# Description

Data from a conjoint experiment in which two partial profiles of credit cards were presented to 946 respondents. The variable bank\$choiceAtt\$choice indicates which profile was chosen. The profiles are coded as the difference in attribute levels. Thus, a "-1" means the profile coded as a choice of "0" has the attribute. A value of 0 means that the attribute was not present in the comparison.

data on age,income and gender (female=1) are also recorded in bank\$demo

## Usage

data(bank)

#### **Format**

```
This R object is a list of two data frames, list(choiceAtt,demo).
List of 2
$ choiceAtt: 'data.frame': 14799 obs. of 16 variables:
\dots$ id: int [1:14799] 1 1 1 1 1 1 1 1 1 1 1
...$ choice: int [1:14799] 1 1 1 1 1 1 1 1 0 1
...$ Med_FInt : int [1:14799] 1 1 1 0 0 0 0 0 0 0
...$ Low_FInt : int [1:14799] 0 0 0 0 0 0 0 0 0 0
...$ Med_VInt: int [1:14799] 0 0 0 0 0 0 0 0 0 0
...$ Rewrd_2: int [1:14799] -1 1 0 0 0 0 0 1 -1 0
...$ Rewrd_3: int [1:14799] 0 -1 1 0 0 0 0 0 1 -1
...$ Rewrd_4: int [1:14799] 0 0 -1 0 0 0 0 0 0 1
...$ Med_Fee: int [1:14799] 0 0 0 1 1 -1 -1 0 0 0
...$ Low_Fee: int [1:14799] 0 0 0 0 0 1 1 0 0 0
...$ Bank_B: int [1:14799] 0 0 0 -1 1 -1 1 0 0 0
...$ Out_State: int [1:14799] 0 0 0 0 -1 0 -1 0 0 0
...$ Med_Rebate: int [1:14799] 0 0 0 0 0 0 0 0 0 0
...$ High_Rebate : int [1:14799] 0 0 0 0 0 0 0 0 0 0
...$ High_CredLine: int [1:14799] 0 0 0 0 0 0 0 -1 -1 -1
...$ Long_Grace: int [1:14799] 0 0 0 0 0 0 0 0 0 0
$ demo :'data.frame': 946 obs. of 4 variables:
...$ id: int [1:946] 1 2 3 4 6 7 8 9 10 11
\dots$ age: int [1:946] 60 40 75 40 30 30 50 50 50 40
...$ income: int [1:946] 20 40 30 40 30 60 50 100 50 40
...$ gender: int [1:946] 1 1 0 0 0 0 1 0 0 0
```

#### **Details**

Each respondent was presented with between 13 and 17 paired comparisons. Thus, this dataset has a panel structure.

#### Source

Allenby and Ginter (1995), "Using Extremes to Design Products and Segment Markets," *JMR*, 392-403.

#### References

Appendix A, Bayesian Statistics and Marketing by Rossi, Allenby and McCulloch. http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

```
data(bank)
cat(" table of Binary Dep Var", fill=TRUE)
print(table(bank$choiceAtt[,2]))
cat(" table of Attribute Variables",fill=TRUE)
mat=apply(as.matrix(bank$choiceAtt[,3:16]),2,table)
print(mat)
cat(" means of Demographic Variables",fill=TRUE)
mat=apply(as.matrix(bank$demo[,2:3]),2,mean)
print(mat)
## example of processing for use with rhierBinLogit
##
if(0)
{
choiceAtt=bank$choiceAtt
Z=bank$demo
## center demo data so that mean of random-effects
## distribution can be interpreted as the average respondent
Z[,1]=rep(1,nrow(Z))
Z[,2]=Z[,2]-mean(Z[,2])
Z[,3]=Z[,3]-mean(Z[,3])
Z[,4]=Z[,4]-mean(Z[,4])
Z=as.matrix(Z)
hh=levels(factor(choiceAtt$id))
nhh=length(hh)
lgtdata=NULL
for (i in 1:nhh) {
        y=choiceAtt[choiceAtt[,1]==hh[i],2]
        nobs=length(y)
        X=as.matrix(choiceAtt[choiceAtt[,1]==hh[i],c(3:16)])
        lgtdata[[i]]=list(y=y,X=X)
```

```
cat("Finished Reading data",fill=TRUE)
fsh()
Data=list(lgtdata=lgtdata,Z=Z)
Mcmc=list(R=10000,sbeta=0.2,keep=20)
set.seed(66)
out=rhierBinLogit(Data=Data,Mcmc=Mcmc)
begin=5000/20
end=10000/20
summary(out$Deltadraw,burnin=begin)
summary(out$Vbetadraw,burnin=begin)
if(0){
## plotting examples
## plot grand means of random effects distribution (first row of Delta)
index=4*c(0:13)+1
matplot(out$Deltadraw[,index],type="l",xlab="Iterations/20",ylab="",
main="Average Respondent Part-Worths")
## plot hierarchical coefs
plot(out$betadraw)
## plot log-likelihood
plot(out$1like,type="1",xlab="Iterations/20",ylab="",main="Log Likelihood")
}
}
```

breg

Posterior Draws from a Univariate Regression with Unit Error Variance

## Description

breg makes one draw from the posterior of a univariate regression (scalar dependent variable) given the error variance = 1.0. A natural conjugate, normal prior is used.

## Usage

```
breg(y, X, betabar, A)
```

## Arguments

betabar k x 1 vector. Prior mean of regression coefficients.

A Prior precision matrix.

#### **Details**

```
model: y = x'\beta + e. e \sim N(0, 1).
prior: \beta \sim N(betabar, A^{-1}).
```

## Value

k x 1 vector containing a draw from the posterior distribution.

# Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

In particular, X must be a matrix. If you have a vector for X, coerce it into a matrix with one column

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=1000} else {R=10}
## simulate data
set.seed(66)
n=100
X=cbind(rep(1,n),runif(n)); beta=c(1,2)
y=X%*%beta+rnorm(n)
##
## set prior
A=diag(c(.05,.05)); betabar=c(0,0)
## make draws from posterior
betadraw=matrix(double(R*2),ncol=2)
for (rep in 1:R) {betadraw[rep,]=breg(y,X,betabar,A)}
## summarize draws
mat=apply(betadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(beta,mat); rownames(mat)[1]="beta"; print(mat)
```

## Description

cgetC obtains a list of censoring points, or cut-offs, used in the ordinal multivariate probit model of Rossi et al (2001). This approach uses a quadratic parameterization of the cut-offs. The model is useful for modeling correlated ordinal data on a scale from 1, ..., k with different scale usage patterns.

## Usage

```
cgetC(e, k)
```

## Arguments

e quadratic parameter (>0 and less than 1) k items are on a scale from  $1, \ldots, k$ 

# Value

A vector of k+1 cut-offs.

# Warning

This is a utility function which implements no error-checking.

## Author(s)

Rob McCulloch and Peter Rossi, Graduate School of Business, University of Chicago.  $\langle Peter.Rossi@ChicagoGsb.edu \rangle$ .

## References

Rossi et al (2001), "Overcoming Scale Usage Heterogeneity," JASA96, 20-31.

## See Also

```
rscaleUsage
```

```
##
cgetC(.1,10)
```

## Description

Panel data with sales volume for a package of Borden Sliced Cheese as well as a measure of display activity and price. Weekly data aggregated to the "key" account or retailer/market level

## Usage

```
data(cheese)
```

#### **Format**

A data frame with 5555 observations on the following 4 variables.

```
RETAILER a list of 88 retailers

VOLUME unit sales

DISP a measure of display activity – per cent ACV on display

PRICE in $
```

#### Source

Boatwright et al (1999), "Account-Level Modeling for Trade Promotion," JASA 94, 1063-1073.

#### References

```
Chapter 3, Bayesian Statistics and Marketing by Rossi et al. http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html
```

```
data(cheese)
cat(" Quantiles of the Variables ",fill=TRUE)
mat=apply(as.matrix(cheese[,2:4]),2,quantile)
print(mat)

##
## example of processing for use with rhierLinearModel
##
if(0)
{
retailer=levels(cheese$RETAILER)
nreg=length(retailer)
nvar=3
```

```
regdata=NULL
for (reg in 1:nreg) {
        y=log(cheese$VOLUME[cheese$RETAILER==retailer[reg]])
        iota=c(rep(1,length(y)))
        X=cbind(iota,cheese$DISP[cheese$RETAILER==retailer[reg]],
                log(cheese$PRICE[cheese$RETAILER==retailer[reg]]))
        regdata[[reg]]=list(y=y,X=X)
}
Z=matrix(c(rep(1,nreg)),ncol=1)
nz=ncol(Z)
##
## run each individual regression and store results
lscoef=matrix(double(nreg*nvar),ncol=nvar)
for (reg in 1:nreg) {
        coef=lsfit(regdata[[reg]]$X,regdata[[reg]]$y,intercept=FALSE)$coef
        if (var(regdata[[reg]]$X[,2])==0) { lscoef[reg,1]=coef[1]; lscoef[reg,3]=coef[2]}
        else {lscoef[reg,]=coef }
}
R=2000
Data=list(regdata=regdata,Z=Z)
Mcmc=list(R=R,keep=1)
set.seed(66)
out=rhierLinearModel(Data=Data,Mcmc=Mcmc)
cat("Summary of Delta Draws",fill=TRUE)
summary(out$Deltadraw)
cat("Summary of Vbeta Draws",fill=TRUE)
summary(out$Vbetadraw)
if(0){
# plot hier coefs
plot(out$betadraw)
}
```

clusterMix

Cluster Observations Based on Indicator MCMC Draws

# Description

clusterMix uses MCMC draws of indicator variables from a normal component mixture model to cluster observations based on a similarity matrix.

## Usage

```
clusterMix(zdraw, cutoff = 0.9, SILENT = FALSE)
```

#### **Arguments**

zdraw R x nobs array of draws of indicators

cutoff cutoff probability for similarity (def=.9)

SILENT logical flag for silent operation (def= FALSE)

## Details

define a similarity matrix, Sim, Sim[i,j]=1 if observations i and j are in same component. Compute the posterior mean of Sim over indicator draws.

clustering is achieved by two means:

Method A: Find the indicator draw whose similarity matrix minimizes, loss(E[Sim]-Sim(z)), where loss is absolute deviation.

Method B: Define a Similarity matrix by setting any element of E[Sim] = 1 if E[Sim] > cutoff. Compute the clustering scheme associated with this "windsorized" Similarity matrix.

#### Value

clustera indicator function for clustering based on method A above clusterb indicator function for clustering based on method B above

#### Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch Chapter 3.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

## See Also

rnmixGibbs

# Examples

```
if(nchar(Sys.getenv("LONG_TEST")) != 0)
## simulate data from mixture of normals
n=500
pvec=c(.5,.5)
mu1=c(2,2)
mu2=c(-2,-2)
Sigma1=matrix(c(1,.5,.5,1),ncol=2)
Sigma2=matrix(c(1,.5,.5,1),ncol=2)
comps=NULL
comps[[1]]=list(mu1,backsolve(chol(Sigma1),diag(2)))
comps[[2]]=list(mu2,backsolve(chol(Sigma2),diag(2)))
dm=rmixture(n,pvec,comps)
## run MCMC on normal mixture
R=2000
Data=list(y=dm$x)
ncomp=2
Prior=list(ncomp=ncomp,a=c(rep(100,ncomp)))
Mcmc=list(R=R,keep=1)
out=rnmixGibbs(Data=Data,Prior=Prior,Mcmc=Mcmc)
begin=500
end=R
## find clusters
outclusterMix=clusterMix(out$zdraw[begin:end,])
##
## check on clustering versus "truth"
   note: there could be switched labels
table(outclusterMix$clustera,dm$z)
table(outclusterMix$clusterb,dm$z)
}
##
```

condMom

 $Computes\ Conditional\ Mean/Var\ of\ One\ Element\ of\ MVN\ given$   $All\ Others$ 

## Description

condMom compute moments of conditional distribution of ith element of normal given all others.

#### Usage

```
condMom(x, mu, sigi, i)
```

## **Arguments**

x vector of values to condition on - ith element not used

mu length(x) mean vector

sigi length(x)-dim covariance matrix

i conditional distribution of ith element

## **Details**

```
x \sim MVN(mu, Sigma).
condMom computes moments of x_i given x_{-i}.
```

## Value

a list containing:

cmean cond mean cvar cond variance

## Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

## References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

```
##
sig=matrix(c(1,.5,.5,.5,1,.5,.5,1),ncol=3)
sigi=chol2inv(chol(sig))
mu=c(1,2,3)
x=c(1,1,1)
condMom(x,mu,sigi,2)
```

$Create\ X$	Matrix for	Use	in	Multinomial	Logit	and	Probit	Rou-
tines								

Description

createX

createX makes up an X matrix in the form expected by Multinomial Logit (rmnlIndepMetrop and rhierMnlRwMixture) and Probit (rmnpGibbs and rmvpGibbs) routines. Requires an array of alternative specific variables and/or an array of "demographics" or variables constant across alternatives which may vary across choice occasions.

## Usage

```
createX(p, na, nd, Xa, Xd, INT = TRUE, DIFF = FALSE, base = p)
```

## Arguments

p	integer - number of choice alternatives
na	integer - number of alternative-specific vars in Xa
nd	integer - number of non-alternative specific vars
Xa	n x p*na matrix of alternative-specific vars
Xd	n x nd matrix of non-alternative specific vars
INT	logical flag for inclusion of intercepts
DIFF	logical flag for differencing wrt to base alternative
base	integer - index of base choice alternative
note: na.nd.Xa.X	Xd can be NULL to indicate lack of Xa or Xd variables.

## Value

```
X matrix – n*(p-DIFF) x [(INT+nd)*(p-1) + na] matrix.
```

# Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

## References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

## See Also

 ${\tt rmnlIndepMetrop}, \, {\tt rmnpGibbs}$ 

## Examples

```
na=2; nd=1; p=3
vec=c(1,1.5,.5,2,3,1,3,4.5,1.5)
Xa=matrix(vec,byrow=TRUE,ncol=3)
Xa=cbind(Xa,-Xa)
Xd=matrix(c(-1,-2,-3),ncol=1)
createX(p=p,na=na,nd=nd,Xa=Xa,Xd=Xd)
createX(p=p,na=na,nd=nd,Xa=Xa,Xd=Xd,base=1)
createX(p=p,na=na,nd=nd,Xa=Xa,Xd=Xd,DIFF=TRUE)
createX(p=p,na=na,nd=nd,Xa=Xa,Xd=Xd,DIFF=TRUE,base=2)
createX(p=p,na=na,nd=NULL,Xa=Xa,Xd=NULL)
createX(p=p,na=NULL,nd=nd,Xa=NULL,Xd=Xd)
```

customerSat

Customer Satisfaction Data

# Description

Responses to a satisfaction survey for a Yellow Pages advertising product. All responses are on a 10 point scale from 1 to 10 (10 is "Excellent" and 1 is "Poor")

## Usage

data(customerSat)

#### **Format**

A data frame with 1811 observations on the following 10 variables.

- q1 Overall Satisfaction
- q2 Setting Competitive Prices
- q3 Holding Price Increase to a Minimum
- q4 Appropriate Pricing given Volume
- q5 Demonstrating Effectiveness of Purchase
- ${\tt q6}$  Reach a Large # of Customers
- q7 Reach of Advertising
- q8 Long-term Exposure
- q9 Distribution
- q10 Distribution to Right Geographic Areas

#### Source

Rossi et al (2001), "Overcoming Scale Usage Heterogeneity," JASA 96, 20-31.

#### References

```
Case Study 3, Bayesian Statistics and Marketing by Rossi et al. http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html
```

### Examples

```
data(customerSat)
apply(as.matrix(customerSat),2,table)
```

detailing

Physician Detailing Data from Manchanda et al (2004)

# Description

Monthly data on detailing (sales calls) on 1000 physicians. 23 mos of data for each Physician. Includes physician covariates. Dependent Variable (scripts) is the number of new prescriptions ordered by the physician for the drug detailed.

## Usage

```
data(detailing)
```

#### **Format**

```
This R object is a list of two data frames, list(counts,demo).
```

List of 2:

```
$ counts: 'data.frame': 23000 obs. of 4 variables:
```

```
\dots$ id: int [1:23000] 1 1 1 1 1 1 1 1 1 1
```

- ... \$ scripts : int [1:23000] 3 12 3 6 5 2 5 1 5 3
- ...\$ detailing: int [1:23000] 1 1 1 2 1 0 2 2 1 1
- ...\$ lagged\_scripts: int [1:23000] 4 3 12 3 6 5 2 5 1 5

\$ demo :'data.frame': 1000 obs. of 4 variables:

- ...\$ id: int [1:1000] 1 2 3 4 5 6 7 8 9 10
- ...\$ generalphys: int [1:1000] 1 0 1 1 0 1 1 1 1 1
- ...\$ specialist: int [1:1000] 0 1 0 0 1 0 0 0 0
- ...\$ mean\_samples: num [1:1000]  $0.722\ 0.491\ 0.339\ 3.196\ 0.348$

## **Details**

generalphys is dummy for if doctor is a "general practitioner," specialist is dummy for if the physician is a specialist in the theraputic class for which the drug is intended, mean\_samples is the mean number of free drug samples given the doctor over the sample.

### Source

Manchanda, P., P. K. Chintagunta and P. E. Rossi (2004), "Response Modeling with Non-Random Marketing Mix Variables," *Journal of Marketing Research* 41, 467-478.

