

Unit 7: Handling data with pandas

Richard Foltyn
University of Glasgow

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1 Handling data with pandas

1.1 Motivation

So far, we have encountered NumPy arrays as the only way to store numerical data (we mostly ignored the built-in containers provided directly in Python). However, while NumPy arrays are great for storing homogenous data without any particular structure, they are somewhat limited when we want to use them for high-level data analysis.

For example, we usually want to process data sets with

1. several variables;
2. multiple observations, which need not be identical across variables (some values may be missing);
3. non-homogenous data types: for examples, names need to be stored as strings, birthdays as dates and income as a floating-point number.

While NumPy can in principle handle such situations, it puts all the burden on the user. Most users would prefer to not have to deal with such low-level details.

Imagine we want to store names, birth dates and annual income for two people:

Name	Date of birth	Income
Alice	1985-01-01	30,000
Bob	1997-05-12	-

No income was reported for Bob, so it's missing. With NumPy, we could do this as follows:

```
[1]: import numpy as np
      from datetime import date

      date1 = date(1985, 1, 1)           # birth date for Alice
      date2 = date(1997, 5, 12)         # birth date for Bob
```

```
data = np.array(['Alice', date1, 30000.0],
                ['Bob', date2, None])

data
```

```
[1]: array(['Alice', datetime.date(1985, 1, 1), 30000.0],
          ['Bob', datetime.date(1997, 5, 12), None], dtype=object)
```

```
[2]: data.dtype           # print array data type
```

```
[2]: dtype('O')
```

While we can create such arrays, they are almost useless for data analysis, in particular since everything is stored as a generic object.

- To be fair, NumPy offers an alternative array type called “[record](#)” or “[structured](#)” array which can handle fields of different data types.

However, the pandas library offers much more beyond that, so there is little reason to use structured arrays.

Pandas was created to offer more versatile data structures that are straightforward to use for storing, manipulating and analysing heterogeneous data:

1. Data is clearly organised in *variables* and *observations*, similar to econometrics programs such as Stata.
2. Each variable is permitted to have a different data type.
3. We can use *labels* to select observations, instead of having to use a linear numerical index as with NumPy.

We could, for example, index a data set using National Insurance Numbers.

4. Pandas offers many convenient data aggregation and reduction routines that can be applied to subsets of data.

For example, we can easily group observations by city and compute average incomes.

5. Pandas also offers many convenient data import / export functions that go beyond what’s in NumPy.

Should we be using pandas at all times, then? No!

- For low-level tasks where performance is essential, use NumPy.
- For homogenous data without any particular data structure, use NumPy.
- On the other hand, if data is heterogeneous, needs to be imported from an external data source and cleaned or transformed before performing computations, use pandas.

There are numerous tutorials on pandas on the internet, so we will keep this unit short and illustrate only the main concepts. Useful references to additional material include:

- The official [user guide](#).
- The official [pandas cheat sheet](#) which nicely illustrates the most frequently used operations.
- The official [API reference](#) with details on every pandas object and function.
- There are numerous tutorials (including videos) available on the internet. See [here](#) for a list.

1.2 Creating pandas data structures

Pandas has two main data structures:

1. *Series* represents observations of a single variable.
2. *DataFrame* is a container for several variables. You can think of each individual column of a *DataFrame* as a *Series*, and each row represents one observation.

The easiest way to create a Series or DataFrame is to create them from pre-existing data.

To access pandas data structures and routines, we need to import them first. The near-universal convention is to make pandas available using the name `pd`:

```
[3]: import pandas as pd
```

Examples:

We can create a DataFrame from a NumPy array:

```
[4]: import numpy as np
import pandas as pd          # universal convention: import using pd
from numpy.random import default_rng

# Draw normally distributed data
rng = default_rng(123)
data = rng.normal(size=(10,3))

# Define variable (or column) names
varnames = ['A', 'B', 'C']

# Create pandas DataFrame
pd.DataFrame(data, columns=varnames)
```

```
[4]:
```

	A	B	C
0	-0.989121	-0.367787	1.287925
1	0.193974	0.920231	0.577104
2	-0.636464	0.541952	-0.316595
3	-0.322389	0.097167	-1.525930
4	1.192166	-0.671090	1.000269
5	0.136321	1.532033	-0.659969
6	-0.311795	0.337769	-2.207471
7	0.827921	1.541630	1.126807
8	0.754770	-0.145978	1.281902
9	1.074031	0.392621	0.005114

This code creates a DataFrame of three variables called A, B and C with 10 observations each.

Alternatively, we can create a DataFrame from non-homogenous data as follows:

```
[5]: # Names (strings)
names = ['Alice', 'Bob']

# Birth dates (datetime objects)
bdates = pd.to_datetime(['1985-01-01', '1997-05-12'])

# Incomes (floats)
incomes = np.array([35000, np.nan])          # code missing income as NaN

# create DataFrame from dictionary
pd.DataFrame({'Name': names, 'Birthdate': bdates, 'Income': incomes})
```

```
[5]:
```

	Name	Birthdate	Income
0	Alice	1985-01-01	35000.0
1	Bob	1997-05-12	NaN

If data types differ across columns, as in the above example, it is often convenient to create the DataFrame by passing a dictionary as an argument. Each key represents a column name and each corresponding value contains the data for that variable.

1.3 Viewing data

With large data sets, you hardly ever want to print the entire `DataFrame`. Pandas by default limits the amount of data shown. You can use the `head()` and `tail()` methods to explicitly display a specific number of rows from the top or the end of a `DataFrame`.

To illustrate, we use a data set of 23 UK universities that contains the following variables:

- Institution: Name of the institution
- Country: Country/nation within the UK (England, Scotland, ...)
- Founded: Year in which university (or a predecessor institution) was founded
- Students: Total number of students
- Staff: Number of academic staff
- Admin: Number of administrative staff
- Budget: Budget in million pounds
- Russell: Binary indicator whether university is a member of the [Russell Group](#), an association of the UK's top research universities.

The data was compiled based on information from Wikipedia.

We read in the data stored in the file `universities.csv` (from the `data/` folder) like this:

```
[6]: import pandas as pd

# relative path to CSV file
file = '../data/universities.csv'

# Load sample data set of UK universities. Individual fields are separated
# using ; so we need to pass sep=';' as an argument.
df = pd.read_csv(file, sep=';')
```

We can now display the first and last three rows:

```
[7]: df.head(3) # show first three rows
```

	Institution	Country	Founded	Students	Staff	Admin	\
0	University of Glasgow	Scotland	1451	30805	2942.0	4003.0	
1	University of Edinburgh	Scotland	1583	34275	4589.0	6107.0	
2	University of St Andrews	Scotland	1413	8984	1137.0	1576.0	

	Budget	Russell
0	626.5	1
1	1102.0	1
2	251.2	0

```
[8]: df.tail(3) # show last three rows
```

	Institution	Country	Founded	Students	Staff	\
20	University of Stirling	Scotland	1967	9548	NaN	
21	Queen's University Belfast	Northern Ireland	1810	18438	2414.0	
22	Swansea University	Wales	1920	20620	NaN	

	Admin	Budget	Russell
20	1872.0	113.3	0
21	1489.0	369.2	1
22	3290.0	NaN	0

To quickly compute some descriptive statistics for the *numerical* variables in the `DataFrame`, we use `describe()`:

```
[9]: df.describe()
```

```
[9]:
```

	Founded	Students	Staff	Admin	Budget	\
count	23.000000	23.000000	20.000000	19.000000	22.000000	
mean	1745.652174	24106.782609	3664.250000	3556.736842	768.609091	
std	256.992149	9093.000735	2025.638038	1550.434342	608.234948	
min	1096.000000	8984.000000	1086.000000	1489.000000	113.300000	
25%	1589.000000	18776.500000	2294.250000	2193.500000	340.850000	
50%	1826.000000	23247.000000	3307.500000	3485.000000	643.750000	
75%	1941.500000	30801.500000	4439.750000	4347.500000	1023.500000	
max	2004.000000	41180.000000	7913.000000	6199.000000	2450.000000	

	Russell
count	23.000000
mean	0.739130
std	0.448978
min	0.000000
25%	0.500000
50%	1.000000
75%	1.000000
max	1.000000

Note that this automatically ignores the columns `Institution` and `Country` as they contain strings, and computing the mean, etc. of a string variable does not make sense.

