

STQA_Session_06

--Data flow testing

Dataflow Coverage

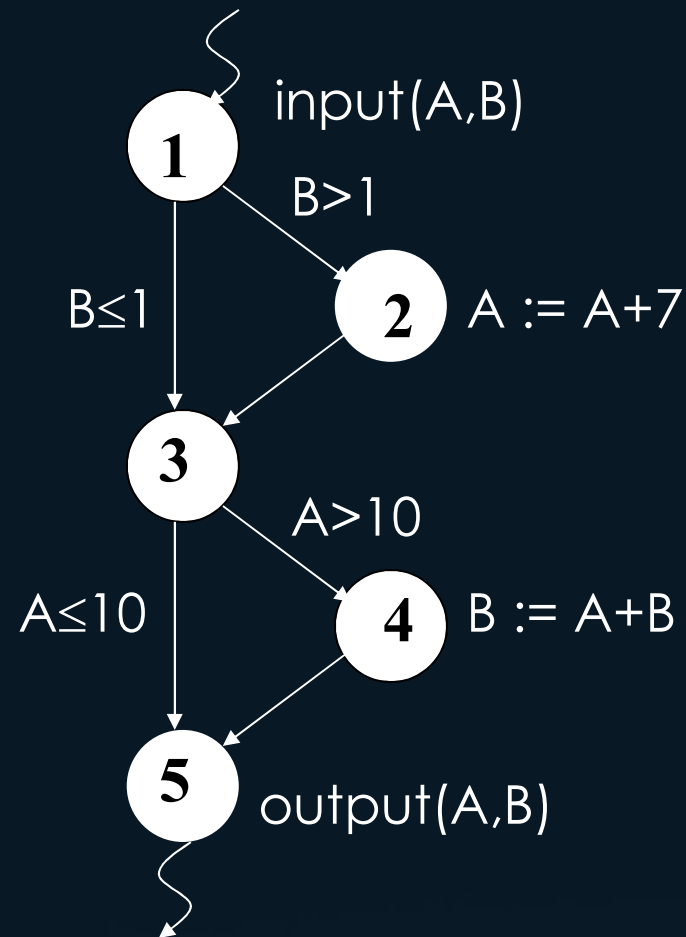
- Based on the idea that program paths along which variables are **defined** and then **used** should be covered.
- A **family of path selection criteria** has been defined, each providing a different degree of coverage.
- CASE **tool support** is very desirable.

Other Dataflow Terms and Definitions

- A path is *definition clear* ("**def-clear**") with respect to a variable v if there is **no re-definition** of v within the path.
- A *definition-use pair* ("**du-pair**") with respect to a variable v is a double (d,u) such that d is a node in the program's flow graph at which v is defined, u is **a node or edge** at which v is used, and there is **a def-clear path** with respect to v from d to u .
- (Note that the definition of a du-pair does not require the existence of a **feasible** def-clear path from d to u .)

Example 1

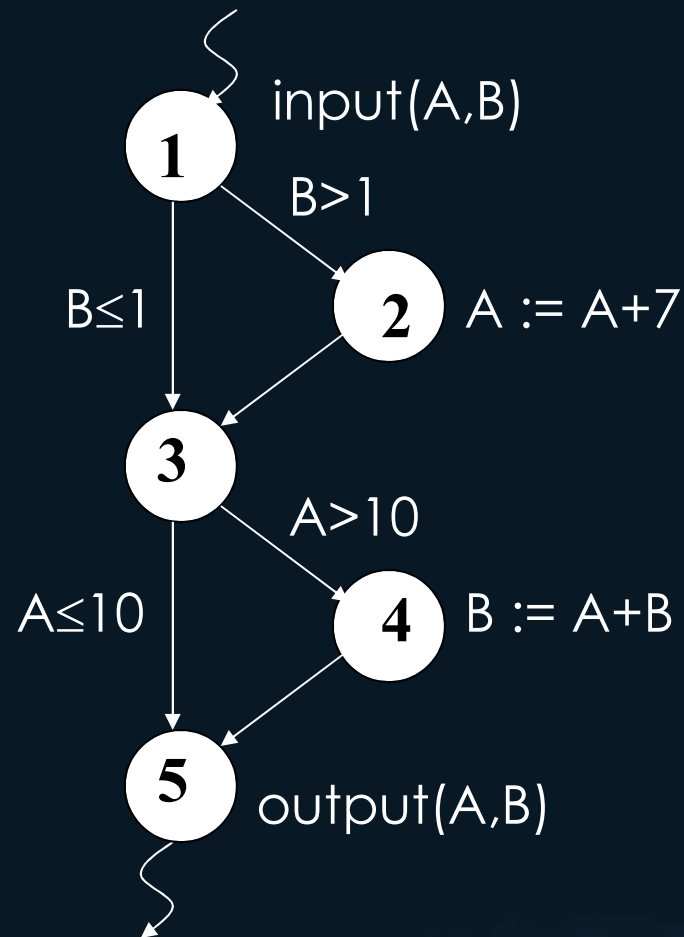
```
1. input(A,B)
   if (B>1) then
2.   A := A+7
   end_if
3. if (A>10) then
4.   B := A+B
   end_if
5. output(A,B)
```



Identifying DU-Pairs – Variable A

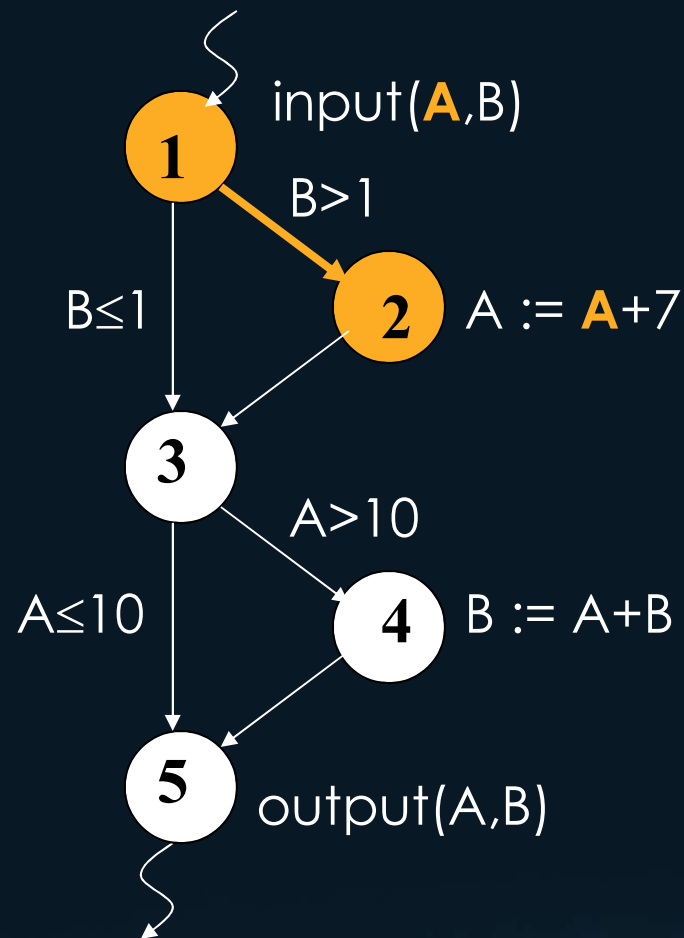
d-c paths

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|----------------|
| (1,2) | <1,2> |
| (1,4) | <1,3,4> |
| (1,5) | <1,3,4,5> |
| | <1,3,5> |
| (1,<3,4>) | <1,3,4> |
| (1,<3,5>) | <1,3,5> |
| (2,4) | <2,3,4> |
| (2,5) | <2,3,4,5> |
| | <2,3,5> |
| (2,<3,4>) | <2,3,4> |
| (2,<3,5>) | <2,3,5> |



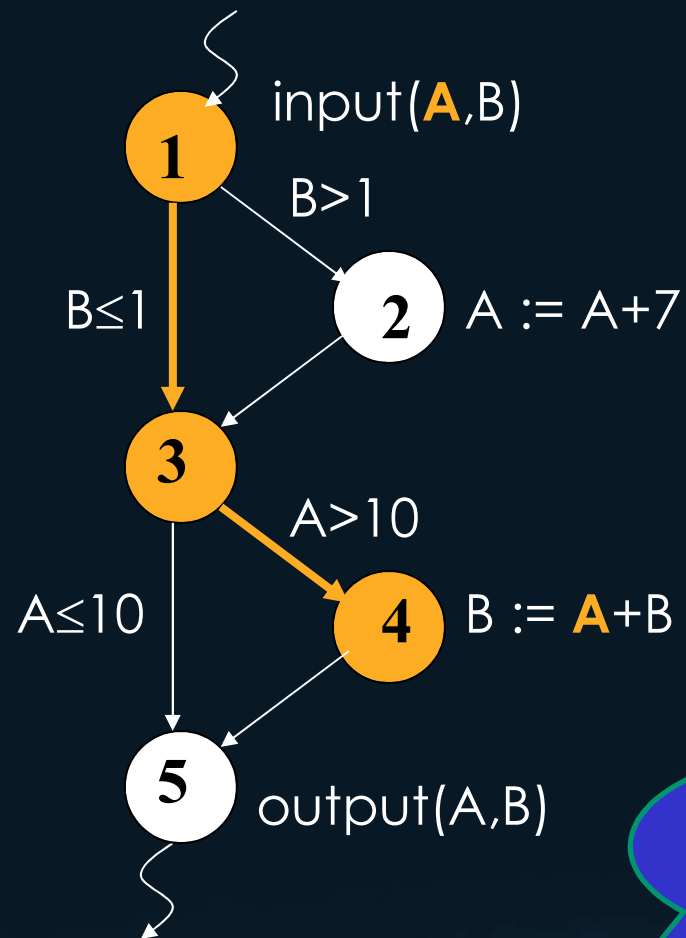
Identifying DU-Pairs – Variable A

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|--------------------|
| (1,2) | <1,2> |
| (1,4) | <1,3,4> |
| (1,5) | <1,3,4,5> |
| | <1,3,5> |
| (1,<3,4>) | <1,3,4> |
| (1,<3,5>) | <1,3,5> |
| (2,4) | <2,3,4> |
| (2,5) | <2,3,4,5> |
| | <2,3,5> |
| (2,<3,4>) | <2,3,4> |
| (2,<3,5>) | <2,3,5> |



Identifying DU-Pairs – Variable A

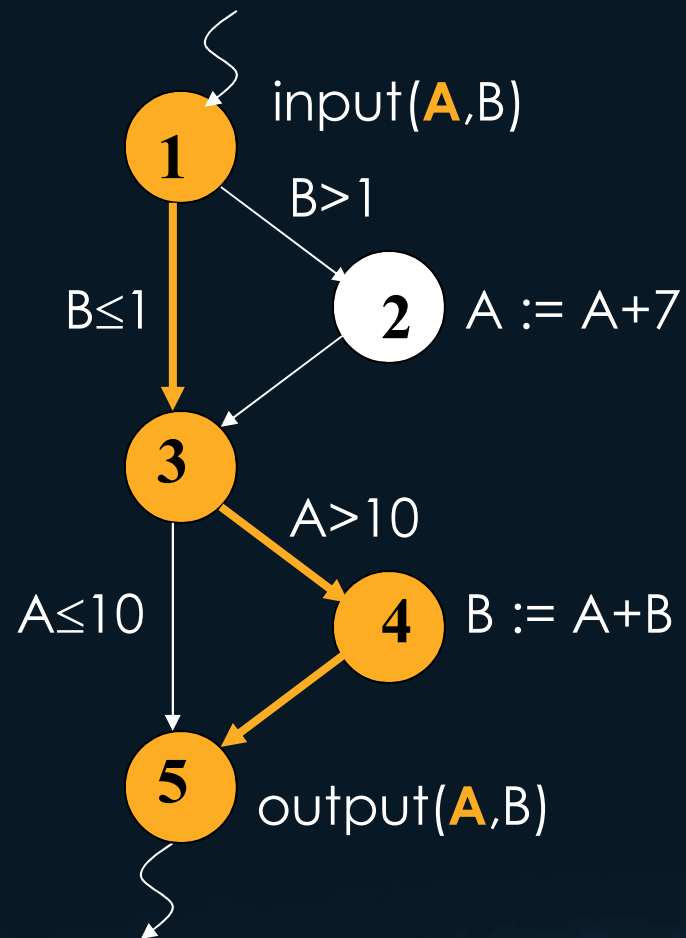
| <u>du-pair</u> | <u>path(s)</u> |
|----------------|----------------------|
| (1,2) | <1,2> |
| (1,4) | <1,3,4> |
| (1,5) | <1,3,4,5> |
| | <1,3,5> |
| (1,<3,4>) | <1,3,4> |
| (1,<3,5>) | <1,3,5> |
| (2,4) | <2,3,4> |
| (2,5) | <2,3,4,5> |
| | <2,3,5> |
| (2,<3,4>) | <2,3,4> |
| (2,<3,5>) | <2,3,5> |



1,2,3,4?

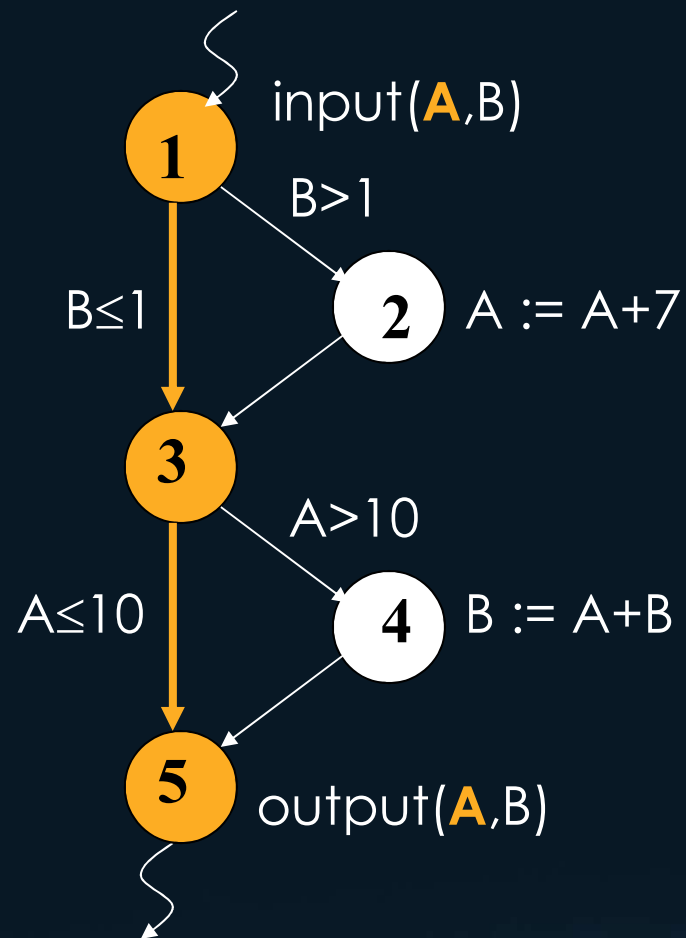
Identifying DU-Pairs – Variable A

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|------------------------|
| (1,2) | <1,2> |
| (1,4) | <1,3,4> |
| (1,5) | <1,3,4,5> |
| | <1,3,5> |
| (1,<3,4>) | <1,3,4> |
| (1,<3,5>) | <1,3,5> |
| (2,4) | <2,3,4> |
| (2,5) | <2,3,4,5> |
| | <2,3,5> |
| (2,<3,4>) | <2,3,4> |
| (2,<3,5>) | <2,3,5> |



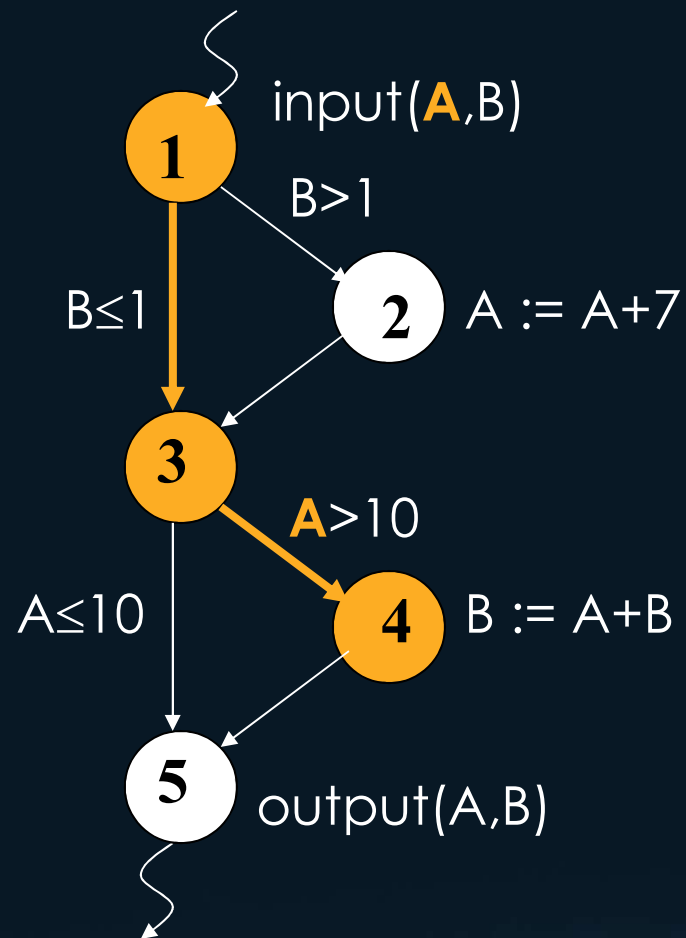
Identifying DU-Pairs – Variable A

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|----------------------|
| (1,2) | <1,2> |
| (1,4) | <1,3,4> |
| (1,5) | <1,3,4,5> |
| | <1,3,5> |
| (1,<3,4>) | <1,3,4> |
| (1,<3,5>) | <1,3,5> |
| (2,4) | <2,3,4> |
| (2,5) | <2,3,4,5> |
| | <2,3,5> |
| (2,<3,4>) | <2,3,4> |
| (2,<3,5>) | <2,3,5> |



