IE 7275 Data Mining in Engineering Homework 1

Deadline 9/21

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Problem1 (twitter account)

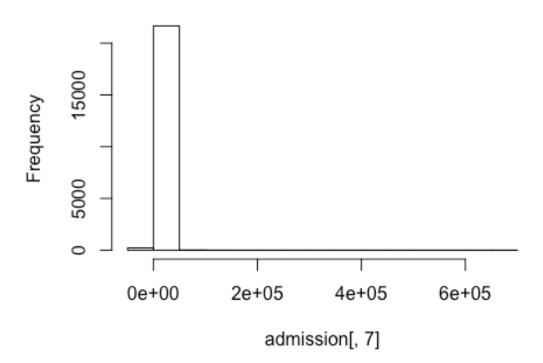
load the data file

- > hw1 <- read.csv("/Users/jingli/Desktop/M01 quasi twitter.csv")
- > View(hw1)

a. how are the data distributed for friends_count

Create the distribution of friends_count
hist(hw1\$friends_count)

Histogram of admission[, 7]

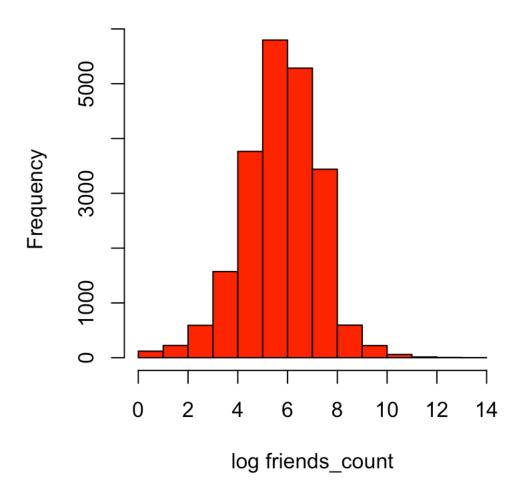


It is hard to tell the distribution from the histogram of original data. After plotting the histogram of log of data the distribution is close to Normal Distribution

install. packages("logging").

hist(log(hw1\$friends_count), xlab = "log friends_count", col = "red", main = "Distribution of log friends count")

Distribution of log friends_count



Compute the summery statistics (min, 1Q mean, mean, median, 3Q, max) on friend_count ##Compute the summery statistics on friends_count? summary(hw1\$friends_count)

Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
-84	123	324	1058	849	660549

b. How are the data quality in friend count variable? Interpret your answer. ##evaluate the data quality of friends count ##whether the data has NULL sum(is.na(hw1\$friends count)) ##whether the data has minus valaues sum(hw1\$friends_count < 0)</pre> > ##evaluate the data quality of friends_count > ##whether the data has NULL > sum(is.na(hw1\$friends_count)) [1] 0 > ##whether the data has minus valaues > sum(hw1\$friends_count < 0)</pre> Γ17 1 > sum(hw1\$friends_count) [1] 23185173 Answer: Based on the above outcomes, there is only one negative value. Comparing to the total number of the data, this value can be ignored. So the data quality of friends counts is good.

d. Produce a 3D scatter plot with highlighting

d. Produce a 3D scatter plot with highlighting

install.packages("scatterplot3d")

library(scatterplot3d)

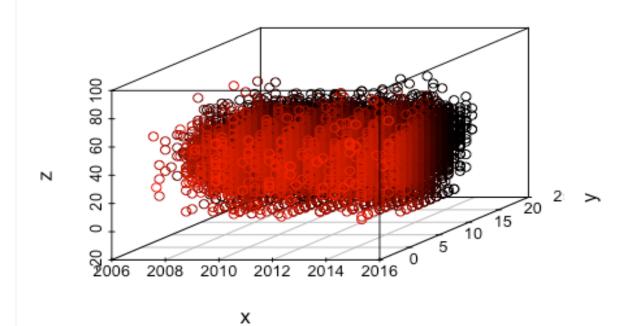
x <- hw1\\$created_at_year

y <- hw1\$education

z <- hw1\$age

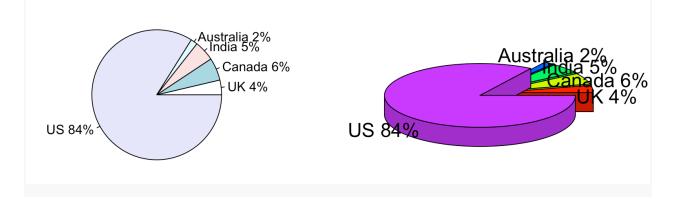
scatterplot3d(x, y, z, highlight.3d = TRUE, main = "3D scatter plot")