```
data(detailing)
cat(" table of Counts Dep Var", fill=TRUE)
print(table(detailing$counts[,2]))
cat(" means of Demographic Variables",fill=TRUE)
mat=apply(as.matrix(detailing$demo[,2:4]),2,mean)
print(mat)
## example of processing for use with rhierNegbinRw
if(0)
{
data(detailing)
counts = detailing$counts
Z = detailing$demo
# Construct the Z matrix
Z[,1] = 1
Z[,2]=Z[,2]-mean(Z[,2])
Z[,3]=Z[,3]-mean(Z[,3])
Z[,4]=Z[,4]-mean(Z[,4])
Z=as.matrix(Z)
id=levels(factor(counts$id))
nreg=length(id)
nobs = nrow(counts$id)
regdata=NULL
for (i in 1:nreg) {
    X = counts[counts[,1] == id[i],c(3:4)]
    X = cbind(rep(1,nrow(X)),X)
    y = counts[counts[,1] == id[i],2]
    X = as.matrix(X)
    regdata[[i]]=list(X=X, y=y)
}
nvar=ncol(X)
                        # Number of X variables
                        # Number of Z variables
nz=ncol(Z)
rm(detailing,counts)
cat("Finished Reading data",fill=TRUE)
Data = list(regdata=regdata, Z=Z)
deltabar = matrix(rep(0,nvar*nz),nrow=nz)
Vdelta = 0.01 * diag(nz)
nu = nvar+3
V = 0.01*diag(nvar)
a = 0.5
b = 0.1
Prior = list(deltabar=deltabar, Vdelta=Vdelta, nu=nu, V=V, a=a, b=b)
R = 10000
keep = 1
```

```
s_beta=2.93/sqrt(nvar)
s_alpha=2.93
c=2
Mcmc = list(R=R, keep = keep, s_beta=s_beta, s_alpha=s_alpha, c=c)
out = rhierNegbinRw(Data, Prior, Mcmc)
# Unit level mean beta parameters
Mbeta = matrix(rep(0,nreg*nvar),nrow=nreg)
ndraws = length(out$alphadraw)
for (i in 1:nreg) { Mbeta[i,] = rowSums(out$Betadraw[i, , ])/ndraws }
cat(" Deltadraws ",fill=TRUE)
summary(out$Deltadraw)
cat(" Vbetadraws ",fill=TRUE)
summary(out$Vbetadraw)
cat(" alphadraws ",fill=TRUE)
summary(out$alphadraw)
if(0){
## plotting examples
plot(out$betadraw)
plot(out$alphadraw)
plot(out$Deltadraw)
}
```

eMixMargDen

 $Compute\ Marginal\ Densities\ of\ A\ Normal\ Mixture\ Averaged\ over\\ MCMC\ Draws$ 

# Description

eMixMargDen assumes that a multivariate mixture of normals has been fitted via MCMC (using rnmixGibbs). For each MCMC draw, the marginal densities for each component in the multivariate mixture are computed on a user-supplied grid and then averaged over draws.

## Usage

```
eMixMargDen(grid, probdraw, compdraw)
```

## Arguments

grid array of grid points, grid[,i] are ordinates for ith component

probdraw array - each row of which contains a draw of probabilities of mixture comp

compdraw list of lists of draws of mixture comp moments

### Details

length(compdraw) is number of MCMC draws. compdraw[[i]] is a list draws of mu and inv Chol root for each of mixture components. compdraw[[i]][[j]] is jth component. compdraw[[i]][[j]]\$mu is mean vector; compdraw[[i]][[j]]\$rooti is the UL decomp of  $Sigma^{-1}$ .

## Value

an array of the same dimension as grid with density values.

## Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type. To avoid errors, call with output from **rnmixGibbs**.

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

### See Also

rnmixGibbs

fsh

Flush Console Buffer

# Description

Flush contents of console buffer. This function only has an effect on the Windows GUI.

## Usage

fsh()

## Value

No value is returned.

## Author(s)

 $Peter\ Rossi,\ Graduate\ School\ of\ Business,\ University\ of\ Chicago,\ \langle Peter.Rossi@ChicagoGsb.edu\rangle.$ 

Compute GHK approximation to Multivariate Normal Integrals

## ghkvec

## Description

ghkvec computes the GHK approximation to the integral of a multivariate normal density over a half plane defined by a set of truncation points.

## Usage

```
ghkvec(L, trunpt, above, r)
```

## **Arguments**

L lower triangular Cholesky root of Covariance matrix

trunpt vector of truncation points

above vector of indicators for truncation above (1) or below (0)

r number of draws to use in GHK

#### Value

approximation to integral

# Note

ghkvec can accept a vector of truncations and compute more than one integral. That is, length(trunpt)/length(above) number of different integrals, each with the same Sigma and mean 0 but different truncation points. See example below for an example with two integrals at different truncation points.

#### Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

## References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 2.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

## Examples

##

```
Sigma=matrix(c(1,.5,.5,1),ncol=2)
L=t(chol(Sigma))
trunpt=c(0,0,1,1)
above=c(1,1)
ghkvec(L,trunpt,above,100)
```

llmnl

Evaluate Log Likelihood for Multinomial Logit Model

## Description

11mml evaluates log-likelihood for the multinomial logit model.

## Usage

```
llmnl(beta,y, X)
```

# Arguments

```
beta k \times 1 coefficient vector y n \times 1 vector of obs on y (1, ..., p) X n*p \times k Design matrix (use createX to make)
```

## Details

```
Let mu_i = X_i\beta, then Pr(y_i = j) = exp(mu_{i,j}) / \sum_k exp(mu_{i,k}). X_i is the submatrix of X corresponding to the ith observation. X has n*p rows. Use createX to create X.
```

## Value

value of log-likelihood (sum of log prob of observed multinomial outcomes).

# Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

# Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

#### See Also

```
createX, rmnlIndepMetrop
```

## Examples

```
##
## Not run: ll=llmnl(beta,y,X)
```

llmnp

Evaluate Log Likelihood for Multinomial Probit Model

## Description

11mnp evaluates the log-likelihood for the multinomial probit model.

## Usage

```
llmnp(beta, Sigma, X, y, r)
```

## **Arguments**

beta	k x 1 vector of coefficients
Sigma	(p-1) x (p-1) Covariance matrix of errors
X	X is $n^*(p-1) \times k$ array. X is from differenced system.
У	y is vector of n indicators of multinomial response $(1, \ldots, p)$ .
r	number of draws used in GHK

# Details

```
X is (p-1)*n \times k matrix. Use createX with DIFF=TRUE to create X.
```

```
Model for each obs: w = Xbeta + e. e \sim N(0, Sigma). censoring mechanism: if y = j(j < p), w_j > max(w_{-j}) and w_j > 0 if y = p, w < 0
```

To use GHK, we must transform so that these are rectangular regions e.g. if  $y = 1, w_1 > 0$  and  $w_1 - w_{-1} > 0$ .

Define  $A_j$  such that if j=1,...,p-1,  $A_jw=A_jmu+A_je>0$  is equivalent to y=j. Thus, if y=j, we have  $A_je>-A_jmu$ . Lower truncation is  $-A_jmu$  and  $cov=A_jSigmat(A_j)$ . For  $j=p,\ e<-mu$ .

## Value

value of log-likelihood (sum of log prob of observed multinomial outcomes).

## Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapters 2 and 4.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

## See Also

```
createX, rmnpGibbs
```

## Examples

```
##
## Not run: ll=llmnp(beta,Sigma,X,y,r)
```

llnhlogit

Evaluate Log Likelihood for non-homothetic Logit Model

## Description

11mnp evaluates log-likelihood for the Non-homothetic Logit model.

#### Usage

```
llnhlogit(theta, choice, lnprices, Xexpend)
```

# Arguments

theta parameter vector (see details section) choice  $n \times 1$  vector of choice  $(1, \ldots, p)$ 

Xexpend n x d array of vars predicting expenditure

#### **Details**

```
Non-homothetic logit model with: ln(psi_i(U)) = alpha_i - e^{k_i}U
```

```
Structure of theta vector alpha: (p \times 1) vector of utility intercepts. k: (p \times 1) vector of utility rotation parms. gamma: (k \times 1) – expenditure variable coefs. tau: (1 \times 1) – logit scale parameter.
```

## Value

value of log-likelihood (sum of log prob of observed multinomial outcomes).

# Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

# Author(s)

Peter Rossi, Graduate School of Business, University of Chicago (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and Mc-Culloch, Chapter 4.

```
http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html
```

# See Also

```
simnhlogit
```

## Examples

```
##
## Not run: ll=llnhlogit(theta,choice,lnprices,Xexpend)
```

lndIChisq

Compute Log of Inverted Chi-Squared Density

## Description

lndIChisq computes the log of an Inverted Chi-Squared Density.

## Usage

```
lndIChisq(nu, ssq, x)
```

## **Arguments**

nu d.f. parameter ssq scale parameter

x ordinate for density evaluation

#### Details

```
Z = \nu * ssq/\chi^2_{\nu}, \ Z \sim Inverted Chi-Squared.
lndIChisq computes the complete log-density, including normalizing constants.
```

# Value

log density value

# Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

# Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 2.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

## See Also

dchisq

## Examples

##

lndIChisq(3,1,2)

lndIWishart

Compute Log of Inverted Wishart Density

# Description

lndIWishart computes the log of an Inverted Wishart density.

## Usage

```
lndIWishart(nu, V, IW)
```

## Arguments

nu d.f. parameter

V "location" parameter

IW ordinate for density evaluation

## **Details**

```
Z \sim \text{Inverted Wishart(nu,V)}. in this parameterization, E[Z] = 1/(nu-k-1)V, V is a k x k matrix lndlWishart computes the complete log-density, including normalizing constants.
```

## Value

log density value

## Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

## References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 2.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

## See Also

rwishart

## Examples

```
##
```

lndIWishart(5,diag(3),(diag(3)+.5))

# Description

lndMvn computes the log of a Multivariate Normal Density.

# Usage

```
lndMvn(x, mu, rooti)
```

## Arguments

x density ordinatemu vector

rooti inv of Upper Triangular Cholesky root of Sigma

## Details

```
z \sim N(mu, \Sigma)
```

#### Value

log density value

## Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 2.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

## See Also

## lndMvst

```
##
Sigma=matrix(c(1,.5,.5,1),ncol=2)
lndMvn(x=c(rep(0,2)),mu=c(rep(0,2)),rooti=backsolve(chol(Sigma),diag(2)))
```

Compute Log of Multivariate Student-t Density

## lndMvst

## Description

lndMvst computes the log of a Multivariate Student-t Density.

## Usage

```
lndMvst(x, nu, mu, rooti,NORMC)
```

## Arguments

x density ordinatenu d.f. parametermu vector

rooti inv of Cholesky root of Sigma

NORMC include normalizing constant, def: FALSE

## **Details**

```
z \sim MVst(mu, nu, \Sigma)
```

## Value

log density value

## Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

## Author(s)

 $Peter\ Rossi,\ Graduate\ School\ of\ Business,\ University\ of\ Chicago,\ \langle Peter.Rossi@ChicagoGsb.edu\rangle.$ 

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 2.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

# See Also

lndMvn

## Examples

```
##
```

```
Sigma=matrix(c(1,.5,.5,1),ncol=2)
lndMvst(x=c(rep(0,2)),nu=4,mu=c(rep(0,2)),rooti=backsolve(chol(Sigma),diag(2)))
```

logMargDenNR

Compute Log Marginal Density Using Newton-Raftery Approx

## Description

 ${\tt logMargDenNR}$  computes log marginal density using the Newton-Raftery approximation. Note: this approximation can be influenced by outliers in the vector of log-likelihoods. Use with  ${\tt care}$ .

## Usage

logMargDenNR(11)

## **Arguments**

11

vector of log-likelihoods evaluated at length(ll) MCMC draws

## Value

approximation to log marginal density value.

## Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

# Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

## References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 6.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

## Description

Panel data on purchases of margarine by 516 households. Demographic variables are included.

## Usage

data(margarine)

#### **Format**

This is an R object that is a list of two data frames, list(choicePrice,demos)

List of 2

\$ choicePrice:'data.frame': 4470 obs. of 12 variables:

- ...\$ hhid: int [1:4470] 2100016 2100016 2100016 2100016
- ...\$ choice : num [1:4470] 1 1 1 1 1 4 1 1 4 1
- ...\$ PPk\_Stk: num [1:4470] 0.66 0.63 0.29 0.62 0.5 0.58 0.29
- ...\$ PBB\_Stk : num [1:4470]  $0.67 \ 0.67 \ 0.5 \ 0.61 \ 0.58 \ 0.45 \ 0.51$
- ...\$ PFLStk : num [1:4470] 1.09 0.99 0.99 0.99 0.99 0.99 0.99
- ...\$ PHse\_Stk: num [1:4470] 0.57 0.57 0.57 0.57 0.45 0.45 0.29
- ...\$ PGen\_Stk: num [1:4470] 0.36 0.36 0.36 0.36 0.33 0.33 0.33
- ...\$ PImp\_Stk: num [1:4470] 0.93 1.03 0.69 0.75 0.72 0.72 0.72
- ...\$ PSS\_Tub : num [1:4470] 0.85 0.85 0.79 0.85 0.85 0.85 0.85
- ...\$ PPk\_Tub: num [1:4470] 1.09 1.09 1.09 1.09 1.07 1.07 1.07
- ...\$ PFL\_Tub : num [1:4470] 1.19 1.19 1.19 1.19 1.19 1.19
- ...\$ PHse\_Tub: num [1:4470] 0.33 0.37 0.59 0.59 0.59 0.59 0.59

Pk is Parkay; BB is BlueBonnett, Fl is Fleischmanns, Hse is house, Gen is generic, Imp is Imperial, SS is Shed Spread. \_Stk indicates stick, \_Tub indicates Tub form.

\$ demos :'data.frame': 516 obs. of 8 variables:

- ...\$ hhid: num [1:516] 2100016 2100024 2100495 2100560
- ...\$ Income: num [1:516] 32.5 17.5 37.5 17.5 87.5 12.5
- ...\$ Fs3\_4: int [1:516] 0 1 0 0 0 0 0 0 0 0
- $\dots$ \$ Fs5: int [1:516] 0 0 0 0 0 0 0 0 1 0
- ...\$ Fam\_Size : int [1:516] 2 3 2 1 1 2 2 2 5 2
- $\dots$ \$ college: int [1:516] 1 1 0 0 1 0 1 0 1 1
- $\dots$ \$ whtcollar: int [1:516] 0 1 0 1 1 0 0 0 1 1
- ...\$ retired: int [1:516] 1 1 1 0 0 1 0 1 0 0

Fs3\_4 is dummy (family size 3-4). Fs5 is dummy for family size >= 5. college,whtcollar,retired are dummies reflecting these statuses.

#### **Details**

choice is a multinomial indicator of one of the 10 brands (in order listed under format). All prices are in \$.

#### Source

Allenby and Rossi (1991), "Quality Perceptions and Asymmetric Switching Between Brands," *Marketing Science* 10, 185-205.

#### References

Chapter 5, *Bayesian Statistics and Marketing* by Rossi et al. http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

