

# **STQA\_Session\_06**

## **--Data flow testing**

# Dataflow Coverage

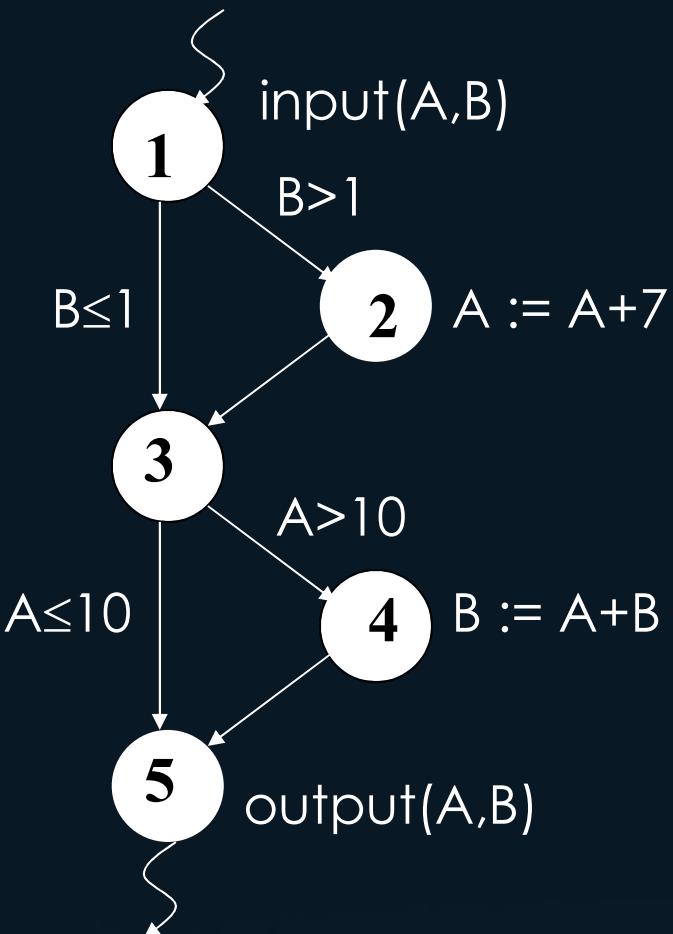
- Based on the idea that program paths along which variables are **defined** and then **used** should be covered.
- A family of path selection criteria has been defined, each providing a different degree of coverage.
- CASE tool support is very desirable.

# Other Dataflow Terms and Definitions

- A path is *definition clear (“def-clear”)* with respect to a variable  $v$  if there is **no re-definition** of  $v$  within the path.
- A *definition-use pair (“du-pair”)* with respect to a variable  $v$  is a double  $(d,u)$  such that  $d$  is a node in the program’s flow graph at which  $v$  is defined,  $u$  is **a node or edge** at which  $v$  is used, and there is **a def-clear path** with respect to  $v$  from  $d$  to  $u$ .
- (Note that the definition of a du-pair does not require the existence of a **feasible** def-clear path from  $d$  to  $u$ .)

# Example 1

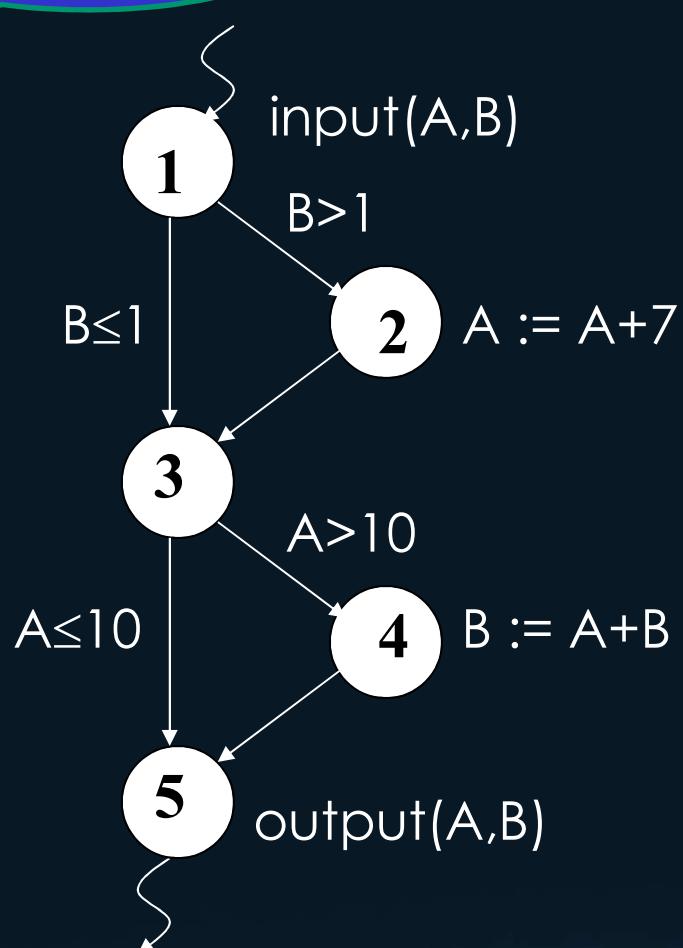
1. `input(A,B)`  
    `if (B>1) then`
2.   `A := A+7`  
    `end_if`
3. `if (A>10) then`
4.   `B := A+B`  
    `end_if`
5. `output(A,B)`



# Identifying DU-Pairs – Variable A

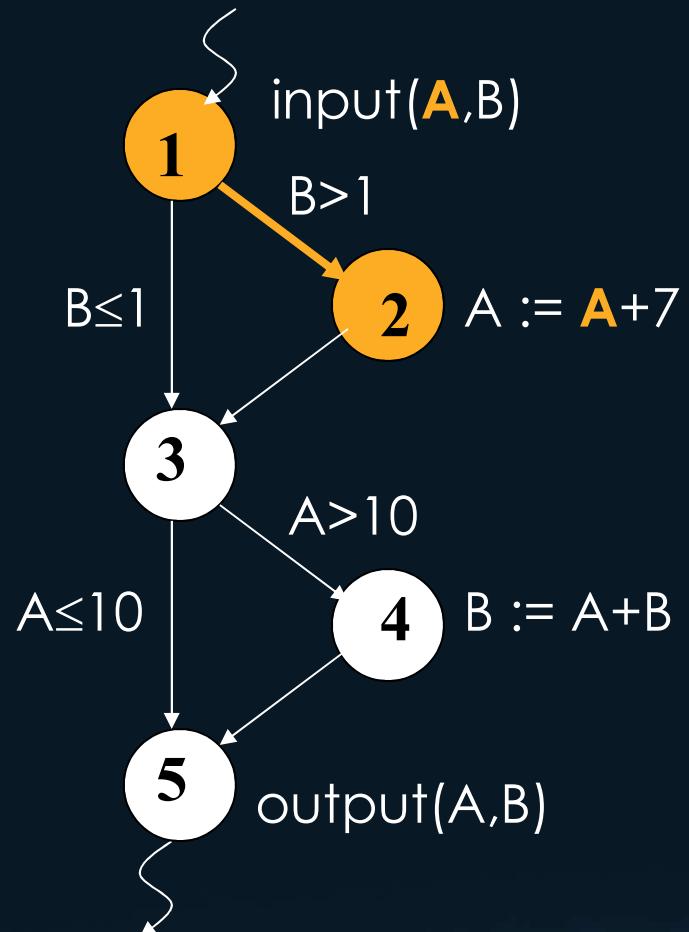
<u>du-pair</u>	<u>path(s)</u>
(1,2)	<1,2>
(1,4)	<1,3,4>
(1,5)	<1,3,4,5>
	<1,3,5>
(1,<3,4>)	<1,3,4>
(1,<3,5>)	<1,3,5>
<hr/>	
(2,4)	<2,3,4>
(2,5)	<2,3,4,5>
	<2,3,5>
(2,<3,4>)	<2,3,4>
(2,<3,5>)	<2,3,5>

d-c paths



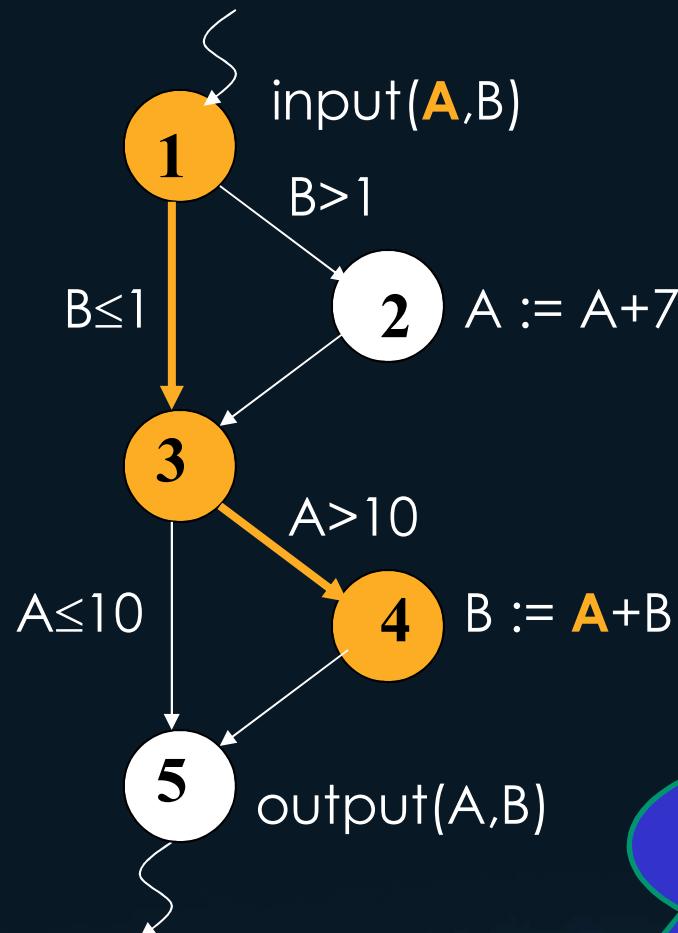
# Identifying DU-Pairs – Variable A

<u>du-pair</u>	<u>path(s)</u>
(1,2)	<1,2>
(1,4)	<1,3,4>
(1,5)	<1,3,4,5>
	<1,3,5>
(1,<3,4>)	<1,3,4>
(1,<3,5>)	<1,3,5>
(2,4)	<2,3,4>
(2,5)	<2,3,4,5>
	<2,3,5>
(2,<3,4>)	<2,3,4>
(2,<3,5>)	<2,3,5>



# Identifying DU-Pairs – Variable A

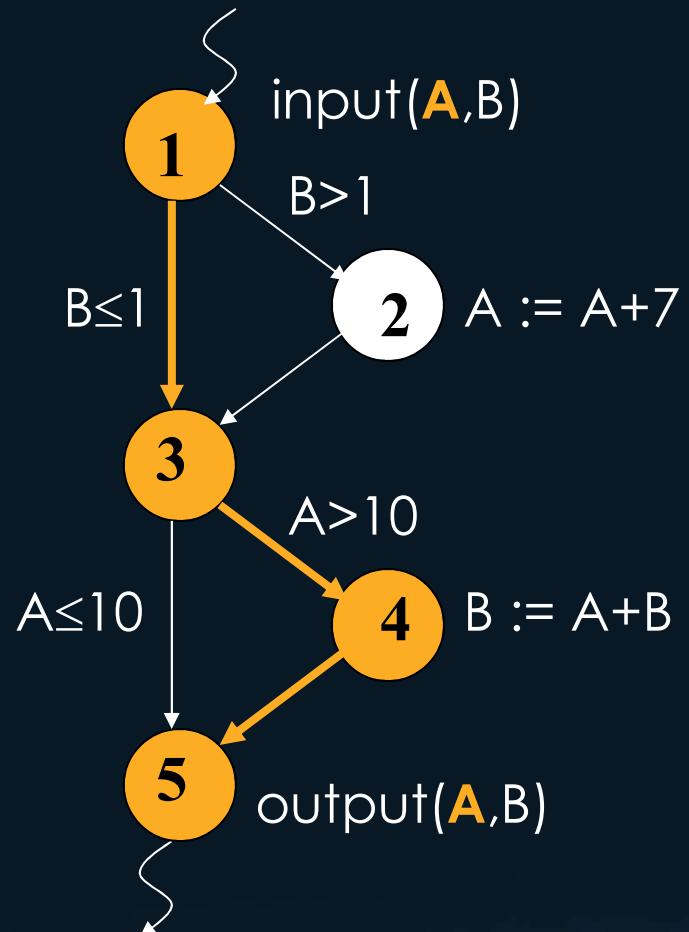
<u>du-pair</u>	<u>path(s)</u>
(1,2)	<1,2>
<b>(1,4)</b>	<b>&lt;1,3,4&gt;</b>
(1,5)	<1,3,4,5>
	<1,3,5>
(1,<3,4>)	<1,3,4>
(1,<3,5>)	<1,3,5>
(2,4)	<2,3,4>
(2,5)	<2,3,4,5>
	<2,3,5>
(2,<3,4>)	<2,3,4>
(2,<3,5>)	<2,3,5>



1,2,3,4?

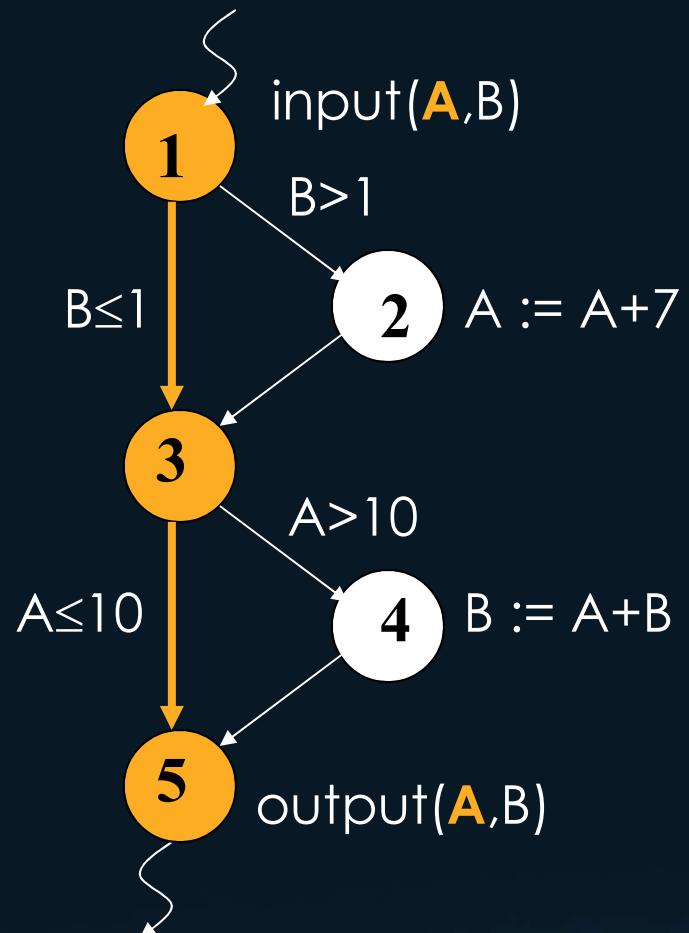
# Identifying DU-Pairs – Variable A

<u>du-pair</u>	<u>path(s)</u>
(1,2)	<1,2>
(1,4)	<1,3,4>
<b>(1,5)</b>	<b>&lt;1,3,4,5&gt;</b>
	<1,3,5>
(1,<3,4>)	<1,3,4>
(1,<3,5>)	<1,3,5>
(2,4)	<2,3,4>
(2,5)	<2,3,4,5>
	<2,3,5>
(2,<3,4>)	<2,3,4>
(2,<3,5>)	<2,3,5>



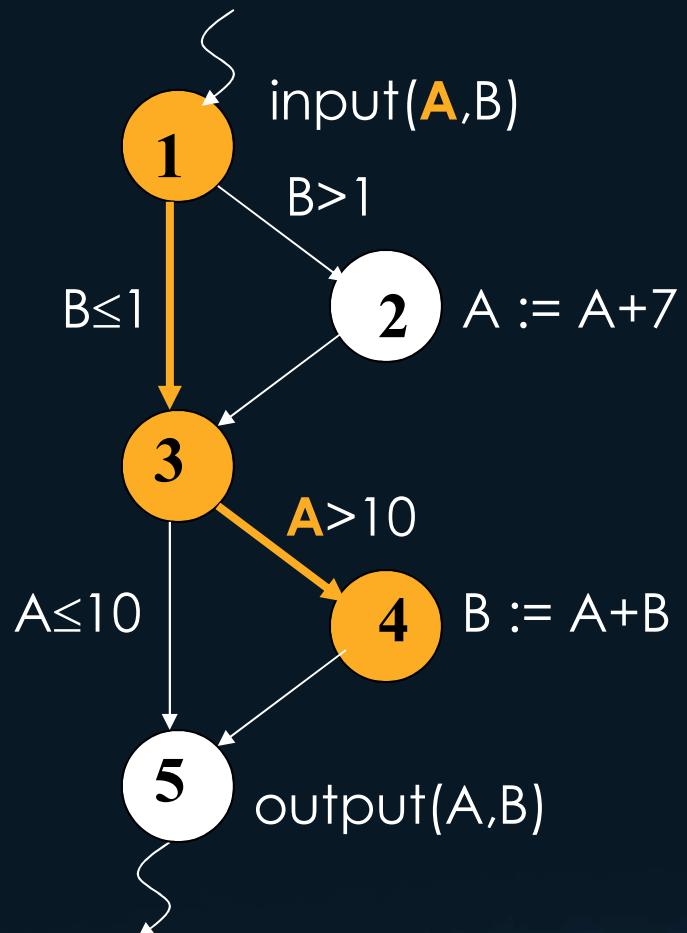
# Identifying DU-Pairs – Variable A

<u>du-pair</u>	<u>path(s)</u>
(1,2)	<1,2>
(1,4)	<1,3,4>
<b>(1,5)</b>	<1,3,4,5> <b>&lt;1,3,5&gt;</b>
(1,<3,4>)	<1,3,4>
(1,<3,5>)	<1,3,5>
(2,4)	<2,3,4>
(2,5)	<2,3,4,5>
	<2,3,5>
(2,<3,4>)	<2,3,4>
(2,<3,5>)	<2,3,5>



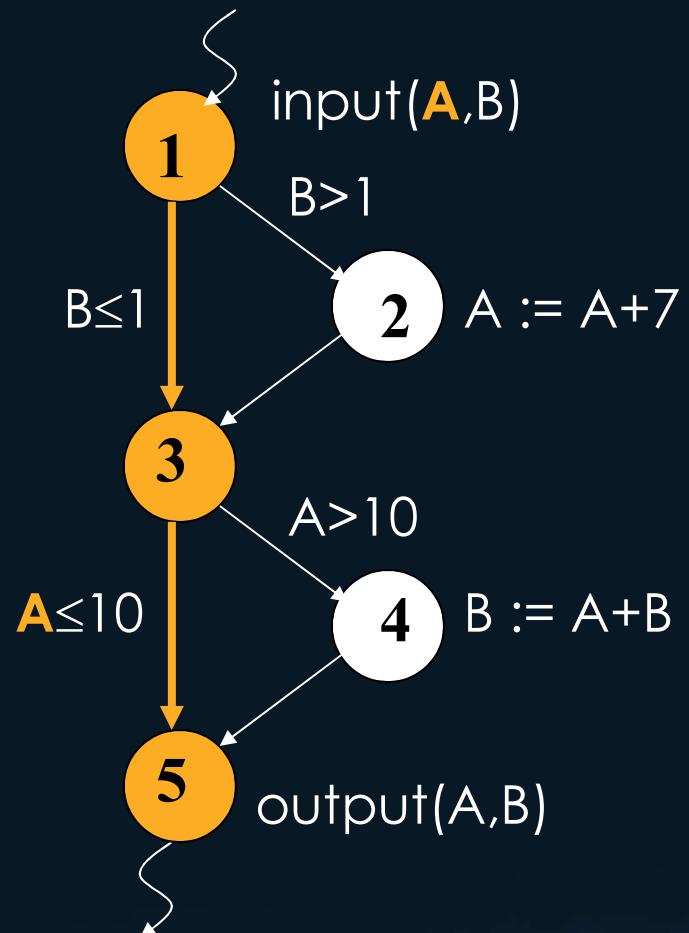
# Identifying DU-Pairs – Variable A

<u>du-pair</u>	<u>path(s)</u>
(1,2)	<1,2>
(1,4)	<1,3,4>
(1,5)	<1,3,4,5>
	<1,3,5>
<b>(1,&lt;3,4&gt;)</b>	<b>&lt;1,3,4&gt;</b>
(1,<3,5>)	<1,3,5>
(2,4)	<2,3,4>
(2,5)	<2,3,4,5>
	<2,3,5>
(2,<3,4>)	<2,3,4>
(2,<3,5>)	<2,3,5>



