



# SYMBOL KNOWLEDGE EXTRACTION

From a Simple Graphical Language

Jinpeng LI, Harold MOUCHERE, Christian VIARD-GAUDIN



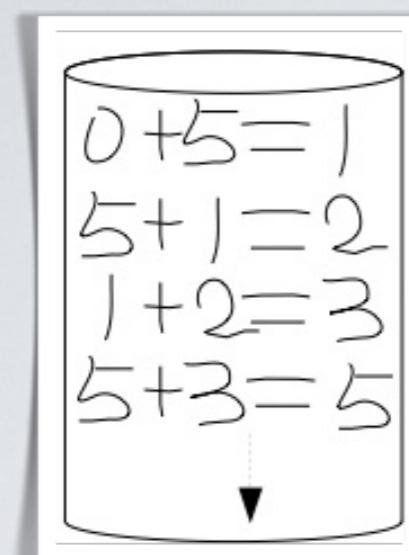
[www.projet-depart.org](http://www.projet-depart.org)

# OUTLINE

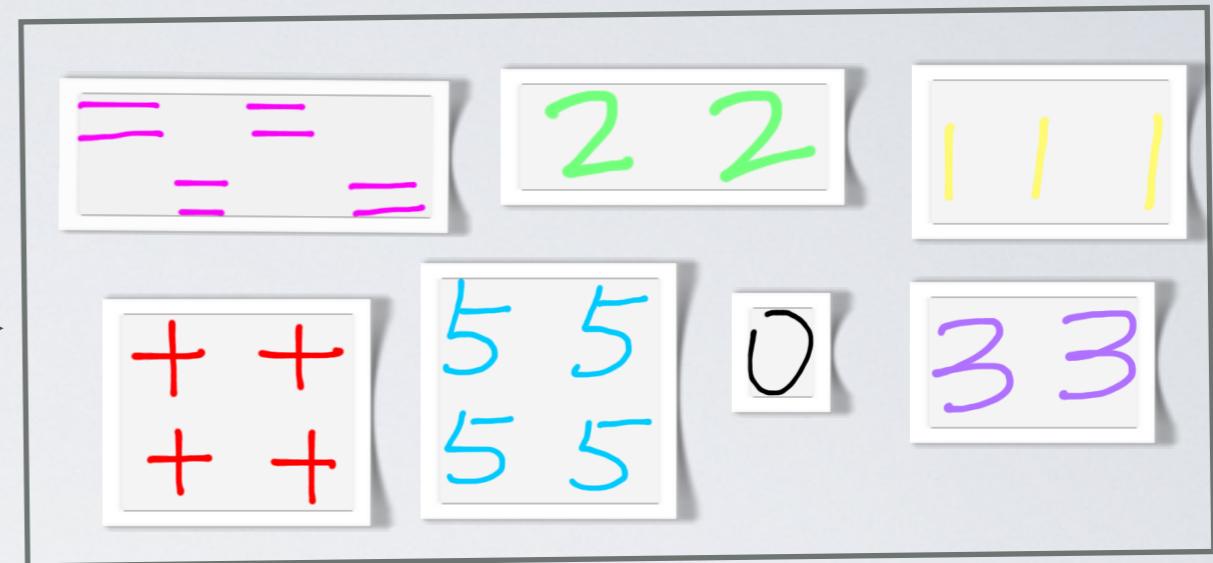
- I. Background
- 2. Graphical Symbol Knowledge Extraction
- 2.1. Quantization (Clustering)
- 2.2. Construction of Relational Graph
- 2.3. Lexicon Extraction
- 3. Conclusion

# BACKGROUND

What is the graphical symbol knowledge extraction?



Symbol  
extraction

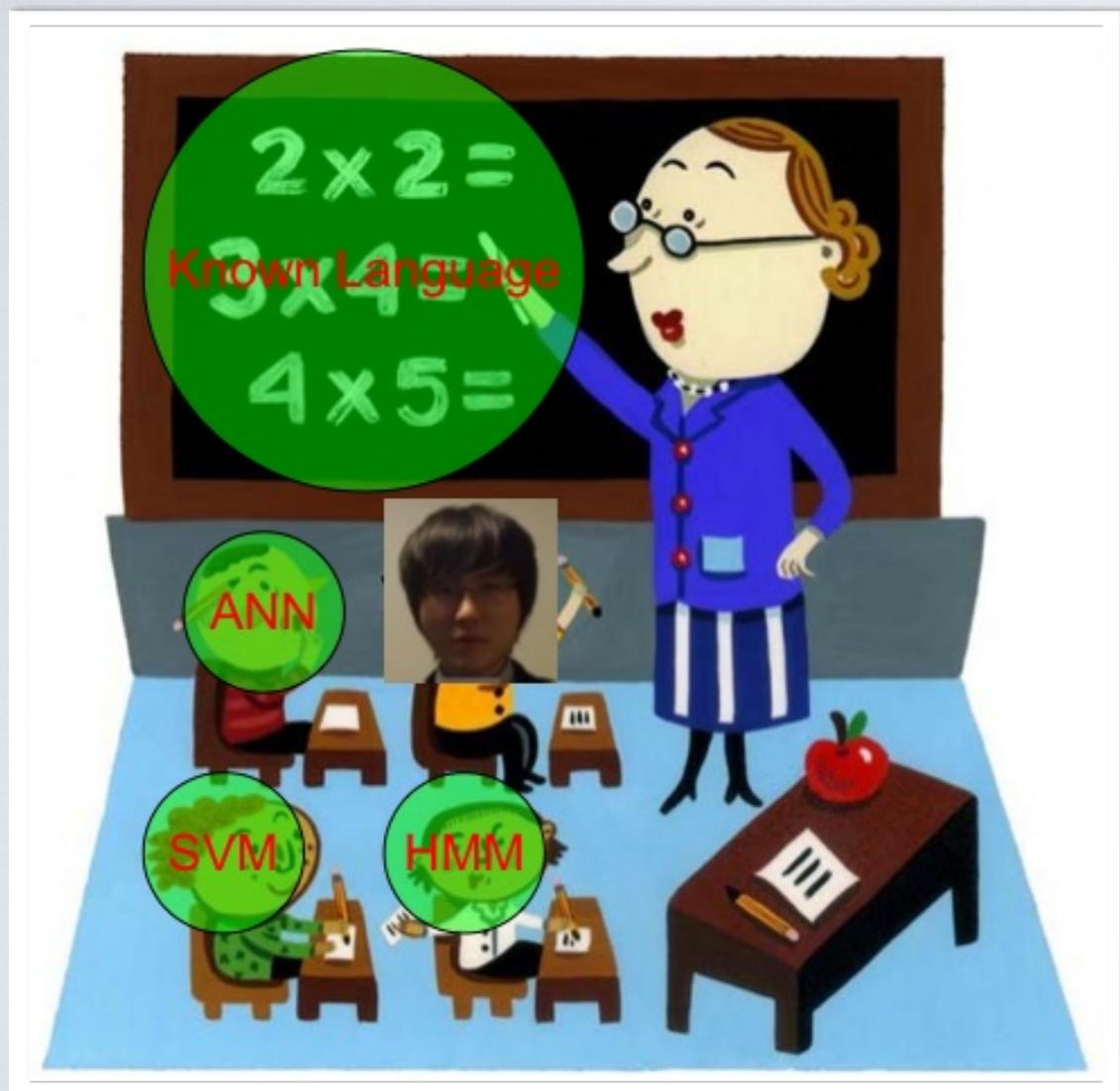


Annotation  
**20** symbols  
have to be labelled

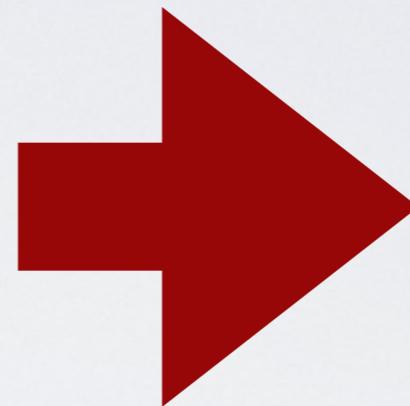


Annotation  
**7** symbols (sets)  
have to be labelled

# TRADITIONAL GRAPHICAL LANGUAGE RECOGNITION



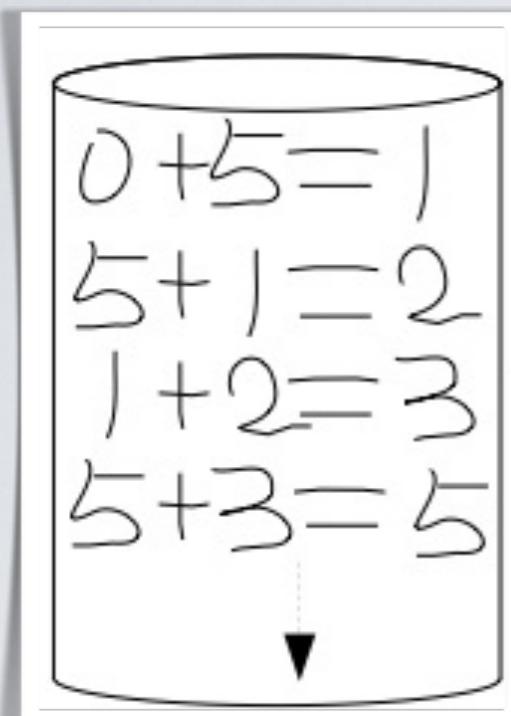
Training



Exams(Tests)