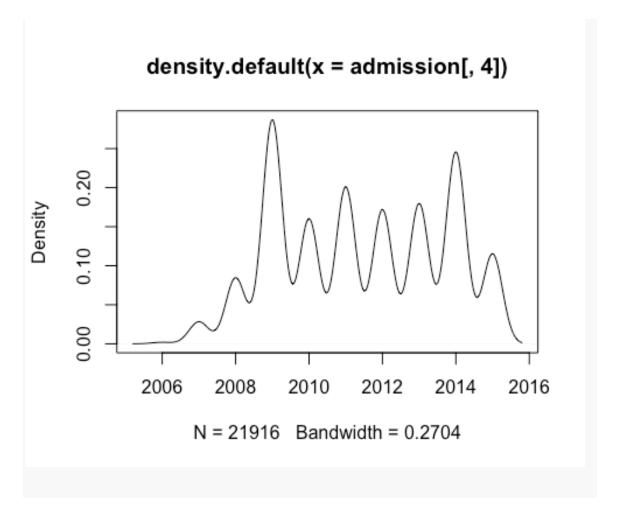
e. Pie chart with percentage

```
## e. pie chart with percentages
library(plotrix)
par(mfrow=c(1,2))
twitter account <- c(650,1000,900,300,14900)
twitter country <- c("UK", "Canada", "India", "Australia", "US")
percent <- round(twitter_account/sum(twitter_account)*100)</pre>
twitter country <- paste(twitter country, percent)# add percents to labels
twitter_country <- paste(twitter_country, "%", sep ="")# ad % to labels
pie(twitter account, labels = twitter country, main = "Pie Chrt for the Country")
##3D pie chart
install.packages("plotrix")
library(plotrix)
pie3D(twitter_account,labels = twitter_country, explode = 0.1,main = "Pie Chart of Countries")
      Pie Chrt for the Country
                                                           Pie Chart of Countries
```



f. Density plot

```
## f. kernel density plot
par(mfrow=c(1,1))
kernel_density <- density(hw1$created_at_year)
plot(kernel_density)
## in 2006, there is a few twitter user.Since 2008,the user of twitter start to increase. It reaches the maximum number,around 0.28, in 2009.The curve of density of created user is wavy from 2010 to 2015. The tendency is decreasing from 2015 to 2016
```



The number of twitter users grows rapidly during 2008 and 2009, and peaked at around 0.27 in 2019. Then it fluctuated between 2012 and 2014, After which it dropped dramatically to the lowest level in 2016.

Problem2 (Cereals Analysis)

a.

Answer: The quantitative variables are calories, protein, fat, sodium, fiber, carbo, sugars, potassium, vitamins, weight, cups and rating.

The ordinal variable is shelf.

The nominal variables are name, mfr, and type.

b.

##load data cereals.csv

cereals<- read.csv("/Users/jingli/Desktop/Cereals.csv")

View(cereals)

sapply(cereals[,4:16],mean,na.rm=TRUE)

```
calories
                             fat
                                      sodium
                                                  fiber
              protein
                        1.012987 159.675325
106.883117
             2.545455
                                               2.151948
                                                  shelf
                                   vitamins
     carbo
                          potass
               sugars
                                  28.246753
                                               2.207792
14.597403
             6.922078
                       96.077922
   weight
                          rating
                 cups
 1.029610
             0.821039
                       42.665705
```

```
> sapply(cereals[,4:16],median,na.rm=TRUE)
```

calories	protein	fat	sodium	fiber	carbo
110.00000	3.00000	1.00000	180.00000	2.00000	14.00000
sugars	potass	vitamins	shelf	weight	cups
7.00000	90.00000	25.00000	2.00000	1.00000	0.75000
rating					
40.40021					

