# 615 Midterm Project

Jingning Yang 10/17/2019

#### Read the "World Value" data

```
library(readxl)
data <- read_excel("/Users/jingningyang/Desktop/F00007693-WV6_Data_United_States_2011_Excel_v20180912.x</pre>
```

#### Clean Data

Delete columns which has replicated values (non-information):

After we delete non-information columns, based on different data structure, we only select totally has 4 options and sounds relative to each other: I pick V4-9, V60, V62, V64 from about 298 variables(survey questions).

Convert selected survey questions from character to numeric:

```
x <- c(1:8,57,59,61) #57,59,61,,99:104
newdata[x] <- apply(newdata[x],2,function(x) as.numeric(as.factor(x)))</pre>
```

#### Preparation for factor analysis

Calculate correlations between selected survey questions:

```
matrix <- cor(newdata[x])
head(round(matrix,2))</pre>
```

```
##
                                        V4: Important in life: Family
## V4: Important in life: Family
                                                                 0.38
## V5: Important in life: Friends
## V6: Important in life: Leisure time
                                                                 0.20
## V7: Important in life: Politics
                                                                 0.19
## V8: Important in life: Work
                                                                 0.19
## V9: Important in life: Religion
                                                                 0.32
                                        V5: Important in life: Friends
                                                                  0.38
## V4: Important in life: Family
## V5: Important in life: Friends
                                                                   1.00
## V6: Important in life: Leisure time
                                                                   0.33
## V7: Important in life: Politics
                                                                   0.21
## V8: Important in life: Work
                                                                   0.08
## V9: Important in life: Religion
                                                                   0.18
                                        V6: Important in life: Leisure time
## V4: Important in life: Family
                                                                        0.20
## V5: Important in life: Friends
                                                                        0.33
## V6: Important in life: Leisure time
                                                                        1.00
## V7: Important in life: Politics
                                                                        0.21
## V8: Important in life: Work
                                                                        0.18
## V9: Important in life: Religion
                                        V7: Important in life: Politics
## V4: Important in life: Family
                                                                   0.19
                                                                   0.21
## V5: Important in life: Friends
```

```
## V6: Important in life: Leisure time
                                                                   0.21
                                                                   1.00
## V7: Important in life: Politics
## V8: Important in life: Work
                                                                   0.19
## V9: Important in life: Religion
                                                                   0.19
                                        V8: Important in life: Work
## V4: Important in life: Family
                                                               0.19
## V5: Important in life: Friends
                                                               0.08
## V6: Important in life: Leisure time
                                                               0.18
## V7: Important in life: Politics
                                                               0.19
## V8: Important in life: Work
                                                               1.00
## V9: Important in life: Religion
                                                               0.16
                                        V9: Important in life: Religion
## V4: Important in life: Family
                                                                   0.32
## V5: Important in life: Friends
                                                                   0.18
## V6: Important in life: Leisure time
                                                                   0.05
## V7: Important in life: Politics
                                                                   0.19
## V8: Important in life: Work
                                                                   0.16
## V9: Important in life: Religion
                                                                   1.00
                                        V10: Feeling of happiness
## V4: Important in life: Family
## V5: Important in life: Friends
                                                             0.25
## V6: Important in life: Leisure time
                                                             0.21
## V7: Important in life: Politics
                                                             0.16
## V8: Important in life: Work
                                                             0.12
## V9: Important in life: Religion
                                                             0.18
                                        V11: State of health (subjective)
## V4: Important in life: Family
                                                                     -0.01
## V5: Important in life: Friends
                                                                      0.05
## V6: Important in life: Leisure time
                                                                      0.08
## V7: Important in life: Politics
                                                                      0.02
## V8: Important in life: Work
                                                                      0.09
## V9: Important in life: Religion
                                                                      0.01
                                        V60: Aims of country: first choice
## V4: Important in life: Family
                                                                      -0.13
## V5: Important in life: Friends
                                                                      -0.07
## V6: Important in life: Leisure time
                                                                      -0.06
## V7: Important in life: Politics
                                                                      -0.11
## V8: Important in life: Work
                                                                      -0.01
## V9: Important in life: Religion
                                                                      -0.07
##
                                        V62: Aims of respondent: first choice
## V4: Important in life: Family
                                                                         -0.05
## V5: Important in life: Friends
                                                                         -0.01
## V6: Important in life: Leisure time
                                                                         -0.10
## V7: Important in life: Politics
                                                                          0.09
## V8: Important in life: Work
                                                                         -0.03
## V9: Important in life: Religion
                                                                         -0.05
                                        V64: Most important: first choice
## V4: Important in life: Family
                                                                     -0.08
## V5: Important in life: Friends
                                                                    -0.09
## V6: Important in life: Leisure time
                                                                     -0.04
## V7: Important in life: Politics
                                                                    -0.04
## V8: Important in life: Work
                                                                     0.00
## V9: Important in life: Religion
                                                                    -0.02
```

```
library(psych)
cortest.bartlett(newdata[x])

## R was not square, finding R from data

## $chisq
## [1] 2272.999

##
## $p.value
## [1] 0

##
## $df
## [1] 55

det(matrix)
```

