Question 2 Find the smallest double precision number point number x > 16 (i.e., the next double precision number after 16), and the largest double precision number x < 16 (i.e., the previous double precision number before 16). In both cases, find all bits of x and the difference from 16, and compare the difference to the machine epsilon eps.

Question 3 Find the forward and backward error for the following functions, where the root is $\frac{1}{3}$, and the approximate root is $x_a = 0.3333$:

(a)
$$f(x) = 3x - 1$$

$$FE = |r - x_a| = 3.3333 \times 10^{-5}$$

$$BE = |3 \times 0.3333 - 1| = 1 \times 10^{-4}$$

(b)
$$f(x) = (3x - 1)^2$$

$$FE = |r - x_a| = 3.3333 \times 10^{-5}$$

$$BE = |(3 \times 0.3333 - 1)^2| = 1 \times 10^{-8}$$

(c)
$$f(x) = (3x - 1)^3$$

$$FE = |r - x_a| = 3.3333 \times 10^{-5}$$

$$BE = f(0.3333) = |(3 \times 0.3333 - 1)^{3}| = 1 \times 10^{-12}$$
(d) $f(x) = (3x - 1)^{\frac{1}{3}}$

$$FE = |r - x_{a}| = 3.3333 \times 10^{-5}$$

$$BE = f(0.3333) = |(3 \times 0.3333 - 1)^{\frac{1}{3}}| = -0.0464$$