# TRADITIONAL GRAPHICAL LANGUAGE RECOGNITION

Known graphical symbols  
(defined manually)



0	:	0	1	:	1	2	:	2
3	:	3	5	:	5	+	:	+
=	:	=						

Recognition

Training

Classifiers

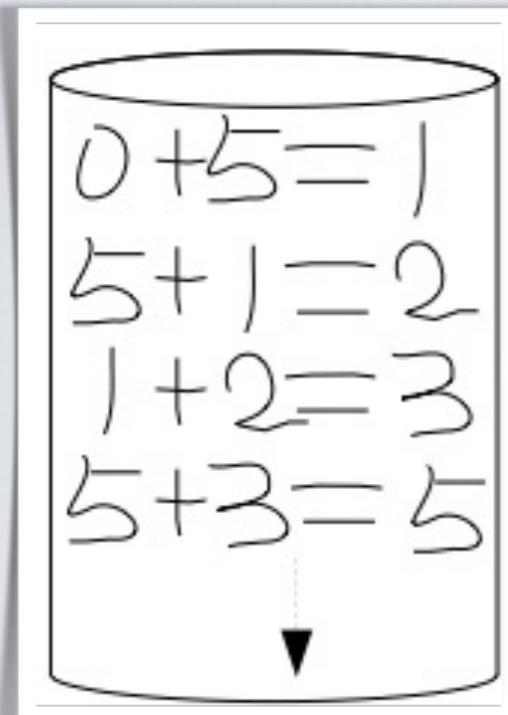
SVM : Support Vector Machine

ANN: Artificial Neural Network

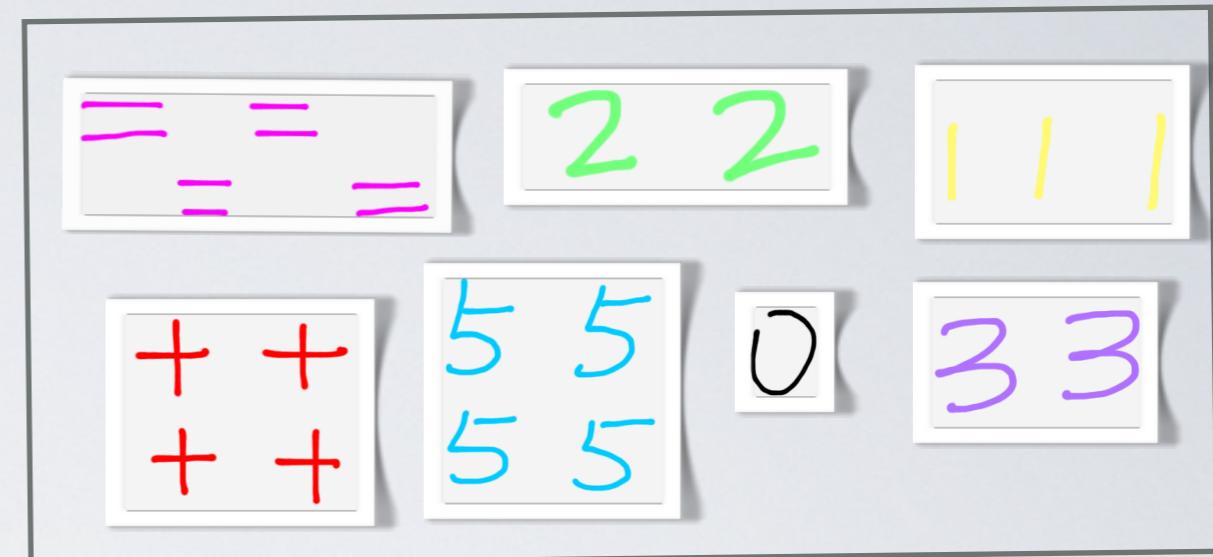
HMM: Hidden Markov Model, etc.

# SYMBOL KNOWLEDGE EXTRACTION

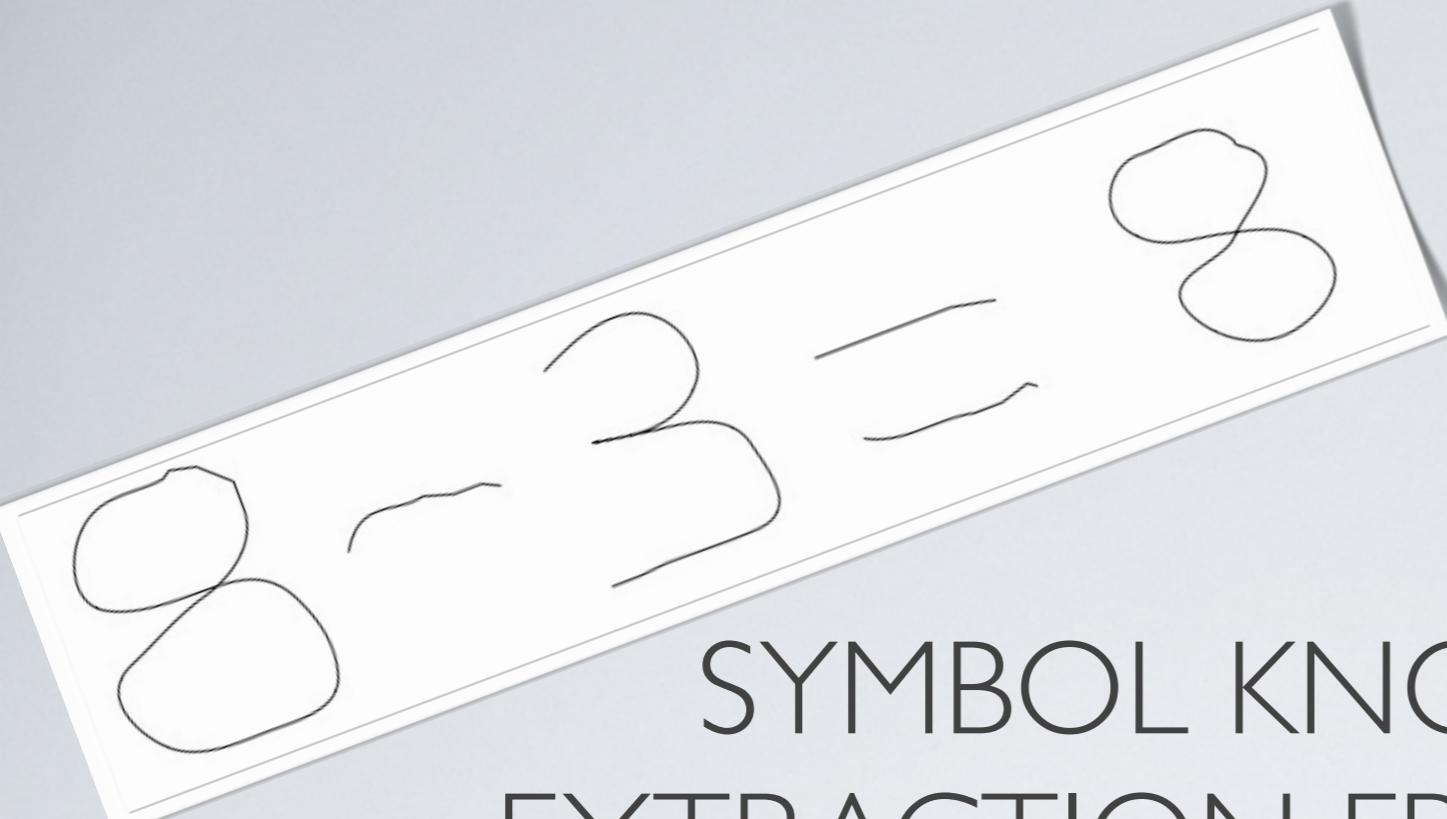
Unknown graphical language



→ Could we recover  
or discover  
these symbols?