## [1] 0.3602762

From output data, Bartlett's test is highly significant, assymptotically chisquare is 2273, and P-value of chi square smaller than 0.001, therefore factor analysis is appropriate.

And since the determinant is 0.36 larger than 0.00001, so our determinant does not seem problematic.

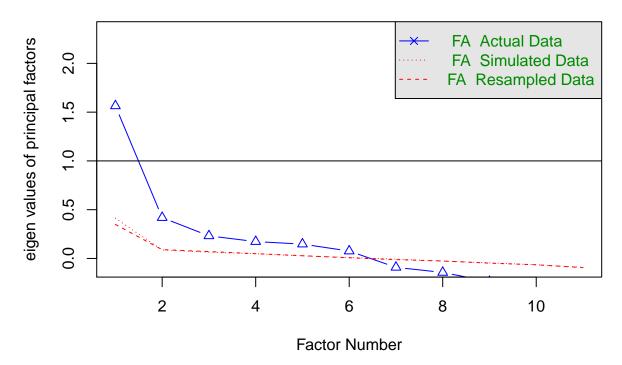
Since my goal is reduce number of variables (selected survey questions) in my data by extracting important one from the data, thus, I will using PCA to do factor extraction.

## Factor extraction by using PCA:

Show scree Plot by using parallel analysis:

```
pc <- principal(newdata[x], nfactors = 11, rotate="none")
#using a bigger device window explicitly showing the graph:
#dev.new(width=10, height=10)
parallel <- fa.parallel(newdata[x], fm='minres', fa='fa', main = "Scree Plot")</pre>
```

## **Scree Plot**

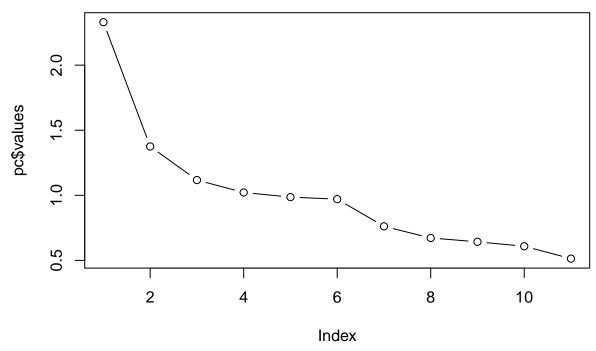


## Parallel analysis suggests that the number of factors = 6 and the number of components = NA
From the parallel analysis, the plot shows from 2 to 6 will be great choice.

scree plot by using another way:

```
plot(pc$values, type="b", main = "Scree Plot")
```

## **Scree Plot**



```
#x axis: component number
#y axis:eigenvalues of principal components and factor analysis
```

Since the elbow part is about the 3rd point from the left, so the evidence from the scree plot and from the eigenvalues suggests 3 component solution may be the best. Thus, combining 2 graphs, we choose 3 as our number of factors.

