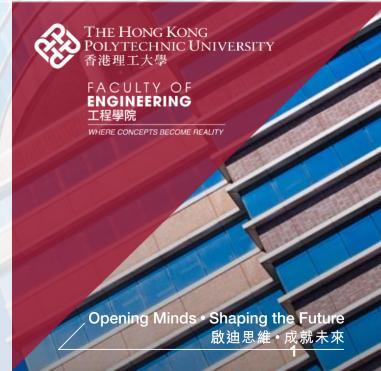
Optimization of Traffic Count Locations for Estimation of Travel Demands with Covariance between Origin-Destination Flows

-- published in Transportation Research Part C

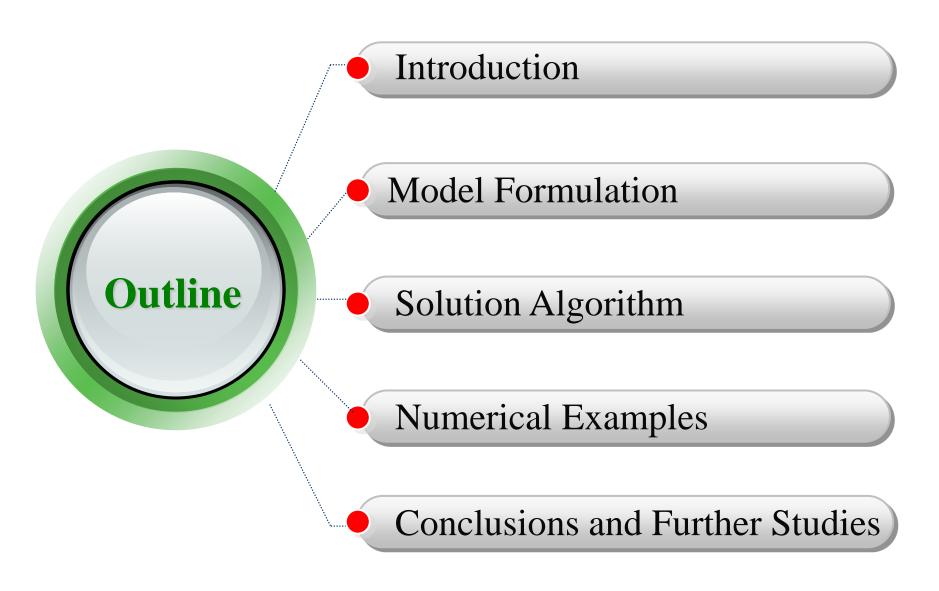
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Fu, H., Lam, W.H.K., Shao, H., Xu, X.P., Lo, H.P., Chen, B.Y., Sze, N.N., Sumalee, A., 2019. Optimization of traffic count locations for estimation of travel demands with covariance between origin-destination flows. Transportation Research Part C: Emerging Technologies 108, 49–73.









Introduction – Hong Kong Statistics

- ❖ Population: 7.48 million
- * Total area: 1,111 km²

(24% land developed)

- Population density:
- > 6,732 persons/km² (Total land average)
- > 28,050 persons/km² (Developed land average) Taipei: 9,950; Tokyo: 6,220; Bangkok: 5,300; Calgary: 1,833
- > 55,000 persons/km² (Highest district)
- Arr Road length = 2,123 km
- No. of licensed vehicles = 784,400 (as at December 2018)
- * 565,200 private cars out of 784,400 licensed vehicles in Hong Kong as at December 2018



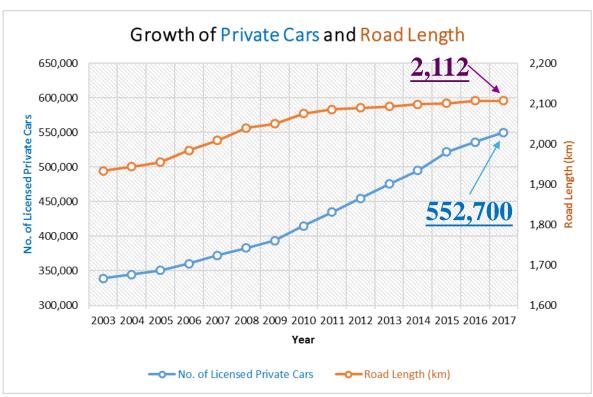




Traffic Congestion in Hong Kong







No. of private cars: increased > 60% over the past 15 years Road length: increased < 10% over the past 15 years

As a result, traffic density is increasing and average private car occupancy for private cars is also increasing.



