Description

Data from a conjoint experiment in which two partial profiles of credit cards were presented to 946 respondents. The variable bank\$choiceAtt\$choice indicates which profile was chosen. The profiles are coded as the difference in attribute levels. Thus, a "-1" means the profile coded as a choice of "0" has the attribute. A value of 0 means that the attribute was not present in the comparison.

data on age,income and gender (female=1) are also recorded in bank\$demo

Usage

data(bank)

Format

```
This R object is a list of two data frames, list(choiceAtt,demo).
List of 2
$ choiceAtt: 'data.frame': 14799 obs. of 16 variables:
\dots$ id: int [1:14799] 1 1 1 1 1 1 1 1 1 1
...$ choice: int [1:14799] 1 1 1 1 1 1 1 1 0 1
...$ Med_FInt : int [1:14799] 1 1 1 0 0 0 0 0 0 0
...$ Low_FInt : int [1:14799] 0 0 0 0 0 0 0 0 0 0
...$ Med_VInt: int [1:14799] 0 0 0 0 0 0 0 0 0 0
...$ Rewrd_2: int [1:14799] -1 1 0 0 0 0 0 1 -1 0
...$ Rewrd_3: int [1:14799] 0 -1 1 0 0 0 0 0 1 -1
...$ Rewrd_4: int [1:14799] 0 0 -1 0 0 0 0 0 0 1
...$ Med_Fee : int [1:14799] 0 0 0 1 1 -1 -1 0 0 0
...$ Low_Fee: int [1:14799] 0 0 0 0 0 1 1 0 0 0
...$ Bank_B: int [1:14799] 0 0 0 -1 1 -1 1 0 0 0
...$ Out_State: int [1:14799] 0 0 0 0 -1 0 -1 0 0 0
...$ Med_Rebate: int [1:14799] 0 0 0 0 0 0 0 0 0 0
...$ High_Rebate : int [1:14799] 0 0 0 0 0 0 0 0 0 0
...$ High_CredLine: int [1:14799] 0 0 0 0 0 0 0 -1 -1 -1
...$ Long_Grace: int [1:14799] 0 0 0 0 0 0 0 0 0 0
$ demo :'data.frame': 946 obs. of 4 variables:
...$ id: int [1:946] 1 2 3 4 6 7 8 9 10 11
\dots$ age: int [1:946] 60 40 75 40 30 30 50 50 50 40
...$ income: int [1:946] 20 40 30 40 30 60 50 100 50 40
...$ gender: int [1:946] 1 1 0 0 0 0 1 0 0 0
```

Details

Each respondent was presented with between 13 and 17 paired comparisons. Thus, this dataset has a panel structure.

Source

Allenby and Ginter (1995), "Using Extremes to Design Products and Segment Markets," *JMR*, 392-403.

References

Appendix A, Bayesian Statistics and Marketing by Allenby, McCulloch, and Rossi. http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

```
data(bank)
cat(" table of Binary Dep Var", fill=TRUE)
print(table(bank$choiceAtt[,2]))
cat(" table of Attribute Variables",fill=TRUE)
mat=apply(as.matrix(bank$choiceAtt[,3:16]),2,table)
print(mat)
cat(" means of Demographic Variables",fill=TRUE)
mat=apply(as.matrix(bank$demo[,2:3]),2,mean)
print(mat)
## example of processing for use with rhierBinLogit
if(nchar(Sys.getenv("LONG_TEST")) != 0)
choiceAtt=bank$choiceAtt
Z=bank$demo
## center demo data so that mean of random-effects
## distribution can be interpretted as the average respondents
Z[,1]=rep(1,nrow(Z))
Z[,2]=Z[,2]-mean(Z[,2])
Z[,3]=Z[,3]-mean(Z[,3])
Z[,4]=Z[,4]-mean(Z[,4])
Z=as.matrix(Z)
hh=levels(factor(choiceAtt$id))
nhh=length(hh)
lgtdata=NULL
for (i in 1:nhh) {
        y=choiceAtt[choiceAtt[,1]==hh[i],2]
        nobs=length(y)
        X=as.matrix(choiceAtt[choiceAtt[,1]==hh[i],c(3:16)])
        lgtdata[[i]]=list(y=y,X=X)
```

```
cat("Finished Reading data",fill=TRUE)
fsh()

Data=list(lgtdata=lgtdata,Z=Z)
Mcmc=list(R=10000,sbeta=0.2,keep=20)
set.seed(66)
out=rhierBinLogit(Data=Data,Mcmc=Mcmc)

cat(" Deltadraws ",fill=TRUE)
mat=apply(out$Deltadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
print(mat)
cat(" Vbetadraws ",fill=TRUE)
mat=apply(out$Vbetadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
print(mat)
}
```

breg

Posterior Draws from a Univariate Regression with Unit Error Variance

Description

breg makes one draw from the posterior of a univariate regression (scalar dependent variable) given the error variance = 1.0. A natural conjugate, normal prior is used.

Usage

```
breg(y, X, betabar, A)
```

Arguments

y vector of values of dep variable.
X n (length(y)) x k Design matrix.

betabar k x 1 vector. Prior mean of regression coefficients.

A Prior precision matrix.

Details

```
model: y = x'\beta + e. e \sim N(0, 1).
prior: \beta \sim N(betabar, A^{-1}).
```

Value

k x 1 vector containing a draw from the posterior distribution.

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

Examples

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=1000} else {R=10}
## simulate data
set.seed(66)
n=100
X=cbind(rep(1,n),runif(n)); beta=c(1,2)
y=X%*%beta+rnorm(n)
## set prior
A=diag(c(.05,.05)); betabar=c(0,0)
## make draws from posterior
betadraw=matrix(double(R*2),ncol=2)
for (rep in 1:R) {betadraw[rep,]=breg(y,X,betabar,A)}
##
## summarize draws
mat=apply(betadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(beta,mat); rownames(mat)[1]="beta"; print(mat)
```

cgetC

Obtain A List of Cut-offs for Scale Usage Problems

Description

cgetC obtains a list of censoring points, or cut-offs, used in the ordinal multivariate probit model of Rossi et al (2001). This approach uses a quadratic parameterization of the cut-offs. The model is useful for modeling correlated ordinal data on a scale from 1, ..., k with different scale usage patterns.

Usage

```
cgetC(e, k)
```

Arguments

e quadratic parameter (>0 and less than 1)

k items are on a scale from $1, \ldots, k$

Value

A vector of k+1 cut-offs.

Warning

This is a utility function which implements no error-checking.

Author(s)

Rob McCulloch and Peter Rossi, Graduate School of Business, University of Chicago. (Peter.Rossi@ChicagoGsb.edu).

References

Rossi et al (2001), "Overcoming Scale Usage Heterogeneity," JASA96, 20-31.

See Also

rscaleUsage

Examples

##

cgetC(.1,10)

cheese

Sliced Cheese Data

Description

Panel data with sales volume for a package of Borden Sliced Cheese as well as a measure of display activity and price. Weekly data aggregated to the "key" account or retailer/market level.

Usage

data(cheese)

Format

A data frame with 5555 observations on the following 4 variables.

```
RETAILER a list of 88 retailers

VOLUME unit sales

DISP a measure of display activity – per cent ACV on display

PRICE in $
```

Source

Boatwright et al (1999), "Account-Level Modeling for Trade Promotion," JASA 94, 1063-1073.

References

Chapter 3, Bayesian Statistics and Marketing by Rossi et al. http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

```
data(cheese)
cat(" Quantiles of the Variables ",fill=TRUE)
mat=apply(as.matrix(cheese[,2:4]),2,quantile)
print(mat)
##
## example of processing for use with rhierLinearModel
if(nchar(Sys.getenv("LONG_TEST")) != 0)
{
retailer=levels(cheese$RETAILER)
nreg=length(retailer)
nvar=3
regdata=NULL
for (reg in 1:nreg) {
        y=log(cheese$VOLUME[cheese$RETAILER==retailer[reg]])
        iota=c(rep(1,length(y)))
        X=cbind(iota,cheese$DISP[cheese$RETAILER==retailer[reg]],
                log(cheese$PRICE[cheese$RETAILER==retailer[reg]]))
        regdata[[reg]]=list(y=y,X=X)
}
Z=matrix(c(rep(1,nreg)),ncol=1)
nz=ncol(Z)
## run each individual regression and store results
lscoef=matrix(double(nreg*nvar),ncol=nvar)
for (reg in 1:nreg) {
        coef=lsfit(regdata[[reg]]$X,regdata[[reg]]$y,intercept=FALSE)$coef
        if (var(regdata[[reg]]$X[,2])==0) { lscoef[reg,1]=coef[1]; lscoef[reg,3]=coef[2]}
```

```
else {lscoef[reg,]=coef }
}
R=2000
Data=list(regdata=regdata,Z=Z)
Mcmc=list(R=R,keep=1)
betamean=array(double(nreg*nvar),dim=c(nreg,nvar))
burnin=100
set.seed(66)
out=rhierLinearModel(Data=Data,Mcmc=Mcmc)
for (k in 1:nvar) { betamean[,k]=apply(out$betadraw[,k,burnin:R],1,mean)}
print(betamean)
cat(" Deltadraws ",fill=TRUE)
mat=apply(out$Deltadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
print(mat)
cat(" Vbetadraws ",fill=TRUE)
mat=apply(out$Vbetadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
print(mat)
if(0){
coefn=c("Intercept", "Display", "LnPrice")
colors=c("blue","green","red","yellow")
par(mfrow=c(nvar,1),mar=c(5.1,15,4.1,13))
for (n in 1:nvar)
   plot(range(betamean[,n]),range(betamean[,n]),
     type="n",main=coefn[n],xlab="ls coef",ylab="post mean")
        points(lscoef[,n],betamean[,n],pch=17,col="blue",cex=1.2)
   abline(c(0,1))
}
}
}
```

condMom

Computes Conditional Mean/Var of One Element of MVN given All Others

Description

 ${\tt condMom}$ compute moments of conditional distribution of ith element of normal given all others.

Usage

```
condMom(x, mu, sigi, i)
```

Arguments

x vector of values to condition on - ith element not used

mu length(x) mean vector

sigi length(x)-dim covariance matrix

i conditional distribution of ith element

Details

```
x \sim MVN(mu, Sigma).
condMom computes moments of x_i given x_{-i}.
```

Value

a list containing:

cmean cond mean cvar cond variance

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

```
##
sig=matrix(c(1,.5,.5,.5,1,.5,.5,1),ncol=3)
sigi=chol2inv(chol(sig))
mu=c(1,2,3)
x=c(1,1,1)
condMom(x,mu,sigi,2)
```

$Create\ X$	Matrix	for l	Use	in	Multinomial	Logit	and	Probit	Rou-
tines									

Description

createX

createX makes up an X matrix in the form expected by Multinomial Logit (rmnlIndepMetrop and rhierMnlRwMixture) and Probit (rmnpGibbs and rmvpGibbs) routines. Requires an array of alternative specific variables and/or an array of "demographics" or variables constant across alternatives which may vary across choice occasions.

Usage

```
createX(p, na, nd, Xa, Xd, INT = TRUE, DIFF = FALSE, base = p)
```

Arguments

p	integer - number of choice alternatives				
na	integer - number of alternative-specific vars in Xa				
nd	integer - number of non-alternive specific vars				
Xa	n x p*na matrix of alternative-specific vars				
Xd	n x nd matrix of non-alternative specific vars				
INT	logical flag for inclusion of intercepts				
DIFF	logical flag for differencing wrt to base alternative				
base	integer - index of base choice alternative				
note: na.nd.Xa.Xd can be NULL to indicate lack of Xa or Xd variable					

Value

```
X matrix – n*(p-DIFF) x [(INT+nd)*(p-1) + na] matrix.
```

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

rmnlIndepMetrop, rmnpGibbs

Examples