Redo PCA by using 3 factors

```
pc2 <- principal(newdata[x], nfactors = 3, rotate="none")
pc2</pre>
```

```
## Principal Components Analysis
## Call: principal(r = newdata[x], nfactors = 3, rotate = "none")
## Standardized loadings (pattern matrix) based upon correlation matrix
                                           PC1
                                                 PC2
                                                       PC3
##
                                                             h2
                                                                  u2 com
## V4: Important in life: Family
                                          0.68 - 0.06
                                                      0.24 0.53 0.47 1.3
## V5: Important in life: Friends
                                          0.64
                                               0.00 0.08 0.42 0.58 1.0
## V6: Important in life: Leisure time
                                          0.54
                                                0.03 -0.08 0.30 0.70 1.1
## V7: Important in life: Politics
                                          0.51
                                                0.08 0.19 0.30 0.70 1.3
## V8: Important in life: Work
                                          0.41
                                                0.17
                                                      0.13 0.21 0.79 1.5
## V9: Important in life: Religion
                                          0.49
                                                0.02
                                                      0.37 0.37 0.63 1.9
                                               0.29 -0.38 0.57 0.43 2.3
## V10: Feeling of happiness
                                          0.58
## V11: State of health (subjective)
                                          0.21
                                                0.36 -0.76 0.74 0.26 1.6
## V60: Aims of country: first choice
                                         -0.26
                                                0.67
                                                      0.22 0.57 0.43 1.5
## V62: Aims of respondent: first choice -0.08
                                                0.47 -0.01 0.23 0.77 1.1
                                         -0.20 0.67 0.31 0.58 0.42 1.6
## V64: Most important: first choice
##
##
                          PC1 PC2 PC3
## SS loadings
                         2.33 1.38 1.12
## Proportion Var
                         0.21 0.13 0.10
```

```
## Cumulative Var
                         0.21 0.34 0.44
## Proportion Explained 0.48 0.29 0.23
## Cumulative Proportion 0.48 0.77 1.00
##
## Mean item complexity = 1.5
## Test of the hypothesis that 3 components are sufficient.
## The root mean square of the residuals (RMSR) is 0.11
## with the empirical chi square 2848.59 with prob < 0
##
## Fit based upon off diagonal values = 0.51
Through output data, Cumulative var shows these 3 principle components explains 44% data with 11 variables.
#Difference between the reproduced cor matrix and the original cor matrix
residuals <- factor.residuals(matrix, pc2$loadings)
residuals <- as.matrix(residuals[upper.tri(residuals)])</pre>
large.resid <- abs(residuals) > 0.05
```

#### ## [1] 0.5818182

For easier to explain the output of factor extraction, we can using orthogonal rotation to decreasing noice for factors as much as possible.

Orthogonal rotation(varimaax):

#proportion of the large residuals

sum(large.resid) / nrow(residuals) #0.58

```
pc3 <- principal(newdata[x], nfactors = 3, rotate = "varimax")
print.psych(pc3, cut=0.3, sort = TRUE, main="table after orthogonal rotation")</pre>
```

```
## Principal Components Analysis
## Call: principal(r = newdata[x], nfactors = 3, rotate = "varimax")
## Standardized loadings (pattern matrix) based upon correlation matrix
                                         item
                                                RC1
                                                      RC2
                                                            RC3
                                                                  h2
                                                                       u2 com
## V4: Important in life: Family
                                            1 0.71
                                                                0.53 0.47 1.1
## V5: Important in life: Friends
                                            2 0.62
                                                                0.42 0.58 1.2
## V9: Important in life: Religion
                                            6 0.59
                                                                0.37 0.63 1.1
## V7: Important in life: Politics
                                            4 0.55
                                                                0.30 0.70 1.0
## V6: Important in life: Leisure time
                                            3 0.46
                                                                0.30 0.70 1.8
## V8: Important in life: Work
                                            5 0.44
                                                                0.21 0.79 1.2
## V64: Most important: first choice
                                                                0.58 0.42 1.0
                                           11
                                                     0.76
## V60: Aims of country: first choice
                                            9
                                                     0.75
                                                                0.57 0.43 1.0
## V62: Aims of respondent: first choice
                                           10
                                                     0.45
                                                                0.23 0.77 1.2
## V11: State of health (subjective)
                                                           0.86 0.74 0.26 1.0
                                            8
## V10: Feeling of happiness
                                            7 0.40
                                                           0.64 0.57 0.43 1.7
##
##
                          RC1 RC2 RC3
## SS loadings
                         2.12 1.40 1.30
## Proportion Var
                         0.19 0.13 0.12
## Cumulative Var
                         0.19 0.32 0.44
## Proportion Explained 0.44 0.29 0.27
## Cumulative Proportion 0.44 0.73 1.00
##
## Mean item complexity = 1.2
## Test of the hypothesis that 3 components are sufficient.
##
```

```
## The root mean square of the residuals (RMSR) is 0.11
## with the empirical chi square 2848.59 with prob < 0
## table after orthogonal rotation
## Fit based upon off diagonal values = 0.51</pre>
```

library(RColorBrewer)
fa.diagram(pc3,simple=TRUE)

#cut=0.3:only loading above 0.3, otherwise correlation is not high enough, so we consider excluding the

According to the results and the questionnaires, We can find the questions that load highly on factor 1 are V4("Important in life:Family") with the highest loading of 0.71, and lowest loading of 0.4 is V10(Feeling of happiness). Factor 2 are mianly explained by V64(Most important:first choice) and V60(Aim of country:first choice) with loading of 0.76 and 0.75. Factor 3 are mainly explained by V11(state of health) with 0.86 and the loweest loading of 0.64 is V10(Feeling of happiness).