Introduction – Vehicle Classification and Occupancy

Hong Kong External Cordon (Boundary between the Northern Part and Southern Part of **Hong Kong Island**)





Time					(Class of	vehicle	•			
		Motor	Private	Taxi	Private	PLB	Good		Non-	Fr.	Bus
		Cycle	Car		LB		Light	Med. /Heavy	Fr. Bus	SD	DD
0700-0800	Pro	5.1	42.8	20.1	2.5	1.1	15.4	4.5	3.2	0.0	5.3
	Оср	1.0	1.3	2.2	6.5	14.6	1.5	1.3	17.7	0.0	62.4
0800-0900	Pro	4.5	56.0	12.6	0.7	0.8	13.0	3.6	3.2	0.1	5.6
Peak hour	Оср	1.0	1.3	2.1	5.7	12.4	1.6	1.5	30.6	44.0	70.4
0900-1000	Pro	3.0	44.9	16.1	0.3	0.6	24.2	4.3	1.8	0.0	4.9
	Оср	1.1	1.3	2.3	4.1	13.6	1.7	1.5	14.7	0.0	39.3
1000-1100	Pro	2.9	45.5	17.0	0.6	0.4	23.4	4.5	1.8	0.1	3.8
	Оср	1.0	1.4	2.2	1.6	12.0	1.5	1.4	13.4	3.5	32.9
1100-1200	Pro	2.1	44.5	18.0	0.4	0.3	24.6	3.9	2.5	0.1	3.7
	Оср	1.1	1.4	2.3	1.7	15.2	1.5	1.3	17.8	1.0	34.9
1200-1300	Pro	2.1	45.9	16.2	1.1	0.5	24.9	3.9	2.1	0.1	3.3
	Оср	1.1	1.4	2.3	4.6	9.4	1.4	1.3	17.7	1.0	35.5
1300-1400	Pro	2.3	43.5	17.6	0.9	0.4	22.3	6.7	2.7	0.0	3.6
	Оср	1.1	1.4	2.3	5.2	10.3	1.5	1.4	15.9	0.0	38.3
1400-1500	Pro	2.8	44.8	17.9	0.8	0.3	23.7	4.4	1.9	0.0	3.4
	Оср	1.1	1.5	2.4	2.1	13.0	1.5	1.3	14.6	0.0	38.6
1500-1600	Pro	2.4	49.1	15.5	1.5	0.3	21.3	4.5	2.0	0.0	3.3
	Оср	1.1	1.5	2.3	6.3	14.7	1.5	1.3	16.3	0.0	39.8
1600-1700	Pro	3.0	45.1	16.1	1.6	0.5	23.4	3.5	2.8	0.1	4.1
	Ocp	1.1	1.5	2.3	3.6	12.1	1.5	1.2	9.7	1.0	41.0
1700-1800	Pro	4.9	56.3	12.3	0.6	0.6	15.9	1.5	3.3	0.1	4.5
	Оср	1.1	1.4	2.3	2.5	13.5	1.6	1.4	19.3	24.0	53.4
1800-1900	Pro	5.9	61.7	12.1	0.3	0.9	9.8	1.2	3.4	0.1	4.7
	Оср	1.1	1.3	2.4	2.1	15.7	1.4	1.3	28.1	1.0	72.3
1900-2000	Pro	3.4	62.6	16.3	0.1	1.0	6.6	1.4	3.3	0.1	5.3
	Оср	1.1	1.3	2.3	1.2	14.6	1.4	1.4	16.2	22.0	53.6
2000-2100	Pro	2.7	57.8	23.4	0.1	1.3	6.1	1.3	1.8	0.0	5.6
	Оср	1.1	1.4	2.4	1.0	11.5	1.4	1.4	13.0	0.0	43.0
2100-2200	Pro	2.7	52.2	31.8	0.1	1.4	4.5	1.3	1.1	0.0	4.9
	Оср	1.1	1.4	2.2	2.5	9.5	1.4	1.3	13.0	0.0	44.6
2200-2300	Pro	2.8	52.9	32.6	0.1	1.4	3.9	0.8	0.9	0.0	4.6
	Оср	1.1	1.4	2.3	2.2	12.2	1.5	1.4	12.9	0.0	46.9
16 hours	Pro	3.4	50.4	17.8	0.7	0.7	16.9	3.3	2.4	0.1	4.4
	Оср	1.1	1.4	2.3	4.5	12.8	1.5	1.4	18.4	11.3	48.8

AM Peak Hour

Average private occupancy car for private cars is 1.4:

Evidence of ride sharing

Legend

Proportion of vehicles in % (Sum may not add up to 100% due to figure rounding)

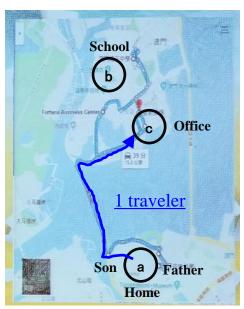
Average occupancy of vehicles



Introduction – Illustration Example

OD: (a-c)

The father drives to office directly, and the son goes to school by bus.