To see low-level information about the data type used in each column, we call `info()`:

```
[10]: df.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 23 entries, 0 to 22
Data columns (total 8 columns):
#   Column      Non-Null Count  Dtype
---  -
0   Institution  23 non-null     object
1   Country     23 non-null     object
2   Founded     23 non-null     int64
3   Students    23 non-null     int64
4   Staff       20 non-null     float64
5   Admin       19 non-null     float64
6   Budget      22 non-null     float64
7   Russell     23 non-null     int64
dtypes: float64(3), int64(3), object(2)
memory usage: 1.6+ KB
```

Pandas automatically discards missing information in computations. For example, the number of academic staff is missing for several universities, so the number of *non-null* entries reported in the table above is less than 23, the overall sample size.

1.4 Indexing

Pandas supports two types of indexing:

1. Indexing by position. This is basically identical to the indexing of other Python and NumPy containers.
2. Indexing by label, i.e., by the values assigned to the row or column index. These labels need not be integers in increasing order, as is the case for NumPy.

We will see how to assign labels below.

Pandas indexing is performed either by using brackets `[]`, or by using `.loc[]` for label indexing, or `.iloc[]` for positional indexing.

Indexing via `[]` can be somewhat confusing:

- specifying `df['name']` returns the column `name` as a `Series` object.

- On the other hand, specifying a range such as `df[5:10]` returns the *rows* associated with the positions 5,...,9.

Examples:

```
[11]: import pandas as pd

# Load sample data set of UK universities
df = pd.read_csv('../data/universities.csv', sep=';')
df['Institution'] # select a single column
```

```
[11]: 0      University of Glasgow
1      University of Edinburgh
2      University of St Andrews
3      University of Aberdeen
4      University of Strathclyde
5              LSE
6              UCL
7      University of Cambridge
8      University of Oxford
9      University of Warwick
10     Imperial College London
11     King's College London
12     University of Manchester
13     University of Bristol
14     University of Birmingham
15     Queen Mary University of London
16     University of York
17     University of Nottingham
18     University of Dundee
19     Cardiff University
20     University of Stirling
21     Queen's University Belfast
22     Swansea University
Name: Institution, dtype: object
```

```
[12]: df[['Institution', 'Students']] # select multiple columns using a list
```

```
[12]:
```

	Institution	Students
0	University of Glasgow	30805
1	University of Edinburgh	34275
2	University of St Andrews	8984
3	University of Aberdeen	14775
4	University of Strathclyde	22640
5	LSE	11850
6	UCL	41180
7	University of Cambridge	23247
8	University of Oxford	24515
9	University of Warwick	27278
10	Imperial College London	19115
11	King's College London	32895
12	University of Manchester	40250
13	University of Bristol	25955
14	University of Birmingham	35445
15	Queen Mary University of London	20560
16	University of York	19470
17	University of Nottingham	30798
18	University of Dundee	15915
19	Cardiff University	25898
20	University of Stirling	9548
21	Queen's University Belfast	18438
22	Swansea University	20620

To return the rows at positions 1, 2 and 3 we use

```
[13]: df[1:4]
```

```
[13]:
```

	Institution	Country	Founded	Students	Staff	Admin	\
1	University of Edinburgh	Scotland	1583	34275	4589.0	6107.0	
2	University of St Andrews	Scotland	1413	8984	1137.0	1576.0	
3	University of Aberdeen	Scotland	1495	14775	1086.0	1489.0	

	Budget	Russell
1	1102.0	1
2	251.2	0
3	219.5	0

Pandas follows the Python convention that indices are 0-based, and the endpoint of a slice is not included.

1.4.1 Manipulating indices

Pandas uses *labels* to index and align data. These can be integer values starting at 0 with increments of 1 for each additional element, which is the default, but they need not be. The two main methods to manipulate indices are:

- `set_index(keys=['column1', ...])`: uses the values of `column1` and optionally additional columns as indices, discarding the current index.
- `reset_index()`: resets the index to its default value, a sequence of increasing integers starting at 0.

Both methods return a new `DataFrame` and leave the original `DataFrame` unchanged. If we want to change the existing `DataFrame`, we need to pass the argument `inplace=True`.

For example, we can replace the row index and use the Roman lower-case characters a, b, c, ... as labels instead of integers:

```
[14]: import pandas as pd
df = pd.read_csv('../data/universities.csv', sep=';')

# Create list of lower-case letters which has same
# length as the number of observations.
index = [chr(97+i) for i in range(len(df))] # len(df) returns number of obs.
index
```

```
[14]: ['a',
      'b',
      'c',
      'd',
      'e',
      'f',
      'g',
      'h',
      'i',
      'j',
      'k',
      'l',
      'm',
      'n',
      'o',
      'p',
      'q',
      'r',
      's',
      't',
      'u',
      'v',
```

```
'w']
```

```
[15]: df['index'] = index                                # create new column 'index'
      df.set_index(keys=['index'], inplace=True)        # set letters as index!

      # print first 3 rows using labels
      df['a':'c']                                     # This is the same as df[:3]
```

```
[15]:
```

	Institution	Country	Founded	Students	Staff	Admin	\
index							
a	University of Glasgow	Scotland	1451	30805	2942.0	4003.0	
b	University of Edinburgh	Scotland	1583	34275	4589.0	6107.0	
c	University of St Andrews	Scotland	1413	8984	1137.0	1576.0	

	Budget	Russell
index		
a	626.5	1
b	1102.0	1
c	251.2	0

To add to the confusion, note that when specifying a range in terms of labels, the last element *is* included! Hence the row with index c in the above example is shown.

We can reset the index to its default integer values using the `reset_index()` method:

```
[16]: # Reset index labels to default value (integers 0, 1, 2, ...)
      df_new = df.reset_index(drop=True)
      df_new.head(3)                                # print first 3 rows of new DataFrame
```

```
[16]:
```

	Institution	Country	Founded	Students	Staff	Admin	\
0	University of Glasgow	Scotland	1451	30805	2942.0	4003.0	
1	University of Edinburgh	Scotland	1583	34275	4589.0	6107.0	
2	University of St Andrews	Scotland	1413	8984	1137.0	1576.0	

	Budget	Russell
0	626.5	1
1	1102.0	1
2	251.2	0

The `drop=True` argument tells pandas to throw away the old index values instead of storing them as a column of the resulting DataFrame.

1.4.2 Selecting elements

To more clearly distinguish between selection by label and by position, pandas provides the `.loc[]` and `.iloc[]` methods of indexing. To make your intention obvious, you should therefore adhere to the following rules:

1. Use `df['name']` only to select *columns* and nothing else.
2. Use `.loc[]` to select by label.
3. Use `.iloc[]` to select by position.

Selection by label

To illustrate, using `.loc[]` unambiguously indexes by label:

```
[17]: df.loc['d':'f', ['Institution', 'Students']]
```

```
[17]:
```

	Institution	Students
index		
d	University of Aberdeen	14775
e	University of Strathclyde	22640
f	LSE	11850

With `.loc[]` we can even perform slicing on column names, which is not possible with the simpler `df[]` syntax:

```
[18]: df.loc['d':'f', 'Institution':'Founded']
```

```
[18]:
```

	Institution	Country	Founded
index			
d	University of Aberdeen	Scotland	1495
e	University of Strathclyde	Scotland	1964
f	LSE	England	1895

This includes all the columns between `Institution` and `Founded`, where the latter is included since we are slicing by label.

Trying to pass in positional arguments will return an error for the given `DataFrame` since the index labels are `a, b, c,...` and not `0, 1, 2...`

```
[19]: df.loc[0:4]
```

```
TypeError: cannot do slice indexing on Index with these indexers [0] of type int
```

However, we can reset the index to its default value. Then the index labels are integers and coincide with their position, so that `.loc[]` works:

```
[20]: df.reset_index(inplace=True, drop=True) # reset index labels to integers,
df.loc[0:4] # drop original index
```

```
[20]:
```

	Institution	Country	Founded	Students	Staff	Admin	\
0	University of Glasgow	Scotland	1451	30805	2942.0	4003.0	
1	University of Edinburgh	Scotland	1583	34275	4589.0	6107.0	
2	University of St Andrews	Scotland	1413	8984	1137.0	1576.0	
3	University of Aberdeen	Scotland	1495	14775	1086.0	1489.0	
4	University of Strathclyde	Scotland	1964	22640	NaN	3200.0	

	Budget	Russell
0	626.5	1
1	1102.0	1
2	251.2	0
3	219.5	0
4	304.4	0

Again, the end point with label 4 is included because we are selecting by label.

