# Exercise 1 Missing Data

number of students

[1] 340823

number of school

[1] 641

number of programs

[1] 33

number of choices

[1] 3086

number of missing test score

[1] 179887

students who apply to same school

[1] 120071

number of students who apply to less than 6 choices

[1] 18954

# Exercise 2 Data

|    | sp<br><chr></chr>      | schoolcode<br><int></int> | programcode<br><chr></chr> | sssdistrict<br><chr></chr> | ssslong<br><dbl></dbl> | ssslat<br><dbl></dbl> | cutoff<br><dbl></dbl> | quality<br><dbl></dbl> | size<br><int></int> |
|----|------------------------|---------------------------|----------------------------|----------------------------|------------------------|-----------------------|-----------------------|------------------------|---------------------|
| 1  | 100101                 | 100101                    |                            | Wa Municipal               | -2.28503               | 10.03062              | NA                    | NA                     | NA                  |
| 2  | 100101 General Arts    | 100101                    | General Arts               | Wa Municipal               | -2.28503               | 10.03062              | 198                   | 244.3924               | 79                  |
| 3  | 100101 Home Economics  | 100101                    | Home Economics             | Wa Municipal               | -2.28503               | 10.03062              | 199                   | 229.4500               | 40                  |
| 4  | 100101 Technical       | 100101                    | Technical                  | Wa Municipal               | -2.28503               | 10.03062              | 201                   | 235.1020               | 49                  |
| 5  | 100102 Agriculture     | 100102                    | Agriculture                | Wa Municipal               | -2.28503               | 10.03062              | 273                   | 292.5556               | 90                  |
| 6  | 100102 Business        | 100102                    | Business                   | Wa Municipal               | -2.28503               | 10.03062              | 283                   | 303.3444               | 90                  |
| 7  | 100102 General Arts    | 100102                    | General Arts               | Wa Municipal               | -2.28503               | 10.03062              | 291                   | 311.1111               | 90                  |
| 8  | 100102 General Science | 100102                    | General Science            | Wa Municipal               | -2.28503               | 10.03062              | 273                   | 298.4333               | 90                  |
| 9  | 100102 Home Economics  | 100102                    | Home Economics             | Wa Municipal               | -2.28503               | 10.03062              | 262                   | 278.8667               | 45                  |
| 10 | 100102 Visual Arts     | 100102                    | Visual Arts                | Wa Municipal               | -2.28503               | 10.03062              | 250                   | 275.2000               | 45                  |

|    | sp<br><chr></chr>      | schoolcode<br><int></int> | programcode<br><chr></chr> | sssdistrict<br><chr></chr> | ssslong<br><dbl></dbl> | ssslat<br><dbl></dbl> | cutoff<br><dbl></dbl> | quality<br><dbl></dbl> | size<br><int></int> |
|----|------------------------|---------------------------|----------------------------|----------------------------|------------------------|-----------------------|-----------------------|------------------------|---------------------|
| 11 | 100103 Agriculture     | 100103                    | Agriculture                | Wa Municipal               | -2.28503               | 10.03062              | NA                    | NA                     | NA                  |
| 12 | 100103 Business        | 100103                    | Business                   | Wa Municipal               | -2.28503               | 10.03062              | NA                    | NA                     | NA                  |
| 13 | 100103 General Arts    | 100103                    | General Arts               | Wa Municipal               | -2.28503               | 10.03062              | NA                    | NA                     | NA                  |
| 14 | 100104 Business        | 100104                    | Business                   | Wa Municipal               | -2.28503               | 10.03062              | NA                    | NA                     | NA                  |
| 15 | 100104 General Arts    | 100104                    | General Arts               | Wa Municipal               | -2.28503               | 10.03062              | 319                   | 337.4444               | 45                  |
| 16 | 100104 General Science | 100104                    | General Science            | Wa Municipal               | -2.28503               | 10.03062              | 313                   | 334.0000               | 45                  |
| 17 | 100104 Home Economics  | 100104                    | Home Economics             | Wa Municipal               | -2.28503               | 10.03062              | 282                   | 309.3556               | 45                  |
| 18 | 100105                 | 100105                    |                            | Wa Municipal               | -2.28503               | 10.03062              | NA                    | NA                     | NA                  |
| 19 | 100105 Business        | 100105                    | Business                   | Wa Municipal               | -2.28503               | 10.03062              | 251                   | 268.0125               | 80                  |
| 20 | 100105 General Arts    | 100105                    | General Arts               | Wa Municipal               | -2.28503               | 10.03062              | 258                   | 274.7375               | 80                  |