Based on the obsersation, we can summarize the factor 1 as hapiness people consider a lot are important in life and label factor 2 as the expectation from people to country, factor 3 as causes of healthy people?

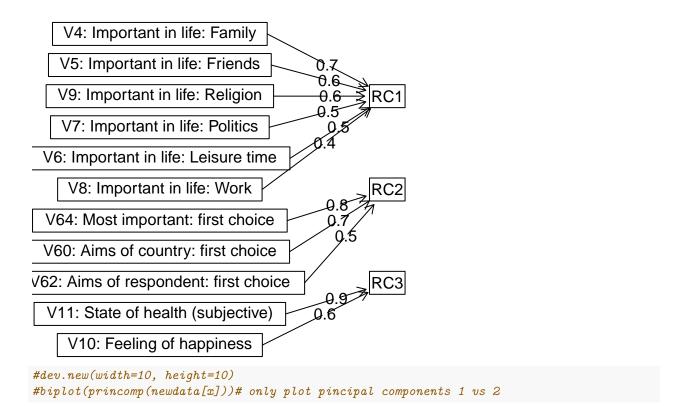
Since all facto1, factor2 and factor3's data are below 0.8 and over 0.3, which is encouraging.

```
library(gplots)

##
## Attaching package: 'gplots'
## The following object is masked from 'package:stats':
##
## lowess
library(ggplot2)

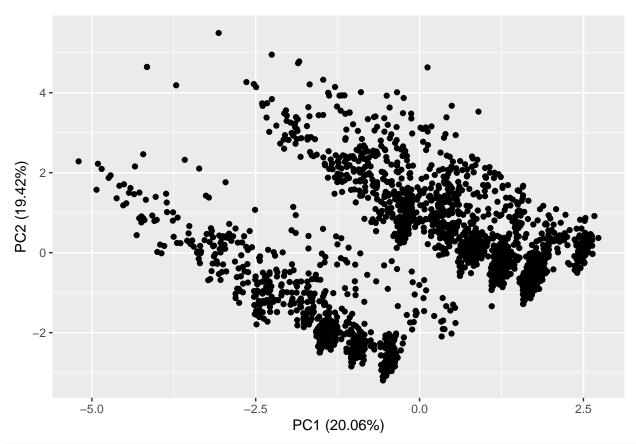
##
## Attaching package: 'ggplot2'
## The following objects are masked from 'package:psych':
##
## %+%, alpha
```

## **Components Analysis**

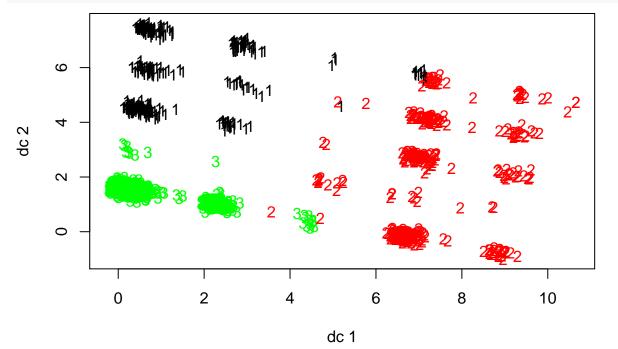


## Ploting PCA

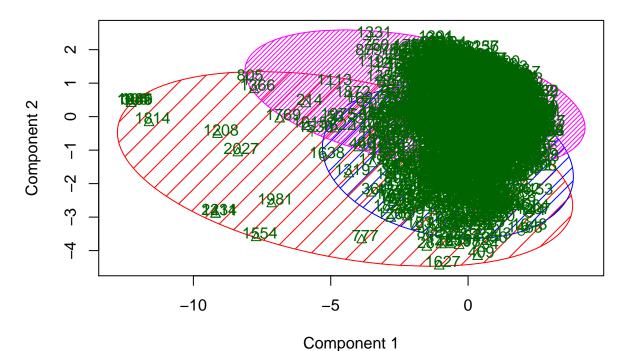
```
library(ggfortify)
autoplot(prcomp(newdata[x]), scale=0)
```



library(cluster)
library(fpc)
clus <- kmeans(newdata[x], centers = 3)
#dev.new(width=10, height=10)
plotcluster(newdata[x], clus\$cluster)</pre>



# CLUSPLOT( newdata[x] )



These two components explain 33.68 % of the point variability.