Somewhat surprisingly, we can also pass boolean arrays to `.loc[]` even though these are clearly not labels:

```
[21]: df.loc[df['Country'] == 'Scotland']
```

```
[21]:
```

	Institution	Country	Founded	Students	Staff	Admin	\
0	University of Glasgow	Scotland	1451	30805	2942.0	4003.0	
1	University of Edinburgh	Scotland	1583	34275	4589.0	6107.0	
2	University of St Andrews	Scotland	1413	8984	1137.0	1576.0	
3	University of Aberdeen	Scotland	1495	14775	1086.0	1489.0	
4	University of Strathclyde	Scotland	1964	22640	NaN	3200.0	
18	University of Dundee	Scotland	1967	15915	1410.0	1805.0	
20	University of Stirling	Scotland	1967	9548	NaN	1872.0	

	Budget	Russell
0	626.5	1
1	1102.0	1

```

2    251.2    0
3    219.5    0
4    304.4    0
18   256.4    0
20   113.3    0

```

Indexing via `.loc[]` supports a few more types of arguments, see the [official documentation](#) for details.

Selection by position

Conversely, if we want to select items exclusively by their position and ignore their labels, we use `.iloc[]`:

```
[22]: df.iloc[0:4, 0:2]           # select first 4 rows, first 2 columns
```

```
[22]:
      Institution  Country
0  University of Glasgow  Scotland
1  University of Edinburgh  Scotland
2  University of St Andrews  Scotland
3  University of Aberdeen  Scotland

```

Again, `.iloc[]` supports a multitude of other arguments, including boolean arrays. See the [official documentation](#) for details.

1.5 Aggregation and reduction

1.5.1 Working with entire DataFrames

The simplest way to perform data reduction is to invoke the desired routine on the entire `DataFrame`:

```
[23]: import pandas as pd

df = pd.read_csv('../data/universities.csv', sep=';')
df.mean(numeric_only=True)
```

```
[23]:
Founded      1745.652174
Students    24106.782609
Staff        3664.250000
Admin        3556.736842
Budget        768.609091
Russell        0.739130
dtype: float64

```

Methods such as `mean()` are by default applied column-wise to each column. The `numeric_only=True` argument is used to discard all non-numeric columns (depending on the version of pandas, `mean()` will issue a warning otherwise).

One big advantage over NumPy is that missing values (represented by `np.nan`) are automatically ignored:

```
[24]: # mean() automatically drops 3 missing observations
df['Staff'].mean()
```

```
[24]: 3664.25
```

1.5.2 Splitting and grouping

Applying aggregation functions to the entire `DataFrame` is similar to what we can do with NumPy. The added flexibility of pandas becomes obvious once we want to apply these functions to subsets of data, i.e., groups, which we can define based on values or index labels.

For example, we can easily group our universities by country:

```
[25]: import pandas as pd

df = pd.read_csv('../data/universities.csv', sep=';')

groups = df.groupby(['Country'])
```

Here `groups` is a special pandas objects which can subsequently be used to process group-specific data. To compute the group-wise averages, we can simply run

```
[26]: groups.mean()
```

```
[26]:
```

	Founded	Students	Staff	Admin \
Country				
England	1745.923077	27119.846154	4336.692308	4112.000000
Northern Ireland	1810.000000	18438.000000	2414.000000	1489.000000
Scotland	1691.428571	19563.142857	2232.800000	2864.571429
Wales	1901.500000	23259.000000	3330.000000	4514.500000

	Budget	Russell
Country		
England	1001.700000	1.000000
Northern Ireland	369.200000	1.000000
Scotland	410.471429	0.285714
Wales	644.800000	0.500000

Groups support column indexing: if we want to only compute the total number of students for each country in our sample, we can do this as follows:

```
[27]: groups['Students'].sum()
```

```
[27]:
```

Country	
England	352558
Northern Ireland	18438
Scotland	136942
Wales	46518

Name: Students, dtype: int64

There are numerous routines to aggregate grouped data, for example:

- `mean()`, `sum()`: averages and sums over numerical items within groups.
- `std()`, `var()`: within-group std. dev. and variances
- `size()`: group sizes
- `first()`, `last()`: first and last elements in each group
- `min()`, `max()`: minimum and maximum elements within a group

Examples:

```
[28]: groups.size() # return number of elements in each group
```

```
[28]:
```

Country	
England	13
Northern Ireland	1
Scotland	7
Wales	2

dtype: int64

```
[29]: groups.first() # return first element in each group
```

```
[29]:
```

	Institution	Founded	Students	Staff \
Country				
England	LSE	1895	11850	1725.0
Northern Ireland	Queen's University Belfast	1810	18438	2414.0
Scotland	University of Glasgow	1451	30805	2942.0

Wales		Cardiff University	1883	25898	3330.0
	Admin	Budget	Russell		
Country					
England	2515.0	415.1	1		
Northern Ireland	1489.0	369.2	1		
Scotland	4003.0	626.5	1		
Wales	5739.0	644.8	1		

We can create custom aggregation routines by calling `agg()` or `aggregate()` on the grouped object. To illustrate, we count the number of universities in each country that have more than 20,000 students:

```
[30]: groups['Students'].agg(lambda x: np.sum(x >= 20000))
```

```
[30]: Country
England          10
Northern Ireland    0
Scotland           3
Wales              2
Name: Students, dtype: int64
```

Note that we called `agg()` only on the column `Students`, otherwise the function would be applied to every column separately, which is not what we want.

The most flexible aggregation method is `apply()` which calls a given function, passing the entire group-specific subset of data (including all columns) as an argument, and glues together the results.

For example, if we want to compute the average budget per student (in pounds), we can do this as follows:

```
[31]: # Budget is in millions of pounds, rescale by 1.0e6
groups.apply(lambda x: x['Budget'].sum() / x['Students'].sum() * 1.0e6)
```

```
[31]: Country
England          36936.050239
Northern Ireland  20023.863760
Scotland          20981.875539
Wales             13861.301002
dtype: float64
```

We couldn't have done this with `agg()`, since `agg()` never gets to see the entire chunk of data but only one column at a time.

This section provided only a first look at pandas's "split-apply-combine" functionality implemented via `groupby`. See the [official documentation](#) for more details.

1.6 Visualisation

We covered plotting with Matplotlib in earlier units. Pandas itself implements some convenience wrappers around Matplotlib plotting routines which allow us to quickly inspect data stored in `DataFrames`. Alternatively, we can extract the numerical data and pass it to Matplotlib's routines manually.

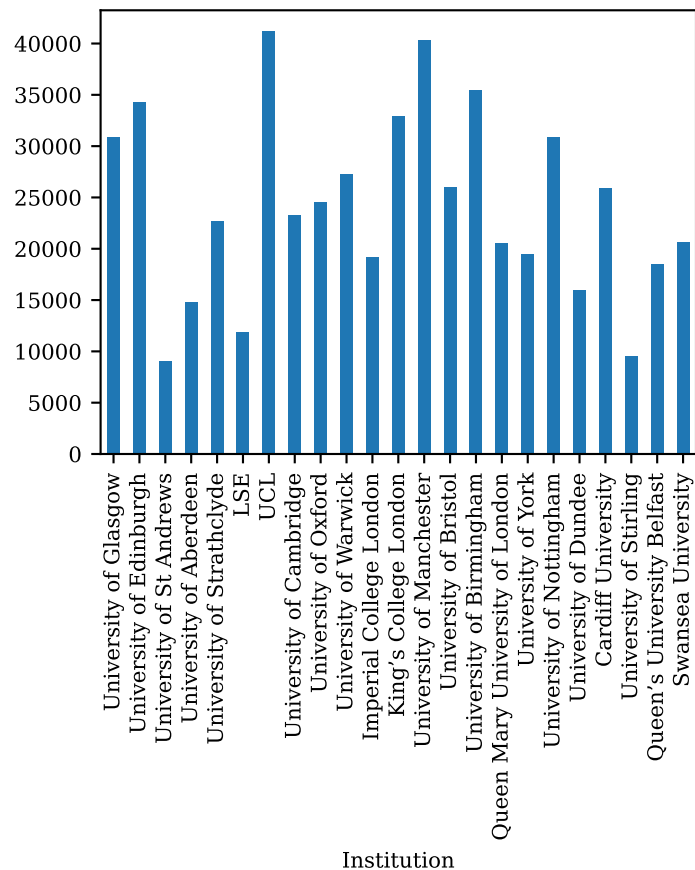
For example, to plot student numbers as a bar chart, we can directly use pandas:

```
[32]: import pandas as pd

df = pd.read_csv('../data/universities.csv', sep=';')

# set institution as label so they automatically show up in plot
df2 = df.set_index(keys=['Institution'])
df2['Students'].plot(kind='bar') # same as df2['Students'].plot.bar()
```