School 1 traveler Office 2 travelers 大马驰游 Father Son Home

OD: (a-b) (b-c)

The father and son travel from home to school together, and then the father travels from school to office alone.

(a) No Ridesharing mode

(b) Ridesharing mode

In the case of "No Ridesharing mode", we assume that all OD demands follow an independent normal distribution:

$$OD(a-c) \sim N(200,30^2)$$

$$OD(a-b) \sim N(150,36^2)$$

$$OD(b-c) \sim N(100, 25^2)$$

Total OD demands: 450

Effect of Ridesharing on the OD demand covariance and average vehicle occupancy

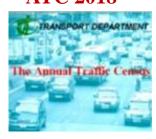
Proportion of travelers	Covariance (a-b, b-c)	Average vehicle
using ridesharing		occupancy
0.0%	0.0	1.00
17.8%	28.5	1.19
50.0%	225.0	1.80
100.0%	900.0	2.25

Average vehicle occupancy: average number of people in a vehicle, including the driver



Introduction – Traffic Flow Variations

111 core stations* in **ATC 2018**



Month to month

Hour to hour

*Core station is a randomly selected count station providing hourly, daily, monthly factors to generalize the traffic characteristics for its own group of links

YEAR Location

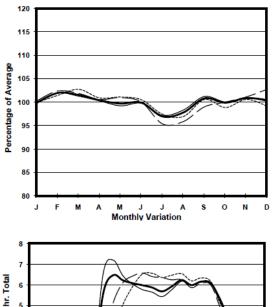
2018

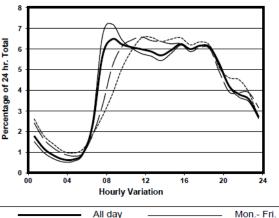
Hong Kong External Cordon(Boundary between the Northern Part and Southern Part of Hong Kong Island)

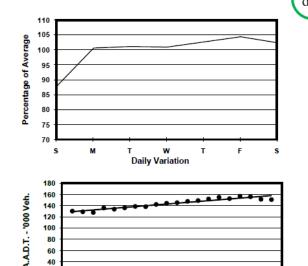
Stations on Cordon/Screenline

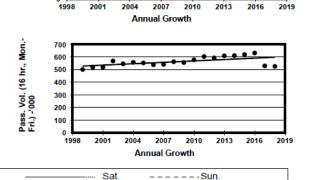
1004, 1021, 2201, 2202, 2206, 2401 and 2407

1. TRAFFIC FLOW VARIATION AND GROWTH











Loop detector detector data data

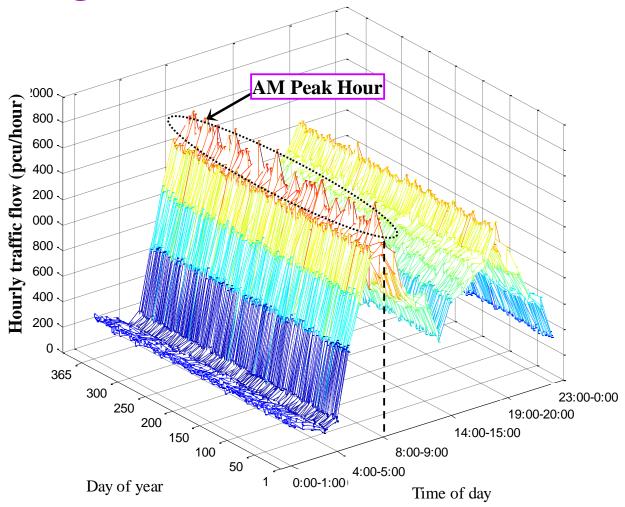
Day to day

Year to year



Introduction

- Hourly Origin-Destination Demands under Uncertainty





Introduction – Contributions

***** Theoretical development:

- Propose a **new criterion** for measuring the estimation accuracy of OD demand covariance in stochastic road networks under uncertainty.
- Introduce a **new model formulation** for investigating how to optimize the traffic count locations for minimizing the weighted maximum deviation of estimated mean and covariance of OD demands from the observed values together with their mathematical properties.

