COMP4680/COMP8650: Advanced Topics in SML

Assignment #2: Convex Sets and Convex Functions

Due: 11:55pm on Friday 17 August, 2018. Submit as a single PDF file via Wattle.

Numbers (e.g., **X.YY**) refer to questions from the textbook *Boyd and Vandenberghe*, "Convex Optimization", 2004. All questions are of equal value.

- Halfspace. Consider the set $H = \{x \in \mathbb{R}^n \mid ||x x_0||_2 \le ||x x_1||_2\}$ for fixed x_0 and x_1 . Show that H is a half-space.
- Polyhedron. Consider the polyhedron in \mathbb{R}^2 defined as the convex hull over the following set of points

$$\{(-1,2),(0,3),(2,0),(2,-2),(0,0),(-1,0)\}.$$

Express the polyhedron in the form $Ax \leq b$.

- 2.12
- **2.15** (a), (b), (e), (f)
- 3.14

Hint: Think of first- and second-order conditions for optimality.

- 3.16
- **3.36** (a), (b) and (e)

Be sure to justify your answers.