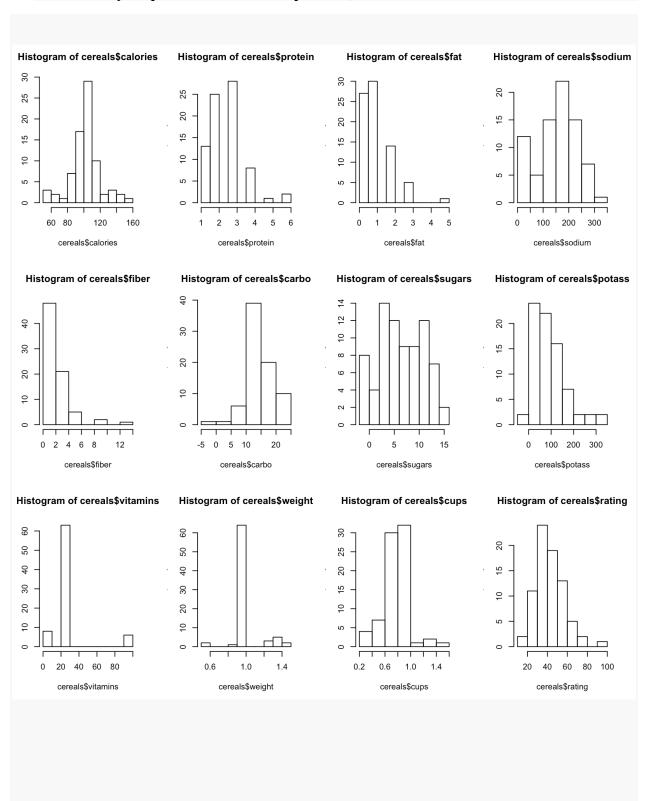
sapply(cereals[,4:16],max,na.rm=TRUE)

```
fiber
                          fat
                                  sodium
                                                       carbo
calories
            protein
                      5.00000 320.00000
                                          14.00000
160.00000
            6.00000
                                                    23.00000
             potass vitamins
                                   shelf
                                            weight
   sugars
                                                         cups
15.00000 330.00000 100.00000
                                 3.00000
                                           1.50000
                                                     1.50000
   ratina
93.70491
```

sapply(cereals[,4:16],sd,na.rm=TRUE)

```
calories
                             fat
                                     sodium
                                                 fiber
             protein
19.4841191
           1.0947897
                      1.0064726 83.8322952
                                             2.3833640
                                   vitamins
     carbo
                          potass
                                                 shelf
               sugars
           4.4448854 71.2868125 22.3425225
4.2789563
                                             0.8325241
    weight
                          rating
                 cups
0.1504768
           0.2327161 14.0472887
```

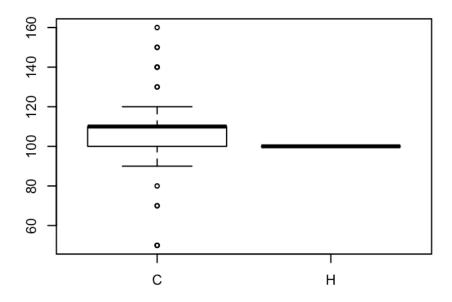
c. summary of quantities values except name, mfr shelf



Values have largest variability?

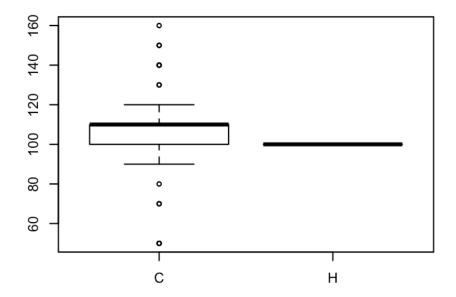
Potassium has the highest variability and sodium has the second highest variability. Fat Fiber Protein Carbo Potass Vitamin Shelf are the variables that seem to be skewed. From the histograms and the table, we see that the extreme variables are Protein Fiber Fat Vitamins Weight rating.

boxplot(cereals\$calories~cereals\$type)



The boxplots shows cold cereals have some variables that have extreme calories. The hot cereal has no variable.

e. boxplot(cereals\$rating~cereals\$shelf)