```
data(margarine)
cat(" Table of Choice Variable ",fill=TRUE)
print(table(margarine$choicePrice[,2]))
cat(" Means of Prices",fill=TRUE)
mat=apply(as.matrix(margarine$choicePrice[,3:12]),2,mean)
print(mat)
cat(" Quantiles of Demographic Variables",fill=TRUE)
mat=apply(as.matrix(margarine$demos[,2:8]),2,quantile)
print(mat)
##
## example of processing for use with rhierMnlRwMixture
##
if(0)
select= c(1:5,7) ## select brands
chPr=as.matrix(margarine$choicePrice)
## make sure to log prices
chPr=cbind(chPr[,1],chPr[,2],log(chPr[,2+select]))
demos=as.matrix(margarine$demos[,c(1,2,5)])
## remove obs for other alts
chPr=chPr[chPr[,2] <= 7,]
chPr=chPr[chPr[,2] != 6,]
## recode choice
chPr[chPr[,2] == 7,2]=6
hhidl=levels(as.factor(chPr[,1]))
lgtdata=NULL
nlgt=length(hhidl)
p=length(select) ## number of choice alts
for (i in 1:nlgt) {
   nobs=sum(chPr[,1]==hhidl[i])
   if(nobs >=5) {
```

```
data=chPr[chPr[,1]==hhidl[i],]
      y=data[,2]
      names(y)=NULL
      X=createX(p=p,na=1,Xa=data[,3:8],nd=NULL,Xd=NULL,INT=TRUE,base=1)
       lgtdata[[ind]]=list(y=y,X=X,hhid=hhidl[i]); ind=ind+1
}
nlgt=length(lgtdata)
## now extract demos corresponding to hhs in lgtdata
##
Z=NULL
nlgt=length(lgtdata)
for(i in 1:nlgt){
   Z=rbind(Z,demos[demos[,1]==lgtdata[[i]]$hhid,2:3])
}
##
## take log of income and family size and demean
##
Z = log(Z)
Z[,1]=Z[,1]-mean(Z[,1])
Z[,2]=Z[,2]-mean(Z[,2])
keep=5
R=20000
mcmc1=list(keep=keep,R=R)
out=rhierMnlRwMixture(Data=list(p=p,lgtdata=lgtdata,Z=Z),Prior=list(ncomp=1),Mcmc=mcmc1)
summary(out$Deltadraw)
summary(out$nmix)
if(0){
## plotting examples
plot(out$nmix)
plot(out$Deltadraw)}
}
```

mixDen

Compute Marginal Density for Multivariate Normal Mixture

## Description

mixDen computes the marginal density for each component of a normal mixture at each of the points on a user-specifed grid.

## Usage

```
mixDen(x, pvec, comps)
```

## Arguments

x array - ith column gives grid points for ith variable

pvec vector of mixture component probabilites

comps list of lists of components for normal mixture

## **Details**

length(comps) is the number of mixture components. comps[[j]] is a list of parameters of the jth component. comps[[j]]\$mu is mean vector; comps[[j]]\$rooti is the UL decomp of  $Sigma^{-1}$ .

#### Value

an array of the same dimension as grid with density values.

## Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

# Author(s)

Peter Rossi, Graduate School of Business, University of Chicago (Peter.Rossi@ChicagoGsb.edu).

## References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 3.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

## See Also

rnmixGibbs

```
## Not run:
##
## see examples in rnmixGibbs documentation
##
## End(Not run)
```

## Description

mixDenBi computes the implied bivariate marginal density from a mixture of normals with specified mixture probabilities and component parameters.

# Usage

```
mixDenBi(i, j, xi, xj, pvec, comps)
```

## Arguments

i	index of first variable
j	index of second variable
xi	grid of values of first variable
хj	grid of values of second variable
pvec	normal mixture probabilities
comps	list of lists of components

#### Details

length(comps) is the number of mixture components. comps[[j]] is a list of parameters of the jth component. comps[[j]]\$mu is mean vector; comps[[j]]\$rooti is the UL decomp of  $Sigma^{-1}$ .

## Value

```
an array (length(xi)=length(xj) x 2) with density value
```

# Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

# Author(s)

Peter Rossi, Graduate School of Business, University of Chicago (Peter.Rossi@ChicagoGsb.edu).

# References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 3.

```
http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html
```

## See Also

```
rnmixGibbs, mixDen
```

## Examples

```
## Not run:
##
## see examples in rnmixGibbs documentation
##
## End(Not run)
```

mnlHess

Computes -Expected Hessian for Multinomial Logit

# Description

mnlHess computes -Expected[Hessian] for Multinomial Logit Model

# Usage

```
mnlHess(beta,y, X)
```

## Arguments

```
beta k \times 1 vector of coefficients  y \qquad \qquad n \times 1 \text{ vector of choices, } (1, \dots, p)   x \qquad \qquad n^*p \times k \text{ Design matrix}
```

## Details

See llmnl for information on structure of X array. Use createX to make X.

#### Value

k x k matrix

# Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

# Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 3.

```
http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html
```

#### See Also

```
llmnl, createX, rmnlIndepMetrop
```

## Examples

```
##
## Not run: mnlHess(beta,y,X)
```

mnpProb

Compute MNP Probabilities

## Description

mnpProb computes MNP probabilities for a given X matrix corresponding to one observation. This function can be used with output from rmnpGibbs to simulate the posterior distribution of market shares or fitted probabilities.

# Usage

```
mnpProb(beta, Sigma, X, r)
```

## Arguments

beta MNP coefficients

Sigma Covariance matrix of latents

X X array for one observation – use createX to make

r number of draws used in GHK (def: 100)

## **Details**

see rmnpGibbs for definition of the model and the interpretation of the beta, Sigma parameters. Uses the GHK method to compute choice probabilities. To simulate a distribution of probabilities, loop over the beta, Sigma draws from rmnpGibbs output.

#### Value

p x 1 vector of choice probabilites

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see  $Bayesian\ Statistics\ and\ Marketing\$ by Rossi, Allenby and McCulloch, Chapters 2 and 4.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

#### See Also

```
rmnpGibbs, createX
```

#### Examples

```
##
## example of computing MNP probabilites
## here I'm thinking of Xa as having the prices of each of the 3 alternatives
Xa=matrix(c(1,.5,1.5),nrow=1)
X=createX(p=3,na=1,nd=NULL,Xa=Xa,Xd=NULL,DIFF=TRUE)
beta=c(1,-1,-2)  ## beta contains two intercepts and the price coefficient
Sigma=matrix(c(1,.5,.5,1),ncol=2)
mnpProb(beta,Sigma,X)
```

momMix

Compute Posterior Expectation of Normal Mixture Model Moments

# Description

momMix averages the moments of a normal mixture model over MCMC draws.

## Usage

```
momMix(probdraw, compdraw)
```

## Arguments

probdraw R x ncomp list of draws of mixture probs

compdraw list of length R of draws of mixture component moments

# Details

R is the number of MCMC draws in argument list above. ncomp is the number of mixture components fitted.

compdraw is a list of lists of lists with mixture components.

compdraw[[i]] is ith draw.

compdraw[[i]][[j]][[1]] is the mean parameter vector for the jth component, ith MCMC draw. compdraw[[i]][[j]][[2]] is the UL decomposition of  $Sigma^{-1}$  for the jth component, ith MCMC draw.

#### Value

a list of the following items ...

mu Posterior Expectation of Mean

sigma Posterior Expecation of Covariance Matrix

sd Posterior Expectation of Vector of Standard Deviations

corr Posterior Expectation of Correlation Matrix

## Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 5.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

## See Also

rmixGibbs

nmat

Convert Covariance Matrix to a Correlation Matrix

## Description

nmat converts a covariance matrix (stored as a vector, col by col) to a correlation matrix (also stored as a vector).

#### Usage

nmat(vec)

#### **Arguments**

vec k x k Cov ma

k x k Cov matrix stored as a k\*k x 1 vector (col by col)

### Details

This routine is often used with apply to convert an  $R \times (k*k)$  array of covariance MCMC draws to correlations. As in corrdraws=apply(vardraws,1,nmat)

#### Value

k\*k x 1 vector with correlation matrix

## Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

# Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

## Examples

```
##
set.seed(66)
X=matrix(rnorm(200,4),ncol=2)
Varmat=var(X)
nmat(as.vector(Varmat))
```

numEff

Compute Numerical Standard Error and Relative Numerical Efficiency

## Description

numEff computes the numerical standard error for the mean of a vector of draws as well as the relative numerical efficiency (ratio of variance of mean of this time series process relative to iid sequence).

## Usage

```
numEff(x, m = as.integer(min(length(x), (100/sqrt(5000)) * sqrt(length(x)))))
```

# Arguments

x R x 1 vector of draws

m number of lags for autocorrelations

#### Details

default for number of lags is chosen so that if R = 5000, m = 100 and increases as the sqrt(R).

#### Value

stderr standard error of the mean of x

f variance ratio (relative numerical efficiency)

## Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 3.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

### Examples

```
numEff(rnorm(1000),m=20)
numEff(rnorm(1000))
```

orangeJuice

Store-level Panel Data on Orange Juice Sales

## Description

yx, weekly sales of refrigerated orange juice at 83 stores. storedemo, contains demographic information on those stores.

### Usage

```
data(orangeJuice)
```

### Format

This R object is a list of two data frames, list(yx,storedemo).

```
List of 2
```

```
...$ price5 : num [1:106139] 0.0495 0.0495 0.0373 0.0495 0.0495
...$ price6: num [1:106139] 0.0530 0.0478 0.0530 0.0530 0.0530
...$ price7: num [1:106139] 0.0389 0.0458 0.0458 0.0458 0.0466
...$ price8: num [1:106139] 0.0414 0.0280 0.0414 0.0414 0.0414
...$ price9: num [1:106139] 0.0289 0.0430 0.0481 0.0423 0.0423
...$ price10: num [1:106139] 0.0248 0.0420 0.0327 0.0327 0.0327
...$ price11 : num [1:106139] 0.0390 0.0390 0.0390 0.0390 0.0382
...$ deal: int [1:106139] 1 0 0 0 0 0 1 1 1 1
\dots$ feat: num [1:106139] 0 0 0 0 0 0 0 0 0 0
...$ profit: num [1:106139] 38.0 30.1 30.0 29.9 29.9
1 Tropicana Premium 64 oz; 2 Tropicana Premium 96 oz; 3 Florida's Natural 64 oz;
4 Tropicana 64 oz; 5 Minute Maid 64 oz; 6 Minute Maid 96 oz;
7 Citrus Hill 64 oz; 8 Tree Fresh 64 oz; 9 Florida Gold 64 oz;
10 Dominicks 64 oz: 11 Dominicks 128 oz.
$ storedemo:'data.frame': 83 obs. of 12 variables:
...$ STORE: int [1:83] 2 5 8 9 12 14 18 21 28 32
...$ AGE60: num [1:83] 0.233 0.117 0.252 0.269 0.178
...$ EDUC: num [1:83] 0.2489 0.3212 0.0952 0.2222 0.2534
...$ ETHNIC: num [1:83] 0.1143 0.0539 0.0352 0.0326 0.3807
...$ INCOME: num [1:83] 10.6 10.9 10.6 10.8 10.0
...$ HHLARGE: num [1:83] 0.1040 0.1031 0.1317 0.0968 0.0572
...$ WORKWOM : num [1:83] 0.304 0.411 0.283 0.359 0.391
...$ HVAL150: num [1:83] 0.4639 0.5359 0.0542 0.5057 0.3866
...$ SSTRDIST: num [1:83] 2.11 3.80 2.64 1.10 9.20
...$ SSTRVOL: num [1:83] 1.143 0.682 1.500 0.667 1.111
...$ CPDIST5: num [1:83] 1.93 1.60 2.91 1.82 0.84
```

### **Details**

store store number
brand brand indicator
week week number
logmove log of the number of units sold
constant a vector of 1
price1 price of brand 1
deal in-store coupon activity
feature feature advertisement
STORE store number
AGE60 percentage of the population that is aged 60 or older
EDUC percentage of the population that is black or Hispanic

...\$ CPWVOL5: num [1:83] 0.377 0.736 0.641 0.441 0.106

```
INCOME median income

HHLARGE percentage of households with 5 or more persons

WORKWOM percentage of women with full-time jobs

HVAL150 percentage of households worth more than $150,000

SSTRDIST distance to the nearest warehouse store

SSTRVOL ratio of sales of this store to the nearest warehouse store

CPDIST5 average distance in miles to the nearest 5 supermarkets

CPWVOL5 ratio of sales of this store to the average of the nearest five stores
```

### Source

Alan L. Montgomery (1997), "Creating Micro-Marketing Pricing Strategies Using Supermarket Scanner Data," *Marketing Science* 16(4) 315-337.

#### References

```
Chapter 5, Bayesian Statistics and Marketing by Rossi et al. http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html
```

```
## Example
## load data
data(orangeJuice)
## print some quantiles of yx data
cat("Quantiles of the Variables in yx data",fill=TRUE)
mat=apply(as.matrix(orangeJuice$yx),2,quantile)
print(mat)
## print some quantiles of storedemo data
cat("Quantiles of the Variables in storedemo data",fill=TRUE)
mat=apply(as.matrix(orangeJuice$storedemo),2,quantile)
print(mat)
## Example 2 processing for use with rhierLinearModel
##
##
if(0)
## select brand 1 for analysis
brand1=orangeJuice$yx[(orangeJuice$yx$brand==1),]
store = sort(unique(brand1$store))
nreg = length(store)
nvar=14
regdata=NULL
```

```
for (reg in 1:nreg) {
        y=brand1$logmove[brand1$store==store[reg]]
        iota=c(rep(1,length(y)))
        X=cbind(iota,log(brand1$price1[brand1$store==store[reg]]),
                     log(brand1$price2[brand1$store==store[reg]]),
                     log(brand1$price3[brand1$store==store[reg]]),
                     log(brand1$price4[brand1$store==store[reg]]),
                     log(brand1$price5[brand1$store==store[reg]]),
                     log(brand1$price6[brand1$store==store[reg]]),
                     log(brand1$price7[brand1$store==store[reg]]),
                     log(brand1$price8[brand1$store==store[reg]]),
                     log(brand1$price9[brand1$store==store[reg]]),
                     log(brand1$price10[brand1$store==store[reg]]),
                     log(brand1$price11[brand1$store==store[reg]]),
                     brand1$deal[brand1$store==store[reg]],
                     brand1$feat[brand1$store==store[reg]])
        regdata[[reg]]=list(y=y,X=X)
## storedemo is standardized to zero mean.
Z=as.matrix(orangeJuice$storedemo[,2:12])
dmean=apply(Z,2,mean)
for (s in 1:nreg){
        Z[s,]=Z[s,]-dmean
iotaz=c(rep(1,nrow(Z)))
Z=cbind(iotaz,Z)
nz=ncol(Z)
Data=list(regdata=regdata,Z=Z)
Mcmc=list(R=R,keep=1)
out=rhierLinearModel(Data=Data,Mcmc=Mcmc)
summary(out$Deltadraw)
summary(out$Vbetadraw)
## plotting examples
plot(out$betadraw)
}
}
```

plot.bayesm.hcoef Plot Method for Hierarchical Model Coefs

## Description

plot.bayesm.hcoef is an S3 method to plot 3 dim arrays of hierarchical coefficients. Arrays are of class bayesm.hcoef with dimensions: cross-sectional unit x coef x MCMC draw.

### Usage

```
## S3 method for class 'bayesm.hcoef':
plot(x,burnin,...)
```

## **Arguments**

x An object of S3 class, bayesm.hcoef burnin no draws to burnin, def: .1\*R ... standard graphics parameters

#### **Details**

Typically, plot.bayesm.hcoef will be invoked by a call to the generic plot function as in plot(object) where object is of class bayesm.hcoef. All of the bayesm hierarchical routines return draws of hierarchical coefficients in this class (see example below). One can also simply invoke plot.bayesm.hcoef on any valid 3-dim array as in plot.bayesm.hcoef (betadraws)

plot.bayesm.hcoef is also exported for use as a standard function, as in plot.bayesm.hcoef(array).

### Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### See Also

rhierMnlRwMixture,rhierLinearModel, rhierLinearMixture,rhierNegbinRw

```
##
## not run
# out=rhierLinearModel(Data,Prior,Mcmc)
# plot(out$betadraws)
#
```

Plot Method for Arrays of MCMC Draws

plot.bayesm.mat

### Description

plot.bayesm.mat is an S3 method to plot arrays of MCMC draws. The columns in the array correspond to parameters and the rows to MCMC draws.

## Usage

```
## S3 method for class 'bayesm.mat':
plot(x,names,burnin,tvalues,TRACEPLOT,DEN,INT, ...)
```

### Arguments

x An object of either S3 class, bayesm.mat, or S3 class, mcmc

names optional character vector of names for coefficients

burnin number of draws to discard for burn-in, def: .1\*nrow(X)

tvalues vector of true values

TRACEPLOT logical, TRUE provide sequence plots of draws and acfs, def: TRUE

DEN logical, TRUE use density scale on histograms, def: TRUE

INT logical, TRUE put various intervals and points on graph, def: TRUE

... standard graphics parameters

#### **Details**

Typically, plot.bayesm.mat will be invoked by a call to the generic plot function as in plot(object) where object is of class bayesm.mat. All of the bayesm MCMC routines return draws in this class (see example below). One can also simply invoke plot.bayesm.mat on any valid 2-dim array as in plot.bayesm.mat(betadraws).