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# Exercise 3 Distance

|    | sssdis<br><fctr></fctr>  | jssdis<br><fctr></fctr> | distance<br><chr></chr> |
|----|--------------------------|-------------------------|-------------------------|
| 1  | Accra Metropolitan       | South Dayi (Kpeve)      | 59.9919865044814        |
| 2  | Ga West (Amasaman)       | South Dayi (Kpeve)      | 64.419456204133         |
| 3  | Tema                     | South Dayi (Kpeve)      | 50.6156936613713        |
| 4  | Dangme East (Ada)        | South Dayi (Kpeve)      | 32.6339719947566        |
| 5  | Dangme West (Dodowa)     | South Dayi (Kpeve)      | 45.8446614334538        |
| 6  | Ga East (Abokobi)        | South Dayi (Kpeve)      | 54.7920897810607        |
| 7  | New Juaben (Koforidua)   | South Dayi (Kpeve)      | 39.2072281117157        |
| 8  | Suhum/Kraboa/Coaltar     | South Dayi (Kpeve)      | 55.6049736817609        |
| 9  | Akwapim South (Nsawam)   | South Dayi (Kpeve)      | 50.1630800018662        |
| 10 | Akwapim North (Akropong) | South Dayi (Kpeve)      | 37.7225740726313        |

1-10 of 20 rows Previous 1 2 Next

|    | sssdis<br><fctr></fctr>   | jssdis<br><fctr></fctr> | distance<br><chr></chr> |
|----|---------------------------|-------------------------|-------------------------|
| 11 | West Akim (Asamankese)    | South Dayi (Kpeve)      | 67.519365351996         |
| 12 | Birim South (Akim Oda)    | South Dayi (Kpeve)      | 88.2993948724899        |
| 13 | Birim North ( New Abirem) | South Dayi (Kpeve)      | 85.1675633406139        |
| 14 | Asuogyaman (Senchi Ferry) | South Dayi (Kpeve)      | 15.2887554205168        |
| 15 | Kwahu North (Donkorkrom)  | South Dayi (Kpeve)      | 49.2951979936485        |
| 16 | Kwahu South (Mpraeso)     | South Dayi (Kpeve)      | 60.3593355374014        |
| 17 | Kwahu West (Nkawkaw)      | South Dayi (Kpeve)      | 70.1887923329991        |
| 18 | Kwaebibirem (Kade)        | South Dayi (Kpeve)      | 71.2056590422866        |
| 19 | Fanteakwa (Begoro)        | South Dayi (Kpeve)      | 38.9767192057032        |
| 20 | East Akim (Kibi)          | South Dayi (Kpeve)      | 47.5074867842705        |