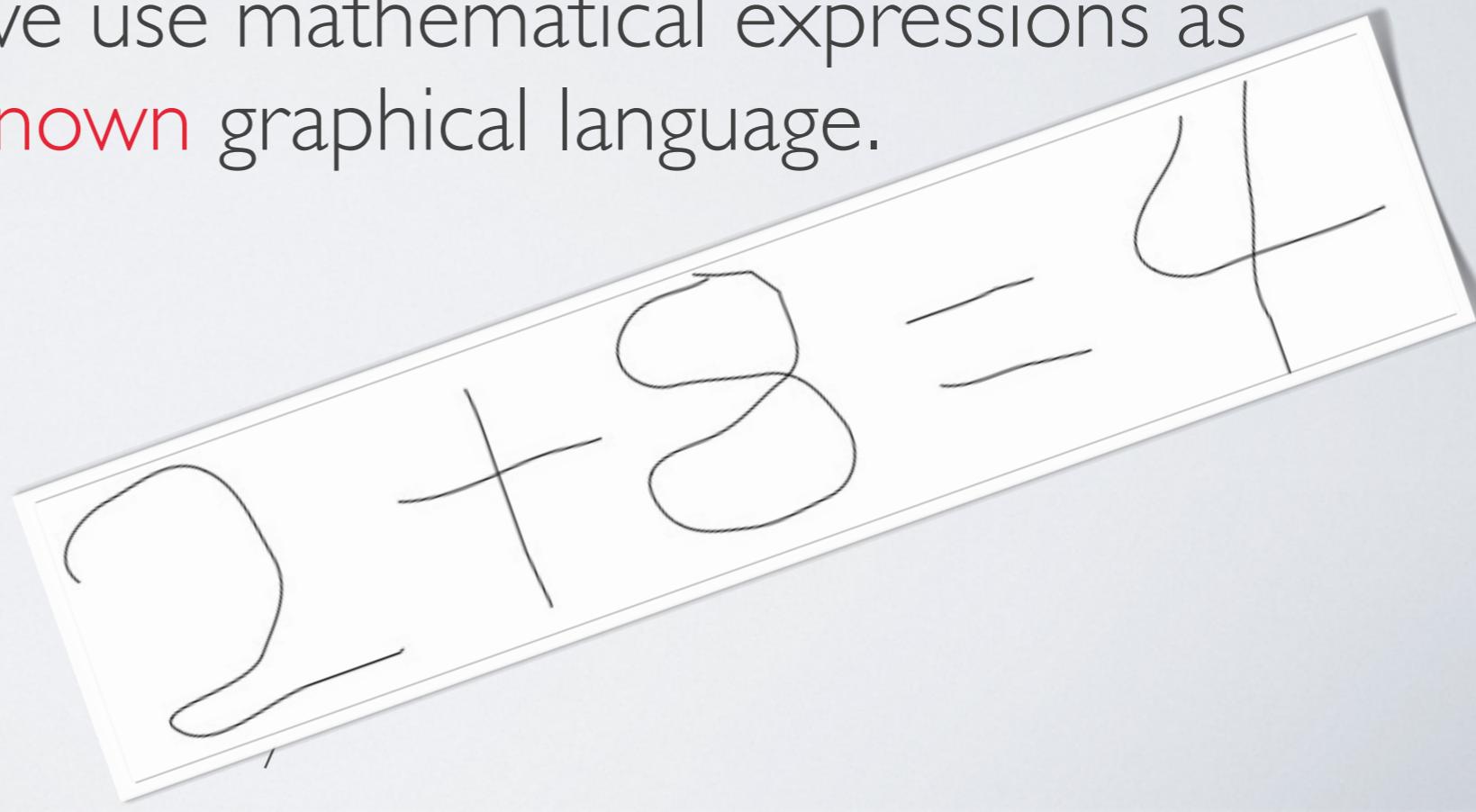


Annotation



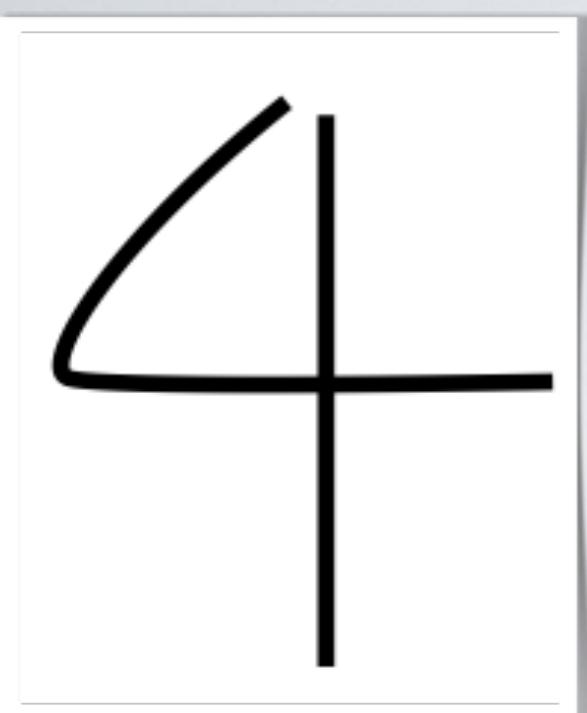
# SYMBOL KNOWLEDGE EXTRACTION FROM A SIMPLE GRAPHICAL LANGUAGE

As an example, we use mathematical expressions as an **unknown** graphical language.

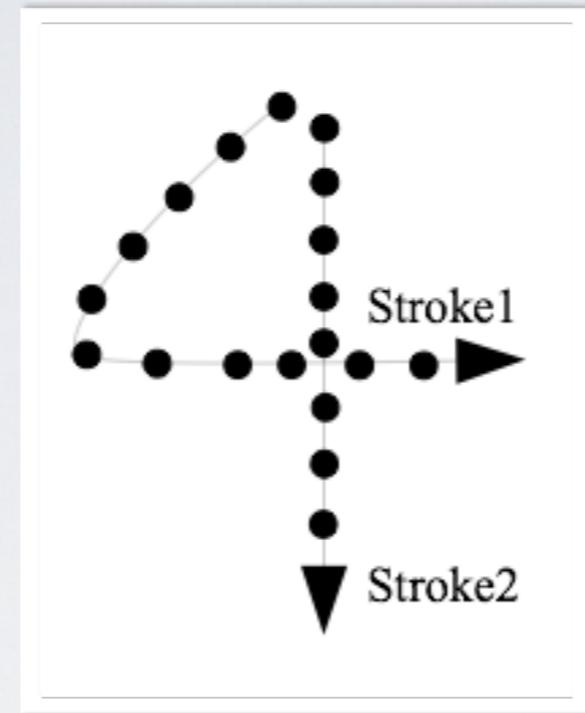


# GRAPHICAL LANGUAGE

Online handwritten strokes



Sampling

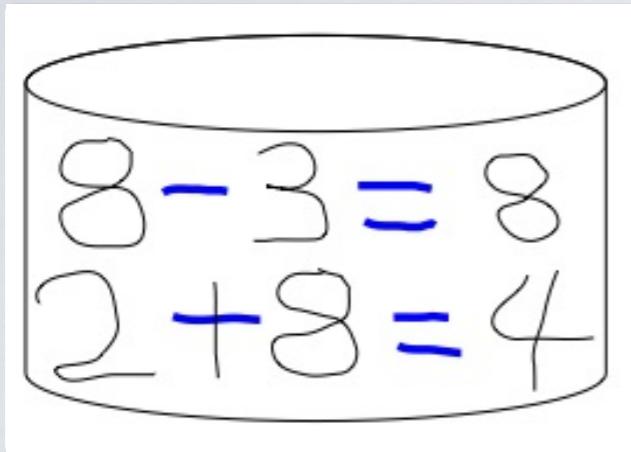


Collected data

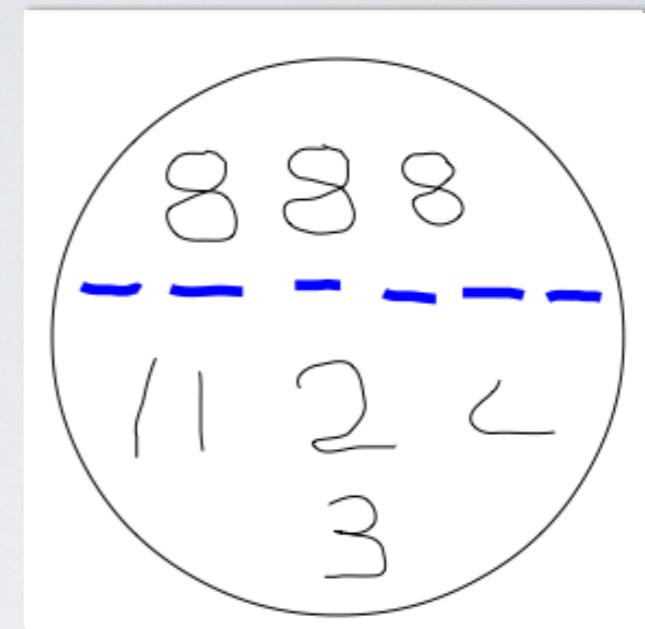
Stroke1:  $((x_1, y_1), (x_2, y_2), (x_3, y_3), \dots)$   
Stroke2:  $((x_1, y_1), (x_2, y_2), (x_3, y_3), \dots)$



# GRAPHICAL SYMBOL KNOWLEDGE EXTRACTION



The base elements  
are strokes.



This horizontal stroke  
repeats six times;  
it is "frequent".

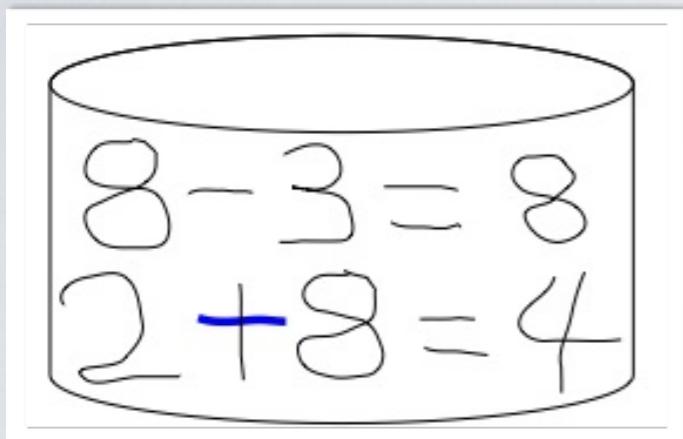
**Grapheme!**

Where is the  
horizontal stroke from?