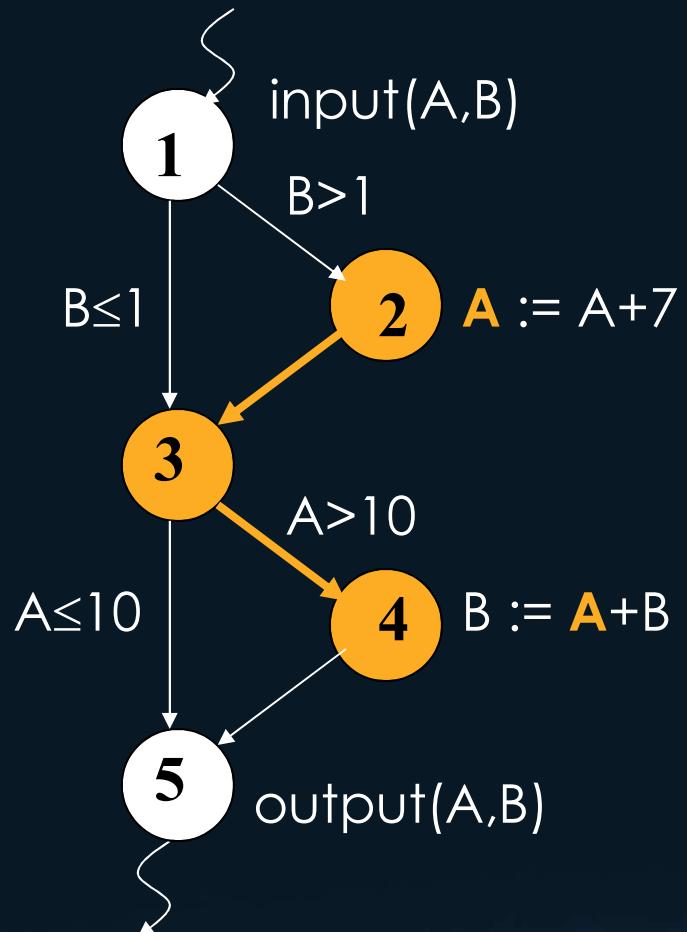
# Identifying DU-Pairs – Variable A

<u>du-pair</u>	<u>path(s)</u>
(1,2)	<1,2>
(1,4)	<1,3,4>
(1,5)	<1,3,4,5>
	<1,3,5>
(1,<3,4>)	<1,3,4>
<b>(1,&lt;3,5&gt;)</b>	<b>&lt;1,3,5&gt;</b>
(2,4)	<2,3,4>
(2,5)	<2,3,4,5>
	<2,3,5>
(2,<3,4>)	<2,3,4>
(2,<3,5>)	<2,3,5>



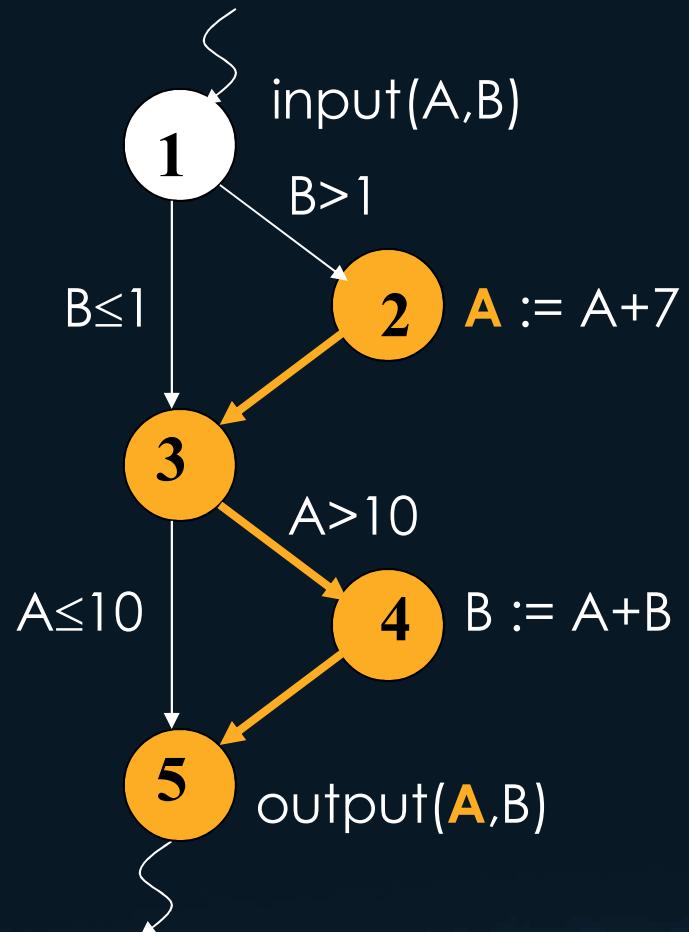
# Identifying DU-Pairs – Variable A

<u>du-pair</u>	<u>path(s)</u>
(1,2)	<1,2>
(1,4)	<1,3,4>
(1,5)	<1,3,4,5>
	<1,3,5>
(1,<3,4>)	<1,3,4>
(1,<3,5>)	<1,3,5>
<b>(2,4)</b>	<b>&lt;2,3,4&gt;</b>
(2,5)	<2,3,4,5>
	<2,3,5>
(2,<3,4>)	<2,3,4>
(2,<3,5>)	<2,3,5>



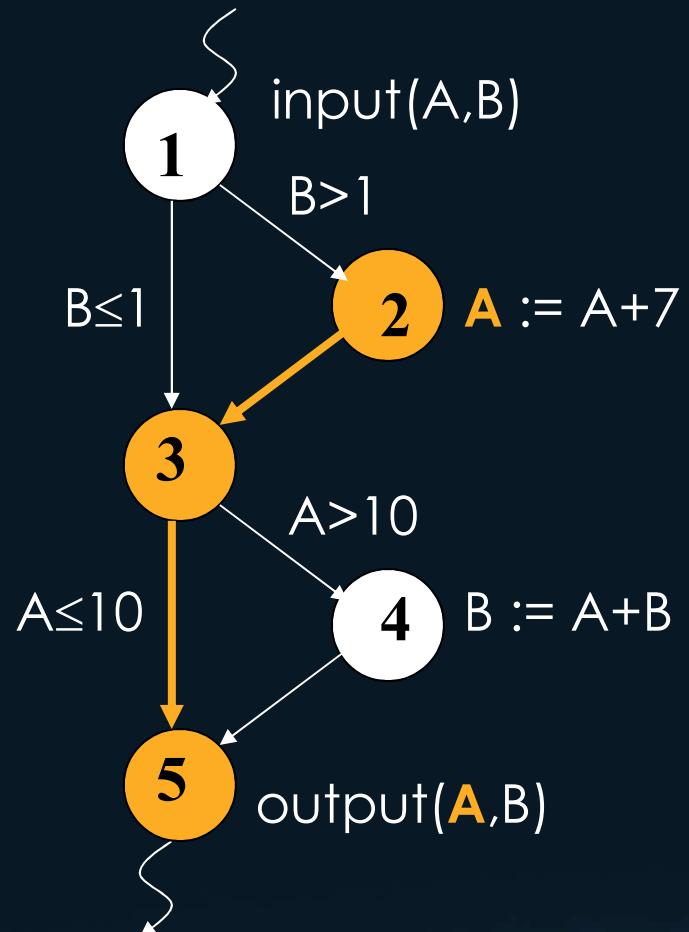
# Identifying DU-Pairs – Variable A

<u>du-pair</u>	<u>path(s)</u>
(1,2)	<1,2>
(1,4)	<1,3,4>
(1,5)	<1,3,4,5>
	<1,3,5>
(1,<3,4>)	<1,3,4>
(1,<3,5>)	<1,3,5>
(2,4)	<2,3,4>
<b>(2,5)</b>	<b>&lt;2,3,4,5&gt;</b>
	<2,3,5>
(2,<3,4>)	<2,3,4>
(2,<3,5>)	<2,3,5>



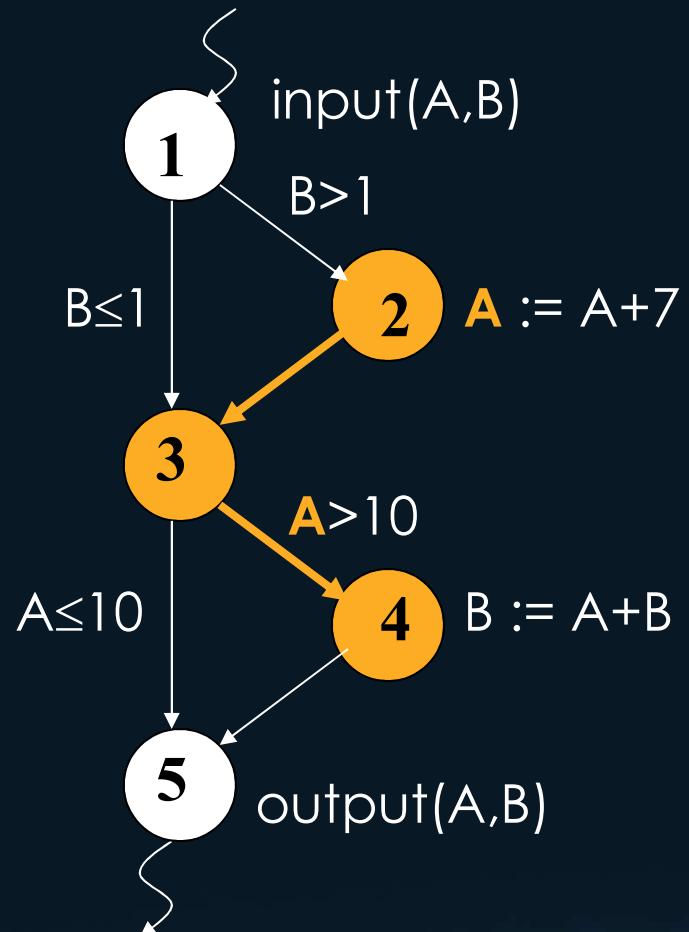
# Identifying DU-Pairs – Variable A

<u>du-pair</u>	<u>path(s)</u>
(1,2)	<1,2>
(1,4)	<1,3,4>
(1,5)	<1,3,4,5>
	<1,3,5>
(1,<3,4>)	<1,3,4>
(1,<3,5>)	<1,3,5>
(2,4)	<2,3,4>
<b>(2,5)</b>	<b>&lt;2,3,4,5&gt;</b>
	<b>&lt;2,3,5&gt;</b>
(2,<3,4>)	<2,3,4>
(2,<3,5>)	<2,3,5>



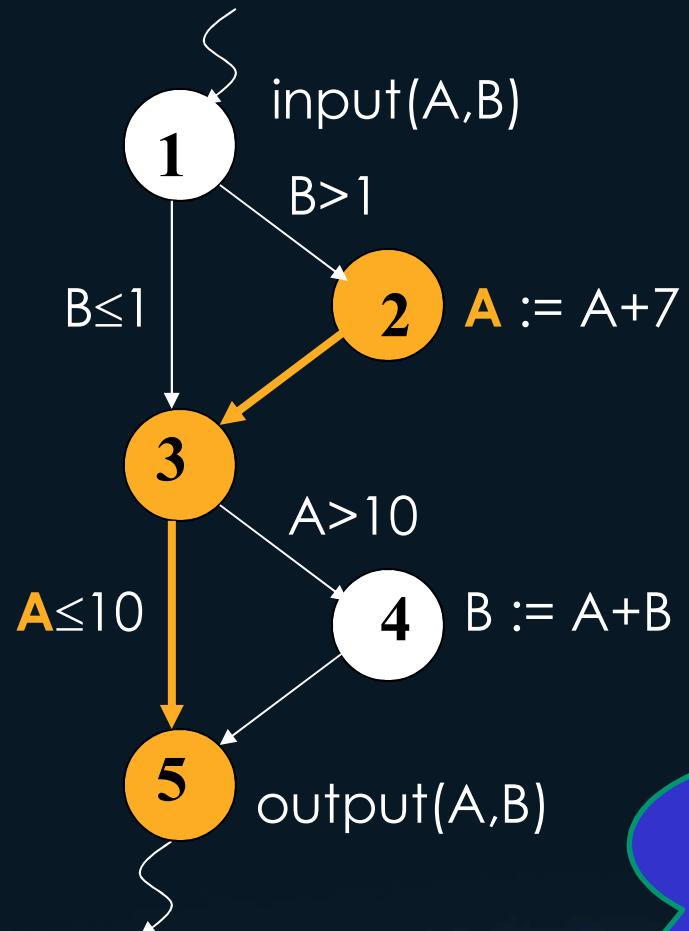
# Identifying DU-Pairs – Variable A

<u>du-pair</u>	<u>path(s)</u>
(1,2)	<1,2>
(1,4)	<1,3,4>
(1,5)	<1,3,4,5>
	<1,3,5>
(1,<3,4>)	<1,3,4>
(1,<3,5>)	<1,3,5>
(2,4)	<2,3,4>
(2,5)	<2,3,4,5>
	<2,3,5>
<b>(2,&lt;3,4&gt;)</b>	<b>&lt;2,3,4&gt;</b>
(2,<3,5>)	<2,3,5>



# Identifying DU-Pairs – Variable A

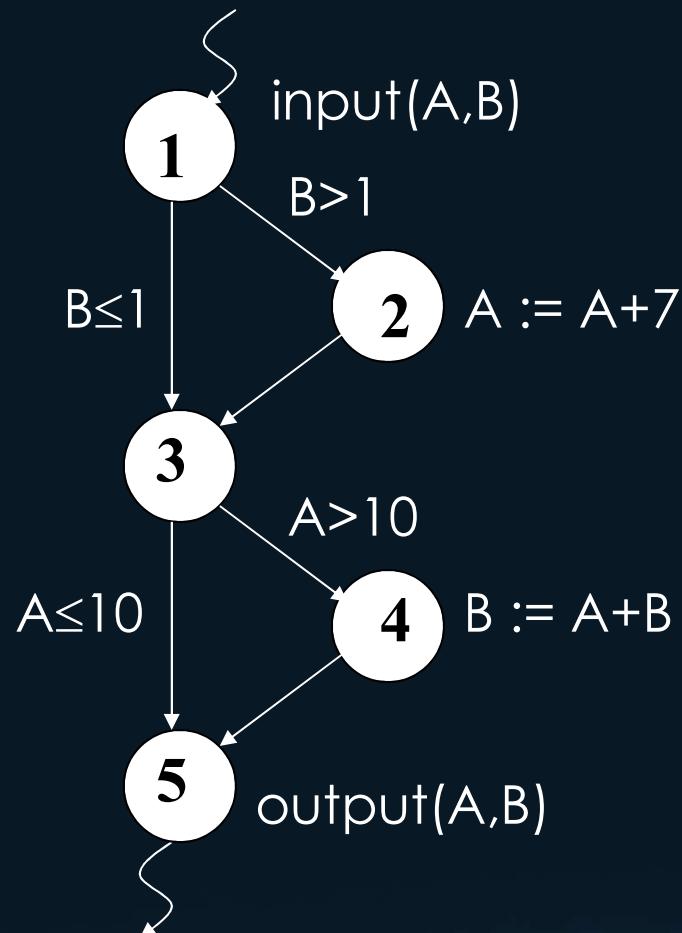
<u>du-pair</u>	<u>path(s)</u>
(1,2)	<1,2>
(1,4)	<1,3,4>
(1,5)	<1,3,4,5>
	<1,3,5>
(1,<3,4>)	<1,3,4>
(1,<3,5>)	<1,3,5>
(2,4)	<2,3,4>
(2,5)	<2,3,4,5>
	<2,3,5>
(2,<3,4>)	<2,3,4>
<b>(2,&lt;3,5&gt;)</b>	<b>&lt;2,3,5&gt;</b>



1,2,3,5?

# Identifying DU-Pairs – Variable B

<u>du-pair</u>	<u>path(s)</u>
(1,4)	<1,2,3,4>
	<1,3,4>
(1,5)	<1,2,3,5>
	<1,3,5>
(1,<1,2>)	<1,2>
(1,<1,3>)	<1,3>
(4,5)	<4,5>



# Dataflow Test Coverage Criteria

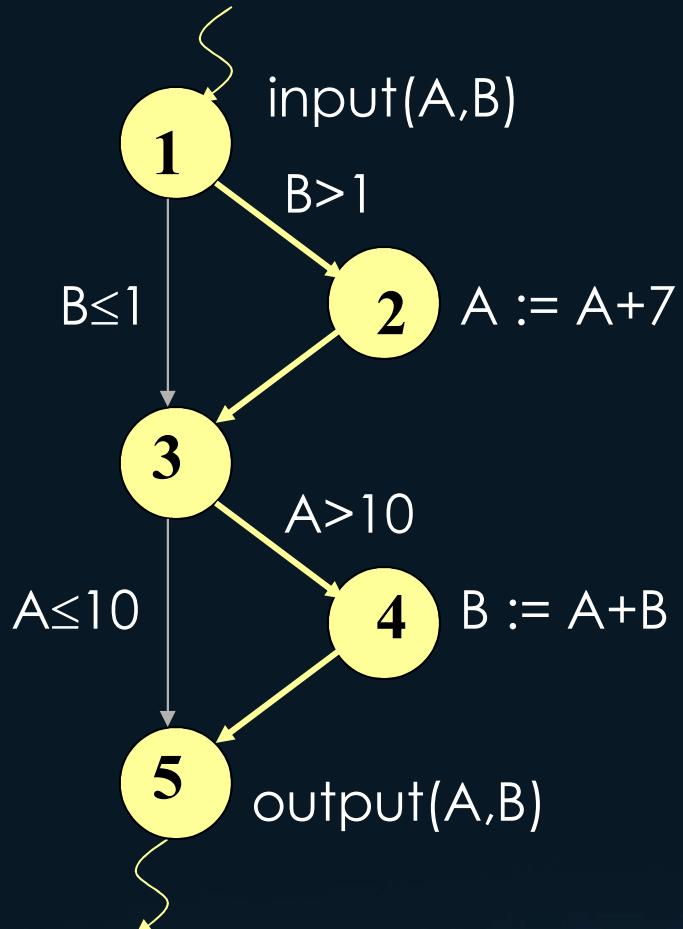
- **All-Defs:** for every program variable  $v$ , at least one def-clear path from **every definition** of  $v$  to **at least one c-use or one p-use** of  $v$  must be covered.

# Dataflow Test Coverage Criteria (cont'd)

- Consider a test case executing path:
  1.  $\langle 1,2,3,4,5 \rangle$
- Identify all def-clear paths covered (i.e., subsumed) by this path for each variable.
- Are all definitions for each variable associated with at least one of the subsumed def-clear paths?

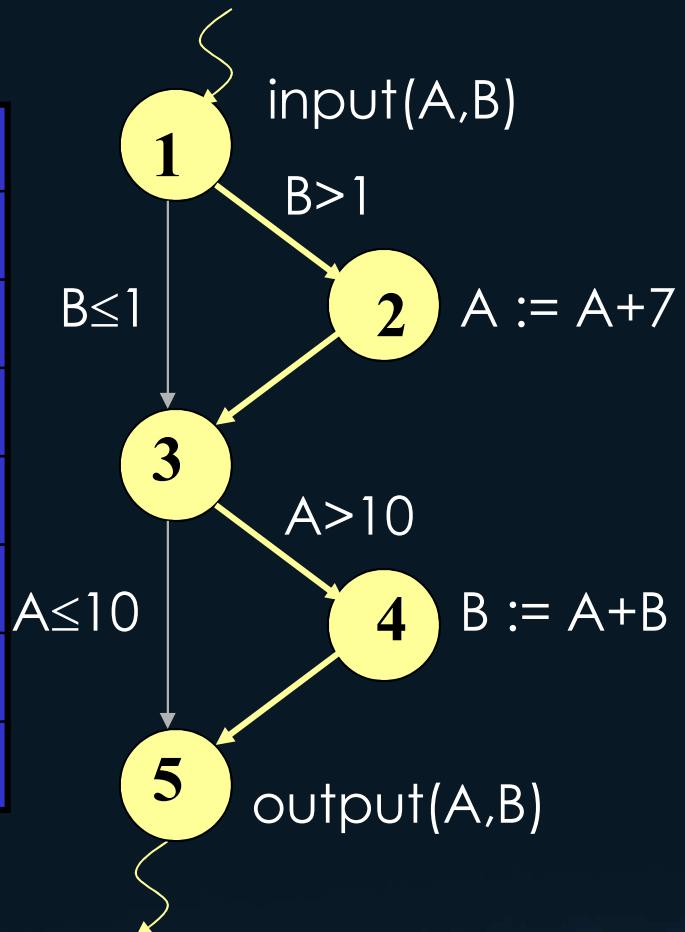
# Def-Clear Paths Subsumed by $\langle 1,2,3,4,5 \rangle$ for Variable A

<u>du-pair</u>	<u>path(s)</u>
(1,2)	$\langle 1,2 \rangle$ ✓
(1,4)	$\langle 1,3,4 \rangle$
(1,5)	$\langle 1,3,4,5 \rangle$
	$\langle 1,3,5 \rangle$
(1, $\langle 3,4 \rangle$ )	$\langle 1,3,4 \rangle$
(1, $\langle 3,5 \rangle$ )	$\langle 1,3,5 \rangle$
<b>(2,4)</b>	$\langle 2,3,4 \rangle$ ✓
<b>(2,5)</b>	$\langle 2,3,4,5 \rangle$ ✓
	$\langle 2,3,5 \rangle$
<b>(2,<math>\langle 3,4 \rangle</math>)</b>	$\langle 2,3,4 \rangle$ ✓
(2, $\langle 3,5 \rangle$ )	$\langle 2,3,5 \rangle$



# Def-Clear Paths Subsumed by $<1,2,3,4,5>$ for Variable B

<u>du-pair</u>	<u>path(s)</u>
(1,4)	$<1,2,3,4>$ ✓
	$<1,3,4>$
(1,5)	$<1,2,3,5>$
	$<1,3,5>$
(4,5)	$<4,5>$ ✓
(1,<1,2>)	$<1,2>$ ✓
(1,<1,3>)	$<1,3>$



## Dataflow Test Coverage Criteria (cont'd)

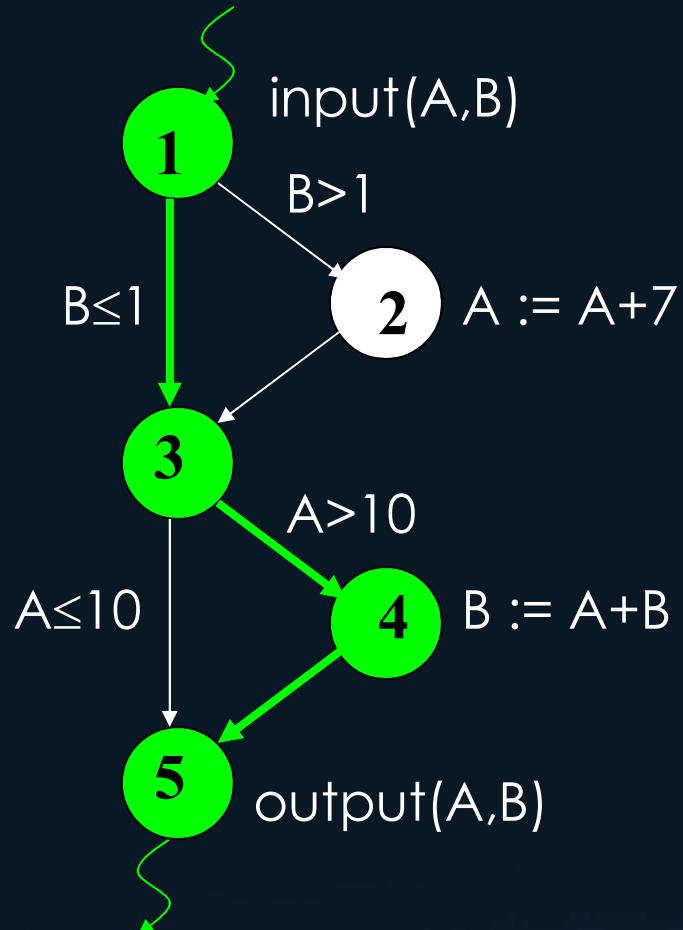
- Since  $\langle 1, 2, 3, 4, 5 \rangle$  covers at least one def-clear path from every definition of A/B to at least one c-use or p-use of A/B, All-Defs coverage is achieved.