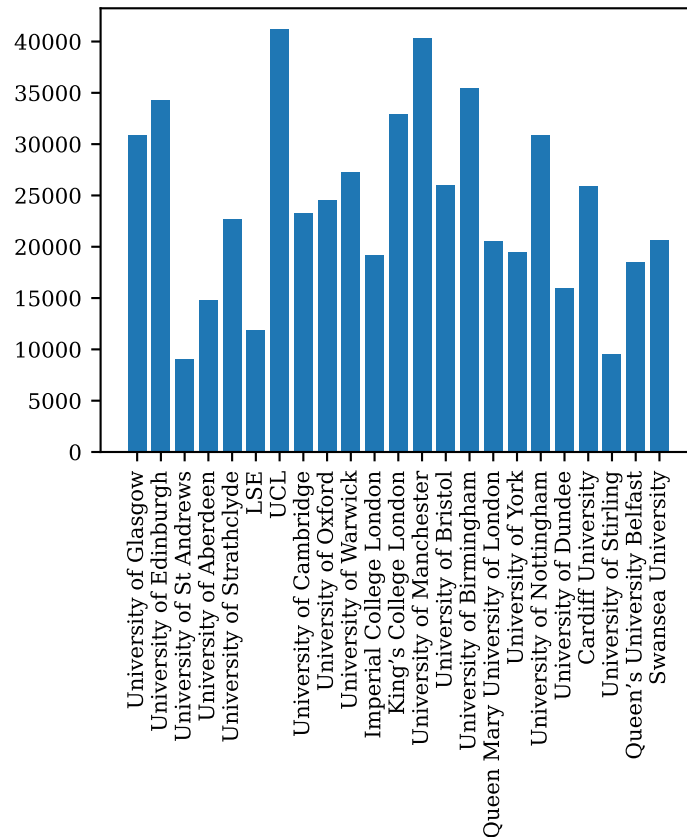
```
[32]: <AxesSubplot:xlabel='Institution'>
```



Alternatively, we can construct the graph using Matplotlib ourselves:

```
[33]: import matplotlib.pyplot as plt

labels = df['Institution'].to_list()          # labels as list
values = df['Students'].to_numpy()           # data as NumPy array
plt.bar(labels, values)
plt.tick_params(axis='x', labelrotation=90)
```



Sometimes Matplotlib's routines directly work with pandas's data structures, sometimes they don't. In cases where they don't, we can convert a `DataFrame` or `Series` object to a NumPy array using the `to_numpy()` method, and convert a `Series` to a Python list using `to_list()`, as illustrated in the example above.

To plot timeseries-like data, we can use the `plot()` method, which optionally accepts arguments to specify which columns should be used for the *x*-axis and which for the *y*-axis:

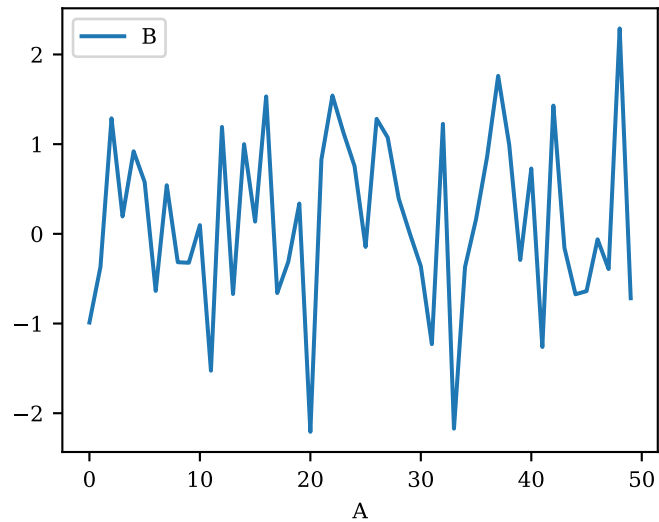
```
[34]: import numpy as np
import pandas as pd

# Instantiate RNG
rng = np.random.default_rng(123)

# Create pandas DataFrame
nobs = 50
df = pd.DataFrame({'A': np.arange(nobs), 'B': rng.normal(size=nobs)})

df.plot(x='A', y='B')           # plot A on x-axis, B on y-axis
```

```
[34]: <AxesSubplot:xlabel='A'>
```



To quickly generate some descriptive statistics, we can use the built-in box plot:

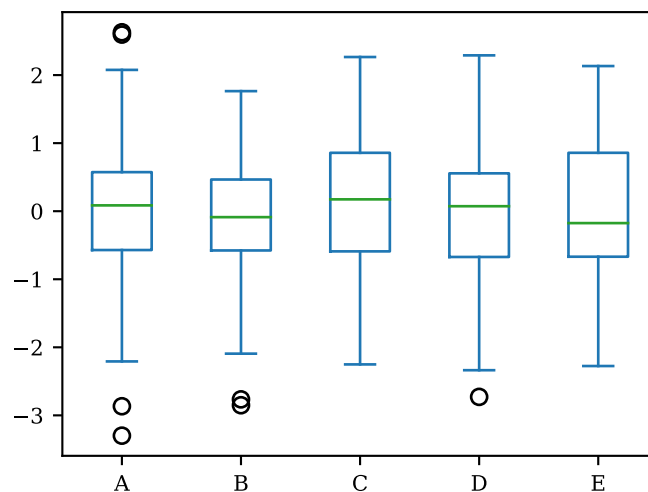
```
[35]: import numpy as np
import pandas as pd

# Instantiate RNG
rng = np.random.default_rng(123)

# Create pandas DataFrame
df = pd.DataFrame(rng.normal(size=(100, 5)),
                  columns=['A', 'B', 'C', 'D', 'E'])

df.plot.box()           # same as df.plot(kind='box')
```

[35]: <AxesSubplot:>

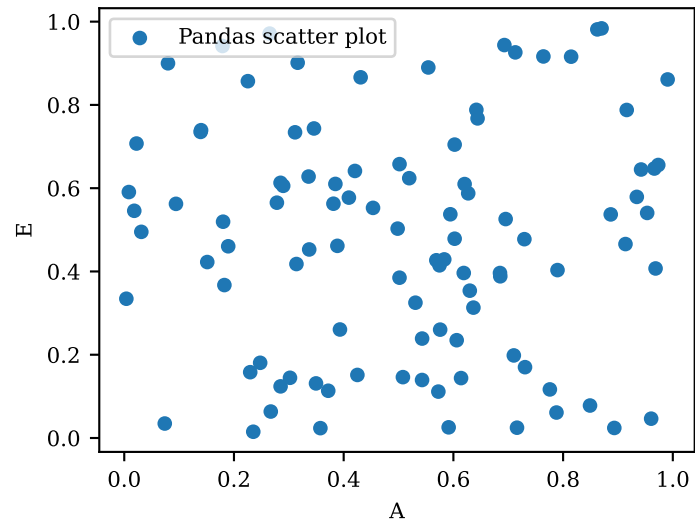


Similarly, we can generate scatter plots, plotting one column against another:

```
[36]: # Create pandas DataFrame
df = pd.DataFrame(rng.uniform(size=(100, 5)),
                  columns=['A', 'B', 'C', 'D', 'E'])

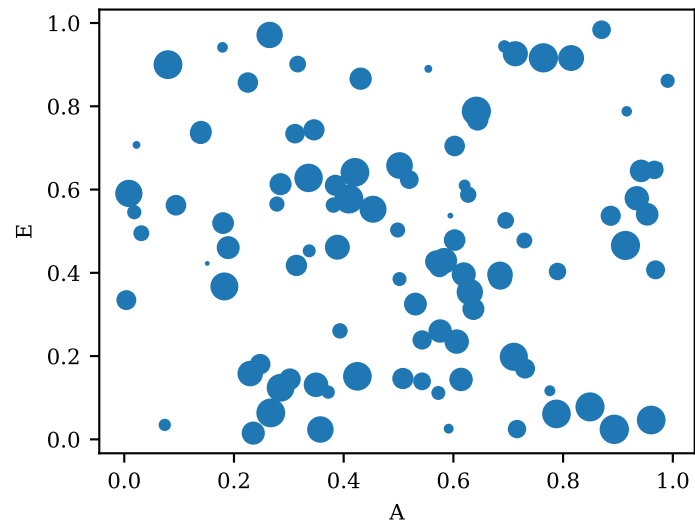
df.plot.scatter(x='A', y='E', label='Pandas scatter plot')
```

```
[36]: <AxesSubplot:xlabel='A', ylabel='E'>
```



```
[37]: # We can even use a column to specify the dot size!
df.plot.scatter(x='A', y='E', s=df['B']*100.0)
```

```
[37]: <AxesSubplot:xlabel='A', ylabel='E'>
```



In general, the wrappers implemented in pandas are useful to get an idea how the data looks like. For reusable code or more complex graphs, we'll usually want to directly use Matplotlib and pass the data converted to NumPy arrays.