```
na=2; nd=1; p=3
vec=c(1,1.5,.5,2,3,1,3,4.5,1.5)
Xa=matrix(vec,byrow=TRUE,ncol=3)
Xa=cbind(Xa,-Xa)
Xd=matrix(c(-1,-2,-3),ncol=1)
createX(p=p,na=na,nd=nd,Xa=Xa,Xd=Xd)
createX(p=p,na=na,nd=nd,Xa=Xa,Xd=Xd,base=1)
createX(p=p,na=na,nd=nd,Xa=Xa,Xd=Xd,DIFF=TRUE)
createX(p=p,na=na,nd=nd,Xa=Xa,Xd=Xd,DIFF=TRUE,base=2)
createX(p=p,na=na,nd=NULL,Xa=Xa,Xd=NULL)
createX(p=p,na=NULL,nd=nd,Xa=NULL,Xd=Xd)
```

customerSat

Customer Satisfaction Data

Description

Responses to a satisfaction survey for a Yellow Pages advertising product. All responses are on a 10 point scale from 1 to 10 (10 is "Excellent" and 1 is "Poor")

Usage

data(customerSat)

Format

A data frame with 1811 observations on the following 10 variables.

- q1 Overall Satisfaction
- q2 Setting Competitive Prices
- q3 Holding Price Increase to a Minimum
- q4 Appropriate Pricing given Volume
- q5 Demonstrating Effectiveness of Purchase
- ${\tt q6}$ Reach a Large # of Customers
- q7 Reach of Advertising
- q8 Long-term Exposure
- q9 Distribution
- q10 Distribution to Right Geographic Areas

Source

Rossi et al (2001), "Overcoming Scale Usage Heterogeneity," JASA 96, 20-31.

References

```
Case Study 3, Bayesian Statistics and Marketing by Rossi et al. http://gsbww.uchicago.edu/fac/peter.rossi/research/bsm.html
```

Examples

```
data(customerSat)
apply(as.matrix(customerSat),2,table)
```

detailing

Physician Detailing Data from Manchanda et al (2004)

Description

Monthly data on detailing (sales calls) on 1000 physicians. 23 mos of data for each Physician. Includes physician covariates. Dependent Variable (scripts) is the number of new prescriptions ordered by the physician for the drug detailed.

Usage

```
data(detailing)
```

Format

```
This R object is a list of two data frames, list(counts,demo). List of 2:
```

LIST OF Z:

\$ counts: 'data.frame': 23000 obs. of 4 variables:

```
\dots$ id: int [1:23000] 1 1 1 1 1 1 1 1 1 1
```

- $\dots \$$ scripts : int [1:23000] 3 12 3 6 5 2 5 1 5 3
- ...\$ detailing: int [1:23000] 1 1 1 2 1 0 2 2 1 1
- ...\$ lagged_scripts: int [1:23000] 4 3 12 3 6 5 2 5 1 5

\$ demo :'data.frame': 1000 obs. of 4 variables:

- ...\$ id: int [1:1000] 1 2 3 4 5 6 7 8 9 10
- ...\$ generalphys: int [1:1000] 1 0 1 1 0 1 1 1 1 1
- ...\$ specialist: int [1:1000] 0 1 0 0 1 0 0 0 0
- ...\$ mean_samples: num [1:1000] $0.722\ 0.491\ 0.339\ 3.196\ 0.348$

Details

generalphys is dummy for if doctor is a "general practitioner," specialist is dummy for if the physician is a specialist in the theraputic class for which the drug is intended, mean_samples is the mean number of free drug samples given the doctor over the sample.

Source

Manchanda, P., P. K. Chintagunta and P. E. Rossi (2004), "Response Modeling with Non-Random Marketing Mix Variables," *Journal of Marketing Research* 41, 467-478.

```
data(detailing)
cat(" table of Counts Dep Var", fill=TRUE)
print(table(detailing$counts[,2]))
cat(" means of Demographic Variables",fill=TRUE)
mat=apply(as.matrix(detailing$demo[,2:4]),2,mean)
print(mat)
##
## example of processing for use with rhierNegbinRw
if(nchar(Sys.getenv("LONG_TEST")) != 0)
data(detailing)
counts = detailing$counts
Z = detailing$demo
# Construct the Z matrix
Z[,1] = 1
Z[,2]=Z[,2]-mean(Z[,2])
Z[,3]=Z[,3]-mean(Z[,3])
Z[,4]=Z[,4]-mean(Z[,4])
Z=as.matrix(Z)
id=levels(factor(counts$id))
nreg=length(id)
nobs = nrow(counts$id)
regdata=NULL
for (i in 1:nreg) {
    X = counts[counts[,1] == id[i],c(3:4)]
    X = cbind(rep(1,nrow(X)),X)
    y = counts[counts[,1] == id[i],2]
    X = as.matrix(X)
    regdata[[i]]=list(X=X, y=y)
nvar=ncol(X)
                        # Number of X variables
                        # Number of Z variables
nz=ncol(Z)
rm(detailing,counts)
cat("Finished Reading data",fill=TRUE)
fsh()
Data = list(regdata=regdata, Z=Z)
deltabar = matrix(rep(0,nvar*nz),nrow=nz)
Vdelta = 0.01 * diag(nz)
nu = nvar+3
V = 0.01*diag(nvar)
a = 0.5
b = 0.1
Prior = list(deltabar=deltabar, Vdelta=Vdelta, nu=nu, V=V, a=a, b=b)
R = 10000
```

```
keep = 1
s_beta=2.93/sqrt(nvar)
s_alpha=2.93
c=2
Mcmc = list(R=R, keep = keep, s_beta=s_beta, s_alpha=s_alpha, c=c)
out = rhierNegbinRw(Data, Prior, Mcmc)
# Unit level mean beta parameters
Mbeta = matrix(rep(0,nreg*nvar),nrow=nreg)
ndraws = length(out$alphadraw)
for (i in 1:nreg) { Mbeta[i,] = rowSums(out$Betadraw[i, , ])/ndraws }
cat(" Deltadraws ",fill=TRUE)
mat=apply(out$Deltadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
print(mat)
cat(" Vbetadraws ",fill=TRUE)
mat=apply(out$Vbetadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
print(mat)
cat(" alphadraws ",fill=TRUE)
mat=apply(matrix(out$alphadraw),2,quantile,probs=c(.01,.05,.5,.95,.99))
print(mat)
}
```

eMixMargDen

 $Compute\ Marginal\ Densities\ of\ A\ Normal\ Mixture\ Averaged\ over\\ MCMC\ Draws$

Description

eMixMargDen assumes that a multivariate mixture of normals has been fitted via MCMC (using rnmixGibbs). For each MCMC draw, the marginal densities for each component in the multivariate mixture are computed on a user-supplied grid and then averaged over draws.

Usage

```
eMixMargDen(grid, probdraw, compdraw)
```

Arguments

grid array of grid points, grid[,i] are ordinates for ith component

probdraw array - each row of which contains a draw of probabilities of mixture comp

compdraw list of lists of draws of mixture comp moments

Details

length(compdraw) is number of MCMC draws. compdraw[[i]] is a list draws of mu and inv Chol root for each of mixture components. compdraw[[i]][[j]] is jth component. compdraw[[i]][[j]]\$mu is mean vector; compdraw[[i]][[j]]\$rooti is the UL decomp of $Sigma^{-1}$.

Value

an array of the same dimension as grid with density values.

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type. To avoid errors, call with output from **rnmixGibbs**.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

rnmixGibbs

fsh

Flush Console Buffer

Description

Flush contents of console buffer. This function only has an effect on the Windows GUI.

Usage

fsh()

Value

No value is returned.

Author(s)

 $Peter Rossi, Graduate School of Business, University of Chicago, \\ \langle Peter.Rossi@ChicagoGsb.edu \rangle.$

Compute GHK approximation to Multivariate Normal Integrals

ghkvec

Description

ghkvec computes the GHK approximation to the integral of a multivariate normal density over a half plane defined by a set of truncation points.

Usage

```
ghkvec(L, trunpt, above, r)
```

Arguments

L lower triangular Cholesky root of Covariance matrix

trunpt vector of truncation points

above vector of indicators for truncation above (1) or below (0)

r number of draws to use in GHK

Value

approximation to integral

Note

ghkvec can accept a vector of truncations and compute more than one integral. That is, length(trunpt)/length(above) number of different integrals, each with the same Sigma and mean 0 but different truncation points. See example below for an example with two integrals at different truncation points.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 3.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

Examples

##

```
Sigma=matrix(c(1,.5,.5,1),ncol=2)
L=t(chol(Sigma))
trunpt=c(0,0,1,1)
above=c(1,1)
ghkvec(L,trunpt,above,100)
```

init.rmultiregfp

Initialize Variables for Multivariate Regression Draw

Description

init.rmultiregfp initializes variables which can be pre-computed for draws from the posterior of a multivariate regression model. init.rmultiregfp should be called prior to use of rmultiregfp

Usage

```
init.rmultiregfp(X, A, Bbar, nu, V)
```

Arguments

Χ Design matrix

Prior Precision matrix (m x k) Α Bbar Prior mean matrix (m x k)

degrees of freedom parmeter for Sigma prior nu

V location parameter for Sigma prior

Details

```
model: Y = XB + U. u_i \sim N(0, \Sigma). u_i is the ith row of U. Y is n x m. X is n x k. B is k
priors: vec(B) \sim N(vec(Bbar, \Sigma(x)A^{-1}))
\Sigma \sim IW(nu, V).
```

Value

A list containing . . .

Inverse of Cholesky Root of (X'X + A)IR

RA Cholesky root of A RA %*% Bbar RABbar

d.f. parm for IWishart prior nu

V location matrix for IWishart prior

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 2.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

```
rmultiregfp
```

llmnl

Evaluate Log Likelihood for Multinomial Logit Model

Description

11mml evaluates log-likelihood for the multinomial logit model.

Usage

```
llmnl(y, X, beta)
```

Arguments

```
y n x 1 vector of obs on y (1, ..., p)
```

X n*p x k Design matrix (use createX to make)

beta k x 1 coefficient vector

Details

```
Let mu_i = X_i\beta, then Pr(y_i = j) = exp(mu_{i,j})/\sum_k exp(mu_{i,k}). X_i is the submatrix of X corresponding to the ith observation. X has n*p rows. Use createX to create X.
```

Value

value of log-likelihood (sum of log prob of observed multinomial outcomes).

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

```
createX, rmnlIndepMetrop
```

Examples

```
##
## Not run: ll=llmnl(y,X,beta)
```

11mnp

Evaluate Log Likelihood for Multinomial Probit Model

Description

11mnp evaluates the log-likelihood for the multinomial probit model.

Usage

```
llmnp(X, y, beta, Sigma, r)
```

Arguments

X X is $n^*(p-1)$ x k array. X is from differenced system.

y y is vector of n indicators of multinomial response $(1, \ldots, p)$.

beta $k \times 1$ vector of coefficients

Sigma (p-1) x (p-1) Covariance matrix of errors

r number of draws used in GHK

Details

```
X is (p-1)*n \times k matrix. Use createX with DIFF=TRUE to create X.
```

Model for each obs: w = Xbeta + e. $e \sim N(0, Sigma)$. censoring mechanism:

```
if y = j(j < p), w_j > max(w_{-j}) and w_j > 0 if y = p, w < 0
```

To use GHK, we must transform so that these are rectangular regions e.g. if $y = 1, w_1 > 0$ and $w_1 - w_{-1} > 0$.

Define A_j such that if j=1,...,p-1, $A_jw=A_jmu+A_je>0$ is equivalent to y=j. Thus, if y=j, we have $A_je>-A_jmu$. Lower truncation is $-A_jmu$ and $cov=A_jSigmat(A_j)$. For $j=p,\ e<-mu$.

Value

value of log-likelihood (sum of log prob of observed multinomial outcomes).

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapters 2 and 4.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

```
createX, rmnpGibbs
```

Examples

```
##
## Not run: ll=llmnp(X,y,beta,Sigma,r)
```

llnhlogit

Evaluate Log Likelihood for non-homothetic Logit Model

Description

11mnp evaluates log-likelihood for the Non-homothetic Logit model.

Usage

```
llnhlogit(theta, choice, lnprices, Xexpend)
```

Arguments

theta parameter vector (see details section) choice $n \ x \ 1 \ vector \ of \ choice \ (1, \dots, p)$

lnprices n x p array of log-prices

Xexpend n x d array of vars predicting expenditure

Details

Non-homothetic logit model with: $ln(psi_i(U)) = alpha_i - e^{k_i}U$

Structure of theta vector

alpha: (p x 1) vector of utility intercepts.

k: (p x 1) vector of utility rotation parms.

gamma: $(k \times 1)$ – expenditure variable coefs.

tau: (1×1) – logit scale parameter.

Value

value of log-likelihood (sum of log prob of observed multinomial outcomes).

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see $Bayesian\ Statistics\ and\ Marketing\$ by Allenby, McCulloch, and Rossi, Chapter 4.

