



# *Compressed Acquisition and Imaging for Ocean Turbulence Monitoring*

**Jingming Ruan<sup>1</sup>, Ivan Vasconcelos<sup>1</sup>, and Dirk-Jan van Manen<sup>2</sup>**

<sup>1</sup> Utrecht University, Netherlands

<sup>2</sup> ETH Zurich, Switzerland



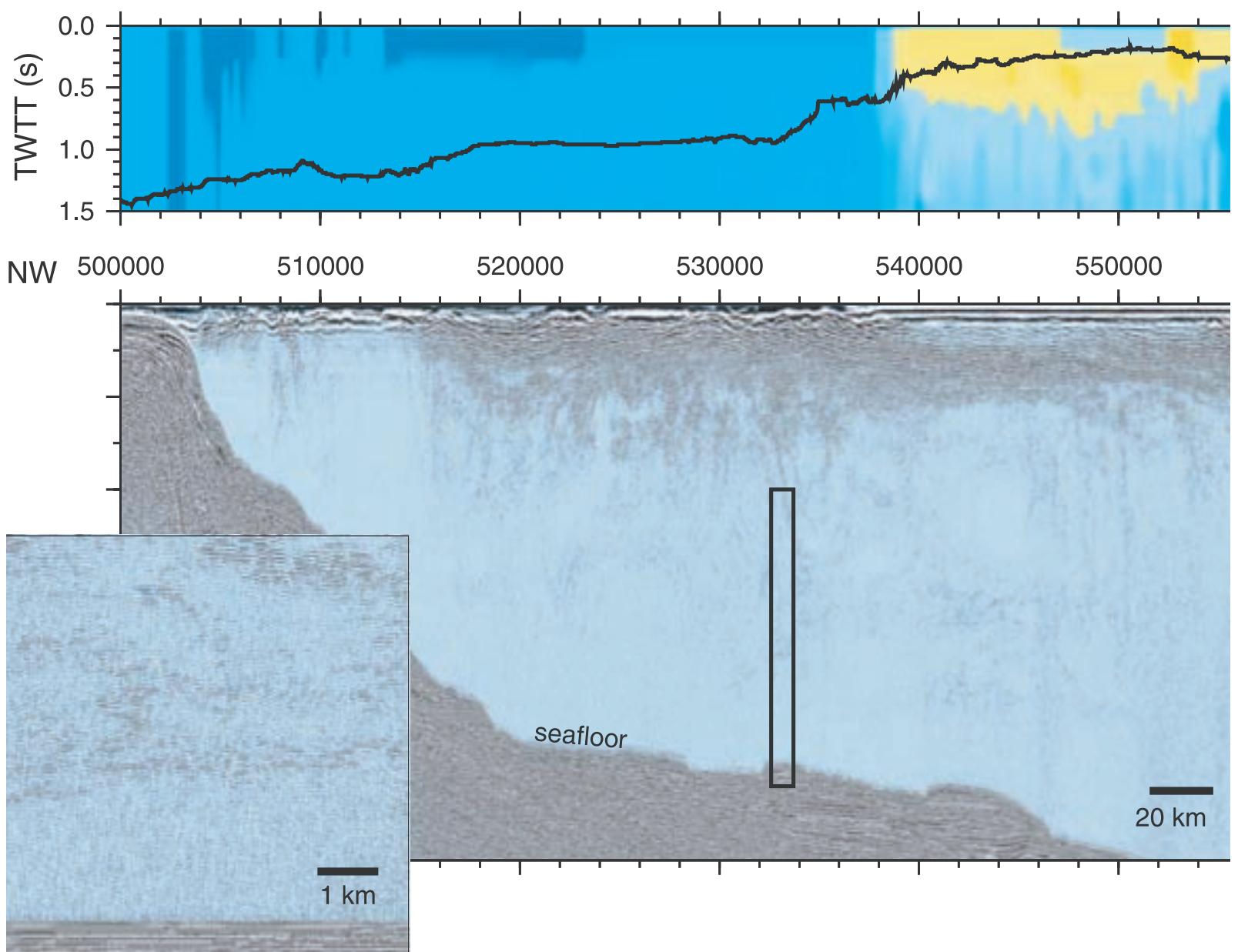
- *Seismic Oceanography*
- *Seismic acquisition*
- *Multicomponent reconstruction*
- *Sediment model*
  - regular sampling & irregular sampling
- *Turbulence model*
  - preconditioning
  - multi-source & multi-receiver (3D)



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# Seismic Oceanography (SO)

Fronts, internal waves,  
eddies, etc.

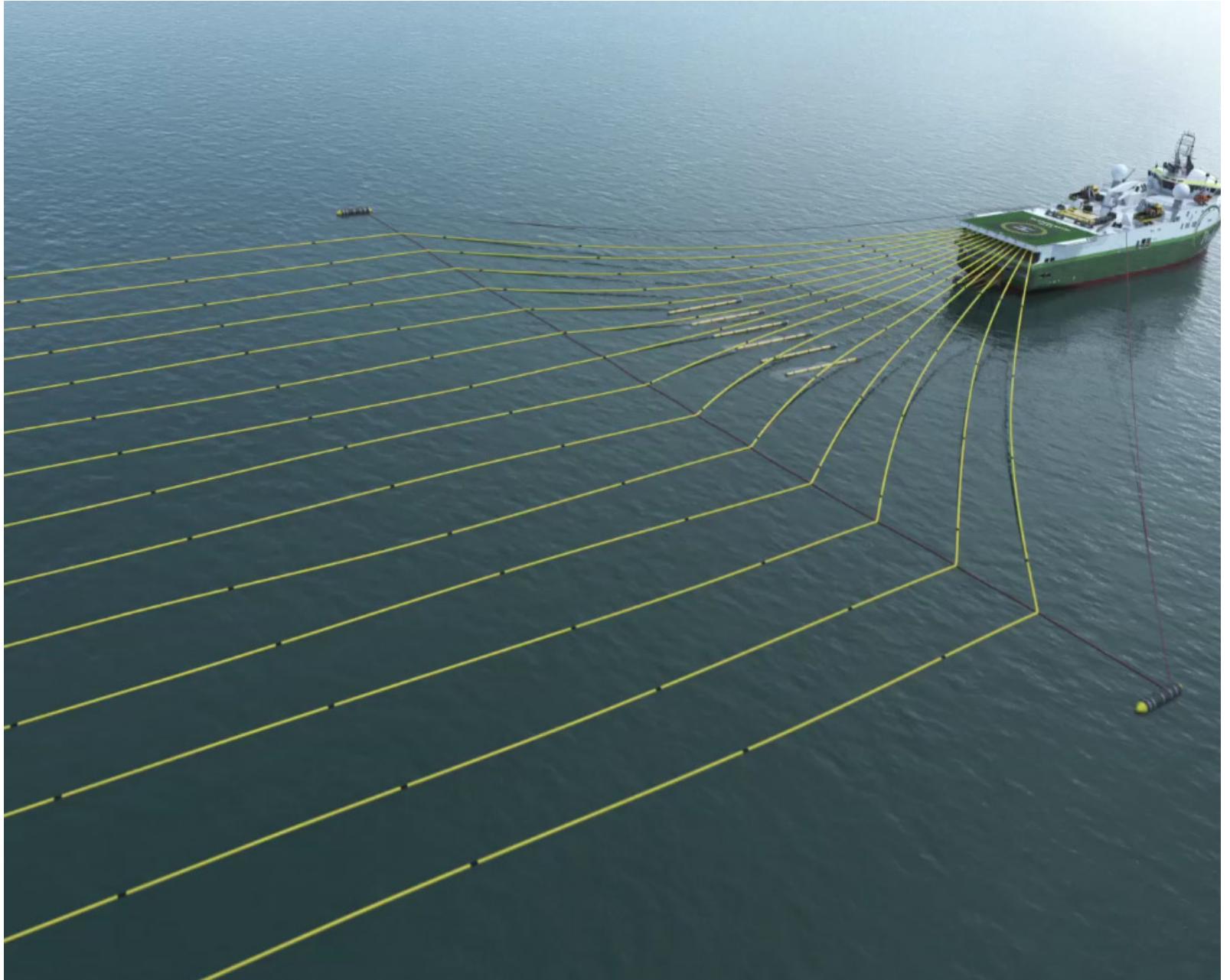


Holbrook, W. Steven, et al. (2003)