# Dataflow Test Coverage Criteria (cont'd)

- **All-Uses:** for **every program variable**  $v$ , at least one def-clear path from **every definition** of  $v$  to **every c-use** and **every p-use** of  $v$  must be covered.
- Consider additional test cases executing paths:
  2.  $\langle 1, 3, 4, 5 \rangle$
  3.  $\langle 1, 2, 3, 5 \rangle$
- Do all three test cases provide All-Uses coverage?

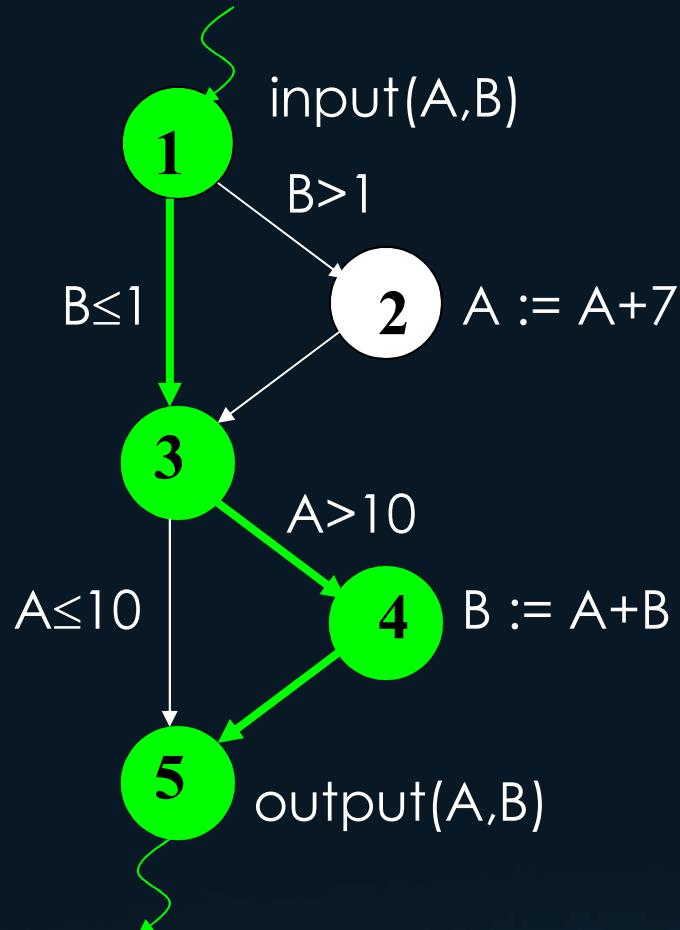
# Def-Clear Paths Subsumed by $<1,3,4,5>$ for Variable A

<u>du-pair</u>	<u>path(s)</u>
(1,2)	$<1,2>$ ✓
(1,4)	$<1,3,4>$ ✓
(1,5)	$<1,3,4,5>$ ✓
	$<1,3,5>$
(1,<3,4>)	$<1,3,4>$ ✓
(1,<3,5>)	$<1,3,5>$
(2,4)	$<2,3,4>$ ✓
(2,5)	$<2,3,4,5>$ ✓
	$<2,3,5>$
(2,<3,4>)	$<2,3,4>$ ✓
(2,<3,5>)	$<2,3,5>$



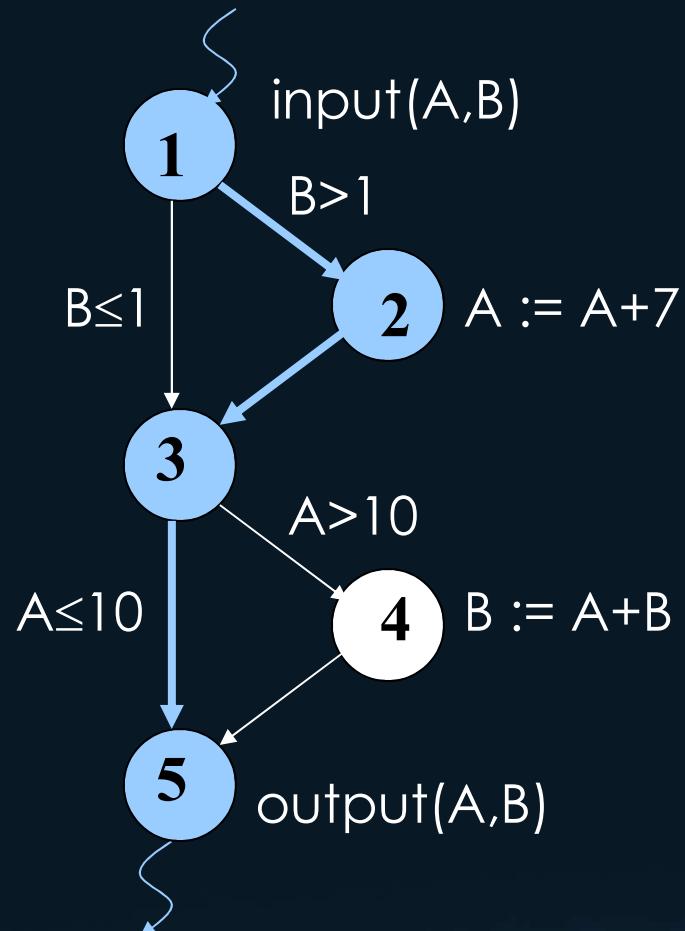
# Def-Clear Paths Subsumed by $<1,3,4,5>$ for Variable B

<u>du-pair</u>	<u>path(s)</u>
(1,4)	$<1,2,3,4>$ ✓
	$<1,3,4>$ ✓
(1,5)	$<1,2,3,5>$
	$<1,3,5>$
(4,5)	$<4,5>$ ✓ ✓
(1,<1,2>)	$<1,2>$ ✓
(1,<1,3>)	$<1,3>$ ✓



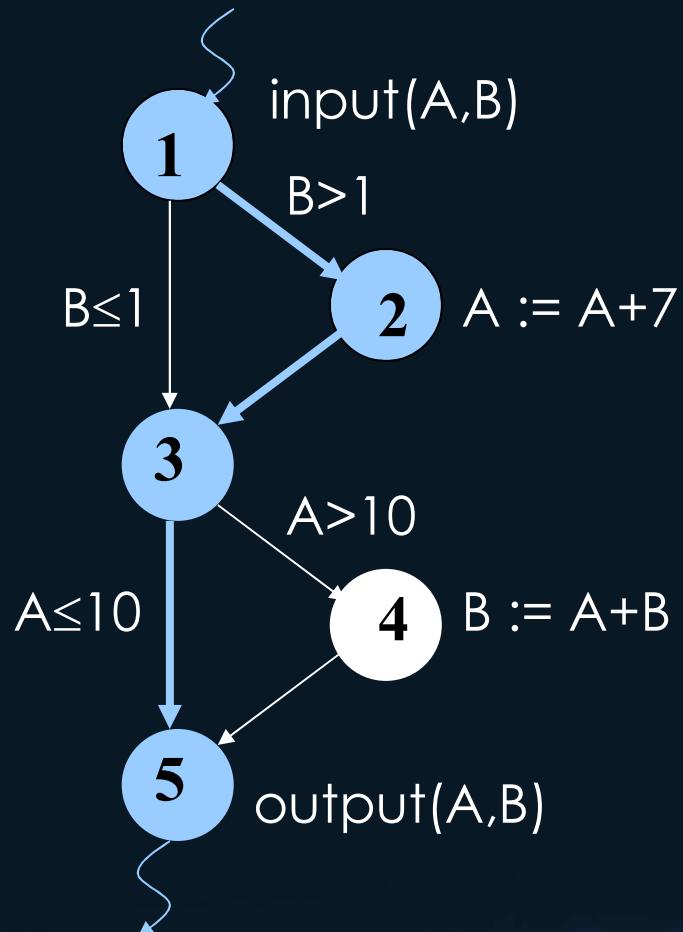
# Def-Clear Paths Subsumed by $\langle 1,2,3,5 \rangle$ for Variable A

<u>du-pair</u>	<u>path(s)</u>
(1,2)	$\langle 1,2 \rangle$ ✓ ✓
(1,4)	$\langle 1,3,4 \rangle$ ✓
(1,5)	$\langle 1,3,4,5 \rangle$ ✓
	$\langle 1,3,5 \rangle$
(1,<3,4>)	$\langle 1,3,4 \rangle$ ✓
(1,<3,5>)	$\langle 1,3,5 \rangle$
(2,4)	$\langle 2,3,4 \rangle$ ✓
(2,5)	$\langle 2,3,4,5 \rangle$ ✓
	$\langle 2,3,5 \rangle$ ✓
(2,<3,4>)	$\langle 2,3,4 \rangle$ ✓
(2,<3,5>)	$\langle 2,3,5 \rangle$ ✓



# Def-Clear Paths Subsumed by $<1,2,3,5>$ for Variable B

<u>du-pair</u>	<u>path(s)</u>
(1,4)	$<1,2,3,4>$ ✓
	$<1,3,4>$ ✓
(1,5)	$<1,2,3,5>$ ✓
	$<1,3,5>$
(4,5)	$<4,5>$ ✓ ✓
(1,<1,2>)	$<1,2>$ ✓ ✓
(1,<1,3>)	$<1,3>$ ✓



## Dataflow Test Coverage Criteria (cont'd)

- Since none of the three test cases covers the du-pair (1,<3,5>) for variable A, **All-Uses Coverage** is not provided.

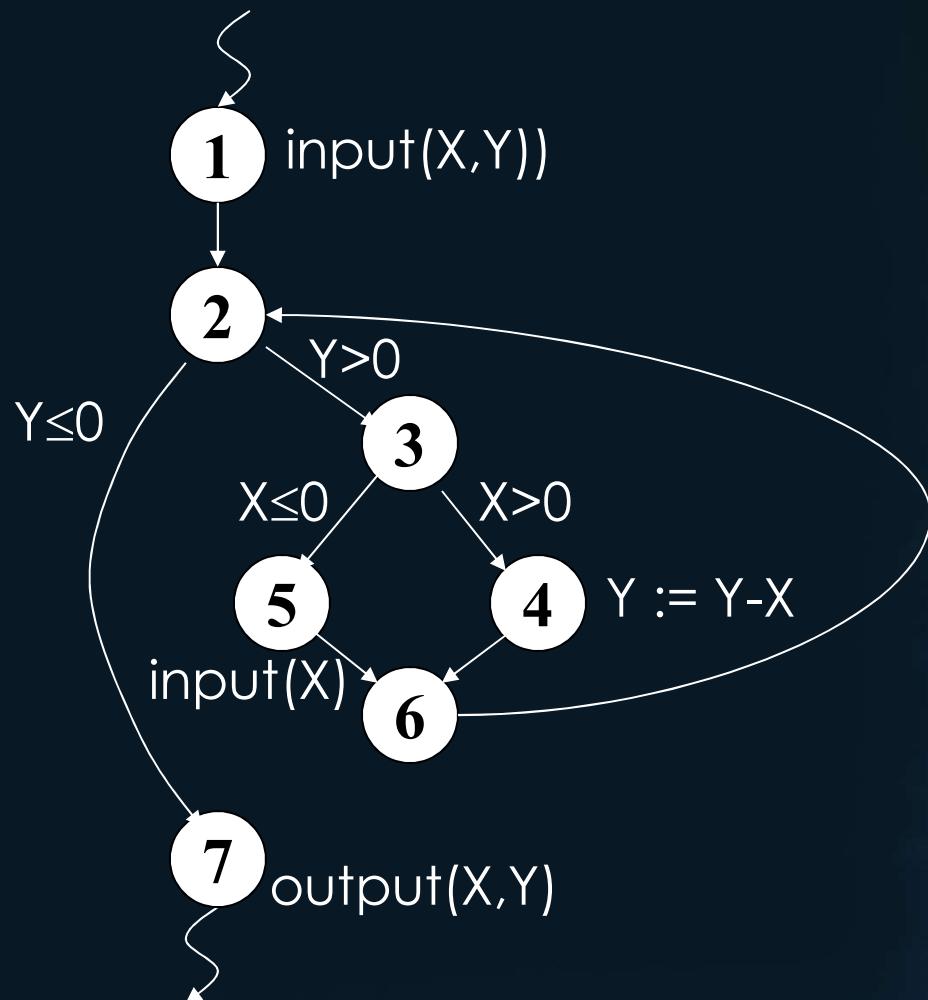
## What would be even stronger than *All-Uses*?

- We have considered the *All-Defs* and the *All-Uses* criteria so far. How could the definition of *All-Uses* be modified to make it even stronger? Recall:

***All-Uses*:** for every program variable  $v$ , **at least one def-clear path** from every definition of  $v$  to every c-use and every p-use of  $v$  must be covered.

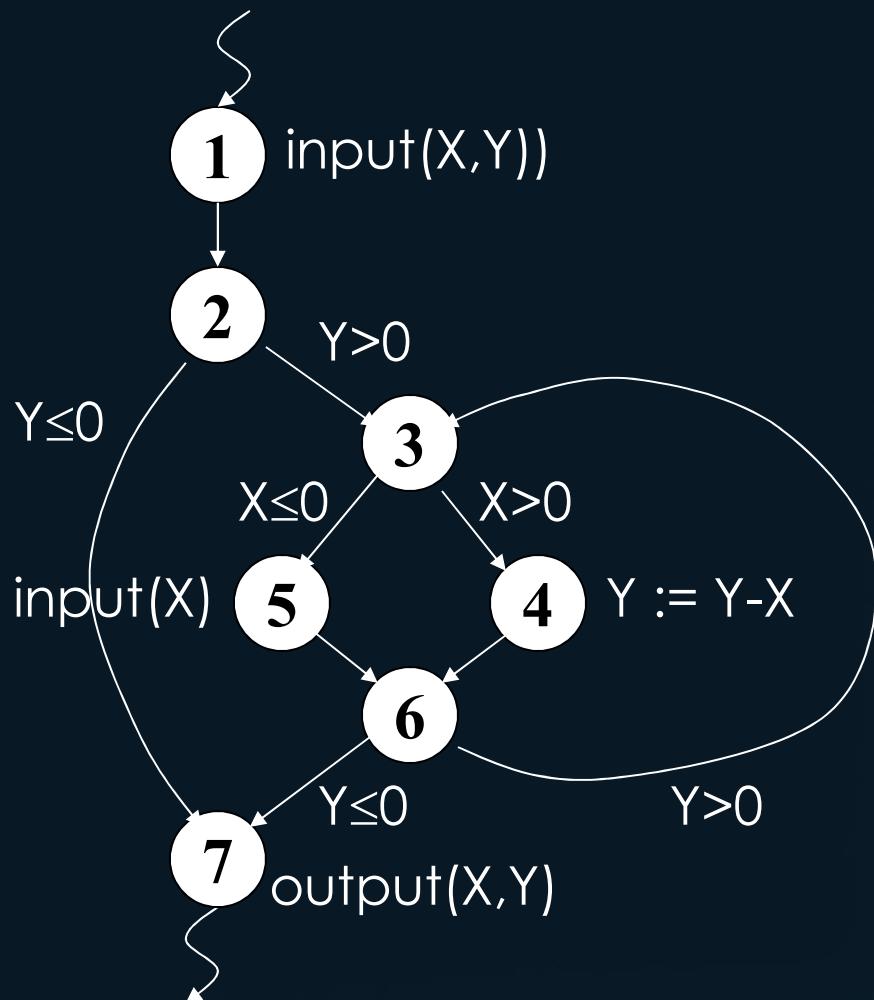
# Exercise

1. `input(X,Y)`
2. `while (Y>0) do`
3.   `if (X>0) then`
4.     `Y := Y-X`
- `else`
5.     `input(X)`
- `end_if_then_else`
6. `end_while`
7. `output(X,Y)`



# Exercise

1. `input(X,Y)`
2. `while (Y>0) do`
3.   `if (X>0) then`
4.     `Y := Y-X`
- `else`
5.     `input(X)`
- `end_if_then_else`
6. `end_while`
7. `output(X,Y)`

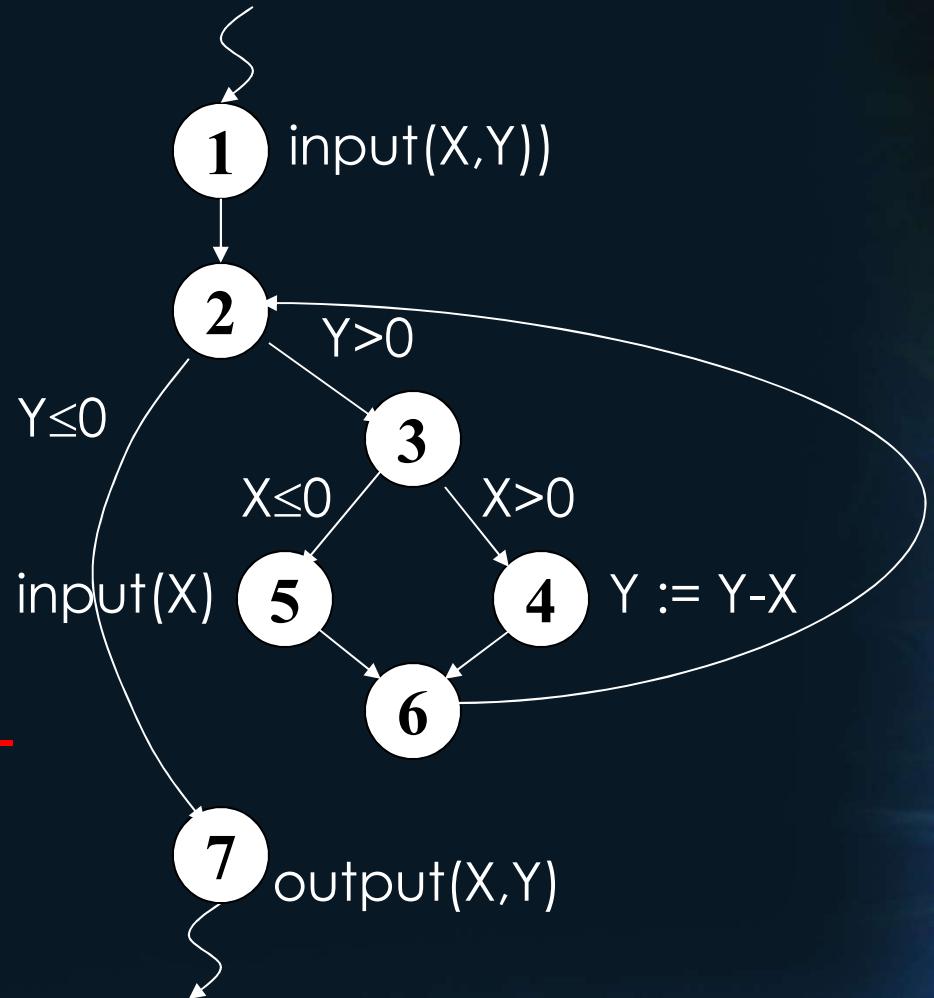


# Exercise

- Identify DU-Pairs for variable X.