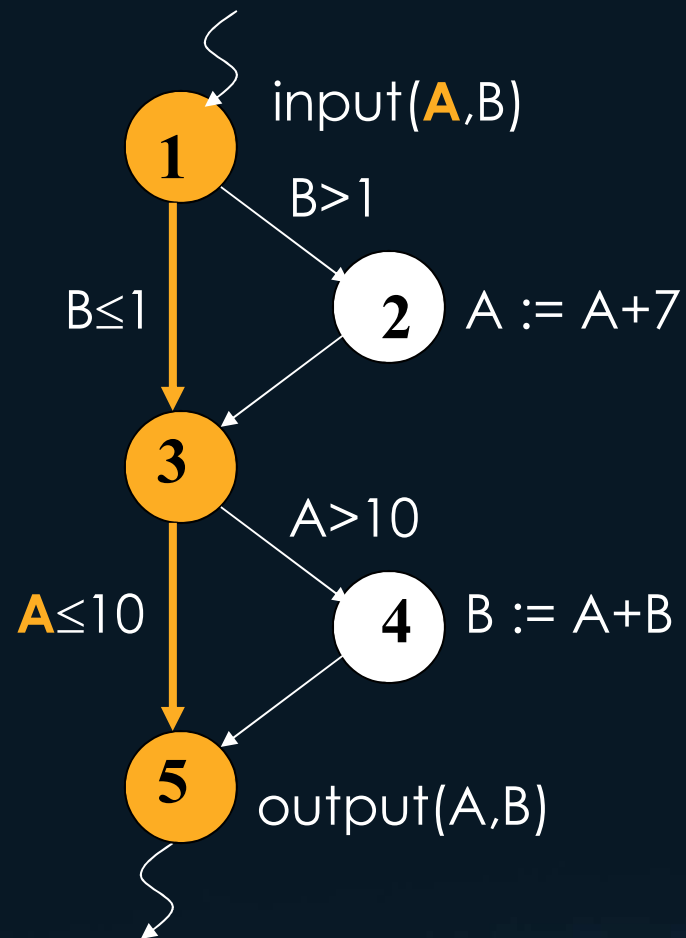
Identifying DU-Pairs – Variable A

| <u>du-pair</u> | <u>path(s)</u> |
|------------------------|----------------------|
| (1,2) | <1,2> |
| (1,4) | <1,3,4> |
| (1,5) | <1,3,4,5> |
| | <1,3,5> |
| (1,<3,4>) | <1,3,4> |
| (1,<3,5>) | <1,3,5> |
| (2,4) | <2,3,4> |
| (2,5) | <2,3,4,5> |
| | <2,3,5> |
| (2,<3,4>) | <2,3,4> |
| (2,<3,5>) | <2,3,5> |



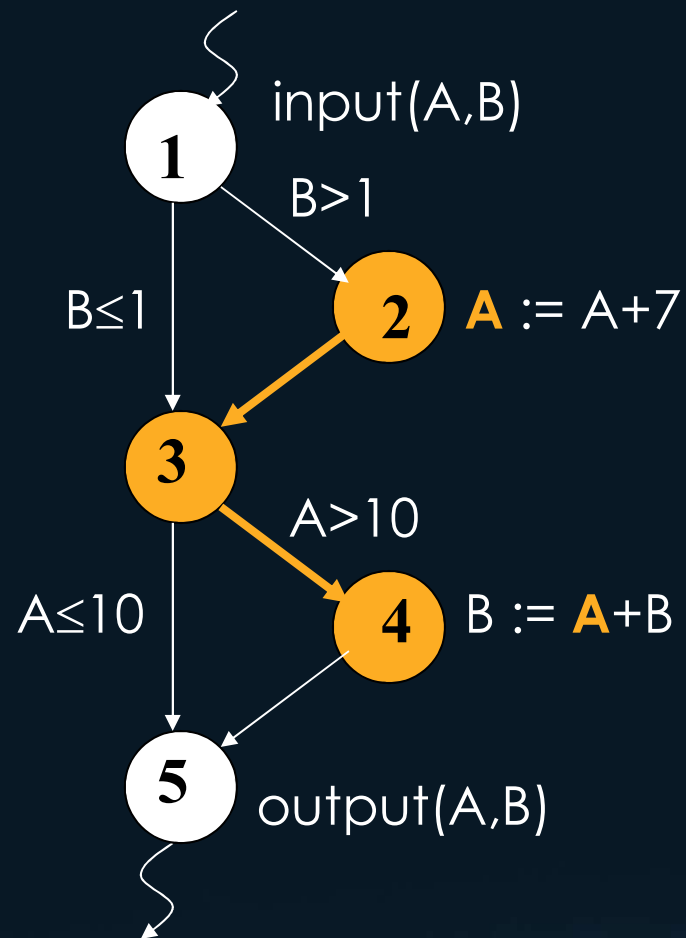
Identifying DU-Pairs – Variable A

| <u>du-pair</u> | <u>path(s)</u> |
|------------------------|----------------------|
| (1,2) | <1,2> |
| (1,4) | <1,3,4> |
| (1,5) | <1,3,4,5> |
| | <1,3,5> |
| (1,<3,4>) | <1,3,4> |
| (1,<3,5>) | <1,3,5> |
| (2,4) | <2,3,4> |
| (2,5) | <2,3,4,5> |
| | <2,3,5> |
| (2,<3,4>) | <2,3,4> |
| (2,<3,5>) | <2,3,5> |



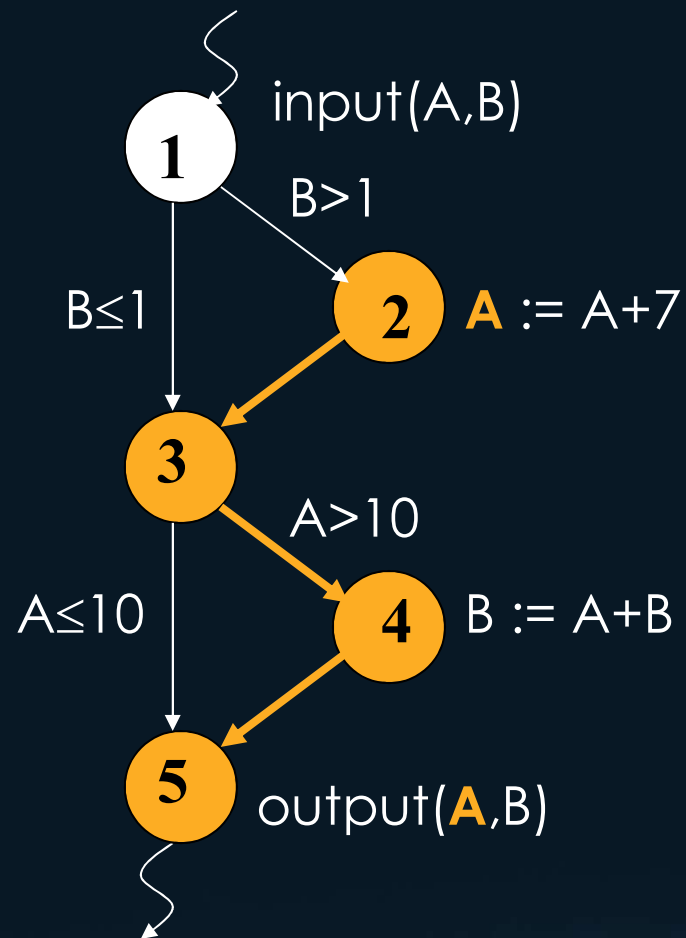
Identifying DU-Pairs – Variable A

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|----------------------|
| (1,2) | <1,2> |
| (1,4) | <1,3,4> |
| (1,5) | <1,3,4,5> |
| | <1,3,5> |
| (1,<3,4>) | <1,3,4> |
| (1,<3,5>) | <1,3,5> |
| (2,4) | <2,3,4> |
| (2,5) | <2,3,4,5> |
| | <2,3,5> |
| (2,<3,4>) | <2,3,4> |
| (2,<3,5>) | <2,3,5> |



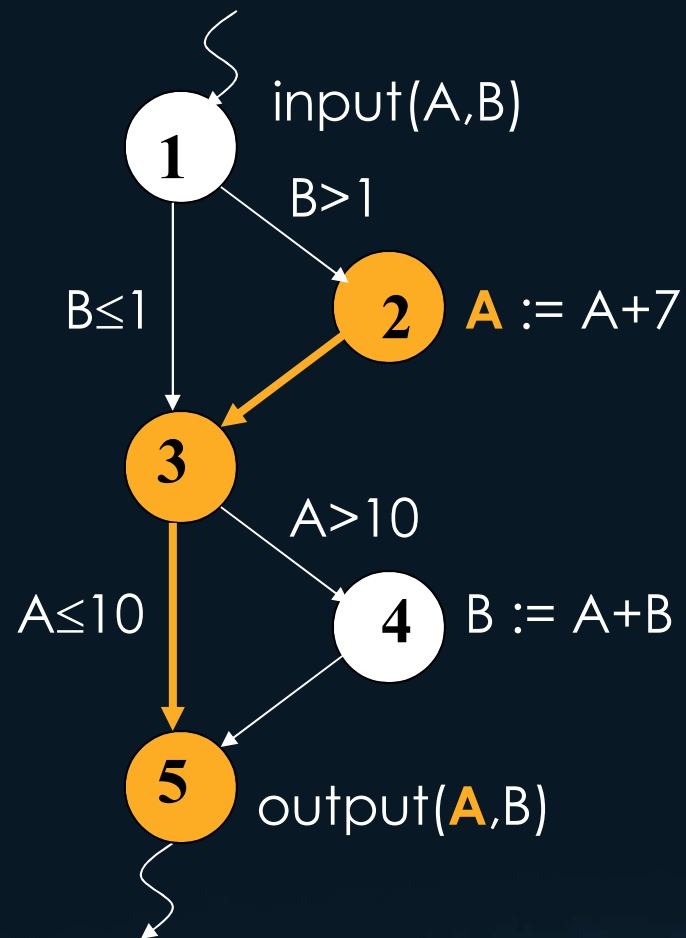
Identifying DU-Pairs – Variable A

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|------------------------|
| (1,2) | <1,2> |
| (1,4) | <1,3,4> |
| (1,5) | <1,3,4,5> |
| | <1,3,5> |
| (1,<3,4>) | <1,3,4> |
| (1,<3,5>) | <1,3,5> |
| (2,4) | <2,3,4> |
| (2,5) | <2,3,4,5> |
| | <2,3,5> |
| (2,<3,4>) | <2,3,4> |
| (2,<3,5>) | <2,3,5> |



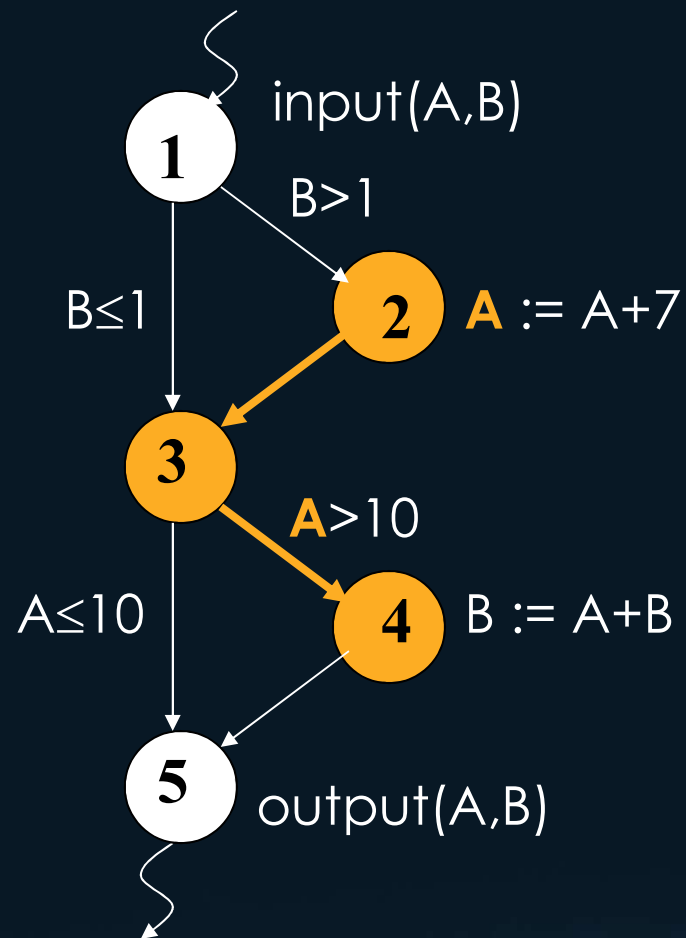
Identifying DU-Pairs – Variable A

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|----------------------|
| (1,2) | <1,2> |
| (1,4) | <1,3,4> |
| (1,5) | <1,3,4,5> |
| | <1,3,5> |
| (1,<3,4>) | <1,3,4> |
| (1,<3,5>) | <1,3,5> |
| (2,4) | <2,3,4> |
| (2,5) | <2,3,4,5> |
| | <2,3,5> |
| (2,<3,4>) | <2,3,4> |
| (2,<3,5>) | <2,3,5> |



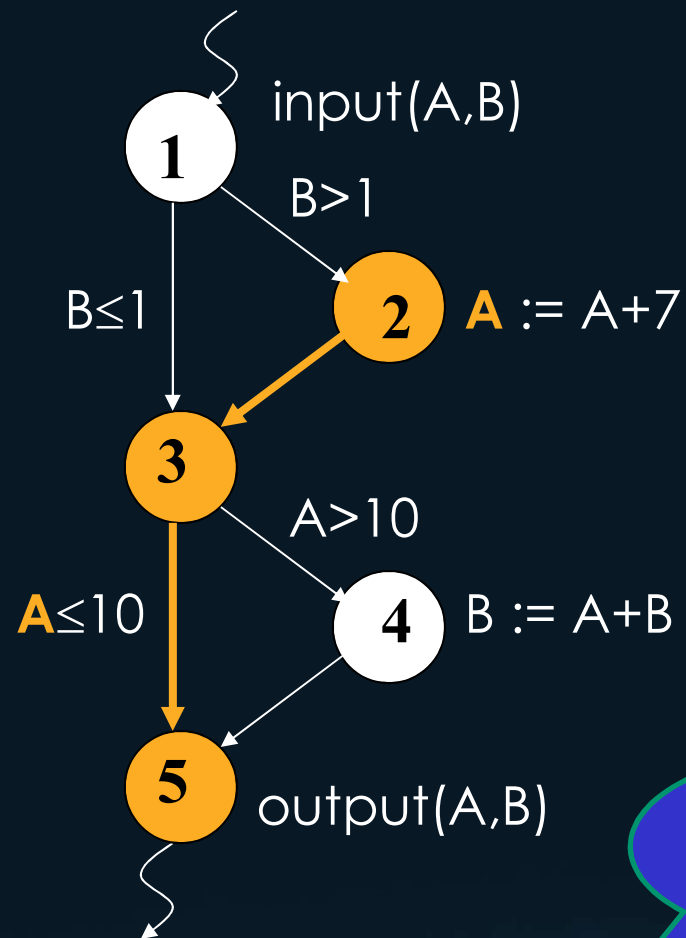
Identifying DU-Pairs – Variable A

| <u>du-pair</u> | <u>path(s)</u> |
|------------------------|----------------------|
| (1,2) | <1,2> |
| (1,4) | <1,3,4> |
| (1,5) | <1,3,4,5> |
| | <1,3,5> |
| (1,<3,4>) | <1,3,4> |
| (1,<3,5>) | <1,3,5> |
| (2,4) | <2,3,4> |
| (2,5) | <2,3,4,5> |
| | <2,3,5> |
| (2,<3,4>) | <2,3,4> |
| (2,<3,5>) | <2,3,5> |



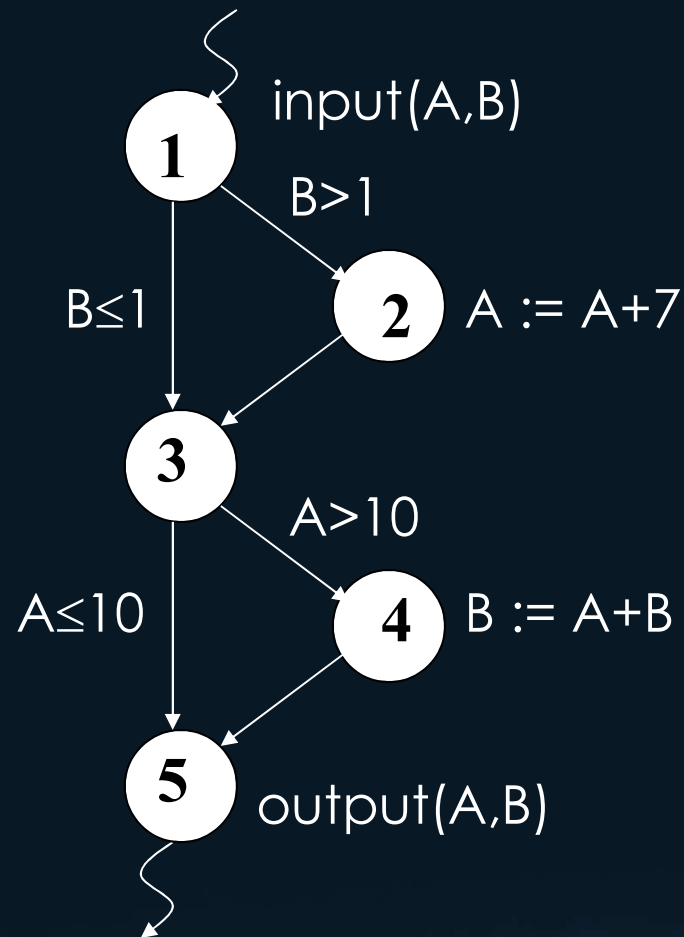
Identifying DU-Pairs – Variable A

| <u>du-pair</u> | <u>path(s)</u> |
|------------------------|----------------------|
| (1,2) | <1,2> |
| (1,4) | <1,3,4> |
| (1,5) | <1,3,4,5> |
| | <1,3,5> |
| (1,<3,4>) | <1,3,4> |
| (1,<3,5>) | <1,3,5> |
| (2,4) | <2,3,4> |
| (2,5) | <2,3,4,5> |
| | <2,3,5> |
| (2,<3,4>) | <2,3,4> |
| (2,<3,5>) | <2,3,5> |



Identifying DU-Pairs – Variable B

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|----------------|
| (1,4) | <1,2,3,4> |
| | <1,3,4> |
| (1,5) | <1,2,3,5> |
| | <1,3,5> |
| (1,<1,2>) | <1,2> |
| (1,<1,3>) | <1,3> |
| (4,5) | <4,5> |



Dataflow Test Coverage Criteria

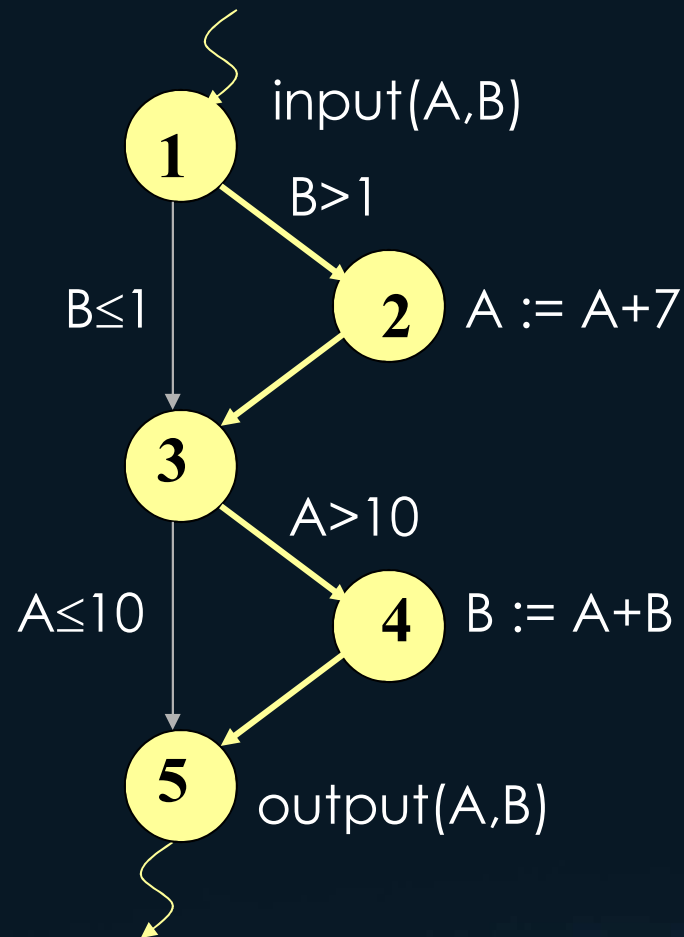
- ***All-Defs:*** for every program variable v , at least one def-clear path from every definition of v to at least one c-use or one p-use of v must be covered.