Methodology development:

- Adopt a weighted-sum objective by considering the effect of mean and covariance OD demand on the traffic count locations.
- Propose the solution algorithm for solving the bi-criteria and/or bi-objective optimization problems.
- Link choice proportions are regarded as stochastic variables and updated by an adapted traffic flow simulator in this study.



Model Formulation – Assumptions

- * A1. It is assumed that all the observed link traffic counts are error free (Yang et al., 1991; Yang and Zhou, 1998).
- ❖ A2. The covariance of traffic demand between each OD pair is positive. Note that the latent demand could not be observed on the basis of traffic counts in practice. As the OD demand is estimated by actual traffic counts in this study, the traffic counts should then be positive. As a result, the covariance between OD flows should also be positive always.
- *A3. It is assumed that there is only one traffic sensor allocated at each selected count location.



Model Formulation

- Sample mean and sample covariance of observed link traffic flows

The sample mean of observed AM Peak hourly link flows vector (\mathbf{v}) over h days can be calculated as:

$$\mathbf{v} = (\cdots, v_a, \cdots)^T = \frac{1}{h} \sum_{l=1}^{h} \mathbf{v}^{(l)}$$
 Sample size h, say 300 weekdays

The sample covariance matrix of observed AM Peak hourly link flows (Σ^{v}) over h days can be calculated as:

$$\Sigma^{\mathbf{v}} = \left\{ \sigma_{a,b}^{v} \right\}_{\tilde{m} \times \tilde{m}} = \frac{1}{h-1} \sum_{l=1}^{h} \left\{ \left(\mathbf{v}^{(l)} - \mathbf{v} \right) \left(\mathbf{v}^{(l)} - \mathbf{v} \right)^{T} \right\}$$

where $\sigma_{a,b}^{\nu}$ is the sample covariance between observed traffic flows V_a and V_b (random variables), $a,b \in \widetilde{\mathbf{A}}$.



Model Formulation

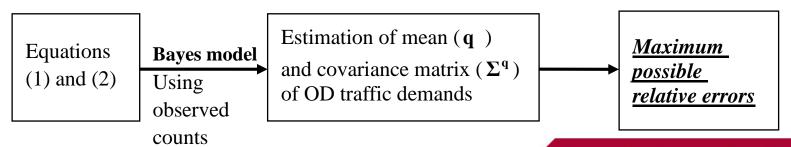
Relationship between observed traffic counts and estimated mean and covariance of OD demand

The mean of observed link flow (v_a) can be obtained by following Equation (1) that:

$$v_{a} = E \left[\sum_{w \in W} p_{a,w} Q_{w} \right] = \sum_{w \in W} p_{a,w} q_{w} \quad \forall \ a \in \widetilde{\mathbf{A}} \quad \text{matrix form} \quad \mathbf{v} = \widetilde{\mathbf{P}} \mathbf{q}$$
 (1)

The covariance between stochastic link flow V_a and V_b can be deduced as:

$$\sigma_{a,b}^{v} = \operatorname{cov}[V_{a}, V_{b}] = \sum_{w \in \mathbf{W}} \sum_{w' \in \mathbf{W}} p_{a,w} p_{b,w'} \sigma_{w,w'}^{q} \quad \forall \ a, b \in \widetilde{\mathbf{A}} \text{ matrix form } \longrightarrow \mathbf{\Sigma}^{\mathbf{v}} = \widetilde{\mathbf{P}} \mathbf{\Sigma}^{\mathbf{q}} \widetilde{\mathbf{P}}^{T} \quad (2)$$





Model Formulation – WMPREM (Yang et al. 1991)

Weighted Maximum possible relative error for the mean OD demand (WMPREM)

Traffic count location scheme Average relative deviation of the mean OD demand

Relative deviation of the estimated **mean** OD demands from the true ones in vector form

OD pair

WMPREM(**z**) = $\max_{\lambda^{mean}} G(\lambda^{mean})$

subject to $\sum p_{a,w} q_w \lambda_w^{mean} = 0 \quad \forall \ a \in \widetilde{\mathbf{A}}$