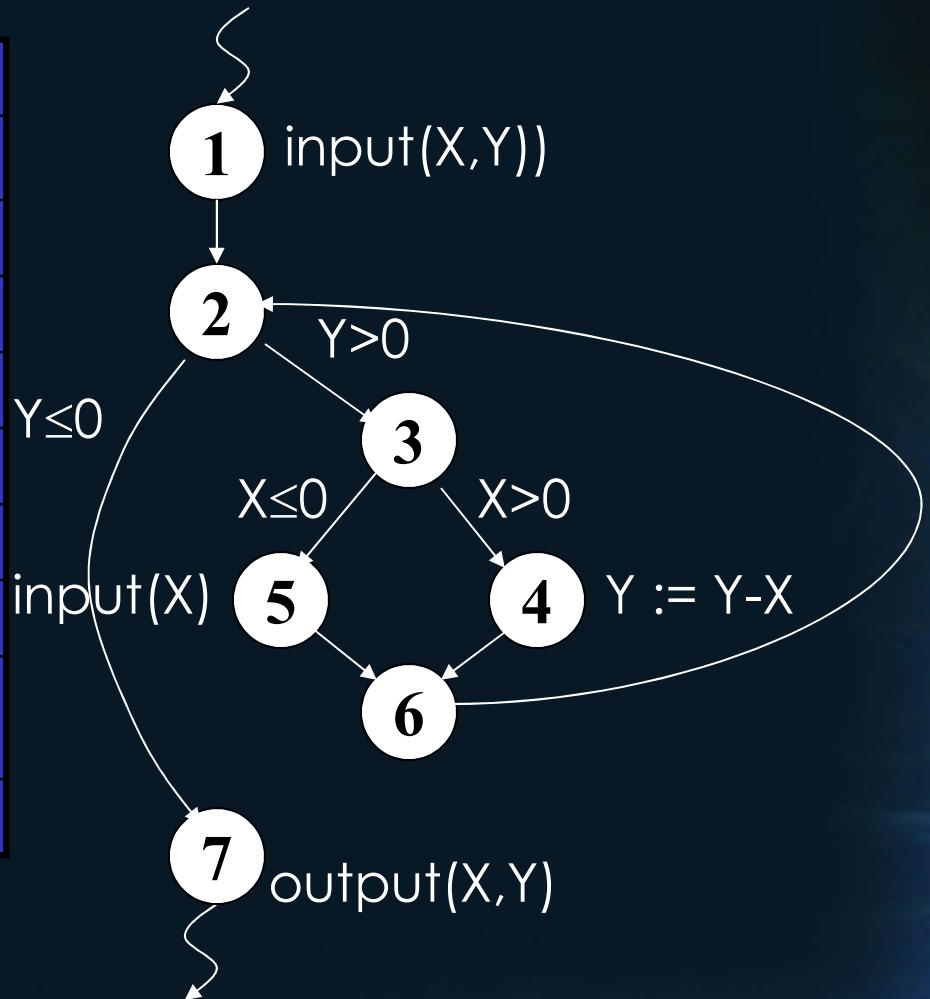
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(1,4)	<1,2,3,4>
	<1,2,3,4,(6,2,3,4)*>
(1,7)	<1,2,7>
	<1,2,3,4,6,2,7>
	<1,2,3,4,6,(2,3,4,6)*,2,7>
(1,<3,4>)	<1,2,3,4>
	<1,2,3,4,(6,2,3,4)*>
(1,<3,5>)	<1,2,3,5>
(5,4)	<5,6,2,3,4>
	<5,6,2,3,4,(6,2,3,4)*>



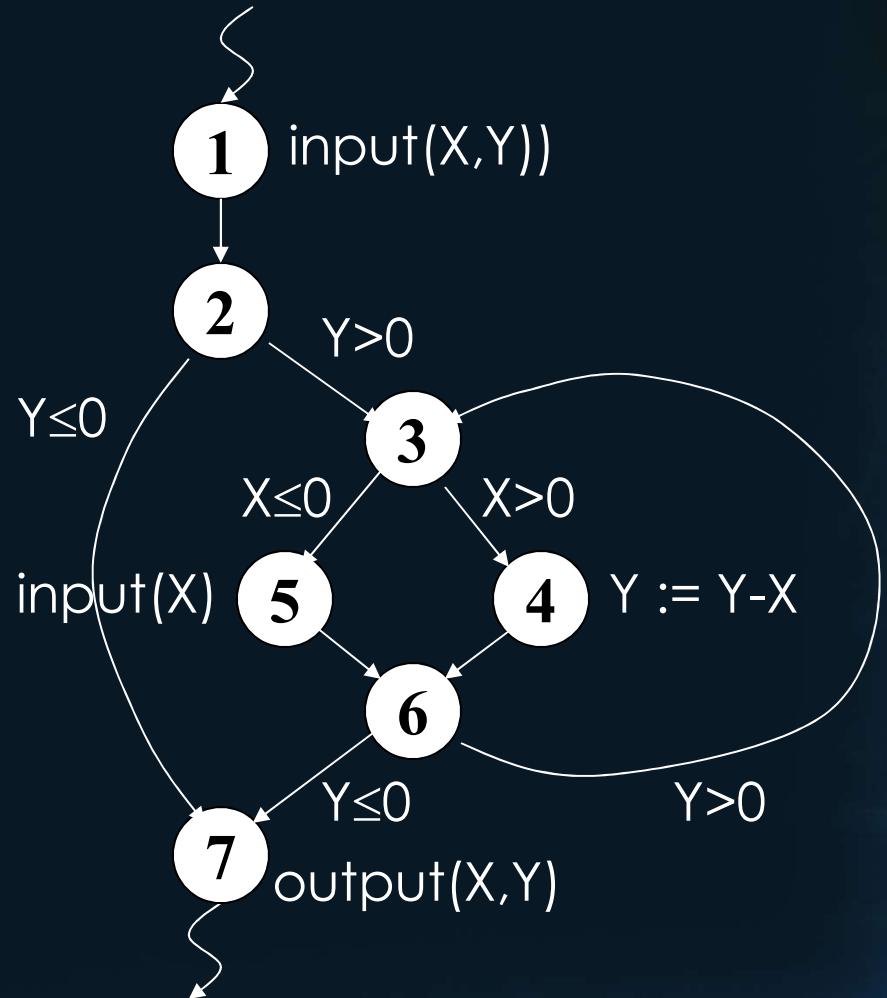
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(5,7)	<5,6,2,7>†
	<5,6,2,3,4,6,2,7>
	<5,6,2,3,4,6,(2,3,4,6)*,2,7>
(5,<3,4>)	<5,6,2,3,4>
	<5,6,2,3,4,(6,2,3,4)*>
(5,<3,5>)	<5,6,2,3,5>
	<5,6,2,3,4,6,2,3,5>†
	<5,6,2,3,4,6,(2,3,4,6)*,2,3,5> †
† infeasible	



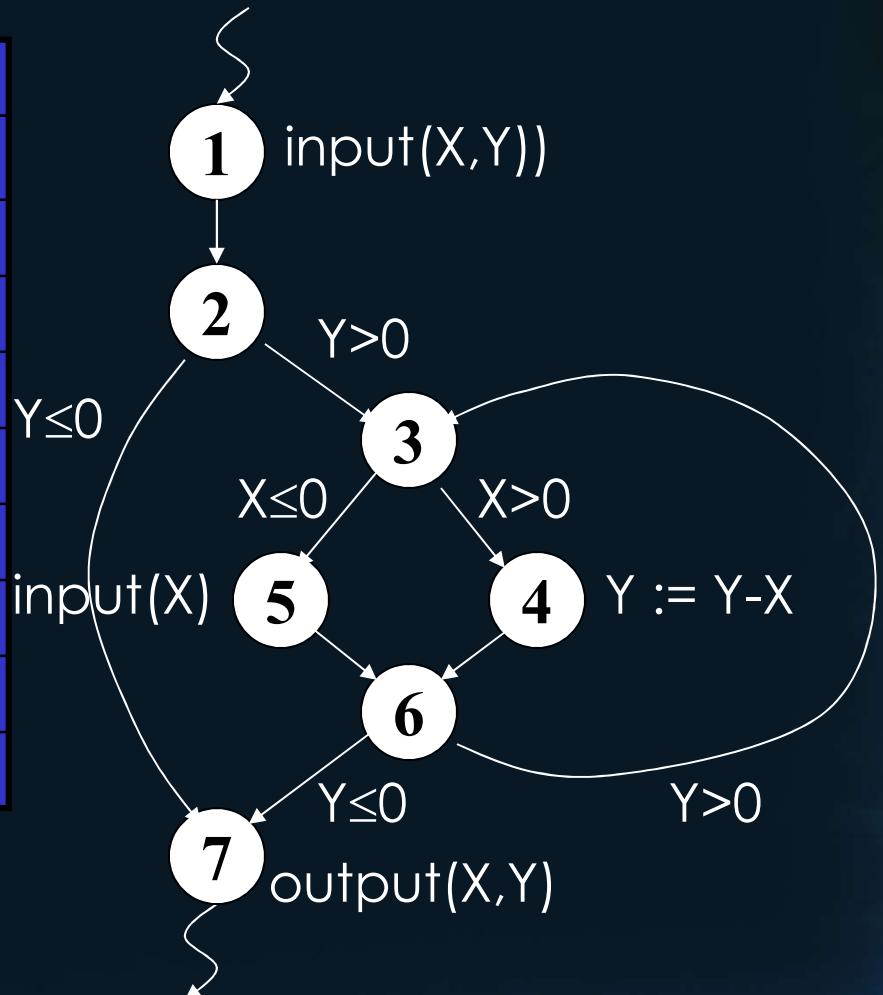
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(1,4)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,7)	<1,2,7>
	<1,2,3,4,6,7>
	<1,2,3,4,6,(3,4,6)*,7>
(1,<3,4>)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,<3,5>)	<1,2,3,5>
(5,4)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>



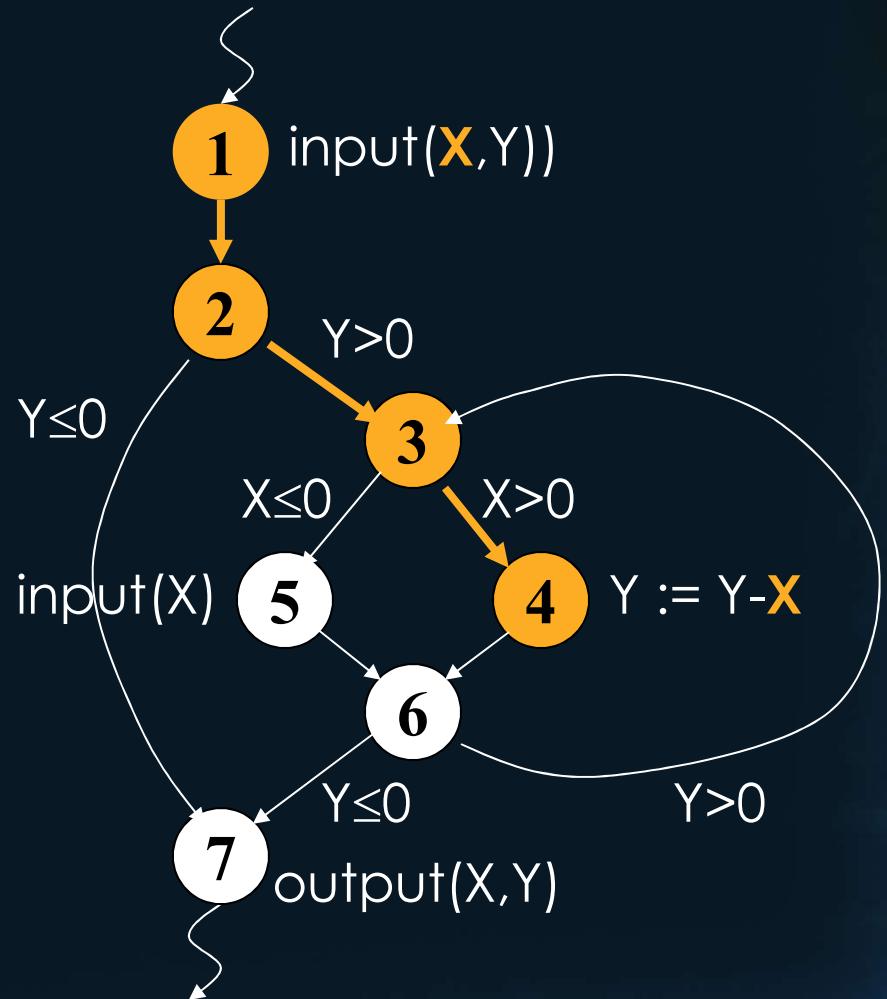
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(5,7)	<5,6,7>†
	<5,6,3,4,6,7>
	<5,6,3,4,6,(3,4,6)*,7>
(5,<3,4>)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>
(5,<3,5>)	<5,6,3,5>
	<5,6,3,4,6,3,5>†
	<5,6,3,4,6,(3,4,6)*,3,5>†
† infeasible	



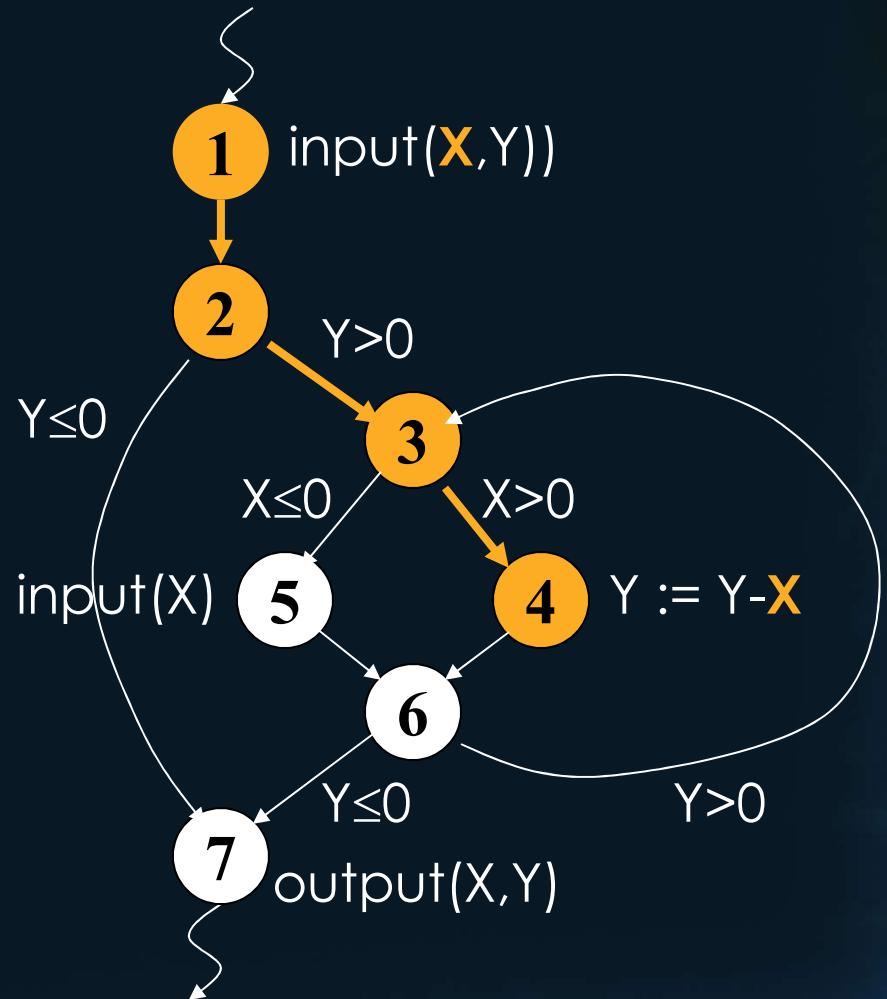
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(1,4)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,7)	<1,2,7>
	<1,2,3,4,6,7>
	<1,2,3,4,6,(3,4,6)*,7>
(1,<3,4>)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,<3,5>)	<1,2,3,5>
(5,4)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>



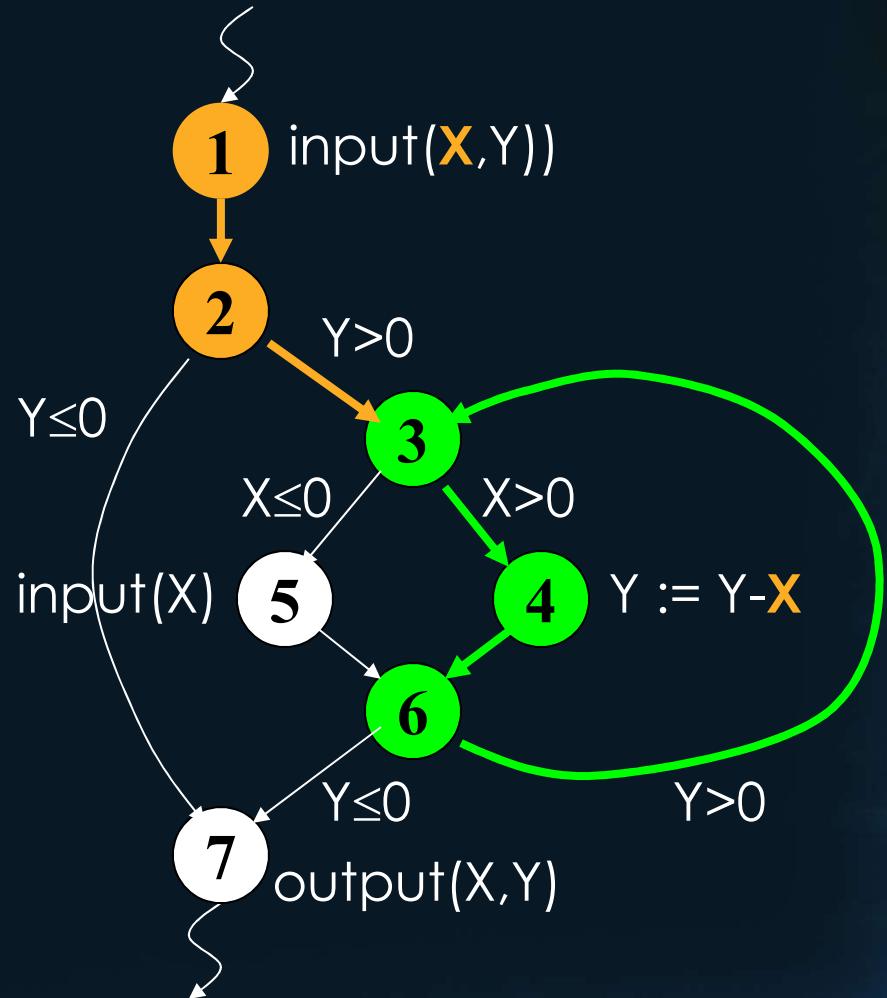
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(1,4)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,7)	<1,2,7>
	<1,2,3,4,6,7>
	<1,2,3,4,6,(3,4,6)*,7>
(1,<3,4>)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,<3,5>)	<1,2,3,5>
(5,4)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>



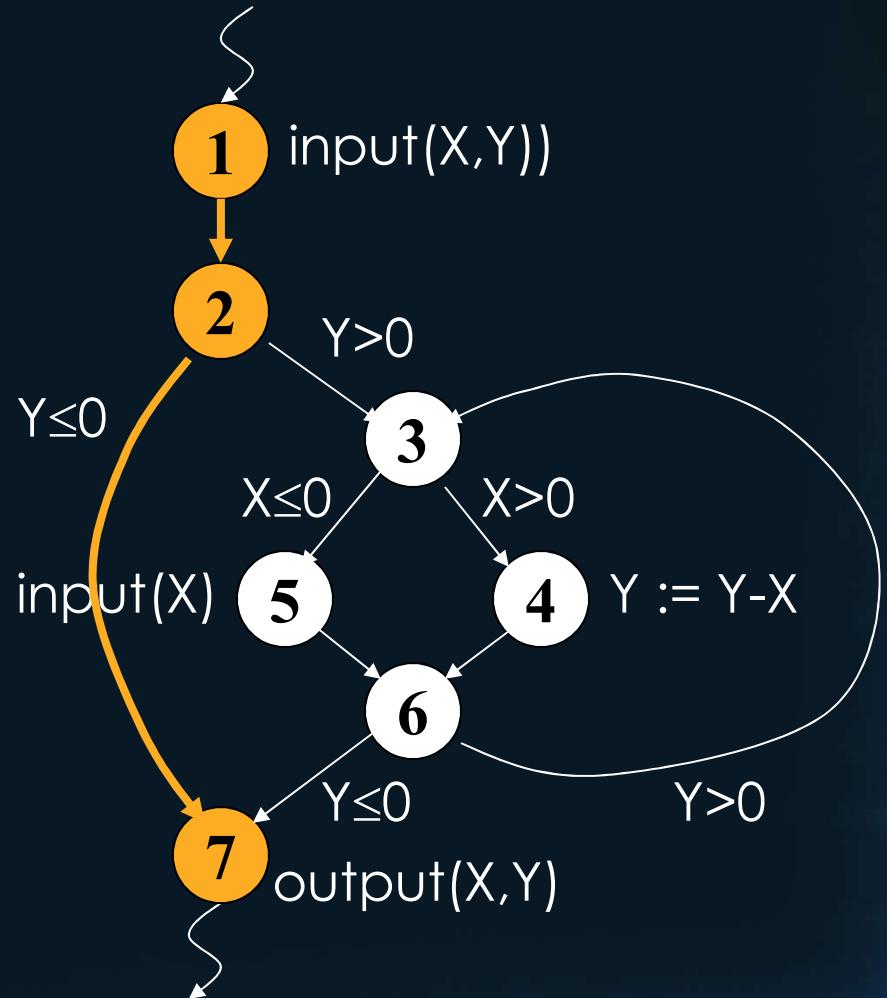
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(1,4)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,7)	<1,2,7>
	<1,2,3,4,6,7>
	<1,2,3,4,6,(3,4,6)*,7>
(1,<3,4>)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,<3,5>)	<1,2,3,5>
(5,4)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>