```
plot.bayesm.mat paints (by default) on the histogram:
```

```
green "[]" delimiting 95% Bayesian Credibility Interval yellow "()" showing \pm 2 numerical standard errors red "|" showing posterior mean
```

plot.bayesm.mat is also exported for use as a standard function, as in plot.bayesm.mat(matrix)

### Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

## Examples

```
##
## not run
# out=runiregGibbs(Data,Prior,Mcmc)
# plot(out$betadraw)
#
```

plot.bayesm.nmix

Plot Method for MCMC Draws of Normal Mixtures

## Description

plot.bayesm.nmix is an S3 method to plot aspects of the fitted density from a list of MCMC draws of normal mixture components. Plots of marginal univariate and bivariate densities are produced.

# Usage

```
## S3 method for class 'bayesm.nmix':
plot(x,names,burnin,Grid,bi.sel,nstd, ...)
```

### Arguments

x	An object of either S3 class, bayesm.nmix, or S3 class, mcmc
names	optional character vector of names for each of the dimensions
burnin	number of draws to discard for burn-in, def: $.1*nrow(X)$
Grid	matrix of grid points for densities, def: mean $+/-$ nstd std deviations
bi.sel	list of vectors, each giving pairs for bivariate distributions, def: $\operatorname{list}(c(1,2))$
nstd	number of standard deviations for default Grid, def: 2
	standard graphics parameters

## Details

Typically, plot.bayesm.nmix will be invoked by a call to the generic plot function as in plot(object) where object is of class bayesm.nmix. These objects are lists of three components. The first component is an array of draws of mixture component probabilties. The second component is not used. The third is a lists of lists with draws of each of the normal components.

plot.bayesm.nmix can also be used as a standard function, as in plot.bayesm.nmix(list).

## Author(s)

 $Peter\ Rossi,\ Graduate\ School\ of\ Business,\ University\ of\ Chicago,\ \langle Peter.Rossi@ChicagoGsb.edu\rangle.$ 

#### See Also

### rnmixGibbs, rhierMnlRwMixture, rhierLinearMixture

### Examples

```
##
## not run
# out=rnmix(Data,Prior,Mcmc)
# plot(out,bi.sel=list(c(1,2),c(3,4),c(1,3)))
# plot bivariate distributions for dimension 1,2; 3,4; and 1,3
#
```

rbiNormGibbs

Illustrate Bivariate Normal Gibbs Sampler

## Description

rbiNormGibbs implements a Gibbs Sampler for the bivariate normal distribution. Intermediate moves are shown and the output is contrasted with the iid sampler. i This function is designed for illustrative/teaching purposes.

### Usage

```
rbiNormGibbs(initx = 2, inity = -2, rho, burnin = 100, R = 500)
```

### Arguments

initx initial value of parameter on x axis (def: 2)
inity initial value of parameter on y axis (def: -2)
rho correlation for bivariate normals
burnin burn-in number of draws (def:100)
R number of MCMC draws (def:500)

### **Details**

```
(theta1,theta2) N((0,0), Sigma=matrix(c(1,rho,rho,1),ncol=2))
```

### Value

R x 2 array of draws

## Author(s)

 $Peter Rossi, Graduate School of Business, University of Chicago, \\ \langle Peter.Rossi@ChicagoGsb.edu \rangle.$ 

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapters 2 and 3.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

# Examples

```
##
## Not run: out=rbiNormGibbs(rho=.95)
```

rbprobitGibbs

Gibbs Sampler (Albert and Chib) for Binary Probit

## Description

rbprobitGibbs implements the Albert and Chib Gibbs Sampler for the binary probit model.

### Usage

```
rbprobitGibbs(Data, Prior, Mcmc)
```

### Arguments

Data list(X,y)

Prior list(betabar,A)Mcmc list(R,keep)

### **Details**

Model:  $z = X\beta + e$ .  $e \sim N(0, I)$ . y=1, if z> 0.

Prior:  $\beta \sim N(betabar, A^{-1})$ .

List arguments contain

X Design Matrix

y n x 1 vector of observations, (0 or 1)

betabar k x 1 prior mean (def: 0)

A k x k prior precision matrix (def: .01I)

R number of MCMC draws

keep thinning parameter - keep every keepth draw (def: 1)

#### Value

betadraw R/keep x k array of betadraws

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 3.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

### See Also

rmnpGibbs

```
##
## rbprobitGibbs example
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}
set.seed(66)
simbprobit=
function(X,beta) {
## function to simulate from binary probit including x variable
y=ifelse((X%*%beta+rnorm(nrow(X)))<0,0,1)</pre>
list(X=X,y=y,beta=beta)
nobs=200
X=cbind(rep(1,nobs),runif(nobs),runif(nobs))
beta=c(0,1,-1)
nvar=ncol(X)
simout=simbprobit(X,beta)
Data1=list(X=simout$X,y=simout$y)
Mcmc1=list(R=R,keep=1)
out=rbprobitGibbs(Data=Data1,Mcmc=Mcmc1)
summary(out$betadraw,tvalues=beta)
if(0){
## plotting example
plot(out$betadraw,tvalues=beta)
```

Draw From Dirichlet Distribution

### rdirichlet

## Description

rdirichlet draws from Dirichlet

### Usage

```
rdirichlet(alpha)
```

### **Arguments**

alpha

vector of Dirichlet parms (must be > 0)

### Value

Vector of draws from Dirichlet

## Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

## Author(s)

 $Peter Rossi, Graduate School of Business, University of Chicago, \\ \langle Peter.Rossi@ChicagoGsb.edu \rangle.$ 

## References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 2.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

```
##
set.seed(66)
rdirichlet(c(rep(3,5)))
```

## Description

rhierBinLogit implements an MCMC algorithm for hierarchical binary logits with a normal heterogeneity distribution. This is a hybrid sampler with a RW Metropolis step for unit-level logit parameters.

rhierBinLogit is designed for use on choice-based conjoint data with partial profiles. The Design matrix is based on differences of characteristics between two alternatives. See Appendix A of Bayesian Statistics and Marketing for details.

## Usage

```
rhierBinLogit(Data, Prior, Mcmc)
```

### Arguments

```
Data
                  list(lgtdata,Z) (note: Z is optional)
                  list(Deltabar, ADelta, nu, V) (note: all are optional)
Prior
                  list(sbeta,R,keep) (note: all but R are optional)
Mcmc
```

### **Details**

```
Model:
             y_{hi} = 1 with pr = exp(x'_{hi}beta_h)/(1 + exp(x'_{hi}beta_h)). beta_h is nvar x 1.
             h=1,...,length(lgtdata) units or "respondents" for survey data.
             beta_h = \text{ZDelta[h,]} + u_h.
             Note: here ZDelta refers to Z%*%Delta, ZDelta[h,] is hth row of this product.
             Delta is an nz x nvar array.
             u_h \sim N(0, V_{beta}).
             Priors:
             delta = vec(Delta) \sim N(vec(Deltabar), V_{beta}(x)ADelta^{-1})
             V_{beta} \sim IW(nu, V)
             Lists contain:
        lgtdata list of lists with each cross-section unit MNL data
lgtdata[[h]]$y n_h vector of binary outcomes (0,1)
lgtdata[[h]] X n_h by nvar design matrix for hth unit
       Deltabar nz x nvar matrix of prior means (def: 0)
          ADelta prior prec matrix (def: .01I)
               nu d.f. parm for IW prior on norm comp Sigma (def: nvar+3)
```

```
V pds location parm for IW prior on norm comp Sigma (def: nuI)
sbeta scaling parm for RW Metropolis (def: .2)
R number of MCMC draws
keep MCMC thinning parm: keep every keepth draw (def: 1)
```

#### Value

a list containing:

Deltadraw R/keep x nz\*nvar matrix of draws of Delta
betadraw nlgt x nvar x R/keep array of draws of betas
Vbetadraw R/keep x nvar\*nvar matrix of draws of Vbeta

11ike R/keep vector of log-like values

reject R/keep vector of reject rates over nlgt units

#### Note

Some experimentation with the Metropolis scaling paramter (sbeta) may be required.

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 5.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

### See Also

### rhierMnlRwMixture

```
Vbeta=diag(nvar)+.5*iota%*%t(iota)
## simulate data
lgtdata=NULL
for (i in 1:nlgt)
{ beta=t(Delta)%*%Z[i,]+as.vector(t(chol(Vbeta))%*%rnorm(nvar))
 X=matrix(runif(nobs*nvar),nrow=nobs,ncol=nvar)
 prob=exp(X%*%beta)/(1+exp(X%*%beta))
 unif=runif(nobs,0,1)
  y=ifelse(unif<prob,1,0)
 lgtdata[[i]]=list(y=y,X=X,beta=beta)
}
out=rhierBinLogit(Data=list(lgtdata=lgtdata,Z=Z),Mcmc=list(R=R))
cat("Summary of Delta draws",fill=TRUE)
summary(out$Deltadraw,tvalues=as.vector(Delta))
cat("Summary of Vbeta draws",fill=TRUE)
summary(out$Vbetadraw,tvalues=as.vector(Vbeta[upper.tri(Vbeta,diag=TRUE)]))
if(0){
## plotting examples
plot(out$Deltadraw,tvalues=as.vector(Delta))
plot(out$betadraw)
plot(out$Vbetadraw,tvalues=as.vector(Vbeta[upper.tri(Vbeta,diag=TRUE)]))
```

rhierLinearMixture

Gibbs Sampler for Hierarchical Linear Model

# Description

rhierLinearMixture implements a Gibbs Sampler for hierarchical linear models with a mixture of normals prior.

### Usage

```
rhierLinearMixture(Data, Prior, Mcmc)
```

### Arguments

Data list(regdata,Z) (Z optional).

Prior list(deltabar,Ad,mubar,Amu,nu,V,nu.e,ssq,ncomp) (all but ncomp are op-

tional).

Mcmc list(R, keep) (R required).

### **Details**

```
Model: length(regdata) regression equations.
             y_i = X_i beta_i + e_i. e_i \sim N(0, tau_i). nvar X vars in each equation.
             Priors:
             tau_i \sim \text{nu.e}^* ssq_i/\chi^2_{nu.e}. tau_i is the variance of e_i.
             beta_i = \text{ZDelta[i,]} + u_i.
             Note: here ZDelta refers to Z%*%D, ZDelta[i,] is ith row of this product.
             Delta is an nz x nvar array.
             u_i \sim N(mu_{ind}, Sigma_{ind}). ind \sim multinomial(pvec).
             pvec \sim \text{dirichlet (a)}
             delta = vec(Delta) \sim N(deltabar, A_d^{-1})
             mu_i \sim N(mubar, Sigma_i(x)Amu^{-1})
             Sigma_i \sim IW(nu,V)
             List arguments contain:
        regdata list of lists with X,y matrices for each of length(regdata) regressions
regdata[[i]]$X X matrix for equation i
regdata[[i]]$y y vector for equation i
       deltabar nz*nvar vector of prior means (def: 0)
               Ad prior prec matrix for vec(Delta) (def: .01I)
           mubar nvar x 1 prior mean vector for normal comp mean (def: 0)
             Amu prior precision for normal comp mean (def: .01I)
              nu d.f. parm for IW prior on norm comp Sigma (def: nvar+3)
                V pds location parm for IW prior on norm comp Sigma (def: nuI)
            nu.e d.f. parm for regression error variance prior (def: 3)
             ssq scale parm for regression error var prior (def: var(y_i))
           ncomp number of components used in normal mixture
                R number of MCMC draws
            keep MCMC thinning parm: keep every keepth draw (def: 1)
         Value
             a list containing
             taudraw
                               R/keep x nreg array of error variance draws
             betadraw
                               nreg x nvar x R/keep array of individual regression coef draws
                               R/keep x nz x nvar array of Deltadraws
             Deltadraw
             nmix
                               list of three elements, (probdraw, NULL, compdraw)
```

#### Note

More on probdraw component of nmix return value list: this is an R/keep by ncomp array of draws of mixture component probs (pvec) More on compdraw component of nmix return value list:

```
compdraw[[i ]] the ith draw of components for mixtures

compdraw[[i ][[j]]] ith draw of the jth normal mixture comp

compdraw[[i ][[j]][[1]]] ith draw of jth normal mixture comp mean vector

compdraw[[i ][[j]][[2]]] ith draw of jth normal mixture cov parm (rooti)

Note: Z should not include an intercept and should be centered for ease of interpretation.
```

Be careful in assessing prior parameter, Amu. .01 can be too small for some applications. See Rossi et al, chapter 5 for full discussion.

## Author(s)

 $Peter Rossi, Graduate School of Business, University of Chicago, \\ \langle Peter.Rossi@ChicagoGsb.edu \rangle.$ 

#### References

For further discussion, see  $Bayesian\ Statistics\ and\ Marketing\$ by Rossi, Allenby and McCulloch, Chapter 3.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

#### See Also

rhierLinearModel

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}

set.seed(66)
nreg=300; nobs=500; nvar=3; nz=2

Z=matrix(runif(nreg*nz),ncol=nz)
Z=t(t(Z)-apply(Z,2,mean))
Delta=matrix(c(1,-1,2,0,1,0),ncol=nz)
tau0=.1
iota=c(rep(1,nobs))

## create arguments for rmixture

tcomps=NULL
a=matrix(c(1,0,0,0.5773503,1.1547005,0,-0.4082483,0.4082483,1.2247449),ncol=3)
```

```
tcomps[[1]]=list(mu=c(0,-1,-2),rooti=a)
tcomps[[2]]=list(mu=c(0,-1,-2)*2,rooti=a)
tcomps[[3]]=list(mu=c(0,-1,-2)*4,rooti=a)
tpvec=c(.4,.2,.4)
                                                           # simulated data with Z
regdata=NULL
betas=matrix(double(nreg*nvar),ncol=nvar)
tind=double(nreg)
for (reg in 1:nreg) {
tempout=rmixture(1,tpvec,tcomps)
betas[reg,]=Delta%*%Z[reg,]+as.vector(tempout$x)
tind[reg]=tempout$z
X=cbind(iota,matrix(runif(nobs*(nvar-1)),ncol=(nvar-1)))
tau=tau0*runif(1,min=0.5,max=1)
y=X%*%betas[reg,]+sqrt(tau)*rnorm(nobs)
regdata[[reg]]=list(y=y,X=X,beta=betas[reg,],tau=tau)
## run rhierLinearMixture
Data1=list(regdata=regdata,Z=Z)
Prior1=list(ncomp=3)
Mcmc1=list(R=R,keep=1)
out1=rhierLinearMixture(Data=Data1,Prior=Prior1,Mcmc=Mcmc1)
cat("Summary of Delta draws",fill=TRUE)
summary(out1$Deltadraw,tvalues=as.vector(Delta))
cat("Summary of Normal Mixture Distribution",fill=TRUE)
summary(out1$nmix)
if(0){
## plotting examples
plot(out1$betadraw)
plot(out1$nmix)
plot(out1$Deltadraw)
```

rhierLinearModel

Gibbs Sampler for Hierarchical Linear Model

### Description

rhierLinearModel implements a Gibbs Sampler for hierarchical linear models with a normal prior.

## Usage

```
rhierLinearModel(Data, Prior, Mcmc)
```

### **Arguments**

Data list(regdata,Z) (Z optional).

Prior list(Deltabar, A, nu. e, ssq, nu, V) (optional).

Mcmc list(R, keep) (R required).

### Details

```
Model: length(regdata) regression equations.
```

 $y_i = X_i beta_i + e_i$ .  $e_i \sim N(0, tau_i)$ . nvar X vars in each equation.