# Multichannel Seismic systems (MSC)

Dense lateral sampling

Expensive

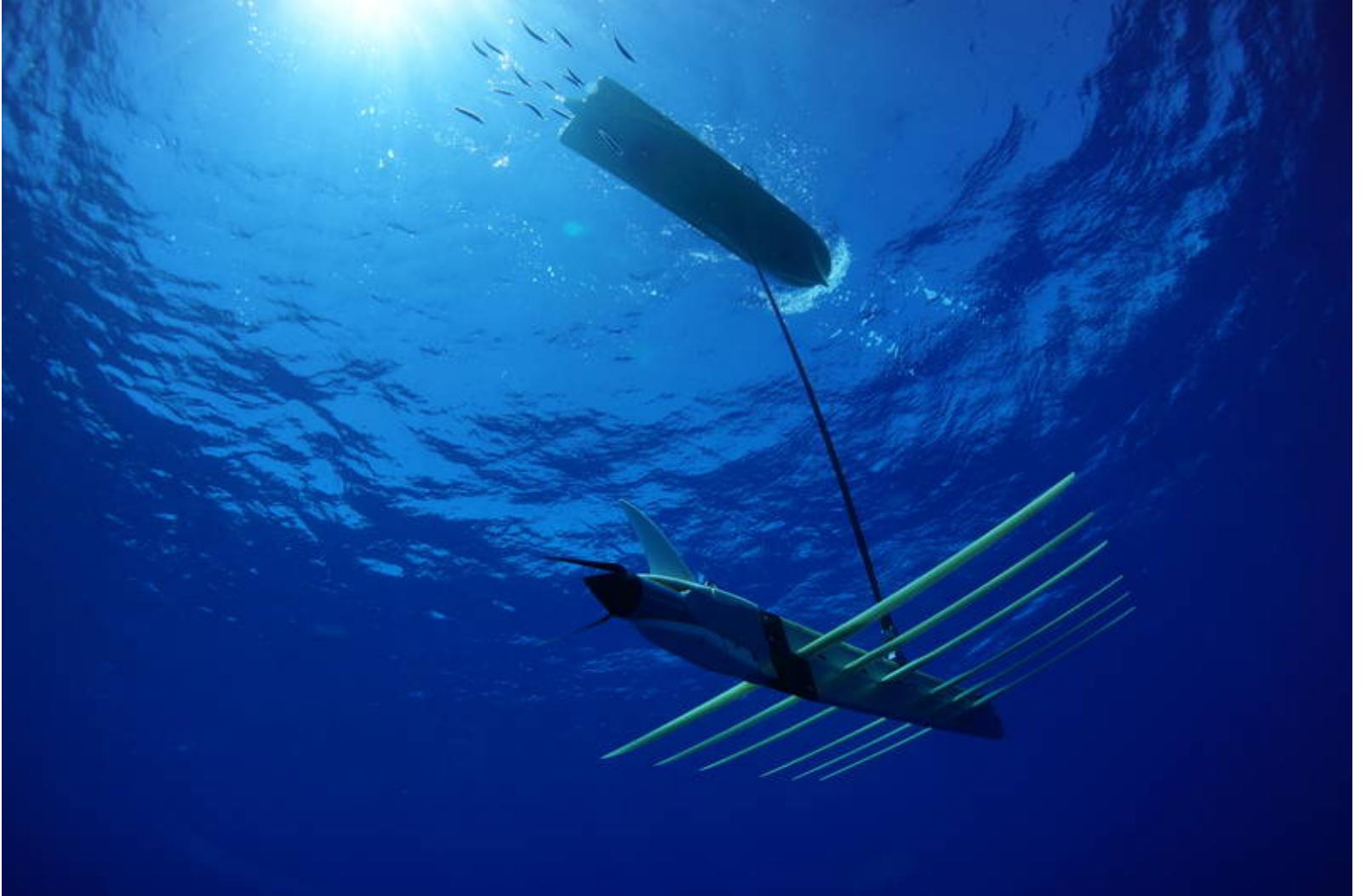


# Multichannel Seismic systems (MSC)

Dense lateral sampling

Expensive

Autonomous platform



# Sampling scheme

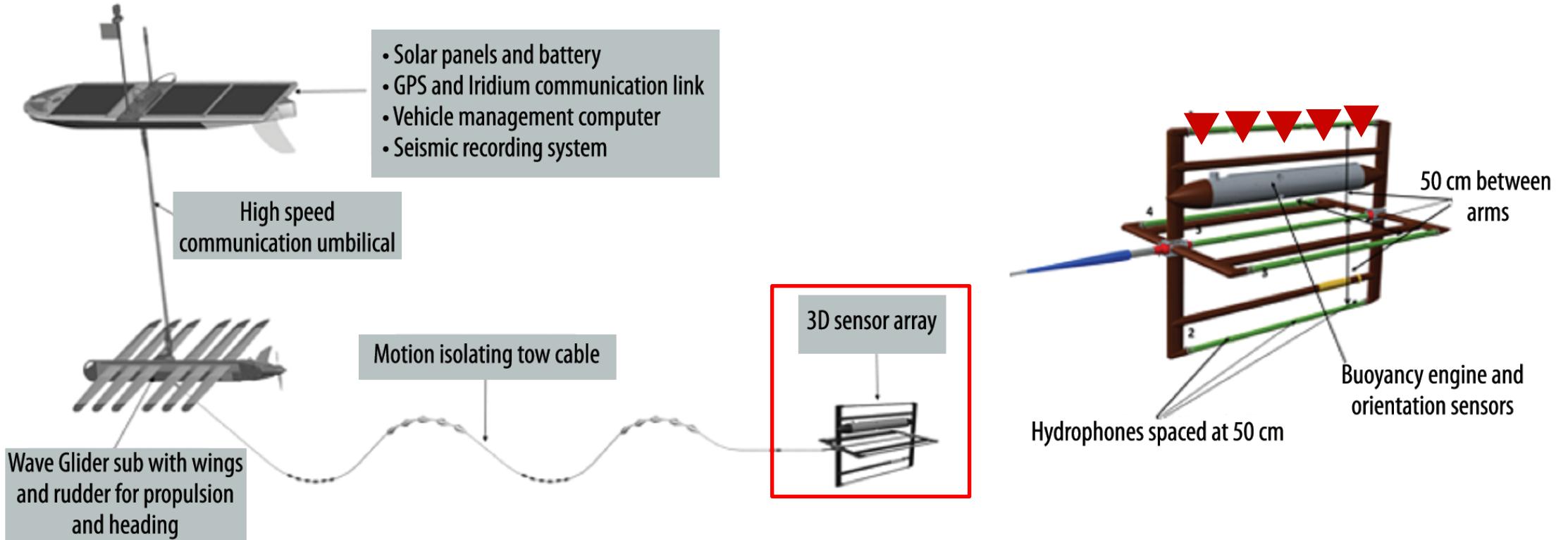
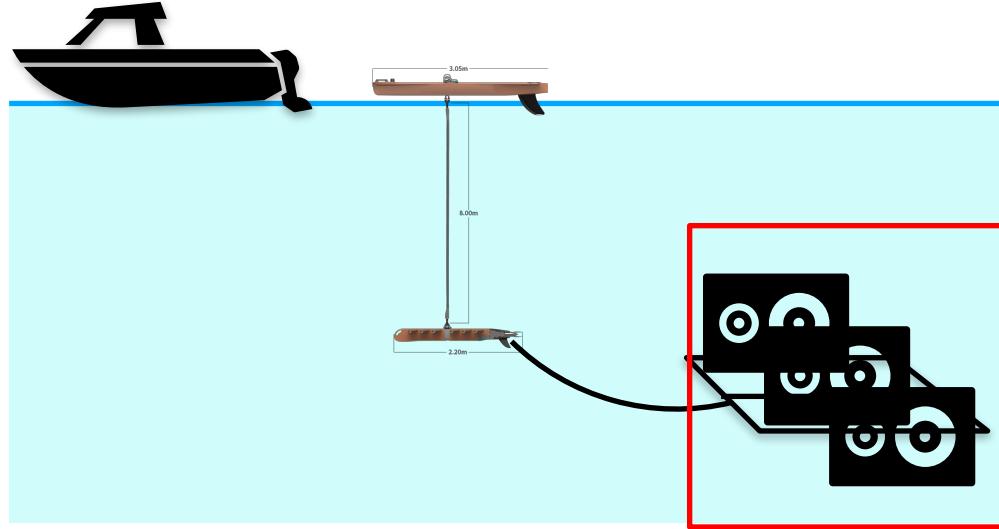


Figure 1. (a) AMV components, decoupling cable, and the 3DSA. (b) Enlarged view of the 3DSA.

Measurements of pressure data and its derivatives in receiver direction.

# Sampling scheme



## Marine Vibrator



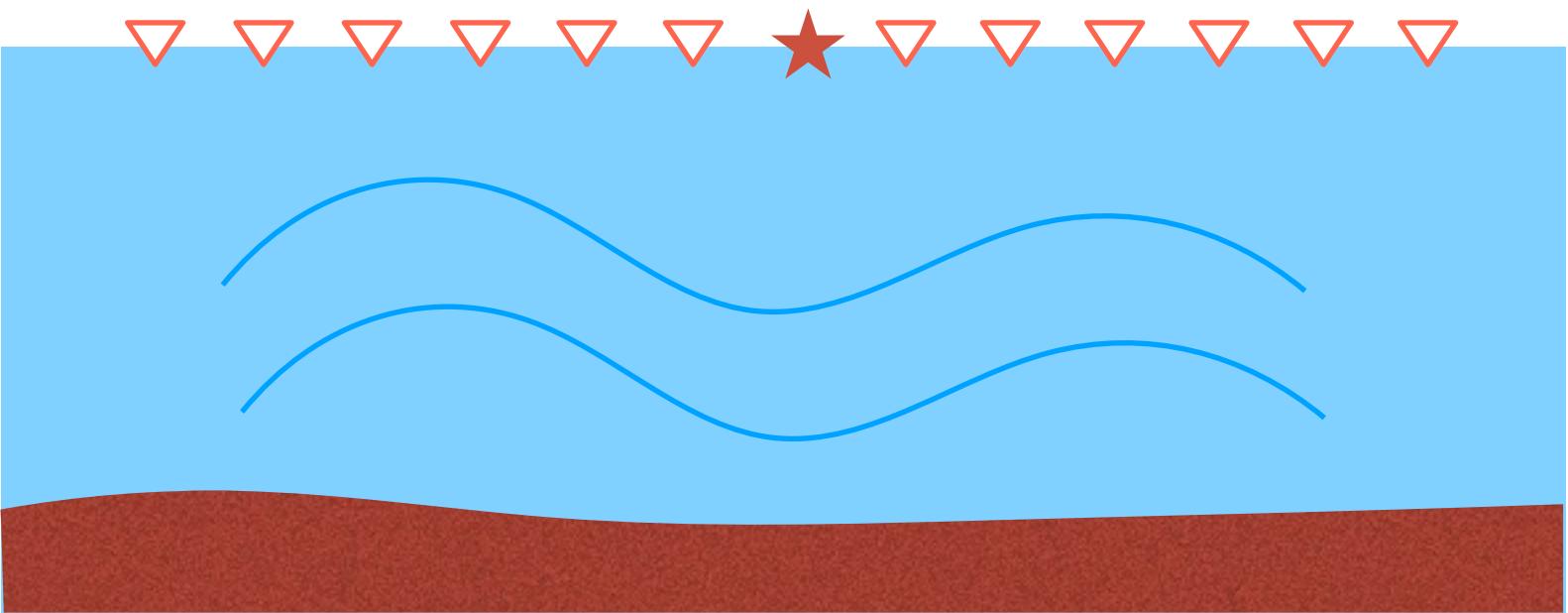
Phase & frequency control

Measurements of derivatives in source direction.