```
http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html
```

See Also

```
simnhlogit
```

Examples

```
##
```

Not run: ll=llnhlogit(theta,choice,lnprices,Xexpend)

Compute Log of Inverted Chi-Squared Density

lndIChisq

Description

lndIChisq computes the log of an Inverted Chi-Squared Density.

Usage

```
lndIChisq(nu, ssq, x)
```

Arguments

nu d.f. parameter ssq scale parameter

x ordinate for density evaluation

Details

```
Z = \nu * ssq/\chi^2_{\nu}, \ Z \sim Inverted Chi-Squared. IndIChisq computes the complete log-density, including normalizing constants.
```

Value

log density value

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 2.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

dchisq

Examples

```
##
```

lndIChisq(3,1,2)

Compute Log of Inverted Wishart Density

lndIWishart

Description

lndIWishart computes the log of an Inverted Wishart density.

Usage

```
lndIWishart(nu, S, IW)
```

Arguments

nu d.f. parameter S "location" parameter

IW ordinate for density evaluation

Details

```
Z = Wishart(nu, V^{-1})^{-1}, \ Z \sim \text{Inverted Wishart(nu,V)}.
IndIWishart computes the complete log-density, including normalizing constants.
```

Value

log density value

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 2.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

rwishart

```
##
IndIWishart(5,diag(3),(diag(3)+.5))
```

Description

lndMvn computes the log of a Multivariate Normal Density.

Usage

```
lndMvn(x, mu, rooti)
```

Arguments

x density ordinatemu mu vector

rooti inv of Cholesky root of Sigma

Details

 $z \sim N(mu, \Sigma)$ note: does not include full normalizing constant

Value

log density value

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 2.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

lndMvst

```
##
Sigma=matrix(c(1,.5,.5,1),ncol=2)
IndMvn(x=c(rep(0,2)),mu=c(rep(0,2)),rooti=backsolve(chol(Sigma),diag(2)))
```

Compute Log of Multivariate Student-t Density

lndMvst

Description

lndMvst computes the log of a Multivariate Student-t Density.

Usage

```
lndMvst(x, nu, mu, rooti)
```

Arguments

x density ordinatenu d.f. parametermu vector

rooti inv of Cholesky root of Sigma

Details

```
z \sim MVst(mu, nu, \Sigma) note: does not include full normalizing constant
```

Value

log density value

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 2.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

lndMvn

Examples

```
##
```

```
Sigma=matrix(c(1,.5,.5,1),ncol=2)
lndMvst(x=c(rep(0,2)),nu=4,mu=c(rep(0,2)),rooti=backsolve(chol(Sigma),diag(2)))
```

logMargDenNR

Compute Log Marginal Density Using Newton-Raftery Approx

Description

 ${\tt logMargDenNR}$ computes log marginal density using the Newton-Raftery approximation. Note: this approximation can be influenced by outliers in the vector of log-likelihoods. Use with ${\tt care}$.

Usage

logMargDenNR(11)

Arguments

11

vector of log-likelihoods evaluated at length(ll) MCMC draws

Value

approximation to log marginal density value.

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 6.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

Description

Panel data on purchases of margarine by 516 households. Demographic variables are included.

Usage

data(margarine)

Format

This is an R object that is a list of two data frames, list(choicePrice,demos)

List of 2

\$ choicePrice:'data.frame': 4470 obs. of 12 variables:

- ...\$ hhid: int [1:4470] 2100016 2100016 2100016 2100016
- ...\$ choice : num [1:4470] 1 1 1 1 1 4 1 1 4 1
- ...\$ PPk_Stk: num [1:4470] 0.66 0.63 0.29 0.62 0.5 0.58 0.29
- ...\$ PBB_Stk : num [1:4470] $0.67 \ 0.67 \ 0.5 \ 0.61 \ 0.58 \ 0.45 \ 0.51$
- ...\$ PFLStk : num [1:4470] 1.09 0.99 0.99 0.99 0.99 0.99 0.99
- ...\$ PHse_Stk: num [1:4470] 0.57 0.57 0.57 0.57 0.45 0.45 0.29
- ...\$ PGen_Stk: num [1:4470] 0.36 0.36 0.36 0.36 0.33 0.33 0.33
- ...\$ PImp_Stk: num [1:4470] 0.93 1.03 0.69 0.75 0.72 0.72 0.72
- ...\$ PSS_Tub: num [1:4470] $0.85 \ 0.85 \ 0.79 \ 0.85 \ 0.85 \ 0.85$
- ...\$ PPk_Tub: num [1:4470] 1.09 1.09 1.09 1.09 1.07 1.07 1.07
- ...\$ PFL_Tub: num [1:4470] 1.19 1.19 1.19 1.19 1.19 1.19
- ...\$ PHse_Tub: num [1:4470] 0.33 0.37 0.59 0.59 0.59 0.59 0.59

Pk is Parkay; BB is BlueBonnett, Fl is Fleischmanns, Hse is house, Gen is generic, Imp is Imperial, SS is Shed Spread. _Stk indicates stick, _Tub indicates Tub form.

\$ demos :'data.frame': 516 obs. of 8 variables:

- ...\$ hhid: num [1:516] 2100016 2100024 2100495 2100560
- ...\$ Income: num [1:516] 32.5 17.5 37.5 17.5 87.5 12.5
- ...\$ Fs3_4: int [1:516] 0 1 0 0 0 0 0 0 0 0
- \dots \$ Fs5: int [1:516] 0 0 0 0 0 0 0 0 1 0
- ...\$ Fam_Size : int [1:516] 2 3 2 1 1 2 2 2 5 2
- \dots \$ college: int [1:516] 1 1 0 0 1 0 1 0 1 1
- \dots \$ whtcollar: int [1:516] 0 1 0 1 1 0 0 0 1 1
- ...\$ retired : int [1:516] 1 1 1 0 0 1 0 1 0 0

Fs3_4 is dummy (family size 3-4). Fs5 is dummy for family size >= 5. college,whtcollar,retired are dummies reflecting these statuses.

Details

choice is a multinomial indicator of one of the 10 brands (in order listed under format). All prices are in \$.

Source

Allenby and Rossi (1991), "Quality Perceptions and Asymmetric Switching Between Brands," *Marketing Science* 10, 185-205.

References

Chapter 5, Bayesian Statistics and Marketing by Rossi et al. http://gsbww.uchicago.edu/fac/peter.rossi/research/bsm.html

```
data(margarine)
cat(" Table of Choice Variable ",fill=TRUE)
print(table(margarine$choicePrice[,2]))
cat(" Means of Prices",fill=TRUE)
mat=apply(as.matrix(margarine$choicePrice[,3:12]),2,mean)
print(mat)
cat(" Quantiles of Demographic Variables",fill=TRUE)
mat=apply(as.matrix(margarine$demos[,2:8]),2,quantile)
print(mat)
##
## example of processing for use with rhierMnlRwMixture
if(nchar(Sys.getenv("LONG_TEST")) != 0)
select= c(1:5,7) ## select brands
chPr=as.matrix(margarine$choicePrice)
## make sure to log prices
chPr=cbind(chPr[,1],chPr[,2],log(chPr[,2+select]))
demos=as.matrix(margarine$demos[,c(1,2,5)])
## remove obs for other alts
chPr=chPr[chPr[,2] <= 7,]
chPr=chPr[chPr[,2] != 6,]
## recode choice
chPr[chPr[,2] == 7,2]=6
hhidl=levels(as.factor(chPr[,1]))
lgtdata=NULL
nlgt=length(hhidl)
p=length(select) ## number of choice alts
for (i in 1:nlgt) {
   nobs=sum(chPr[,1]==hhidl[i])
   if(nobs >=5) {
```

```
data=chPr[chPr[,1]==hhidl[i],]
      y=data[,2]
      names(y)=NULL
      X=createX(p=p,na=1,Xa=data[,3:8],nd=NULL,Xd=NULL,INT=TRUE,base=1)
       lgtdata[[ind]]=list(y=y,X=X,hhid=hhidl[i]); ind=ind+1
}
nlgt=length(lgtdata)
## now extract demos corresponding to hhs in lgtdata
##
Z=NULL
nlgt=length(lgtdata)
for(i in 1:nlgt){
   Z=rbind(Z,demos[demos[,1]==lgtdata[[i]]$hhid,2:3])
}
##
## take log of income and family size and demean
##
Z=log(Z)
Z[,1]=Z[,1]-mean(Z[,1])
Z[,2]=Z[,2]-mean(Z[,2])
keep=5
R=20000
mcmc1=list(keep=keep,R=R)
out=rhierMnlRwMixture(Data=list(p=p,lgtdata=lgtdata,Z=Z),Prior=list(ncomp=1),Mcmc=mcmc1)
begin=100/keep; end=R/keep
cat(" Posterior Mean of Delta ",fill=TRUE)
mat=apply(out$Deltadraw[begin:end,],2,mean)
print(matrix(mat,ncol=6))
pmom=momMix(out$probdraw[begin:end,],out$compdraw[begin:end])
cat(" posterior expectation of mu",fill=TRUE)
print(pmom$mu)
cat(" posterior expectation of sd",fill=TRUE)
print(pmom$sd)
cat(" posterior expectation of correlations",fill=TRUE)
print(pmom$corr)
}
```

mixDen

Compute Marginal Density for Multivariate Normal Mixture

Description

mixDen computes the marginal density for each component of a normal mixture at each of the points on a user-specified grid.

Usage

```
mixDen(x, pvec, comps)
```

Arguments

x array - ith column gives grid points for ith variable

pvec vector of mixture component probabilites

comps list of lists of components for normal mixture

Details

length(comps) is the number of mixture components. comps[[j]] is a list of parameters of the jth component. comps[[j]]\$mu is mean vector; comps[[j]]\$rooti is the UL decomp of $Sigma^{-1}$.

Value

an array of the same dimension as grid with density values.

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 5.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

rnmixGibbs

mnlHess

Computes -Expected Hessian for Multinomial Logit

Description

mnlHess computes -Expected[Hessian] for Multinomial Logit Model

Usage

```
mnlHess(y, X, beta)
```

Arguments

y n x 1 vector of choices, $(1, \ldots, p)$

X n*p x k Design matrix
beta k x 1 vector of coefficients

Details

See llmnl for information on structure of X array. Use createX to make X.

Value

k x k matrix

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 3.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

```
llmnl, createX, rmnlIndepMetrop
```

```
##
## Not run: mnlHess(y,X,beta)
```

momMix Compute Posterior Expectation of Normal Mixture Model Moments

Description

momMix averages the moments of a normal mixture model over MCMC draws.

Usage

```
momMix(probdraw, compdraw)
```

Arguments

probdraw R x ncomp list of draws of mixture probs

compdraw list of length R of draws of mixture component moments

Details

R is the number of MCMC draws in argument list above.

ncomp is the number of mixture components fitted.

compdraw is a list of lists of lists with mixture components.

compdraw[[i]] is ith draw.

compdraw[[i]][[j]][[1]] is the mean parameter vector for the jth component, ith MCMC draw. compdraw[[i]][[j]][[2]] is the UL decomposition of $Sigma^{-1}$ for the jth component, ith MCMC draw.

Value

a list of the following items ...

mu Posterior Expectation of Mean

sigma Posterior Expecation of Covariance Matrix

sd Posterior Expectation of Vector of Standard Deviations

corr Posterior Expectation of Correlation Matrix

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 5.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

rmixGibbs

nmat

Convert Covariance Matrix to a Correlation Matrix

Description

nmat converts a covariance matrix (stored as a vector, col by col) to a correlation matrix (also stored as a vector).

Usage

nmat(vec)

Arguments

vec

k x k Cov matrix stored as a k*k x 1 vector (col by col)

Details

This routine is often used with apply to convert an R x (k*k) array of covariance MCMC draws to correlations. As in corrdraws=apply(vardraws,1,nmat)

Value

k*k x 1 vector with correlation matrix

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

 $Peter\ Rossi,\ Graduate\ School\ of\ Business,\ University\ of\ Chicago,\ \langle Peter.Rossi@ChicagoGsb.edu\rangle.$

Examples

```
##
set.seed(66)
X=matrix(rnorm(200,4),ncol=2)
Varmat=var(X)
nmat(as.vector(Varmat))
```

numEff

Compute Numerical Standard Error and Relative Numerical Efficiency

Description

numEff computes the numerical standard error for the mean of a vector of draws as well as the relative numerical efficiency (ratio of variance of mean of this time series process relative to iid sequence).

Usage