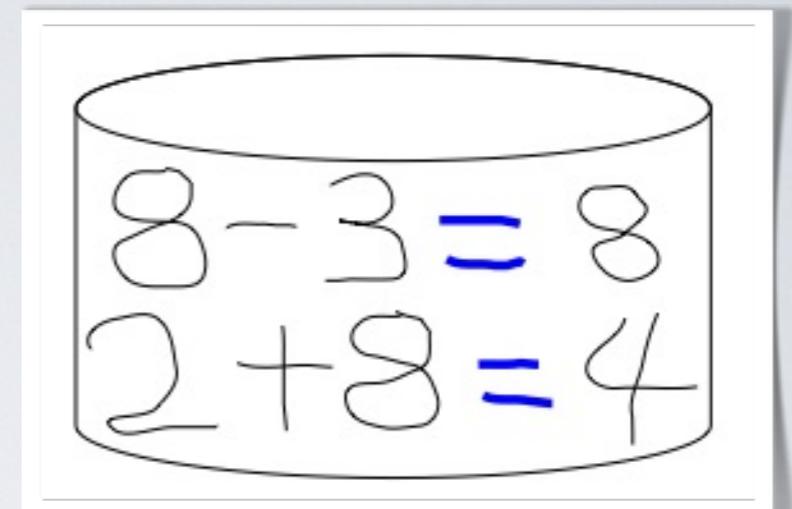
One stroke



# GRAPHICAL SYMBOL KNOWLEDGE EXTRACTION



From a part of symbol,  
"plus"

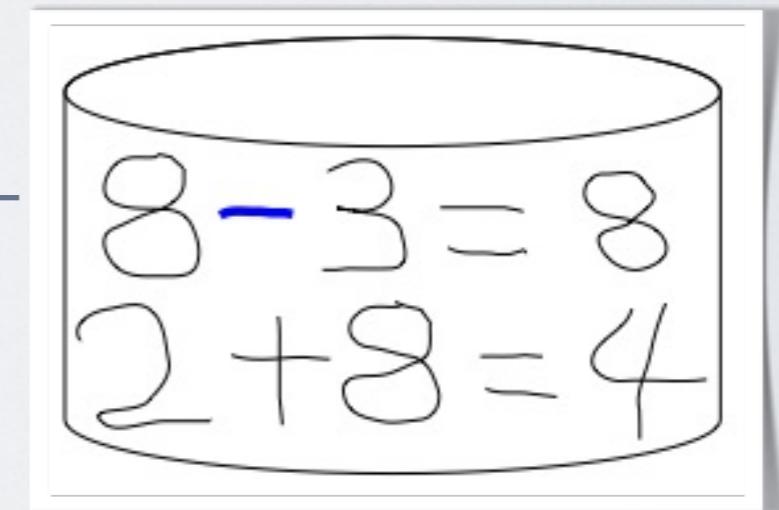


From two same symbols  
"equal"



**Grapheme!**

Where is the  
horizontal stroke from?

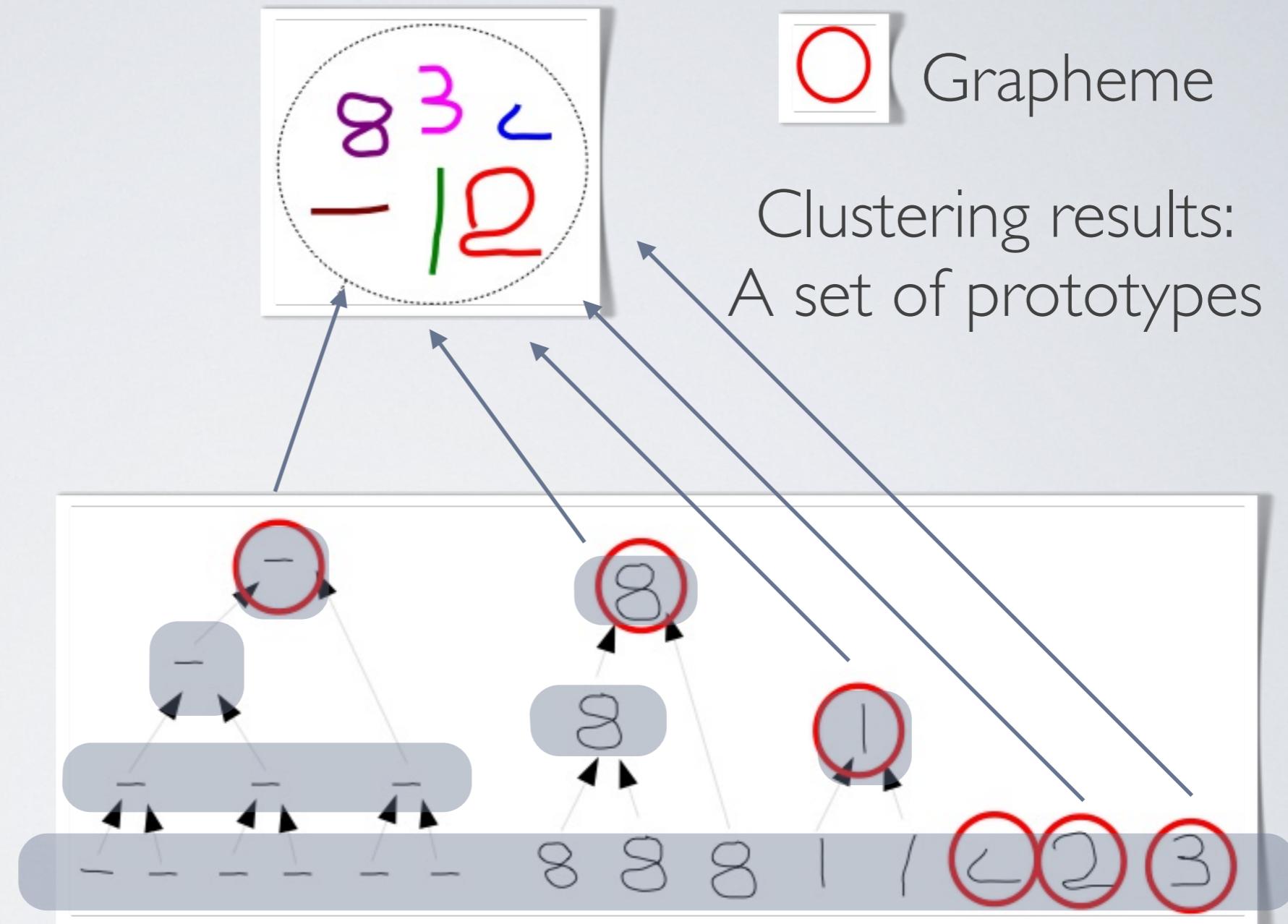
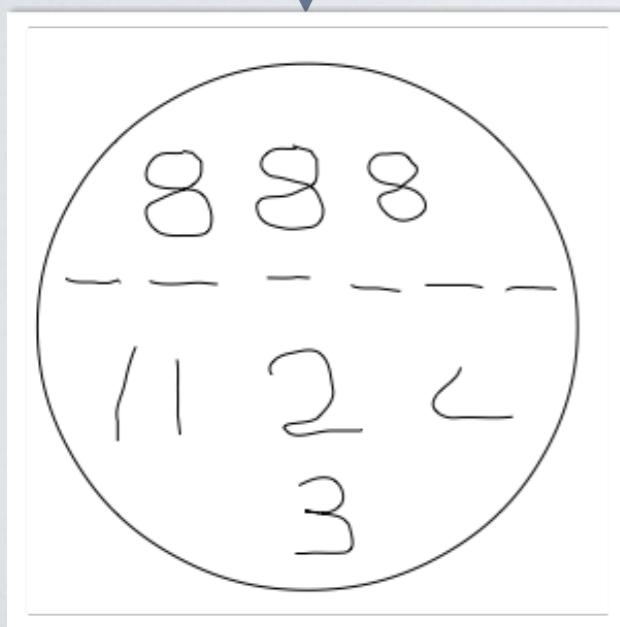
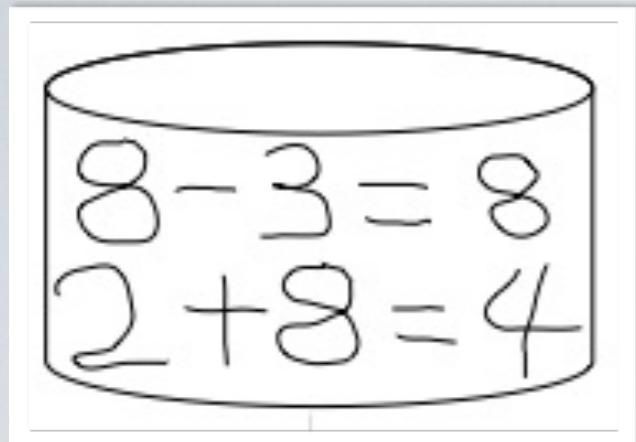


From a symbol,  
"minus"

# OUTLINES

- 1. Background
- 2. Symbol Knowledge Extraction
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# HIERARCHICAL CLUSTERING