11-20 of 20 rows Previous 1 2 Next

# Exercise 4 Descriptive Characteristics

```
> print(table1)
avg_cutoff sd_cutoff avg_quality sd_quality avg_distance sd_distance rank1 317.0717 52.01054 337.9208 46.83908 34.14635 47.71170
         317.0717 52.01054
299.6604 48.84759
                                   321.3895
                                                43.17346
                                                                32.92892
rank2
rank3
         287.1835 47.11865
                                   310.1029
                                                41.13584
                                                                30.67485
                                                                              43.79528
rank4
         273.9045 45.89648
                                   298.6397
                                                39.60251
                                                                26.48110
                                                                              41.63369
rank5
         256.5197
                    31.89327
                                   284.1636
                                                25.75738
                                                                30.26231
                                                                              28.38107
         251.4231 31.62788
                                                25.65834
rank6
                                   279.6407
                                                               30.84805
                                                                              28.37482
> table_25 = change_name(table_25)
> print(table_25)
      avg_cutoff sd_cutoff avg_quality sd_quality avg_distance sd_distance
                                 306.7529
                                              38.94246
        283.4534 44.59166
                                                                28.27913
         270.0009
                     41.40760
                                   294.3333
                                                35.90342
                                                                28.69947
rank2
                                                                              43.71274
rank3
         261.2568 40.43917
                                   286.6283
                                                34.93599
                                                                27.67535
                                                                              42.15750
                                                               25.34848
rank4
         251.4020 39.75034
                                   278.2927
                                                34.20236
                                                                              40.95437
         246.8855 31.22731
242.4731 30.73168
                                               25.74618
25.52473
                                                              29.32590
29.82050
rank5
                                   274.3982
                                                                              28.78110
                                   270.5157
rank6
                                                                              28 64225
> table_50 = change_name(table_50)
> print(table_50)
      avg_cutoff sd_cutoff avg_quality sd_quality avg_distance sd_distance
rank1
         301.0173 45.03198
                                   322.7784
                                                39.25254
                                                                31.69949
                                                                              48.20433
         285.1532 42.37029
                                   308.0621
                                                36.63525
                                                                31.22761
                                                                              46.57879
rank2
         273.9051 41.35209
262.0434 40.85982
rank3
                                   298.0751
                                                35.49417
                                                                29.81820
                                                                              45.01575
rank4
                                   288.0557
                                                34.66926
                                                                26.12894
                                                                              42.53877
         253.4241 31.44824
248.7229 31.12694
                                   280.8732
rank5
                                                25.36836
                                                                29.94637
                                                                              28.51642
                                               25.21741
rank6
                                   276.7619
                                                               30.73509
                                                                              28.56983
> table_75 = change_name(table_75)
> print(table_75)
      avg_cutoff sd_cutoff avg_quality sd_quality avg_distance sd_distance 323.0130 43.53460 342.9473 38.32348 34.86944 48.94770
rank1 323.0130 43.53460
rank2 304.1427 42.36073
                                                36.63066
                                   325.3159
                                                                33.46690
                                                                              46.83600
         290.5017 41.65390
276.2045 41.29130
rank3
                                   313.0342
                                                35.69395
                                                                31.35241
                                                                              44.98074
rank4
                                   300.7063
                                                34.98959
                                                                26.97811
                                                                              42.57398
rank5
         260.0547 31.18633
254.6174 31.21378
                                   287.4211
                                                24.47648
                                                                30.78063
                                                                              28.11440
                                                24.75947
rank6
                                   282.5944
                                                               31.30439
                                                                              28.20151
> table_100 = change_name(table_100)
      avg_cutoff sd_cutoff avg_quality sd_quality avg_distance sd_distance 362.1617 38.09107 380.4723 24 05746
> print(table_100)
                                  380.4723
rank1
rank2
         340.5253 38.24956
                                   358.9266
                                                33.94823
                                                                38.49917
                                                                              45.44718
         324.1210 39.78167
306.9100 41.69904
rank3
                                   343.6262
                                                34.51467
                                                                33.97069
                                                                              42.73751
                                                              27.51189
31.05815
31.59482
rank4
                                   328.3540
                                                35.64904
                                                                              40.39295
         266.4038 30.28669
260.5411 30.53754
rank5
                                   294.6718
                                               22.71537
23.10501
                                                22.71537
                                                                              28.04709
rank6
                                  289.3772
                                                                             28.02791
```

### Exercise 5 Data Creation

```
[1] 1.227407 2.244599 2.218549 2.246759 2.721831 2.280621 1.018992 1.465101 2.332168
[10] 2.028502 2.387183 2.089950 1.565467 2.846867 1.584632 2.674591 1.572447 1.533642
[19] 1.373446 1.464452
> X2[1:20]
 [1] 2.7310964 12.0238082 3.3911078 3.4090453 6.0187106 0.7536921 7.7037087
[8] 12.2640644 6.7635886 6.7426512 8.1600422 4.0815624 2.3634361 4.3802726 [15] 6.6004558 2.6077004 7.4811872 5.9427934 4.4314386 8.2670895
> X3[1:20]
 [1] 0 0 1 1 0 0 0 1 0 0 1 0 1 0 0 0 1 0 0 0
> e[1:20]
 [1] 2.3883829 4.4928205 3.6174976 1.3691200 3.6450301 1.9789293 1.0404695 3.9154502
 [9] 2.4766193 0.6540830 1.8954995 1.6514924 1.7552042 1.9645526 4.4308561 1.8464937
[17] 0.6312023 1.6108071 0.8735494 1.4582745
> Y[1:20]
 [1] 1.9032843 -3.1350882 3.8277599 1.5970899 1.9943875 4.5373519 -4.1700785
[8] -4.7640866 -0.3120093 -2.4801004 -1.9839194 0.9860258 2.1066723 1.9385475 [15] 0.8920039 3.2090729 -3.6149303 -1.3973371 -0.9666107 -3.7247639
> ydum[1:20]
 [1] 1 0 1 1 1 1 1 0 0 1 0 0 1 1 1 1 1 1 0 0 0 0
```