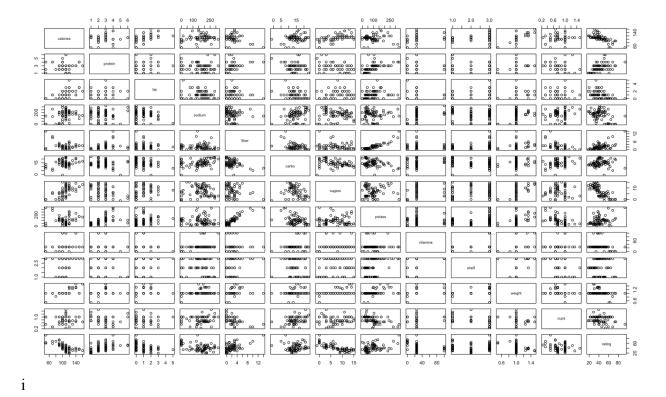
The mean of shelf_1 is similar to shelf 3 so we can choose shelf_1 and shelf_2 or shelf_1 and shelf_3 $\frac{1}{3}$

```
f.
cor(cereals[4:16])
```

```
> cor(cereals[4:16])
           calories
                                         fat
                                                   sodium
                         protein
                                 0.498609814
                                              0.300649227
calories
         1.00000000
                     0.019066068
                     1.000000000
protein
         0.01906607
                                 0.208430990 -0.054674348
fat
         0.49860981
                     0.208430990
                                 1.000000000 -0.005407464
sodium
         0.30064923 -0.054674348 -0.005407464
                                              1.000000000
fiber
        -0.29341275
                     0.500330043
                                 0.016719237 -0.070675009
carbo
         0.25068091 -0.130863648 -0.318043492
                                              0.355983473
sugars
         0.56234029 -0.329141777
                                 0.270819175
                                              0.101451381
potass
        -0.06660886 0.549407400
                                 0.193278602 -0.032603467
vitamins
         0.26535630 0.007335371 -0.031156266
                                              0.361476688
shelf
         0.09723437 0.133864789
                                 0.263691089 -0.069719015
weight
         0.69609108 0.216158486
                                 0.214625033
                                              0.308576451
         0.08719955 -0.244469158 -0.175892142
cups
                                              0.119664615
rating
        fiber
                          carbo
                                                potass
                                    sugars
calories -0.29341275
                     0.25068091
                                0.56234029 -0.06660886
protein
         0.50033004 -0.13086365 -0.32914178
                                            0.54940740
                                0.27081918
fat
         0.01671924 -0.31804349
                                            0.19327860
sodium
        -0.07067501
                     0.35598347
                                0.10145138 -0.03260347
fiber
         1.00000000 -0.35608274 -0.14120539
                                            0.90337367
carbo
        -0.35608274
                     1.00000000 -0.33166538 -0.34968522
        -0.14120539 -0.33166538
sugars
                                1.00000000
                                            0.02169581
         0.90337367 -0.34968522
potass
                                0.02169581
                                            1.00000000
vitamins -0.03224268
                     0.25814755
                                0.12513726
                                            0.02069869
shelf
         0.29753906 -0.10179030
                                0.10043789
                                            0.36066341
weight
         0.24722563
                     0.13513642
                                0.45064760
                                            0.41630315
                     0.36393247 -0.03235762 -0.49519495
cups
        -0.51306093
rating
         0.58416042
                     0.05205466 -0.75967466
                                            0.38016537
```

```
vitamins
                            shelf
                                      weight
                                                     cups
calories
          0.265356298
                       0.09723437
                                   0.6960911
                                               0.08719955
protein
          0.007335371
                       0.13386479
                                   0.2161585 -0.24446916
fat
         -0.031156266
                       0.26369109
                                   0.2146250 -0.17589214
sodium
          0.361476688 -0.06971902
                                   0.3085765
                                              0.11966461
fiber
         -0.032242679
                       0.29753906
                                   0.2472256 -0.51306093
carbo
          0.258147549 -0.10179030
                                   0.1351364
                                              0.36393247
                       0.10043789
                                   0.4506476 -0.03235762
          0.125137260
sugars
                       0.36066341
potass
          0.020698687
                                   0.4163032 -0.49519495
vitamins
          1.000000000
                       0.29926167
                                   0.3203241
                                              0.12840454
shelf
          0.299261665
                       1.00000000
                                   0.1907620 -0.33526876
weight
          0.320324059
                       0.19076197
                                   1.0000000 -0.19958272
cups
          0.128404543 -0.33526876 -0.1995827
                                               1.00000000
ratina
         -0.240543611
                       0.02515882 -0.2981240 -0.20316006
              rating
calories -0.68937603
protein
          0.47061846
fat
         -0.40928366
sodium
         -0.40129520
fiber
          0.58416042
carbo
          0.05205466
sugars
         -0.75967466
potass
          0.38016537
vitamins -0.24054361
shelf
          0.02515882
weight
         -0.29812398
         -0.20316006
cups
rating
          1.00000000
                                                             cor
```

plot(cereals[4:16])



strongly correlated: Potassium and fiber are strong correlated.