1.7 Exercises

The following exercises use data files from the `data/` folder.

1.7.1 Exercise 1: Basic data manipulations

In this exercise, we will perform some basic data manipulation and plot the results.

1. Load the CSV file `FRED_QTR.csv` (using `sep=', '`). Set the columns `Year` and `Quarter` as (joint) indices.

Hint: You can do this by specifying these column names in the `index_col` argument of `read_csv()`. Alternatively, you can call `set_index()` once you have loaded the data.

2. This data comes at a quarterly frequency. Convert it to annual values by computing the average values for each year.

Hint: Group the data by `Year` using the `groupby()` function and compute the mean on the grouped data.

3. Compute two new variables from the annualised data and add them to the `DataFrame`:

- `Inflation`, defined as the growth rate of `CPI` (consumer price index)
- `GDP_growth`, defined as the growth rate of `GDP`

4. Drop all rows with missing values (these show up as `NaN`).

Hint: There is no need to manually filter out `NaN` values, you can use the `dropna()` method instead.

5. Plot the columns `GDP_growth`, `Inflation`, `UNRATE` (unemployment rate) and `LFPART` (labour force participation) using the pandas plotting routines. Use the option `subplots=True` and `layout=(2, 2)` to create a 2×2 grid. See the documentation for `plot()` for details.

1.7.2 Exercise 2: Decade averages

Load the FRED data from the CSV file `FRED_QTR.csv` (using `sep=', '`) and perform the following tasks:

1. Compute the quarterly GDP growth rate and inflation, similar to what you did in the previous exercise.
2. Add the column `Decade` which contains the decade for every observation. Use 1940 to code the 40s, 1950 for the 50s, etc.
3. We want to retain only observations for decades for which all 40 quarters are present:
 1. Group the data by `Decade` and count the number of observations using `count()`.
 2. A decade should be kept in the data set only if *all* variables have the full 40 observations.
 3. Drop all observations for which this is not the case.
4. With the remaining observations, compute the decade averages for quarterly GDP growth, inflation and the unemployment rate (`UNRATE`). Annualise the GDP growth and inflation figures by multiplying them by 4.
5. Create a bar chart that plots these three variables by decade.

1.7.3 Exercise 3: Group averages

Load the universities data from the CSV file `universities.csv` (using `sep=';'`) and perform the following tasks:

1. Group the data by Russell Group membership using the indicator variable `Russell`. For each group, compute the averages of the following ratios using `apply()`:
 - The ratio of academic staff (`Staff`) to students (`Students`)
 - The ratio of administrative staff (`Admin`) to students.
 - The budget (`Budget`) per student in pounds.

Additionally, compute the number of universities in each group.

2. Repeat the task using a different approach:
 1. Compute the above ratios and add them as new columns to the initial `DataFrame`.
 2. Group the data by Russell Group membership.
 3. Compute the mean of each ratio using `mean()`.
 4. Compute the number of universities in each group using `count()`, and store the result in the column `Count` in the `DataFrame` you obtained in the previous step.
3. Create a bar chart, plotting the value for universities in and outside of the Russell Group for each of the four statistics computed above.

1.7.4 Exercise 4: Grouping by multiple dimensions

Load the universities data from the CSV file `universities.csv` (using `sep=' ; '`) and perform the following tasks:

1. Create an indicator `Pre1800` which is `True` for universities founded before the year 1800.
2. Group the data by `Country` and the value of `Pre1800`.
Hint: You need to pass a list of column names to `groupby()`.
3. Compute the number of universities for each combination of `(Country, Pre1800)`.
4. Create a bar chart showing the number of pre- and post-1800 universities by country (i.e., create four groups of bars, each group showing one bar for pre- and one for post-1800).
5. Create a bar chart showing the number of universities by country by pre- and post-1800 period (i.e., create two groups of bars, each group showing four bars, one for each country.)

1.7.5 Exercise 5: Okun's law (advanced)

In this exercise, we will estimate [Okun's law](#) on quarterly data for each of the last eight decades.

Okun's law relates unemployment to the output gap. One version (see Jones: Macroeconomics, 2019) is stated as follows:

$$u_t - \bar{u}_t = \alpha + \beta \left(\frac{Y_t - \bar{Y}_t}{\bar{Y}_t} \right)$$

where u_t is the unemployment rate, \bar{u}_t is the natural rate of unemployment, Y_t is output (GDP) and \bar{Y}_t is potential output. We will refer to $u_t - \bar{u}_t$ as “cyclical unemployment” and to the term in parenthesis on the right-hand side as the “output gap.” Okun's law says that the coefficient β is negative, i.e., cyclical unemployment is higher when the output gap is low (negative) because the economy is in a recession.

Load the FRED data from the CSV file `FRED_QTR.csv` (using `sep=' , '`) and perform the following tasks:

1. Compute the output gap and cyclical unemployment rate as defined above and add them as columns to the `DataFrame`.
2. Assign each observation to a decade as you did in previous exercises.
3. Write a function `regress_okun()` which accepts a `DataFrame` containing a decade-specific subsample as the only argument, and estimates the coefficients α (the intercept) and β (the slope) of the above regression equation.

This function should return a `DataFrame` of a single row and two columns which store the intercept and slope.

Hint: Use NumPy's `lstsq()` to perform the regression. To regress the dependent variable y on regressors X , you need to call `lstsq(X, y)`. To include the intercept, you will manually have to create X such that the first column contains only ones.

4. Group the data by decade and call the `apply()` method, passing `regress_okun` you wrote as the argument.
5. Plot your results: for each decade, create a scatter plot of the raw data and overlay it with the regression line you estimated.

1.8 Solutions

These solutions illustrate *one* possible way to solve the exercises. Pandas is extremely flexible (maybe too flexible) and allows us to perform these tasks in many different ways, so your implementation might look very different.

The solutions are also provided as Python scripts in the [lectures/solutions/unit07/](#) folder.