```
numEff(x, m = as.integer(min(length(x), (100/sqrt(5000)) * sqrt(length(x)))))
```

Arguments

x R x 1 vector of draws

m number of lags for autocorrelations

Details

default for number of lags is chosen so that if R = 5000, m = 100 and increases as the sqrt(R).

Value

stderr standard error of the mean of x

f variance ratio (relative numerical efficiency)

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 3.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

Examples

```
numEff(rnorm(1000),m=20)
numEff(rnorm(1000))
```

rbprobitGibbs

Gibbs Sampler (Albert and Chib) for Binary Probit

Description

rbprobitGibbs implements the Albert and Chib Gibbs Sampler for the binary probit model.

Usage

```
rbprobitGibbs(Data, Prior, Mcmc)
```

Arguments

Data list(X,y)

Prior list(betabar,A)Mcmc list(R,keep)

Details

Model: $z = X\beta + e$. $e \sim N(0, I)$. y=1, if z> 0.

Prior: $\beta \sim N(betabar, A^{-1})$.

List arguments contain

X Design Matrix

y n x 1 vector of observations, (0 or 1)

betabar k x 1 prior mean (def: 0)

A k x k prior precision matrix (def: .01I)

R number of MCMC draws

keep thinning parameter - keep every keepth draw (def: 1)

Value

betadraw R/keep x k array of betadraws

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 3.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

rmnpGibbs

Examples

```
## rbprobitGibbs example
\label{eq:condition} \mbox{if(nchar(Sys.getenv("LONG_TEST")) != 0) } \{\mbox{R=2000}\} \mbox{ else } \{\mbox{R=10}\}
set.seed(66)
simbprobit=
function(X,beta) {
## function to simulate from binary probit including x variable
y=ifelse((X%*%beta+rnorm(nrow(X)))<0,0,1)</pre>
list(X=X,y=y,beta=beta)
X=cbind(rep(1,nobs),runif(nobs),runif(nobs))
beta=c(0,1,-1)
nvar=ncol(X)
simout=simbprobit(X,beta)
Data=list(X=simout$X,y=simout$y)
Mcmc=list(R=R,keep=1)
out=rbprobitGibbs(Data=Data,Mcmc=Mcmc)
cat(" Betadraws ",fill=TRUE)
mat=apply(out$betadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(beta,mat); rownames(mat)[1]="beta"; print(mat)
```

rdirichlet

Draw From Dirichlet Distribution

Description

rdirichlet draws from Dirichlet

Usage

```
rdirichlet(alpha)
```

Arguments

```
alpha vector of Dirichlet parms (must be > 0)
```

Value

Vector of draws from Dirichlet

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

Examples

```
##
set.seed(66)
rdirichlet(c(rep(3,5)))
```

rhierBinLogit

MCMC Algorithm for Hierachical Binary Logit

Description

rhierBinLogit implements an MCMC algorithm for hierarchical binary logits with a normal heterogeneity distribution. This is a hybrid sampler with a RW Metropolis step for unit-level logit parameters.

rhierBinLogit is designed for use on choice-based conjoint data with partial profiles. The Design matrix is based on differences of characteristics between two alternatives. See Appendix A of *Bayesian Statistics and Marketing* for details.

Usage

```
rhierBinLogit(Data, Prior, Mcmc)
```

Arguments

Data list(lgtdata,Z) (note: Z is optional)

Prior list(Deltabar, ADelta, nu, V) (note: all are optional)

Mcmc list(sbeta, R, keep) (note: all but R are optional)

Details

```
Model:
```

 $y_{hi} = 1$ with $pr = exp(x'_{hi}beta_h)/(1 + exp(x'_{hi}beta_h)$. $beta_h$ is nvar x 1. $h=1,\ldots$, length(lgtdata) units or "respondents" for survey data.

 $beta_h = \text{ZDelta[h,]} + u_h.$

Note: here ZDelta refers to Z%*%Delta, ZDelta[h,] is hth row of this product.

Delta is an nz x nvar array.

 $u_h \sim N(0, V_{beta}).$

Priors:

 $delta = vec(Delta) \sim N(vec(Deltabar), V_{beta}(x)ADelta^{-1})$

 $V_{beta} \sim IW(nu, V)$

Lists contain:

lgtdata list of lists with each cross-section unit MNL data

lgtdata[[h]]\$y n_h vector of binary outcomes (0,1)

lgtdata[[h]] X n_h by nvar design matrix for hth unit

Deltabar nz x nvar matrix of prior means (def: 0)

ADelta prior prec matrix (def: .01I)

nu d.f. parm for IW prior on norm comp Sigma (def: nvar+3)

V pds location parm for IW prior on norm comp Sigma (def: nuI)

sbeta scaling parm for RW Metropolis (def: .2)

R number of MCMC draws

keep MCMC thinning parm: keep every keepth draw (def: 1)

Value

a list containing:

Deltadraw R/keep x nz*nvar matrix of draws of Delta
betadraw nlgt x nvar x R/keep array of draws of betas
Vbetadraw R/keep x nvar*nvar matrix of draws of Vbeta

11ike R/keep vector of log-like values

reject R/keep vector of reject rates over nlgt units

Note

Some experimentation with the Metropolis scaling paramter (sbeta) may be required.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 5.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

rhierMnlRwMixture

Examples

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=10000} else {R=10}
set.seed(66)
nvar=5
                                 ## number of coefficients
nlgt=1000
                                 ## number of cross-sectional units
nobs=10
                                 ## number of observations per unit
                                 ## number of regressors in mixing distribution
nz=2
## set hyper-parameters
       B=ZDelta + U
Z=matrix(c(rep(1,nlgt),runif(nlgt,min=-1,max=1)),nrow=nlgt,ncol=nz)
Delta=matrix(c(-2,-1,0,1,2,-1,1,-.5,.5,0),nrow=nz,ncol=nvar)
iota=matrix(1,nrow=nvar,ncol=1)
Vbeta=diag(nvar)+.5*iota%*%t(iota)
## simulate data
lgtdata=NULL
for (i in 1:nlgt)
{ beta=t(Delta)%*%Z[i,]+as.vector(t(chol(Vbeta))%*%rnorm(nvar))
 X=matrix(runif(nobs*nvar),nrow=nobs,ncol=nvar)
 prob=exp(X%*%beta)/(1+exp(X%*%beta))
  unif=runif(nobs,0,1)
 y=ifelse(unif<prob,1,0)
 lgtdata[[i]]=list(y=y,X=X,beta=beta)
}
Data=list(Dat=lgtdata,Demo=Z)
out=rhierBinLogit(Data=list(lgtdata=lgtdata,Z=Z),Mcmc=list(R=R))
cat(" Deltadraws ",fill=TRUE)
mat=apply(out$Deltadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(as.vector(Delta),mat); rownames(mat)[1]="delta"; print(mat)
cat(" Vbetadraws ",fill=TRUE)
mat=apply(out$Vbetadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
```

```
mat=rbind(as.vector(Vbeta),mat); rownames(mat)[1]="Vbeta"; print(mat)
if(0){
    td=as.vector(Delta)
    par(mfrow=c(2,2))
    matplot(out$Deltadraw[,(1:nvar)],type="l")
    abline(h=td[1:nvar],col=(1:nvar))
    matplot(out$Deltadraw[,((nvar+1):(2*nvar))],type="l")
    abline(h=td[(nvar+1):(2*nvar)],col=(1:nvar))
    matplot(out$Vbetadraw[,c(1,7,13,19,25)],type="l")
    abline(h=1.5)
    matplot(out$Vbetadraw[,-c(1,7,13,19,25)],type="l")
    abline(h=.5)
}
```

rhierLinearModel

Gibbs Sampler for Hierarchical Linear Model

Description

rhierLinearModel implements a Gibbs Sampler for hierarchical linear models.

Usage

```
rhierLinearModel(Data, Prior, Mcmc)
```

Arguments

Data list(regdata,Z) (Z optional).

Prior list(Deltabar, A, nu.e, ssq, nu, V) (optional).

Mcmc list(R,keep) (R required).

Details

```
Model: length(regdata) regression equations. y_i = X_i beta_i + e_i. e_i \sim N(0, tau_i). nvar X vars in each equation. Priors: tau_i \sim \text{nu.e*} ssq_i/\chi^2_{nu.e}. tau_i is the variance of e_i. beta_i \sim \text{N(ZDelta[i,]}, V_{beta}. Note: ZDelta is the matrix Z * Delta; [i,] refers to ith row of this product. vec(Delta) given V_{beta} \sim N(vec(Deltabar), V_{beta}(x)A^{-1}). V_{beta} \sim IW(nu, V). Delta, Deltabar are nz x nvar. A is nz x nz. V_{beta} is nvar x nvar. Note: if you don't have any z vars, set Z=iota (nreg x 1). List arguments contain:
```

```
regdata list of lists with X,y matrices for each of length(regdata) regressions regdata[[i]]$X X matrix for equation i regdata[[i]]$y y vector for equation i

Deltabar nz x nvar matrix of prior means (def: 0)

A nz x nz matrix for prior precision (def: .01I)

nu.e d.f. parm for regression error variance prior (def: 3)

ssq scale parm for regression error var prior (def: var(y_i))

nu d.f. parm for Vbeta prior (def: nvar+3)

V Scale location matrix for Vbeta prior (def: nu*I)

R number of MCMC draws

keep MCMC thinning parm: keep every keepth draw (def: 1)
```

a list containing

betadraw nreg x nvar x R/keep array of individual regression coef draws

taudraw R/keep x nreg array of error variance draws

R/keep x nz x nvar array of Deltadraws

R/keep x nvar*nvar array of Vbeta draws

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 3.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

Examples

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}

nreg=100; nobs=100; nvar=3
Vbeta=matrix(c(1,.5,0,.5,2,.7,0,.7,1),ncol=3)
Z=cbind(c(rep(1,nreg)),3*runif(nreg)); Z[,2]=Z[,2]-mean(Z[,2])
nz=ncol(Z)
Delta=matrix(c(1,-1,2,0,1,0),ncol=2)
Delta=t(Delta) # first row of Delta is means of betas
Beta=matrix(rnorm(nreg*nvar),nrow=nreg)%*%chol(Vbeta)+Z%*%Delta
tau=.1
iota=c(rep(1,nobs))
regdata=NULL
for (reg in 1:nreg) { X=cbind(iota,matrix(runif(nobs*(nvar-1)),ncol=(nvar-1)))
```

```
y=X%*%Beta[reg,]+sqrt(tau)*rnorm(nobs); regdata[[reg]]=list(y=y,X=X) }
nu.e=3
ssq=NULL
for(reg in 1:nreg) {ssq[reg]=var(regdata[[reg]]$y)}
V=nu*diag(c(rep(1,nvar)))
A=diag(c(rep(.01,nz)),ncol=nz)
Deltabar=matrix(c(rep(0,nz*nvar)),nrow=nz)
Data=list(regdata=regdata,Z=Z)
Prior=list(Deltabar=Deltabar, A=A, nu.e=nu.e, ssq=ssq, nu=nu, V=V)
Mcmc=list(R=R,keep=1)
out=rhierLinearModel(Data=Data,Mcmc=Mcmc)
cat(" Deltadraws ",fill=TRUE)
mat=apply(out$Deltadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(as.vector(Delta),mat); rownames(mat)[1]="delta"; print(mat)
cat(" Vbetadraws ",fill=TRUE)
mat=apply(out$Vbetadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(as.vector(Vbeta),mat); rownames(mat)[1]="Vbeta"; print(mat)
```

rhierMnlRwMixture

MCMC Algorithm for Hierarchical Multinomial Logit with Mixture of Normals Heterogeneity

Description

rhierMnlRwMixture is a MCMC algorithm for a hierarchical multinomial logit with a mixture of normals heterogeneity distribution. This is a hybrid Gibbs Sampler with a RW Metropolis step for the MNL coefficients for each panel unit.

Usage

```
rhierMnlRwMixture(Data, Prior, Mcmc)
```

Arguments

 ${\tt Data} \qquad \qquad {\tt list(p,lgtdata,Z)} \ (\ Z \ is \ optional)$

Prior list(deltabar,Ad,mubar,Amu,nu,V,ncomp) (all but ncomp are optional)

Mcmc list(s,c,R,keep) (R required)

Details