#### Priors:

 $tau_i \sim \text{nu.e}^* ssq_i/\chi^2_{nu.e}$ .  $tau_i$  is the variance of  $e_i$ .

 $beta_i \sim N(ZDelta[i,], V_{beta}).$ 

Note: ZDelta is the matrix Z \* Delta; [i,] refers to ith row of this product.

vec(Delta) given  $V_{beta} \sim N(vec(Deltabar), V_{beta}(x)A^{-1}).$ 

 $V_{beta} \sim IW(nu, V)$ .

Delta, Deltabar are nz x nvar. A is nz x nz.  $V_{beta}$  is nvar x nvar.

Note: if you don't have any z vars, set Z=iota (nreg x 1).

List arguments contain:

regdata list of lists with X,y matrices for each of length(regdata) regressions

regdata[[i]]\$X X matrix for equation i

regdata[[i]]\$y y vector for equation i

Deltabar nz x nvar matrix of prior means (def: 0)

A nz x nz matrix for prior precision (def: .01I)

nu.e d.f. parm for regression error variance prior (def: 3)

ssq scale parm for regression error var prior (def:  $var(y_i)$ )

nu d.f. parm for Vbeta prior (def: nvar+3)

V Scale location matrix for Vbeta prior (def: nu\*I)

R number of MCMC draws

keep MCMC thinning parm: keep every keepth draw (def: 1)

### Value

a list containing

betadraw nreg x nvar x R/keep array of individual regression coef draws

taudraw R/keep x nreg array of error variance draws  $R/keep \times nz \times nvar array of Deltadraws$ 

Vbetadraw R/keep x nvar\*nvar array of Vbeta draws

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 3.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

#### See Also

### rhierLinearMixture

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}
nreg=100; nobs=100; nvar=3
Vbeta=matrix(c(1,.5,0,.5,2,.7,0,.7,1),ncol=3)
Z=cbind(c(rep(1,nreg)),3*runif(nreg)); Z[,2]=Z[,2]-mean(Z[,2])
nz=ncol(Z)
Delta=matrix(c(1,-1,2,0,1,0),ncol=2)
Delta=t(Delta) # first row of Delta is means of betas
Beta=matrix(rnorm(nreg*nvar),nrow=nreg)%*%chol(Vbeta)+Z%*%Delta
iota=c(rep(1,nobs))
regdata=NULL
for (reg in 1:nreg) { X=cbind(iota,matrix(runif(nobs*(nvar-1)),ncol=(nvar-1)))
        y=X%*%Beta[reg,]+sqrt(tau)*rnorm(nobs); regdata[[reg]]=list(y=y,X=X) }
Data1=list(regdata=regdata,Z=Z)
Mcmc1=list(R=R,keep=1)
out=rhierLinearModel(Data=Data1,Mcmc=Mcmc1)
cat("Summary of Delta draws",fill=TRUE)
summary(out$Deltadraw,tvalues=as.vector(Delta))
cat("Summary of Vbeta draws",fill=TRUE)
summary(out$Vbetadraw,tvalues=as.vector(Vbeta[upper.tri(Vbeta,diag=TRUE)]))
if(0){
## plotting examples
plot(out$betadraw)
plot(out$Deltadraw)
}
```

rhierMnlRwMixture

MCMC Algorithm for Hierarchical Multinomial Logit with Mixture of Normals Heterogeneity

## Description

rhierMnlRwMixture is a MCMC algorithm for a hierarchical multinomial logit with a mixture of normals heterogeneity distribution. This is a hybrid Gibbs Sampler with a RW Metropolis step for the MNL coefficients for each panel unit.

### Usage

```
rhierMnlRwMixture(Data, Prior, Mcmc)
```

## **Arguments**

Data list(p,lgtdata,Z) ( Z is optional)

Prior list(a,deltabar,Ad,mubar,Amu,nu,V,ncomp) (all but ncomp are optional)

Mcmc list(s,w,R,keep) (R required)

deltabar nz\*nvar vector of prior means (def: 0)

### **Details**

Model:

```
y_i \sim MNL(X_i, beta_i). i=1,..., length(lgtdata). theta<sub>i</sub> is nvar x 1.
              beta_i = \text{ZDelta[i,]} + u_i.
              Note: here ZDelta refers to Z%*%D, ZDelta[i,] is ith row of this product.
              Delta is an nz x nvar array.
              u_i \sim N(mu_{ind}, Sigma_{ind}). ind \sim \text{multinomial(pvec)}.
              Priors:
              pvec \sim dirichlet (a)
              delta = vec(Delta) \sim N(deltabar, A_d^{-1})
              mu_i \sim N(mubar, Sigma_i(x)Amu^{-1})
              Sigma_i \sim IW(nu,V)
              Lists contain:
                 p p is number of choice alternatives
         lgtdata list of lists with each cross-section unit MNL data
lgtdata[[i]]$y n_i vector of multinomial outcomes (1, ..., m)
lgtdata[[i]]X n_i by nvar design matrix for ith unit
                 a vector of length noomp of Dirichlet prior parms (def: rep(5,ncomp))
```

```
Ad prior prec matrix for vec(D) (def: .01I)
```

mubar nvar x 1 prior mean vector for normal comp mean (def: 0)

Amu prior precision for normal comp mean (def: .01I)

nu d.f. parm for IW prior on norm comp Sigma (def: nvar+3)

V pds location parm for IW prior on norm comp Sigma (def: nuI)

ncomp number of components used in normal mixture

s scaling parm for RW Metropolis (def: 2.93/sqrt(nvar))

w fractional likelihood weighting parm (def: .1)

R number of MCMC draws

keep MCMC thinning parm: keep every keepth draw (def: 1)

### Value

a list containing:

Deltadraw R/keep x nz\*nvar matrix of draws of Delta, first row is initial value

betadraw nlgt x nvar x R/keep array of draws of betas

nmix list of 3 components, probdraw, NULL, compdraw log-like log-likelihood for each kept draw (length R/keep)

#### Note

More on probdraw component of nmix list:

R/keep x ncomp matrix of draws of probs of mixture components (pvec)

More on compdraw component of return value list:

compdraw[[i ]] the ith draw of components for mixtures

compdraw[[i ][[j]]] ith draw of the jth normal mixture comp

compdraw[[i ][[j]][[1]]] ith draw of jth normal mixture comp mean vector

compdraw[[i ][[j]][[2]]] ith draw of jth normal mixture cov parm (rooti)

Note: Z should **not** include an intercept and is centered for ease of interpretation.

Be careful in assessing prior parameter, Amu. .01 is too small for many applications. See Rossi et al, chapter 5 for full discussion.

Note: as of version 2.0-2 of bayesm, the fractional weight parameter has been changed to a weight between 0 and 1. w is the fractional weight on the normalized pooled likelihood. This differs from what is in Rossi et al chapter 5, i.e.

$$like_{i}^{(1)}(1-w)xlike_{p}ooled^{(n_{i}/N)}*w)$$

Large R values may be required (>20,000).

### Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 5.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

#### See Also

```
rmnlIndepMetrop
```

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=10000} else {R=10}
set.seed(66)
p=3
                                    # num of choice alterns
ncoef=3
nlgt=300
                                    # num of cross sectional units
nz=2
Z=matrix(runif(nz*nlgt),ncol=nz)
Z=t(t(Z)-apply(Z,2,mean))
                                    # demean Z
ncomp=3
                                        # no of mixture components
Delta=matrix(c(1,0,1,0,1,2),ncol=2)
comps=NULL
comps[[1]]=list(mu=c(0,-1,-2),rooti=diag(rep(1,3)))
\texttt{comps[[2]]=list(mu=c(0,-1,-2)*2,rooti=diag(rep(1,3)))}
comps[[3]]=list(mu=c(0,-1,-2)*4,rooti=diag(rep(1,3)))
pvec=c(.4,.2,.4)
simmnlwX= function(n,X,beta) {
 ## simulate from MNL model conditional on X matrix
 k=length(beta)
 Xbeta=X%*%beta
  j=nrow(Xbeta)/n
 Xbeta=matrix(Xbeta,byrow=TRUE,ncol=j)
 Prob=exp(Xbeta)
  iota=c(rep(1,j))
 denom=Prob%*%iota
 Prob=Prob/as.vector(denom)
 y=vector("double",n)
 ind=1:j
 for (i in 1:n)
      {yvec=rmultinom(1,1,Prob[i,]); y[i]=ind%*%yvec}
 return(list(y=y,X=X,beta=beta,prob=Prob))
}
## simulate data
simlgtdata=NULL
```

```
ni=rep(50,300)
for (i in 1:nlgt)
{ betai=Delta%*%Z[i,]+as.vector(rmixture(1,pvec,comps)$x)
   Xa=matrix(runif(ni[i]*p,min=-1.5,max=0),ncol=p)
   X=createX(p,na=1,nd=NULL,Xa=Xa,Xd=NULL,base=1)
   outa=simmnlwX(ni[i],X,betai)
   simlgtdata[[i]]=list(y=outa$y,X=X,beta=betai)
}
## plot betas
if(0){
## set if(1) above to produce plots
bmat=matrix(0,nlgt,ncoef)
for(i in 1:nlgt) {bmat[i,]=simlgtdata[[i]]$beta}
par(mfrow=c(ncoef,1))
for(i in 1:ncoef) hist(bmat[,i],breaks=30,col="magenta")
}
     set parms for priors and Z
Prior1=list(ncomp=5)
keep=5
Mcmc1=list(R=R,keep=keep)
Data1=list(p=p,lgtdata=simlgtdata,Z=Z)
out=rhierMnlRwMixture(Data=Data1,Prior=Prior1,Mcmc=Mcmc1)
cat("Summary of Delta draws",fill=TRUE)
summary(out$Deltadraw,tvalues=as.vector(Delta))
cat("Summary of Normal Mixture Distribution",fill=TRUE)
summary(out$nmix)
if(0) {
## plotting examples
plot(out$betadraw)
plot(out$nmix)
```

rhierNegbinRw

MCMC Algorithm for Negative Binomial Regression

### Description

rhierNegbinRw implements an MCMC strategy for the hierarchical Negative Binomial (NBD) regression model. Metropolis steps for each unit level set of regression parameters are automatically tuned by optimization. Over-dispersion parameter (alpha) is common across units.

### Usage

```
rhierNegbinRw(Data, Prior, Mcmc)
```

#### Arguments

Data list(regdata,Z)

Prior list(Deltabar, Adelta, nu, V, a, b)

Mcmc list(R,keep,s\_beta,s\_alpha,c,Vbeta0,Delta0)

### Details

```
\begin{split} & \text{Model: } y_i \sim \text{NBD}(\text{mean=lambda, over-dispersion=alpha)}. \\ & lambda = exp(X_ibeta_i) \\ & \text{Prior: } beta_i \sim N(Delta'z_i, Vbeta). \\ & vec(Delta|Vbeta) \sim N(vec(Deltabar), Vbeta(x)Adelta). \\ & Vbeta \sim IW(nu, V). \\ & alpha \sim Gamma(a, b). \\ & \text{note: prior mean of } alpha = a/b, variance = a/(b^2) \\ & \text{list arguments contain:} \end{split}
```

regdata list of lists with data on each of nreg units
regdata[[i]]\$X nobs\_i x nvar matrix of X variables
regdata[[i]]\$y nobs\_i x 1 vector of count responses

Z nreg x nz mat of unit chars (def: vector of ones)

Deltabar nz x nvar prior mean matrix (def: 0)

Adelta nz x nz pds prior prec matrix (def: .01I)

nu d.f. parm for IWishart (def: nvar+3)

V location matrix of IWishart prior (def: nuI)

a Gamma prior parm (def: .5)

b Gamma prior parm (def: .1)

R number of MCMC draws

keep MCMC thinning parm: keep every keepth draw (def: 1)

s\_beta scaling for beta| alpha RW inc cov (def: 2.93/sqrt(nvar))

s\_alpha scaling for alpha | beta RW inc cov (def: 2.93)

c fractional likelihood weighting parm (def:2)

VbetaO starting value for Vbeta (def: I)

DeltaO starting value for Delta (def: 0)

#### Value

a list containing:

llike R/keep vector of values of log-likelihood betadraw  $nreg \ x \ nvar \ x \ R/keep$  array of beta draws

alphadraw R/keep vector of alpha draws
acceptrbeta acceptance rate of the beta draws
acceptralpha acceptance rate of the alpha draws

### Note

The NBD regression encompasses Poisson regression in the sense that as alpha goes to infinity the NBD distribution tends to the Poisson.

For "small" values of alpha, the dependent variable can be extremely variable so that a large number of observations may be required to obtain precise inferences.

For ease of interpretation, we recommend demeaning Z variables.

## Author(s)

Sridhar Narayanam & Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 5.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

#### See Also

rnegbinRw

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}
##
set.seed(66)
simnegbin =
function(X, beta, alpha) {
# Simulate from the Negative Binomial Regression
lambda = exp(X %*% beta)
y=NULL
for (j in 1:length(lambda))
    y = c(y,rnbinom(1,mu = lambda[j],size = alpha))
return(y)
}
nreg = 100  # Number of cross sectional units
T = 50  # Number of observations per unit
```

```
nobs = nreg*T
                  # Number of X variables
nvar=2
                  # Number of Z variables
nz=2
# Construct the Z matrix
Z = cbind(rep(1,nreg),rnorm(nreg,mean=1,sd=0.125))
Delta = cbind(c(0.4,0.2), c(0.1,0.05))
alpha = 5
Vbeta = rbind(c(0.1,0),c(0,0.1))
# Construct the regdata (containing X)
simnegbindata = NULL
for (i in 1:nreg) {
    betai = as.vector(Z[i,]%*%Delta) + chol(Vbeta)%*%rnorm(nvar)
    X = cbind(rep(1,T),rnorm(T,mean=2,sd=0.25))
    simnegbindata[[i]] = list(y=simnegbin(X,betai,alpha), X=X,beta=betai)
}
Beta = NULL
for (i in 1:nreg) {Beta=rbind(Beta,matrix(simnegbindata[[i]]$beta,nrow=1))}
Data1 = list(regdata=simnegbindata, Z=Z)
Mcmc1 = list(R=R)
out = rhierNegbinRw(Data=Data1, Mcmc=Mcmc1)
cat("Summary of Delta draws",fill=TRUE)
summary(out$Deltadraw,tvalues=as.vector(Delta))
cat("Summary of Vbeta draws",fill=TRUE)
summary(out$Vbetadraw,tvalues=as.vector(Vbeta[upper.tri(Vbeta,diag=TRUE)]))
cat("Summary of alpha draws",fill=TRUE)
summary(out$alpha,tvalues=alpha)
if(0){
## plotting examples
plot(out$betadraw)
plot(out$alpha,tvalues=alpha)
plot(out$Deltadraw,tvalues=as.vector(Delta))
```

rivGibbs

Gibbs Sampler for Linear "IV" Model

## Description

rivGibbs is a Gibbs Sampler for a linear structural equation with an arbitrary number of instruments.

## Usage

```
rivGibbs(Data, Prior, Mcmc)
```

### **Arguments**

Data list(z,w,x,y)

 ${\tt Prior} \hspace{1cm} {\tt list(md,Ad,mbg,Abg,nu,V) \ (optional)}$ 

Mcmc list(R, keep) (R required)

### **Details**

```
Model:
```

x = z' delta + e1.

y = beta \* x + w'gamma + e2.

 $e1, e2 \sim N(0, Sigma).$ 

Note: if intercepts are desired in either equation, include vector of ones in z or w

Priors

 $delta \sim N(md, Ad^{-1}). \ vec(beta, gamma) \sim N(mbg, Abg^{-1})$ 

 $Sigma \sim IW(nu,V)$ 

List arguments contain:

**z** matrix of obs on instruments

y vector of obs on lhs var in structural equation

x "endogenous" var in structural eqn

w matrix of obs on "exogenous" vars in the structural eqn

md prior mean of delta (def: 0)

Ad pds prior prec for prior on delta (def: .01I)

mbg prior mean vector for prior on beta,gamma (def: 0)

Abg pds prior prec for prior on beta,gamma (def: .01I)

nu d.f. parm for IW prior on Sigma (def: 5)

V pds location matrix for IW prior on Sigma (def: nuI)

R number of MCMC draws

keep MCMC thinning parm: keep every keepth draw (def: 1)

#### Value

a list containing:

deltadraw R/keep x dim(delta) array of delta draws

betadraw R/keep x 1 vector of beta draws

gammadraw R/keep x dim(gamma) array of gamma draws

Sigmadraw R/keep x 4 array of Sigma draws

## Author(s)

Rob McCulloch and Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 5.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

## Examples