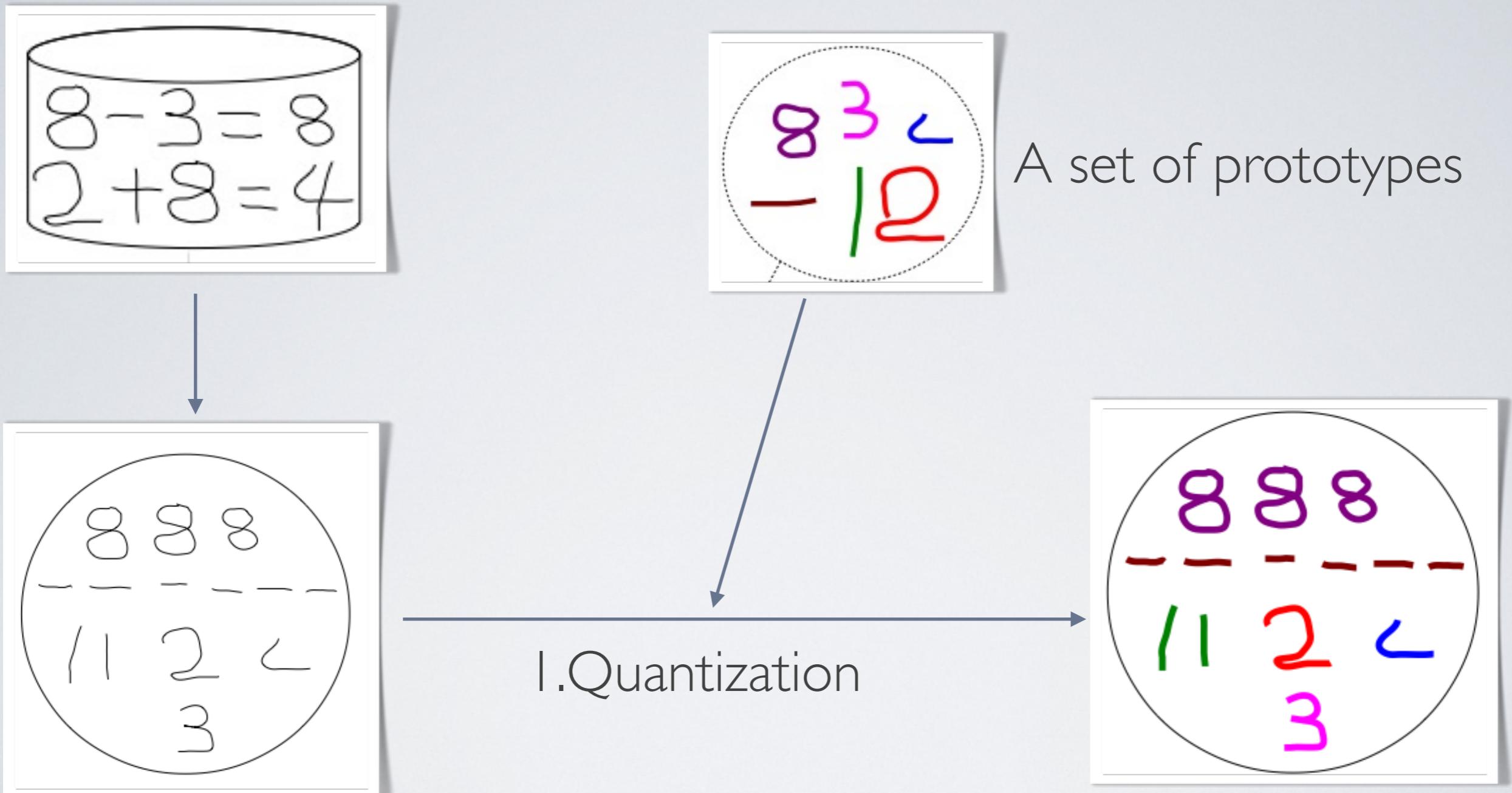


Grapheme

Clustering results:  
A set of prototypes

[1] Lance, G. N. & Williams, W.T., A General Theory of Classificatory Sorting Strategies: I. Hierarchical Systems, The Computer Journal, 1967, 9, 373-380

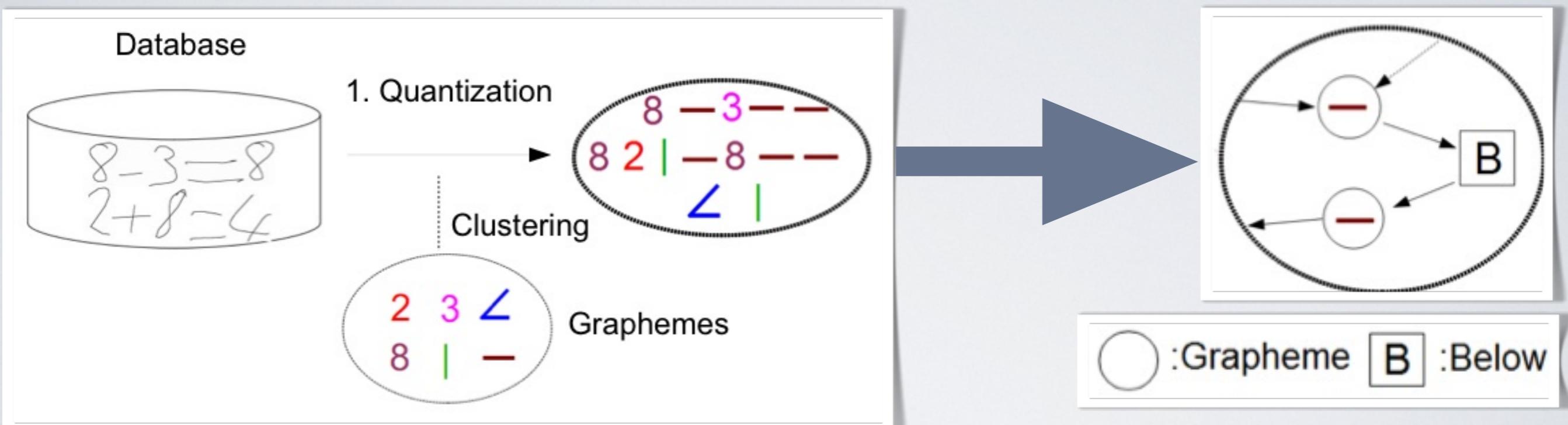
# QUANTIZATION



[1] Lance, G. N. & Williams, W.T., A General Theory of Classificatory Sorting Strategies: I. Hierarchical Systems, The Computer Journal, 1967, 9, 373-380

# GRAPHICAL SYMBOL DISCOVER

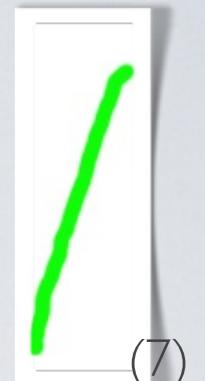
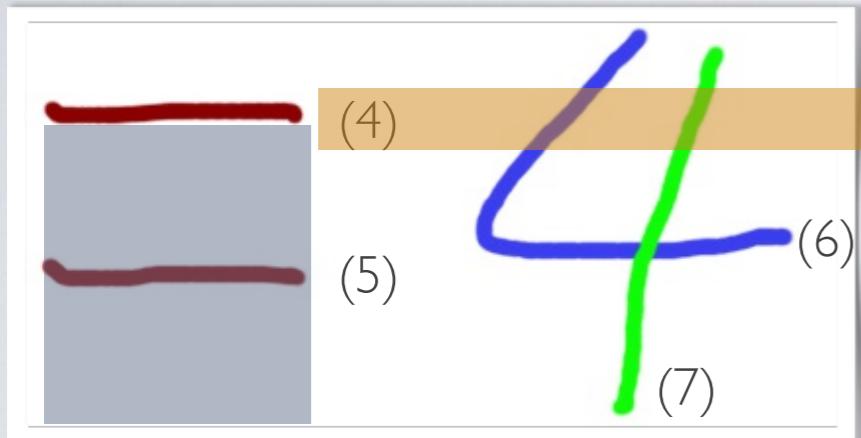
2. Construction of relational graph



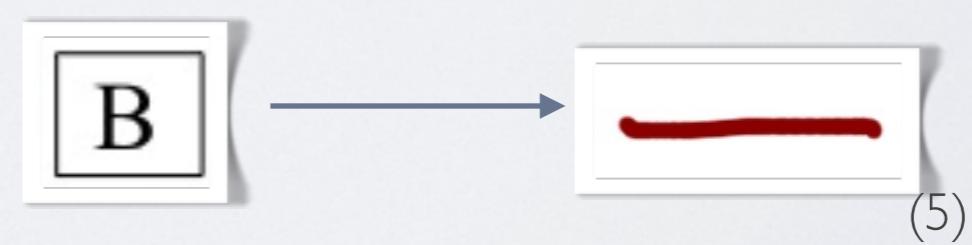
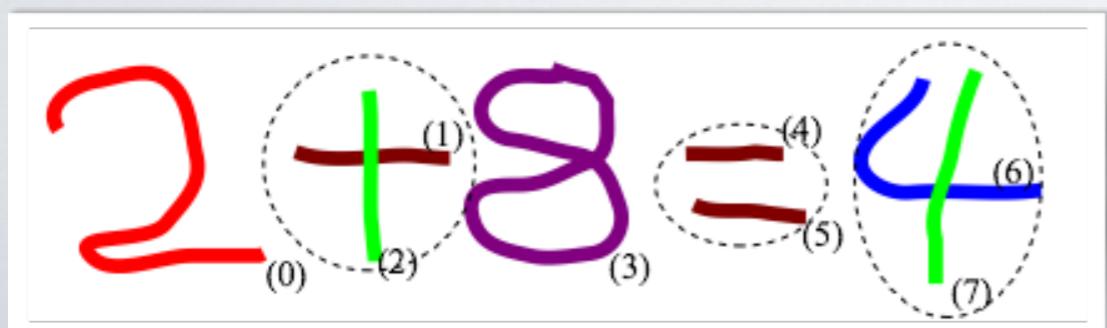
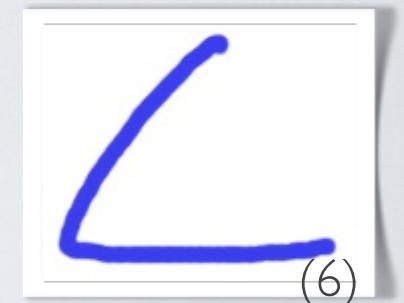
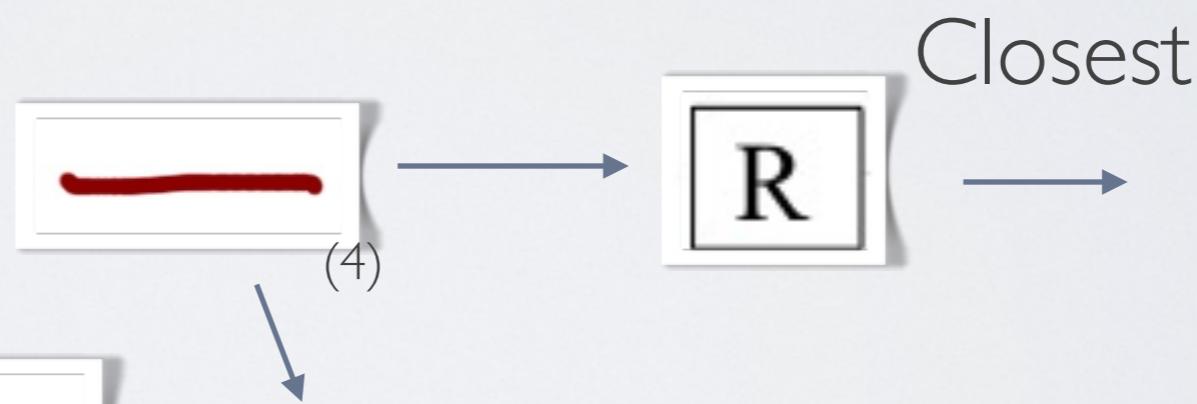
# SPATIAL RELATIONS