# Sampling scheme

Autonomous platform

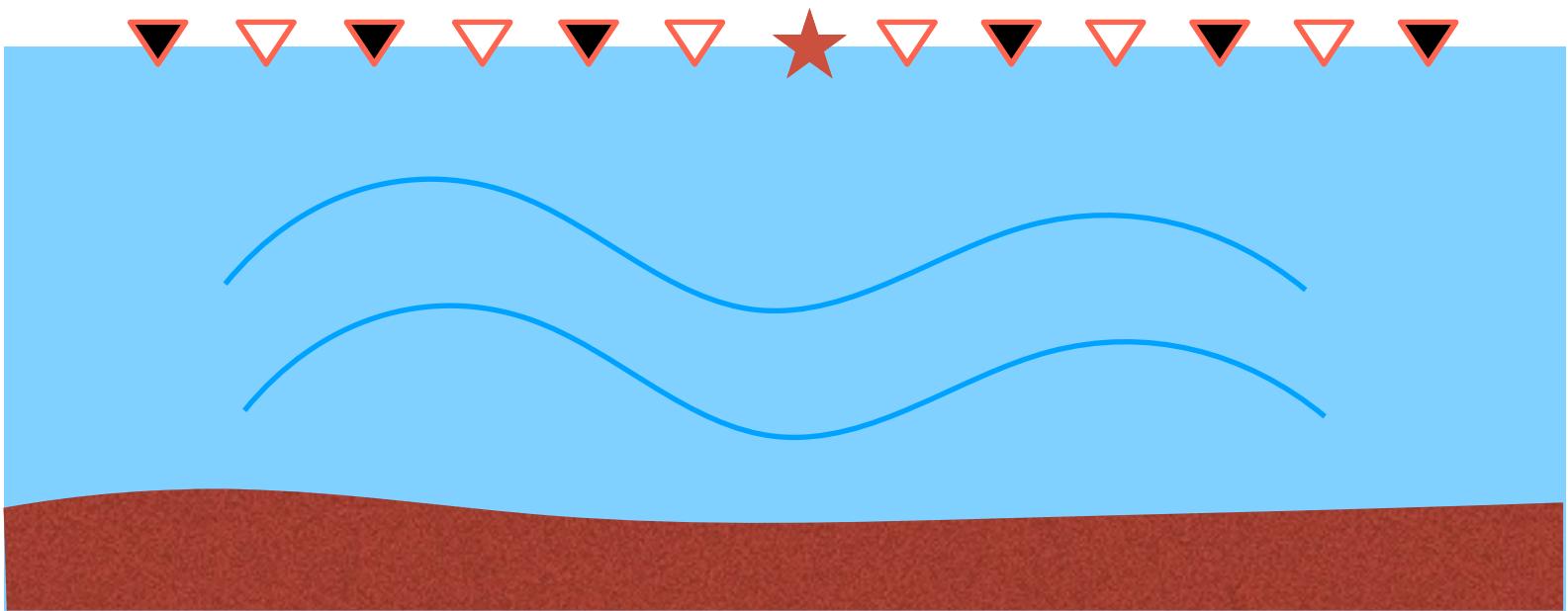
Sampling scheme:



# Sampling scheme

Autonomous platform

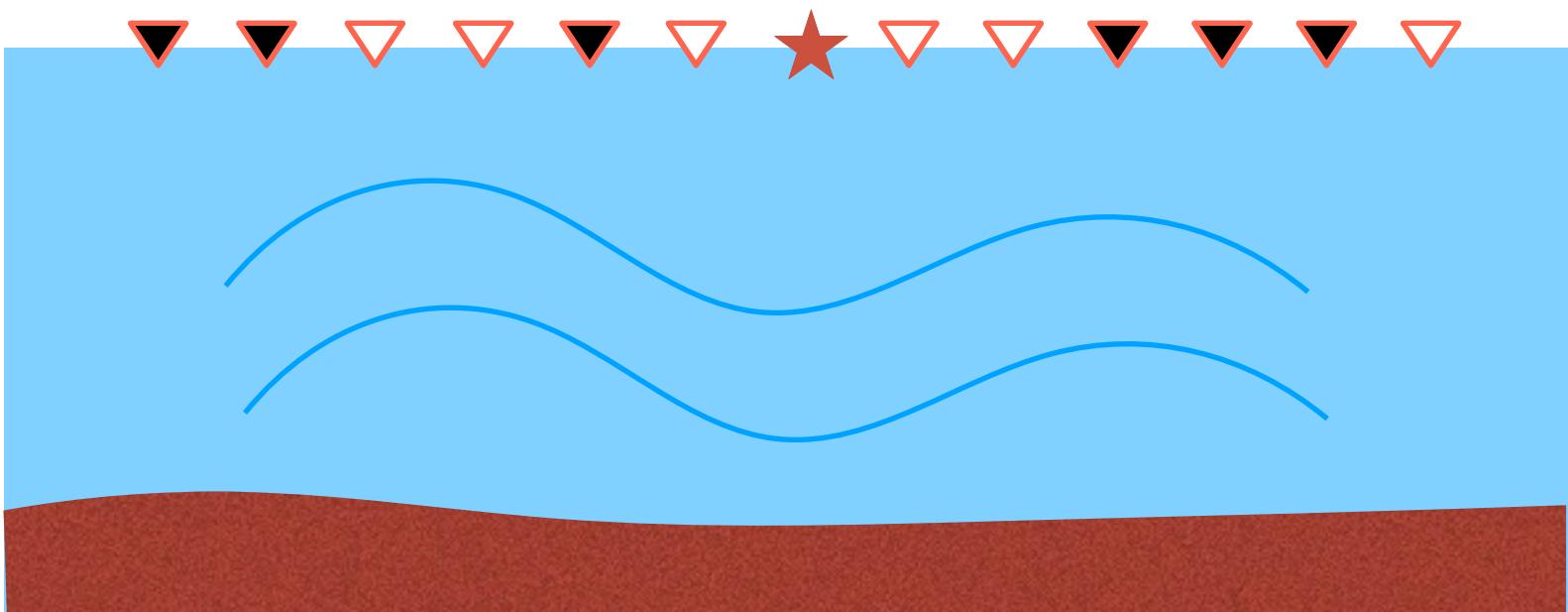
Sampling scheme:  
– regular sampling



# Sampling scheme

Autonomous platform

Sampling scheme:  
– regular sampling  
– irregular sampling

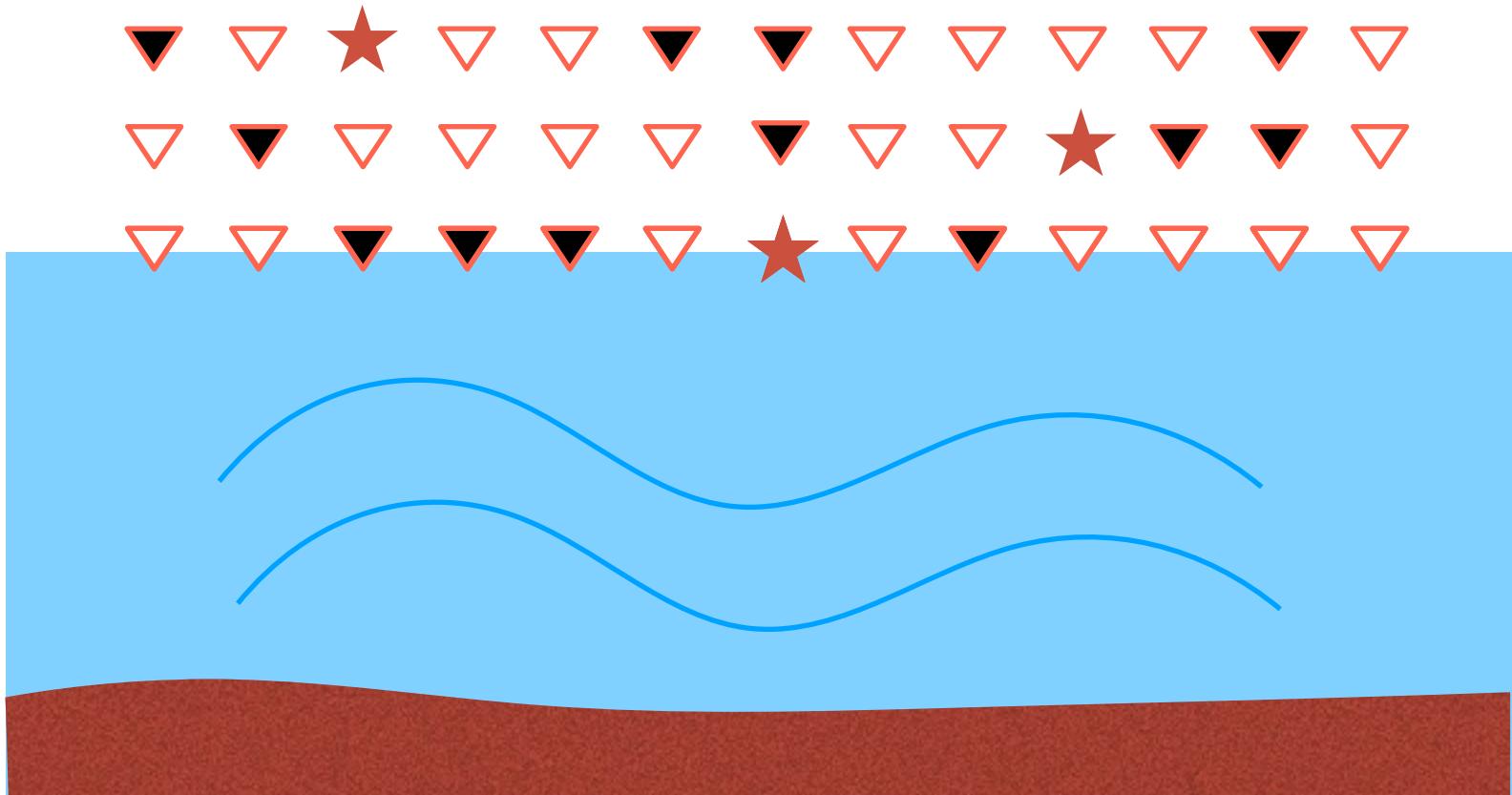


# Sampling scheme

Autonomous platform

Sampling scheme:  
– regular sampling  
– irregular sampling

Multi-source





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## Equations

Sinc interpolator

$$p(y_0) = \sum_{m=-\infty}^{\infty} p\left(\frac{m}{\sigma}\right) \text{sinc}(\sigma y_0 - m)$$

Multichannel sampling theorem (Linden, 1959; Robertsson, 2008)

$$p(y_0) = \sum_{m=-\infty}^{\infty} \left\{ p\left(\frac{2m}{\sigma}\right) + (y_0 - \frac{2m}{\sigma}) \times \boxed{\partial_y p\left(\frac{2m}{\sigma}\right)} \right\} \text{sinc}^2\left(\sigma \frac{y_0}{2} - m\right)$$

## Multicomponent reconstruction

With data and its first-order  
spatial derivatives

$$d_{obs} = S d_{model}$$

$$d_{obs} = \begin{pmatrix} d_t \\ d_I \end{pmatrix} \text{ and } S = \begin{pmatrix} R_r \\ D_I \end{pmatrix}$$

$$D_I = R_r * F^{-1} * \text{diag}(ik_n) * F$$

## Multicomponent reconstruction

With data, its first- and second-order spatial derivatives

$$d_{obs} = S d_{model}$$

$$d_{obs} = \begin{pmatrix} d_t \\ d_1 \\ d_2 \end{pmatrix} \text{ and } S = \begin{pmatrix} R_r \\ D_1 \\ D_2 \end{pmatrix}$$

$$D_1 = R_r * F^{-1} * \text{diag}(ik_n) * F$$

$$D_2 = R_r * F^{-1} * \text{diag}[(ik_n)^2] * F$$

## Choice of the solvers& their Preconditioning

Solvers: LSQR, SPGL1

Domains: Fourier, Curvelet

Packages: Pylops(Python)  
SPOT(MATLAB)

$$d_{mod} = F^{-1} d_f$$

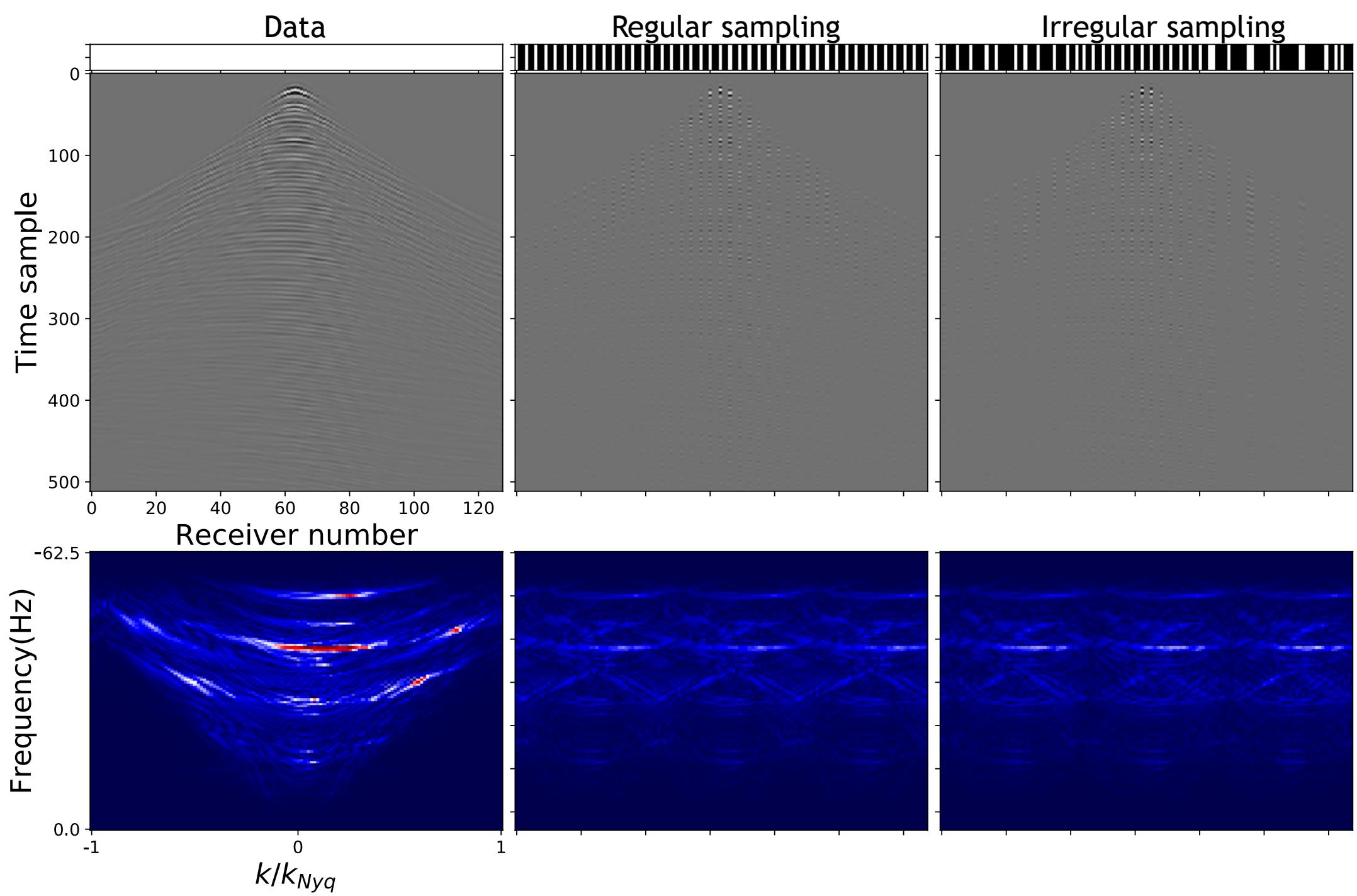
$$d_{obs} = SF^{-1} d_f$$

$$LSQR: \min \|d_{obs} - SF^{-1}d_{mod}\|_2$$

$$SPGL1(BPDN): \min \|d_{mod}\|_1 \text{ s.t. } \|d_{obs} - SF^{-1}d_{mod}\|_2 < \tau$$



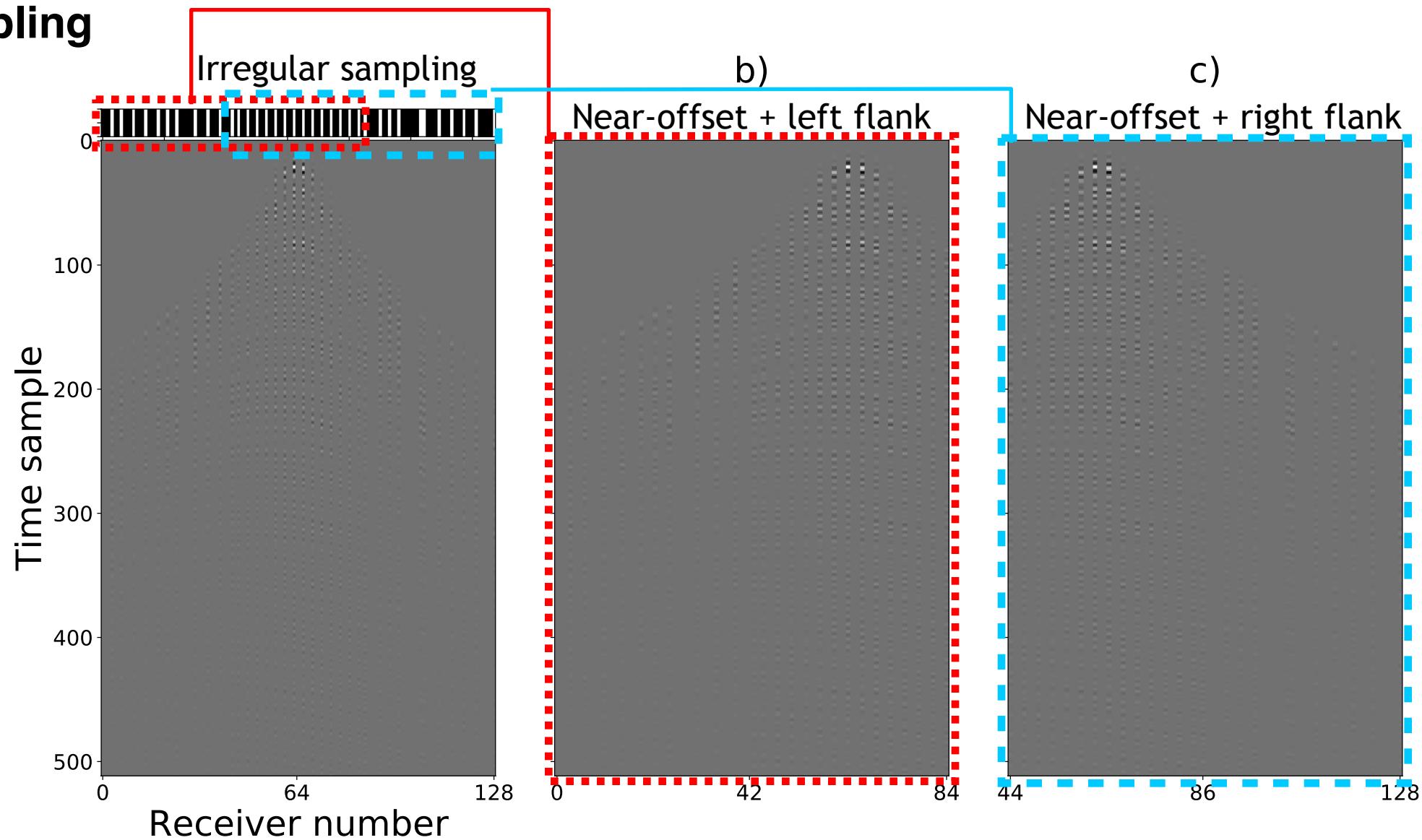
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## Partitioned sampling