```
y_i \sim MNL(X_i, theta_i). i=1,..., length(lgtdata). theta<sub>i</sub> is nvar x 1.
             theta_i = \text{ZDelta[i,]} + u_i.
             Note: here ZDelta refers to Z%*%D, ZDelta[i,] is ith row of this product.
             Delta is an nz x nvar array.
             u_i \sim N(mu_{ind}, Sigma_{ind}). ind \sim multinomial(pvec).
             Priors:
             pvec \sim dirichlet (a)
             delta = vec(Delta) \sim N(deltabar, A_d^{-1})
             mu_j \sim N(mubar, Sigma_j(x)Amu^{-1})
             Sigma_i \sim IW(nu,V)
             Lists contain:
               p p is number of choice alternatives
        lgtdata list of lists with each cross-section unit MNL data
lgtdata[[i]] $\ n_i vector of multinomial outcomes (1, ..., m)
lgtdata[[i]] X n_i by nvar design matrix for ith unit
       deltabar nz*nvar vector of prior means (def: 0)
              Ad prior prec matrix for vec(D) (def: .01I)
           mubar nvar x 1 prior mean vector for normal comp mean (def: 0)
             Amu prior precision for normal comp mean (def: .01I)
              nu d.f. parm for IW prior on norm comp Sigma (def: nvar+3)
                V pds location parm for IW prior on norm comp Sigma (def: nuI)
           ncomp number of components used in normal mixture
                s scaling parm for RW Metropolis (def: 2.93/sqrt(nvar))
                c fraction likelihood weighting parm (def: 2)
                R number of MCMC draws
            keep MCMC thinning parm: keep every keepth draw (def: 1)
         Value
             a list containing:
             Deltadraw
                               R/keep x nz*nvar matrix of draws of Delta, first row is initial value
             betadraw
                               nlgt x nvar x R/keep array of draws of betas
                               R/keep x ncomp matrix of draws of probs of mixture components (pvec)
             probdraw
```

list of lists (length R/keep)

compdraw

Note

More on compdraw component of return value list:

```
compdraw[[i ]] the ith draw of components for mixtures compdraw[[i ][[j]]] ith draw of the jth normal mixture comp compdraw[[i ][[j]][[1]]] ith draw of jth normal mixture comp mean vector compdraw[[i ][[j]][[2]]] ith draw of jth normal mixture cov parm (rooti)
```

Note: Z does **not** include an intercept and is centered for ease of interpretation.

Be careful in assessing prior parameter, Amu. .01 is too small for many applications. See Allenby et al, chapter 5 for full discussion.

Large R values may be requires (>20,000).

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 5.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

rmnlIndepMetrop

Examples

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0)
set.seed(66)
p=3
                                    # num of choice alterns
ncoef=3
nlgt=300
                                    # num of cross sectional units
nz=2
Z=matrix(runif(nz*nlgt),ncol=nz)
Z=t(t(Z)-apply(Z,2,mean))
                                    # demean Z
ncomp=3
                                        # no of mixture components
Delta=matrix(c(1,0,1,0,1,2),ncol=2)
comps=NULL
comps[[1]]=list(mu=c(0,-1,-2),rooti=diag(rep(1,3)))
comps[[2]]=list(mu=c(0,-1,-2)*2,rooti=diag(rep(1,3)))
comps[[3]]=list(mu=c(0,-1,-2)*4,rooti=diag(rep(1,3)))
pvec=c(.4,.2,.4)
```

```
## simulate data
simlgtdata=NULL
ni=rep(50,300)
for (i in 1:nlgt)
{ betai=Delta%*%Z[i,]+as.vector(rmixture(1,pvec,comps)$x)
   X=NULL
   for(j in 1:ni[i])
      { Xone=cbind(rbind(c(rep(0,p-1)),diag(p-1)),runif(p,min=-1.5,max=0))
        X=rbind(X,Xone) }
   outa=simmnlwX(ni[i],X,betai)
   simlgtdata[[i]]=list(y=outa$y,X=X,beta=betai)
}
## plot betas
if(0){
## set if(1) above to produce plots
bmat=matrix(0,nlgt,ncoef)
for(i in 1:nlgt) {bmat[i,]=simlgtdata[[i]]$beta}
par(mfrow=c(ncoef,1))
for(i in 1:ncoef) hist(bmat[,i],breaks=30,col="magenta")
##
     set parms for priors and Z
nu=ncoef+3
V=nu*diag(rep(1,ncoef))
Ad=.01*(diag(rep(1,nz*ncoef)))
mubar=matrix(rep(0,ncoef),nrow=1)
deltabar=rep(0,ncoef*nz)
Amu=matrix(.01,ncol=1)
a=rep(5,ncoef)
R=10000
keep=5
c=2
s=2.93/sqrt(ncoef)
Data1=list(p=p,lgtdata=simlgtdata,Z=Z)
Prior1=list(ncomp=ncomp,nu=nu,V=V,Amu=Amu,mubar=mubar,a=a,Ad=Ad,deltabar=deltabar)
Mcmc1=list(s=s,c=c,R=R,keep=keep)
out=rhierMnlRwMixture(Data=Data1,Prior=Prior1,Mcmc=Mcmc1)
if(R < 1000) \{begin=1\} else \{begin=1000/keep\}
end=R/keep
cat(" Deltadraws ",fill=TRUE)
mat=apply(out$Deltadraw[begin:end,],2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(as.vector(Delta),mat); rownames(mat)[1]="delta"; print(mat)
tmom=momMix(matrix(pvec,nrow=1),list(comps))
pmom=momMix(out$probdraw[begin:end,],out$compdraw[begin:end])
mat=rbind(tmom$mu,pmom$mu)
rownames(mat)=c("true", "post expect")
cat(" mu and posterior expectation of mu",fill=TRUE)
print(mat)
```

```
mat=rbind(tmom$sd,pmom$sd)
rownames(mat)=c("true", "post expect")
cat(" std dev and posterior expectation of sd",fill=TRUE)
print(mat)
mat=rbind(as.vector(tmom$corr),as.vector(pmom$corr))
rownames(mat)=c("true","post expect")
cat(" corr and posterior expectation of corr",fill=TRUE)
print(t(mat))
if(0) {
## set if(1) to produce plots
par(mfrow=c(4,1))
plot(out$betadraw[1,1,])
abline(h=simlgtdata[[1]]$beta[1])
plot(out$betadraw[2,1,])
abline(h=simlgtdata[[2]]$beta[1])
plot(out$betadraw[100,3,])
abline(h=simlgtdata[[100]]$beta[3])
plot(out$betadraw[101,3,])
abline(h=simlgtdata[[101]]$beta[3])
par(mfrow=c(4,1))
plot(out$Deltadraw[,1])
abline(h=Delta[1,1])
plot(out$Deltadraw[,2])
abline(h=Delta[2,1])
plot(out$Deltadraw[,3])
abline(h=Delta[3,1])
plot(out$Deltadraw[,6])
abline(h=Delta[3,2])
begin=1000/keep
end=R/keep
ngrid=50
grid=matrix(0,ngrid,ncoef)
rgm=matrix(c(-3,-7,-10,3,1,0),ncol=2)
for(i in 1:ncoef) {rg=rgm[i,]; grid[,i]=rg[1] + ((1:ngrid)/ngrid)*(rg[2]-rg[1])}
mden=eMixMargDen(grid,out$probdraw[begin:end,],out$compdraw[begin:end])
par(mfrow=c(2,ncoef))
for(i in 1:ncoef)
{plot(grid[,i],mden[,i],type="l")}
for(i in 1:ncoef)
tden=mixDen(grid,pvec,comps)
for(i in 1:ncoef)
{plot(grid[,i],tden[,i],type="l")}
}
}
```

rhierNegbinRw

MCMC Algorithm for Negative Binomial Regression

Description

rhierNegbinRw implements an MCMC strategy for the hierarchical Negative Binomial (NBD) regression model. Metropolis steps for each unit level set of regression parameters are automatically tuned by optimization. Over-dispersion parameter (alpha) is common across units.

Usage

```
rhierNegbinRw(Data, Prior, Mcmc)
```

Arguments

Data list(regdata,Z)

Prior list(Deltabar, Adelta, nu, V, a, b)

Mcmc list(R,keep,s_beta,s_alpha,c,Vbeta0,Delta0)

Details

```
Model: y_i \sim \text{NBD}(\text{mean=lambda}, \text{over-dispersion=alpha}).
             lambda = exp(X_ibeta_i)
             Prior: beta_i \sim N(Delta'z_i, Vbeta).
             vec(Delta|Vbeta) \sim N(vec(Deltabar), Vbeta(x)Adelta).
             Vbeta \sim IW(nu, V).
             alpha \sim Gamma(a, b).
             note: prior mean of alpha = a/b, variance = a/(b^2)
            list arguments contain:
        regdata list of lists with data on each of nreg units
regdata[[i]]$X nobs_i x nvar matrix of X variables
regdata[[i]]$y nobs_i x 1 vector of count responses
               Z nreg x nz mat of unit chars (def: vector of ones)
       Deltabar nz x nvar prior mean matrix (def: 0)
          Adelta nz x nz pds prior prec matrix (def: .01I)
              nu d.f. parm for IWishart (def: nvar+3)
               V location matrix of IWishart prior (def: nuI)
               a Gamma prior parm (def: .5)
               b Gamma prior parm (def: .1)
               R number of MCMC draws
            keep MCMC thinning parm: keep every keepth draw (def: 1)
         s_beta scaling for beta alpha RW inc cov (def: 2.93/sqrt(nvar))
        s_alpha scaling for alpha | beta RW inc cov (def: 2.93)
               c fractional likelihood weighting parm (def:2)
         VbetaO starting value for Vbeta (def: I)
         DeltaO starting value for Delta (def: 0)
```

a list containing:

llike R/keep vector of values of log-likelihood betadraw $nreg \ x \ nvar \ x \ R/keep$ array of beta draws

alphadraw R/keep vector of alpha draws
acceptrbeta acceptance rate of the beta draws
acceptralpha acceptance rate of the alpha draws

Note

The NBD regression encompasses Poisson regression in the sense that as alpha goes to infinity the NBD distribution tends to the Poisson.

For "small" values of alpha, the dependent variable can be extremely variable so that a large number of observations may be required to obtain precise inferences.

For ease of interpretation, we recommend demeaning Z variables.

Author(s)

Sridhar Narayanam & Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 5.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

rnegbinRw

Examples

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0)
{
##
set.seed(66)
simnegbin =
function(X, beta, alpha) {
# Simulate from the Negative Binomial Regression
lambda = exp(X %*% beta)
y=NULL
for (j in 1:length(lambda))
    y = c(y,rnbinom(1,mu = lambda[j],size = alpha))
return(y)
}
nreg = 100  # Number of cross sectional units
```

```
# Number of observations per unit
T = 50
nobs = nreg*T
                  # Number of X variables
nvar=2
nz=2
                  # Number of Z variables
# Construct the Z matrix
Z = cbind(rep(1,nreg),rnorm(nreg,mean=1,sd=0.125))
Delta = cbind(c(0.4,0.2), c(0.1,0.05))
alpha = 5
Vbeta = rbind(c(0.1,0),c(0,0.1))
# Construct the regdata (containing X)
simnegbindata = NULL
for (i in 1:nreg) {
    betai = as.vector(Z[i,]%*%Delta) + chol(Vbeta)%*%rnorm(nvar)
    X = cbind(rep(1,T),rnorm(T,mean=2,sd=0.25))
    simnegbindata[[i]] = list(y=simnegbin(X,betai,alpha), X=X,beta=betai)
}
Beta = NULL
for (i in 1:nreg) {Beta=rbind(Beta,matrix(simnegbindata[[i]]$beta,nrow=1))}
Data = list(regdata=simnegbindata, Z=Z)
Deltabar = matrix(rep(0,nvar*nz),nrow=nz)
Vdelta = 0.01 * diag(nvar)
nu = nvar+3
V = 0.01*diag(nvar)
a = 0.5
b = 0.1
Prior = list(Deltabar=Deltabar, Vdelta=Vdelta, nu=nu, V=V, a=a, b=b)
R=10000
keep =1
s_beta=2.93/sqrt(nvar)
s_alpha=2.93
Mcmc = list(R=R, keep = keep, s_beta=s_beta, s_alpha=s_alpha, c=c)
out = rhierNegbinRw(Data, Prior, Mcmc)
# Unit level mean beta parameters
Mbeta = matrix(rep(0,nreg*nvar),nrow=nreg)
ndraws = length(out$alphadraw)
for (i in 1:nreg) { Mbeta[i,] = rowSums(out$Betadraw[i, , ])/ndraws }
cat(" Deltadraws ",fill=TRUE)
mat=apply(out$Deltadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(as.vector(Delta),mat); rownames(mat)[1]="Delta"; print(mat)
cat(" Vbetadraws ",fill=TRUE)
mat=apply(out$Vbetadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(as.vector(Vbeta),mat); rownames(mat)[1]="Vbeta"; print(mat)
cat(" alphadraws ",fill=TRUE)
mat=apply(matrix(out$alphadraw),2,quantile,probs=c(.01,.05,.5,.95,.99))
```