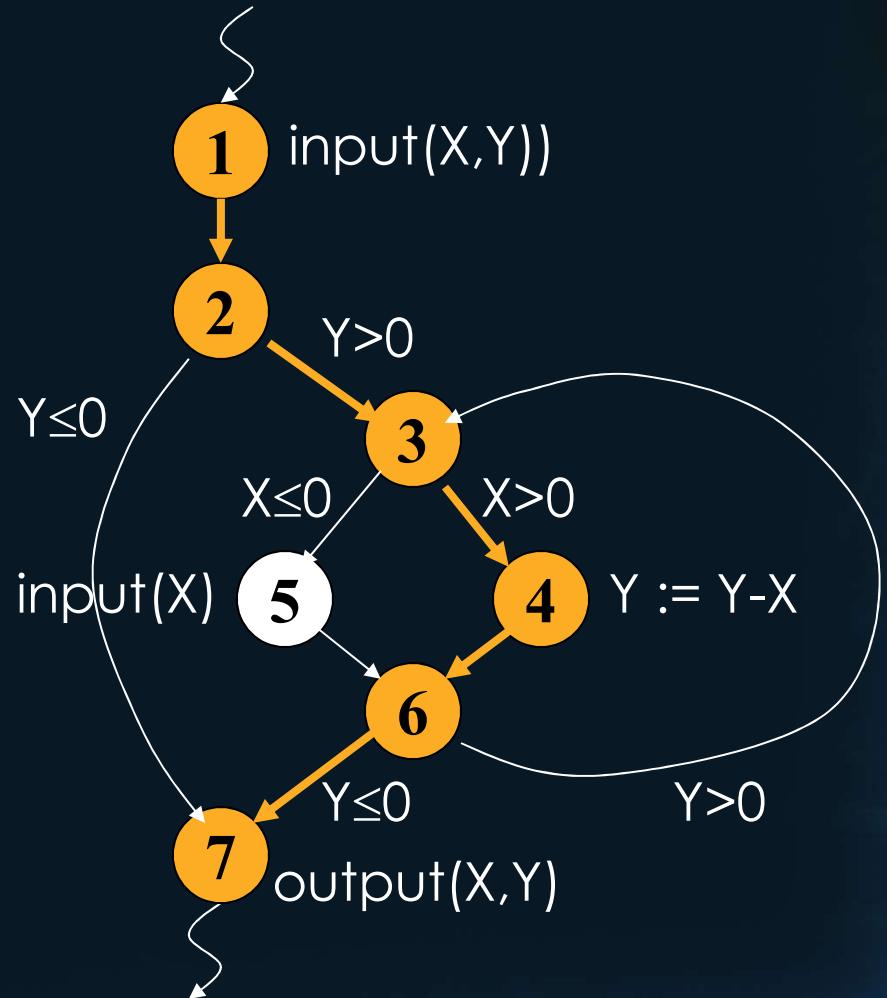
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(1,4)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
<b>(1,7)</b>	<b>&lt;1,2,7&gt;</b>
	<1,2,3,4,6,7>
	<1,2,3,4,6,(3,4,6)*,7>
(1,<3,4>)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,<3,5>)	<1,2,3,5>
(5,4)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>



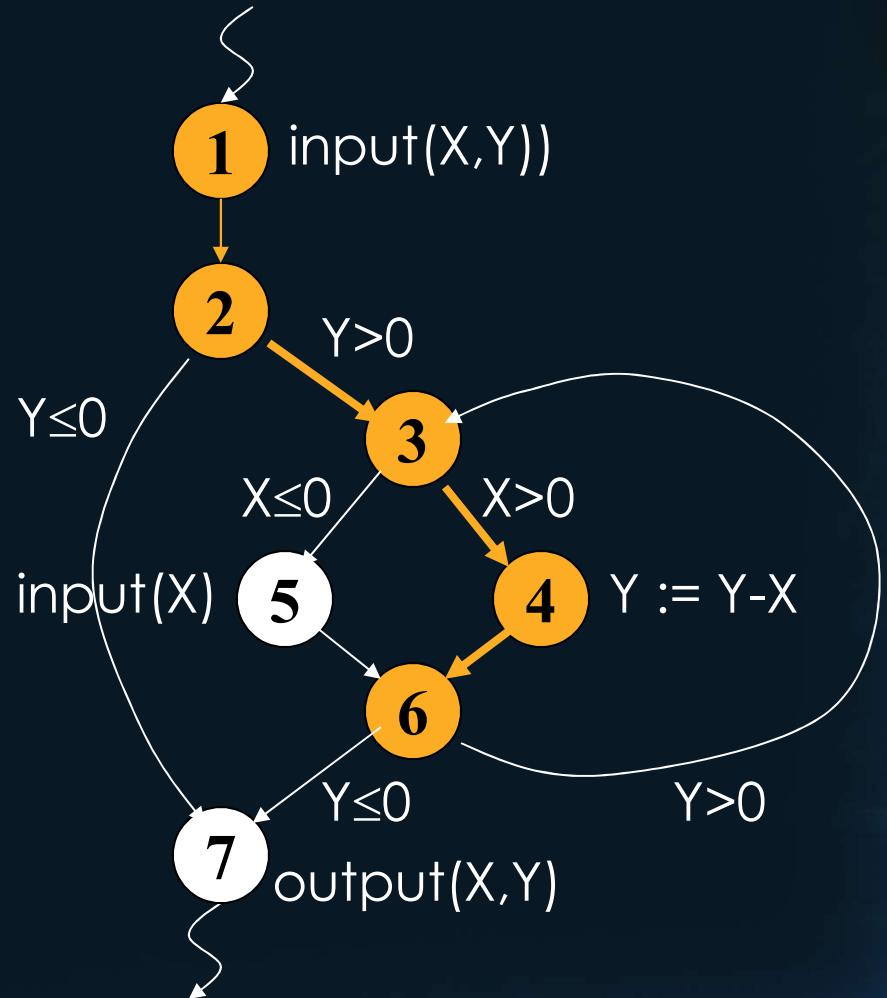
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(1,4)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
<b>(1,7)</b>	<1,2,7>
	<b>&lt;1,2,3,4,6,7&gt;</b>
	<1,2,3,4,6,(3,4,6)*,7>
(1,<3,4>)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,<3,5>)	<1,2,3,5>
(5,4)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>



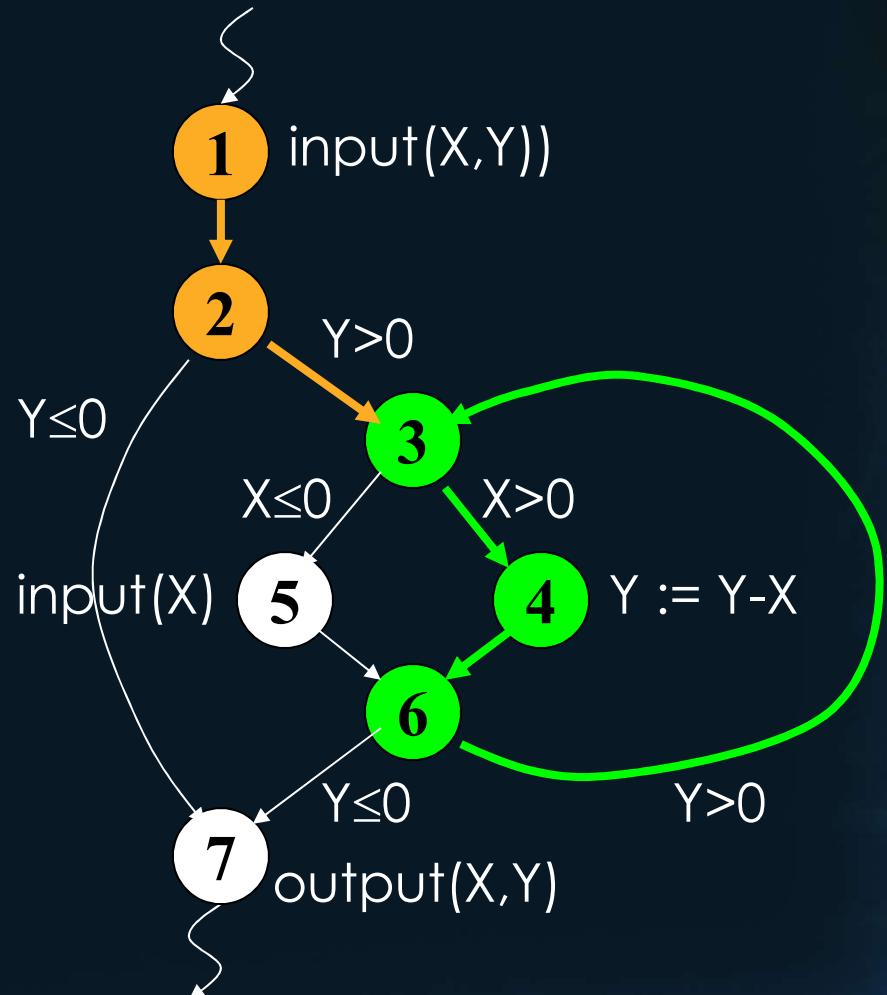
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(1,4)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
<b>(1,7)</b>	<1,2,7>
	<1,2,3,4,6,7>
	<b>&lt;1,2,3,4,6,(3,4,6)*,7&gt;</b>
(1,<3,4>)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,<3,5>)	<1,2,3,5>
(5,4)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>



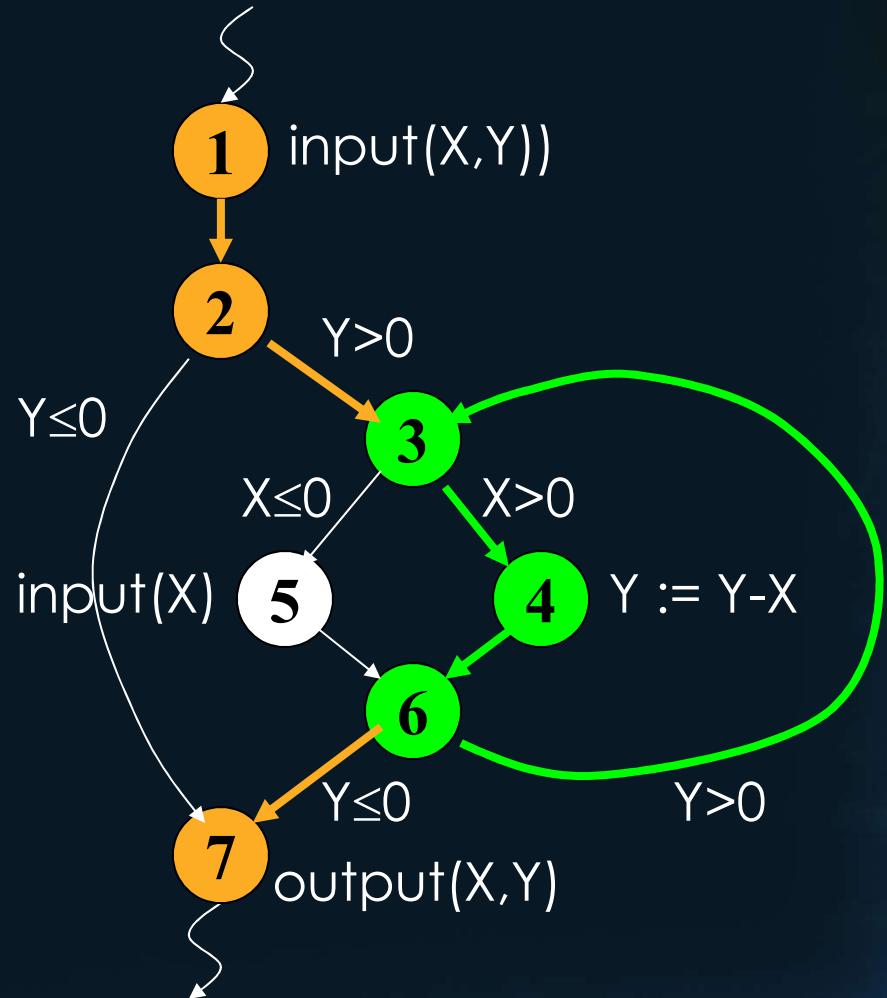
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(1,4)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
<b>(1,7)</b>	<1,2,7>
	<1,2,3,4,6,7>
	<b>&lt;1,2,3,4,6,(3,4,6)*,7&gt;</b>
(1,<3,4>)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,<3,5>)	<1,2,3,5>
(5,4)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>



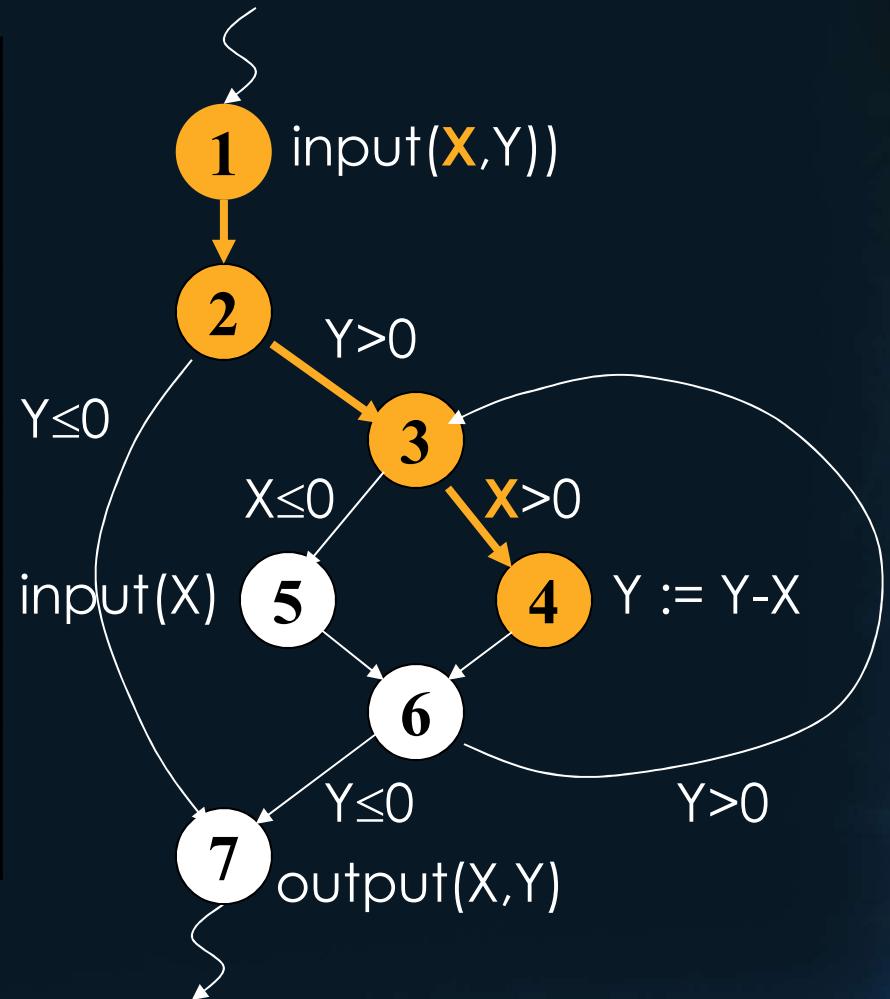
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(1,4)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
<b>(1,7)</b>	<1,2,7>
	<1,2,3,4,6,7>
	<b>&lt;1,2,3,4,6,(3,4,6)*,7&gt;</b>
(1,<3,4>)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,<3,5>)	<1,2,3,5>
(5,4)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>



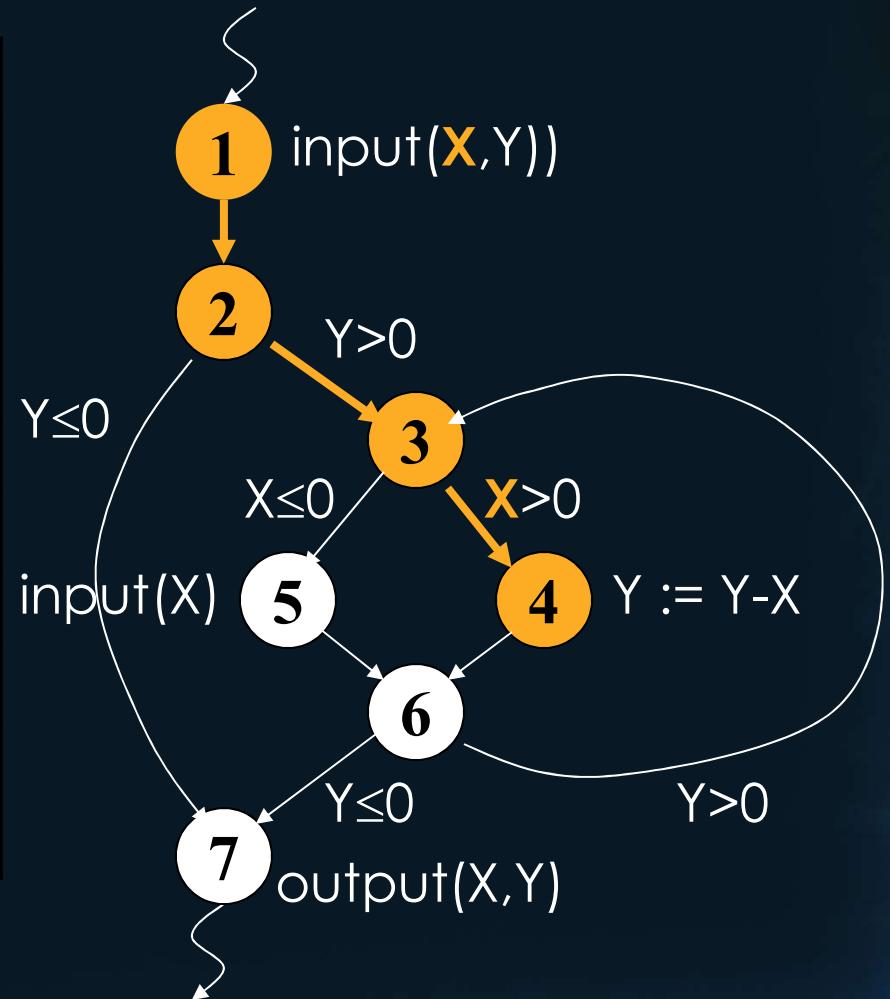
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(1,4)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,7)	<1,2,7>
	<1,2,3,4,6,7>
	<1,2,3,4,6,(3,4,6)*,7>
<b>(1,&lt;3,4&gt;)</b>	<b>&lt;1,2,3,4&gt;</b>
	<1,2,3,4,(6,3,4)*>
(1,<3,5>)	<1,2,3,5>
(5,4)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>



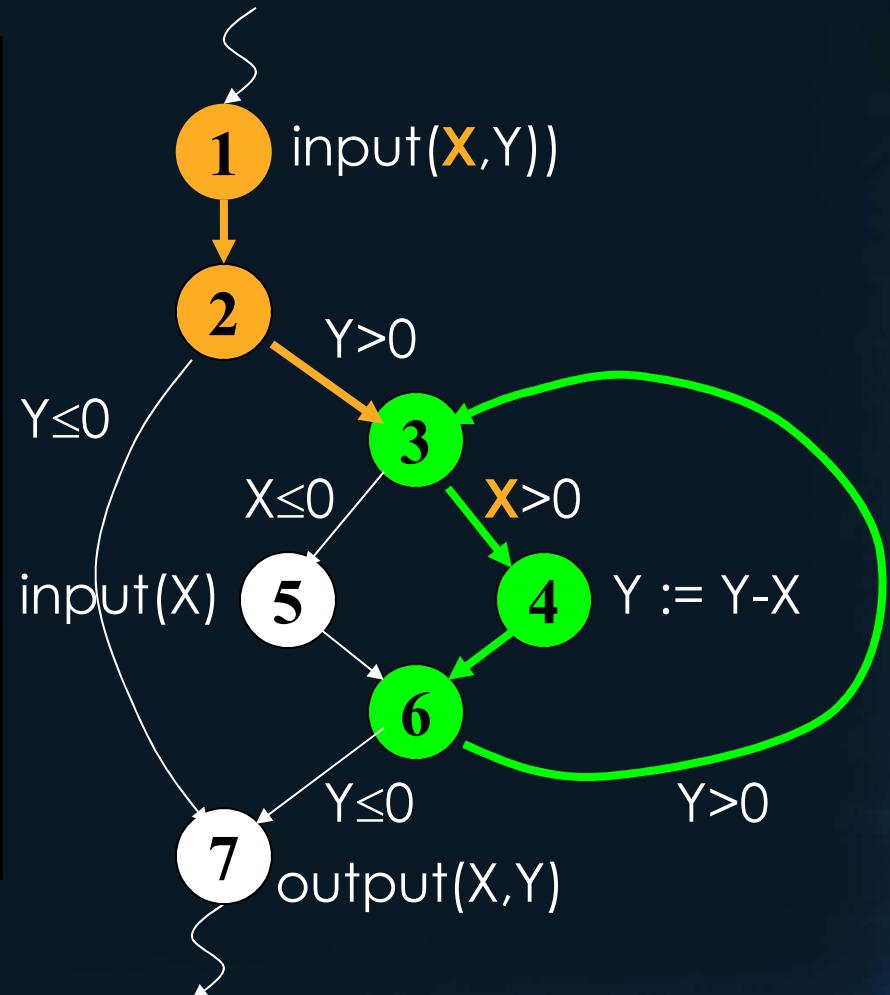
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(1,4)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,7)	<1,2,7>
	<1,2,3,4,6,7>
	<1,2,3,4,6,(3,4,6)*,7>
(1,<3,4>)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,<3,5>)	<1,2,3,5>
(5,4)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>