ii In the graph, there is a strong correlation between two variables. So we can dismiss one of them.

iii

After we normalize the data, we can conclude there is no change in the correlation matrix of the variables.

g.

pcs.cor <- prcomp(na.omit(cereals[,-c(1:3)]))

```
summary(pcs.cor)
  > pcs.cor <- prcomp(na.omit(cereals[,-c(1:3)]))</pre>
   > summary(pcs.cor)
   Importance of components:
                                                                                PC1
                                                                                                      PC2
                                                                                                                                PC3
                                                                                                                                                       PC4
                                                                                                                                                                              PC5
                                                                                                                                                                                                     PC6
                                                                                                                                                                                                                            PC7
                                                                                                                                                                                                                                                   PC8
                                                                                                                                                                                                                                                                          PC9
                                                                                                                                                                                                                                                                                               PC10
                                                                                                                                                                                                                                                                                                                 PC11
                                                                                                                                                                                                                                                                                                                                         PC12
  Standard deviation
                                                                    84.8289 71.3721 22.37869 18.8655 8.62931 2.37580 2.08502 0.80551 0.69493 0.53223 0.1844 0.06684 5.26e-08
  Proportion of Variance 0.5438 0.3850 0.03785 0.0269 0.00563 0.00043 0.00033 0.00005 0.00004 0.00002 0.00000 0.00000 0.00000 0.00000
   Cumulative Proportion 0.5438 0.9288 0.96661 0.9935 0.99914 0.99956 0.99989 0.99994 0.99998 1.00000 1.0000 1.0000 1.00e+00
  > summary(pcs.cor)
   Importance of components:
                                                                                PC1
                                                                                                      PC2
                                                                                                                                PC3
                                                                                                                                                       PC4
                                                                                                                                                                              PC5
                                                                                                                                                                                                     PC6
                                                                                                                                                                                                                            PC7
                                                                                                                                                                                                                                                   PC8
                                                                                                                                                                                                                                                                          PC9
                                                                                                                                                                                                                                                                                              PC10
                                                                                                                                                                                                                                                                                                                 PC11
                                                                                                                                                                                                                                                                                                                                         PC12
                                                                                                                                                                                                                                                                                                                                                                   PC13
                                                                    84.8289 71.3721 22.37869 18.8655 8.62931 2.37580 2.08502 0.80551 0.69493 0.53223 0.1844 0.06684 5.26e-08
   Standard deviation
   Proportion of Variance 0.5438 0.3850 0.03785 0.0269 0.00563 0.00043 0.00003 0.00005 0.00004 0.00002 0.0000 0.00000 0.00000 0.00000
  Cumulative Proportion 0.5438 0.9288 0.96661 0.9935 0.99914 0.99956 0.99989 0.99994 0.99998 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.000000 1.00000 1.00000 1.000000 1.000000 1.000000 1.000000 1.00000 1.00000 1.00000 1.0000
```

The first principal component is the projection of the data sets onto the new basis vectors and the variance of the PC1 covers 54.38% of the whole information. We only need two 2 principal components to cover the 92.88%, which is more than 90%, of the total variability. Then we can reduce the variables from 13 to 2 to do the analysis.

Problem3(House Median Price in Boston)

bostonhousing<-read.csv("/Users/jingli/Desktop/BostonHousing.csv") View(bostonhousing)

a.

based on the original data, we can find that categorical data is binary, so we use MIN MAX to rescale data from 0 to 1.

```
min <- sapply(bostonhousing,function(x) min(x))
```

max<-sapply(bostonhousing,function(x) max(x))</pre>

max_min <- bostonhousing

for(i in 1:14){max min[,i]=(max min[,i]-min[i])/(max[i]-min[i])}

b.