We predefine three spatial relations:

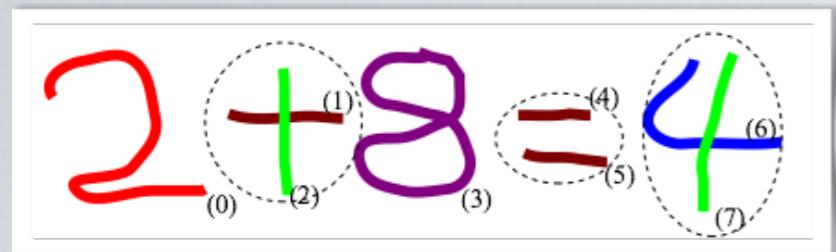
**Right**, **Below**, and **Intersection**



Reference stroke

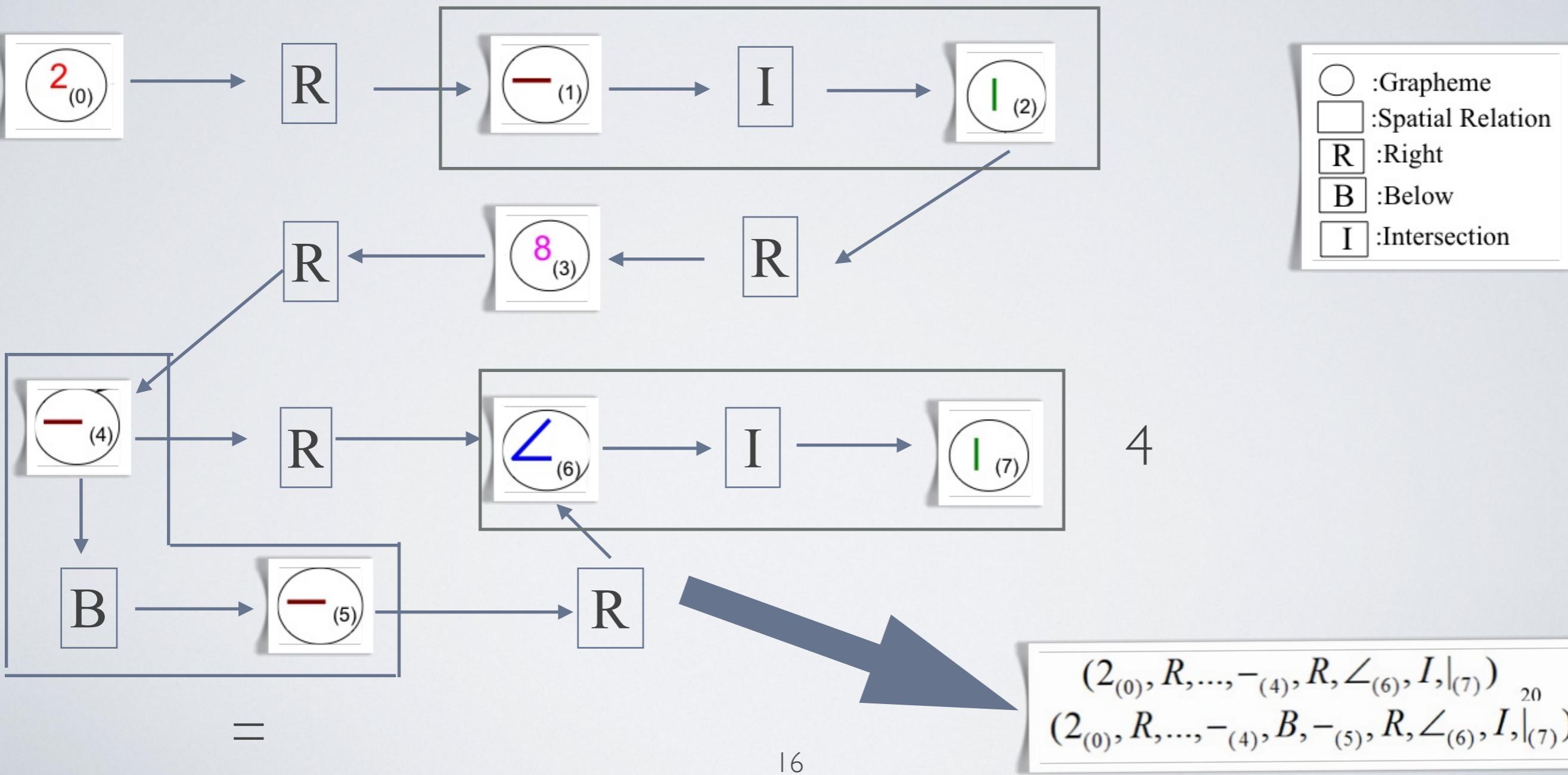


# RELATIONAL GRAPH



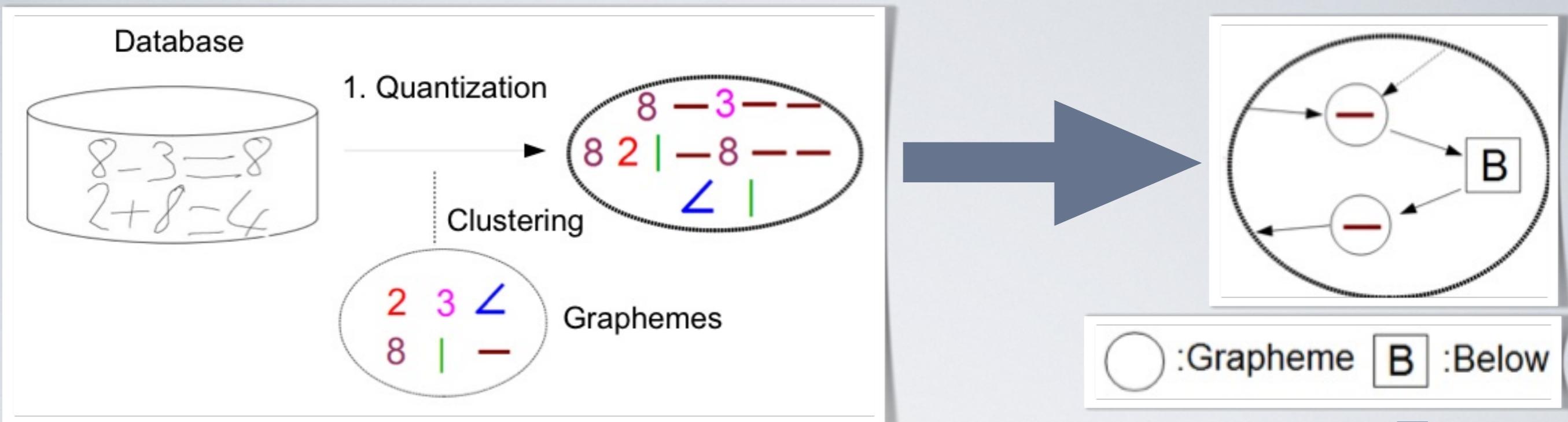
Directed acyclic graph

+

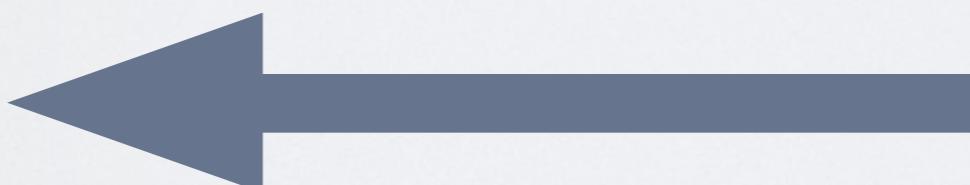
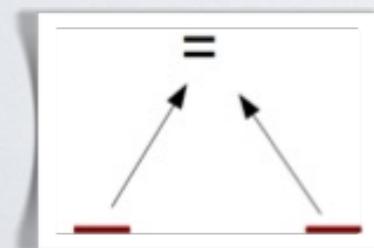