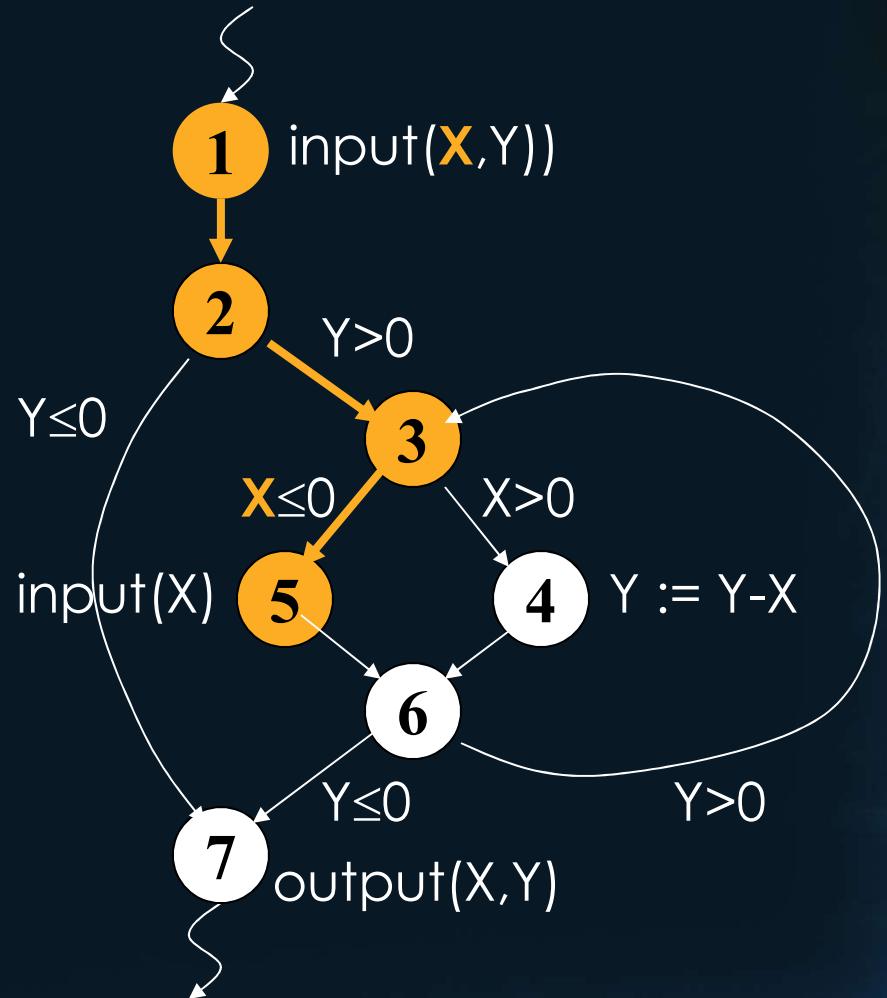
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(1,4)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,7)	<1,2,7>
	<1,2,3,4,6,7>
	<1,2,3,4,6,(3,4,6)*,7>
(1,<3,4>)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,<3,5>)	<1,2,3,5>
(5,4)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>



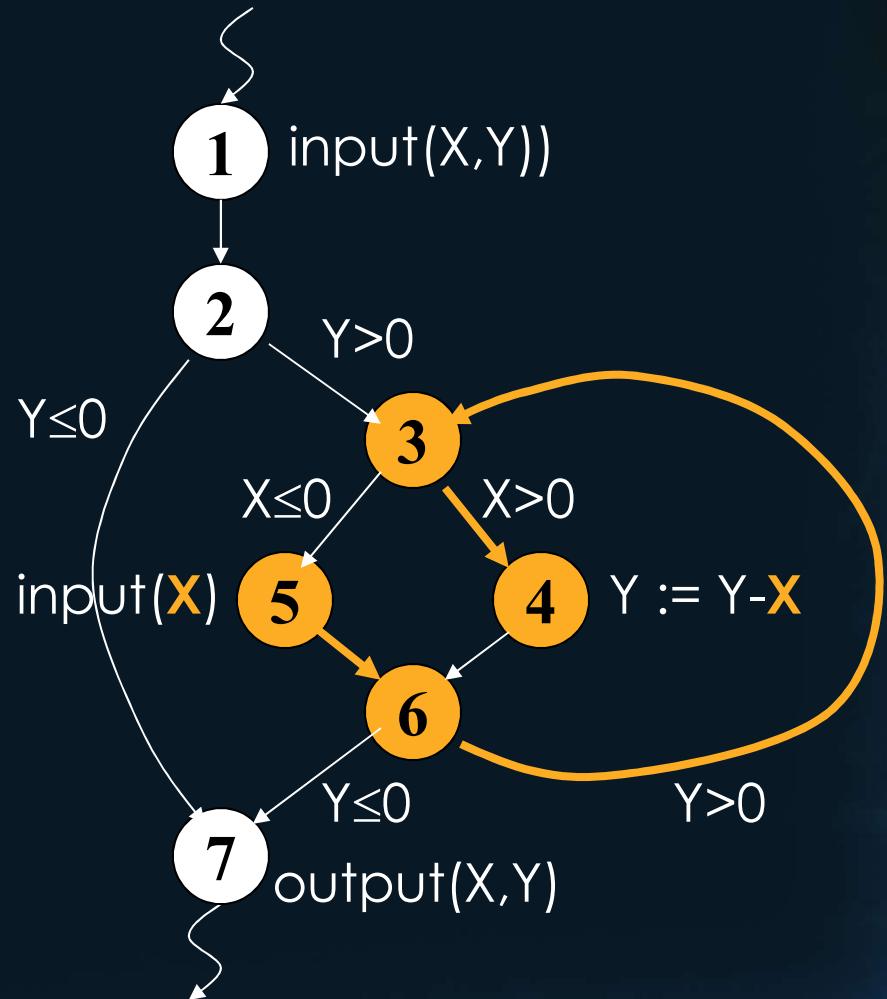
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(1,4)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,7)	<1,2,7>
	<1,2,3,4,6,7>
	<1,2,3,4,6,(3,4,6)*,7>
(1,<3,4>)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
<b>(1,&lt;3,5&gt;)</b>	<b>&lt;1,2,3,5&gt;</b>
(5,4)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>



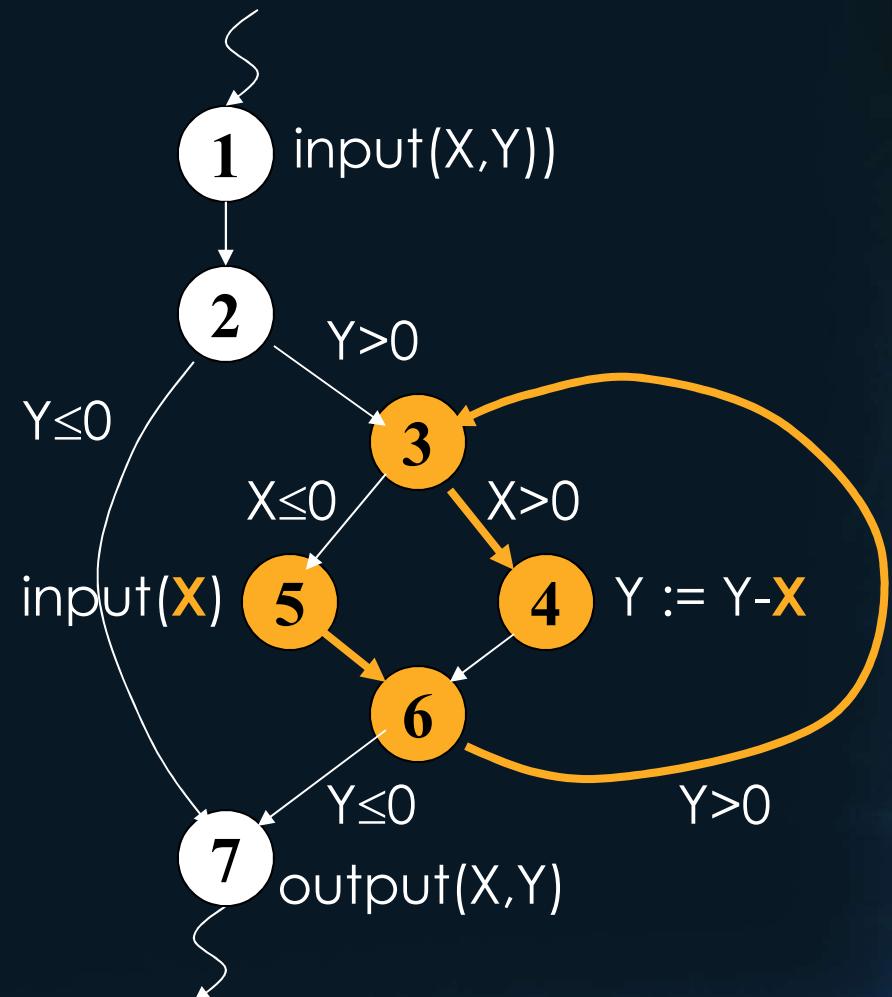
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(1,4)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,7)	<1,2,7>
	<1,2,3,4,6,7>
	<1,2,3,4,6,(3,4,6)*,7>
(1,<3,4>)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,<3,5>)	<1,2,3,5>
<b>(5,4)</b>	<b>&lt;5,6,3,4&gt;</b>
	<5,6,3,4,(6,3,4)*>



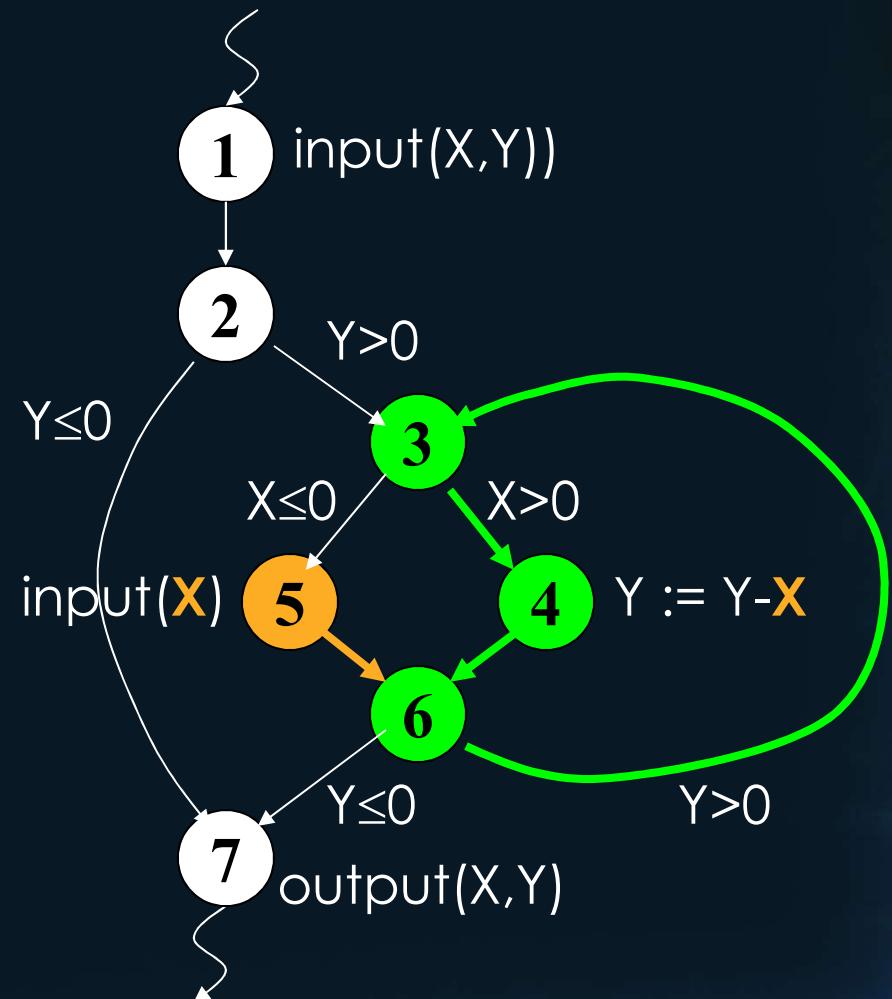
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(1,4)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,7)	<1,2,7>
	<1,2,3,4,6,7>
	<1,2,3,4,6,(3,4,6)*,7>
(1,<3,4>)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,<3,5>)	<1,2,3,5>
<b>(5,4)</b>	<5,6,3,4>
	<b>&lt;5,6,3,4,(6,3,4)*&gt;</b>



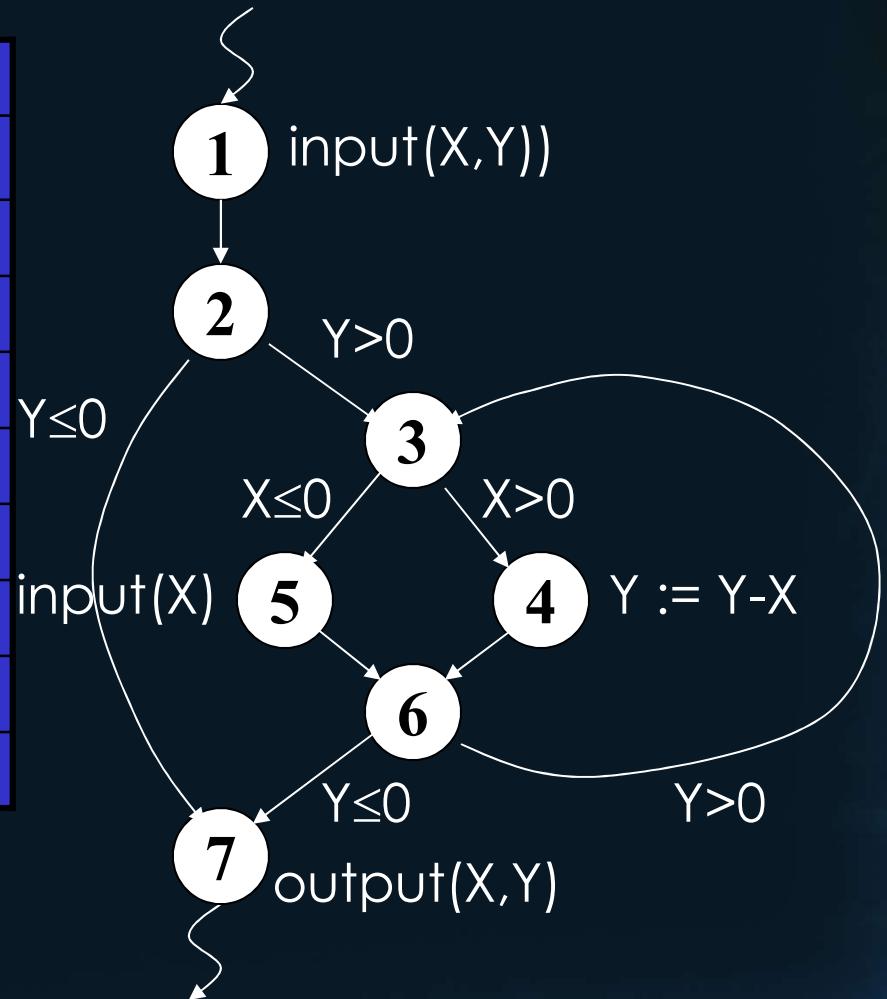
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(1,4)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,7)	<1,2,7>
	<1,2,3,4,6,7>
	<1,2,3,4,6,(3,4,6)*,7>
(1,<3,4>)	<1,2,3,4>
	<1,2,3,4,(6,3,4)*>
(1,<3,5>)	<1,2,3,5>
<b>(5,4)</b>	<5,6,3,4>
	<b>&lt;5,6,3,4,(6,3,4)*&gt;</b>



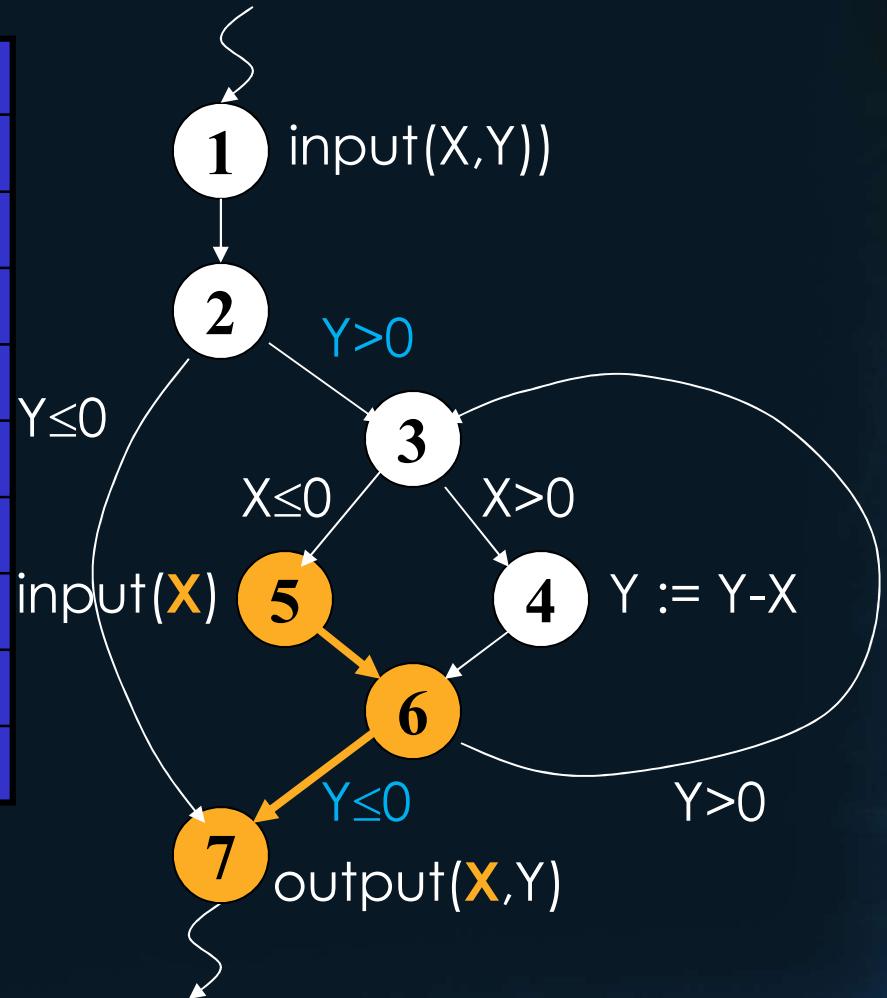
# Identifying DU-Pairs – Variable X

<b><u>du-pair</u></b>	<b><u>path(s)</u></b>
(5,7)	<5,6,7>
	<5,6,3,4,6,7>
	<5,6,3,4,6,(3,4,6)*,7>
(5,<3,4>)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>
(5,<3,5>)	<5,6,3,5>
	<5,6,3,4,6,3,5>
	<5,6,3,4,6,(3,4,6)*,3,5>



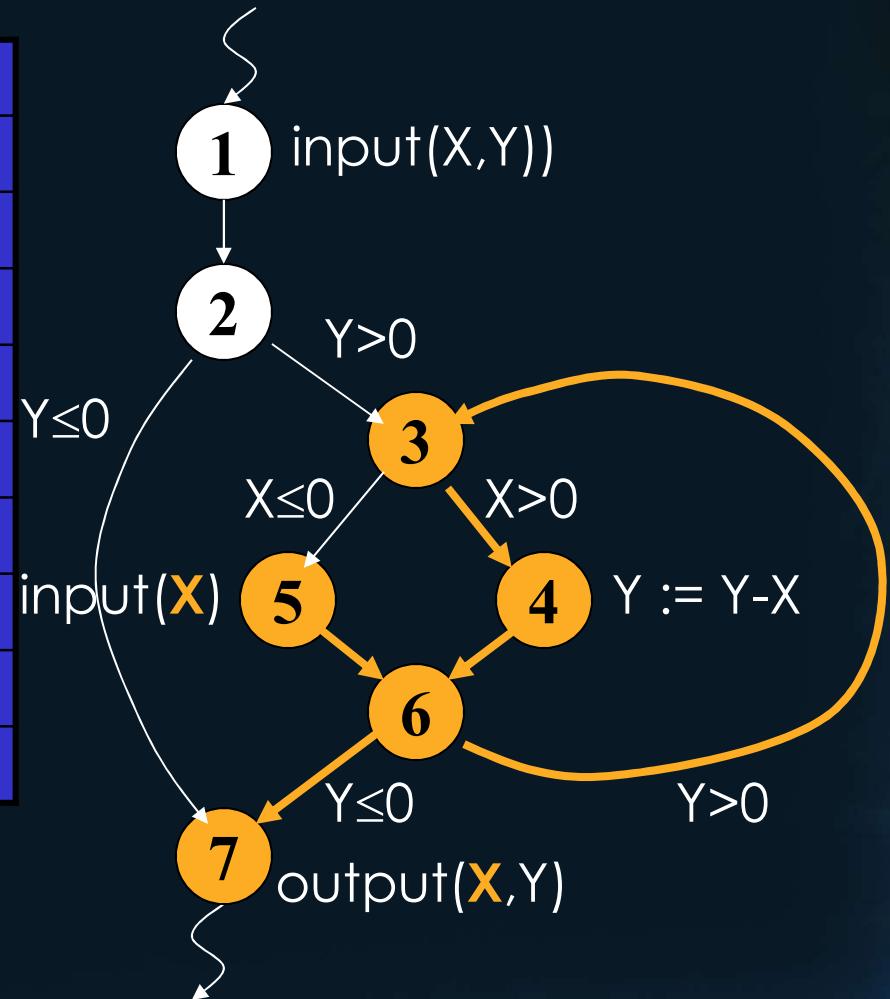
# Identifying DU-Pairs – Variable X

<u>du-pair</u>	<u>path(s)</u>
(5,7)	<5,6,7> † <5,6,3,4,6,7> <5,6,3,4,6,(3,4,6)*,7>
(5,<3,4>)	<5,6,3,4> <5,6,3,4,(6,3,4)*>
(5,<3,5>)	<5,6,3,5> <5,6,3,4,6,3,5> <5,6,3,4,6,(3,4,6)*,3,5>
† infeasible	