$$d_{obs}^L = P d_f^L$$

$$d_{obs}^R = P d_f^R$$

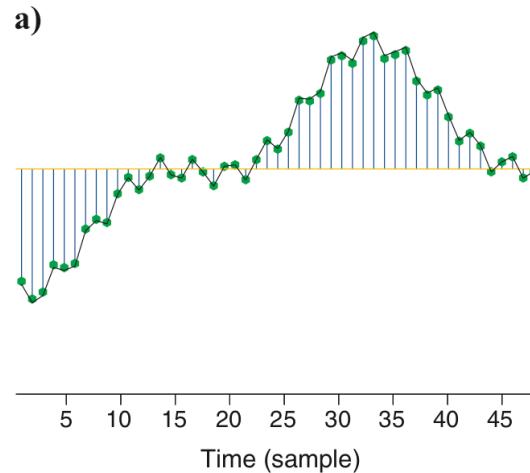


# Irregular sampling

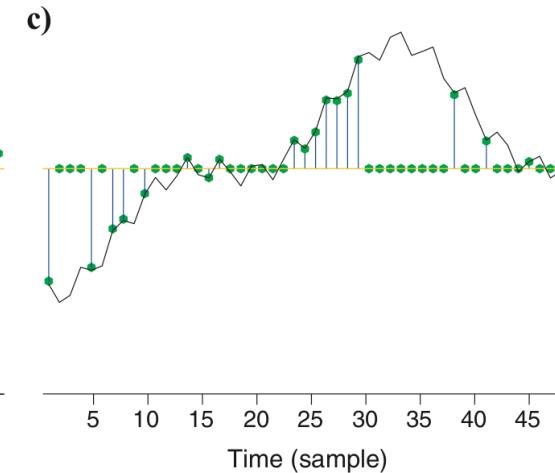
Regular sampling: strong imprint

Irregular sampling: weak imprint

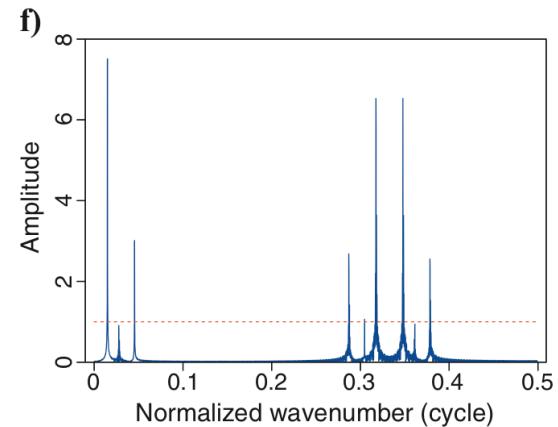
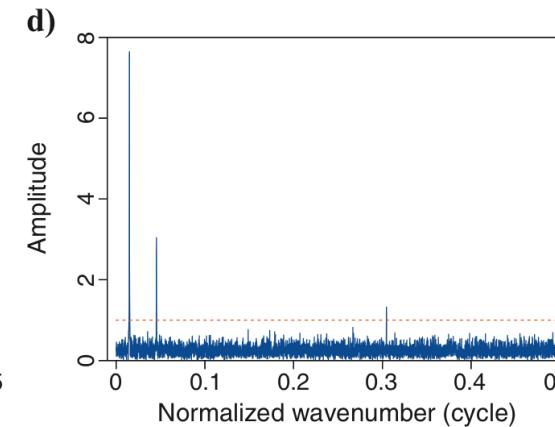
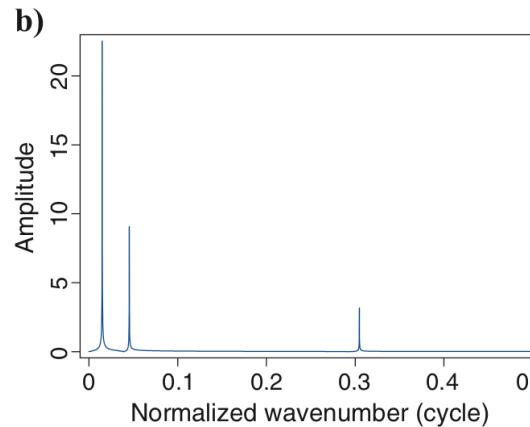
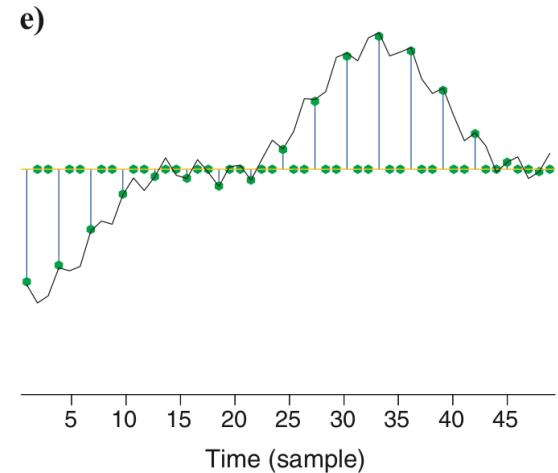
Data



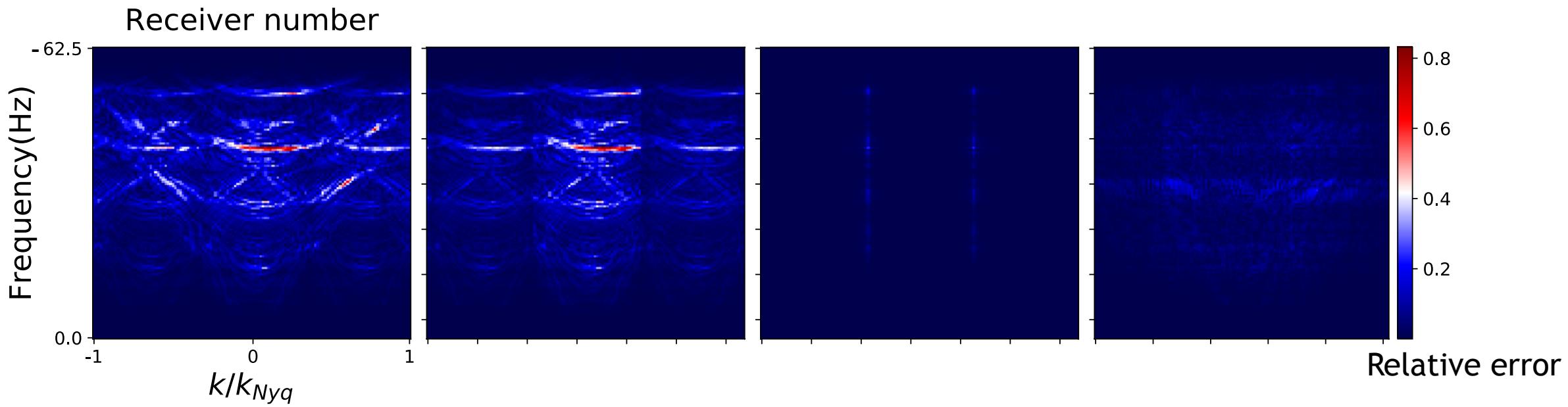
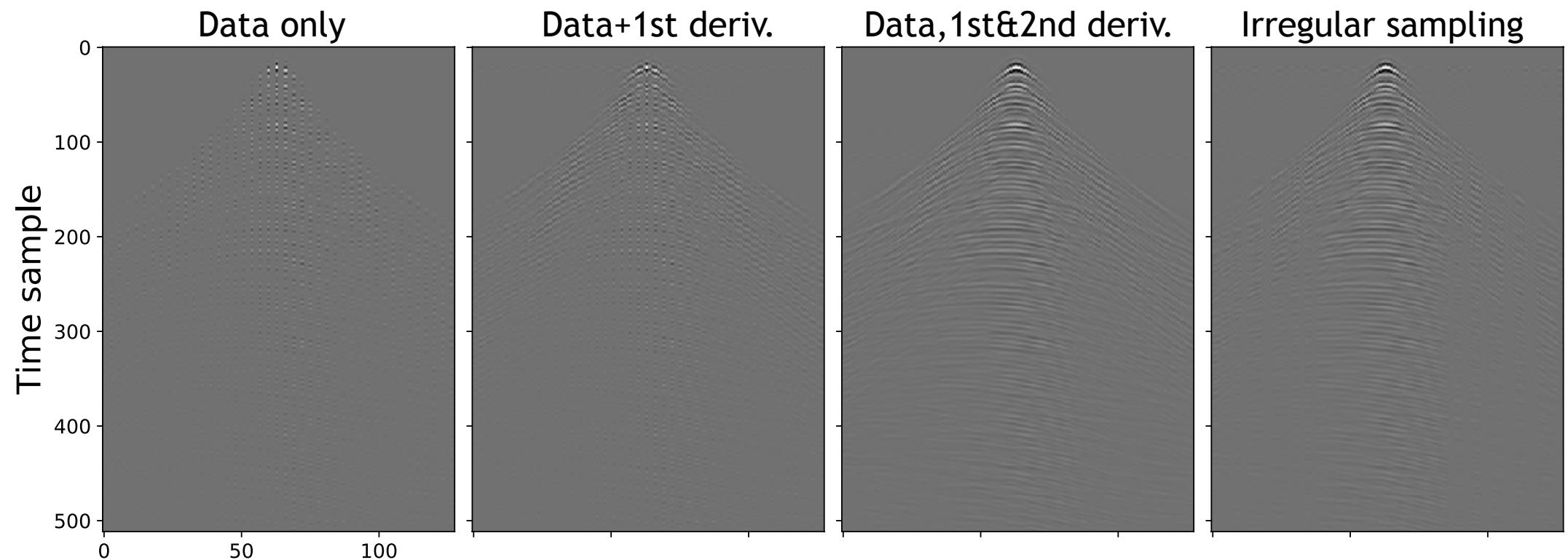
Irregular sampling



