1.307158	4.173058	7.048902	2.450000
##	I(hgt_new^2)	age_new:Smoke	Sex:Smoke	Sex:hgt_new	
##	1.914491	4.584832	1.984749	3.788526	

After removing $\text{age_new} * \text{hgt_new}$ from the model, we can see that the qqplot is still approximately a straight line and the variance of the SR vs fitted model is still acceptable. And all the VIF values are now below 10, which is a good sign. Since the model is now adequate, i.e. the SR vs fitted diagram has constant variance, residual plots more or less follows a straight line, and all VIF values are acceptable, I will conduct variable selection now using backward selection.

```
bw <- step(model5, direction = c("backward"))
```

```
## Start:  AIC=-2511.21
## log(FEV) ~ age_new + Sex + Smoke + hgt_new + Smoke * age_new +
##      Sex * Smoke + Sex * hgt_new + I(age_new^2) + I(hgt_new^2)
##
##           Df Sum of Sq   RSS   AIC
## - Sex:Smoke    1  0.004010 13.641 -2513.0
## - I(age_new^2)  1  0.005291 13.642 -2513.0
## - Sex:hgt_new   1  0.019820 13.656 -2512.3
## - I(hgt_new^2)  1  0.034472 13.671 -2511.6
## <none>                13.637 -2511.2
## - age_new:Smoke    1  0.050456 13.687 -2510.8
##
## Step:  AIC=-2513.02
## log(FEV) ~ age_new + Sex + Smoke + hgt_new + I(age_new^2) + I(hgt_new^
## 2) +
##      age_new:Smoke + Sex:hgt_new
##
##           Df Sum of Sq   RSS   AIC
## - I(age_new^2)  1  0.005138 13.646 -2514.8
## - Sex:hgt_new   1  0.026899 13.668 -2513.7
## - I(hgt_new^2)  1  0.034446 13.675 -2513.4
## <none>                13.641 -2513.0
## - age_new:Smoke    1  0.047715 13.688 -2512.7
##
## Step:  AIC=-2514.77
## log(FEV) ~ age_new + Sex + Smoke + hgt_new + I(hgt_new^2) + age_new:Sm
## ke +
```

```
##      Sex:hgt_new
##
##              Df Sum of Sq    RSS    AIC
## - Sex:hgt_new   1  0.026412 13.672 -2515.5
## - I(hgt_new^2)   1  0.030764 13.677 -2515.3
## <none>                                13.646 -2514.8
## - age_new:Smoke  1  0.042861 13.689 -2514.7
##
## Step:  AIC=-2515.51
## log(FEV) ~ age_new + Sex + Smoke + hgt_new + I(hgt_new^2) + age_new:Smoke
##
##              Df Sum of Sq    RSS    AIC
## - I(hgt_new^2)   1    0.0147 13.687 -2516.8
## - age_new:Smoke  1    0.0369 13.709 -2515.7
## <none>                                13.672 -2515.5
## - Sex            1    0.1587 13.831 -2510.0
## - hgt_new        1   11.9183 25.590 -2107.5
##
## Step:  AIC=-2516.8
## log(FEV) ~ age_new + Sex + Smoke + hgt_new + age_new:Smoke
##
##              Df Sum of Sq    RSS    AIC
## - age_new:Smoke  1    0.0396 13.726 -2516.9
## <none>                                13.687 -2516.8
## - Sex            1    0.1446 13.832 -2511.9
## - hgt_new        1   12.0771 25.764 -2105.1
##
## Step:  AIC=-2516.91
## log(FEV) ~ age_new + Sex + Smoke + hgt_new
##
##              Df Sum of Sq    RSS    AIC
## <none>                                13.726 -2516.9
## - Smoke      1    0.1025 13.829 -2514.1
## - Sex        1    0.1317 13.858 -2512.7
## - age_new    1    1.0323 14.759 -2471.5
## - hgt_new    1   13.7401 27.467 -2065.3

summary(bw)

##
## Call:
## lm(formula = log(FEV) ~ age_new + Sex + Smoke + hgt_new, data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.63443 -0.08644  0.01167  0.09492  0.40904
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  0.905221   0.008657 104.571 < 2e-16 ***
## age_new      0.823228   0.117836   6.986 7.01e-12 ***
## Sex1         0.029236   0.011716   2.496  0.0128 *
## Smoke1      -0.046015   0.020905  -2.201  0.0281 *
```

```
## hgt_new      2.907738   0.114082  25.488 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1454 on 649 degrees of freedom
## Multiple R-squared:  0.8106, Adjusted R-squared:  0.8095
## F-statistic: 694.6 on 4 and 649 DF,  p-value: < 2.2e-16
```

From the summary, the final model that I will pick is $\log(\text{FEV}) = 0.905221 + 0.823228 * \text{age_new} + 0.029236 * \text{Sex} - 0.046015 * \text{Smoke} + 2.907738 * \text{hgt_new}$. We can interpret the model as follows: If age_new increases by 1 unit, with all variables being constant, FEV increases by $(0.069084 * 100)$ percent. If hgt_new increases by 1 unit, with all variables being constant, FEV increases by $(0.0244012 * 100)$ percent. With this fitted model, the estimated mean FEV for Sex = 1 (ie male) is $(0.029236 * 100)$ percent more than for Sex = 0 (ie female) With this fitted model, the estimated mean FEV for Smoke = 1 (ie current smoker) is $(0.046015 * 100)$ percent more than for Smoke = 0 (ie current non-smoker)

```
model6 <- lm(formula = log(FEV) ~ age_new + Sex + Smoke + hgt_new, data =
data)
```

```
anova(model6)
```

```
## Analysis of Variance Table
```

```
##
```

```
## Response: log(FEV)
```

```
##           Df Sum Sq Mean Sq  F value    Pr(>F)
## age_new     1  43.192   43.192 2042.151 < 2.2e-16 ***
## Sex         1   1.568    1.568   74.158 < 2.2e-16 ***
## Smoke       1   0.262    0.262   12.365 0.0004679 ***
## hgt_new     1  13.740   13.740  649.647 < 2.2e-16 ***
## Residuals 649  13.726    0.021
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```