

Gradient Descent With Momentum.

velocity

$$V_{dw} = \beta V_{dw} + (1 - \beta) dw \quad \text{acceleration}$$

$$V_{db} = \beta V_{db} + (1 - \beta) db$$

$$W = W - \alpha V_{dw}, \quad b = b - \alpha V_{db}$$

Hyperparameters: α, β $\beta = 0.9$ (average our last 10 gradients)

acceleration (next gradient)

changes current velocity (momentum) by some extent.

RMSprop

$$S_{dw} = \beta_2 S_{dw} + (1 - \beta_2) dw^2$$

$$S_{db} = \beta_2 S_{db} + (1 - \beta_2) db^2$$

$$W := W - \alpha \frac{dw}{\sqrt{S_{dw} + \epsilon}}$$

$$b := b - \alpha \frac{db}{\sqrt{S_{db} + \epsilon}}$$

Adam optimization algorithm.

$$V_{dw} = 0, \quad S_{dw} = 0, \quad V_{db} = 0, \quad S_{db} = 0$$

On iteration t :

compute dw, db through mini-batch.

$$V_{dw} = \beta_1 V_{dw} + (1 - \beta_1) dw, \quad V_{db} = \beta_1 V_{db} + (1 - \beta_1) db \quad \leftarrow \text{"momentum"} \beta_1$$

$$S_{dw} = \beta_2 S_{dw} + (1 - \beta_2) dw^2, \quad S_{db} = \beta_2 S_{db} + (1 - \beta_2) db^2 \quad \leftarrow \text{"RMSprop"} \beta_2$$

$$V_{dw}^{\text{corrected}} = V_{dw} / (1 - \beta_1)^t, \quad V_{db}^{\text{corrected}} = \dots$$

$$S_{dw}^{\text{corrected}} = \dots, \quad S_{db}^{\text{corrected}} = \dots$$

$$W := W - \alpha \frac{V_{dw}^{\text{corrected}}}{\sqrt{S_{dw}^{\text{corrected}} + \epsilon}} \quad b := \dots$$

Hyperparameter choice :

→ α : needs to be tune

$$\beta_1 = 0.9 \rightarrow (dw)$$

$$\beta_2 = 0.999 \rightarrow (dw^2)$$

$$\underline{\epsilon = 10^{-8}} \quad \text{Avoid divided by zero Exception.}$$