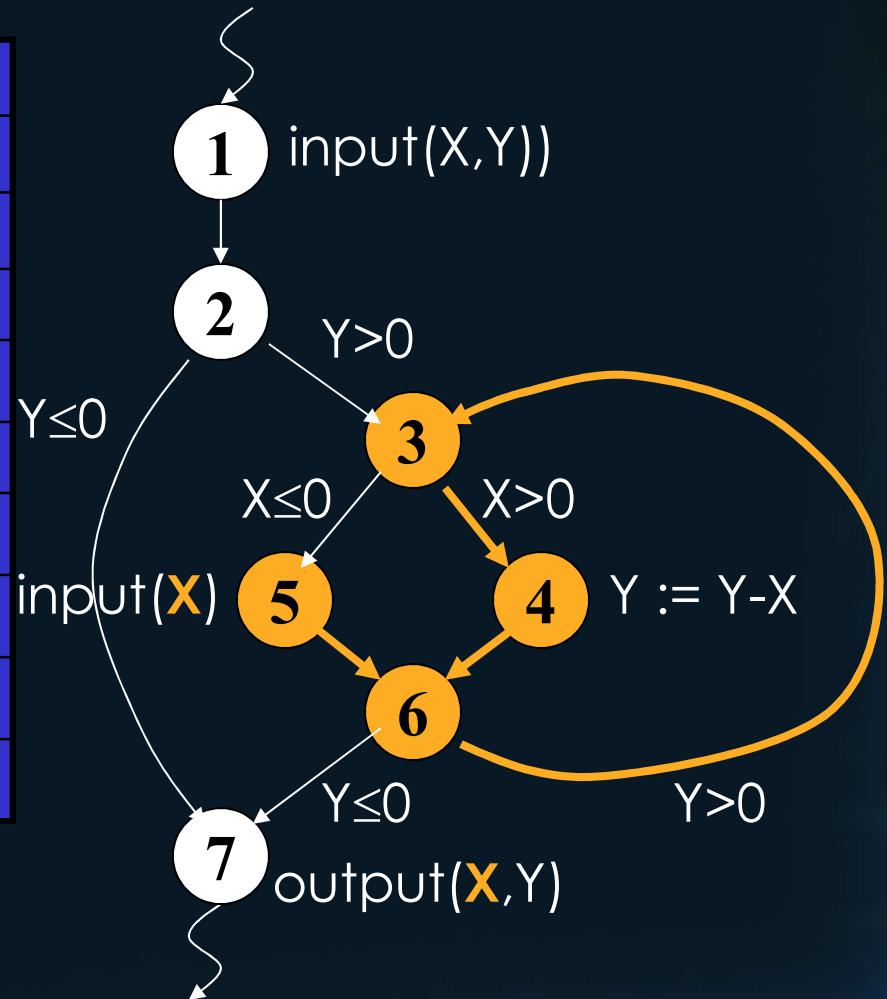
# Identifying DU-Pairs – Variable X

<u>du-pair</u>	<u>path(s)</u>
(5,7)	<5,6,7> †
	<5,6,3,4,6,7>
	<5,6,3,4,6,(3,4,6)*,7>
(5,<3,4>)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>
(5,<3,5>)	<5,6,3,5>
	<5,6,3,4,6,3,5>
	<5,6,3,4,6,(3,4,6)*,3,5>
† infeasible	



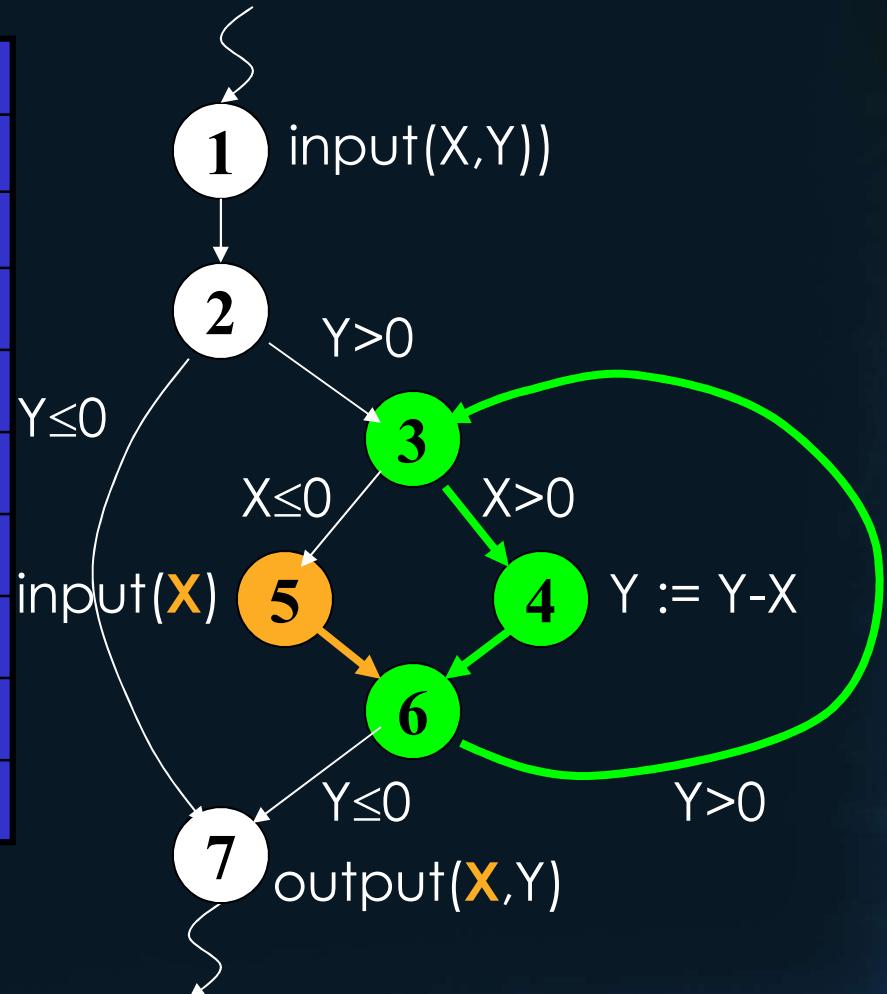
# Identifying DU-Pairs – Variable X

<u>du-pair</u>	<u>path(s)</u>
(5,7)	<5,6,7> † <5,6,3,4,6,7> <b>&lt;5,6,3,4,6,(3,4,6)*,7&gt;</b>
(5,<3,4>)	<5,6,3,4> <5,6,3,4,(6,3,4)*>
(5,<3,5>)	<5,6,3,5> <5,6,3,4,6,3,5> <5,6,3,4,6,(3,4,6)*,3,5>
† infeasible	



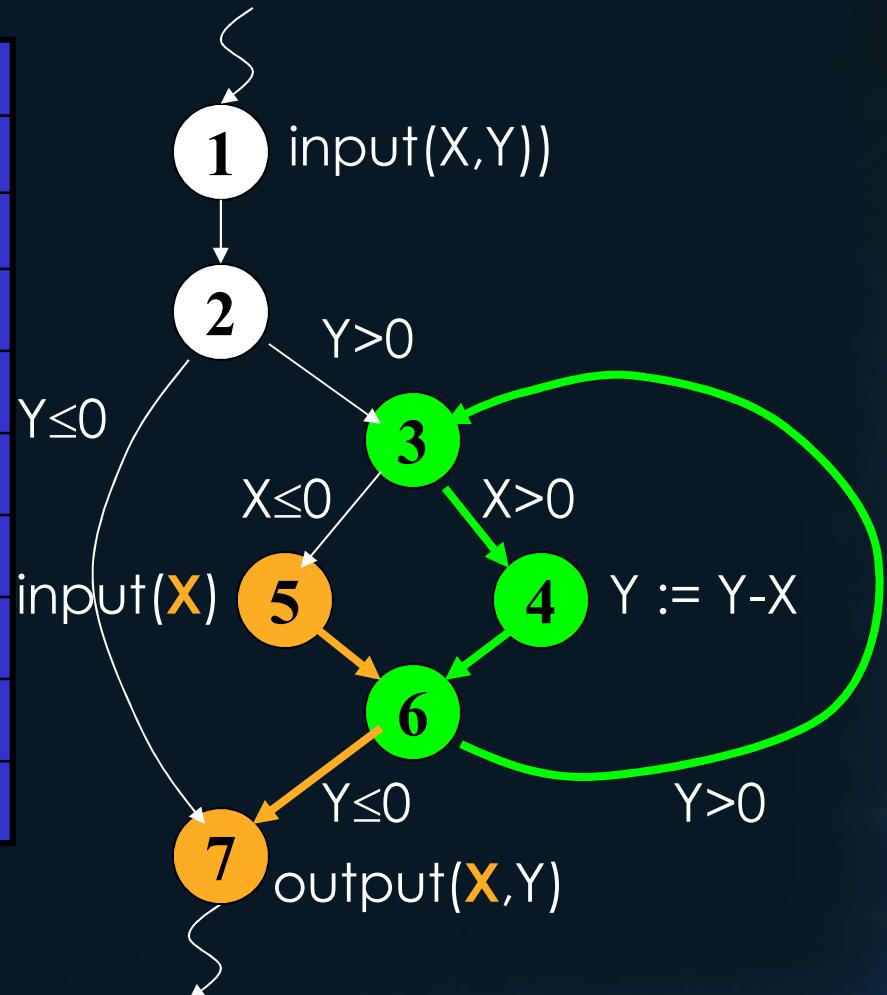
# Identifying DU-Pairs – Variable X

<u>du-pair</u>	<u>path(s)</u>
(5,7)	<5,6,7> † <5,6,3,4,6,7> <b>&lt;5,6,3,4,6,(3,4,6)*,7&gt;</b>
(5,<3,4>)	<5,6,3,4> <5,6,3,4,(6,3,4)*>
(5,<3,5>)	<5,6,3,5> <5,6,3,4,6,3,5> <5,6,3,4,6,(3,4,6)*,3,5>
† infeasible	



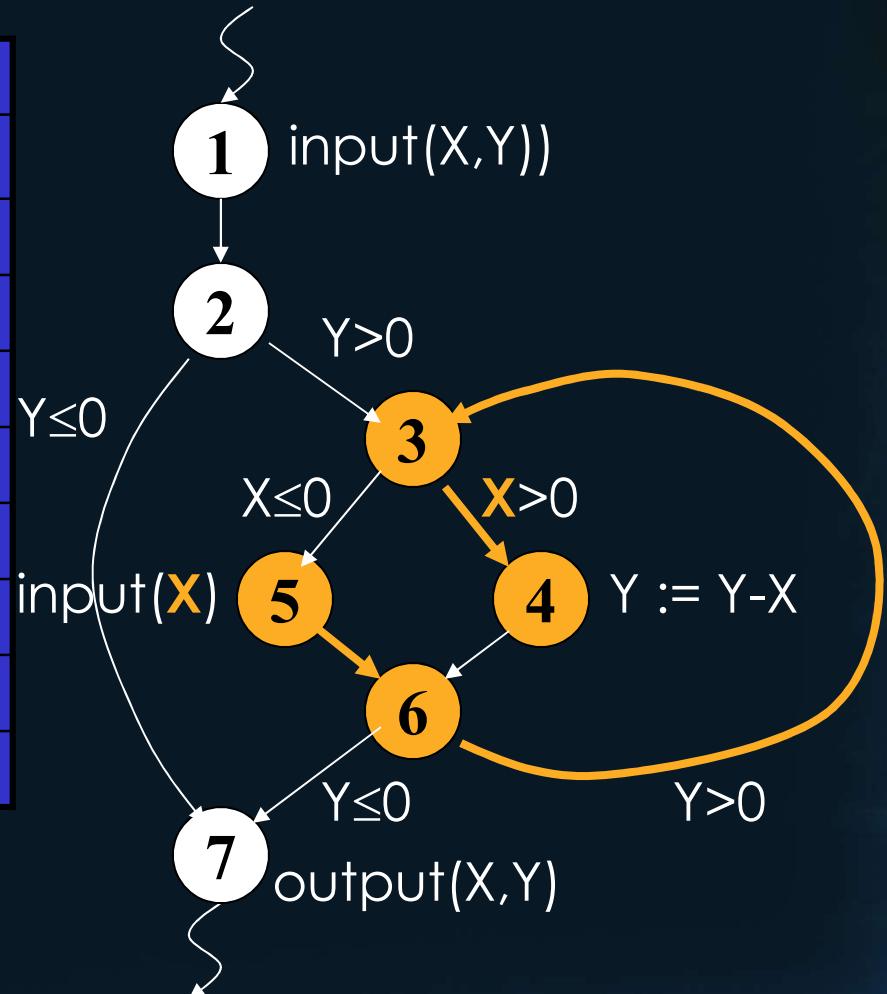
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(5,7)	<5,6,7> † <5,6,3,4,6,7> <b>&lt;5,6,3,4,6,(3,4,6)*,7&gt;</b>
(5,<3,4>)	<5,6,3,4> <5,6,3,4,(6,3,4)*>
(5,<3,5>)	<5,6,3,5> <5,6,3,4,6,3,5> <5,6,3,4,6,(3,4,6)*,3,5>
† infeasible	



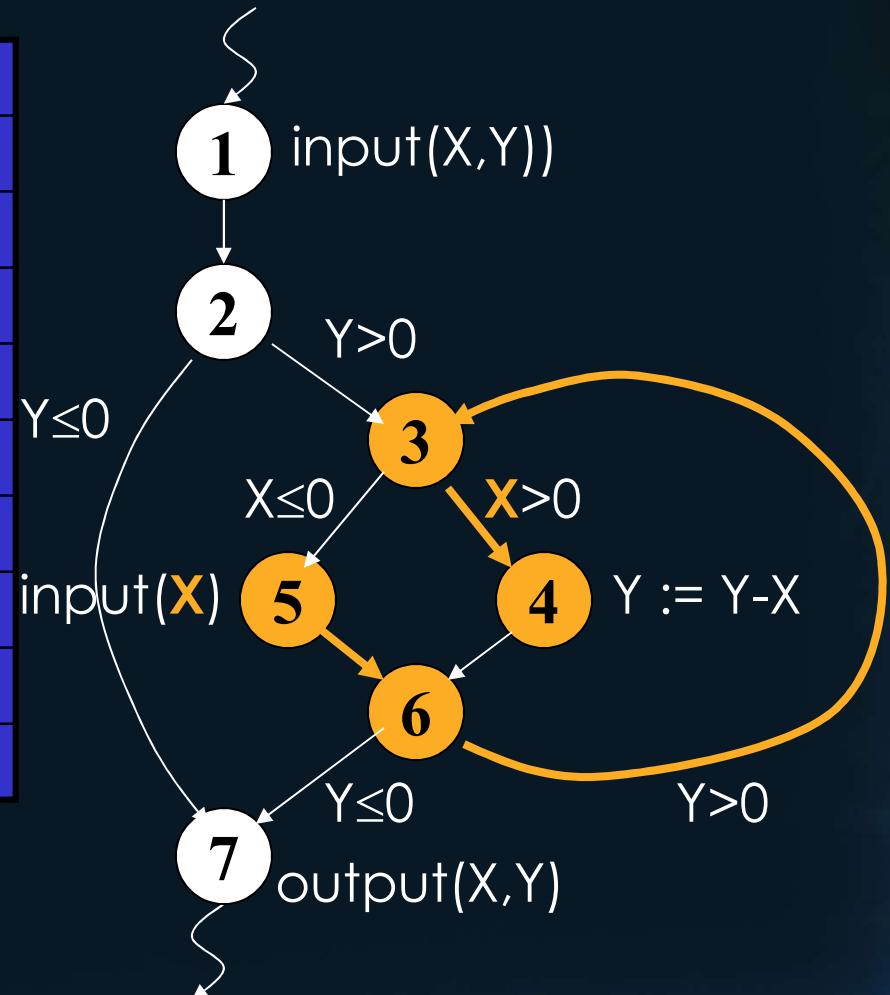
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(5,7)	<5,6,7> †
	<5,6,3,4,6,7>
	<5,6,3,4,6,(3,4,6)*,7>
(5,<3,4>)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>
(5,<3,5>)	<5,6,3,5>
	<5,6,3,4,6,3,5>
	<5,6,3,4,6,(3,4,6)*,3,5>
† infeasible	



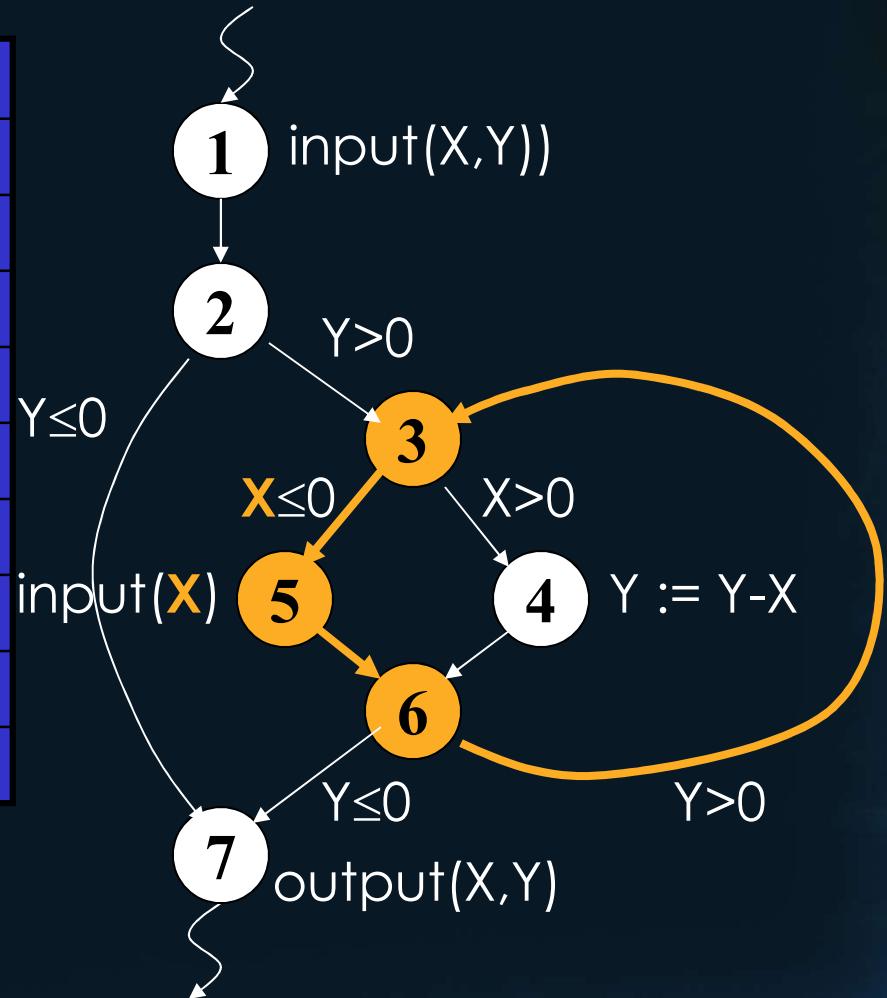
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(5,7)	<5,6,7> †
	<5,6,3,4,6,7>
	<5,6,3,4,6,(3,4,6)*7>
(5,<3,4>)	<5,6,3,4>
	<5,6,3,4,(6,3,4)*>
(5,<3,5>)	<5,6,3,5>
	<5,6,3,4,6,3,5>
	<5,6,3,4,6,(3,4,6)*,3,5>
† infeasible	