```
mat=rbind(as.vector(alpha),mat); rownames(mat)[1]="alpha"; print(mat)
}
```

rivGibbs

Gibbs Sampler for Linear "IV" Model

Description

rivGibbs is a Gibbs Sampler for a linear structural equation with an arbitrary number of instruments.

Usage

```
rivGibbs(Data, Prior, Mcmc)
```

Arguments

Data list(z,w,x,y)

Prior list(md,Ad,mbg,Abg,nu,V) (optional)

Mcmc list(R,keep) (R required)

Details

```
Model:
x = z' delta + e1.
 y = beta * x + w'gamma + e2.
 e1, e2 \sim N(0, Sigma).
 Priors:
 delta \sim N(md, Ad^{-1}). vec(beta, gamma) \sim N(mbg, Abg^{-1})
 Sigma \sim IW(nu,V)
 List arguments contain:
   z matrix of obs on instruments
   y vector of obs on lhs var in structural equation
   x "endogenous" var in structural eqn
   w matrix of obs on "exogenous" vars in the structural eqn
  md prior mean of delta (def: 0)
  Ad pds prior prec for prior on delta (def: .01I)
 mbg prior mean vector for prior on beta,gamma (def: 0)
 Abg pds prior prec for prior on beta,gamma (def: .01I)
  nu d.f. parm for IW prior on Sigma (def: 5)
   V pds location matrix for IW prior on Sigma (def: nuI)
   R number of MCMC draws
keep MCMC thinning parm: keep every keepth draw (def: 1)
```

```
a list containing:
```

deltadraw R/keep x dim(delta) array of delta draws

betadraw R/keep x 1 vector of beta draws

gammadraw R/keep x dim(gamma) array of gamma draws

Sigmadraw R/keep x 4 array of Sigma draws

Examples

```
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}
set.seed(66)
simIV = function(delta,beta,Sigma,n,z,w,gamma) {
eps = matrix(rnorm(2*n),ncol=2) %*% chol(Sigma)
x = z \%*\% delta + eps[,1]; y = beta*x + eps[,2] + w\%*%gamma
list(x=as.vector(x),y=as.vector(y)) }
n = 200; p=1 \# number of instruments
z = cbind(rep(1,n),matrix(runif(n*p),ncol=p))
w = matrix(1,n,1)
rho=.8
Sigma = matrix(c(1,rho,rho,1),ncol=2)
delta = c(1,4); beta = .5; gamma = c(1)
simiv = simIV(delta,beta,Sigma,n,z,w,gamma)
Mcmc=list(); Prior=list(); Data = list()
Data$z = z; Data$w=w; Data$x=simiv$x; Data$y=simiv$y
Mcmc\$R = R
Mcmc$keep=1
out=rivGibbs(Data=Data,Prior=Prior,Mcmc=Mcmc)
cat(" deltadraws ",fill=TRUE)
mat=apply(out$deltadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(delta,mat); rownames(mat)[1]="delta"; print(mat)
cat(" betadraws ",fill=TRUE)
qout=quantile(out$betadraw,probs=c(.01,.05,.5,.95,.99))
mat=matrix(qout,ncol=1)
mat=rbind(beta,mat); rownames(mat)=c("beta",names(qout)); print(mat)
cat(" Sigma draws",fill=TRUE)
mat=apply(out$Sigmadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(as.vector(Sigma),mat); rownames(mat)[1]="Sigma"; print(mat)
```

Gibbs Sampler for Normal Mixtures w/o Error Checking

50

rmixGibbs

Description

rmixGibbs makes one draw using the Gibbs Sampler for a mixture of multivariate normals.

Usage

```
rmixGibbs(y, Bbar, A, nu, V, a, p, z, comps)
```

Arguments

y data array - rows are obs

Bbar prior mean for mean vector of each norm comp

A prior precision parameter

nu prior d.f. parm

V prior location matrix for covariance priro

a Dirichlet prior parms

p prior prob of each mixture component

z component identities for each observation – "indicators"

comps list of components for the normal mixture

Details

rmixGibbs is not designed to be called directly. Instead, use rnmixGibbs wrapper function.

Value

a list containing:

p draw mixture probilities

z draw of indicators of each component

comps new draw of normal component parameters

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Rob McCulloch and Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 5.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

rnmixGibbs

rmixture

Draw from Mixture of Normals

Description

rmixture simulates iid draws from a Multivariate Mixture of Normals

Usage

```
rmixture(n, pvec, comps)
```

Arguments

n number of observations

pvec ncomp x 1 vector of prior probabilities for each mixture component

comps list of mixture component parameters

Details

comps is a list of length, ncomp = $\operatorname{length}(\operatorname{pvec})$. $\operatorname{comps}[[j]][[1]]$ is mean vector for the jth component. $\operatorname{comps}[[j]][[2]]$ is the inverse of the cholesky root of Sigma for that component

Value

A list containing . . .

x An n x length(comps[[1]][[1]]) array of iid draws

z A n x 1 vector of indicators of which component each draw is taken from

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

See Also

rnmixGibbs

 $MCMC\ Algorithm\ for\ Multinomial\ Logit\ Model$

rmnlIndepMetrop

Description

rmnIndepMetrop implements Independence Metropolis for the MNL.

Usage

```
rmnlIndepMetrop(Data, Prior, Mcmc)
```

Arguments

Data list(p,y,X)

Prior list(A,betabar) optional

Mcmc list(R,keep,nu)

Details

Model: y ~ MNL(X,beta). $Pr(y = j) = exp(x_j'beta) / \sum_k e^{x_k'beta}$.

Prior: $beta \sim N(betabar, A^{-1})$

list arguments contain:

p number of alternatives

y nobs vector of multinomial outcomes $(1, \ldots, p)$

X nobs*m x nvar matrix

A nvar x nvar pds prior prec matrix (def: .01I)

betabar nvar x 1 prior mean (def: 0)

R number of MCMC draws

keep MCMC thinning parm: keep every keepth draw (def: 1)

nu degrees of freedom parameter for independence t density (def: 6)

Value

a list containing:

betadraw R/keep x nvar array of beta draws acceptr acceptance rate of Metropolis draws

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 5.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

```
rhierMnlRwMixture
```

Examples

##

```
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}

set.seed(66)
n=200; p=3; beta=c(1,-1,1.5,.5)
simout=simmnl(p,n,beta)
A=diag(c(rep(.01,length(beta)))); betabar=rep(0,length(beta))

Data=list(y=simout$y,X=simout$X,p=p); Mcmc=list(R=R,keep=1); Prior=list(A=A,betabar=betabar)
out=rmnlIndepMetrop(Data=Data,Prior=Prior,Mcmc=Mcmc)
cat(" Betadraws ",fill=TRUE)
mat=apply(out$betadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(beta,mat); rownames(mat)[1]="beta"; print(mat)
```

rmnpGibbs

Gibbs Sampler for Multinomial Probit

Description

rmnpGibbs implements the McCulloch/Rossi Gibbs Sampler for the multinomial probit model.

Usage

```
rmnpGibbs(Data, Prior, Mcmc)
```

Arguments

Data list(p, y, X)

Prior list(betabar,A,nu,V) (optional)

Mcmc list(beta0,sigma0,R,keep) (R required)

Details

```
w_i = X_i \beta + e. e \sim N(0, Sigma). note: w_i, e are (p-1) x 1.
    y_i = j, if w_{ij} > max(0, w_{i,-j}) j=1,...,p-1. w_{i,-j} means elements of w_i other than the jth.
    y_i = p, if all w_i < 0.
    priors:
    beta \sim N(betabar, A^{-1})
     Sigma \sim IW(nu, V)
     to make up X matrix use createX with DIFF=TRUE.
    List arguments contain
       p number of choices or possible multinomial outcomes
       y n x 1 vector of multinomial outcomes
       X n*(p-1) x k Design Matrix
betabar k x 1 prior mean (def: 0)
       A k x k prior precision matrix (def: .01I)
      nu d.f. parm for IWishart prior (def: (p-1) + 3)
       V pds location parm for IWishart prior (def: nu*I)
  beta0 initial value for beta
 sigma0 initial value for sigma
       R number of MCMC draws
   keep thinning parameter - keep every keepth draw (def: 1)
Value
    a list containing:
                       R/keep x k array of betadraws
    betadraw
                       R/keep x (p-1)*(p-1) array of sigma draws – each row is in vector form
     sigmadraw
Note
    beta is not identified. beta/\operatorname{sqrt}(sigma_{11}) and \operatorname{Sigma}/sigma_{11} are. See Allenby et al or
    example below for details.
```

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see Bayesian Statistics and Marketing by Allenby, McCulloch, and Rossi, Chapter 4.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

rmvpGibbs

Examples

```
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}
set.seed(66)
p=3
n=500
beta=c(-1,1,1,2)
Sigma=matrix(c(1,.5,.5,1),ncol=2)
k=length(beta)
x1=runif(n*(p-1),min=-1,max=1); x2=runif(n*(p-1),min=-1,max=1)
I2=diag(rep(1,p-1)); xadd=rbind(I2)
for(i in 2:n) { xadd=rbind(xadd,I2)}
X=cbind(xadd,x1,x2)
simout=simmnp(X,p,500,beta,Sigma)
Data=list(p=p,y=simout$y,X=simout$X)
Mcmc=list(R=R,keep=1)
out=rmnpGibbs(Mcmc=Mcmc,Data=Data)
cat(" Betadraws ",fill=TRUE)
mat=apply(out$betadraw/sqrt(out$sigmadraw[,1]),2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(beta,mat); rownames(mat)[1]="beta"; print(mat)
cat(" Sigmadraws ",fill=TRUE)
mat=apply(out$sigmadraw/out$sigmadraw[,1],2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(as.vector(Sigma),mat); rownames(mat)[1]="sigma"; print(mat)
```

rmultireg

Draw from the Posterior of a Multivariate Regression

Description

rmultireg draws from the posterior of a Multivariate Regression model with a natural conjugate prior.

Usage

```
rmultireg(Y, X, Bbar, A, nu, V)
```

Arguments

Y n x m matrix of observations on m dep vars

X n x k matrix of observations on indep vars (supply intercept)

Bbar k x m matrix of prior mean of regression coefficients

A k x k Prior precision matrix nu d.f. parameter for Sigma

V m x m pdf location parameter for prior on Sigma

Details

Model: Y = XB + U. $cov(u_i) = Sigma$. B is k x m matrix of coefficients. Sigma is m x m covariance.

Priors: beta given $Sigma \sim N(betabar, Sigma(x)A^{-1})$. betabar = vec(Bbar); beta = vec(B)

 $Sigma \sim IW(nu, V)$.

Value

A list of the components of a draw from the posterior

B draw of regression coefficient matrix

Sigma draw of Sigma

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

rmultiregfp,init.rmultiregfp

Examples

```
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}
set.seed(66)
n = 200
m=2
X=cbind(rep(1,n),runif(n))
k=ncol(X)
B=matrix(c(1,2,-1,3),ncol=m)
Sigma=matrix(c(1,.5,.5,1),ncol=m); RSigma=chol(Sigma)
Y=X%*%B+matrix(rnorm(m*n),ncol=m)%*%RSigma
betabar=rep(0,k*m);Bbar=matrix(betabar,ncol=m)
A=diag(rep(.01,k))
nu=3; V=nu*diag(m)
betadraw=matrix(double(R*k*m),ncol=k*m)
Sigmadraw=matrix(double(R*m*m),ncol=m*m)
for (rep in 1:R)
   {out=rmultireg(Y,X,Bbar,A,nu,V);betadraw[rep,]=out$B
    Sigmadraw[rep,]=out$Sigma}
cat(" Betadraws ",fill=TRUE)
mat=apply(betadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(as.vector(B),mat); rownames(mat)[1]="beta"
print(mat)
cat(" Sigma draws",fill=TRUE)
mat=apply(Sigmadraw, 2, quantile, probs=c(.01,.05,.5,.95,.99))
mat=rbind(as.vector(Sigma),mat); rownames(mat)[1]="Sigma"
print(mat)
```

rmultiregfp

Draw from the Posterior of a Multivariate Regression

Description

rmultiregfp draws from the posterior of a Multivariate Regression model with a natural conjugate prior.

Usage