Dataflow Test Coverage Criteria (cont'd)

- Consider a test case executing path:
1. **<1,2,3,4,5>**
- Identify **all def-clear paths covered (i.e., subsumed)** by this path for each variable.
- Are **all definitions for each variable** associated with at least one of the subsumed def-clear paths?

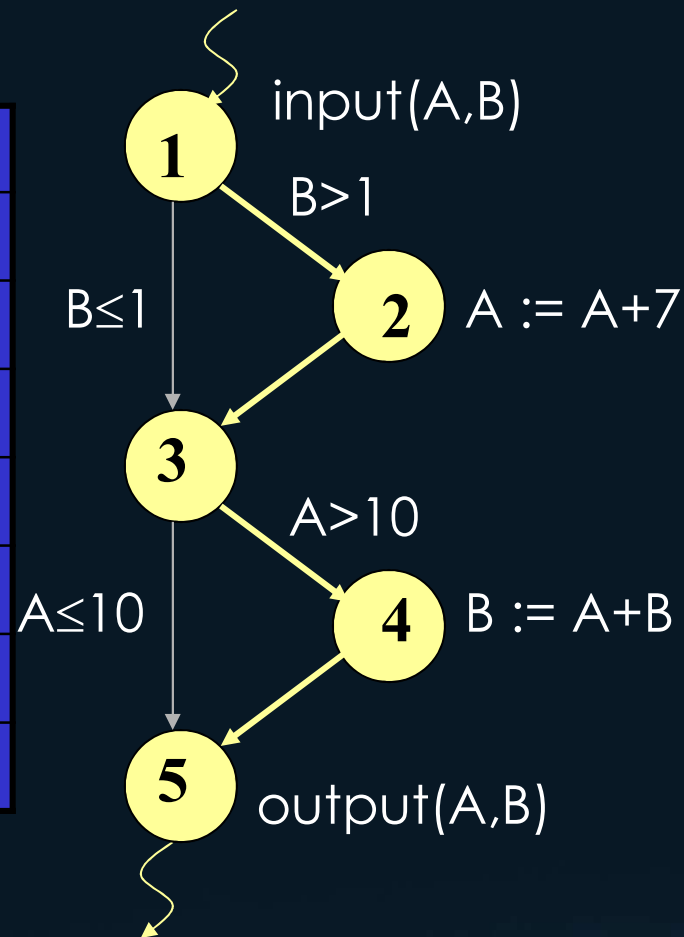
Def-Clear Paths Subsumed by $\langle 1,2,3,4,5 \rangle$ for Variable A

| <u>du-pair</u> | <u>path(s)</u> |
|---|-----------------------------|
| (1,2) | $\langle 1,2 \rangle$ ✓ |
| (1,4) | $\langle 1,3,4 \rangle$ |
| (1,5) | $\langle 1,3,4,5 \rangle$ |
| | $\langle 1,3,5 \rangle$ |
| (1, $\langle 3,4 \rangle$) | $\langle 1,3,4 \rangle$ |
| (1, $\langle 3,5 \rangle$) | $\langle 1,3,5 \rangle$ |
| (2,4) | $\langle 2,3,4 \rangle$ ✓ |
| (2,5) | $\langle 2,3,4,5 \rangle$ ✓ |
| | $\langle 2,3,5 \rangle$ |
| (2,$\langle 3,4 \rangle$) | $\langle 2,3,4 \rangle$ ✓ |
| (2, $\langle 3,5 \rangle$) | $\langle 2,3,5 \rangle$ |



Def-Clear Paths Subsumed by $\langle 1,2,3,4,5 \rangle$ for Variable B

| <u>du-pair</u> | <u>path(s)</u> |
|-----------------------------|-----------------------------|
| (1,4) | $\langle 1,2,3,4 \rangle$ ✓ |
| | $\langle 1,3,4 \rangle$ |
| (1,5) | $\langle 1,2,3,5 \rangle$ |
| | $\langle 1,3,5 \rangle$ |
| (4,5) | $\langle 4,5 \rangle$ ✓ |
| (1, $\langle 1,2 \rangle$) | $\langle 1,2 \rangle$ ✓ |
| (1, $\langle 1,3 \rangle$) | $\langle 1,3 \rangle$ |



Dataflow Test Coverage Criteria (cont'd)

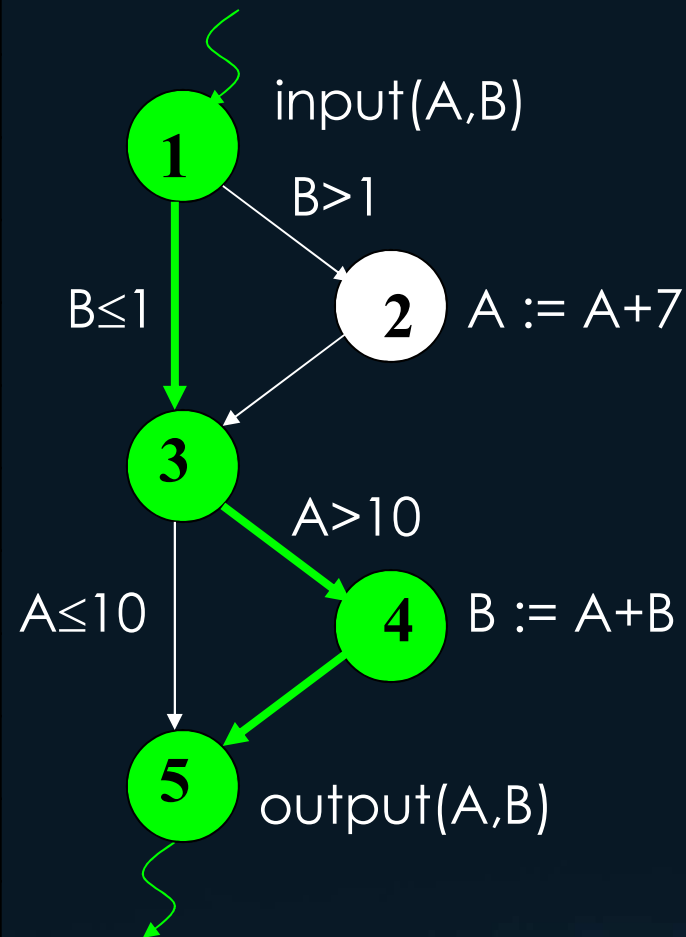
- Since $\langle 1, 2, 3, 4, 5 \rangle$ covers at least one def-clear path from every definition of A/B to at least one c-use or p-use of A/B, All-Defs coverage is achieved.

Dataflow Test Coverage Criteria (cont'd)

- **All-Uses:** for every program variable **v**, at least one def-clear path from **every definition** of **v** to **every c-use** and **every p-use** of **v** must be covered.
- Consider additional test cases executing paths:
 - 2. **<1,3,4,5>**
 - 3. **<1,2,3,5>**
- Do all three test cases provide All-Uses coverage?

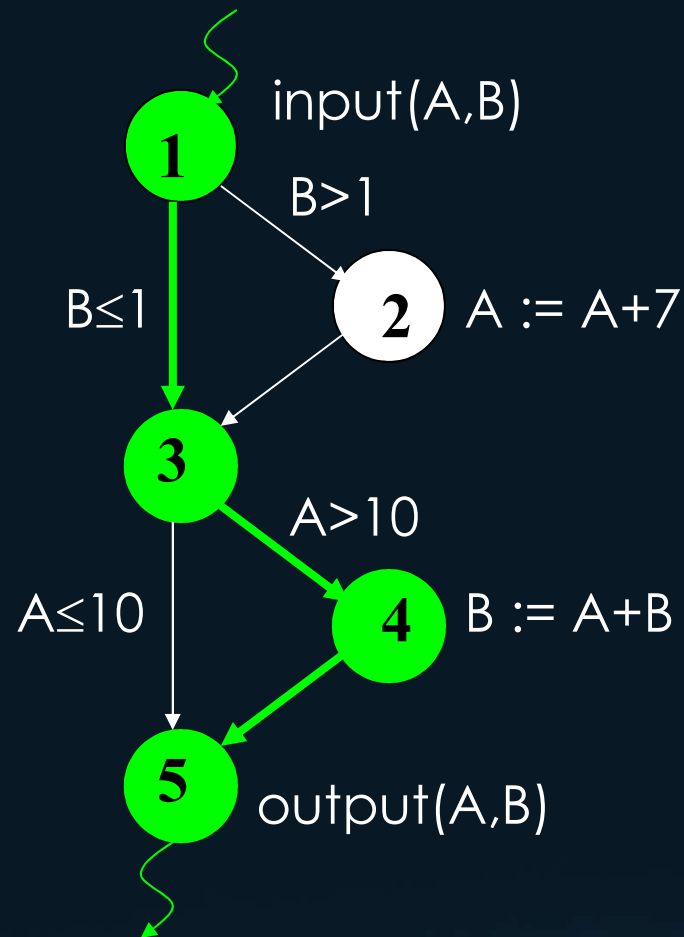
Def-Clear Paths Subsumed by $\langle 1,3,4,5 \rangle$ for Variable A

| <u>du-pair</u> | <u>path(s)</u> |
|-----------------------------|-----------------------------|
| (1,2) | $\langle 1,2 \rangle$ ✓ |
| (1,4) | $\langle 1,3,4 \rangle$ ✓ |
| (1,5) | $\langle 1,3,4,5 \rangle$ ✓ |
| | $\langle 1,3,5 \rangle$ |
| (1, $\langle 3,4 \rangle$) | $\langle 1,3,4 \rangle$ ✓ |
| (1, $\langle 3,5 \rangle$) | $\langle 1,3,5 \rangle$ |
| (2,4) | $\langle 2,3,4 \rangle$ ✓ |
| (2,5) | $\langle 2,3,4,5 \rangle$ ✓ |
| | $\langle 2,3,5 \rangle$ |
| (2, $\langle 3,4 \rangle$) | $\langle 2,3,4 \rangle$ ✓ |
| (2, $\langle 3,5 \rangle$) | $\langle 2,3,5 \rangle$ |



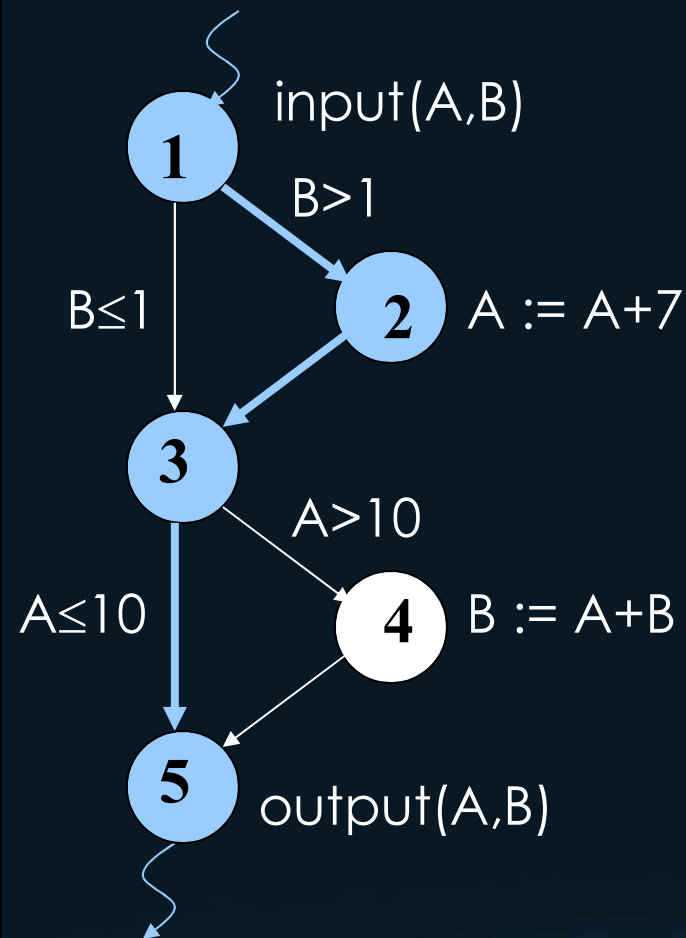
Def-Clear Paths Subsumed by $\langle 1, 3, 4, 5 \rangle$ for Variable B

| <u>du-pair</u> | <u>path(s)</u> |
|------------------------------|--------------------------------|
| (1,4) | $\langle 1, 2, 3, 4 \rangle$ ✓ |
| | $\langle 1, 3, 4 \rangle$ ✓ |
| (1,5) | $\langle 1, 2, 3, 5 \rangle$ |
| | $\langle 1, 3, 5 \rangle$ |
| (4,5) | $\langle 4, 5 \rangle$ ✓ ✓ |
| (1, $\langle 1, 2 \rangle$) | $\langle 1, 2 \rangle$ ✓ |
| (1, $\langle 1, 3 \rangle$) | $\langle 1, 3 \rangle$ ✓ |



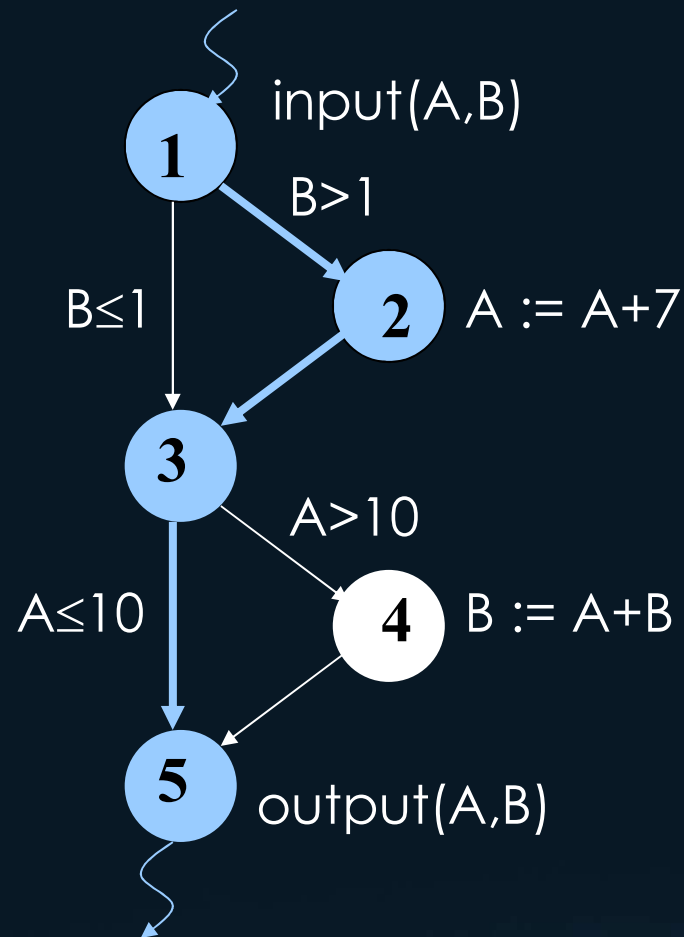
Def-Clear Paths Subsumed by $\langle 1,2,3,5 \rangle$ for Variable A

| <u>du-pair</u> | <u>path(s)</u> |
|-----------------------------|-----------------------------|
| (1,2) | $\langle 1,2 \rangle$ ✓ ✗ |
| (1,4) | $\langle 1,3,4 \rangle$ ✓ |
| (1,5) | $\langle 1,3,4,5 \rangle$ ✓ |
| | $\langle 1,3,5 \rangle$ |
| (1, $\langle 3,4 \rangle$) | $\langle 1,3,4 \rangle$ ✓ |
| (1, $\langle 3,5 \rangle$) | $\langle 1,3,5 \rangle$ |
| (2,4) | $\langle 2,3,4 \rangle$ ✓ |
| (2,5) | $\langle 2,3,4,5 \rangle$ ✓ |
| | $\langle 2,3,5 \rangle$ ✗ |
| (2, $\langle 3,4 \rangle$) | $\langle 2,3,4 \rangle$ ✓ |
| (2, $\langle 3,5 \rangle$) | $\langle 2,3,5 \rangle$ ✗ |



Def-Clear Paths Subsumed by $\langle 1, 2, 3, 5 \rangle$ for Variable B

| <u>du-pair</u> | <u>path(s)</u> |
|------------------------------|--------------------------------|
| (1,4) | $\langle 1, 2, 3, 4 \rangle$ ✓ |
| | $\langle 1, 3, 4 \rangle$ ✓ |
| (1,5) | $\langle 1, 2, 3, 5 \rangle$ ✓ |
| | $\langle 1, 3, 5 \rangle$ |
| (4,5) | $\langle 4, 5 \rangle$ ✓ ✓ |
| (1, $\langle 1, 2 \rangle$) | $\langle 1, 2 \rangle$ ✓ ✓ |
| (1, $\langle 1, 3 \rangle$) | $\langle 1, 3 \rangle$ ✓ |