Link choice proportion by OD

Estimated **mean** OD demand

Boundary constraint

Set of links with traffic count locations

Conservation condition of observed mean link flows

Set of OD pairs

 $\lambda_w^{mean} = (q_w^* - q_w)/q_w$ denote the **relative deviation** of the estimated **mean** OD demand (q_w) from the true one (q_w^*) for OD pair $w \in \mathbf{W}$, q_w^* is the true **mean** (or actual average) OD demand for OD pair $w \in \mathbf{W}$



Model Formulation – WMPREC (This Study)

Weighted *Maximum possible relative error* for the covariance OD demand (WMPREC)

Traffic count location scheme

Average relative deviation of the OD demand **covariance**

WMPREC(\mathbf{z}) = $\max_{\lambda^{\text{cov}}} H(\lambda^{\text{cov}})$

Relative deviation of the estimated OD demand **covariance** from the true ones in vector form

OD pair

Link OD choice proportion

Estimated OD demand **covariance**

subject to $\sum_{w \in \mathbf{W}} \sum_{w' \in \mathbf{W}} p_{a,w} p_{b,w'} \sigma_{w,w'}^q \lambda_{w,w'}^{\text{cov}} = 0$

$$\lambda_{w,w'}^{\text{cov}} \ge -1$$

Conservation condition of observed link flow covariances

Boundary constraint

 $\lambda_{w,w'}^{\text{cov}} = \left(\sigma_{w,w'}^{q^*} - \sigma_{w,w'}^{q}\right) / \sigma_{w,w'}^{q}$ denote the *relative deviation* of the estimated OD demand **covariance** $(\sigma_{w,w'}^{q})$ from the true one $(\sigma_{w,w'}^{q^*})$ between OD pairs w and w'.



Model Formulation – Properties of WMPREC

Property 1: If \tilde{P} is a matrix with full column rank, i.e., $rank(\tilde{P}) = the number of column of <math>\tilde{P}$, Σ^q must be **uniquely** identified when the number of sensors is greater than or equal to the number of OD pairs

Property 2: The WMPREM $(G(\lambda^{mean}))$ and WMPREC $(H(\lambda^{cov}))$ are both finite if and only if the OD Covering Rule is satisfied.

OD Covering Rule: the traffic count locations should be allocated on the network so that the traffic flows (or vehicles/hour) between **any OD pair** can be observed.



Model Formulation – Optimal traffic count location model (bi-objective model)

Traffic count location scheme

$$\min \begin{cases} O_1 = \text{WMPREM}(\mathbf{z}) \\ O_2 = \text{WMPREC}(\mathbf{z}) \end{cases}$$
 Objective Function

s.t.

$$\sum_{i=1}^{m} \delta_{w,a} z_a \ge 1 \quad \forall w \in \mathbf{W} \quad \mathbf{OD covering rule}$$

Constraints

Denote \tilde{P} as the sub-matrix of OD-link choice proportion matrix P with the element $p_{a,w}$, $a \in \tilde{A}$ $rank(\tilde{P}) = \tilde{m}$ link independence rule

$$rank(\widetilde{P}) = \widetilde{m}$$
 link independence rule

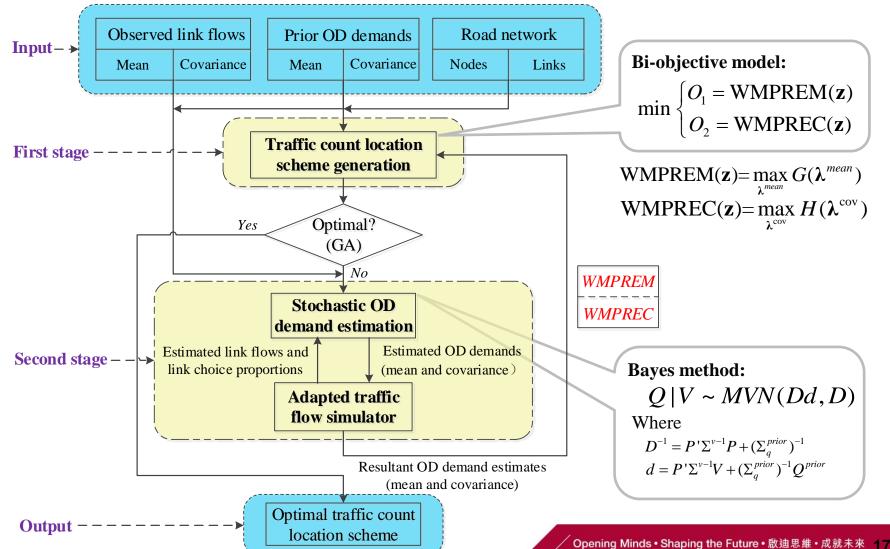
Denote \tilde{m} as number of observed links

 $\Pr(V_a > \overline{v}) \ge p^0 \ \forall a \in \widetilde{\mathbf{A}}$ maximal probability of flow intercepting rule \overline{V}_a is the estimated link flow, \overline{v} is a given threshold, p^0 is a given probability. e.g. $p^0 = 70\%$. $\sum c_a z_a \leq B$ budget constraint

where c_a is the cost for installing and maintaining one sensor on link a and B is the budget.