Implementcorrelationanalysis for all features compared to the class (MEDV>30) in the last column. Rank features based on their correlation coefficients and identify the top 5 features. The top 5 features are

MEDV RM ZN DIS CHAS(top 5 features)

bostonhousing<-read.csv("/Users/jingli/Desktop/BostonHousing.csv")

cor(bostonhousing)[,14]

ZN	INDUS	CHAS	NOX
0.3652962	-0.3662756	0.1086312	-0.2325018
AGE	DIS	RAD	TAX
-0.1911959	0.1188865	-0.1979240	-0.2736867
LSTAT	MEDV	CATMEDV	
-0.4699108	0.7897888	1.0000000	
	0.3652962 AGE -0.1911959 LSTAT	0.3652962 -0.3662756 AGE DIS -0.1911959 0.1188865 LSTAT MEDV	0.3652962 -0.3662756 0.1086312 AGE DIS RAD -0.1911959 0.1188865 -0.1979240

order(cor(bostonhousing)[,14],decreasing = TRUE)

```
> order(cor(bostonhousing)[,14],decreasing = TRUE)
[1] 14 13 6 2 8 4 1 7 9 5 10 3 11 12
```

bostonhousing<-read.csv("/Users/jingli/Desktop/BostonHousing.csv")
pca_bh<-prcomp(bostonhousing)
summary(pca_bh)

Importance of components:

PC1 PC2 PC3 PC4 Standard deviation 169.761 28.74148 16.35153 8.93818 Proportion of Variance 0.958 0.02746 0.00889 0.00266 Cumulative Proportion 0.958 0.98543 0.99431 0.99697 PC5 PC6 PC7 PC8 PC9 Standard deviation 6.88113 4.13097 3.68806 2.9939 1.66185 Proportion of Variance 0.00157 0.00057 0.00045 0.0003 0.00009 0.99854 0.99911 0.99956 0.9999 0.99995 Cumulative Proportion PC10 PC11 PC12 **PC13 PC14** Standard deviation 1.05055 0.47515 0.244 0.1959 0.05386 Proportion of Variance 0.00004 0.00001 0.000 0.00000 0.00000 0.99999 1.00000 1.000 1.0000 1.00000 Cumulative Proportion

bostonhousing<-read.csv("/Users/jingli/Desktop/BostonHousing.csv")
pea bh<-pre>prcomp(bostonhousing)</pr>

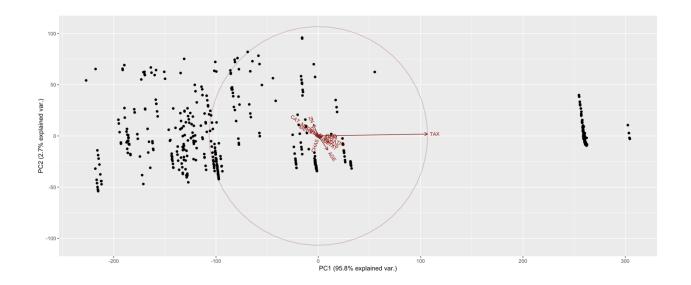
summary(pca bh)

pca_bhs<-prcomp(max_min)</pre>

```
summary(pca bhs)
Importance of components:
                               PC1
                                       PC2
                                                PC3
                                                         PC4
                                                                   PC5
Standard deviation
                           0.6676 0.3925 0.3108 0.24363 0.20205
Proportion of Variance 0.4918 0.1699 0.1066 0.06549 0.04504
Cumulative Proportion
                           0.4918 0.6617 0.7683 0.83380 0.87884
                                PC6
                                          PC7
                                                   PC8
                                                             PC9
                                                                     PC10
                           0.16712 0.14737 0.13434 0.10468 0.08886
Standard deviation
Proportion of Variance 0.03082 0.02396 0.01991 0.01209 0.00871
Cumulative Proportion
                           0.90966 0.93362 0.95354 0.96563 0.97434
                                         PC12
                                                  PC13
                                                            PC14
                               PC11
Standard deviation
                           0.08449 0.08208 0.07481 0.06150
Proportion of Variance 0.00788 0.00743 0.00618 0.00417
Cumulative Proportion 0.98222 0.98965 0.99583 1.00000
intall.packages("devtools")
install.packages("ggplot2")
library(devtools)
install github("ggbiplot", "vqv")
## Warning: Username parameter is deprecated. Please use vqv/ggbiplot
## Skipping install of 'ggbiplot' from a github remote, the SHA1 (7325e880) has not changed
since last install.
## Use `force = TRUE` to force installation
library(ggbiplot)
## Loading required package: ggplot2
##
## Attaching package: 'ggplot2'
## The following objects are masked from 'package:psych':
##
##
    %+%, alpha
## Loading required package: plyr
## Loading required package: scales
```