Dataflow Test Coverage Criteria (cont'd)

- Since none of the three test cases covers the du-pair $(1, \langle 3, 5 \rangle)$ for variable A, **All-Uses Coverage is not provided.**

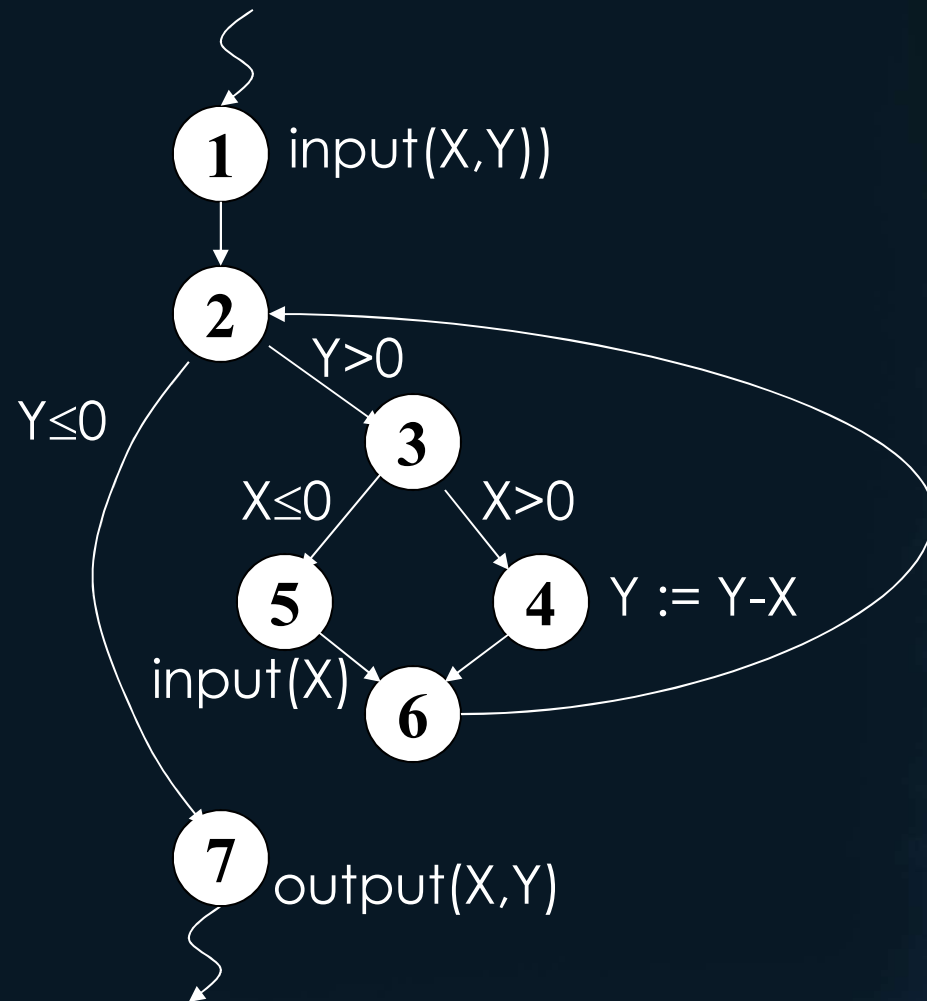
What would be even stronger than *All-Uses*?

- We have considered the *All-Defs* and the *All-Uses* criteria so far. How could the definition of *All-Uses* be modified to make it even stronger? Recall:

All-Uses: for every program variable v , **at least one def-clear path** from every definition of v to every c-use and every p-use of v must be covered.

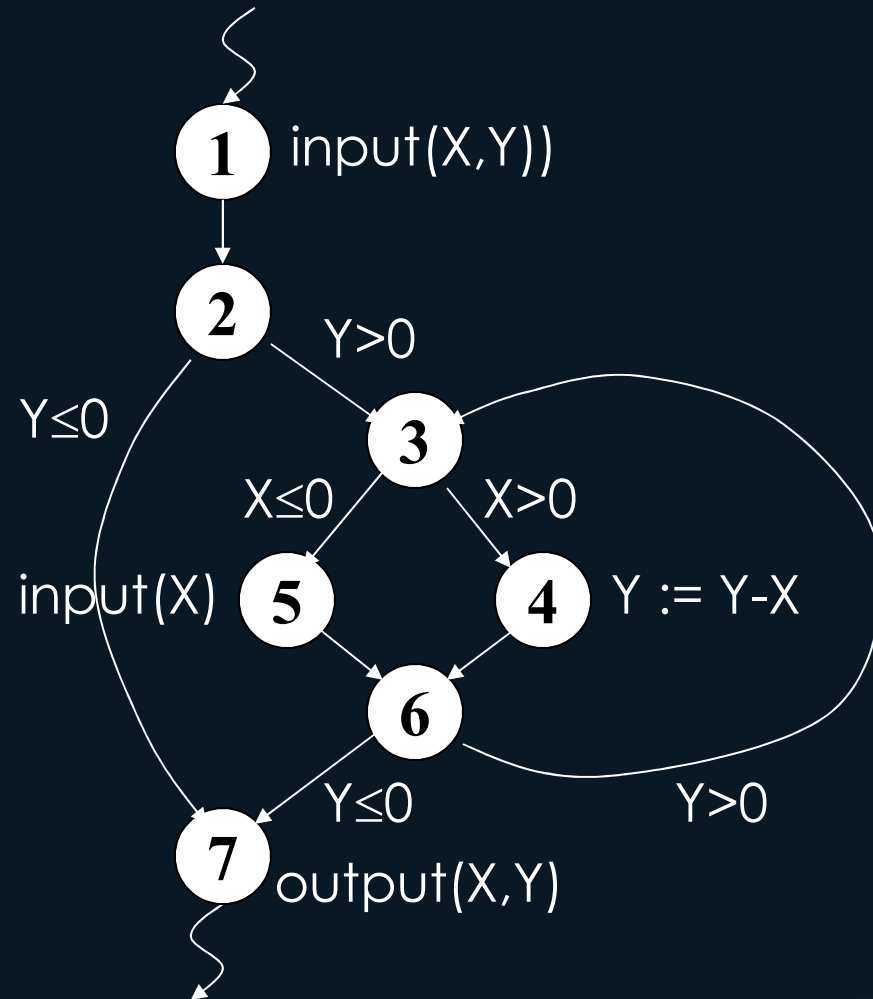
Exercise

```
1. input(X,Y)
2. while (Y>0) do
3.   if (X>0) then
4.     Y := Y-X
   else
5.     input(X)
   end_if_then_else
6. end_while
7. output(X,Y)
```



Exercise

1. input(X,Y)
2. while (Y>0) do
3. if (X>0) then
4. Y := Y-X
- else
5. input(X)
- end_if_then_else
6. end_while
7. output(X,Y)

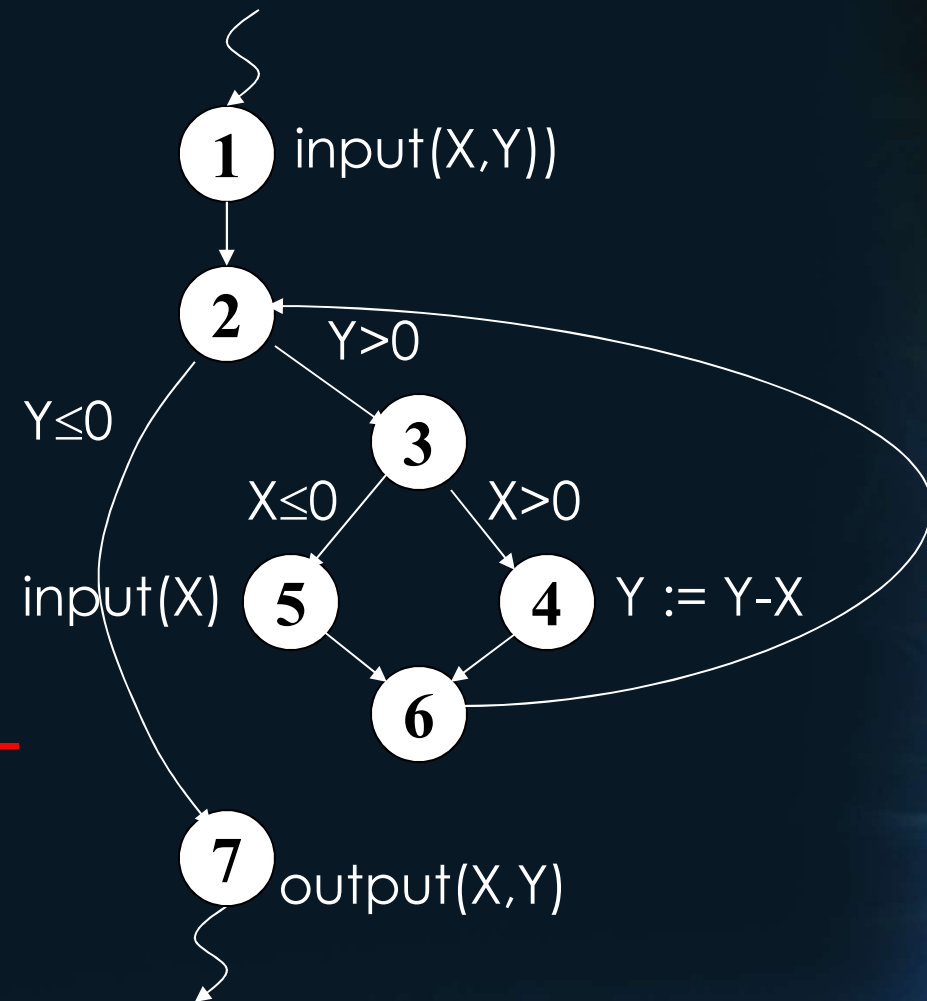


Exercise

- Identify DU-Pairs for variable X.

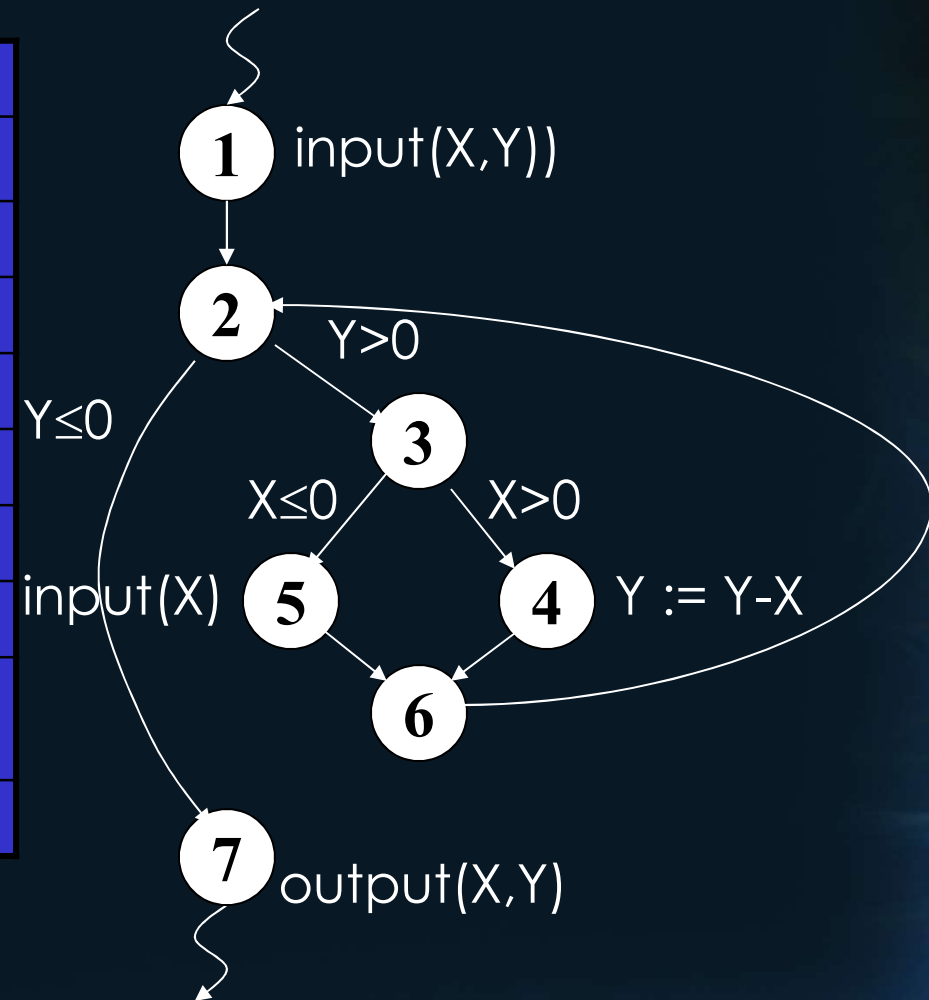
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|----------------------------|
| (1,4) | <1,2,3,4> |
| | <1,2,3,4,(6,2,3,4)*> |
| (1,7) | <1,2,7> |
| | <1,2,3,4,6,2,7> |
| | <1,2,3,4,6,(2,3,4,6)*,2,7> |
| (1,<3,4>) | <1,2,3,4> |
| | <1,2,3,4,(6,2,3,4)*> |
| (1,<3,5>) | <1,2,3,5> |
| (5,4) | <5,6,2,3,4> |
| | <5,6,2,3,4,(6,2,3,4)*> |



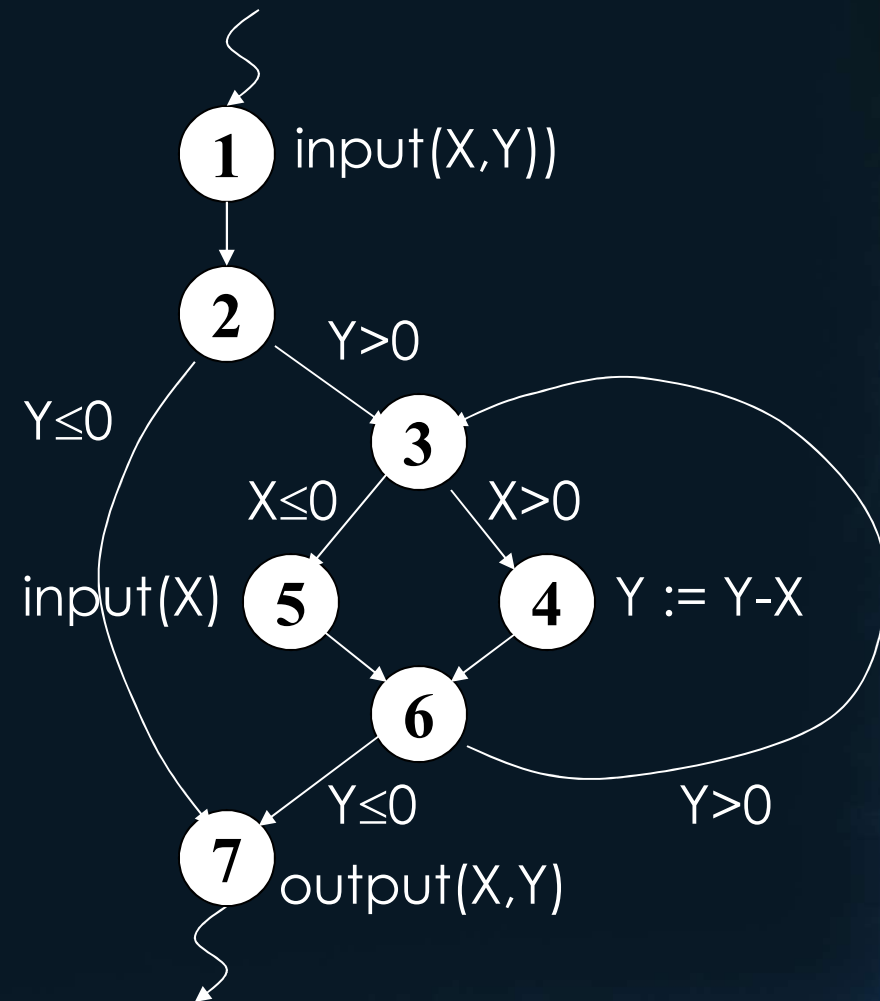
Identifying DU-Pairs – Variable X

| du-pair | path(s) |
|--------------|---------------------------------|
| (5,7) | <5,6,2,7>† |
| | <5,6,2,3,4,6,2,7> |
| | <5,6,2,3,4,6,(2,3,4,6)*,2,7> |
| (5,<3,4>) | <5,6,2,3,4> |
| | <5,6,2,3,4,(6,2,3,4)*> |
| (5,<3,5>) | <5,6,2,3,5> |
| | <5,6,2,3,4,6,2,3,5>† |
| | <5,6,2,3,4,6,(2,3,4,6)*,2,3,5>† |
| † infeasible | |



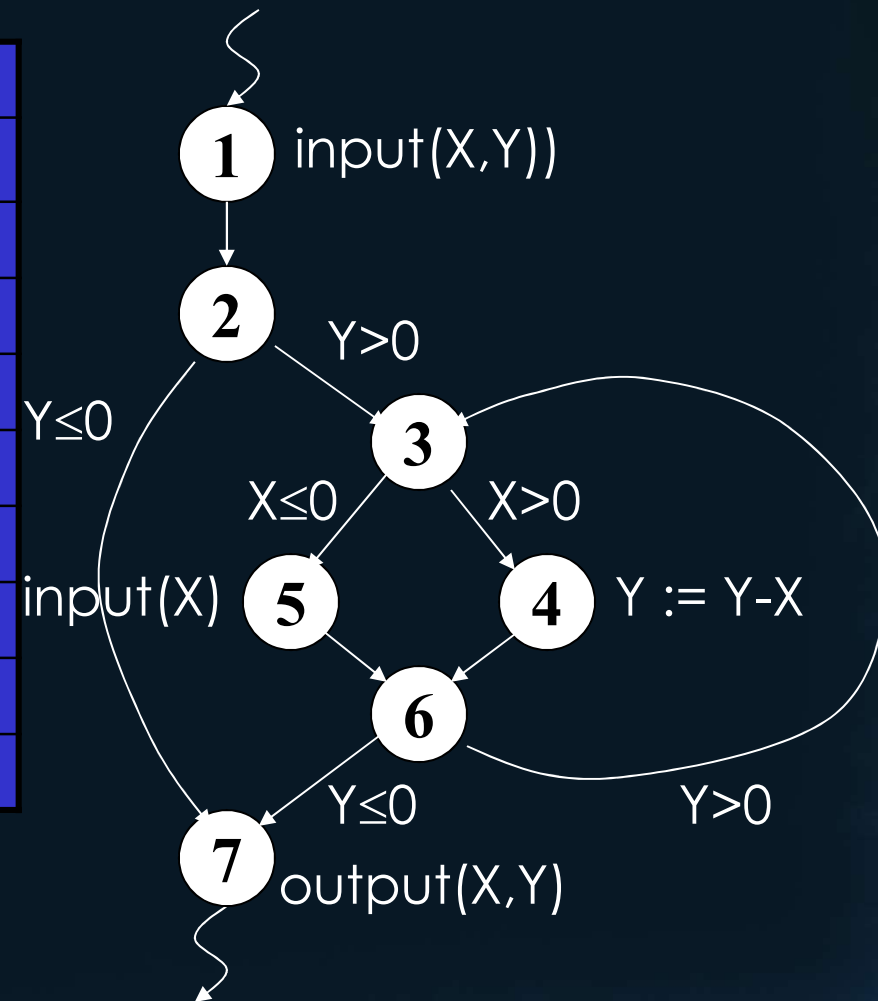
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|------------------------|
| (1,4) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,7) | <1,2,7> |
| | <1,2,3,4,6,7> |
| | <1,2,3,4,6,(3,4,6)*,7> |
| (1,<3,4>) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,<3,5>) | <1,2,3,5> |
| (5,4) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |



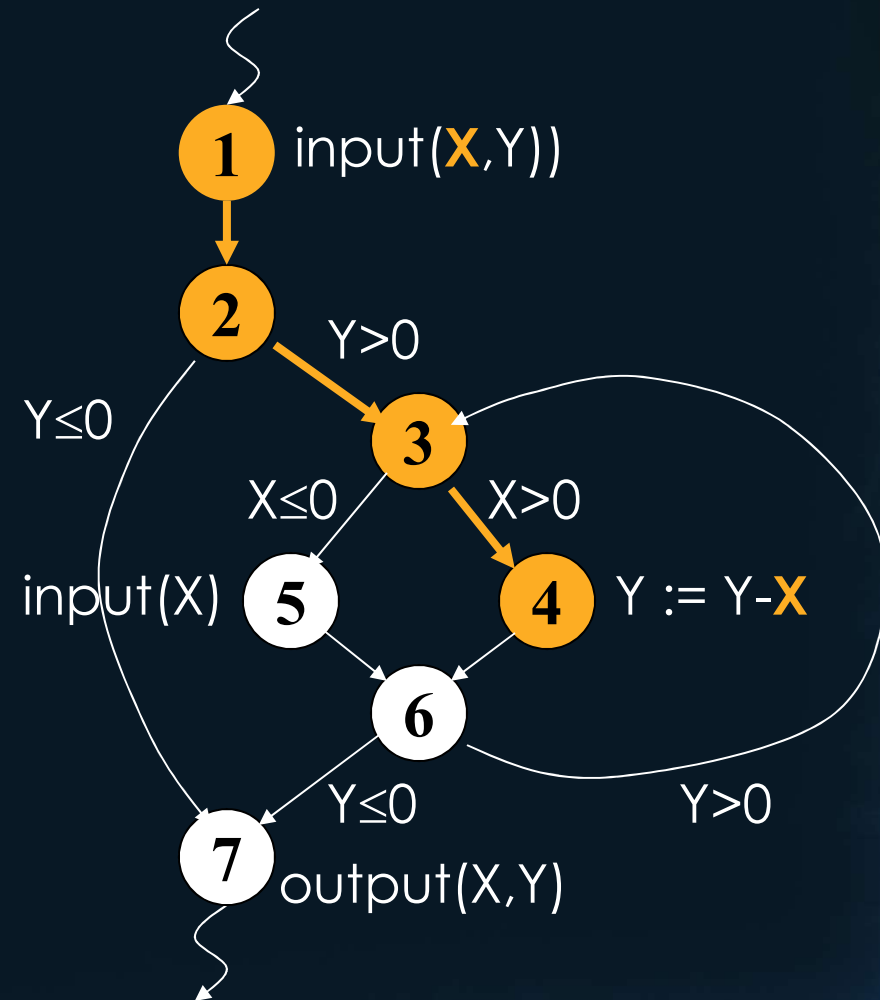
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|---------------------------|
| (5,7) | <5,6,7>† |
| | <5,6,3,4,6,7> |
| | <5,6,3,4,6,(3,4,6)*,7> |
| (5,<3,4>) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |
| (5,<3,5>) | <5,6,3,5> |
| | <5,6,3,4,6,3,5>† |
| | <5,6,3,4,6,(3,4,6)*,3,5>† |
| † infeasible | |



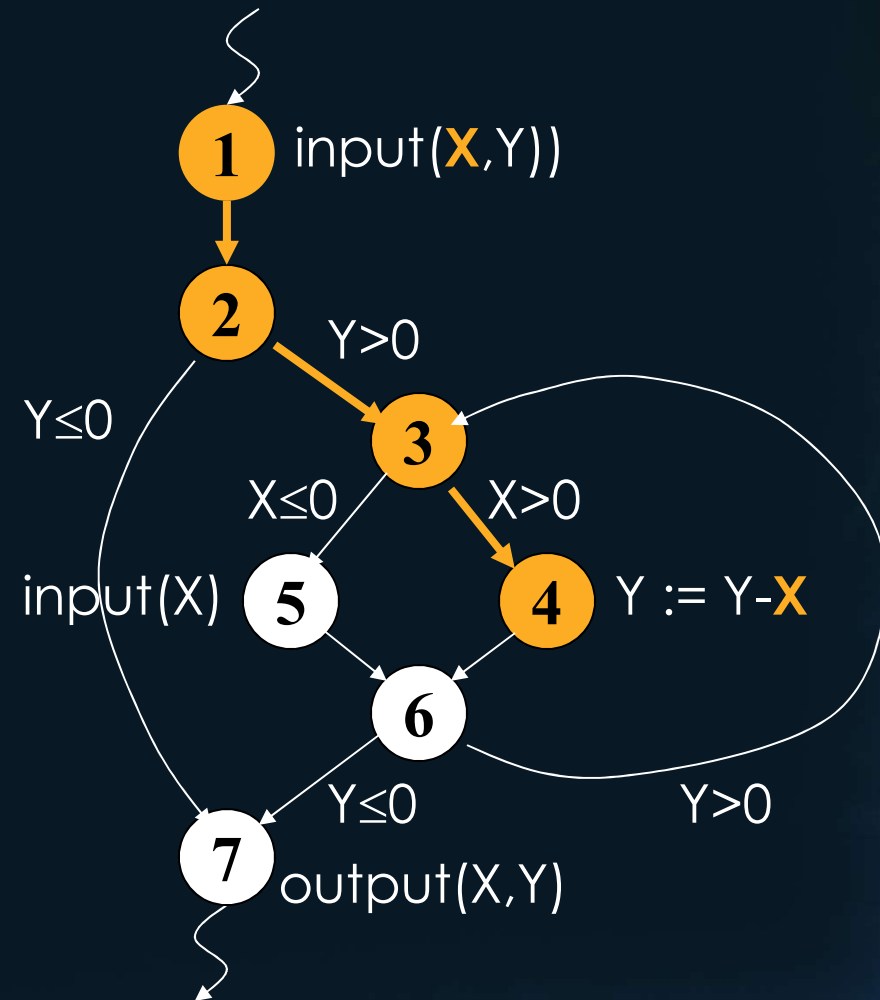
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|------------------------|
| (1,4) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,7) | <1,2,7> |
| | <1,2,3,4,6,7> |
| | <1,2,3,4,6,(3,4,6)*,7> |
| (1,<3,4>) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,<3,5>) | <1,2,3,5> |
| (5,4) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |



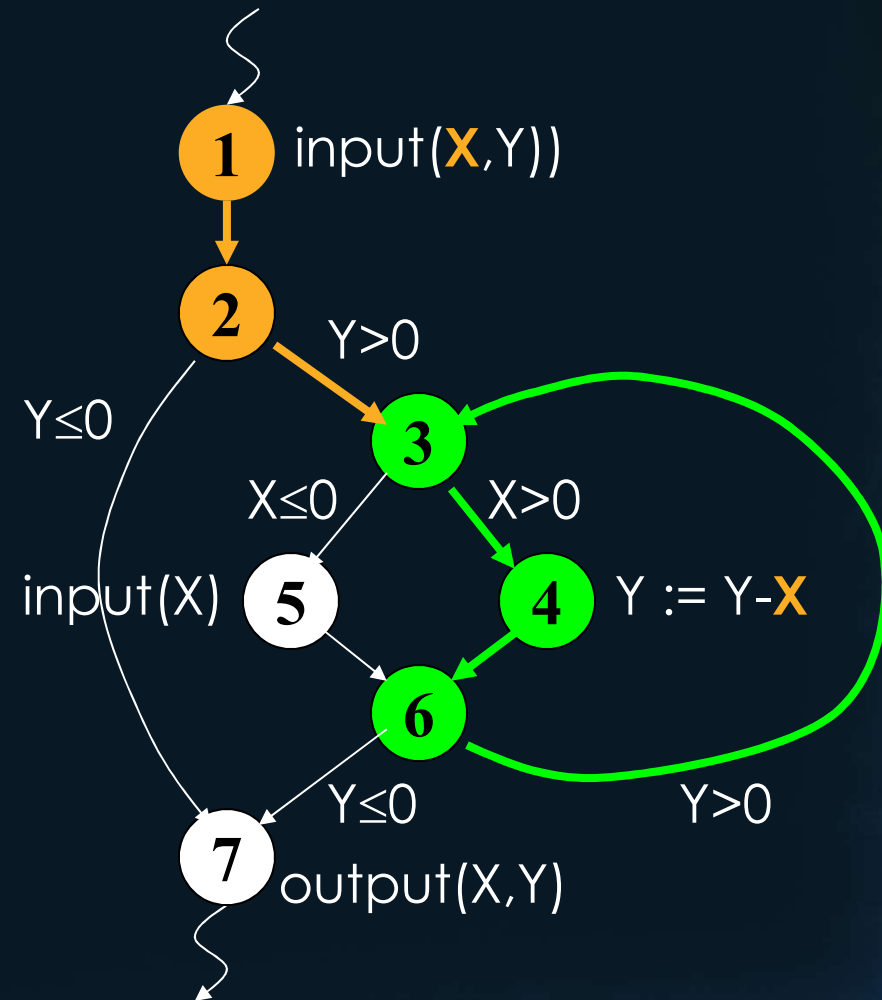
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|------------------------|
| (1,4) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,7) | <1,2,7> |
| | <1,2,3,4,6,7> |
| | <1,2,3,4,6,(3,4,6)*,7> |
| (1,<3,4>) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,<3,5>) | <1,2,3,5> |
| (5,4) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |



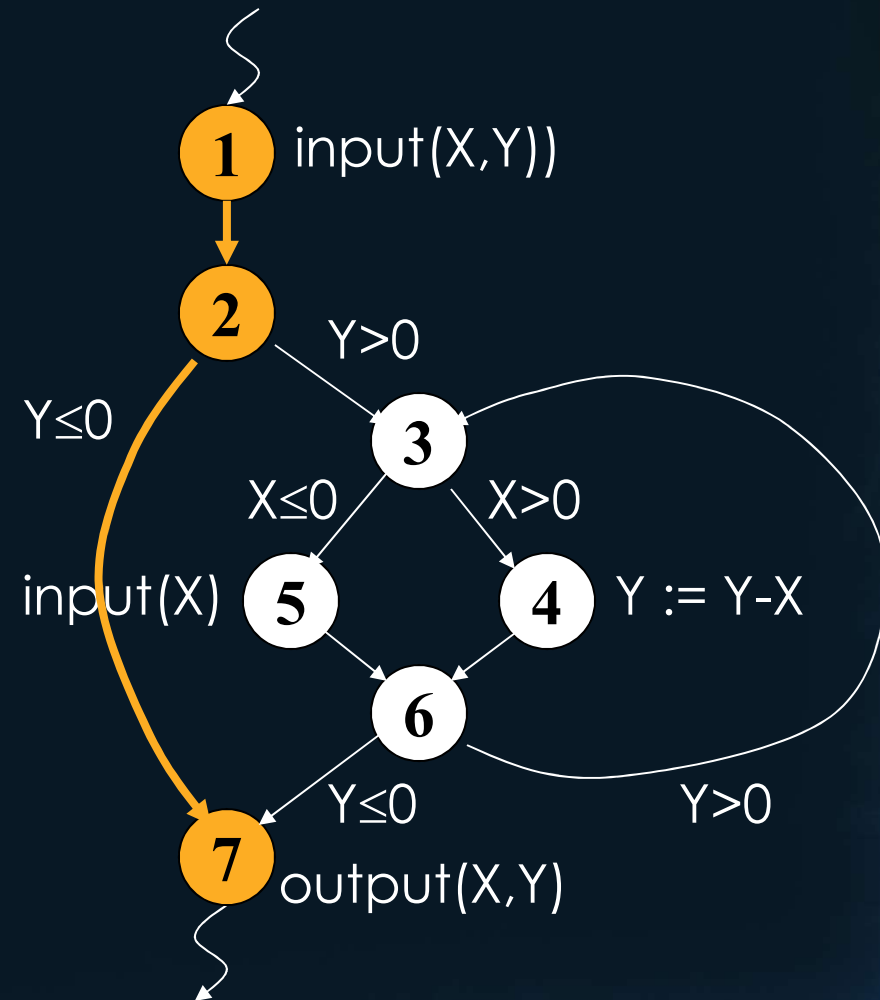
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|------------------------|
| (1,4) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,7) | <1,2,7> |
| | <1,2,3,4,6,7> |
| | <1,2,3,4,6,(3,4,6)*,7> |
| (1,<3,4>) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,<3,5>) | <1,2,3,5> |
| (5,4) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |



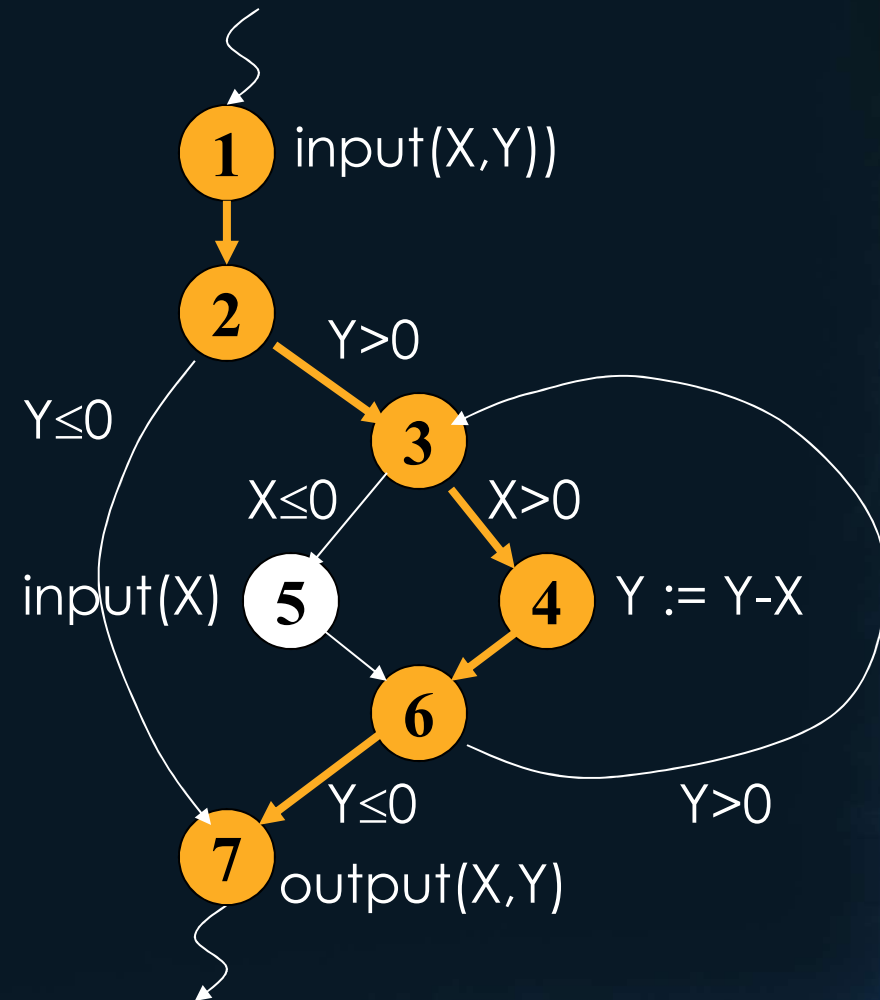
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|------------------------|
| (1,4) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,7) | <1,2,7> |
| | <1,2,3,4,6,7> |
| | <1,2,3,4,6,(3,4,6)*,7> |
| (1,<3,4>) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,<3,5>) | <1,2,3,5> |
| (5,4) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |



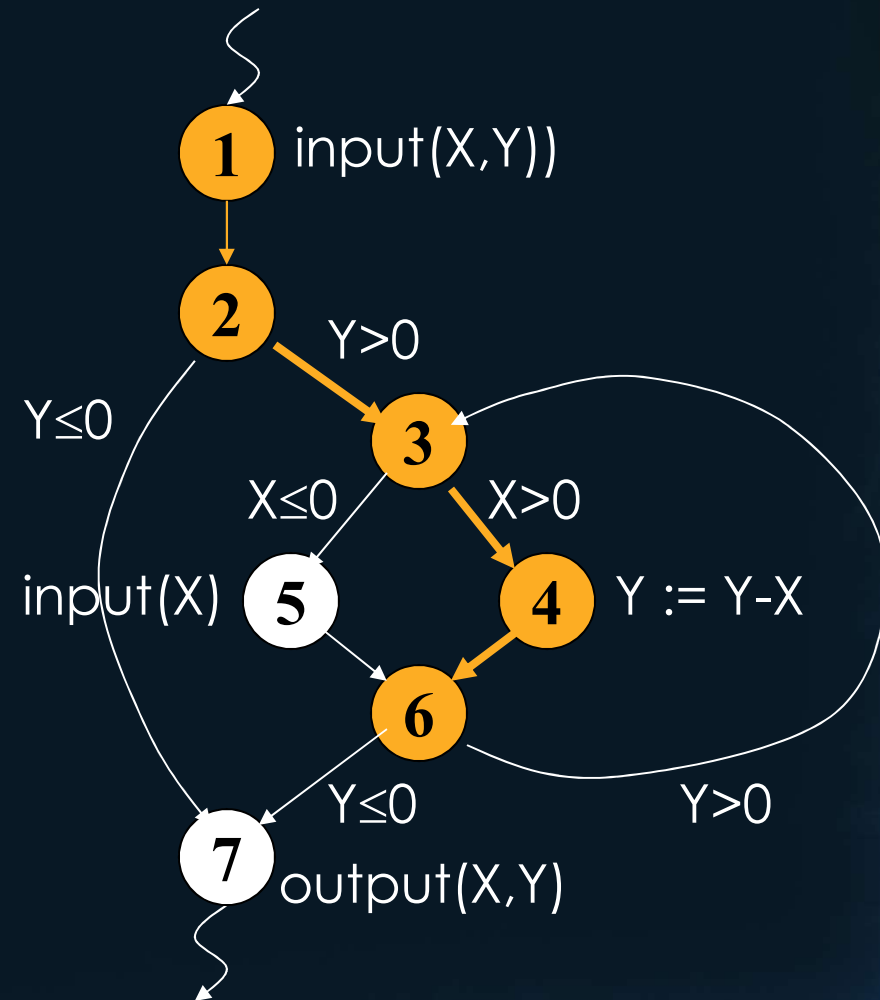
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|----------------------------|
| (1,4) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,7) | <1,2,7> |
| | <1,2,3,4,6,7> |
| | <1,2,3,4,6,(3,4,6)*,7> |
| (1,<3,4>) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,<3,5>) | <1,2,3,5> |
| (5,4) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |



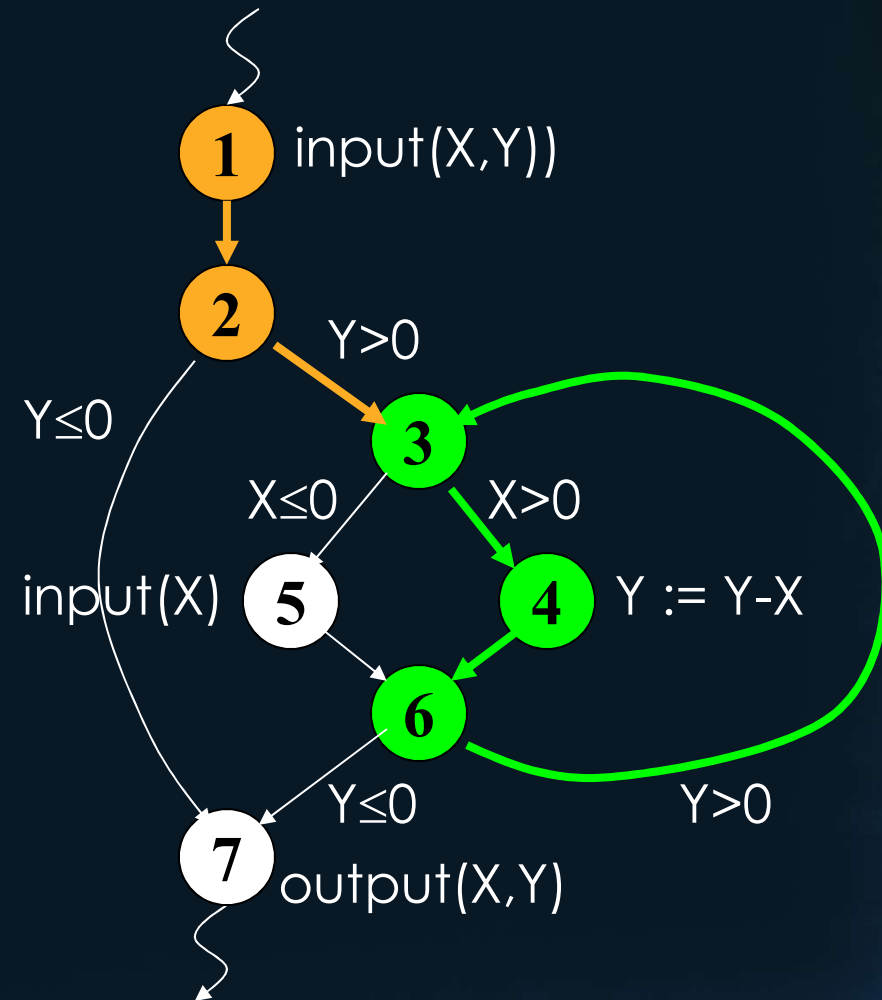
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|-------------------------------------|
| (1,4) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,7) | <1,2,7> |
| | <1,2,3,4,6,7> |
| | <1,2,3,4,6,(3,4,6)*,7> |
| (1,<3,4>) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,<3,5>) | <1,2,3,5> |
| (5,4) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |



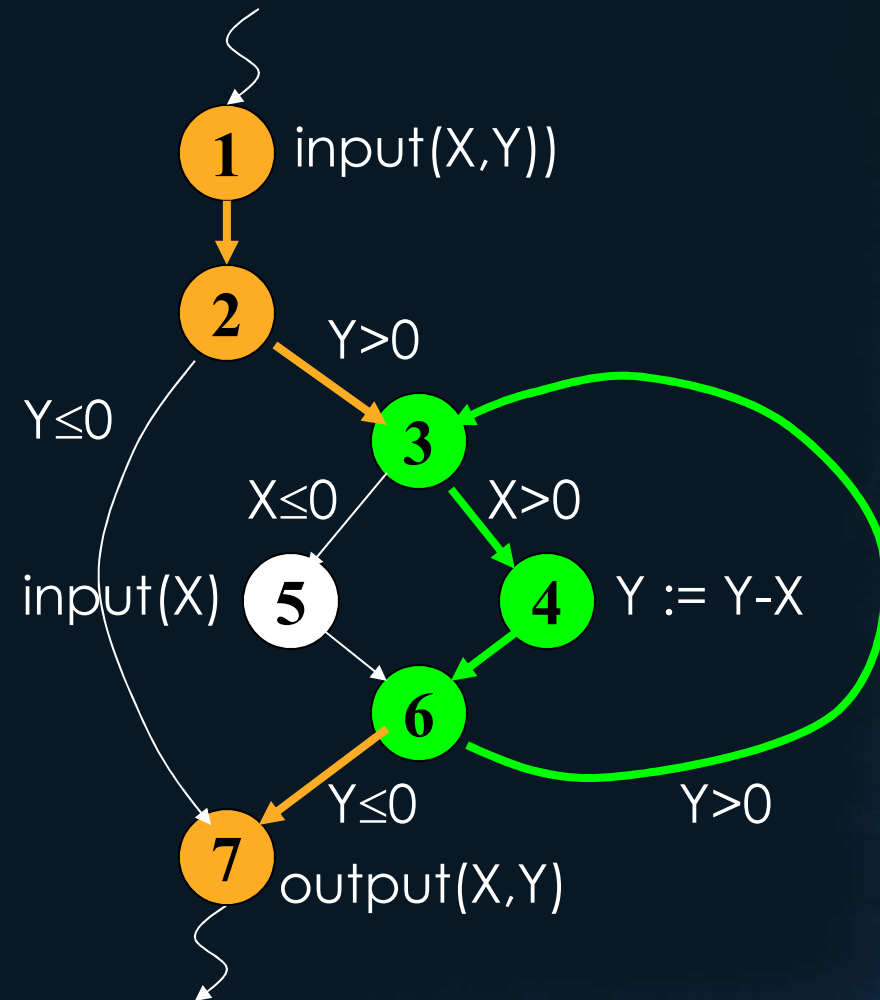
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|-------------------------------------|
| (1,4) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,7) | <1,2,7> |
| | <1,2,3,4,6,7> |
| | <1,2,3,4,6,(3,4,6)*,7> |
| (1,<3,4>) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,<3,5>) | <1,2,3,5> |
| (5,4) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |



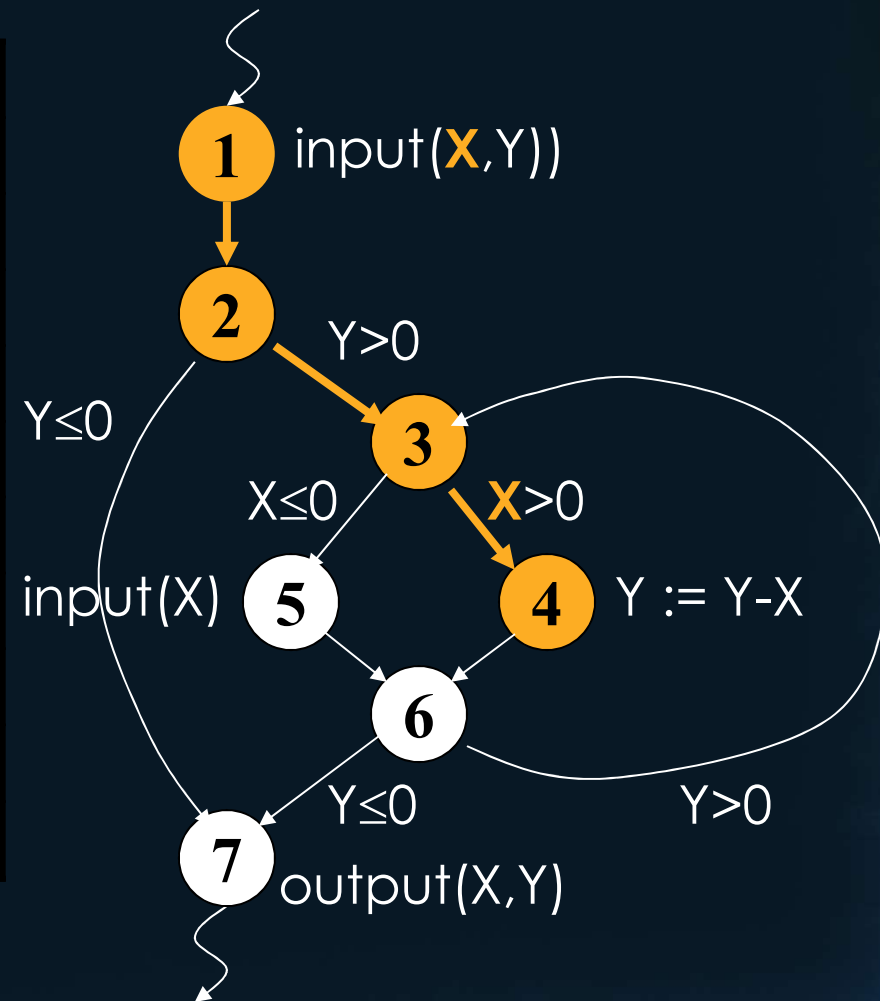
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|-------------------------------------|
| (1,4) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,7) | <1,2,7> |
| | <1,2,3,4,6,7> |
| | <1,2,3,4,6,(3,4,6)*,7> |
| (1,<3,4>) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,<3,5>) | <1,2,3,5> |
| (5,4) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |



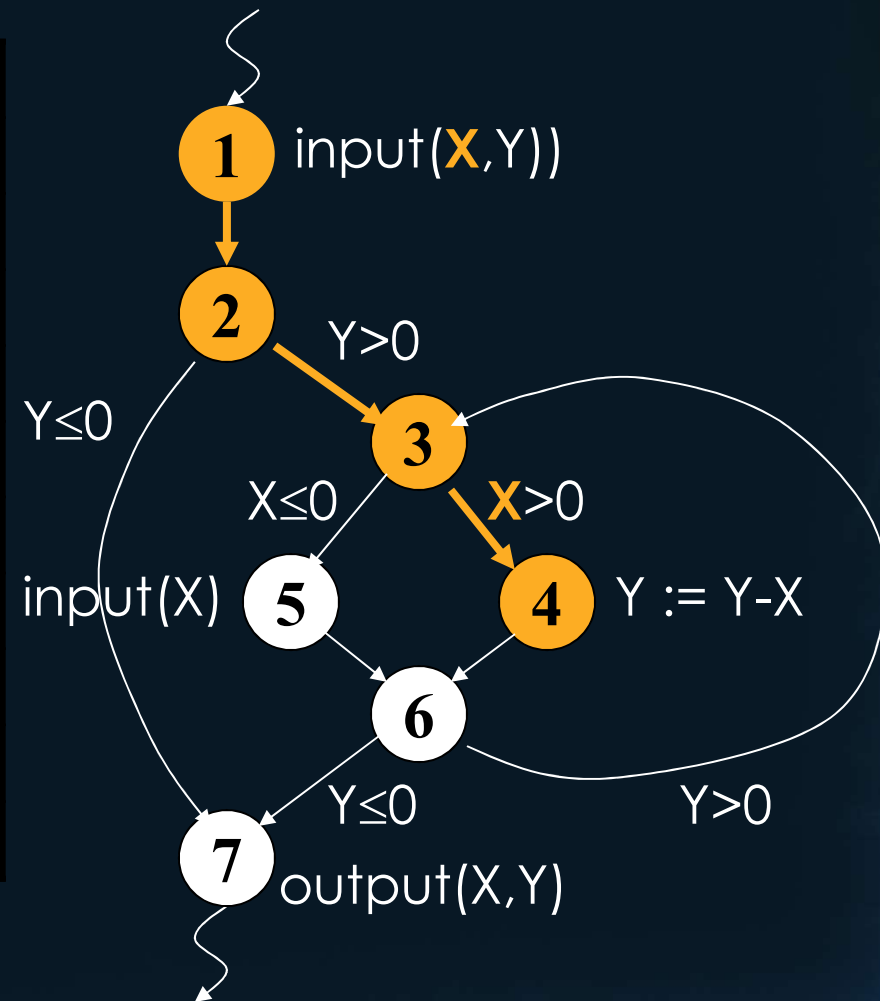
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|------------------------|------------------------|
| (1,4) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,7) | <1,2,7> |
| | <1,2,3,4,6,7> |
| | <1,2,3,4,6,(3,4,6)*,7> |
| (1,<3,4>) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,<3,5>) | <1,2,3,5> |
| (5,4) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |



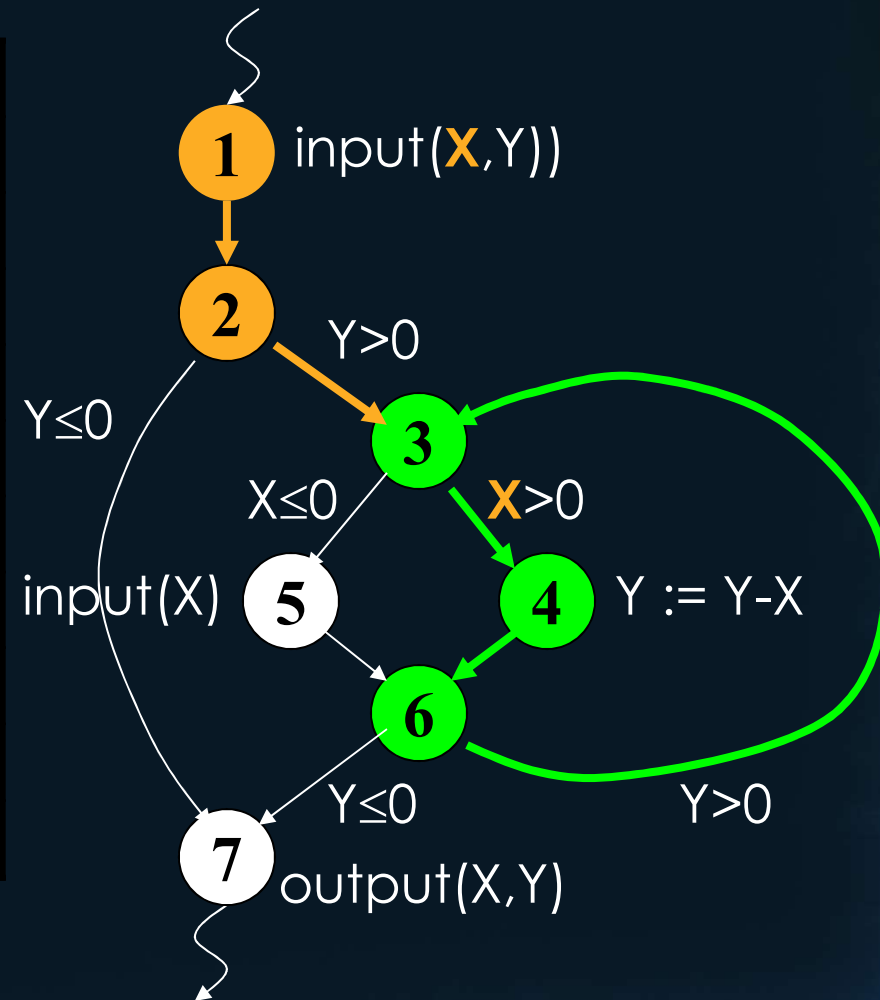
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|------------------------|---------------------------------|
| (1,4) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,7) | <1,2,7> |
| | <1,2,3,4,6,7> |
| | <1,2,3,4,6,(3,4,6)*,7> |
| (1,<3,4>) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,<3,5>) | <1,2,3,5> |
| (5,4) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |



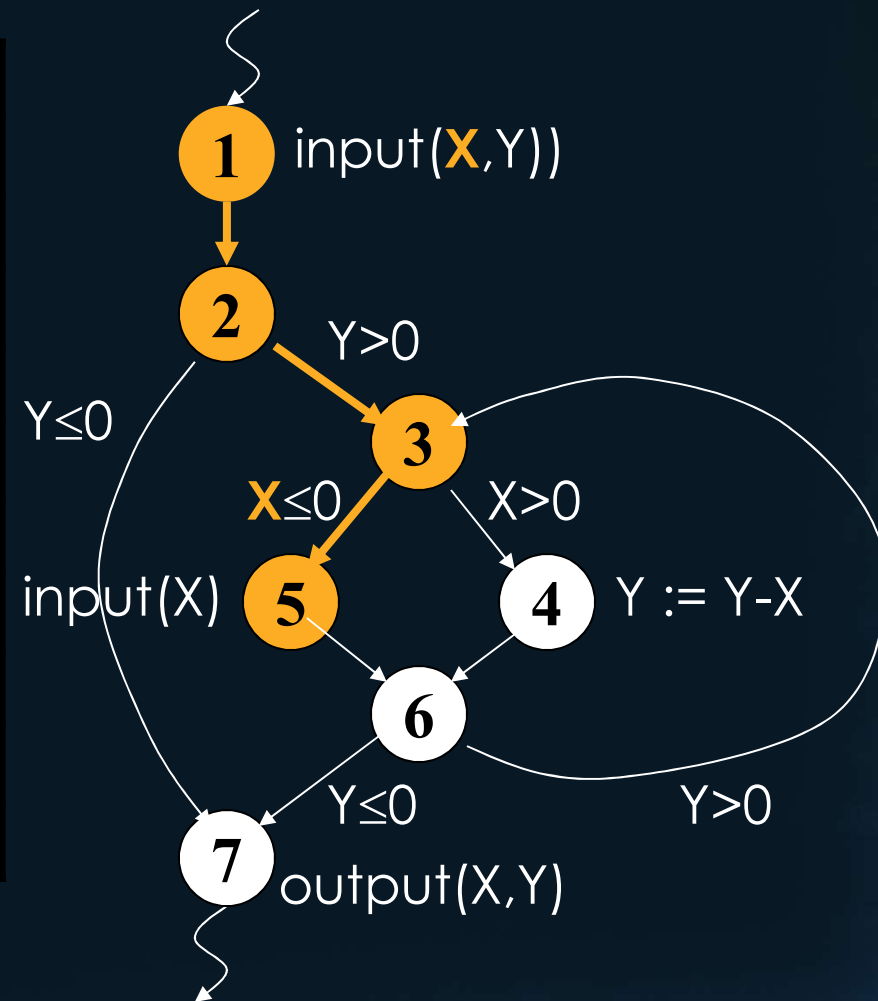
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|------------------------|---------------------------------|
| (1,4) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,7) | <1,2,7> |
| | <1,2,3,4,6,7> |
| | <1,2,3,4,6,(3,4,6)*,7> |
| (1,<3,4>) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,<3,5>) | <1,2,3,5> |
| (5,4) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |



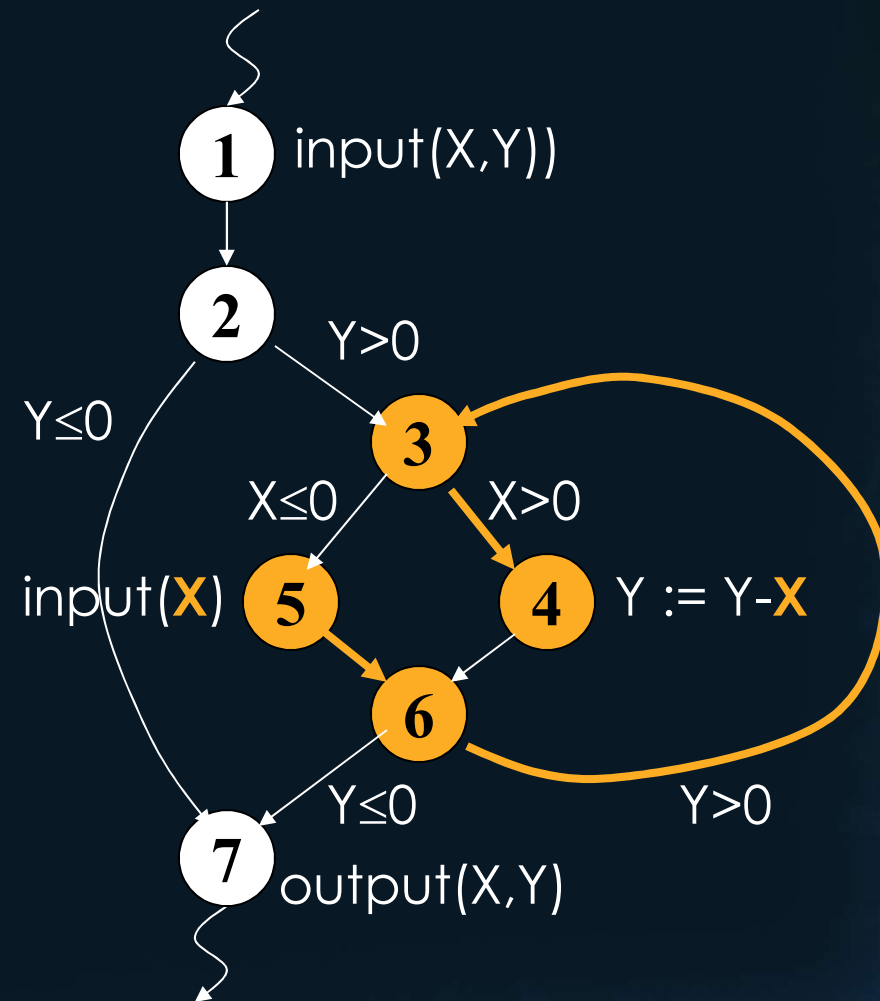
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|------------------------|------------------------|
| (1,4) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,7) | <1,2,7> |
| | <1,2,3,4,6,7> |
| | <1,2,3,4,6,(3,4,6)*,7> |
| (1,<3,4>) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,<3,5>) | <1,2,3,5> |
| (5,4) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |



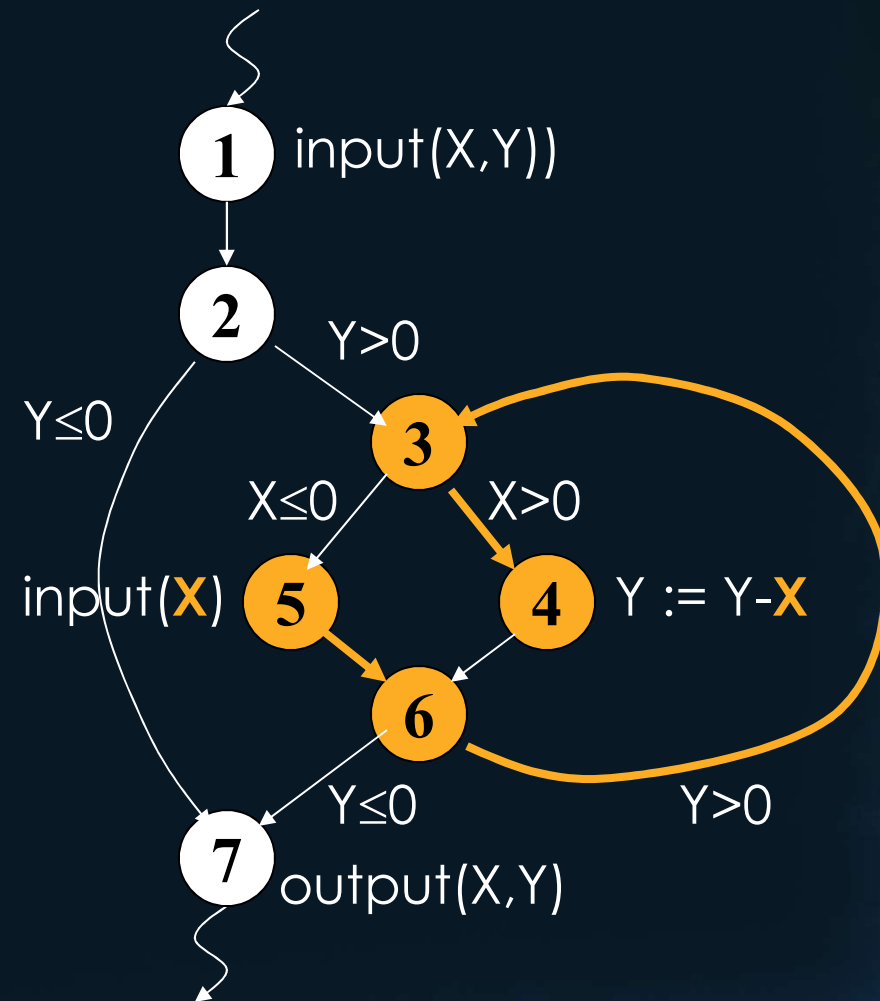
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|------------------------|
| (1,4) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,7) | <1,2,7> |
| | <1,2,3,4,6,7> |
| | <1,2,3,4,6,(3,4,6)*,7> |
| (1,<3,4>) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,<3,5>) | <1,2,3,5> |
| (5,4) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |



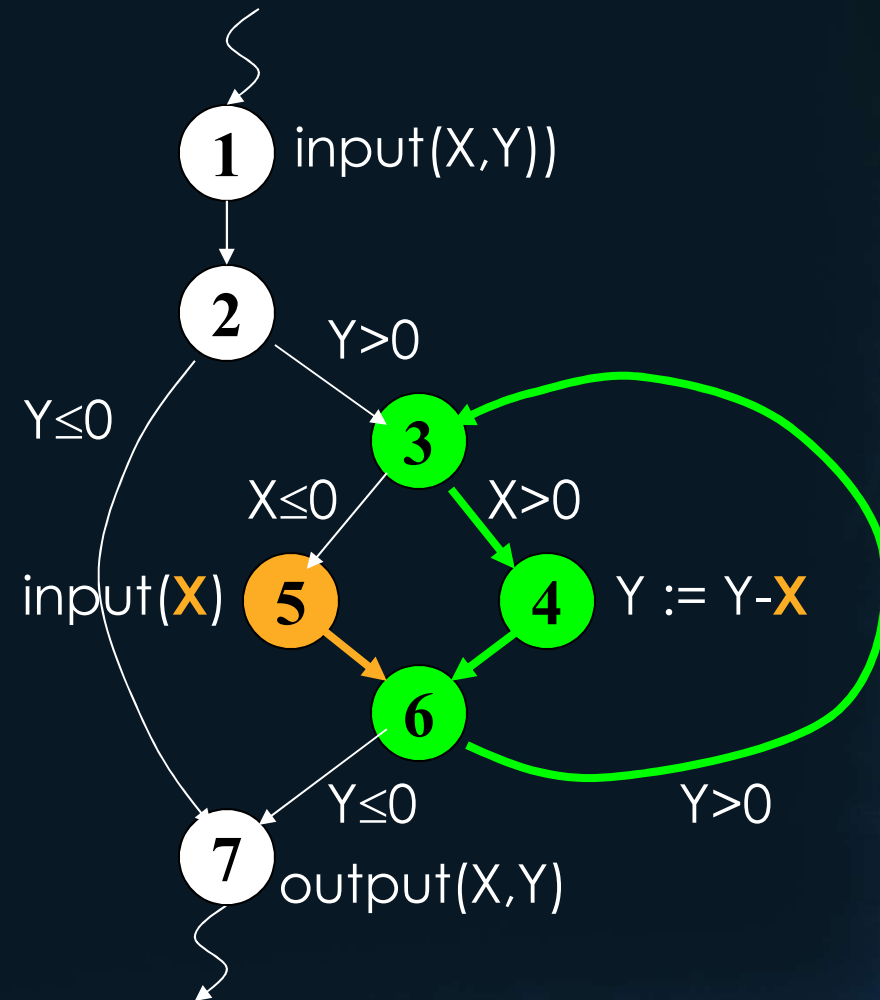
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|---------------------------------|
| (1,4) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,7) | <1,2,7> |
| | <1,2,3,4,6,7> |
| | <1,2,3,4,6,(3,4,6)*,7> |
| (1,<3,4>) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,<3,5>) | <1,2,3,5> |
| (5,4) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |



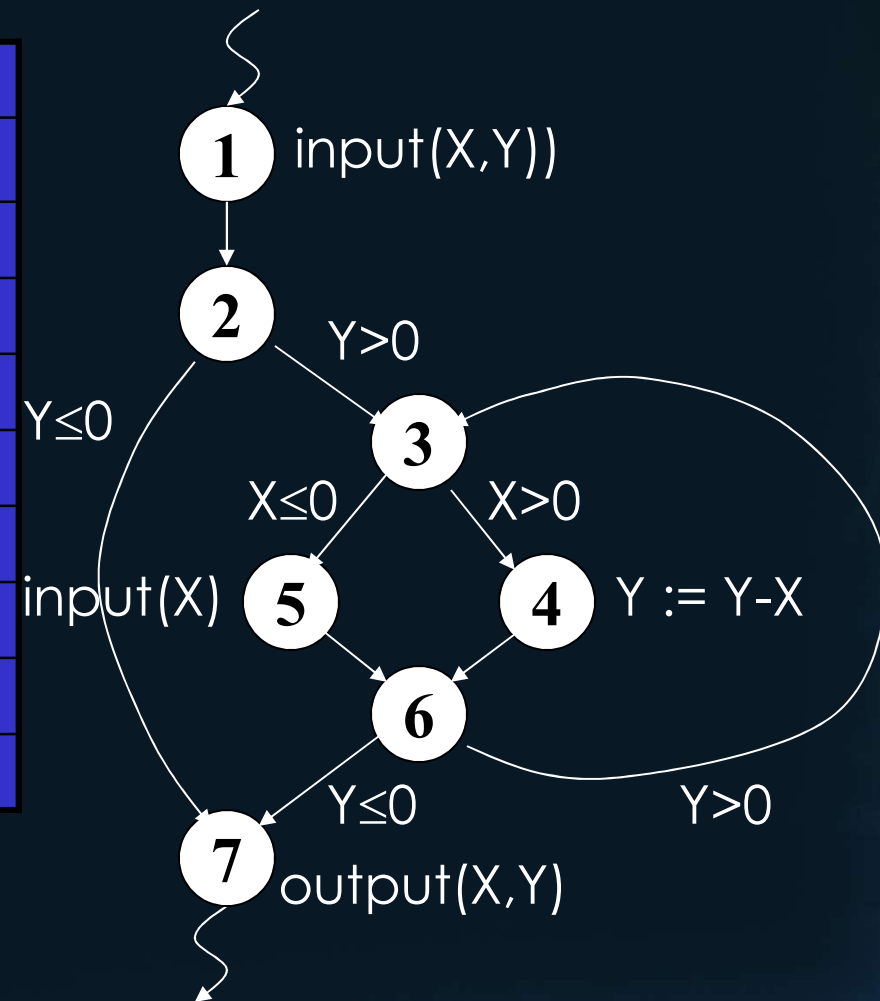
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|---------------------------------|
| (1,4) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,7) | <1,2,7> |
| | <1,2,3,4,6,7> |
| | <1,2,3,4,6,(3,4,6)*,7> |
| (1,<3,4>) | <1,2,3,4> |
| | <1,2,3,4,(6,3,4)*> |
| (1,<3,5>) | <1,2,3,5> |
| (5,4) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |



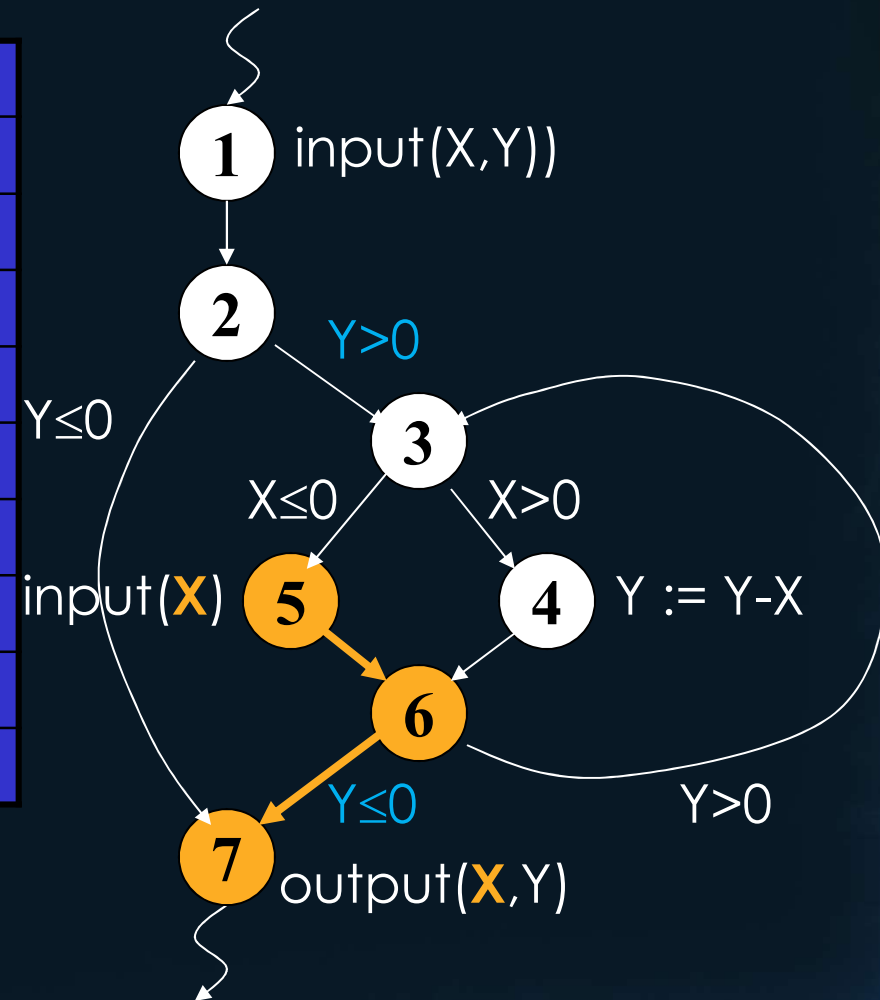
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|--------------------------|
| (5,7) | <5,6,7> |
| | <5,6,3,4,6,7> |
| | <5,6,3,4,6,(3,4,6)*,7> |
| (5,<3,4>) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |
| (5,<3,5>) | <5,6,3,5> |
| | <5,6,3,4,6,3,5> |
| | <5,6,3,4,6,(3,4,6)*,3,5> |