```
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}
set.seed(66)
simIV = function(delta,beta,Sigma,n,z,w,gamma) {
eps = matrix(rnorm(2*n),ncol=2) %*% chol(Sigma)
x = z \%*\% delta + eps[,1]; y = beta*x + eps[,2] + w\%*%gamma
list(x=as.vector(x),y=as.vector(y)) }
n = 200; p=1 \# number of instruments
z = cbind(rep(1,n),matrix(runif(n*p),ncol=p))
w = matrix(1,n,1)
rho=.8
Sigma = matrix(c(1,rho,rho,1),ncol=2)
delta = c(1,4); beta = .5; gamma = c(1)
simiv = simIV(delta,beta,Sigma,n,z,w,gamma)
Mcmc1=list(); Data1 = list()
Data1$z = z; Data1$w=w; Data1$x=simiv$x; Data1$y=simiv$y
Mcmc1R = R
Mcmc1$keep=1
out=rivGibbs(Data=Data1,Mcmc=Mcmc1)
cat("Summary of Beta draws",fill=TRUE)
summary(out$betadraw,tvalues=beta)
cat("Summary of Sigma draws",fill=TRUE)
summary(out$Sigmadraw,tvalues=as.vector(Sigma[upper.tri(Sigma,diag=TRUE)]))
if(0){
## plotting examples
plot(out$betadraw)
```

rmixGibbs

Gibbs Sampler for Normal Mixtures w/o Error Checking

## Description

rmixGibbs makes one draw using the Gibbs Sampler for a mixture of multivariate normals.

### Usage

```
rmixGibbs(y, Bbar, A, nu, V, a, p, z, comps)
```

### Arguments

y data array - rows are obs

Bbar prior mean for mean vector of each norm comp

A prior precision parameter

nu prior d.f. parm

V prior location matrix for covariance priro

a Dirichlet prior parms

p prior prob of each mixture component

z component identities for each observation – "indicators"

comps list of components for the normal mixture

#### Details

rmixGibbs is not designed to be called directly. Instead, use rnmixGibbs wrapper function.

# Value

a list containing:

p draw mixture probabilities

z draw of indicators of each component

comps new draw of normal component parameters

### Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

### Author(s)

Rob McCulloch and Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

### References

For further discussion, see *Bayesian Statistics and Marketing* by Allenby, McCulloch, and Rossi, Chapter 5.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

#### See Also

rnmixGibbs

rmixture

Draw from Mixture of Normals

## Description

rmixture simulates iid draws from a Multivariate Mixture of Normals

### Usage

```
rmixture(n, pvec, comps)
```

## Arguments

n number of observations

pvec ncomp x 1 vector of prior probabilities for each mixture component

comps list of mixture component parameters

#### Details

comps is a list of length, ncomp = length(pvec). comps[[j]][[1]] is mean vector for the jth component. comps[[j]][[2]] is the inverse of the cholesky root of Sigma for that component

## Value

A list containing . . .

x An n x length(comps[[1]][[1]]) array of iid draws

z A n x 1 vector of indicators of which component each draw is taken from

### Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

### Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### See Also

rnmixGibbs

 $MCMC\ Algorithm\ for\ Multinomial\ Logit\ Model$ 

## rmnlIndepMetrop

## Description

rmnIndepMetrop implements Independence Metropolis for the MNL.

## Usage

```
rmnlIndepMetrop(Data, Prior, Mcmc)
```

## Arguments

 ${\tt Data} \qquad \qquad {\tt list}(p,\!y,\!X)$ 

Prior list(A,betabar) optional

 ${\tt Mcmc} \qquad \qquad {\tt list(R,keep,nu)}$ 

#### **Details**

Model:  $y \sim \text{MNL}(X, \text{beta})$ .  $Pr(y = j) = \exp(x_j' \text{beta}) / \sum_k e^{x_k' \text{beta}}$ .

Prior: beta  $\sim N(betabar, A^{-1})$ 

list arguments contain:

p number of alternatives

y nobs vector of multinomial outcomes  $(1, \ldots, p)$ 

X nobs\*p x nvar matrix

A nvar x nvar pds prior prec matrix (def: .01I)

betabar nvar x 1 prior mean (def: 0)

R number of MCMC draws

keep MCMC thinning parm: keep every keepth draw (def: 1)

nu degrees of freedom parameter for independence t density (def: 6)

### Value

a list containing:

betadraw R/keep x nvar array of beta draws

loglike R/keep vector of loglike values for each draw

acceptr acceptance rate of Metropolis draws

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 5.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

#### See Also

rhierMnlRwMixture

```
##
```

```
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}
set.seed(66)
n=200; p=3; beta=c(1,-1,1.5,.5)
simmnl= function(p,n,beta) {
 # note: create X array with 2 alt.spec vars
 k=length(beta)
 X1=matrix(runif(n*p,min=-1,max=1),ncol=p)
 X2=matrix(runif(n*p,min=-1,max=1),ncol=p)
 X=createX(p,na=2,nd=NULL,Xd=NULL,Xa=cbind(X1,X2),base=1)
 Xbeta=X%*%beta # now do probs
 p=nrow(Xbeta)/n
 Xbeta=matrix(Xbeta,byrow=TRUE,ncol=p)
 Prob=exp(Xbeta)
 iota=c(rep(1,p))
 denom=Prob%*%iota
 Prob=Prob/as.vector(denom)
 # draw y
 y=vector("double",n)
  ind=1:p
  for (i in 1:n)
        { yvec=rmultinom(1,1,Prob[i,]); y[i]=ind%*%yvec }
   return(list(y=y,X=X,beta=beta,prob=Prob))
}
simout=simmnl(p,n,beta)
Data1=list(y=simout$y,X=simout$X,p=p); Mcmc1=list(R=R,keep=1)
out=rmnlIndepMetrop(Data=Data1,Mcmc=Mcmc1)
cat("Summary of beta draws",fill=TRUE)
summary(out$betadraw,tvalues=beta)
if(0){
```

```
## plotting examples
plot(out$betadraw)
}
```

rmnpGibbs

Gibbs Sampler for Multinomial Probit

## Description

rmnpGibbs implements the McCulloch/Rossi Gibbs Sampler for the multinomial probit model.

### Usage

```
rmnpGibbs(Data, Prior, Mcmc)
```

## Arguments

Data list(p, y, X)

Prior list(betabar,A,nu,V) (optional)

Mcmc list(beta0,sigma0,R,keep) (R required)

## Details

```
model:
    w_i = X_i \beta + e. e \sim N(0, Sigma). note: w_i, e are (p-1) x 1.
    y_i = j, if w_{ij} > max(0, w_{i,-j}) j=1,...,p-1. w_{i,-j} means elements of w_i other than the jth.
    y_i = p, if all w_i < 0.
    priors:
    beta \sim N(betabar, A^{-1})
    Sigma \sim IW(nu,V)
    to make up X matrix use createX with DIFF=TRUE.
    List arguments contain
       p number of choices or possible multinomial outcomes
       y n x 1 vector of multinomial outcomes
       X n*(p-1) x k Design Matrix
betabar k x 1 prior mean (def: 0)
       A k x k prior precision matrix (def: .01I)
      nu d.f. parm for IWishart prior (def: (p-1) + 3)
       V pds location parm for IWishart prior (def: nu*I)
```

```
beta0 initial value for beta
sigma0 initial value for sigma
    R number of MCMC draws
keep thinning parameter - keep every keepth draw (def: 1)
```

#### Value

a list containing:

betadraw R/keep x k array of betadraws

sigmadraw R/keep x (p-1)\*(p-1) array of sigma draws – each row is in vector form

### Note

beta is not identified. beta/sqrt( $sigma_{11}$ ) and Sigma/ $sigma_{11}$  are. See Allenby et al or example below for details.

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 4.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

### See Also

rmvpGibbs

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}
set.seed(66)
p=3
n=500
beta=c(-1,1,1,2)
Sigma=matrix(c(1,.5,.5,1),ncol=2)
k=length(beta)
X1=matrix(runif(n*p,min=0,max=2),ncol=p); X2=matrix(runif(n*p,min=0,max=2),ncol=p)
X=createX(p,na=2,nd=NULL,Xa=cbind(X1,X2),Xd=NULL,DIFF=TRUE,base=p)
simmnp= function(X,p,n,beta,sigma) {
  indmax=function(x) {which(max(x)==x)}
 Xbeta=X%*%beta
  w=as.vector(crossprod(chol(sigma),matrix(rnorm((p-1)*n),ncol=n)))+ Xbeta
  w=matrix(w,ncol=(p-1),byrow=TRUE)
 maxw=apply(w,1,max)
```

```
y=apply(w,1,indmax)
 y=ifelse(maxw < 0,p,y)
 return(list(y=y,X=X,beta=beta,sigma=sigma))
}
simout=simmnp(X,p,500,beta,Sigma)
Data1=list(p=p,y=simout$y,X=simout$X)
Mcmc1=list(R=R,keep=1)
out=rmnpGibbs(Data=Data1,Mcmc=Mcmc1)
cat(" Summary of Betadraws ",fill=TRUE)
betatilde=out$betadraw/sqrt(out$sigmadraw[,1])
attributes(betatilde)$class="bayesm.mat"
summary(betatilde,tvalues=beta)
cat(" Summary of Sigmadraws ",fill=TRUE)
sigmadraw=out$sigmadraw/out$sigmadraw[,1]
attributes(sigmadraw)$class="bayesm.var"
summary(sigmadraw,tvalues=as.vector(Sigma[upper.tri(Sigma,diag=TRUE)]))
if(0){
## plotting examples
plot(betatilde,tvalues=beta)
```

rmultireg

Draw from the Posterior of a Multivariate Regression

## Description

rmultireg draws from the posterior of a Multivariate Regression model with a natural conjugate prior.

## Usage

```
rmultireg(Y, X, Bbar, A, nu, V)
```

# Arguments

Y n x m matrix of observations on m dep vars

 ${\tt X}$  n x k matrix of observations on indep vars (supply intercept)

Bbar k x m matrix of prior mean of regression coefficients

A k x k Prior precision matrix nu d.f. parameter for Sigma

V m x m pdf location parameter for prior on Sigma

#### Details

```
Model: Y = XB + U. cov(u_i) = Sigma. B is k x m matrix of coefficients. Sigma is m x m covariance.
Priors: beta given Sigma \sim N(betabar, Sigma(x)A^{-1}). betabar = vec(Bbar); beta = vec(B)
```

 $\widetilde{Sigma} \sim \mathrm{IW}(\mathrm{nu}, \mathrm{V}).$ 

### Value

A list of the components of a draw from the posterior

B draw of regression coefficient matrix

Sigma draw of Sigma

### Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 2.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}
set.seed(66)
n=200
m=2
X=cbind(rep(1,n),runif(n))
k=ncol(X)
B=matrix(c(1,2,-1,3),ncol=m)
Sigma=matrix(c(1,.5,.5,1),ncol=m); RSigma=chol(Sigma)
Y=X%*%B+matrix(rnorm(m*n),ncol=m)%*%RSigma
betabar=rep(0,k*m);Bbar=matrix(betabar,ncol=m)
A=diag(rep(.01,k))
nu=3; V=nu*diag(m)
betadraw=matrix(double(R*k*m),ncol=k*m)
Sigmadraw=matrix(double(R*m*m),ncol=m*m)
for (rep in 1:R)
   {out=rmultireg(Y,X,Bbar,A,nu,V);betadraw[rep,]=out$B
```

```
Sigmadraw[rep,]=out$Sigma}

cat(" Betadraws ",fill=TRUE)
mat=apply(betadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(as.vector(B),mat); rownames(mat)[1]="beta"
print(mat)
cat(" Sigma draws",fill=TRUE)
mat=apply(Sigmadraw,2,quantile,probs=c(.01,.05,.5,.95,.99))
mat=rbind(as.vector(Sigma),mat); rownames(mat)[1]="Sigma"
print(mat)
```

rmvpGibbs

Gibbs Sampler for Multivariate Probit

## Description

rmvpGibbs implements the Edwards/Allenby Gibbs Sampler for the multivariate probit model.

## Usage

```
rmvpGibbs(Data, Prior, Mcmc)
```

### Arguments

Data list(p,y,X)

Prior list(betabar,A,nu,V) (optional)

Mcmc list(beta0,sigma0,R,keep) (R required)

### Details

```
betabar k x 1 prior mean (def: 0)

A k x k prior precision matrix (def: .01I)

nu d.f. parm for IWishart prior (def: (p-1) + 3)

V pds location parm for IWishart prior (def: nu*I)

beta0 initial value for beta

sigma0 initial value for sigma

R number of MCMC draws

keep thinning parameter - keep every keepth draw (def: 1)
```

### Value

a list containing:

betadraw R/keep x k array of betadraws

sigmadraw R/keep x p\*p array of sigma draws – each row is in vector form

### Note

beta and Sigma are not identified. Correlation matrix and the betas divided by the appropriate standard deviation are. See Allenby et al for details or example below.

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 4.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

## See Also

rmnpGibbs

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}

set.seed(66)
p=3
n=500
beta=c(-2,0,2)
Sigma=matrix(c(1,.5,.5,.5,1,.5,.5,.5,1),ncol=3)
k=length(beta)
I2=diag(rep(1,p)); xadd=rbind(I2)
for(i in 2:n) { xadd=rbind(xadd,I2)}; X=xadd
```

```
simmvp= function(X,p,n,beta,sigma) {
 w=as.vector(crossprod(chol(sigma),matrix(rnorm(p*n),ncol=n)))+ X%*%beta
 y=ifelse(w<0,0,1)
 return(list(y=y,X=X,beta=beta,sigma=sigma))
}
simout=simmvp(X,p,500,beta,Sigma)
Data1=list(p=p,y=simout$y,X=simout$X)
Mcmc1=list(R=R,keep=1)
out=rmvpGibbs(Data=Data1,Mcmc=Mcmc1)
ind=seq(from=0,by=p,length=k)
inda=1:3
ind=ind+inda
cat(" Betadraws ",fill=TRUE)
betatilde=out$betadraw/sqrt(out$sigmadraw[,ind])
attributes(betatilde)$class="bayesm.mat"
summary(betatilde,tvalues=beta/sqrt(diag(Sigma)))
rdraw=matrix(double((R)*p*p),ncol=p*p)
rdraw=t(apply(out$sigmadraw,1,nmat))
attributes(rdraw)$class="bayesm.var"
tvalue=nmat(as.vector(Sigma))
dim(tvalue)=c(p,p)
tvalue=as.vector(tvalue[upper.tri(tvalue,diag=TRUE)])
cat(" Draws of Correlation Matrix ",fill=TRUE)
summary(rdraw,tvalues=tvalue)
if(0){
plot(betatilde,tvalues=beta/sqrt(diag(Sigma)))
```

rmvst

 $Draw\ from\ Multivariate\ Student-t$ 

### Description

rmvst draws from a Multivariate student-t distribution.

#### Usage

```
rmvst(nu, mu, root)
```

# Arguments

nu d.f. parameter mu mean vector

root Upper Tri Cholesky Root of Sigma

#### Value

length(mu) draw vector

## Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

### See Also

lndMvst

## Examples

```
##
set.seed(66)
rmvst(nu=5,mu=c(rep(0,2)),root=chol(matrix(c(2,1,1,2),ncol=2)))
```

rnegbinRw

MCMC Algorithm for Negative Binomial Regression

# Description

rnegbinRw implements a Random Walk Metropolis Algorithm for the Negative Binomial (NBD) regression model. beta | alpha and alpha | beta are drawn with two different random walks.