#### Exercise 6 OLS

The correlation between Y and X1 is 0.2094291, which is smaller than 1.2

Coefficients for each variable

- X1 1.1921859
- X2 -0.9046174
- X3 0.1099006

# Exercise 7 Discrete Choice

#### For probit

```
Call:
glm(formula = ydum ~ X1 + X2 + X3, family = binomial(link = "probit"))
Deviance Residuals:
Min 1Q Median 3Q Max
-3.5045 -0.1050 0.0063 0.2472 3.7964
                                        Max
Coefficients:
           Estimate Std. Error z value Pr(>|z|)
(Intercept) 2.96541 0.10011 29.621 <2e-16 ***
X1 1.23433 0.04459 27.684 <2e-16 ***
X1
           X2
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 13718.6 on 9999 degrees of freedom
Residual deviance: 4322.9 on 9996 degrees of freedom
AIC: 4330.9
Number of Fisher Scoring iterations: 8
```

The coefficient of X1 is 1.23, which is significant.

The coefficient of X2 is -0.91, which is significant.

The coefficient of X3 is 0.13, which is not significant.

- 1.23 means that one unit change in X1 will cause 1.23 unit change in ydum.
- -0.91 means that one unit change in X2 will cause -0.91 unit change in ydum.
- 0.13 means that one unit change in X3 will cause 0.13 unit change in ydum.

#### For linear

The coefficient of X1 is 0.14, which is significant.

The coefficient of X2 is -0.10, which is significant.

The coefficient of X3 is 0.01, which is not significant.

- 0.14 means that one unit change in X1 will cause 0.14 unit change in ydum.
- -0.10 means that one unit change in X2 will cause -0.10 unit change in ydum.
- 0.01 means that one unit change in X3 will cause 0.01 unit change in ydum.

```
For logit
```

The coefficient of X1 is 2.21, which is significant.

The coefficient of X2 is -1.65, which is significant.

The coefficient of X3 is 0.24, which is not significant.

- 2.21 means that one unit change in X1 will cause 2.21 unit change in ydum.
- -1.65 means that one unit change in X2 will cause -1.65 unit change in ydum.
- 0.24 means that one unit change in X3 will cause 0.24 unit change in ydum.

# Exercise 8 Marginal Effects

```
probitmfx(formula = ydum ~ X1 + X2 + X3, data = data, atmean = TRUE)
Marginal Effects:
dF/dx Std. Err. z P>|z|

X1 0.4924149 0.0177859 27.6857 < 2e-16 ***

X2 -0.3669907 0.0075174 -48.8187 < 2e-16 ***

X3 0.0539974 0.0186723 2.8918 0.00383 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
dF/dx is for discrete change for the following variables:
[1] "X3"
glm.fit: fitted probabilities numerically 0 or 1 occurredCall:
logitmfx(formula = ydum \sim X1 + X2 + X3, data = data, atmean = TRUE)
Marginal Effects:
         dF/dx Std. Err.
                                    Z
                                        P> | Z |
X1 0.5547272 0.0207585 26.723 < 2e-16 ***
X2 -0.4132169  0.0093871 -44.020 < 2e-16 ***
X3 0.0608904 0.0209894
                             2.901 0.00372 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
dF/dx is for discrete change for the following variables:
[1] "X3"
For probit
```

|    | marginal effect | standard error |
|----|-----------------|----------------|
| X1 | 0.4924149       | 0.0177859      |
| X2 | -0.3669907      | 0.0075174      |
| Х3 | 0.0539974       | 0.0186723      |

#### For logit

|    | marginal effect | standard error |
|----|-----------------|----------------|
| X1 | 0.5547272       | 0.0207585      |
| X2 | -0.4132169      | 0.0093871      |
| Х3 | 0.0608904       | 0.0209894      |