Problem Statement and Model Formulation





Solution Algorithm

*Since the integer linear programming problem is NP-hard, the proposed model is intractable and so heuristic solution algorithm is used in this study.

For example,

- Firefly Algorithm (FA) (used in this study)
- Genetic Algorithm (GA)
- Branch and bound method
- Backtracking method
- > Tabu search algorithm
- > etc.



Solution Algorithm – Fitness Function

Firefly Algorithm (FA)

Weighted-sum approach

$$\min_{z} \text{WMPRE}(\mathbf{z}) = \alpha \cdot \text{WMPREC}(\mathbf{z}) + (1 - \alpha) \cdot \text{WMPREM}(\mathbf{z})$$

where $0 \le \alpha \le 1$ is the weight of the WMPREC and $(1-\alpha)$ is the weight of WMPREM

• Bi-objective approach

$$\min \begin{cases} O_1 = \text{WMPREM}(\mathbf{z}) \\ O_2 = \text{WMPREC}(\mathbf{z}) \end{cases}$$

As for our bi-objective problem, the solution is **non-dominated** (**Pareto optimal**) In each iteration, the non-dominated solutions but **not a unique optimal solution** will be determined. The population in the next iteration will be generated based on the non-dominated solutions.

In the following numerical examples, only the results of the weighted-sum approach will be presented to illustrate the key findings.

Opening Minds • Shaping the Future • ® blaze # • 成就未来



Example 1 – Small Road Network

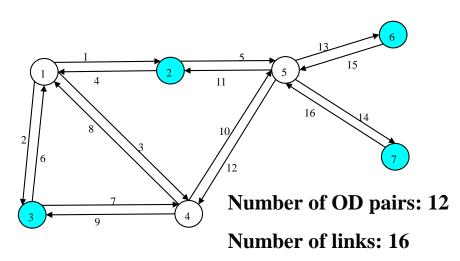


Table 1 The network parameters

OD number	Origin-Destination	Routes	Prior mean OD demands
1	2-3	4-2; 4-3-9	168
2	2-6	4-3-10-13; 5-13	240
3	2-7	4-3-10-14; 5-14	96
4	3-2	6-1; 7-8-1; 7-10-11	208
5	3-6	6-1-5-13; 6-3-10-13; 7-10-13	224
6	3-7	6-1-5-14; 6-3-10-14; 7-10-14	240
7	6-2	15-11; 15-12-8-1	144
8	6-3	15-12-9; 15-12-8-2	168
9	6-7	15-14	184
10	7-2	16-11; 16-12-8-1	120
11	7-3	16-12-8-2; 16-12-9	136
12	7-6	16-13	208

Table 2 Initial Link choice proportions by OD pairs

							1	1				,	1
OD pair Link	1	2	3	4	5	6	7	8	9	10	11	12	Link flow
1				0.9	0.2	0.3	0.4			0.4			485.6
2	0.8							0.4			0.5		350
3	0.2	0.2	0.2	0.1	0.4	0.3							358.1
4 5	1	0.2	0.2										284
5		0.8	0.8		0.2	0.3							477
6				0.9	0.6	0.6							565.9
7				0.1	0.4	0.4							274.1
8				0.1			0.4	0.4		0.4	0.5		343.9
9	0.2							0.6			0.5		240
10		0.2	0.2	0.1	0.8	0.7 5							560.1
11				0.1			0.6			0.6			235.4
12							0.4	1		0.4	1		511.8
13		1			1							1	840
14			1			1			1				650
15							1	1	1				620
16										1	1	1	580