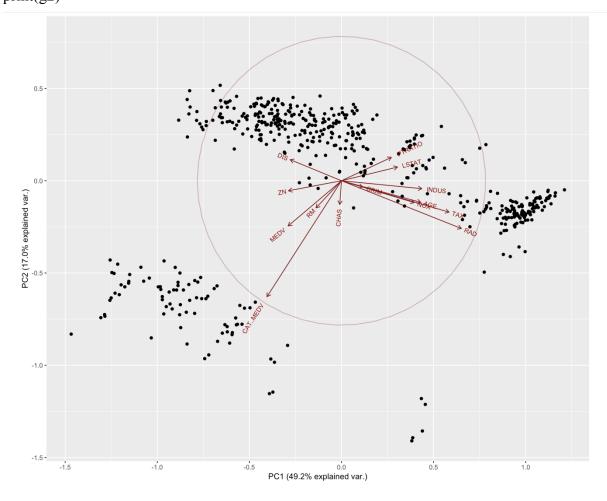
##

```
## Attaching package: 'scales'
## The following objects are masked from 'package:psych':
##
## alpha, rescale
## The following object is masked from 'package:plotrix':
##
## rescale
## Loading required package: grid
pca_bh<-prcomp(bostonhousing)
g1 <- ggbiplot(pca_bh, obs.scale = 1, var.scale = 1, ellipse = TRUE, circle = TRUE)
g1 <- g1 + scale_color_discrete(name = ")
g1 <- g1 + theme(legend.direction = 'horizontal', legend.position = 'top')
print(g1)</pre>
```



```
min <- sapply(bostonhousing,function(x) min(x))
max<-sapply(bostonhousing,function(x) max(x))
max_min <- bostonhousing
for(i in 1:14){max_min[,i]= (max_min[,i]-min[i])/(max[i]-min[i])}
pca_bhs<-prcomp(max_min)

g2 <- ggbiplot(pca_bhs, obs.scale = 1, var.scale = 1, ellipse = TRUE, circle = TRUE)
g2 <- g2 + scale_color_discrete(name = ")
g2 <- g2 + theme(legend.direction = 'horizontal', legend.position = 'top')
print(g2)</pre>
```