1.8.1 Solution for exercise 1

One possible implementation looks as follows:

```
[38]: import pandas as pd

filepath = '../data/FRED_QTR.csv'

df = pd.read_csv(filepath, sep=',', index_col=['Year', 'Quarter'])
# Alternatively, set index columns later
# df = pd.read_csv(filepath, sep=',')
# df.set_index(keys=['Year', 'Quarter'], inplace=True)

# Convert to annual frequency
# Group by year
grp = df.groupby(['Year'])
# Compute annual data as mean of quarterly values
df_year = grp.mean()

# Alternative ways to perform the same aggregation:
# df_year = grp.agg('mean')
# df_year = grp.agg(np.mean)

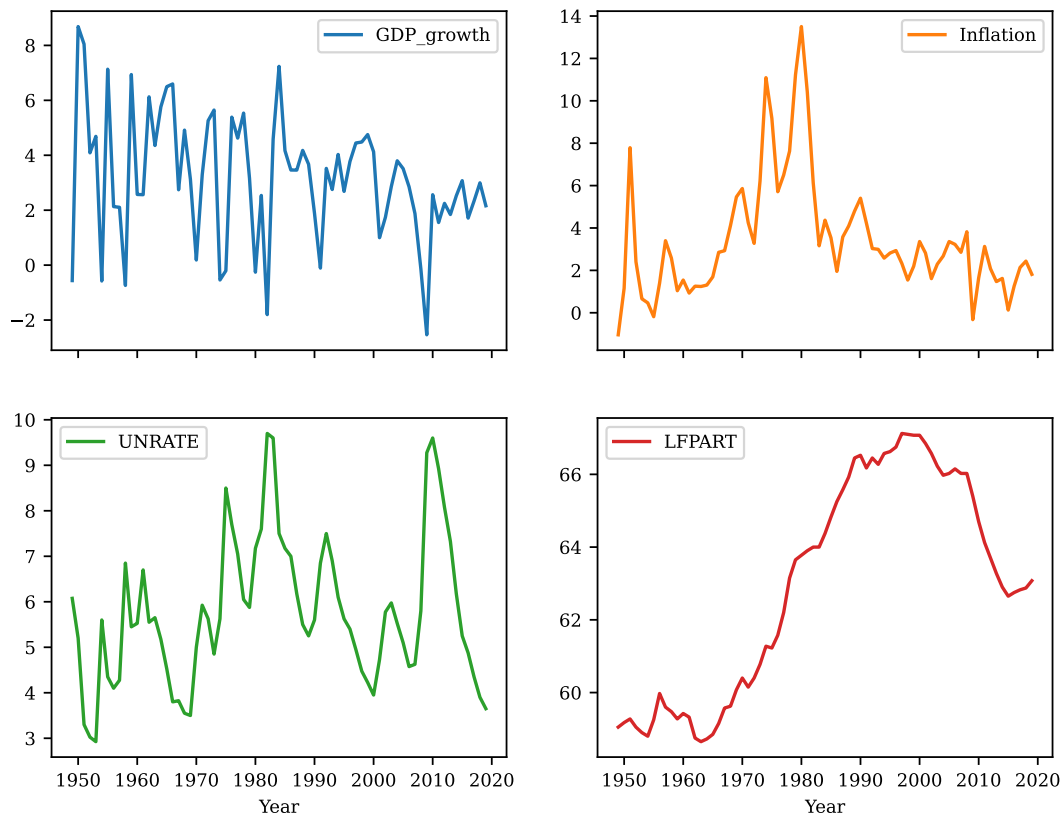
# Compute CPI and GDP growth rates (in percent)
df_year['Inflation'] = df_year['CPI'].diff() / df_year['CPI'].shift() * 100.0
df_year['GDP_growth'] = df_year['GDP'].diff() / df_year['GDP'].shift() * 100.0

# Drop all rows that contain any NaNs
df_year = df_year.dropna(axis=0)

# Columns to plot
varnames = ['GDP_growth', 'Inflation', 'UNRATE', 'LFPART']
df_year.plot.line(y=varnames, subplots=True, layout=(2, 2),
                  sharex=True, figsize=(8, 6))

# Alternatively, we can call plot() directly, which
# defaults to generating a line plot:
#
# df_year.plot(y=varnames, subplots=True, layout=(2, 2),
#              sharex=True, figsize=(10, 10))
```

```
[38]: array([[<AxesSubplot:xlabel='Year'>, <AxesSubplot:xlabel='Year'>],
              [<AxesSubplot:xlabel='Year'>, <AxesSubplot:xlabel='Year'>]],
          dtype=object)
```



A few comments:

1. We can set the index column when loading a CSV file by passing the column names as `index_col`:

```
df = pd.read_csv(filepath, sep=',', index_col=['Year', 'Quarter'])
```

Alternatively, we can first load the CSV file and set the index later:

```
df = pd.read_csv(filepath, sep=',')
df.set_index(keys=['Year', 'Quarter'], inplace=True)
```

2. There are several ways to compute the means of grouped data:

1. We can call `mean()` on the group object directly:

```
df_year = grp.mean()
```

2. Alternatively, we can call `agg()` and pass it the aggregation routine that should be applied:

```
df_year = grp.agg('mean')
df_year = grp.agg(np.mean)
```

Here we again have multiple options: pandas understands 'mean' if passed as a string (which might not be the case for some other functions), or we pass an actual function such as `np.mean`.

3. The easiest way to compute differences between adjacent rows is to use the `diff()` method, which returns $x_t - x_{t-1}$. Pandas then automatically matches the correct values and sets the first observation to NaN as there is no preceding value to compute the difference.

To compute a growth rate $(x_t - x_{t-1})/x_{t-1}$, we additionally need to lag a variable to get the correct period in the denominator. In pandas this is achieved using the `shift()` method (which defaults to shifting by 1 period).

1.8.2 Solution for exercise 2

This time we do not specify `index_cols` when reading in the CSV data since we need `Year` as a regular variable, not as the index.

We then compute the decade for each year, using the fact that `//` performs division with integer truncation. As an example, $1951 // 10$ is 195, and $(1951 // 10) * 10 = 1950$, which we use to represent the 1950s.

```
[39]: import pandas as pd

filepath = '../data/FRED_QTR.csv'

df = pd.read_csv(filepath, sep=',')

# Compute GDP growth rates, inflation (in percent)
df['GDP_growth'] = df['GDP'].diff() / df['GDP'].shift() * 100.0
df['Inflation'] = df['CPI'].diff() / df['CPI'].shift() * 100.0

# Assign decade using // to truncate division to
# integer part. So we have 194x // 10 = 194 for any x.
df['Decade'] = (df['Year'] // 10) * 10

grp = df.groupby(['Decade'])

# Print number of obs. by decade
print(grp.count())

# Create series that contains True for each
# decade if all variables have 40 observations.
use_decade = (grp.count() == 40).all(axis=1)
# Convert series to DataFrame, assign column name 'Keep'
df_decade = use_decade.to_frame('Keep')
# merge into original DataFrame, matching rows on value
# of column 'Decade'
df = df.merge(df_decade, on='Decade')
# Restrict data only to rows which are part of complete decade
df = df.loc[df['Keep'], :].copy()
# Drop 'Keep' column
del df['Keep']

# Compute average growth rates and unemployment rate by decade
grp = df.groupby(['Decade'])

df_avg = grp[['GDP_growth', 'Inflation', 'UNRATE']].mean()
# Convert to (approximate) annualised growth rates
df_avg['GDP_growth'] *= 4.0
df_avg['Inflation'] *= 4.0
```

	Year	Quarter	GDP	CPI	UNRATE	LFPART	GDPPOT	NROU	GDP_growth \
Decade									
1940	8	8	8	8	8	8	4	4	7
1950	40	40	40	40	40	40	40	40	40
1960	40	40	40	40	40	40	40	40	40
1970	40	40	40	40	40	40	40	40	40
1980	40	40	40	40	40	40	40	40	40
1990	40	40	40	40	40	40	40	40	40
2000	40	40	40	40	40	40	40	40	40
2010	40	40	40	40	40	40	40	40	40

	Inflation
Decade	
1940	7
1950	40

1960	40
1970	40
1980	40
1990	40
2000	40
2010	40

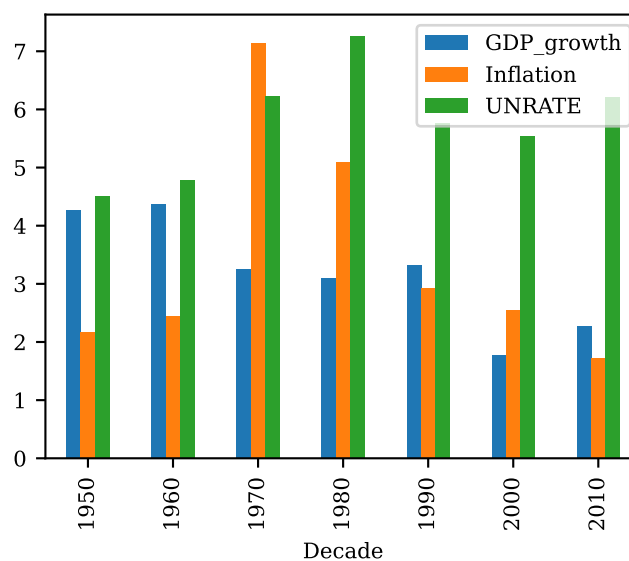
The tricky part is to keep only observations for “complete” decades that have 40 quarters of data. We see that this is not the case for the 1940s:

1. We group by `Decade` and use `count()` to determine the number of non-missing observations for each variable.
2. `count() == 40` evaluates to `True` for some variable if it has 40 observations.
3. We then use `all()` to aggregate across all variables, i.e., we require 40 observations for every variable to keep the decade.
4. Finally, we merge the indicator whether a decade should be kept in the data set using `merge()`, where we match on the value of the column `Decade`. Note that the argument to `merge()` must be a `DataFrame`, so we first have to convert our indicator data.
5. Finally, we keep only those observations which have a flag that is `True`.

The rest of the exercise is straightforward as it just repeats what we have done previously. You can create the bar chart directly with pandas as follows:

```
[40]: df_avg.plot.bar(y=['GDP_growth', 'Inflation', 'UNRATE'])
```

```
[40]: <AxesSubplot:xlabel='Decade'>
```



1.8.3 Solution for exercise 3

We first read in the CSV file, specifying ';' as the field separator:

```
[41]: import pandas as pd

# Load CSV file
filepath = '../data/universities.csv'
df = pd.read_csv(filepath, sep=';')
```

For the first task we use `apply()` to create a new `Series` object for each ratio of interest.

We compute the ratios for each institution which will result in NaNs if either the numerator or denominator is missing. We thus use `np.nanmean()` to compute averages, ignoring any NaNs.