Table 3 The prior covariance matrix of OD demands

OD No.	1	2	3	4	5	6	7	8	9	10	11	12
1	1129.0											
2	1240.2	625.0										
3	366.6	450.1	368.6									
4	820.6	1996.1	354.9	1296.0								
5	831.5	996.1	333.1	648.2	900.0							
6	1526.3	1877.5	596.7	1461.7	1384.5	2304.0						
7	824.5	954.7	354.9	678.6	709.0	1089.7	829.4					
8	973.4	1151.3	429.8	841.6	960.2	1565.1	758.9	1129.0				
9	1049.1	1287.0	407.9	884.5	1282.3	1745.6	943.0	1077.9	1354.2			
10	490.6	514.0	123.2	325.3	471.1	756.6	274.6	447.7	544.4	576.0		
11	782.3	765.2	322.1	706.7	599.0	1205.9	570.2	769.1	780.8	279.2	739.8	
12	825.2	1047.5	295.6	819.0	726.2	1522.6	618.5	861.9	959.4	397.8	556.9	1730.6

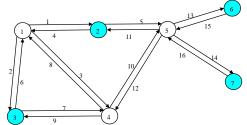


Effects of OD demand covariance on the optimal traffic count locations

 $\min_{\mathbf{z}} \text{ WMPRE}(\mathbf{z}) = \alpha \cdot \text{WMPREC}(\mathbf{z}) + (1 - \alpha) \cdot \text{WMPREM}(\mathbf{z})$

α=0 (only mean)

Number of traffic sensors	WMPRE	The optimal traffic count location scheme selected by WMPREM
5	3.84	3,10,13,15,16
7	2.59	3,4,7,10,13,14,16
8	1.71	1,4,7,10,12,13,14,15
_11	0.17	2,3,4,7,8,9,10,11,12,13,15,16



$\alpha = 0.5$ (both)

Number of traffic sensors	WMPRE	The optimal traffic count location scheme selected by WMPRE
5	2.99	3,5,10,15,16
7	1.79	1,2,4,5,7,13,16
8	1.36	1,3,6,9,11,12,13,14
11	0.15	1,2,3,4,5,7,9,11,12,13,15

$\alpha=1$ (only covariance)

Number of traffic sensors	WMPRE	The optimal traffic count location scheme selected by WMPREC
5	1.78	3,5,10,15,16
7	0.84	1,5,6,9,12,13,14
8	0.77	2,5,6,9,11,13,14,16
11	0.05	1,5,6,9,10,11,12,13,14,15,16

Findings

- 1. links traversed by OD pairs 3-2 & 2-6 with **larger covariance** should be covered by traffic sensors if WMPREC is considered in the objective function.
- 2. Considering the estimation accuracy of **covariance (WMPREC)** could reduce the number of sensors needed so as to have a similar overall estimation accuracy.



Effects of OD demand covariance on the optimal traffic

count locations

 $\min_{\mathbf{z}} \text{ WMPRE}(\mathbf{z}) = \alpha \cdot \text{WMPREC}(\mathbf{z}) + (1 - \alpha) \cdot \text{WMPREM}(\mathbf{z})$

$\alpha=0$ (only mean)

Number of traffic sensors	WMPREM	WMPREC	"Real" relative error of mean OD demands	"Real" relative error of covariance of OD demands
5	3.84	4.21	0.31	0.55
7	2.59	1.82	0.27	0.39
8	1.71	1.33	0.20	0.31
11	0.17	0.33	0.11	0.19

α =0.5 (both)

Number of traffic sensors	WMPREM	WMPREC	"Real" relative error of mean OD demands	"Real" relative error of covariance of OD demands
5	3.92	2.05	0.35	0.29
7	2.65	0.92	0.31	0.21
8	1.80	0.91	0.24	0.17
11	0.21	0.08	0.12	0.09

α =1 (only covariance)

Number of traffic sensors	WMPREM	WMPREC	"Real" relative error of mean OD demands	"Real" relative error of covariance of OD demands
5	4.03	1.78	0.40	0.11
7	2.75	0.84	0.39	0.07
8	1.86	0.77	0.25	0.06
11	0.23	0.05	0.15	0.02

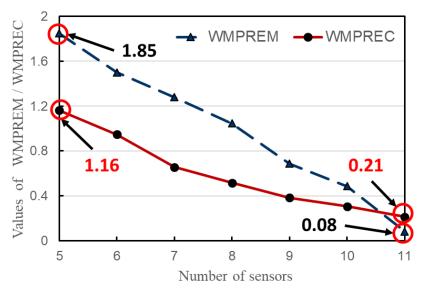
Finding:

Considering WMPREC can effectively reduce the estimation error of OD demand covariance



Effects of the number of traffic sensors on estimation reliability

 $\min_{\mathbf{z}} \text{ WMPRE}(\mathbf{z}) = \alpha \cdot \text{WMPREC}(\mathbf{z}) + (1 - \alpha) \cdot \text{WMPREM}(\mathbf{z}) \qquad \alpha = 0.5$