Regular sampling



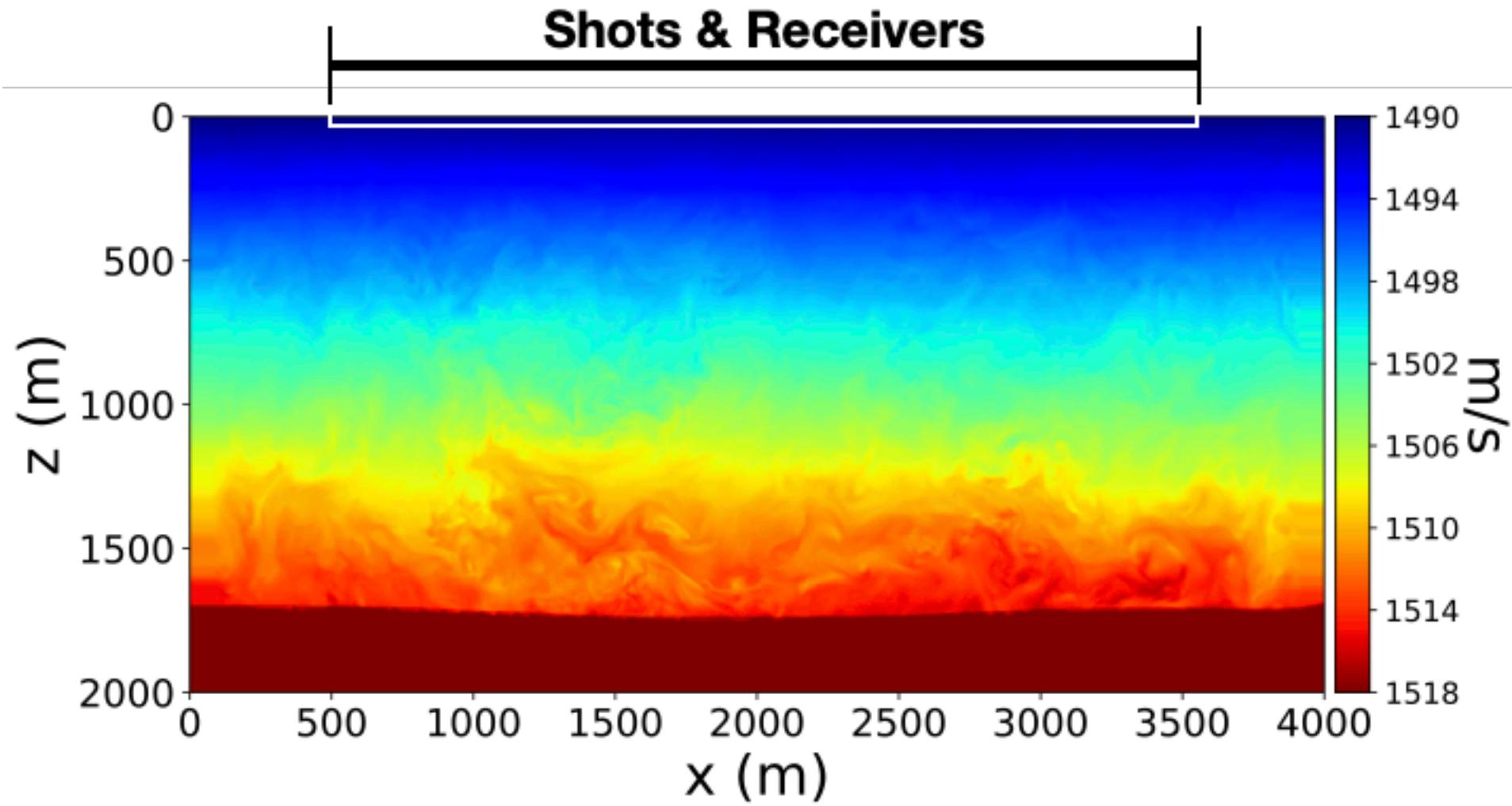
Felix J. Herrmann(2010)