Finally, we combine all Series into a DataFrame. We do this by specifying the data passed to `DataFrame()` as a dictionary, since then we can specify the column names as keys.

```
[42]: # Variant 1
# Compute means using apply()

grp = df.groupby(['Russell'])

# Create Series objects with the desired means
staff = grp.apply(lambda x: np.nanmean(x['Staff'] / x['Students']))
admin = grp.apply(lambda x: np.nanmean(x['Admin'] / x['Students']))
# Budget in millions of pounds
budget = grp.apply(lambda x: np.nanmean(x['Budget'] / x['Students']))
# Convert to pounds
budget *= 1.0e6
# Count number of institutions in each group.
# We can accomplish this by calling size() on the group object.
count = grp.size()

# Create a new DataFrame. Each column is a Series object.
df_all = pd.DataFrame({'Staff_Student': staff,
                       'Admin_Student': admin,
                       'Budget_Student': budget,
                       'Count': count})

df_all
```

```
[42]:
```

	Staff_Student	Admin_Student	Budget_Student	Count
Russell				
0	0.096219	0.147762	16847.834366	6
1	0.155131	0.169079	35406.453649	17

For the second task, we first insert additional columns which contain the ratios of interest for each university.

We then drop all unused columns, group by the Russell indicator and compute the means by directly calling `mean()` on the group object.

```
[43]: # Variant 2:
# Compute ratios first, apply aggregation later

# Create new variables directly in original DataFrame
df['Staff_Student'] = df['Staff'] / df['Students']
df['Admin_Student'] = df['Admin'] / df['Students']
# Budget in pounds (original Budget is in million pounds)
df['Budget_Student'] = df['Budget'] / df['Students'] * 1.0e6

# Keep only newly constructed ratios
columns_keep = [name for name in df.columns
                 if name.endswith('_Student')]
# Also keep Russell indicator
columns_keep += ['Russell']
df = df[columns_keep].copy()

# Aggregate by Russell indicator
grp = df.groupby(['Russell'])
# Count number of institutions in each group.
# We can accomplish this by calling size() on the group object.
count = grp.size()
```

```
df_all = grp.mean()
# Add counter
df_all['Count'] = count

df_all
```

```
[43]:
```

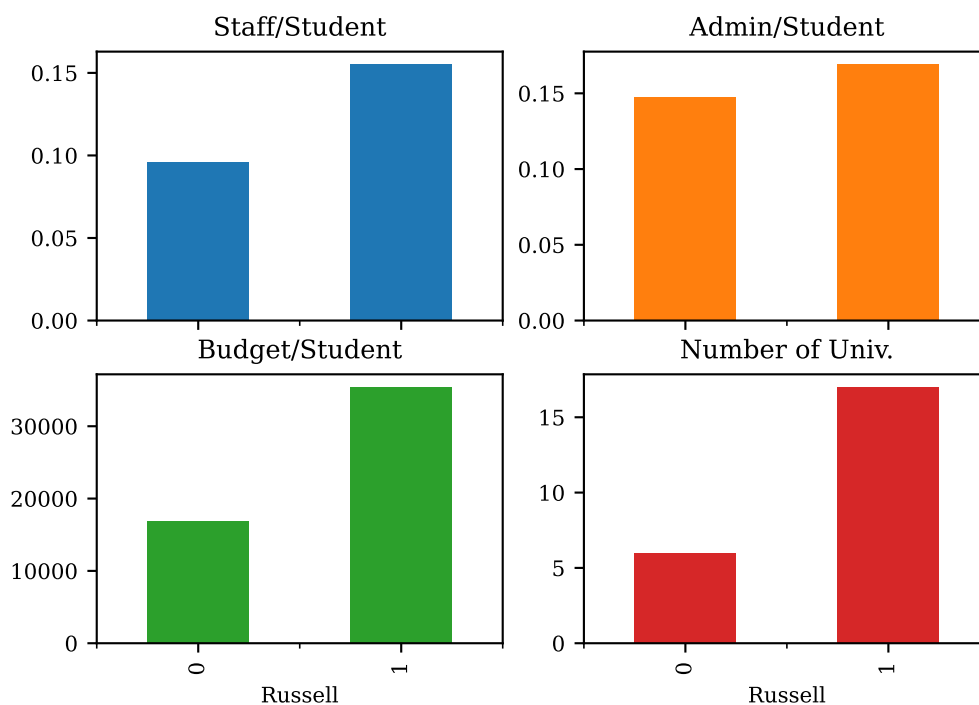
	Staff_Student	Admin_Student	Budget_Student	Count
Russell				
0	0.096219	0.147762	16847.834366	6
1	0.155131	0.169079	35406.453649	17

We plot the results using pandas's `bar()` function. Since the data is of vastly different magnitudes, we specify `sharey=False` so that each panel will have its own scaling on the y-axis.

```
[44]: # Plot results as bar charts, one panel for each variable

# Pretty titles
title = ['Staff/Student', 'Admin/Student', 'Budget/Student', 'Number of Univ.']
# Create bar chart using pandas's bar() function
df_all.plot.bar(sharey=False, subplots=True, layout=(2, 2), legend=False,
                title=title, figsize=(6, 4))
```

```
[44]: array([[<AxesSubplot:title={'center':'Staff/Student'}, xlabel='Russell'>,
  <AxesSubplot:title={'center':'Admin/Student'}, xlabel='Russell'>],
  [<AxesSubplot:title={'center':'Budget/Student'}, xlabel='Russell'>,
  <AxesSubplot:title={'center':'Number of Univ.'}, xlabel='Russell'>]],
  dtype=object)
```



1.8.4 Solution for exercise 4

We create an indicator variable called `Pre1800` which is set to `True` whenever the founding year in column `Founded` is lower than 1800.

We then group the data by Country and Pre1800 and count the number of universities in each group using `count()`.

```
[45]: import pandas as pd

# Load CSV file
filepath = '../data/universities.csv'
df = pd.read_csv(filepath, sep=';')

# Create mask for founding period
df['Pre1800'] = (df['Founded'] < 1800)

# Create group by country and founding period;
grp = df.groupby(['Country', 'Pre1800'])

# Number of universities by country and founding period.
# Since we are grouping by two attributes, this will create a
# Series with a multi-level (hierarchical) index
count = grp.size()

count
```

```
[45]: Country      Pre1800
      England      False      8
              True       5
Northern Ireland False      1
Scotland        False      3
              True       4
Wales           False      2
dtype: int64
```

The resulting Series only contains values for those combinations that are actually present in the data. For example, the combination (Wales, True) does not show up because there are no Welsh universities founded before 1800 in our sample. We will have to “complete” the data and add zero entries in all such cases.

First, we create a DataFrame with countries in rows and the number of universities for the pre- and post-1800 periods in columns. To accomplish this, we need to pivot the second row index using the `unstack()` method. The `level=-1` argument tells it to use the last row index, and `fill_value=0` will assign zeros to all elements that were not present in the initial DataFrame, such as the combination (Wales, True).

```
[46]: # DataFrame with countries in rows, Pre-1800 indicator in columns

# Pivot inner index level to create separate columns for True/False
# values of Pre1800 indicator
df_count = count.unstack(level=-1, fill_value=0)

# Set name of column index to something pretty: this will
# be used as the legend title
df_count.columns.rename('Founding year', inplace=True)
# Rename columns to get pretty labels in legend
df_count.rename(columns={True: 'Before 1800', False: 'After 1800'},
                inplace=True)

df_count
```

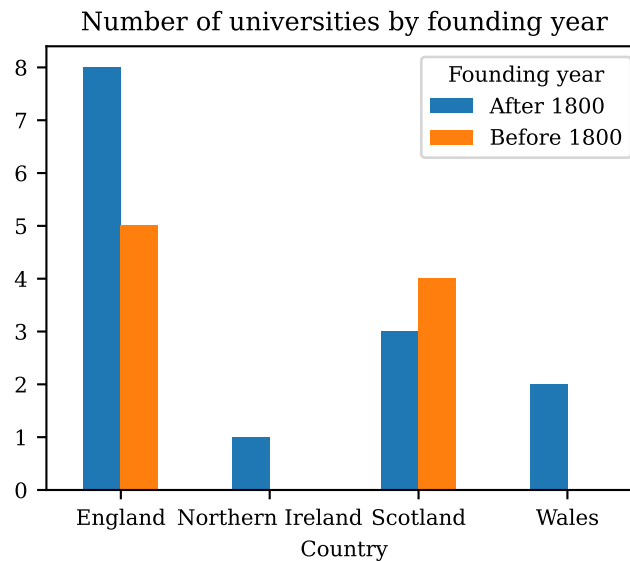
```
[46]: Founding year      After 1800  Before 1800
Country
England                8             5
Northern Ireland       1             0
Scotland               3             4
Wales                  2             0
```

Whenever we use pandas's built-in plotting functions, these use index names and labels to automatically label the graph. We therefore first have to assign these objects "pretty" names.