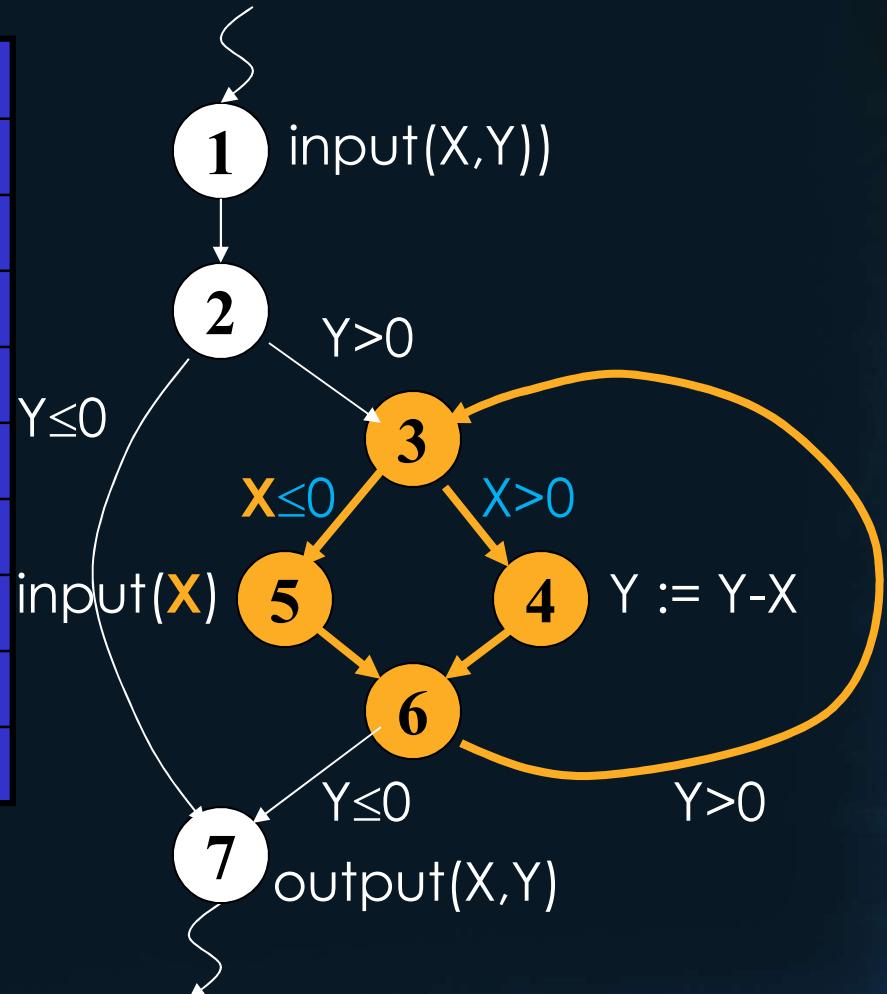
# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(5,7)	<5,6,7> † <5,6,3,4,6,7> <5,6,3,4,6,(3,4,6)*7>
(5,<3,4>)	<5,6,3,4> <5,6,3,4,(6,3,4)*>
(5,<3,5>)	<b>&lt;5,6,3,5&gt;</b> <5,6,3,4,6,3,5> <5,6,3,4,6,(3,4,6)*,3,5>
† infeasible	



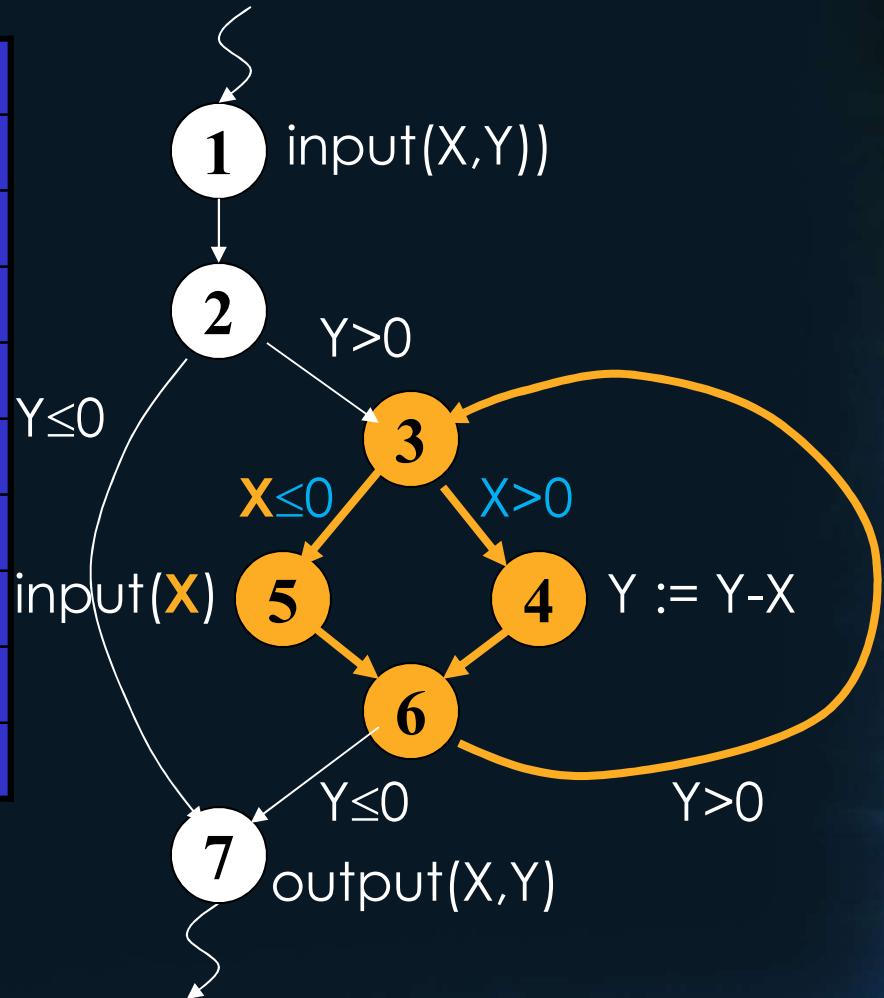
# Identifying DU-Pairs – Variable X

<u>du-pair</u>	<u>path(s)</u>
(5,7)	<5,6,7> † <5,6,3,4,6,7> <5,6,3,4,6,(3,4,6)*7>
(5,<3,4>)	<5,6,3,4> <5,6,3,4,(6,3,4)*>
(5,<3,5>)	<5,6,3,5> <b>&lt;5,6,3,4,6,3,5&gt; †</b> <5,6,3,4,6,(3,4,6)*,3,5>
<b>† infeasible</b>	



# Identifying DU-Pairs – Variable X

<b>du-pair</b>	<b>path(s)</b>
(5,7)	<5,6,7> † <5,6,3,4,6,7> <5,6,3,4,6,(3,4,6)*7>
(5,<3,4>)	<5,6,3,4> <5,6,3,4,(6,3,4)*>
(5,<3,5>)	<5,6,3,5> <5,6,3,4,6,3,5> † <5,6,3,4,6,(3,4,6)*,3,5> †
† <b>infeasible</b>	



# More Dataflow Terms and Definitions

- A path (either partial or complete) is **simple** if all edges within the path are distinct (i.e., different).
- A path is **loop-free** if all nodes within the path are distinct (i.e., different).

# Simple and Loop-Free Paths

path	Simple?	Loop-free?
<1,3,4,2>	Yes	Yes
<1,2,3,2>	Yes	No
<1,2,3,1,2>	No	No
<1,2,3,2,4>	Yes	No

## Simple and Loop-Free Paths (cont'd)

Which is *stronger*, **simple** or **loop-free**?

环路为1

无环路

# More Dataflow Terms and Definitions

A path  $\langle n_1, n_2, \dots, n_j, n_k \rangle$  is a **du-path** with respect to a variable  $v$  if  $v$  is defined at node  $n_1$  and either:

1. there is a **c-use** of  $v$  at node  $n_k$  and  $\langle n_1, n_2, \dots, n_j, n_k \rangle$  is a def-clear **simple** path,

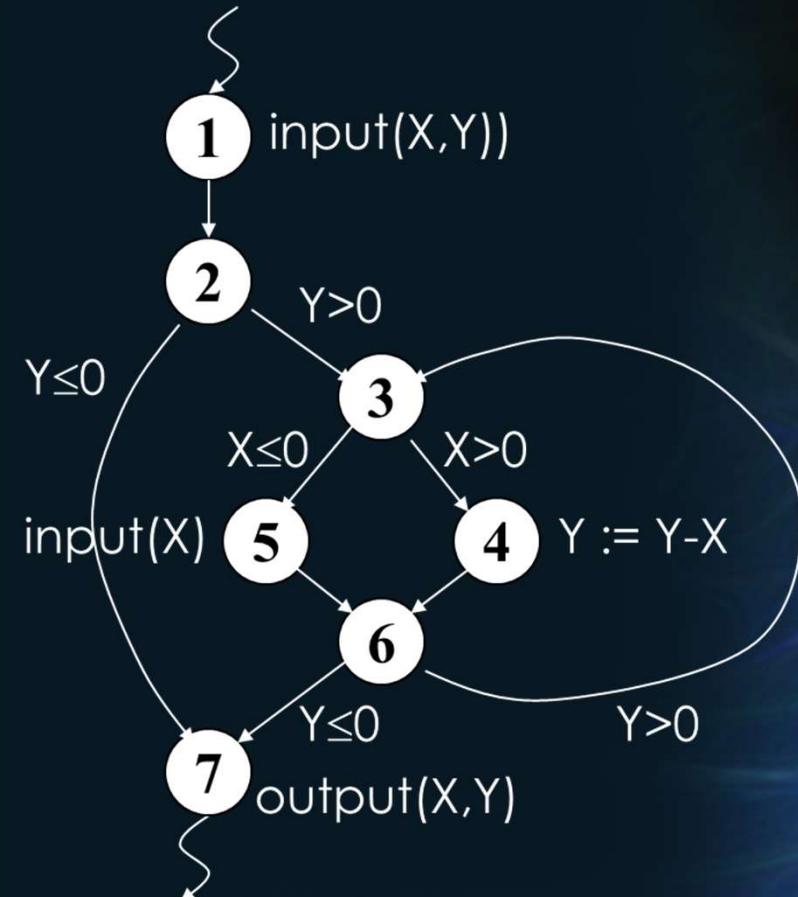
or

1. there is a **p-use** of  $v$  at edge  $\langle n_j, n_k \rangle$  and  $\langle n_1, n_2, \dots, n_j \rangle$  is a def-clear **loop-free** path.

NOTE!

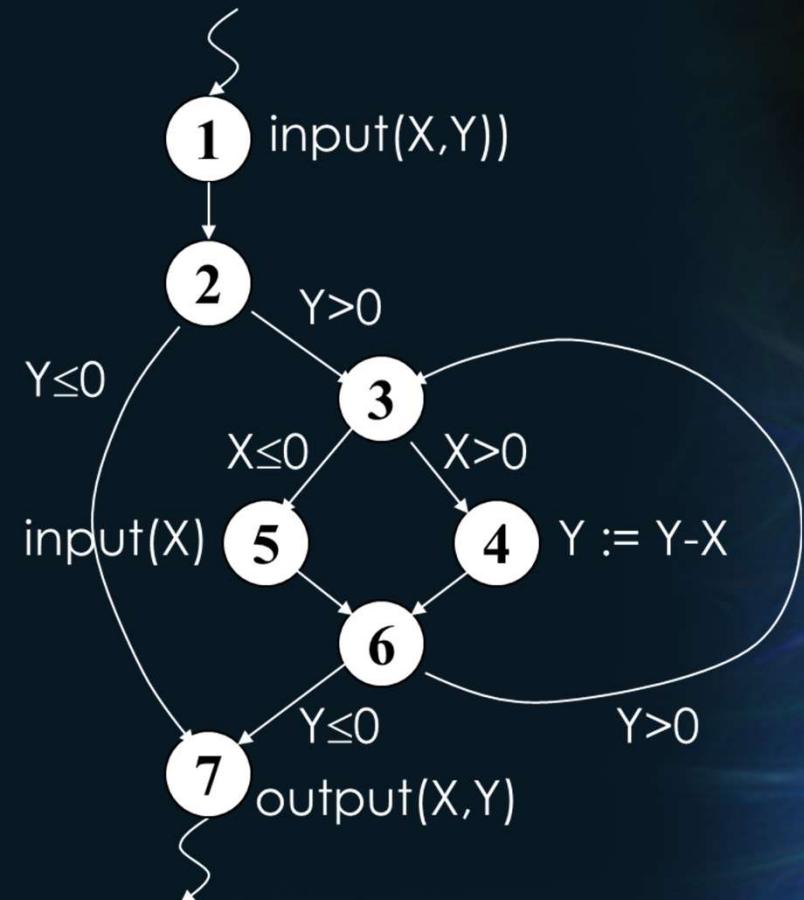
# Identifying du-paths

<u>du-pair</u>	<u>path(s)</u>	<u>du-path?</u>
X: (1,4)	<1,2,3,4>	Yes
	<1,2,3,4,(6,3,4)*>	No
X: (1,7)	<1,2,7>	Yes
	<1,2,3,4,6,7>	Yes
	<1,2,3,4,6,(3,4,6)*,7>	No
X: (1,<3,4>)	<1,2,3,4>	Yes
	<1,2,3,4,(6,3,4)*>	No
X: (1,<3,5>)	<1,2,3,5>	Yes
X: (5,4)	<5,6,3,4>	Yes
p-use	<5,6,3,4,(6,3,4)*>	No



# Identifying du-paths

<u>du-pair</u>	<u>path(s)</u>	<u>du-path?</u>
X: (5,7)	<5,6,7> †	Yes
	<5,6,3,4,6,7>	Yes
	<5,6,3,4,6,(3,4,6)*,7>	No
X: (5,<3,4>)	<5,6,3,4>	Yes
	<5,6,3,4,(6,3,4)*>	No
X: (5,<3,5>)	<5,6,3,5>	Yes
	<5,6,3,4,6,3,5> †	No
	<5,6,3,4,6,(3,4,6)*,3,5> †	No
† infeasible		



s1

suda, 2022/10/5

# Another Dataflow Test Coverage Criterion

- **All-DU-Paths:** for **every program variable v**, **every du-path** from **every definition** of v to **every c-use** and **every p-use** of v must be covered.

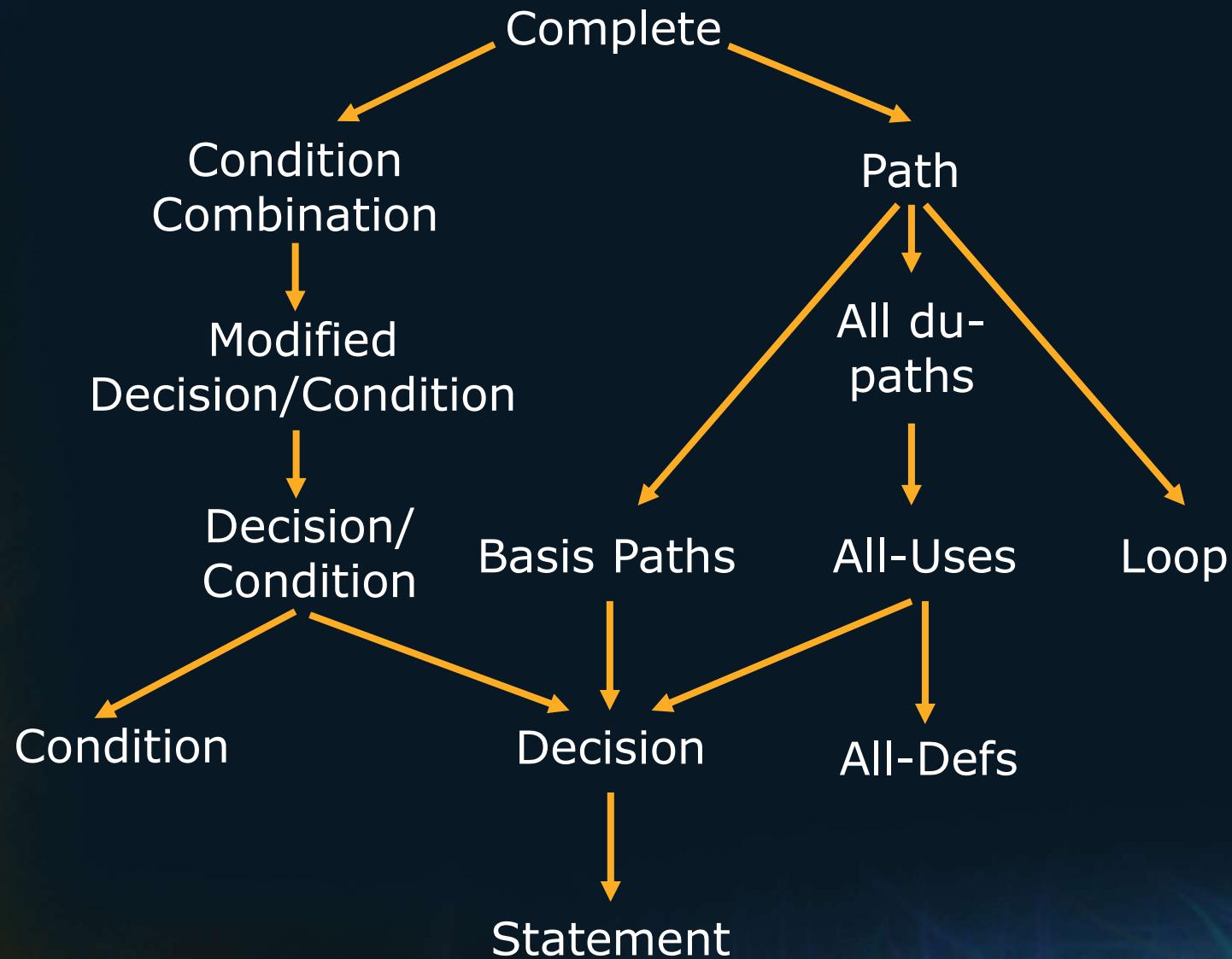
# Exercise

- Identify du pairs, all c-uses and p-uses for **variable Y** in Exercise.
- Identify whether or not each def-clear path is feasible, and whether or not it is a du-path.
- Finally, receive the test suite to satisfy **All-DU-Paths** of this program.

# Recall

- **All-Defs:** for every program variable  $v$ , at least one def-clear path from **every** definition of  $v$  to **at least one** c-use or one p-use of  $v$  must be covered.
- **All-Uses:** for every program variable  $v$ , at least one def-clear path from **every** definition of  $v$  to **every** c-use and **every** p-use of  $v$  must be covered.
- **All-DU-Paths:** for every program variable  $v$ , **every** du-path from **every** definition of  $v$  to **every** c-use and **every** p-use of  $v$  must be covered.

# Summary of White-Box Coverage Relationships



# The Commission Problem

A rifle salesperson sells rifle locks, stocks, and barrels. Locks cost \$45, stocks cost \$30, and barrels cost \$25. The salesperson had to sell at least one complete rifle per month, and production limits were such that the most the salesperson could sell in a month was 70 locks, 80 stocks, and 90 barrels.

Suppose the commission is computed as follows: 10% on sales up to (and including) \$1000, 15% on the next \$800, and 20% on any sales in excess of \$1800.

The commission program produces a monthly sales report that gave the total number of locks, stocks, and barrels sold, the salesperson's total dollar sales, and, finally, the commission.

## 佣金程序的问题描述

- 步枪销售商在亚利桑那州境内销售制造商制造的步枪锁、准星和枪管
- 枪锁卖45美元，准星卖30美元，枪管卖25美元
- 销售商每月至少要售出一枝完整的步枪，生产限额考虑到大多数销售商在一个月内可销售70个枪锁、80个准星和90个枪管
- 销售商在每访问一个镇子之后，给制造商发出电报，说明在那个镇子中售出的枪锁、准星和枪管数量

## 佣金程序的问题描述（续）

- 到了月末，销售商要发出一封很短的电报，通知一个枪锁被售出，以便制造商知道当月的销售情况
- 销售商的佣金为：销售额不到（含）1000美元的部分，为10%，1000（不含）到1800（含）美元的部分，为15%，超过1800美元的部分为20%
- 佣金程序生成月份销售报告，汇总售出的枪锁、准星和枪管总数，销售商的总销售额，以及佣金

```
1 Program Commission (INPUT,OUTPUT)

2 Dim locks,stocks,barrels As Integer
3 Dim lockPrice,stockPrice,barrelPrice As Real
4 Dim totalLocks,totalStocks,totalBarrels As Integer
5 Dim lockSales,stockSales,barrelSales As Real
6 Dim sales,commission As Real

7 lockPrice = 45.0
8 stockPrice = 30.0
9 barrelPrice = 25.0
10 totalLocks = 0
11 totalStocks = 0
12 totalBarrels = 0
```

```
13    Input(locks)
14    While NOT(locks = - 1)      'loop condition uses -1 to indicate end of
15        Input(stocks,barrels)
16        totalLocks = totalLocks + locks
17        totalStocks = totalStocks + stocks
18        totalBarrels = totalBarrels + barrels
19        Input(locks)
20    EndWhile
21    Output("Locks sold:",totalLocks)
22    Output("Stocks sold:",totalStocks)
23    Output("Barrels sold:",totalBarrels)
24    lockSales = lockPrice * totalLocks
25    stockSales = stockPrice * totalStocks
26    barrelSales = barrelPrice * totalBarrels
27    sales = lockSales + stockSales + barrelSales
28    Output("Total sales:",sales)
```

```
29     If(sales>1800.0)
30         Then
31             commission = 0.10 * 1000.0
32             commission = commission + 0.15 * 800.0
33             commission = commission + 0.20 * (sales - 1800.0)
34     Else If(sales>1000.0)
35         Then
36             commission = 0.10 * 1000.0
37             commission = commission + 0.15 * (sales - 1000.0)
38         Else commission = 0.10 * sales
39     EndIf
40 EndIf
41 Output("Commission is $",commission)
42 End Commission
```

# Homework

- Draw control flow graph.
- For these variable: LockPrice, TotalStocks, Barrels, LockSales, Sales, Commission
  - List du-pairs and def-clear paths
  - Design test cases to satisfy all du-path coverage.