```
rmultiregfp(Y, X, Fparm)
```

Arguments

Y n x m matrix of observations on m dep vars

X n x k matrix of observations on indep vars (supply intercept)

Fparm a list of prior parameters prepared by init.rmultiregfp

Details

```
Model: Y = XB + U. cov(u_i) = Sigma. B is k x m matrix of coefficients. Sigma is an m x m covariance matrix.
Priors: beta given Sigma \sim N(betabar, Sigma(x)A^{-1}). betabar = vec(Bbar); beta = vec(B).
```

 $Sigma \sim IW(nu,V)$.

prepare Fparm by call init.rmultiregfp

Value

A list of the components of a draw from the posterior

B draw of regression coefficient matrix

Sigma draw of Sigma

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

```
rmultireg,init.rmultiregfp
```

rmvpGibbs

Gibbs Sampler for Multivariate Probit

Description

rmvpGibbs implements the Edwards/Allenby Gibbs Sampler for the multivariate probit model.

Usage

```
rmvpGibbs(Data, Prior, Mcmc)
```

Arguments

Data list(p,y,X)

Prior list(betabar,A,nu,V) (optional)

Mcmc list(beta0,sigma0,R,keep) (R required)

Details

```
model:
    w_i = X_i beta + e. e \sim N(0, Sigma). note: w_i is p x 1.
    y_{ij} = 1, if w_{ij} > 0, else y_i = 0. j=1,...,p.
    priors:
    beta \sim N(betabar, A^{-1})
    Sigma \sim IW(nu, V)
    to make up X matrix use createX
    List arguments contain
       p dimension of multivariate probit
       X n*p x k Design Matrix
       y n*p x 1 vector of 0,1 outcomes
betabar k x 1 prior mean (def: 0)
       A k x k prior precision matrix (def: .01I)
      nu d.f. parm for IWishart prior (def: (p-1) + 3)
       V pds location parm for IWishart prior (def: nu*I)
  beta0 initial value for beta
 sigma0 initial value for sigma
       R number of MCMC draws
```

keep thinning parameter - keep every keepth draw (def: 1)

Value

a list containing:

betadraw R/keep x k array of betadraws

sigmadraw R/keep x p*p array of sigma draws – each row is in vector form

Note

beta and Sigma are not identified. Correlation matrix and the betas divided by the appropriate standard deviation are. See Allenby et al for details or example below.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 4.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

rmnpGibbs

Examples

```
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}
set.seed(66)
p=3
n=500
beta=c(-2,0,2)
Sigma=matrix(c(1,.5,.5,.5,1,.5,.5,.5,1),ncol=3)
k=length(beta)
I2=diag(rep(1,p)); xadd=rbind(I2)
for(i in 2:n) { xadd=rbind(xadd,I2)}; X=xadd
simout=simmvp(X,p,500,beta,Sigma)
Data=list(p=p,y=simout$y,X=simout$X)
Mcmc=list(R=R,keep=1)
out=rmvpGibbs(Data=Data,Mcmc=Mcmc)
ind=seq(from=0,by=p,length=k)
inda=1:3
ind=ind+inda
cat(" Betadraws ",fill=TRUE)
mat=apply(out$betadraw/sqrt(out$sigmadraw[,ind]),2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(beta,mat); rownames(mat)[1]="beta"; print(mat)
rdraw=matrix(double((R)*p*p),ncol=p*p)
rdraw=t(apply(out$sigmadraw,1,nmat))
cat(" Draws of Correlation Matrix ",fill=TRUE)
mat=apply(rdraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(as.vector(Sigma),mat); rownames(mat)[1]="Sigma"; print(mat)
```

rmvst

 $Draw\ from\ Multivariate\ Student-t$

Description

rmvst draws from a Multivariate student-t distribution.

Usage

```
rmvst(nu, mu, root)
```

Arguments

nu d.f. parameter mu mean vector

root Upper Tri Cholesky Root of Sigma

Value

length(mu) draw vector

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

lndMvst

Examples

```
##
```

```
set.seed(66)
rmvst(nu=5,mu=c(rep(0,2)),root=chol(matrix(c(2,1,1,2),ncol=2)))
```

rnegbinRw

MCMC Algorithm for Negative Binomial Regression

Description

rnegbinRw implements a Random Walk Metropolis Algorithm for the Negative Binomial (NBD) regression model. beta | alpha and alpha | beta are drawn with two different random walks.

Usage

```
rnegbinRw(Data, Prior, Mcmc)
```

Arguments

Data list(y,X)

Prior list(betabar,A,a,b)

Mcmc list(R,keep,s_beta,s_alpha,beta0

Details

```
Model: y \sim NBD(mean = lambda, over - dispersion = alpha). lambda = exp(x'beta)

Prior: beta \sim N(betabar, A^{-1})
alpha \sim Gamma(a, b).
note: prior mean of alpha = a/b, variance = a/(b^2)
list arguments contain:

y nobs vector of counts (0,1,2,\dots)
X nobs x nvar matrix

betabar nvar x 1 prior mean (def: 0)
A nvar x nvar pds prior prec matrix (def: .01I)
a Gamma prior parm (def: .5)
b Gamma prior parm (def: .1)
R number of MCMC draws

keep MCMC thinning parm: keep every keepth draw (def: 1)
s_beta scaling for beta| alpha RW inc cov matrix (def: 2.93/sqrt(nvar)
```

Value

a list containing:

betadraw R/keep x nvar array of beta draws alphadraw R/keep vector of alpha draws

s_alpha scaling for alpha | beta RW inc cov matrix (def: 2.93)

11ike R/keep vector of log-likelihood values evaluated at each draw

acceptrate acceptance rate of the beta draws acceptralpha acceptance rate of the alpha draws

Note

The NBD regression encompasses Poisson regression in the sense that as alpha goes to infinity the NBD distribution tends toward the Poisson.

For "small" values of alpha, the dependent variable can be extremely variable so that a large number of observations may be required to obtain precise inferences.

Author(s)

Sridhar Narayanam & Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

rhierNegbinRw

Examples

```
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=1000} else {R=10}
set.seed(66)
simnegbin =
function(X, beta, alpha) {
# Simulate from the Negative Binomial Regression
lambda = exp(X %*% beta)
y=NULL
for (j in 1:length(lambda))
    y = c(y,rnbinom(1,mu = lambda[j],size = alpha))
return(y)
}
nobs = 500
nvar=2
                  # Number of X variables
alpha = 5
Vbeta = diag(nvar)*0.01
# Construct the regdata (containing X)
simnegbindata = NULL
beta = c(0.6, 0.2)
X = cbind(rep(1,nobs),rnorm(nobs,mean=2,sd=0.5))
simnegbindata = list(y=simnegbin(X,beta,alpha), X=X, beta=beta)
Data = simnegbindata
betabar = rep(0,nvar)
A = 0.01 * diag(nvar)
a = 0.5; b = 0.1
Prior = list(betabar=betabar, A=A, a=a, b=b)
keep = 1
s_beta=2.93/sqrt(nvar); s_alpha=2.93
Mcmc = list(R=R, keep = keep, s_beta=s_beta, s_alpha=s_alpha)
out = rnegbinRw(Data, Prior, Mcmc)
cat(" betadraws ",fill=TRUE)
```

```
mat=apply(out$betadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(beta,mat); rownames(mat)[1]="beta"; print(mat)
cat(" alphadraws ",fill=TRUE)
mat=apply(matrix(out$alphadraw),2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(as.vector(alpha),mat); rownames(mat)[1]="alpha"; print(mat)
```

rnmixGibbs

Gibbs Sampler for Normal Mixtures

Description

rnmixGibbs implements a Gibbs Sampler for normal mixtures.

Usage

```
rnmixGibbs(Data, Prior, Mcmc)
```

Arguments

Data list(y)

Prior list(Mubar, A, nu, V, a, ncomp) (only ncomp required)

Mcmc list(R,keep) (R required)

Details

```
Model:
```

```
y_i \sim N(mu_{ind_i}, Sigma_{ind_i}).
ind \sim iid multinomial(p). p is a nomp x 1 vector of probs.
```

Priors:

```
mu_j \sim N(mubar, Sigma_j(x)A^{-1}). \ mubar = vec(Mubar).
```

 $Sigma_i \sim IW(nu,V)$.

note: this is the natural conjugate prior – a special case of multivariate regression. $p \sim \text{Dirchlet}(a)$.

Output of the components is in the form of a list of lists.

compsdraw[[i]] is ith draw – list of ncomp lists.

compsdraw[[i]][[j]] is list of parms for jth normal component.

jcomp=compsdraw[[i]][j]]. Then jth comp $\sim N(jcomp[[1]], Sigma)$, Sigma = t(R)%*%R, $R^{-1} = \text{jcomp}[[2]]$.

List arguments contain:

```
y n x k array of data (rows are obs)
```

Mubar k x 1 array with prior mean of normal comp means (def: 0)

A 1 x 1 precision parameter for prior on mean of normal comp (def: .01)

nu d.f. parameter for prior on Sigma (normal comp cov matrix) (def: k+3)

V k x k location matrix of IW prior on Sigma (def: nuI)

```
a ncomp x 1 vector of Dirichlet prior parms (def: rep(5,ncomp))
ncomp number of normal components to be included
R number of MCMC draws
keep MCMC thinning parm: keep every keepth draw (def: 1)
```

a list containing:

probdraw R/keep x ncomp array of mixture prob draws

zdraw R/keep x nobs array of indicators of mixture comp identity for each obs

compdraw R/keep lists of lists of comp parm draws

Note

In this model, the component normal parameters are not-identified due to label-switching. However, the fitted mixture of normals density is identified as it is invariant to label-switching. See Allenby et al, chapter 5 for details. Use eMixMargDen or momMix to compute posterior expectation or distribution of various identified parameters.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 5.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

```
rmixture, rmixGibbs ,eMixMargDen, momMix
```

Examples

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}

set.seed(66)
dim=5; k=3  # dimension of simulated data and number of "true" components
sigma = matrix(rep(0.5,dim^2),nrow=dim);diag(sigma)=1
sigfac = c(1,1,1);mufac=c(1,2,3); compsmv=list()
for(i in 1:k) compsmv[[i]] = list(mu=mufac[i]*1:dim,sigma=sigfac[i]*sigma)
comps = list()  # change to "rooti" scale
for(i in 1:k) comps[[i]] = list(mu=compsmv[[i]][[1]],rooti=solve(chol(compsmv[[i]][[2]])))
pvec=(1:k)/sum(1:k)
nobs=5000
dm = rmixture(nobs,pvec,comps)
```

```
Data=list(y=dm$x)
ncomp=9
Prior=list(ncomp=ncomp,a=c(rep(1,ncomp)))
Mcmc=list(R=R,keep=1)
out=rnmixGibbs(Data=Data,Prior=Prior,Mcmc=Mcmc)
tmom=momMix(matrix(pvec,nrow=1),list(comps))
if(R < 1000) {begin=1} else {begin=500}
pmom=momMix(out$probdraw[begin:R,],out$compdraw[begin:R])
mat=rbind(tmom$mu,pmom$mu)
rownames(mat)=c("true", "post expect")
cat(" mu and posterior expectation of mu",fill=TRUE)
print(mat)
mat=rbind(tmom$sd,pmom$sd)
rownames(mat)=c("true","post expect")
cat(" std dev and posterior expectation of sd",fill=TRUE)
print(mat)
mat=rbind(as.vector(tmom$corr),as.vector(pmom$corr))
rownames(mat)=c("true","post expect")
cat(" corr and posterior expectation of corr",fill=TRUE)
print(t(mat))
```

 ${\tt rscaleUsage}$

MCMC Algorithm for Multivariate Ordinal Data with Scale Usage Heterogeneity.

Description

rscaleUsage implements an MCMC algorithm for multivariate ordinal data with scale usage heterogeniety.