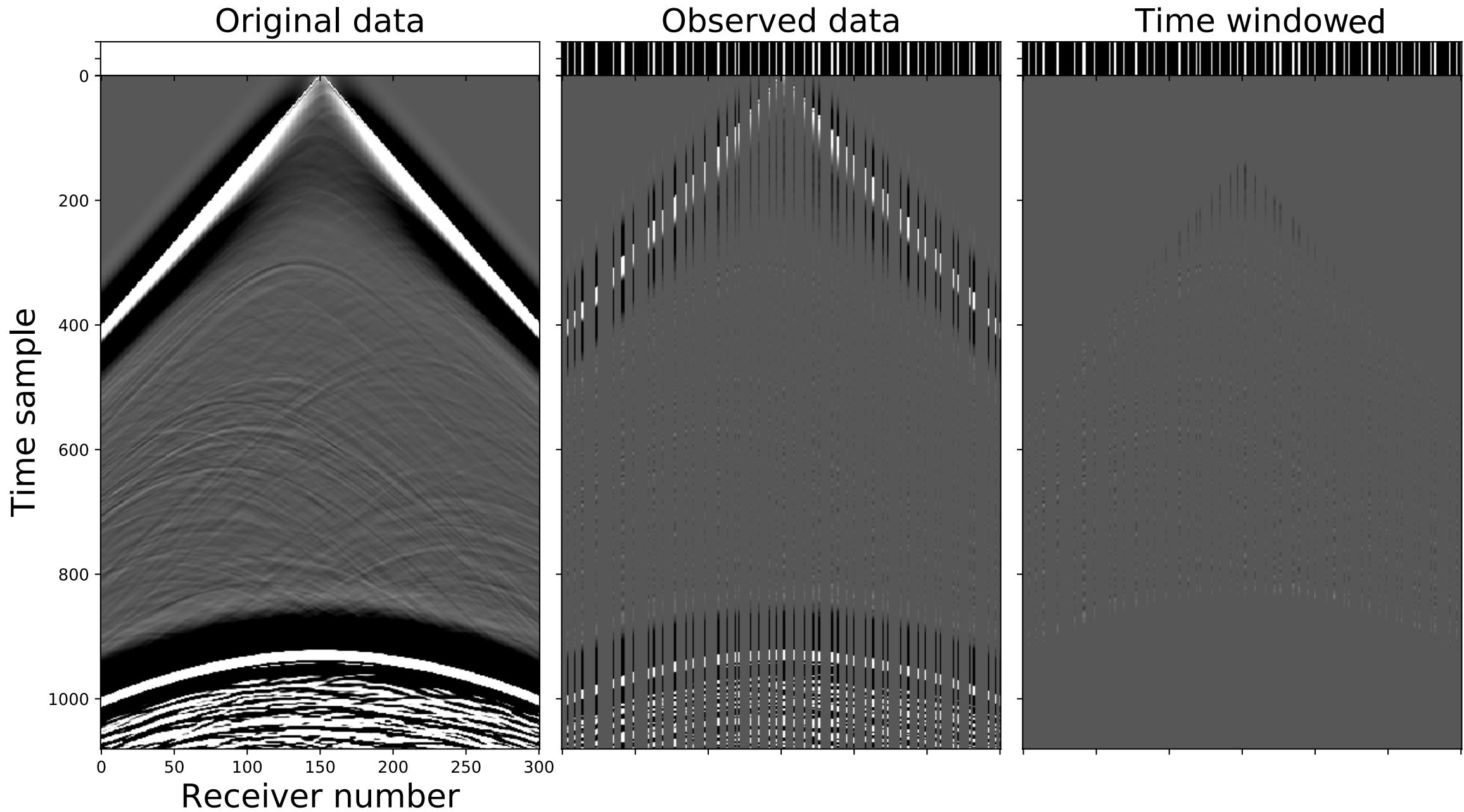


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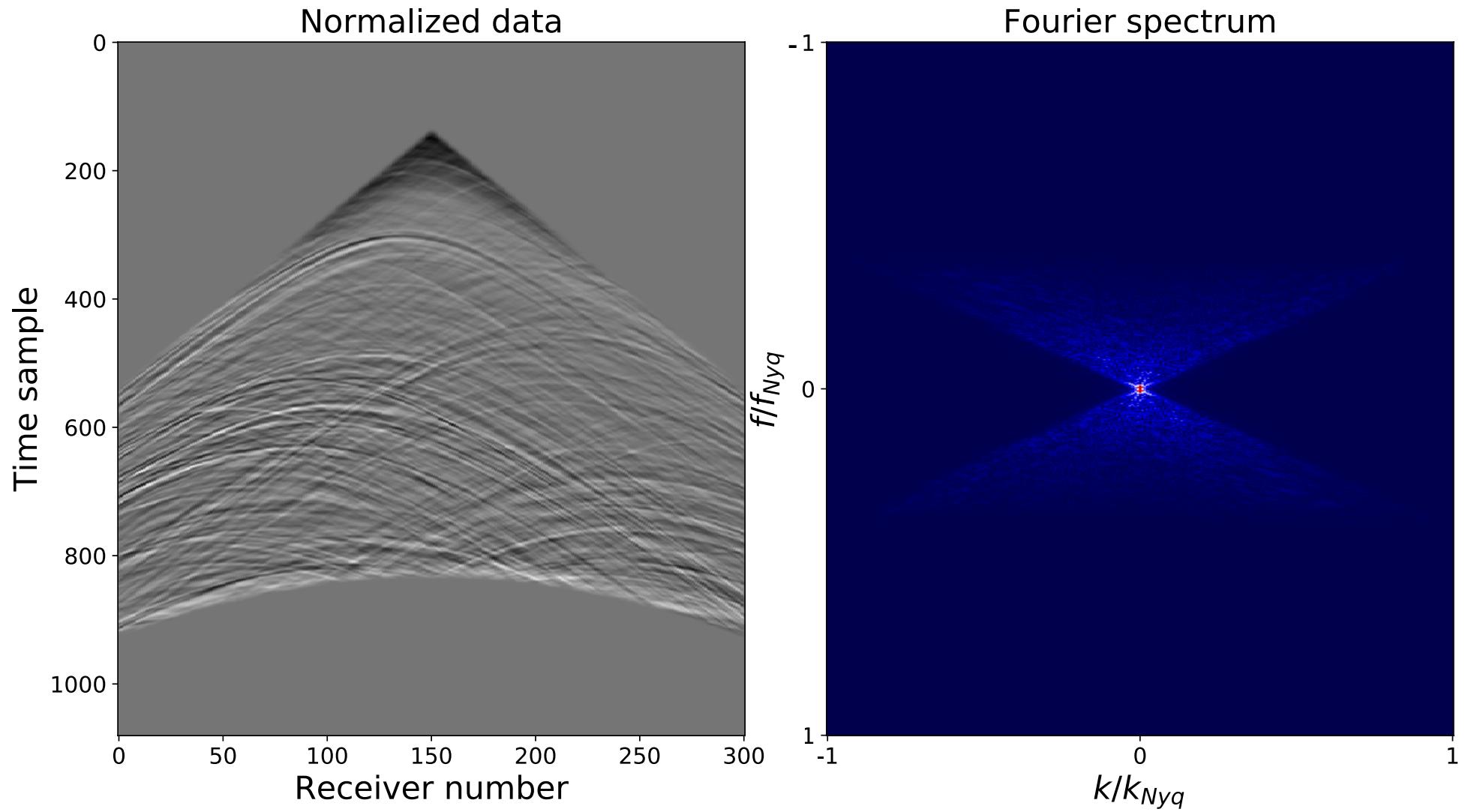
# Turbulence model



## Sampling—1/6 traces



# Normalized data and its wavenumber-frequency spectrum



# Preconditioning for ocean turbulence wavefield

Prior information:

$P_{xt}$ : space-time domain

$P_{k\omega}$ : Fourier domain

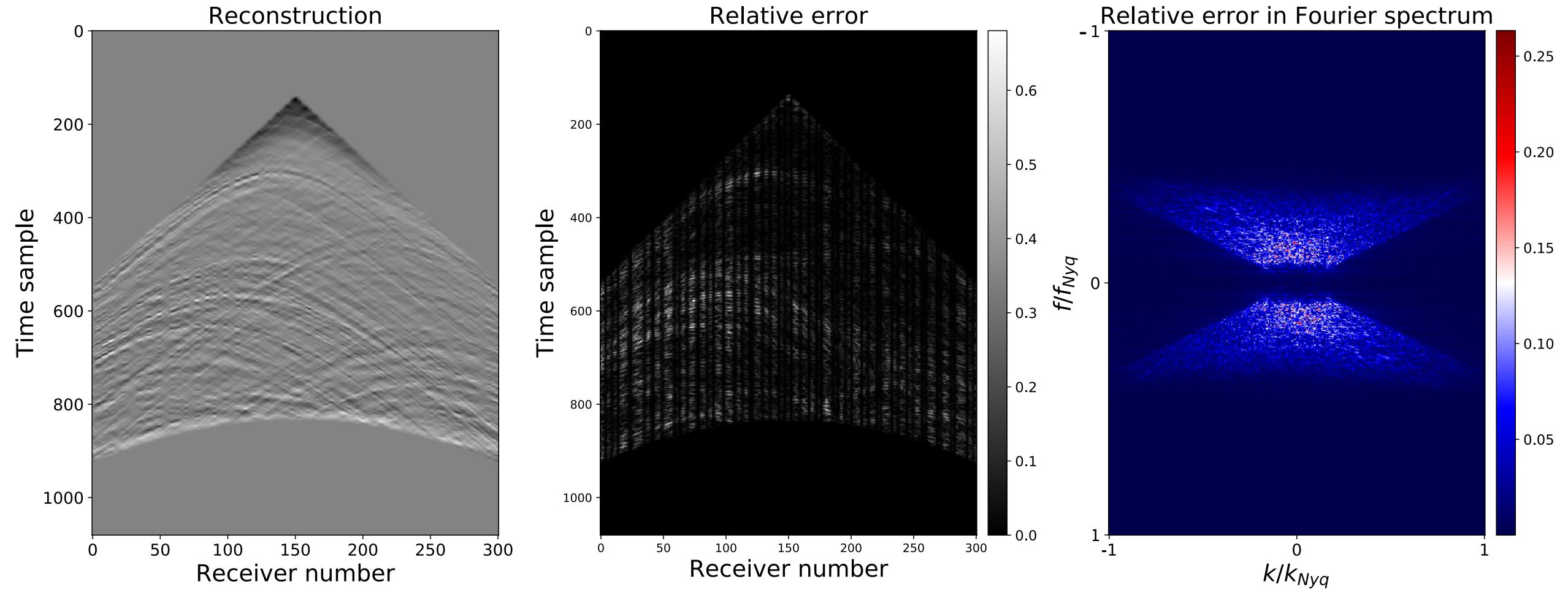
$$\underline{\underline{d_{mod} = F^{-1} d_f}}$$

$$\underline{\underline{d_{obs} = SF^{-1} d_f}}$$

$$d_{obs} = SP_{xt} F^{-1} P_{k\omega} \hat{d}_f$$

$$d_{mod}^P = P_{xt} F^{-1} P_{k\omega} \hat{d}_f$$

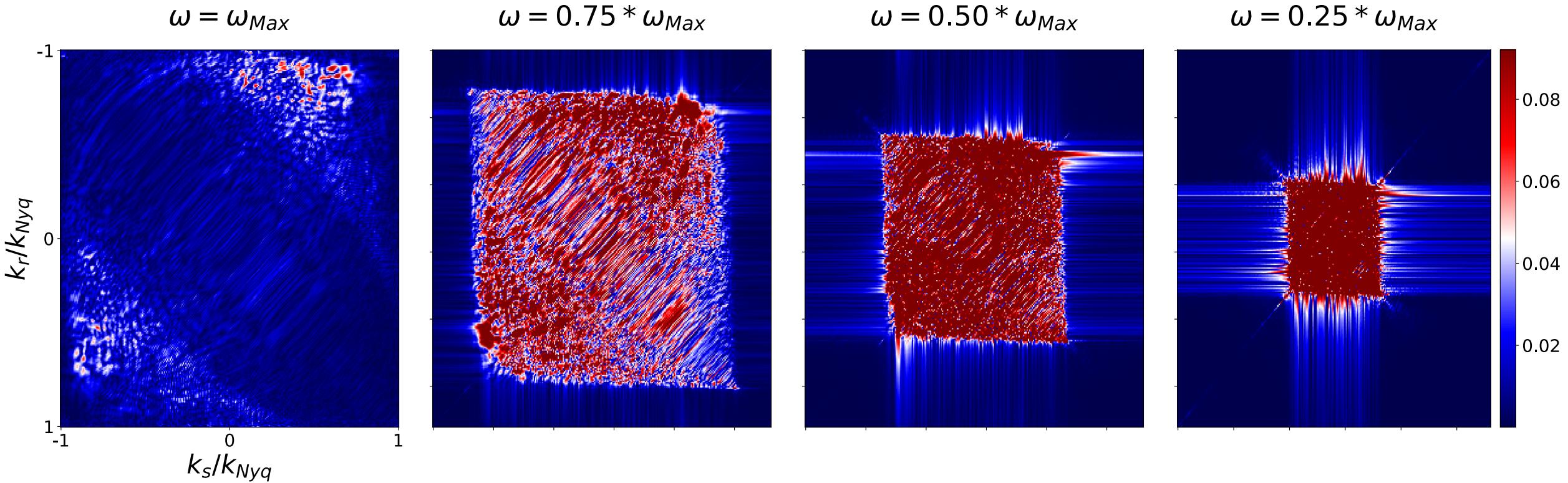
# Reconstruction



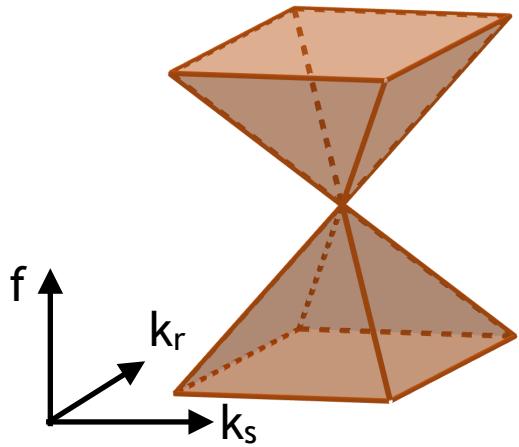
# 3D Reconstruction: multi-source, multi-receiver