We can then generate the bar chart as follows:

```
[47]: # Create bar chart by country
title = 'Number of universities by founding year'
# pass rot=0 to undo the rotation of x-tick labels
# which pandas applies by default
df_count.plot.bar(xlabel='Country', rot=0, title=title)
```

```
[47]: <AxesSubplot:title={'center':'Number of universities by founding year'},
      xlabel='Country'>
```



Note how the legend title is automatically set to the column index name and the legend labels use the column index labels.

We create the second DataFrame with the founding period in rows and country names in columns in exactly the same way, but now call `unstack(level=0)` so that the first index level will be pivoted.

```
[48]: # Pivot first row index level to create separate columns for each country
df_count = count.unstack(level=0, fill_value=0)

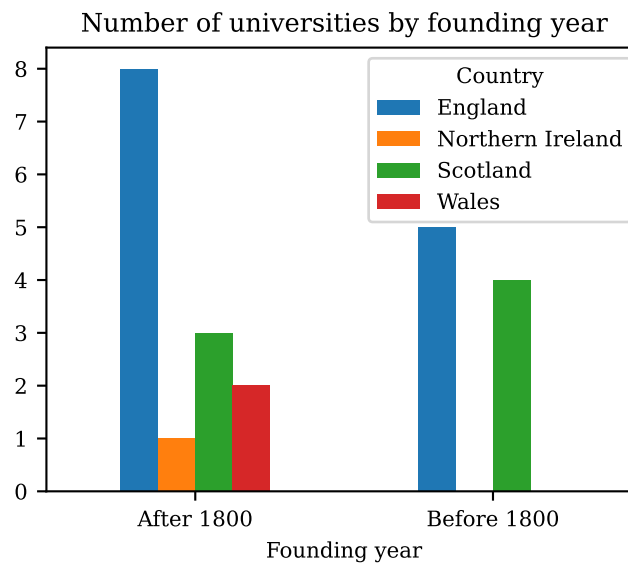
# Set index name to something pretty
df_count.index.rename('Founding year', inplace=True)
# Rename index labels to get pretty text in legend
df_count.rename(index={True: 'Before 1800', False: 'After 1800'},
                inplace=True)

df_count
```

```
[48]: Country      England  Northern Ireland  Scotland  Wales
Founding year
After 1800          8             1           3       2
Before 1800          5             0           4       0
```

```
[49]: # Create bar chart by founding year
# pass rot=0 to undo the rotation of x-tick labels
# which pandas applies by default
df_count.plot.bar(rot=0, title=title)
```

```
[49]: <AxesSubplot:title={'center':'Number of universities by founding year'},
      xlabel='Founding year'>
```



1.8.5 Solution for exercise 5

This exercise is quite involved, so we will discuss it in parts. First, we write the function that will be called by `apply()` to process sub-sets of the data which belong to a single decade:

```
[50]: def regress_okun(x):
    # x is a DataFrame, restricted to rows for the current decade

    # Extract dependent and regressor variables
    outcome = x['unempl_gap'].to_numpy()
    GDP_gap = x['GDP_gap'].to_numpy()

    # Regressor matrix including intercept
    regr = np.ones((len(GDP_gap), 2))
    # overwrite second column with output gap
    regr[:,1] = GDP_gap

    # Solve least-squares problem (pass rcond=None to avoid a warning)
    coefs, *rest = np.linalg.lstsq(regr, outcome, rcond=None)

    # Construct DataFrame which will be returned to apply()
    # Convert data to 1 x 2 matrix
    data = coefs[None]
    columns = ['Const', 'GDP_gap']
    df_out = pd.DataFrame(data, columns=columns)

    return df_out
```

This function is passed in a single argument which is a `DataFrame` restricted to the sub-sample that is currently being processed.

- Our task is to perform the required calculations and to return the result as a `DataFrame`. `apply()` then glues together all decade-specific `DataFrames` to form the result of the operation.
- We first extract the relevant variables as NumPy arrays, and we create a regressor matrix which has ones in the first column. This column represents the intercept.

- We invoke `lstsq()` to run the regression. `lstsq()` returns several arguments which we mop up in the tuple `*rest` since we are only interested in the regression coefficients.

Note that we wouldn't be using `lstsq()` to run OLS on a regular basis, but it's sufficient for this use case.

- Finally, we build the `DataFrame` to be returned by this function. It has only one row (since we ran only one regression) and two columns, one for each regression coefficient.

This was the hard part. We now need to perform some standard manipulations to prepare the data:

1. We construct the output gap (in percent), which we store in the column `GDP_gap`.
2. We construct the cyclical unemployment rate and store it in the column `unempl_gap`.
3. We determine the decade each observation belongs to using the same code as in previous exercises.
4. We then drop all unused variables from the `DataFrame` and also all observations which contain missing values.

Lastly, we can call `apply()` to run the regression for each decade.

```
[51]: import pandas as pd
import numpy as np
import matplotlib.pyplot as plt

# Load CSV file
filepath = '../data/FRED_QTR.csv'
df = pd.read_csv(filepath, sep=',')

# Generate output gap (in percent)
df['GDP_gap'] = (df['GDP'] - df['GDPPOT']) / df['GDPPOT'] * 100.0

# Generate deviations of unempl. rate from natural unempl. rate
df['unempl_gap'] = df['UNRATE'] - df['NROU']

# Assign decade using // to truncate division to
# integer part. So we have 194x // 10 = 194 for any x.
df['Decade'] = (df['Year'] // 10) * 10

# Keep only variables of interest
df = df[['Decade', 'GDP_gap', 'unempl_gap']]
# Drop rows with any missing obs.
df = df.dropna(axis=0)

# Group by decade
grp = df.groupby(['Decade'])

# Apply regression routine to sub-set of data for each decade
df_reg = grp.apply(regress_okun)
# Get rid of second row index introduced by apply()
df_reg = df_reg.reset_index(level=-1, drop=True)

# Display intercept and slope coefficients
# estimated for each decade.
df_reg
```

```
[51]:
```

	Const	GDP_gap
Decade		
1940	-0.259986	-0.567257
1950	-0.277104	-0.494637
1960	-0.331665	-0.467206
1970	-0.032063	-0.398751
1980	-0.178001	-0.666688
1990	-0.102465	-0.489427
2000	-0.355138	-0.723567
2010	-0.279333	-0.983768

The following code creates 8 panels of scatter plots showing the raw data and overlays a regression line for each decade.

```
[52]: # Number of plots (= number of decades)
Nplots = len(df_reg)

# Fix number of columns, determine rows as needed
ncol = 2
nrow = int(np.ceil(Nplots / ncol))

fig, axes = plt.subplots(nrow, ncol, sharey=True, sharex=True,
                        figsize=(6, 11))

for i, ax in enumerate(axes.flatten()):

    # decade in current iteration
    decade = df_reg.index.values[i]
    # restrict DataFrame to decade-specific data
    dfi = df.loc[df['Decade'] == decade]
    # Scatter plot of raw data
    ax.scatter(dfi['GDP_gap'], dfi['unempl_gap'], color='steelblue',
              alpha=0.7, label='Raw data')

    # Extract regression coefficients
    const = df_reg.loc[decade, 'Const']
    slope = df_reg.loc[decade, 'GDP_gap']

    # plot regression line:
    # We need to provide one point and a slope to define the line to be plotted.
    ax.axline((0.0, const), slope=slope, color='red',
              lw=2.0, label='Regression line')

    # Add label containing the current decade
    ax.text(0.95, 0.95, f"{decade}'s", transform=ax.transAxes,
           va='top', ha='right')

    # Add legend in the first panel only
    if i == 0:
        ax.legend(loc='lower left', frameon=False)

    # Add x- and y-labels, but only for those panels
    # that are on the left/lower boundary of the figure
    if i >= nrow * (ncol - 1):
        ax.set_xlabel('Output gap (%)')
    if (i % ncol) == 0:
        ax.set_ylabel('Cycl. unempl. rate (%-points)')

fig.suptitle("Okun's law")
```

```
[52]: Text(0.5, 0.98, "Okun's law")
```

Okun's law