Problem4

a. the first principal component is much bigger than others, all features are not at the same scale . Consequently, results will be influenced by original data, and it has the highest proportion of original variance

```
> wine <-read.csv("/Users/jingli/Desktop/Wine.csv")</pre>
> View(wine)
> pcs.cor <- prcomp(wine[,-1])</pre>
> summary(pcs.cor)
Importance of components:
                           PC1
                                    PC2
                                            PC3
                                                    PC4
                                                            PC5
                                                                   PC6
                                                                          PC7
                                                                                 PC8
                                                                                        PC9
                                                                                             PC10
                                                                                                     PC11
Standard deviation
                      314.9632 13.13527 3.07215 2.23409 1.10853 0.91710 0.5282 0.3891 0.3348 0.2678 0.1938 0.1452 0.09057
Proportion of Variance 0.9981 0.00174 0.00009 0.00005 0.00001 0.00001 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
Cumulative Proportion
                        0.9981 0.99983 0.99992 0.99997 0.99998 0.99999 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000
> View(pcs.cor)
> pcs.cor$rotation
                                                                                  PC5
                                                                     PC4
                              PC1
                                            PC2
                                                         PC3
                                                                                               PC6
                                                                                                            PC7
                                                                                                                          PC8
                    -0.0016592647 -1.203406e-03 -0.016873809
                                                             0.141446778
                                                                          0.020336977 -0.194120104
                                                                                                    0.923280337 -2.848207e-01
Alcohol
                     0.0006810156 -2.154982e-03 -0.122003373
                                                                         -0.612883454 -0.742472963
Malic Acid
                                                             0.160389543
                                                                                                   -0.150109941
                                                                                                                 6.467447e-02
Δsh
                    -0.0001949057 -4.593693e-03 -0.051987430
                                                             -0.009772810
                                                                          0.020175575
                                                                                      -0.041752912
                                                                                                    0.045009549
                                                                                                                 1.493395e-01
Ash Alcalinity
                     0.0046713006 -2.645039e-02 -0.938593003 -0.330965260
                                                                          0.064352340
                                                                                       0.024065303
                                                                                                    0.031526583
                                                                                                                -1.515391e-02
Magnesium
                    -0.0178680075 -9.993442e-01 0.029780248 -0.005393756
                                                                          -0.006149345
                                                                                       0.001923782
                                                                                                    0.001797363
                                                                                                                 3.552212e-03
Total_Phenols
                    -0.0009898297 -8.779622e-04
                                                0.040484644 -0.074584656
                                                                          0.315245063
                                                                                      -0.278716809
                                                                                                    -0.020185710
                                                                                                                 1.772379e-01
                    -0.0015672883
                                   5.185073e-05
                                                 0.085443339
                                                                          0.524761088
Flavanoids
                                                             -0.169086724
                                                                                       -0.433597955
                                                                                                    -0.038868518
                                                                                                                 2.481166e-01
0.010805561
                                                                          -0.029647512
                                                                                       0.021952834
                                                                                                   -0.004665483
Proanthocyanins
                    -0.0006006078 -5.004400e-03
                                                0.024659382
                                                             -0.050120952
                                                                          0.251182529
                                                                                       -0.241884488
                                                                                                   -0.309799487
                                                                                                                 -8.704332e-01
                    -0.0023271432 -1.510035e-02 -0.291398464
                                                             0.878893693
                                                                          0.331747051 -0.002739609
                                                                                                   -0.112836514
Color_Intensity
                                                                                                                 8.128692e-02
                    -0.0001713800
                                  7.626731e-04
                                                0.025977662 -0.060034945
                                                                          0.051524077
                                                                                       0.023776167
                                                                                                    0.030819813
                                                                                                                2.951904e-03
Hue
0D280_0D315
                    -0.0007049316 3.495364e-03
                                                0.070323969 -0.178200254
                                                                          0.260639176 -0.288912753 0.101973518
                                                                                                                1.867145e-01
Proline
                    -0.9998229365 1.777381e-02 -0.004528682 -0.003112916 -0.002298569 0.001212255 -0.001076189 -1.034095e-05
                              PC9
                                           PC10
                                                        PC11
                                                                      PC12
                                                                                    PC13
Al cohol
                    -8.660061e-02 2.245000e-03 -0.0149715080 -1.565141e-02
                                                                            8.029245e-03
Malic_Acid
                    -1.566214e-02
                                   1.850935e-02
                                                -0.0231876506
                                                              6.729555e-02
                                                                            -1.109039e-02
Ash
                    -7.364985e-02 8.679965e-02 0.9540106426
                                                              -1.320630e-01 -1.736857e-01
Ash_Alcalinity
                    -2.044578e-03 -3.554028e-03 -0.0528216953
                                                              5.393806e-03
                                                                            1.939563e-03
Maanesium
                     1.963668e-03 4.051542e-05 -0.0030248882
                                                               6.208885e-04
Total Phenols
                    -2.556729e-01 -8.471951e-01 0.0088016070
                                                              3.882903e-03
                                                                            -2.669144e-02
                    -3.783067e-01 5.201384e-01 -0.1332046120
                                                              -3.748803e-02 6.959853e-02
Flavanoids
Nonflavanoid_Phenols -3.675204e-02 -3.771319e-02
                                                0.1991789841
                                                              1.475524e-01
                                                                            9.664662e-01
                     5.152017e-02 -9.722752e-03 0.1356214601 -1.311883e-02 -1.760357e-02
Proanthocyanins
                     9.902908e-02 2.314712e-02 -0.0098196717
                                                              5.035557e-02 -4.632943e-03
Color_Intensity
Hue
                    -3.306512e-02 3.846983e-02 0.0975106606
                                                              9.755619e-01 -1.665508e-01
0D280_0D315
                     8.737465e-01 -1.701708e-02 0.0284851062
                                                              1.163025e-02 4.419224e-02
Proline
                     7.255852e-05 -4.926638e-05 -0.0002404522
                                                              -9.999951e-05
                                                                            3.626701e-05
>
```

b.

After we normalized data, all features data are at the same scale, which means all variables have equal variability. so results are not influent by original data. we can find that we need 8 PCs to account for more than 90% of total variability. The Alternative to performing PCA is to perform PCA on correction matrix instead of the covariance matrix.