# Usage

```
rnegbinRw(Data, Prior, Mcmc)
```

# Arguments

Data list(y,X)

Prior list(betabar,A,a,b)

Mcmc list(R,keep,s\_beta,s\_alpha,beta0

#### **Details**

```
Model: y \sim NBD(mean = lambda, over - dispersion = alpha).
    lambda = exp(x'beta)
    Prior: beta \sim N(betabar, A^{-1})
    alpha \sim Gamma(a, b).
    note: prior mean of alpha = a/b, variance = a/(b^2)
    list arguments contain:
       y nobs vector of counts (0,1,2,...)
      X nobs x nvar matrix
betabar nvar x 1 prior mean (def: 0)
       A nvar x nvar pds prior prec matrix (def: .01I)
       a Gamma prior parm (def: .5)
       b Gamma prior parm (def: .1)
       R number of MCMC draws
   keep MCMC thinning parm: keep every keepth draw (def: 1)
 s_beta scaling for beta alpha RW inc cov matrix (def: 2.93/sqrt(nvar)
s_alpha scaling for alpha | beta RW inc cov matrix (def: 2.93)
```

#### Value

a list containing:

betadraw R/keep x nvar array of beta draws alphadraw R/keep vector of alpha draws

11ike R/keep vector of log-likelihood values evaluated at each draw

acceptrbeta acceptance rate of the beta draws acceptralpha acceptance rate of the alpha draws

### Note

The NBD regression encompasses Poisson regression in the sense that as alpha goes to infinity the NBD distribution tends toward the Poisson.

For "small" values of alpha, the dependent variable can be extremely variable so that a large number of observations may be required to obtain precise inferences.

# Author(s)

Sridhar Narayanam & Peter Rossi, Graduate School of Business, University of Chicago,  $\langle Peter.Rossi@ChicagoGsb.edu \rangle$ .

### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby, McCulloch. http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

#### See Also

### rhierNegbinRw

#### Examples

```
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=1000} else {R=10}
set.seed(66)
simnegbin =
function(X, beta, alpha) {
   Simulate from the Negative Binomial Regression
lambda = exp(X %*% beta)
y=NULL
for (j in 1:length(lambda))
    y = c(y,rnbinom(1,mu = lambda[j],size = alpha))
return(y)
}
nobs = 500
nvar=2
                  # Number of X variables
alpha = 5
Vbeta = diag(nvar)*0.01
# Construct the regdata (containing X)
simnegbindata = NULL
beta = c(0.6, 0.2)
X = cbind(rep(1,nobs),rnorm(nobs,mean=2,sd=0.5))
simnegbindata = list(y=simnegbin(X,beta,alpha), X=X, beta=beta)
Data1 = simnegbindata
Mcmc1 = list(R=R)
out = rnegbinRw(Data=Data1,Mcmc=Mcmc1)
cat("Summary of alpha/beta draw",fill=TRUE)
summary(out$alphadraw,tvalues=alpha)
summary(out$betadraw,tvalues=beta)
if(0){
## plotting examples
plot(out$betadraw)
}
```

rnmixGibbs

Gibbs Sampler for Normal Mixtures

## Description

rnmixGibbs implements a Gibbs Sampler for normal mixtures.

#### Usage

```
rnmixGibbs(Data, Prior, Mcmc)
```

#### **Arguments**

Data list(y)

Prior list(Mubar, A, nu, V, a, ncomp) (only ncomp required)

Mcmc list(R,keep) (R required)

### Details

```
Model:
  y_i \sim N(mu_{ind_i}, Sigma_{ind_i}).
  ind \sim iid multinomial(p). p is a noomp x 1 vector of probs.
  mu_i \sim N(mubar, Sigma_i(x)A^{-1}). \ mubar = vec(Mubar).
  Sigma_i \sim IW(nu, V).
  note: this is the natural conjugate prior – a special case of multivariate regression.
  p \sim \text{Dirchlet(a)}.
  Output of the components is in the form of a list of lists.
  compsdraw[[i]] is ith draw – list of ncomp lists.
  compsdraw[[i]][[j]] is list of parms for jth normal component.
  jcomp=compsdraw[[i]][j]]. Then jth comp \sim N(jcomp[[1]], Sigma), Sigma = t(R)\%*\%R,
  R^{-1} = \text{jcomp}[[2]].
  List arguments contain:
     y n x k array of data (rows are obs)
Mubar 1 x k array with prior mean of normal comp means (def: 0)
    A 1 x 1 precision parameter for prior on mean of normal comp (def: .01)
    nu d.f. parameter for prior on Sigma (normal comp cov matrix) (def: k+3)
    V k x k location matrix of IW prior on Sigma (def: nuI)
     a ncomp x 1 vector of Dirichlet prior parms (def: rep(5,ncomp))
ncomp number of normal components to be included
    R number of MCMC draws
  keep MCMC thinning parm: keep every keepth draw (def: 1)
```

#### Value

nmix

a list containing: probdraw,zdraw,compdraw

#### Note

more details on contents of nmix:

probdraw R/keep x ncomp array of mixture prob draws

zdraw R/keep x nobs array of indicators of mixture comp identity for each obs

compdraw R/keep lists of lists of comp parm draws

In this model, the component normal parameters are not-identified due to label-switching. However, the fitted mixture of normals density is identified as it is invariant to label-switching. See Allenby et al, chapter 5 for details. Use eMixMargDen or momMix to compute posterior expectation or distribution of various identified parameters.

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 3.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

#### See Also

rmixture, rmixGibbs ,eMixMargDen, momMix, mixDen, mixDenBi

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}
set.seed(66)
dim=5; k=3
             # dimension of simulated data and number of "true" components
sigma = matrix(rep(0.5,dim^2),nrow=dim);diag(sigma)=1
sigfac = c(1,1,1); mufac=c(1,2,3); compsmv=list()
for(i in 1:k) compsmv[[i]] = list(mu=mufac[i]*1:dim,sigma=sigfac[i]*sigma)
comps = list() # change to "rooti" scale
for(i in 1:k) comps[[i]] = list(mu=compsmv[[i]][[1]],rooti=solve(chol(compsmv[[i]][[2]])))
pvec=(1:k)/sum(1:k)
nobs=500
dm = rmixture(nobs,pvec,comps)
Data1=list(y=dm$x)
ncomp=9
Prior1=list(ncomp=ncomp)
Mcmc1=list(R=R,keep=1)
out=rnmixGibbs(Data=Data1,Prior=Prior1,Mcmc=Mcmc1)
cat("Summary of Normal Mixture Distribution",fill=TRUE)
```

```
summary(out)
tmom=momMix(matrix(pvec,nrow=1),list(comps))
mat=rbind(tmom$mu,tmom$sd)
cat(" True Mean/Std Dev",fill=TRUE)
print(mat)

if(0){
##
## plotting examples
##
plot(out)
}
```

 ${\tt rordprobitGibbs}$ 

Gibbs Sampler for Ordered Probit

## Description

rordprobitGibbs implements a Gibbs Sampler for the ordered probit model.

### Usage

```
rordprobitGibbs(Data, Prior, Mcmc)
```

# Arguments

 $\begin{array}{ll} {\tt Data} & {\tt list}(X,\,y,\,k) \\ {\tt Prior} & {\tt list}({\tt betabar},\,A,\,{\tt dstarbar},\,{\tt Ad}) \\ {\tt Mcmc} & {\tt list}(R,\,{\tt keep},\,s,\,{\tt change},\,{\tt draw}) \\ \end{array}$ 

### Details

```
Model: z = X\beta + e. e \sim N(0,I). y=1,...,k. cutoff=c( c [1] ,...c [k+1] ). y=k, if c [k] <= z < c [k+1] . Prior: \beta \sim N(betabar,A^{-1}). dstar \sim N(dstarbar,Ad^{-1}). List arguments contain X n x nvar Design Matrix y n x 1 vector of observations, (1,...,k) k the largest possible value of y betabar nvar x 1 prior mean (def: 0) A nvar x nvar prior precision matrix (def: .01I) dstarbar ndstar x 1 prior mean, ndstar=k-2 (def: 0) Ad ndstar x ndstar prior precision matrix (def:I)
```

```
    s scaling parm for RW Metropolis (def: 2.93/sqrt(nvar))
    R number of MCMC draws
    keep thinning parameter - keep every keepth draw (def: 1)
```

#### Value

betadraw  $R/\text{keep} \times k \text{ matrix of betadraws}$  cutdraw  $R/\text{keep} \times (k-1) \text{ matrix of cutdraws}$  dstardraw  $R/\text{keep} \times (k-2) \text{ matrix of dstardraws}$ 

accept a value of acceptance rate in RW Metropolis

#### Note

```
set c[1]=-100. c[k+1]=100. c[2] is set to 0 for identification.

The relationship between cut-offs and dstar is c[3] = \exp(\mathrm{dstar}[1]), c[4] = c[3] + \exp(\mathrm{dstar}[2]), ..., c[k] = c[k-1] + \exp(\mathrm{datsr}[k-2])
Be careful in assessing prior parameter, Ad. .1 is too small for many applications.
```

### Author(s)

 $Peter Rossi, Graduate School of Business, University of Chicago, \\ \langle Peter.Rossi@ChicagoGsb.edu \rangle.$ 

### References

```
Bayesian Statistics and Marketing by Rossi, Allenby and McCulloch http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html
```

### See Also

```
rbprobitGibbs
```

```
##
## rordprobitGibbs example
##
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}

## simulate data for ordered probit model

simordprobit=function(X, betas, cutoff){
    z = X%*%betas + rnorm(nobs)
    y = cut(z, br = cutoff, right=TRUE, include.lowest = TRUE, labels = FALSE)
    return(list(y = y, X = X, k=(length(cutoff)-1), betas= betas, cutoff=cutoff ))
}
set.seed(66)
nobs=300
```

```
X=cbind(rep(1,nobs),runif(nobs, min=0, max=5),runif(nobs,min=0, max=5))
   betas=c(0.5, 1, -0.5)
   cutoff=c(-100, 0, 1.0, 1.8, 3.2, 100)
   simout=simordprobit(X, betas, cutoff)
  Data=list(X=simout$X,y=simout$y, k=k)
## set Mcmc for ordered probit model
   Mcmc=list(R=R)
   out=rordprobitGibbs(Data=Data,Mcmc=Mcmc)
   cat(" ", fill=TRUE)
   cat("acceptance rate= ",accept=out$accept,fill=TRUE)
## outputs of betadraw and cut-off draws
   cat(" Summary of betadraws",fill=TRUE)
   summary(out$betadraw,tvalues=betas)
   cat(" Summary of cut-off draws",fill=TRUE)
   summary(out$cutdraw,tvalues=cutoff[2:k])
if(0){
## plotting examples
plot(out$cutdraw)
```

rscaleUsage

MCMC Algorithm for Multivariate Ordinal Data with Scale Usage Heterogeneity.

## Description

rscaleUsage implements an MCMC algorithm for multivariate ordinal data with scale usage heterogeniety.

### Usage

```
rscaleUsage(Data,Prior, Mcmc)
```

### Arguments

Data list(k,x)

 $Prior \\ list(nu,V,mubar,Am,gsigma,gl11,gl22,gl12,Lambdanu,LambdaV,ge) (optional)$ 

Mcmc list(R,keep,ndghk,printevery,e,y,mu,Sigma,sigma,tau,Lambda) (optional)

#### Details

```
Model: n=nrow(x) individuals respond to m=ncol(x) questions. all questions are on a scale 1,\ldots,k. for respondent i and question j, x_{ij}=d, if c_{d-1}\leq y_{ij}\leq c_d. d=1,\ldots,k. c_d=a+bd+ed^2. y_i=mu+tau_i*iota+sigma_i*z_i.\ z_i\sim N(0,Sigma). Priors: (tau_i,ln(sigma_i))\sim N(phi,Lamda).\ phi=(0,lambda_{22}). mu\sim N(mubar,Am^{-1}). Sigma \sim IW(nu,V). Lambda \sim IW(Lambdanu,LambdaV). e\sim unif on a grid.
```

#### Value

a list containing:

Sigmadraw R/keep x m\*m array of Sigma draws
mudraw R/keep x m array of mu draws
taudraw R/keep x n array of tau draws
sigmadraw R/keep x n array of sigma draws
Lambdadraw R/keep x 4 array of Lamda draws
edraw R/keep x 1 array of e draws

### Warning

 $tau_i$ ,  $sigma_i$  are identified from the scale usage patterns in the m questions asked per respondent (# cols of x). Do not attempt to use this on data sets with only a small number of total questions!

### Note

It is **highly** recommended that the user choose the default settings. This means not specifying the argument Prior and setting R in Mcmc and Data only. If you wish to change prior settings and/or the grids used, please read the case study in Allenby et al carefully.

## Author(s)

Rob McCulloch and Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby, and McCulloch, Case Study on Scale Usage Heterogeneity.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

## Examples

```
##
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=1000} else {R=5}
{
data(customerSat)
surveydat = list(k=10,x=as.matrix(customerSat))

Mcmc1 = list(R=R)
set.seed(66)
out=rscaleUsage(Data=surveydat,Mcmc=Mcmc1)
summary(out$mudraw)
}
```

rsurGibbs

Gibbs Sampler for Seemingly Unrelated Regressions (SUR)

### Description

rsurGibbs implements a Gibbs Sampler to draw from the posterior of the Seemingly Unrelated Regression (SUR) Model of Zellner

### Usage

```
rsurGibbs(Data, Prior, Mcmc)
```

## Arguments

Data list(regdata)

Prior list(betabar, A, nu, V)

Mcmc list(R, keep)

### **Details**

```
Model: y_i = X_i bet a_i + e_i. i=1,...,m. m regressions. (e(1,k),...,e(m,k)) \sim N(0,Sigma). k=1,...,nobs.
```

We can also write as the stacked model:

y = Xbeta + e where y is a nobs\*m long vector and k=length(beta)=sum(length(betai)).

Note: we must have the same number of observations in each equation but we can have different numbers of X variables

```
Priors: beta \sim N(betabar, A^{-1}). Sigma \sim IW(nu, V).
```

List arguments contain

regdata list of lists, regdata[[i]]=list(y=yi,X=Xi)

```
betabar k x 1 prior mean (def: 0)

A k x k prior precision matrix (def: .01I)

nu d.f. parm for Inverted Wishart prior (def: m+3)

V scale parm for Inverted Wishart prior (def: nu*I)

R number of MCMC draws

keep thinning parameter - keep every keepth draw
```

#### Value

list of MCMC draws

betadraw R x k array of betadraws

Sigmadraw R x (m\*m) array of Sigma draws

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 3.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

#### See Also

```
rmultireg
```

```
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=1000} else {R=10}
## simulate data from SUR
set.seed(66)
beta1=c(1,2)
beta2=c(1,-1,-2)
nobs=100
nreg=2
iota=c(rep(1,nobs))
X1=cbind(iota,runif(nobs))
X2=cbind(iota,runif(nobs),runif(nobs))
Sigma=matrix(c(.5,.2,.2,.5),ncol=2)
U=chol(Sigma)
E=matrix(rnorm(2*nobs),ncol=2)
y1=X1%*%beta1+E[,1]
y2=X2%*%beta2+E[,2]
## run Gibbs Sampler
regdata=NULL
regdata[[1]]=list(y=y1,X=X1)
```

```
regdata[[2]]=list(y=y2,X=X2)

Mcmc1=list(R=R)

out=rsurGibbs(Data=list(regdata=regdata),Mcmc=Mcmc1)

cat("Summary of beta draws",fill=TRUE)
summary(out$betadraw,tvalues=c(beta1,beta2))
cat("Summary of Sigmadraws",fill=TRUE)
summary(out$Sigmadraw,tvalues=as.vector(Sigma[upper.tri(Sigma,diag=TRUE)]))

if(0){
plot(out$betadraw,tvalues=c(beta1,beta2))
}
```

rtrun

Draw from Truncated Univariate Normal

# Description

rtrun draws from a truncated univariate normal distribution

## Usage

```
rtrun(mu, sigma, a, b)
```

## Arguments

 $\begin{array}{ll} \mathtt{mu} & \mathtt{mean} \\ \mathtt{sigma} & \mathtt{sd} \end{array}$ 

a lower boundb upper bound

#### Details

Note that due to the vectorization of the rnorm, quorm commands in R, all arguments can be vectors of equal length. This makes the inverse CDF method the most efficient to use in R.

#### Value

draw (possibly a vector)

### Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 2.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

#### Examples

```
##
set.seed(66)
rtrun(mu=c(rep(0,10)),sigma=c(rep(1,10)),a=c(rep(0,10)),b=c(rep(2,10)))
```

runireg

IID Sampler for Univariate Regression

## Description

runizeg implements an iid sampler to draw from the posterior of a univariate regression with a conjugate prior.

#### Usage

```
runireg(Data, Prior, Mcmc)
```

### Arguments

Data list(y,X)

Prior list(betabar, A, nu, ssq)

Mcmc list(R, keep)

## **Details**

