Analiza si vizualizarea datelor

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Self Organizing Map (SOM)

Outline

- Introduction and definitions of neural networks
- Introduction SOM
- Algorithm
- Example
- Conclusions

Neural networks

- A set of interconnected neurons/information processing units
- A technique designed to model how the brain performs a particular task
- Used to extract the pattern of information from data sets where numbers are vast and has hidden relations
- Ability to handle noisy data

Neural network learning

- By learning we can extract information
- This information is stored on the links between the neurons (also called weights)

Neural network

Weights

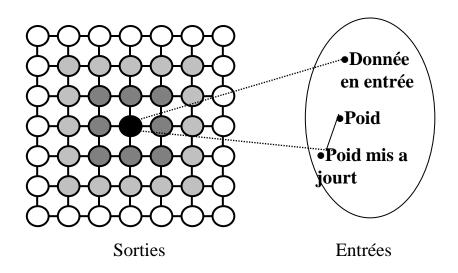
- Using neural networks can perform two types of learning:
- Supervised
- Unsupervised

Self-organisation

- The brain cells are self organizing themselves in groups, according to incoming information.
- This incoming information is not only received by a single neural cell, but also influences other cells in its neighbourhood.
- SOMs mechanism is also based on this principle

The principle of SOMs

- SOM produces the similarity graph of the input data
- Converts non-linear relationships between high dimensional data into simple geometric relationships



SOM

- Introduced in 1984 by Teuvo Kohonen
- Vector quantization + vector projection
- Technique based on unsupervised learning
- Used in classification and visualization of large data sets
- Used in many areas

Fields of application

Applications

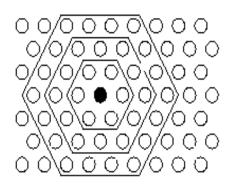
- Exploratory data analysis, clustering
- Quantification, variable selection, outlier detection
- Diagnosis, prediction, missing data

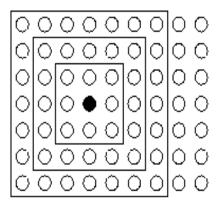
Domains

- Socio-economic
- TextMining
- Telecomunication
- Industrial Processes

SOM Architecture

- Set of neurons / cluster units
- Each neuron is assigned with a prototype vector that is taken from the input data set
- The neurons of the map can be arranged either on a rectangular or a hexagonal lattice





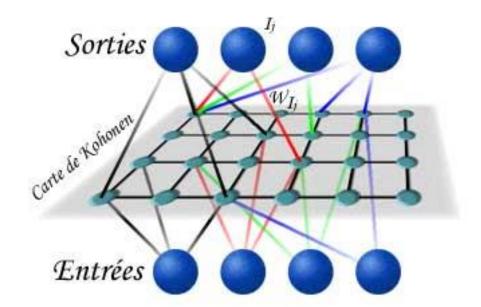
Hexagonal neighborhood

Rectangular neighborhood

SOM

• Cost function:

$$C(w) = \sum_{i} \sum_{k} h_{k,s(x_i)} ||x_i - w_k||^2$$



SOMs Algorithm

1. Initialisation step

- Define the topology map
- Randomly initialize all the prototypes for each neuron

2. Competition step

- Have a given datum x_i randomly chosen
- Determine the winning neuron according to the rule:

$$s(x_i) = A \operatorname{rgmin}_{1 \le k \le m} \|x_i - w_k\|^2$$

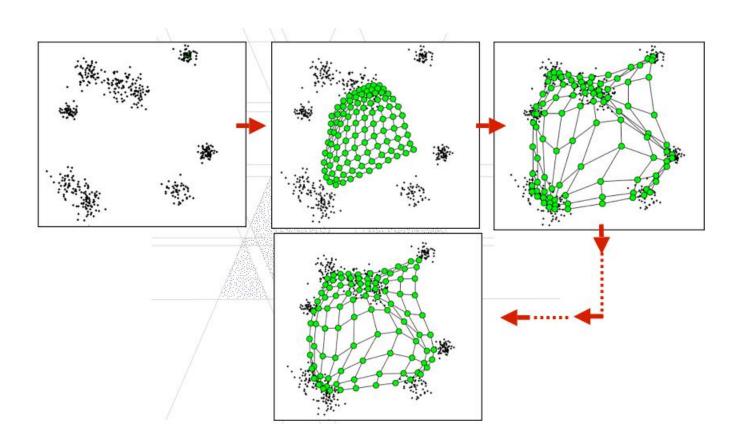
3. Adaptation step

Adapt prototypes under rule

$$W_k(t+1) = W_k(t) + \varepsilon(t)h_{k,s(x_i)}(x_i - W_k(t))$$

4. Repeat steps 2 and 3 until the updates prototypes are insignificant

Self organizing step



Self organizing step

The map is organized by checking the following properties:

Each neuron specializes in a portion of the input space

Similar data have near projections on the map

Data visualization using SOMs

- Visualization of clusters and shape of the data (projections, U-matrices and other distance matrices)
- Visualization of components/variables (scatter plots, components planes)
- Visualization of data projections

Example: Countries of the world