# LEXICON EXTRACTION

## 2. Construction of relational graph



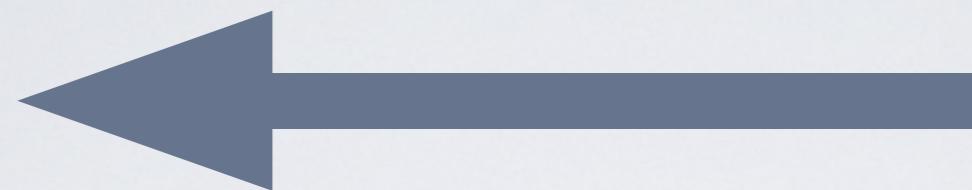
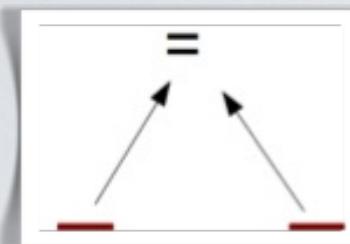
3. Lexicon extraction    Reduce the description length



$(2_{(0)}, R, \dots, -_{(4)}, R, \angle_{(6)}, I, |_{(7)})$   
 $(2_{(0)}, R, \dots, -_{(4)}, B, -_{(5)}, R, \angle_{(6)}, I, |_{(7)})$

# MINIMUM DESCRIPTION LENGTH PRINCIPLE

3. Lexicon extraction    Reduce the description length



$(2_{(0)}, R, \dots, -_{(4)}, R, \angle_{(6)}, I, |_{(7)})$   
 $(2_{(0)}, R, \dots, -_{(4)}, B, -_{(5)}, R, \angle_{(6)}, I, |_{(7)})$

As a naive example, we try to analyze a sequence, "1234-2/1234".

We define the description length (DL) as the **number of letters**.

$$DL("1234-2/1234") = 11$$

[2] Marcken, C. D., Linguistic Structure as Composition and Perturbation,  
In Meeting of the Association for Computational Linguistics, Morgan Kaufmann Publishers,  
1996, 335-341

# MINIMUM DESCRIPTION LENGTH PRINCIPLE

As a naive example, we try to analyze a sequence, "I234-2/I234".

We define the description length (DL) as the **number of letters**.

$$DL("I234-2/I234")=11$$

If we replace "I2" as **S**,  $DL("S34-2/S34")+DL("I2")=11.$

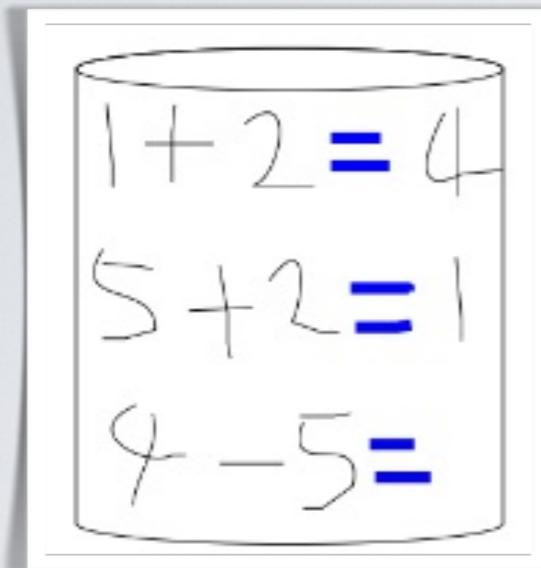
If we replace "I23" as **S**,  $DL("S4-2/S4")+DL("I23")=10$

If we replace "I234" as **S**,  $DL("S-2/S")+DL("I234")=9.$

Best lexical unit

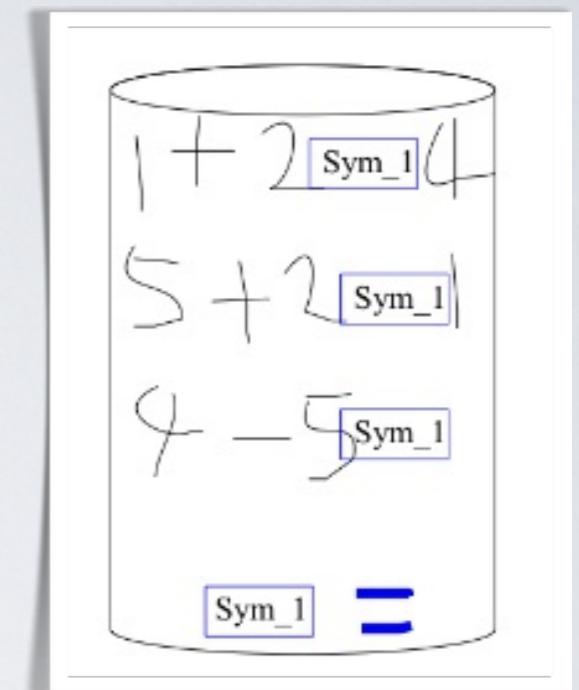
[2] Marcken, C. D., Linguistic Structure as Composition and Perturbation,  
In Meeting of the Association for Computational Linguistics, Morgan Kaufmann Publishers,  
1996, 335-341

# MINIMUM DESCRIPTION LENGTH PRINCIPLE

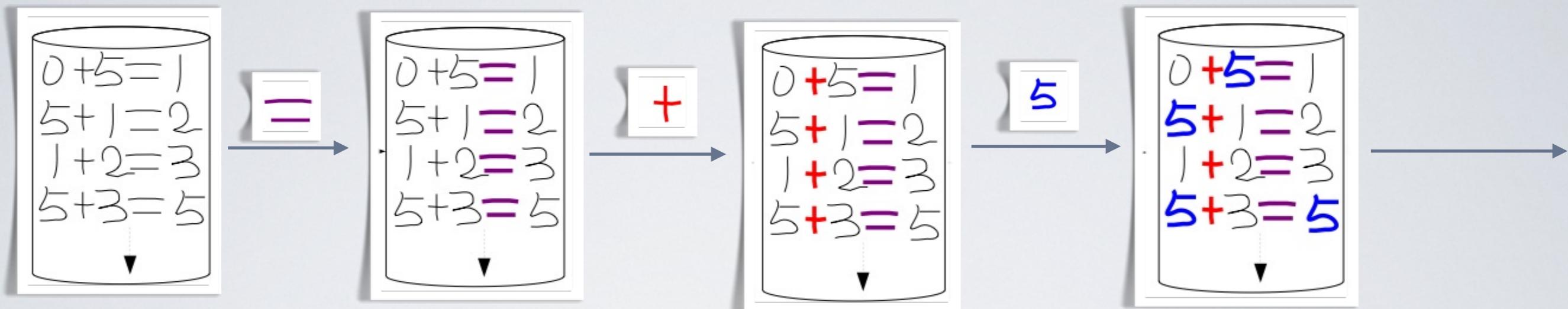


Replace frequent patterns  
in order to compress data

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# DISCOVER WORDS ITERATIVELY



Lexicon:

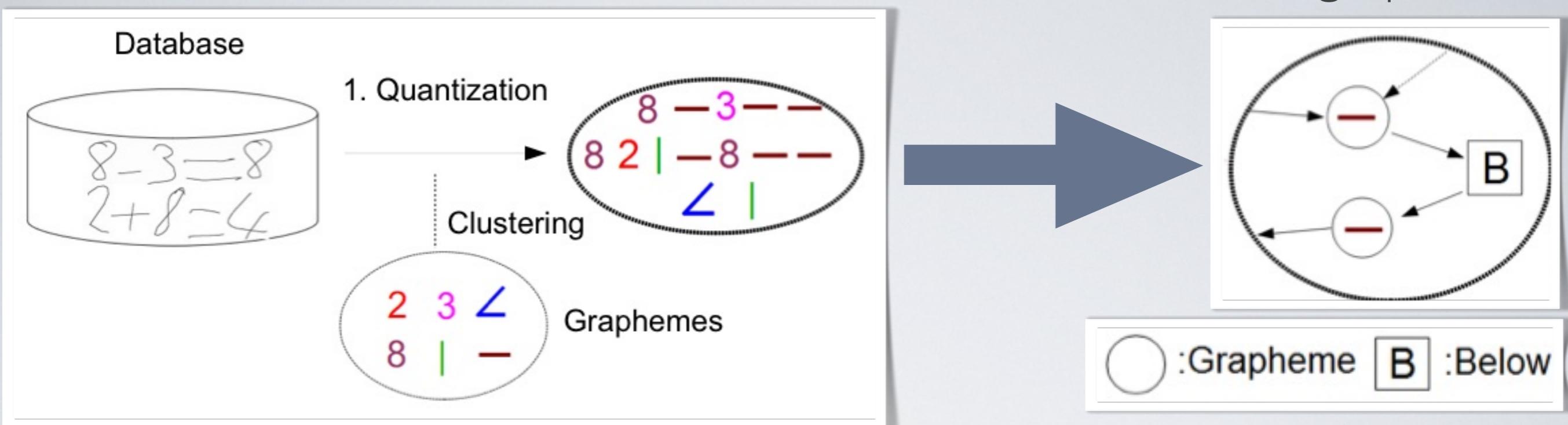
=

+

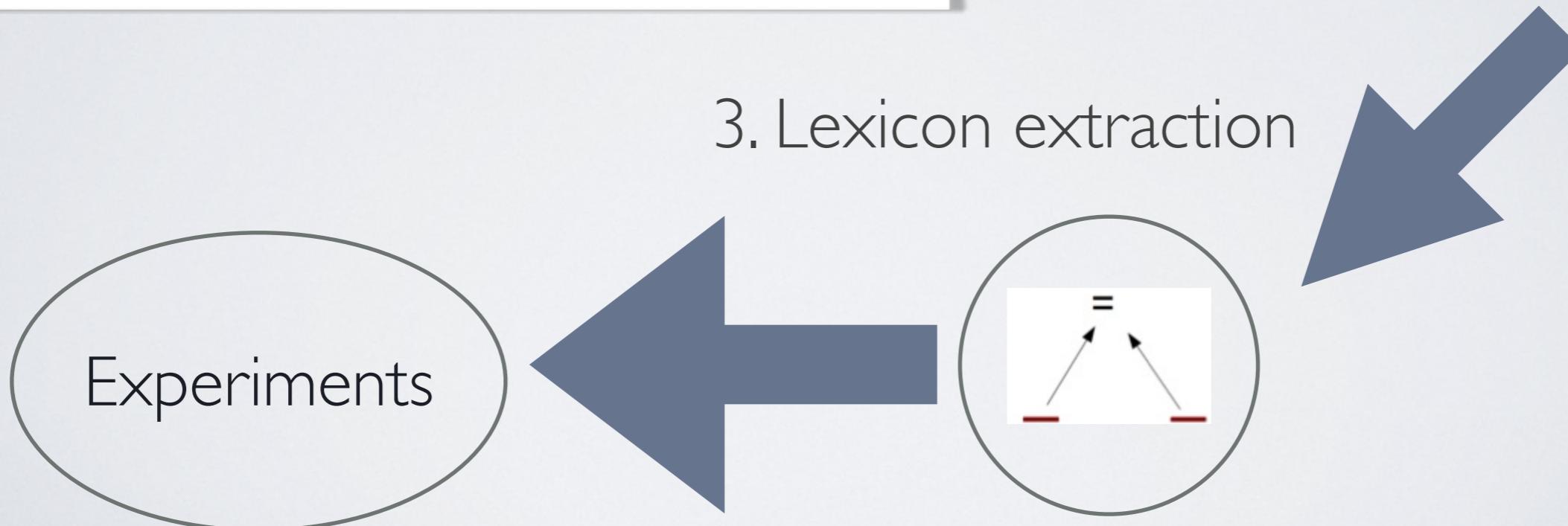
5

# LEXICON EXTRACTION

## 2. Construction of relational graph

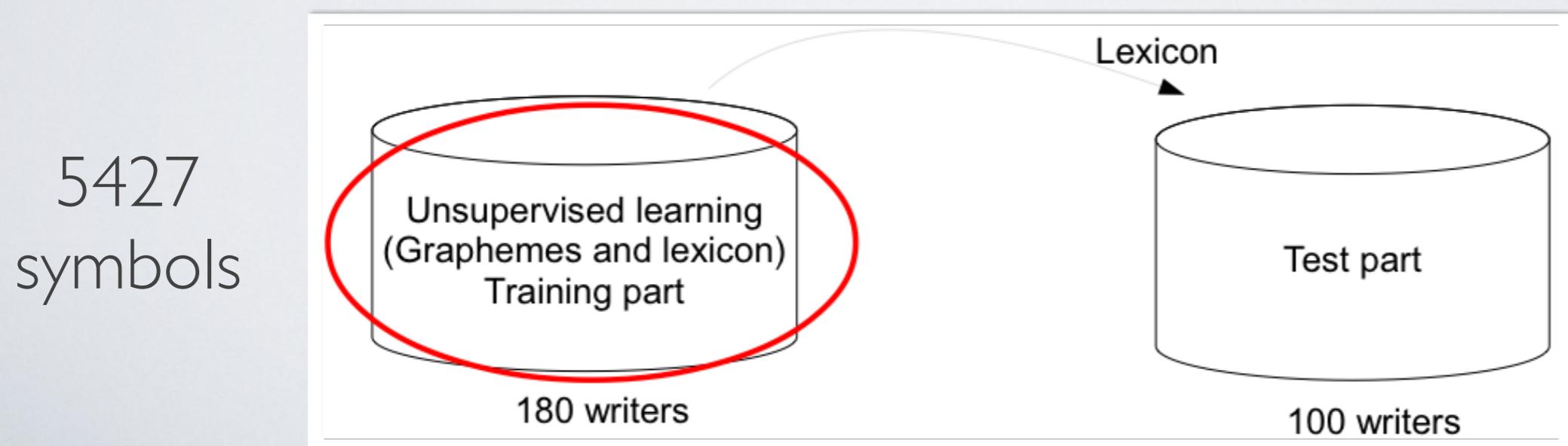
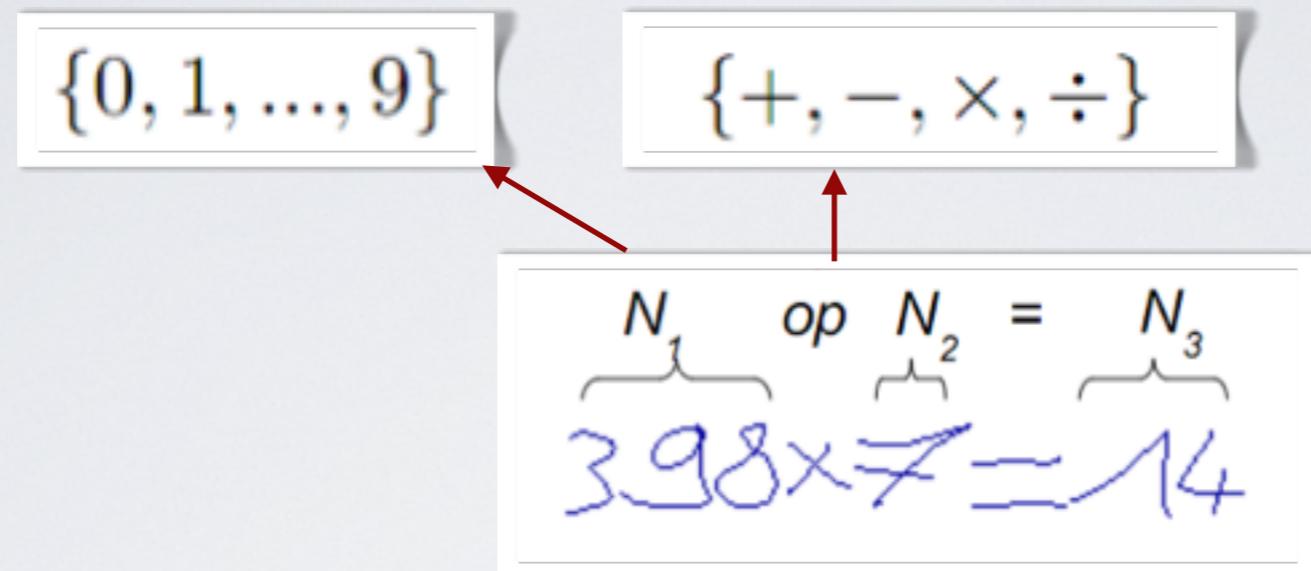


## 3. Lexicon extraction

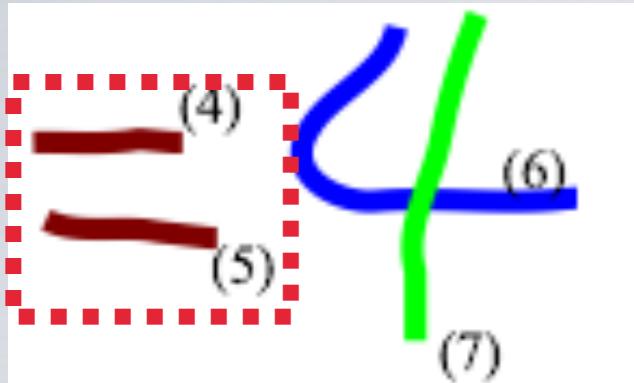


# SYNTHETIC DATABASE FROM REAL HANDWRITTEN ISOLATED CHARACTERS

$N_{i=\{1,2,3\}}$  is 70% of 1 digit, 20% of 2 digits and 10% of 3 digits randomly.



# RECALL RATE (EXPERIMENTS)



$$R_{\text{Recall}} = \frac{|S(e, G) \cap S(e, L)|}{|S(e, G)|} = 0.5$$

**S(e, G)**:ground-truth for the expression.

$$S(e, G) = \{\{-_{(4)}, -_{(5)}\}, \{\angle_{(6)}, |_{(7)}\}\}$$

**S(e, L)**:hierarchical segmentation using lexicon **L**.

$$S(e, L) = \{\{-_{(4)}\}, \{-_{(5)}\}, \{-_{(4)}, -_{(5)}\}, \{\angle_{(6)}\}, \{|_{(7)}\}\}$$

We got the recall rate of 74%(2245 symbols)  
on the test part of our database.  
24

# CONCLUSION

- Extraction of graphemes and quantization
- Construction of relational graph
- Lexicon extraction using minimum description length principle
- The recall rate of 74% (2245 symbols) is obtained.

# FUTURE WORK

- Reduce the description length on relational graphs instead of sequences [3].
- Unsupervised spatial relation learning for complex spatial relations.

[3]Jinpeng Li, Harold Mouchère and Christian Viard-Gaudin. Unsupervised Handwritten Graphical Symbol Learning Using Minimum Description Length Principle on Relational Graph, International Conference on Knowledge Discovery and Information Retrieval, KDIR 2011, Paris, France.

THANKYOU FOR  
YOUR ATTENTION

Questions?

Presentation can be downloaded from **Lijinpeng.org**