Usage

```
rscaleUsage(Data,Prior, Mcmc)
```

Arguments

Data list(k,x)

 $\label{eq:prior} {\tt Prior} \qquad \qquad {\tt list(nu,V,mubar,Am,gsigma,gl11,gl22,gl12,Lambdanu,LambdaV,ge)} \ (optional)$

 ${\tt Mcmc} \qquad \qquad {\tt list(R,keep,ndghk,printevery,e,y,mu,Sigma,sigma,tau,Lambda)\ (optional)}$

Details

```
Model: n=nrow(x) individuals respond to m=ncol(x) questions. all questions are on a scale 1,\ldots,k. for respondent i and question j, x_{ij}=d, if c_{d-1}\leq y_{ij}\leq c_d. d=1,\ldots,k. c_d=a+bd+ed^2. y_i=mu+tau_i*iota+sigma_i*z_i.\ z_i\sim N(0,Sigma). Priors: (tau_i,ln(sigma_i))\sim N(phi,Lamda).\ phi=(0,lambda_{22}). mu\sim N(mubar,Am^{-1}). Sigma \sim \mathrm{IW}(\mathrm{nu},\mathrm{V}). Lambda \sim \mathrm{IW}(\mathrm{Lambdanu},\mathrm{LambdaV}). e \sim unif on a grid.
```

Value

a list containing:

Sigmadraw R/keep x m*m array of Sigma draws
mudraw R/keep x m array of mu draws
taudraw R/keep x n array of tau draws
sigmadraw R/keep x n array of sigma draws
Lambdadraw R/keep x 4 array of Lamda draws
edraw R/keep x 1 array of e draws

Warning

 tau_i , $sigma_i$ are identified from the scale usage patterns in the m questions asked per respondent (# cols of x). Do not attempt to use this on data sets with only a small number of total questions!

Note

It is **highly** recommended that the user choose the default settings. This means not specifying the argument Prior and setting R in Mcmc and Data only. If you wish to change prior settings and/or the grids used, please read the case study in Allenby et al carefully.

Author(s)

Rob McCulloch and Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Case Study on Scale Usage Heterogeneity.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

Examples

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0)
{
data(customerSat)
surveydat = list(k=10,x=as.matrix(customerSat))

R=1000
mcmc = list(R=R)
set.seed(66)
out=rscaleUsage(Data=surveydat,Mcmc=mcmc)

cat(" mudraws ",fill=TRUE)
mat=apply(out$mudraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
print(mat)
}
```

rtrun

Draw from Truncated Univariate Normal

Description

rtrun draws from a truncated univariate normal distribution

Usage

```
rtrun(mu, sigma, a, b)
```

Arguments

mu	mean
sigma	sd

a lower boundb upper bound

Details

Note that due to the vectorization of the rnorm, quorm commands in R, all arguments can be vectors of equal length. This makes the inverse CDF method the most efficient to use in R.

Value

```
draw (possibly a vector)
```

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 2.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

Examples

```
##
set.seed(66)
rtrun(mu=c(rep(0,10)),sigma=c(rep(1,10)),a=c(rep(0,10)),b=c(rep(2,10)))
```

runireg

Draw from Posterior for Univariate Regression

Description

runized draws from posterior for univariate regression with a natural conjugate prior.

Usage

```
runireg(y, X, betabar, A, nu, ssq)
```

Arguments

y $n \times 1 \text{ dep var}$

X n x k Design matrix

betabar prior mean

A k x k pds prior precision matrix nu d.f. parameter for sigma-sq prior ssq scale parameter for sigma-sq prior

Details

```
Model: y = Xbeta + e. e \sim N(0, sigmasq).
```

Priors: beta given sigmasq ~ $N(betabar, sigmasq * A^{-1})$. $sigmasq \sim \text{eqn(nu*ssq)}/\chi^2_{nu}$.

a list with one draw from posterior

beta beta draw sigmasq draw

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 2.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

runiregGibbs

Examples

```
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=1000} else {R=10}
set.seed(66)
n=100
X=cbind(rep(1,n),runif(n)); beta=c(1,2); sigsq=.25
y=X%*%beta+rnorm(n,sd=sqrt(sigsq))
A=diag(c(.05,.05)); betabar=c(0,0)
nu=3; ssq=1.0
betadraw=matrix(double(R*2),ncol=2)
sigsqdraw=double(R)
for (rep in 1:R)
   {out=runireg(y,X,betabar,A,nu,ssq);betadraw[rep,]=out$beta
    sigsqdraw[rep]=out$sigmasq}
cat(" Betadraws ",fill=TRUE)
mat=apply(betadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(beta,mat); rownames(mat)[1]="beta"; print(mat)
cat(" Sigma-sq draws",fill=TRUE)
cat(" sigma-sq= ",sigsq,fill=TRUE)
print(quantile(sigsqdraw,probs=c(.01,.05,.5,.95,.99)))
```

Gibbs Sampler for Univariate Regression

runiregGibbs

Description

runiregGibbs implements a Gibbs Sampler to draw from posterior for univariate regression with a conditionally conjugate prior.

Usage

```
runiregGibbs(Data, Prior, Mcmc)
```

Arguments

Data list(y,X)

Prior list(betabar,A, nu, ssq)
Mcmc list(sigmasq,R,keep)

Details

```
Model: y = Xbeta + e. e \sim N(0, sigmasq).
```

Priors: $beta \sim N(betabar, A^{-1})$. $sigmasq \sim (nu * ssq)/chisq_{nu}$. List arguments contain

X Design Matrix

y n x 1 vector of observations, (0 or 1)

betabar k x 1 prior mean (def: 0)

A k x k prior precision matrix (def: .01I)

nu d.f. parm for Inverted Chi-square prior

ssq scale parm for Inverted Chi-square prior

R number of MCMC draws

keep thinning parameter - keep every keepth draw

Value

list of MCMC draws

betadraw R x k array of betadraws sigmasqdraw R vector of sigma-sq draws

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 3.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

```
runireg
```

Examples

```
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}
set.seed(66)
n=100
X=cbind(rep(1,n),runif(n)); beta=c(1,2); sigsq=.25
y=X%*%beta+rnorm(n,sd=sqrt(sigsq))
A=diag(c(.05,.05)); betabar=c(0,0)
nu=3; ssq=1.0

Data=list(y=y,X=X); Mcmc=list(R=R,keep=1) ; Prior=list(A=A,betabar=betabar,nu=nu,ssq=ssq)
out=runiregGibbs(Data=Data,Prior=Prior,Mcmc=Mcmc)
cat(" Betadraws ",fill=TRUE)
mat=apply(out$betadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(beta,mat); rownames(mat)[1]="beta"; print(mat)
cat(" Sigma-sq draws",fill=TRUE)
cat(" sigma-sq= ",sigsq,fill=TRUE)
print(quantile(out$sigmasqdraw,probs=c(.01,.05,.5,.95,.99)))
```

rwishart

Draw from Wishart and Inverted Wishart Distribution

Description

rwishart draws from the Wishart and Inverted Wishart distributions.

Usage

```
rwishart(nu, V)
```

Arguments

nu d.f. parameter

V pds location matrix

Details

In the parameterization used here, $W \sim W(nu, V)$, E[W] = nuV.

If you want to use an Inverted Wishart prior, you *must invert the location matrix* before calling rwishart, e.g.

```
Sigma \sim IW(nu, V); Sigma^{-1} \sim W(nu, V^{-1}).
```

Value

W	Wishart draw
IW	Inverted Wishart draw
C	Upper tri root of W
CI	$inv(C), W^{-1} = CICI'$

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 2.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

Examples

```
##
set.seed(66)
rwishart(5,diag(3))$IW
```

Scotch

Survey Data on Brands of Scotch Consumed

Description

from Simmons Survey. Brands used in last year for those respondents who report consuming scotch.

Usage

data(Scotch)

Format

A data frame with 2218 observations on the following 21 variables. All variables are coded 1 if consumed in last year, 0 if not.

```
Chivas.Regal a numeric vector
Dewar.s.White.Label a numeric vector
Johnnie.Walker.Black.Label a numeric vector
J...B a numeric vector
Johnnie.Walker.Red.Label a numeric vector
Other.Brands a numeric vector
Glenlivet a numeric vector
Cutty.Sark a numeric vector
Glenfiddich a numeric vector
Pinch..Haig. a numeric vector
Clan.MacGregor a numeric vector
Ballantine a numeric vector
Macallan a numeric vector
Passport a numeric vector
Black...White a numeric vector
Scoresby.Rare a numeric vector
Grants a numeric vector
Ushers a numeric vector
White. Horse a numeric vector
Knockando a numeric vector
the.Singleton a numeric vector
```

Source

Edwards, Y. and G. Allenby (2003), "Multivariate Analysis of Multiple Response Data," *JMR* 40, 321-334.

References

```
Chapter 4, Bayesian Statistics and Marketing by Rossi et al. http://gsbww.uchicago.edu/fac/peter.rossi/research/bsm.html
```

Examples

```
data(Scotch)
cat(" Frequencies of Brands", fill=TRUE)
mat=apply(as.matrix(Scotch),2,mean)
print(mat)
##
## use Scotch data to run Multivariate Probit Model
```

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0){
##
y=as.matrix(Scotch)
p=ncol(y); n=nrow(y)
dimnames(y)=NULL
y=as.vector(t(y))
y=as.integer(y)
I_p=diag(p)
X=rep(I_p,n)
X=matrix(X,nrow=p)
X=t(X)
R=2000
Data=list(p=p,X=X,y=y)
Mcmc=list(R=R)
set.seed(66)
out=rmvpGibbs(Data=Data,Mcmc=Mcmc)
ind=(0:(p-1))*p + (1:p)
cat(" Betadraws ",fill=TRUE)
mat=apply(out$betadraw/sqrt(out$sigmadraw[,ind]),2,quantile,probs=c(.01,.05,.5,.95,.99))
print(mat)
rdraw=matrix(double((R)*p*p),ncol=p*p)
rdraw=t(apply(out$sigmadraw,1,nmat))
cat(" Draws of Correlation Matrix ",fill=TRUE)
mat=apply(rdraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
## correlation matrix too large to print -- summarize
quantile(round(mat,digits=2))
}
```

simmnl

Simulate from Multinomial Logit Model

Description

simmal simulates from the MNL model.

Usage

```
simmnl(p, n, beta)
```

Arguments

p number choice alternativesn number of observationsbeta MNL coefficient vector

Details

simml will simulate two uniformly distributed X vars and add intercepts.

Value

y n x 1 vector of multinomial outcomes (1, ..., p)

Χ

beta beta vector

prob n x j array of choice probabilities

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

llmnl, rmnlIndepMetrop

simmnlwX

 $Simulate\ from\ MNL\ given\ X\ Matrix$

Description

simmnlwX simulates from MNL given X Matrix.

Usage

```
simmnlwX(n, X, beta)
```

Arguments

n number of obs

X n*p x k Design matrix (p is number of choice alts)

beta k x 1 coefficient vector

a list containing:

y n x 1 vector of multinomial outcomes (1, ..., nrow(X)/n)

X Design matrix beta coefficient vector

prob n x p array of choice probs

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

simmnl

simmnp

Simulate from Multinomial Probit Model

Description

simmvp simulates from the multinomial probit model.

Usage

```
simmnp(X, p, n, beta, sigma)
```

Arguments

X n*(p-1) x length(beta) Design matrix

p number of choice alternatives

n number of observations

beta coefficient vector

sigma (p-1) x (p-1) covariance matrix

a list of

y n vector of multinomial $(1, \ldots, p)$ outcomes

X Design matrix beta coefficients

sigma covariance matrix

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 4.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

rmnpGibbs

simmvp

Simulate from Multivariate Probit Model

Description

simmup simulates from the multivariate probit model.

Usage

```
simmvp(X, p, n, beta, sigma)
```

Arguments

X n*p x length(beta) Design matrix

p dimension of the MVP n number of observations

beta coefficient vector

sigma p x p covariance matrix

a list of

y p*n vector of 0/1 binary outcomes

X Design matrix beta coefficients

sigma covariance matrix

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi.

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

rmvpGibbs

simnhlogit

Simulate from Non-homothetic Logit Model

Description

simnhlogit simulates from the non-homothetic logit model

Usage

```
simnhlogit(theta, lnprices, Xexpend)
```

Arguments

theta coefficient vector

lnprices n x p array of prices

Xexpend n x k array of values of expenditure variables

Details

For detail on parameterization, see llnhlogit.

a list containing:

y n x 1 vector of multinomial outcomes (1, ..., p)

Xexpend expenditure variables

lnprices price array
theta coefficients

prob n x p array of choice probabilities

Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

References

For further discussion, see $Bayesian\ Statistics\ and\ Marketing\$ by Allenby, McCulloch, and Rossi

http://gsbwww.uchicago.edu/fac/peter.rossi/research/bsm.html

See Also

llnhlogit