Effects of number of sensors on WMPREM and WMPREC

Finding:

- It could be observed that when the number of traffic sensors increases, both the **optimal solutions** for WMPREM and WMPREC decrease;
- The reduction range of WMPREM is remarkably greater than that of WMPREC when the number of traffic sensors increases;



Effects of traffic congestion on the proposed model

- WMPREC is more sensitive to traffic congestion

$$\min_{\mathbf{z}} \text{ WMPRE}(\mathbf{z}) = \alpha \cdot \text{WMPREC}(\mathbf{z}) + (1 - \alpha) \cdot \text{WMPREM}(\mathbf{z}) \qquad \alpha = 0.5 \text{ (Both)}$$

Scenario A: Uncongested condition

Scenario B: Congested condition

(HALVE Mean and covariance of OD demand) (DOUBLE Mean and covariance of OD demand)

Relative increase for WMPREM and WMPREC under congested condition compared to that under uncongested condition

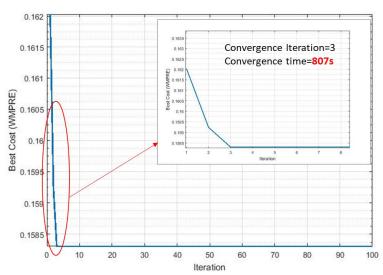
	WMPREM			WMPREC		
Number of traffic sensors	Scenario A	Scenario B	Relative increase (WMPREM _B -WMPREM _A)/ WMPREM _A	Scenario A	Scenario B	Relative increase (WMPREC _B -WMPREC _A)/ WMPREC _A
5	3.64	4.13	13.5%	4.01	6.88	71.5%
7	2.56	3.26	27.4%	2.72	2.97	9.1%
8	2.04	2.26	11.0%	1.99	1.77	-10.9%
11	0.95	0.97	1.9%	0.87	0.88	1.0%

Finding:

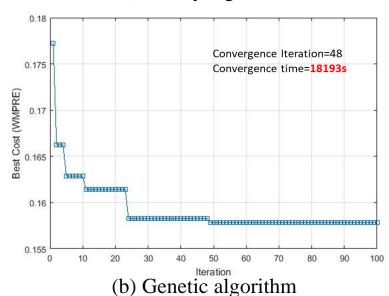
WMPREC is more sensitive to the traffic congestion.

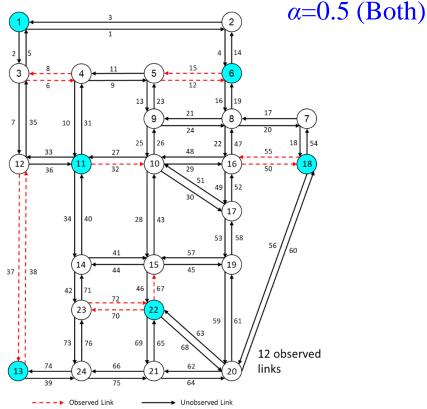


Example 2 – Convergence of solution algorithm



(a) Firefly algorithm





Optimal location schemes

Number of selected OD pairs: 30

Number of links: 76

Number of selected traffic count locations: 12



Conclusions

- An integer programming model is proposed for optimizing traffic account locations for simultaneous estimation of both mean and covariance of the OD demands using traffic counts.
- ❖ Weighted maximum possible relative error for the **covariance** (**WMPREC**) matrix of OD demand is proposed for measuring the quality of the estimated OD **covariance** matrix together with their properties.
- Links traversed by OD pairs with **larger covariance** should be covered by traffic sensors particularly when the covariance of OD demand in increasing in stochastic road networks with uncertainties.
- * Considering the estimation accuracy of **covariance** (**WMPREC**) could reduce the number of sensors required so as to have a similar overall estimation accuracy.
- **WMPREC** is **more sensitive** to the traffic congestion.



Further Studies

- * To facilitate the presentation of essential idea, only the simplest case with constant weighting parameter α is considered in this paper. How to determine different weighting parameters for various OD pairs may be investigated for further study.
- * To develop efficient solution algorithm to solve the proposed model for large-scale road networks in practice.
- To extend the proposed model to consider multi-user classes with vehicular flow and vehicle occupancy data in multi-modal road network.
- * To determine the optimal traffic count locations with considering the probability of sensor failure, as well as the counting errors of the traffic sensors.



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