281 shots & 281 receivers

Fourier Spectrum



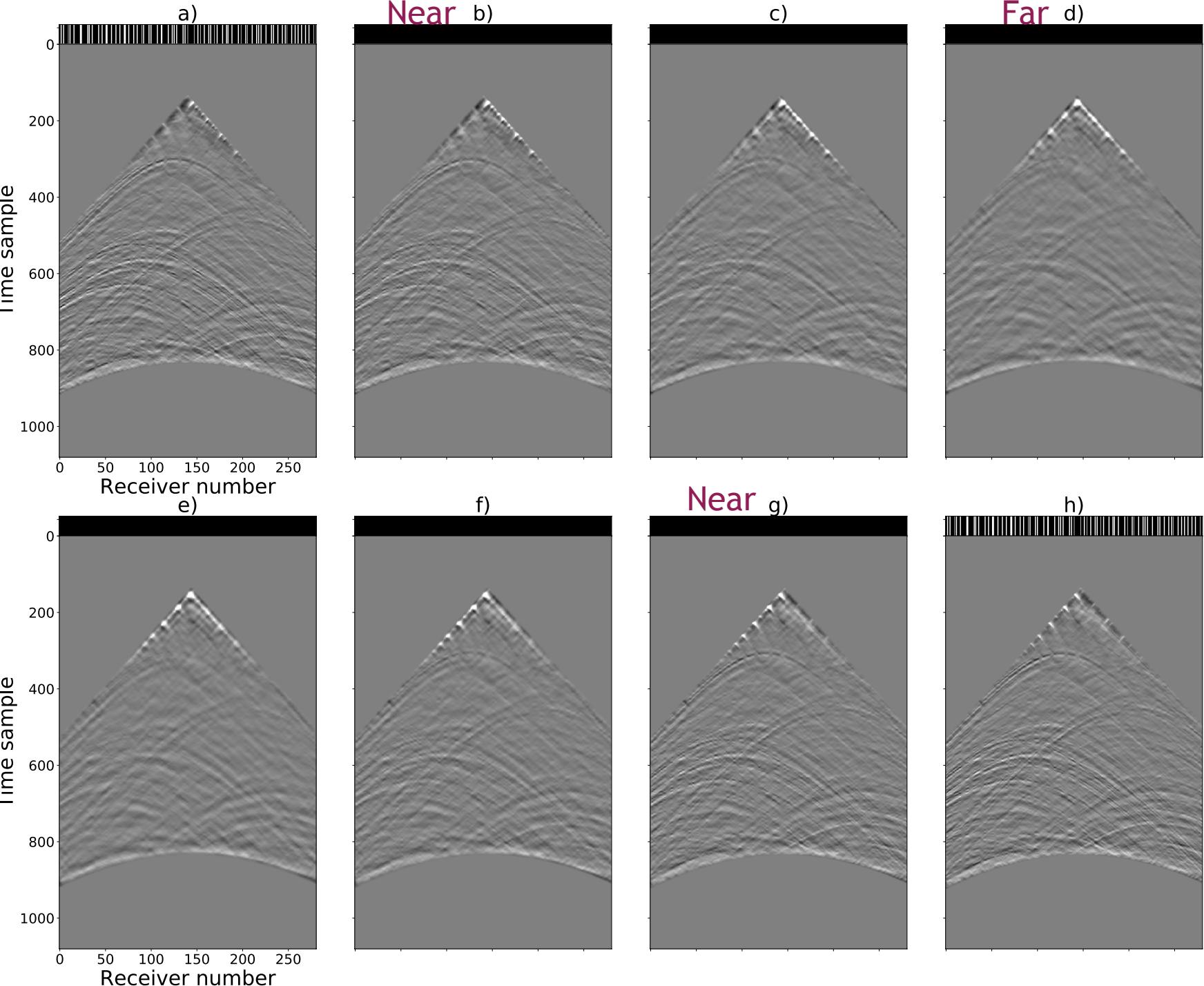
Preconditioner in Fourier domain



# 3D Reconstruction

Irregular sampling  
&  
1/4 decimation

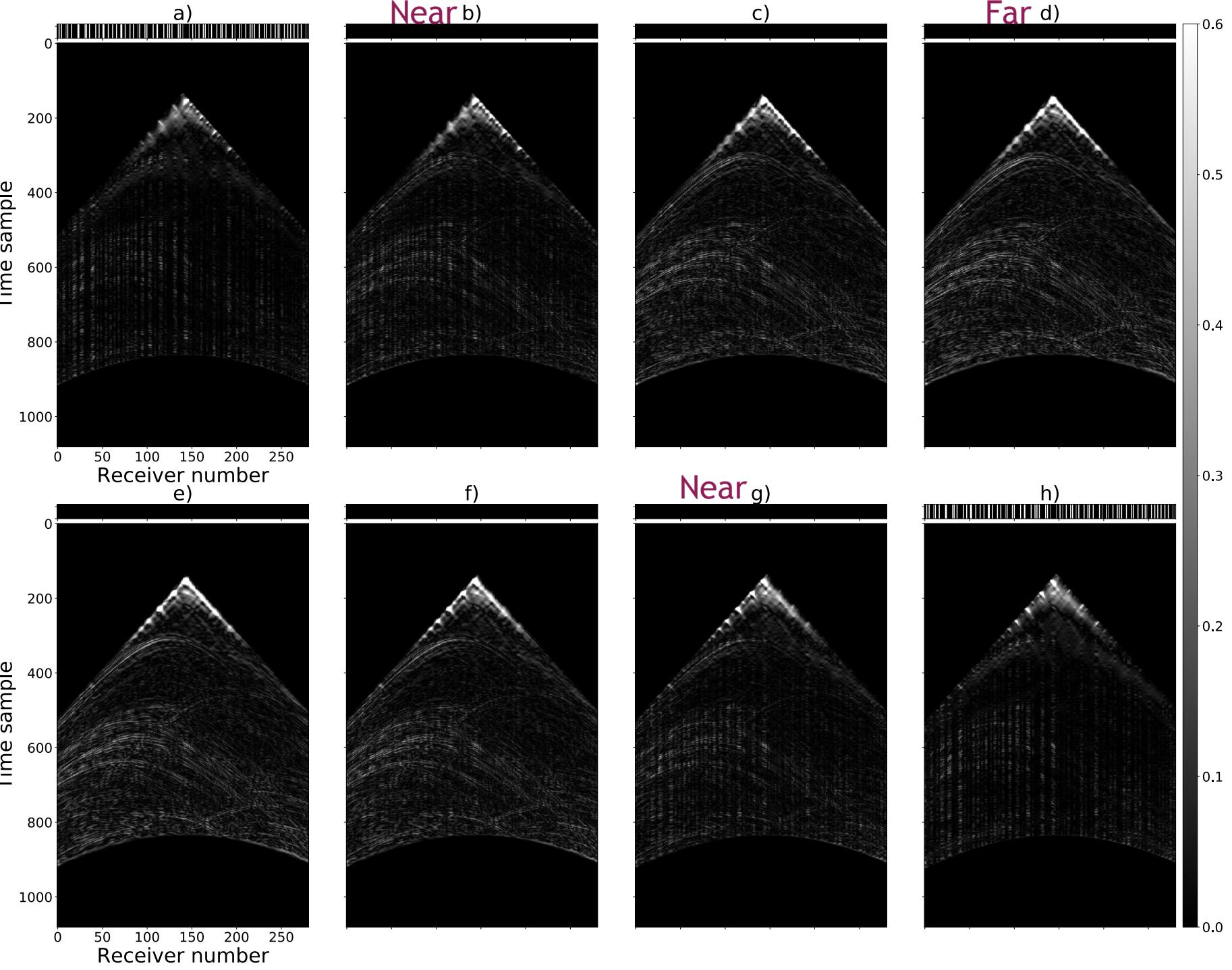
$$d_{obs} = \begin{pmatrix} d_t \\ d_{r1} \\ d_{r2} \\ d_{s1} \\ d_{s2} \\ d_{r1s1} \\ d_{r2s1} \\ d_{r1s2} \\ d_{r2s2} \end{pmatrix} \quad \text{and} \quad S = \begin{pmatrix} R_r \\ D_{r1} \\ D_{r1} \\ D_{s1} \\ D_{s2} \\ D_{r1s1} \\ D_{r2s1} \\ D_{r1s2} \\ D_{r2s2} \end{pmatrix}$$



# 3D Reconstruction

Irregular sampling  
&  
1/4 decimation

$$d_{obs} = \begin{pmatrix} d_t \\ d_{r1} \\ d_{r2} \\ d_{s1} \\ d_{s2} \\ d_{r1s1} \\ d_{r2s1} \\ d_{r1s2} \\ d_{r2s2} \end{pmatrix} \quad \text{and} \quad S = \begin{pmatrix} R_r \\ D_{r1} \\ D_{s1} \\ D_{s2} \\ D_{r1s1} \\ D_{r2s1} \\ D_{r1s2} \\ D_{r2s2} \end{pmatrix}$$





## Conclusion

- *Reconstruction*
  - derivatives
  - irregular sampling & preconditioning
- *Using data structure*
  - space-time domain
  - Fourier domain ...
- *Source and receiver reconstruction*
- *Promising for turbulence monitoring*

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