```
Model: y = Xbeta + e. e \sim N(0, sigmasq).
```

Priors:  $beta \sim N(betabar, sigmasq * A^{-1})$ .  $sigmasq \sim (nu * ssq)/chisq_{nu}$ . List arguments contain

X n x k Design Matrix

y n x 1 vector of observations

betabar k x 1 prior mean (def: 0)

A k x k prior precision matrix (def: .01I)

nu d.f. parm for Inverted Chi-square prior (def: 3)

```
ssq scale parm for Inverted Chi-square prior (def: var(y))
R number of draws
keep thinning parameter - keep every keepth draw
```

#### Value

list of iid draws

betadraw R x k array of betadraws sigmasqdraw R vector of sigma-sq draws

## Author(s)

 $Peter Rossi, Graduate School of Business, University of Chicago, \\ \langle Peter.Rossi@ChicagoGsb.edu \rangle.$ 

### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 2.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

#### See Also

runiregGibbs

```
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=2000} else {R=10}
set.seed(66)
n=200
X=cbind(rep(1,n),runif(n)); beta=c(1,2); sigsq=.25
y=X%*%beta+rnorm(n,sd=sqrt(sigsq))
out=runireg(Data=list(y=y,X=X),Mcmc=list(R=R))
cat("Summary of beta/sigma-sq draws",fill=TRUE)
summary(out$betadraw,tvalues=beta)
summary(out$sigmasqdraw,tvalues=sigsq)
if(0){
## plotting examples
plot(out$betadraw)
}
```

Gibbs Sampler for Univariate Regression

## runiregGibbs

## Description

runiregGibbs implements a Gibbs Sampler to draw from posterior of a univariate regression with a conditionally conjugate prior.

# Usage

```
runiregGibbs(Data, Prior, Mcmc)
```

## Arguments

 ${\tt Data} \qquad \qquad {\tt list}(y,\!X)$ 

Prior list(betabar,A, nu, ssq)
Mcmc list(sigmasq,R,keep)

#### **Details**

```
Model: y = Xbeta + e. e \sim N(0, sigmasq).
```

Priors:  $beta \sim N(betabar, A^{-1})$ .  $sigmasq \sim (nu * ssq)/chisq_{nu}$ . List arguments contain

X n x k Design Matrix

y n x 1 vector of observations

betabar k x 1 prior mean (def: 0)

A k x k prior precision matrix (def: .01I)

nu d.f. parm for Inverted Chi-square prior (def: 3)

ssq scale parm for Inverted Chi-square prior (def:var(y))

R number of MCMC draws

keep thinning parameter - keep every keepth draw

### Value

list of MCMC draws

betadraw R x k array of betadraws sigmasqdraw R vector of sigma-sq draws

## Author(s)

 $Peter\ Rossi,\ Graduate\ School\ of\ Business,\ University\ of\ Chicago,\ \langle Peter.Rossi@ChicagoGsb.edu\rangle.$ 

#### References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 3.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

#### See Also

```
runireg
```

## Examples

```
if(nchar(Sys.getenv("LONG_TEST")) != 0) {R=1000} else {R=10}
set.seed(66)
n=100
X=cbind(rep(1,n),runif(n)); beta=c(1,2); sigsq=.25
y=X%*%beta+rnorm(n,sd=sqrt(sigsq))

Data1=list(y=y,X=X); Mcmc1=list(R=R)
out=runiregGibbs(Data=Data1,Mcmc=Mcmc1)

cat("Summary of beta and Sigma draws",fill=TRUE)
summary(out$betadraw,tvalues=beta)
summary(out$sigmasqdraw,tvalues=sigsq)

if(0){
## plotting examples
plot(out$betadraw)
}
```

rwishart

Draw from Wishart and Inverted Wishart Distribution

# Description

rwishart draws from the Wishart and Inverted Wishart distributions.

## Usage

```
rwishart(nu, V)
```

# Arguments

nu d.f. parameter

V pds location matrix

### **Details**

In the parameterization used here,  $W \sim W(nu, V)$ , E[W] = nuV.

If you want to use an Inverted Wishart prior, you *must invert the location matrix* before calling rwishart, e.g.

```
Sigma \sim IW(nu, V); Sigma^{-1} \sim W(nu, V^{-1}).
```

#### Value

W	Wishart draw
IW	Inverted Wishart draw
C	Upper tri root of W
CI	$inv(C), W^{-1} = CICI'$

## Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

## References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 2.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

## Examples

```
##
set.seed(66)
rwishart(5,diag(3))$IW
```

Scotch

Survey Data on Brands of Scotch Consumed

## Description

from Simmons Survey. Brands used in last year for those respondents who report consuming scotch.

## Usage

data(Scotch)

#### **Format**

A data frame with 2218 observations on the following 21 variables. All variables are coded 1 if consumed in last year, 0 if not.

```
Chivas.Regal a numeric vector
Dewar.s.White.Label a numeric vector
Johnnie.Walker.Black.Label a numeric vector
J...B a numeric vector
Johnnie.Walker.Red.Label a numeric vector
Other.Brands a numeric vector
Glenlivet a numeric vector
Cutty.Sark a numeric vector
Glenfiddich a numeric vector
Pinch..Haig. a numeric vector
Clan.MacGregor a numeric vector
Ballantine a numeric vector
Macallan a numeric vector
Passport a numeric vector
Black...White a numeric vector
Scoresby.Rare a numeric vector
Grants a numeric vector
Ushers a numeric vector
White. Horse a numeric vector
Knockando a numeric vector
the.Singleton a numeric vector
```

### Source

Edwards, Y. and G. Allenby (2003), "Multivariate Analysis of Multiple Response Data," JMR 40, 321-334.

# References

```
Chapter 4, Bayesian Statistics and Marketing by Rossi et al. http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html
```

```
data(Scotch)
cat(" Frequencies of Brands", fill=TRUE)
mat=apply(as.matrix(Scotch),2,mean)
print(mat)
##
## use Scotch data to run Multivariate Probit Model
```

```
##
if(0){
##
y=as.matrix(Scotch)
p=ncol(y); n=nrow(y)
dimnames(y)=NULL
y=as.vector(t(y))
y=as.integer(y)
I_p=diag(p)
X=rep(I_p,n)
X=matrix(X,nrow=p)
X=t(X)
R=2000
Data=list(p=p,X=X,y=y)
Mcmc=list(R=R)
set.seed(66)
out=rmvpGibbs(Data=Data,Mcmc=Mcmc)
ind=(0:(p-1))*p + (1:p)
cat(" Betadraws ",fill=TRUE)
mat=apply(out$betadraw/sqrt(out$sigmadraw[,ind]),2,quantile,probs=c(.01,.05,.5,.95,.99))
attributes(mat)$class="bayesm.mat"
summary(mat)
rdraw=matrix(double((R)*p*p),ncol=p*p)
rdraw=t(apply(out$sigmadraw,1,nmat))
attributes(rdraw)$class="bayesm.var"
cat(" Draws of Correlation Matrix ",fill=TRUE)
summary(rdraw)
}
```

simnhlogit

Simulate from Non-homothetic Logit Model

### Description

simnhlogit simulates from the non-homothetic logit model

#### Usage

```
simnhlogit(theta, lnprices, Xexpend)
```

# Arguments

 $\begin{array}{ll} \hbox{\tt theta} & \hbox{\tt coefficient vector} \\ \hbox{\tt lnprices} & \hbox{\tt n} \ \hbox{\tt x} \ \hbox{\tt p} \ \hbox{\tt array} \ \hbox{\tt of prices} \\ \end{array}$ 

Xexpend n x k array of values of expenditure variables

#### **Details**

For detail on parameterization, see llnhlogit.

#### Value

a list containing:

y n x 1 vector of multinomial outcomes (1, ..., p)

Xexpend expenditure variables

lnprices price array
theta coefficients

prob n x p array of choice probabilities

## Warning

This routine is a utility routine that does **not** check the input arguments for proper dimensions and type.

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

## References

For further discussion, see *Bayesian Statistics and Marketing* by Rossi, Allenby and McCulloch, Chapter 4.

http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

#### See Also

llnhlogit

summary.bayesm.mat Summarize Mcmc Parameter Draws

## Description

summary.bayesm.mat is an S3 method to summarize marginal distributions given an array
of draws

# Usage

```
## S3 method for class 'bayesm.mat':
summary(object, names, burnin = trunc(0.1 * nrow(X)), tvalues, QUANTILES = TRUE, TRAILER = TRUE
```

## Arguments

object (hereafter X) is an array of draws, usually an object of class

"bayesm.mat"

names optional character vector of names for the columns of X

burnin number of draws to burn-in, def: .1\*nrow(X)

tvalues optional vector of "true" values for use in simulation examples

QUANTILES logical for should quantiles be displayed, def: TRUE

TRAILER logical for should a trailer be displayed, def: TRUE

... optional arguments for generic function

### **Details**

Typically, summary.bayesm.nmix will be invoked by a call to the generic summary function as in summary(object) where object is of class bayesm.mat. Mean, Std Dev, Numerical Standard error (of estimate of posterior mean), relative numerical efficiency (see numEff) and effective sample size are displayed. If QUANTILES=TRUE, quantiles of marginal distirbutions in the columns of X are displayed.

summary.bayesm.mat is also exported for direct use as a standard function, as in summary.bayesm.mat(matrix).

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

### See Also

```
summary.bayesm.var, summary.bayesm.nmix
```

## Examples

```
##
## not run
# out=rmnpGibbs(Data,Prior,Mcmc)
# summary(out$betadraw)
#
```

summary.bayesm.nmix Summarize Draws of Normal Mixture Components

## Description

summary.bayesm.nmix is an S3 method to display summaries of the distribution implied by draws of Normal Mixture Components. Posterior means and Variance-Covariance matrices are displayed.

Note: 1st and 2nd moments may not be very interpretable for mixtures of normals. This summary function can take a minute or so. The current implementation is not efficient.

## Usage

```
## S3 method for class 'bayesm.nmix':
summary(object, names,burnin = trunc(0.1 * nrow(probdraw)), ...)
```

#### **Arguments**

object an object of class "bayesm.nmix" - a list of lists of draws

names optional character vector of names fo reach dimension of the density

burnin number of draws to burn-in, def: .1\*nrow(probdraw)

... parms to send to summary

#### Details

an object of class "bayesm.nmix" is a list of three components:

probdraw a matrix of R/keep rows by  $\dim$  of normal mix of mixture prob draws

second comp not used

compdraw list of lists with draws of mixture comp parms

## Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

## See Also

```
summary.bayesm.mat, summary.bayesm.var
```

```
##
## not run
# out=rnmix(Data,Prior,Mcmc)
# summary(out)
#
```

Summarize Draws of Var-Cov Matrices

summary.bayesm.var

### Description

summary.bayesm.var is an S3 method to summarize marginal distributions given an array of draws

## Usage

```
## S3 method for class 'bayesm.var':
summary(object, names, burnin = trunc(0.1 * nrow(Vard)), tvalues, QUANTILES = FALSE , ...)
```

### Arguments

object (herafter, Vard) is an array of draws of a covariance matrix

names optional character vector of names for the columns of Vard

burnin number of draws to burn-in, def: .1\*nrow(Vard)

tvalues optional vector of "true" values for use in simulation examples

QUANTILES logical for should quantiles be displayed, def: TRUE

... optional arguments for generic function

### **Details**

Typically, summary.bayesm.var will be invoked by a call to the generic summary function as in summary(object) where object is of class bayesm.var. Mean, Std Dev, Numerical Standard error (of estimate of posterior mean), relative numerical efficiency (see numEff) and effective sample size are displayed. If QUANTILES=TRUE, quantiles of marginal distirbutions in the columns of Vard are displayed.

Vard is an array of draws of a covariance matrix stored as vectors. Each row is a different draw.

The posterior mean of the vector of standard deviations and the correlation matrix are also displayed

### Author(s)

Peter Rossi, Graduate School of Business, University of Chicago, (Peter.Rossi@ChicagoGsb.edu).

### See Also

summary.bayesm.mat, summary.bayesm.nmix

## Examples

```
##
## not run
# out=rmnpGibbs(Data,Prior,Mcmc)
# summary(out$sigmadraw)
#
```

tuna

Data on Canned Tuna Sales

### Description

Volume of canned tuna sales as well as a measure of display activity, log price and log wholesale price. Weekly data aggregated to the chain level. This data is extracted from the Dominick's Finer Foods database maintained by the University of Chicago http://http://research.chicagogsb.ed Brands are seven of the top 10 UPCs in the canned tuna product category.

## Usage

data(tuna)

### Format

A data frame with 338 observations on the following 30 variables.

WEEK a numeric vector

MOVE1 unit sales of Star Kist 6 oz.

MOVE2 unit sales of Chicken of the Sea 6 oz.

MOVE3 unit sales of Bumble Bee Solid 6.12 oz.

 ${\tt MOVE4}$  unit sales of Bumble Bee Chunk 6.12 oz.

MOVE5 unit sales of Geisha 6 oz.

MOVE6 unit sales of Bumble Bee Large Cans.

MOVE7 unit sales of HH Chunk Lite 6.5 oz.

NSALE1 a measure of display activity of Star Kist 6 oz.

NSALE2 a measure of display activity of Chicken of the Sea 6 oz.

NSALE3 a measure of display activity of Bumble Bee Solid 6.12 oz.

NSALE4 a measure of display activity of Bumble Bee Chunk 6.12 oz.

NSALE5 a measure of display activity of Geisha 6 oz.

NSALE6 a measure of display activity of Bumble Bee Large Cans.

NSALE7 a measure of display activity of HH Chunk Lite 6.5 oz.

LPRICE1 log of price of Star Kist 6 oz.

```
LPRICE2 log of price of Chicken of the Sea 6 oz.

LPRICE3 log of price of Bumble Bee Solid 6.12 oz.

LPRICE4 log of price of Bumble Bee Chunk 6.12 oz.

LPRICE5 log of price of Geisha 6 oz.

LPRICE6 log of price of Bumble Bee Large Cans.

LPRICE7 log of price of HH Chunk Lite 6.5 oz.

LWHPRIC1 log of wholesale price of Star Kist 6 oz.

LWHPRIC2 log of wholesale price of Chicken of the Sea 6 oz.

LWHPRIC3 log of wholesale price of Bumble Bee Solid 6.12 oz.

LWHPRIC4 log of wholesale price of Bumble Bee Chunk 6.12 oz.

LWHPRIC5 log of wholesale price of Geisha 6 oz.

LWHPRIC6 log of wholesale price of Bumble Bee Large Cans.

LWHPRIC7 log of wholesale price of HH Chunk Lite 6.5 oz.

FULLCUST total customers visits
```

#### Source

Chevalier, A. Judith, Anil K. Kashyap and Peter E. Rossi (2003), "Why Don't Prices Rise During Periods of Peak Demand? Evidence from Scanner Data," *The American Economic Review*, 93(1), 15-37.

### References

Chapter 7, Bayesian Statistics and Marketing by Rossi et al. http://faculty.chicagogsb.edu/peter.rossi/research/bsm.html

```
data(tuna)
cat(" Quantiles of sales",fill=TRUE)
mat=apply(as.matrix(tuna[,2:5]),2,quantile)
print(mat)
## example of processing for use with rivGibbs
##
if(0)
{
 data(tuna)
 t = dim(tuna)[1]
  customers = tuna[,30]
  sales = tuna[,2:8]
 lnprice = tuna[,16:22]
 lnwhPrice= tuna[,23:29]
  share=sales/mean(customers)
  shareout=as.vector(1-rowSums(share))
 lnprob=log(share/shareout)
```

```
# create w matrix
 I1=as.matrix(rep(1, t))
 IO=as.matrix(rep(0, t))
 intercept=rep(I1, 4)
 brand1=rbind(I1, I0, I0, I0)
 brand2=rbind(I0, I1, I0, I0)
 brand3=rbind(I0, I0, I1, I0)
 w=cbind(intercept, brand1, brand2, brand3)
## choose brand 1 to 4
 y=as.vector(as.matrix(lnprob[,1:4]))
 X=as.vector(as.matrix(lnprice[,1:4]))
 lnwhPrice=as.vector(as.matrix (lnwhPrice[1:4]))
 z=cbind(w, lnwhPrice)
 Data=list(z=z, w=w, x=X, y=y)
 Mcmc=list(R=R, keep=1)
 set.seed(66)
 out=rivGibbs(Data=Data,Mcmc=Mcmc)
 cat(" betadraws ",fill=TRUE)
 summary(out$betadraw)
if(0){
## plotting examples
plot(out$betadraw)
}
```