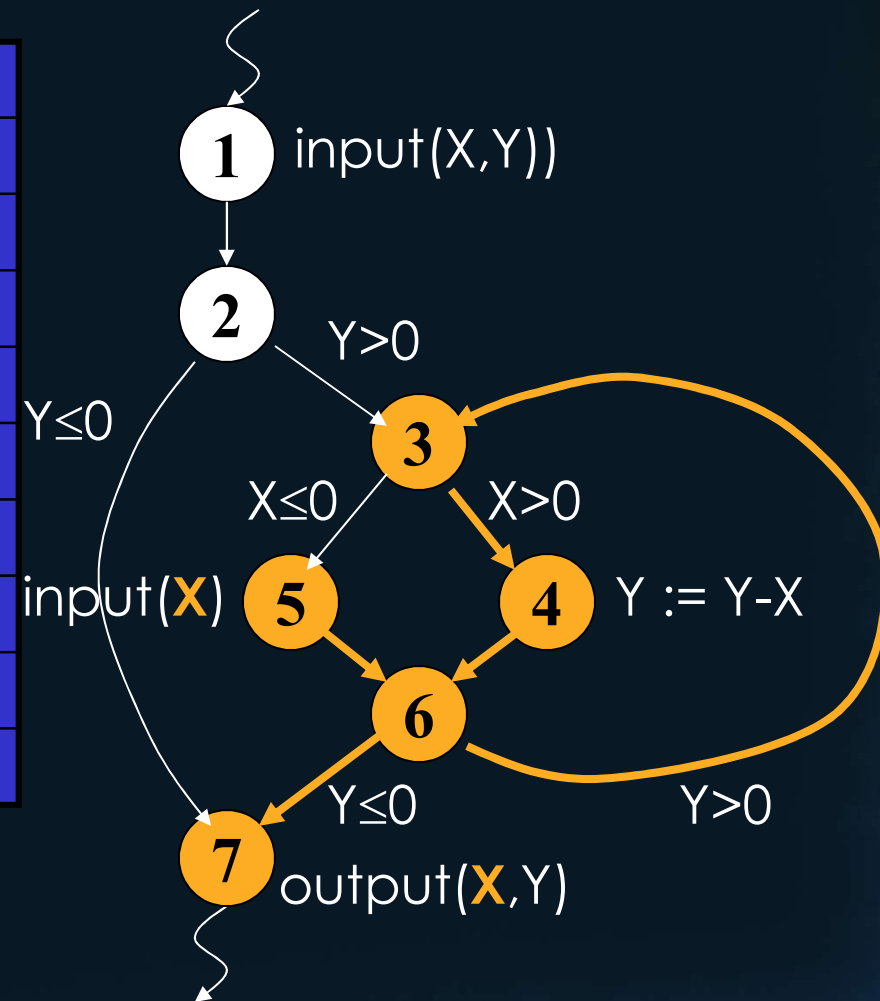
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|---------------------|--------------------------|
| (5,7) | <5,6,7> † |
| | <5,6,3,4,6,7> |
| | <5,6,3,4,6,(3,4,6)*,7> |
| (5,<3,4>) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |
| (5,<3,5>) | <5,6,3,5> |
| | <5,6,3,4,6,3,5> |
| | <5,6,3,4,6,(3,4,6)*,3,5> |
| † infeasible | |



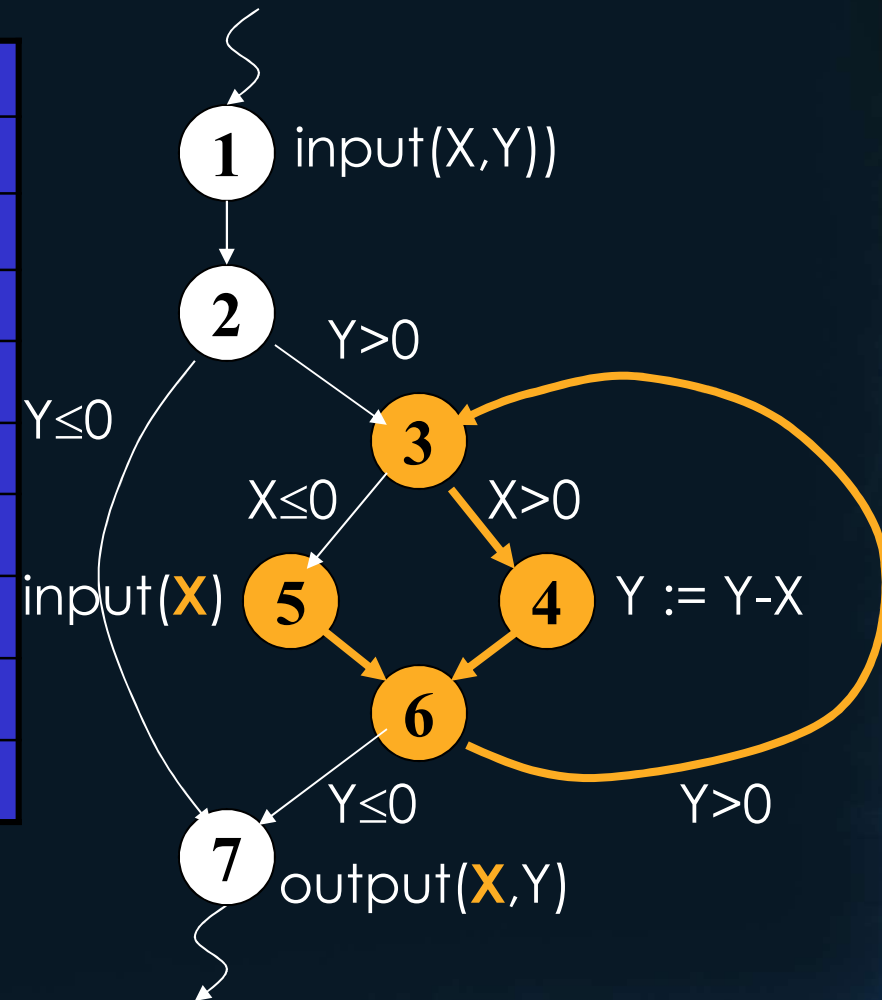
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------------------|---|
| (5,7) | $\langle 5,6,7 \rangle \dagger$ |
| | $\langle 5,6,3,4,6,7 \rangle$ |
| | $\langle 5,6,3,4,6,(3,4,6)^*,7 \rangle$ |
| $(5, \langle 3,4 \rangle)$ | $\langle 5,6,3,4 \rangle$ |
| | $\langle 5,6,3,4,(6,3,4)^* \rangle$ |
| $(5, \langle 3,5 \rangle)$ | $\langle 5,6,3,5 \rangle$ |
| | $\langle 5,6,3,4,6,3,5 \rangle$ |
| | $\langle 5,6,3,4,6,(3,4,6)^*,3,5 \rangle$ |
| \dagger infeasible | |



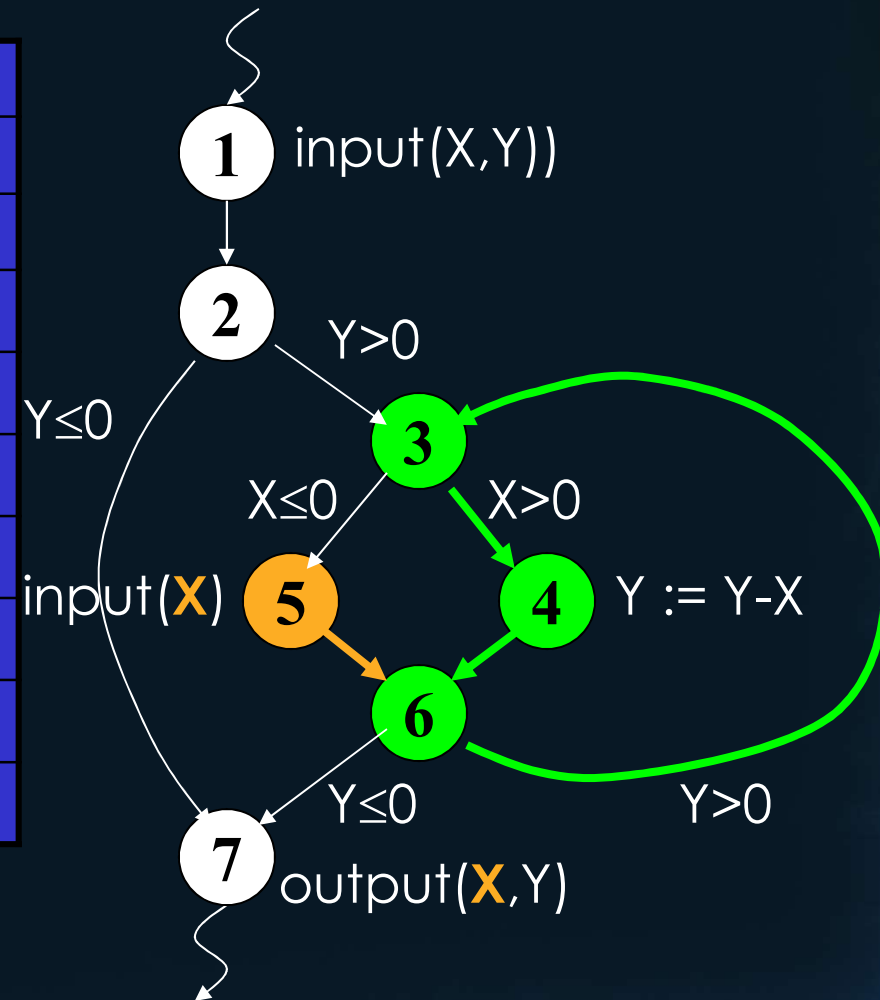
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------------------|---|
| (5,7) | $\langle 5,6,7 \rangle \dagger$ |
| | $\langle 5,6,3,4,6,7 \rangle$ |
| | $\langle 5,6,3,4,6,(3,4,6)^*,7 \rangle$ |
| $(5, \langle 3,4 \rangle)$ | $\langle 5,6,3,4 \rangle$ |
| | $\langle 5,6,3,4,(6,3,4)^* \rangle$ |
| $(5, \langle 3,5 \rangle)$ | $\langle 5,6,3,5 \rangle$ |
| | $\langle 5,6,3,4,6,3,5 \rangle$ |
| | $\langle 5,6,3,4,6,(3,4,6)^*,3,5 \rangle$ |
| \dagger infeasible | |



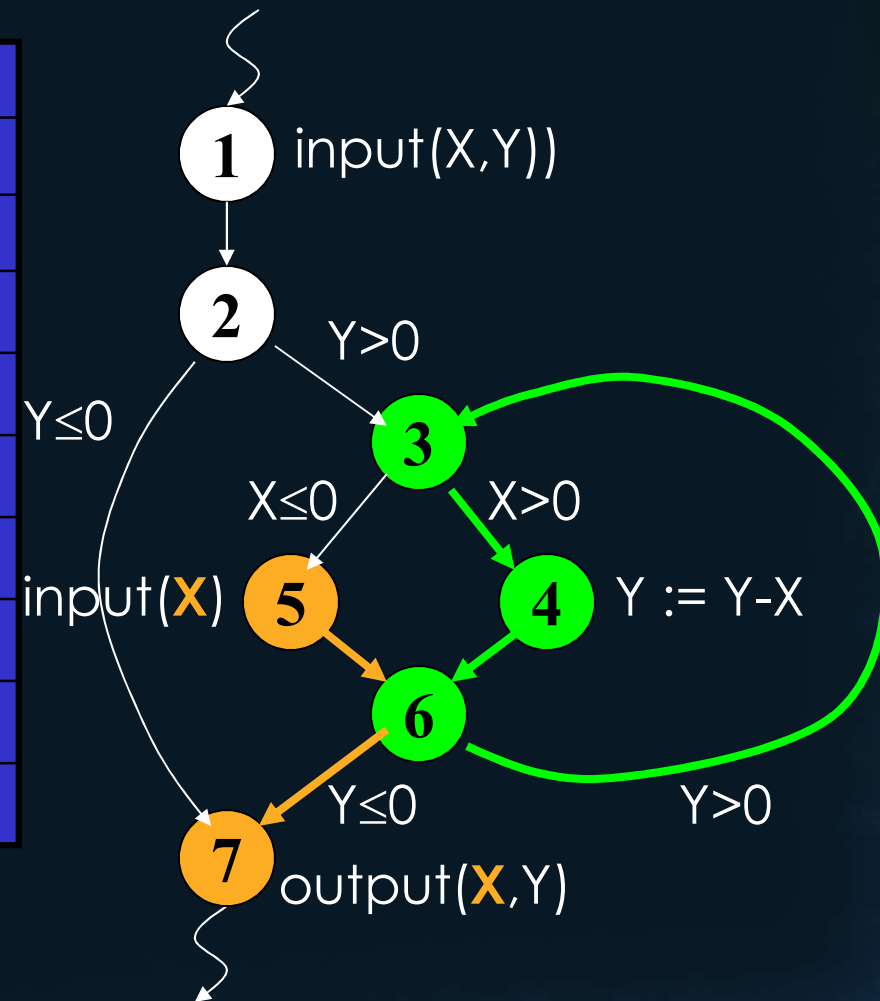
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|-------------------------------------|
| (5,7) | <5,6,7> † |
| | <5,6,3,4,6,7> |
| | <5,6,3,4,6,(3,4,6)*,7> |
| (5,<3,4>) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |
| (5,<3,5>) | <5,6,3,5> |
| | <5,6,3,4,6,3,5> |
| | <5,6,3,4,6,(3,4,6)*,3,5> |
| † infeasible | |



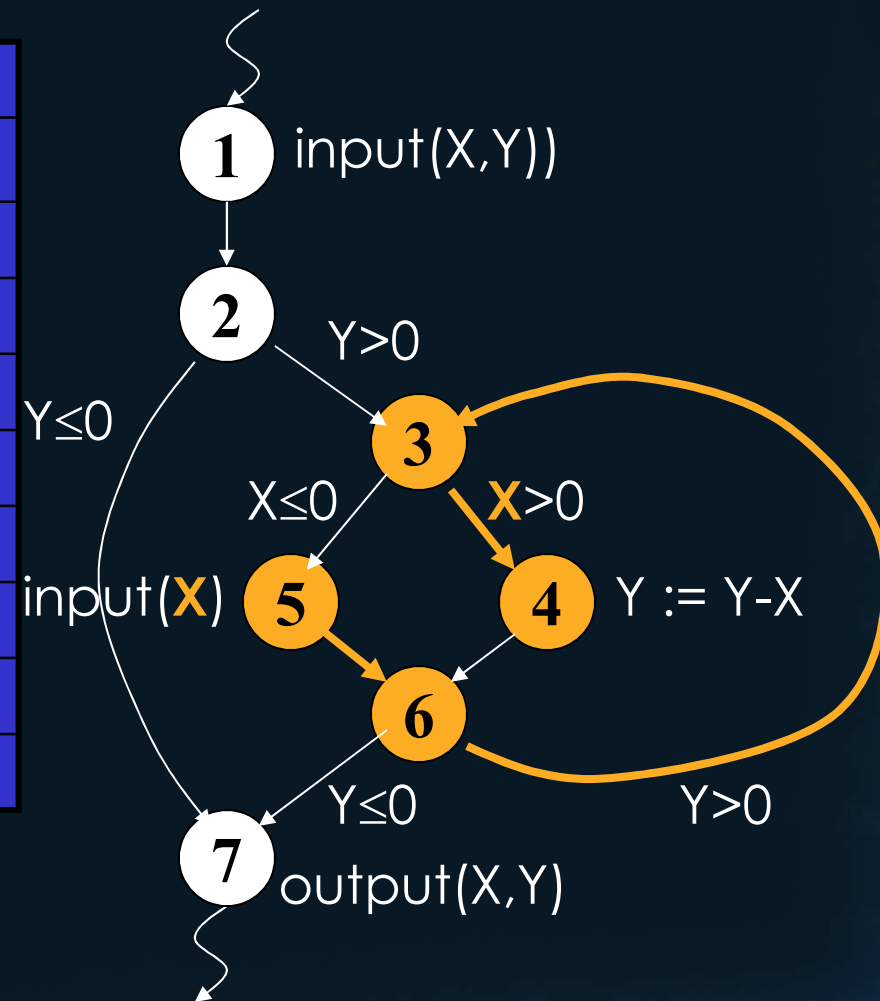
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|----------------|-------------------------------------|
| (5,7) | <5,6,7> † |
| | <5,6,3,4,6,7> |
| | <5,6,3,4,6,(3,4,6)*,7> |
| (5,<3,4>) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |
| (5,<3,5>) | <5,6,3,5> |
| | <5,6,3,4,6,3,5> |
| | <5,6,3,4,6,(3,4,6)*,3,5> |
| † infeasible | |



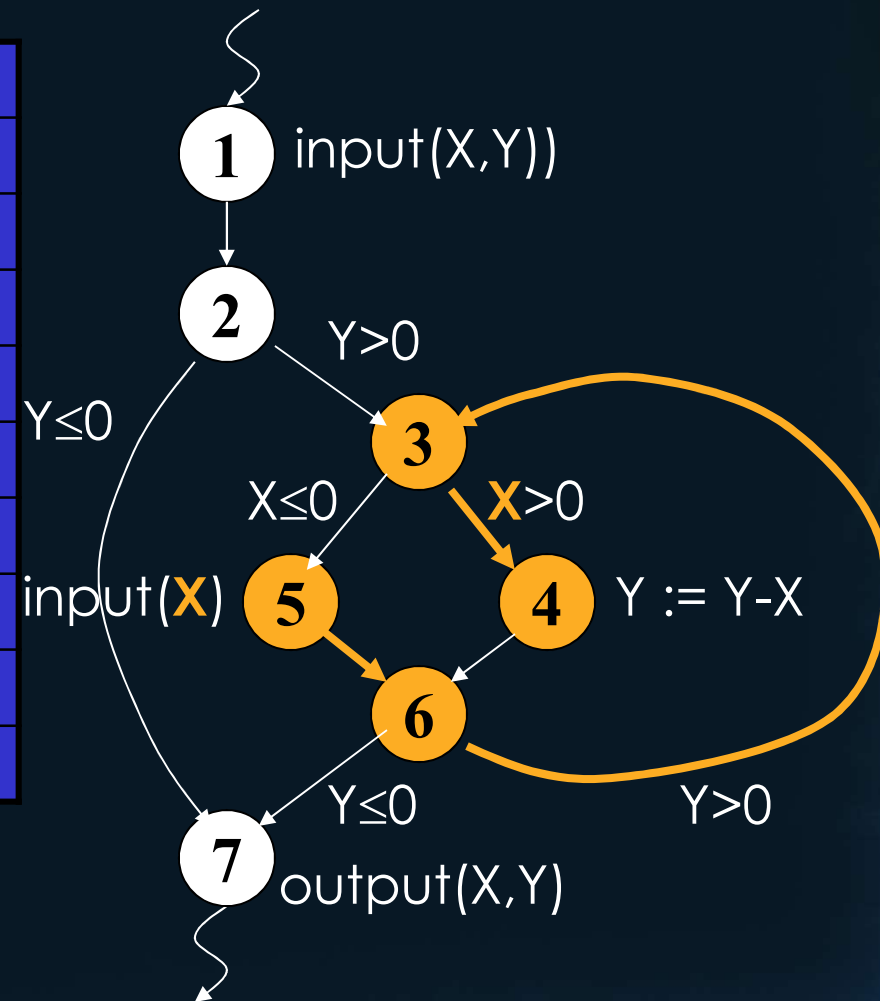
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|------------------------|--------------------------|
| (5,7) | <5,6,7> † |
| | <5,6,3,4,6,7> |
| | <5,6,3,4,6,(3,4,6)*,7> |
| (5,<3,4>) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |
| (5,<3,5>) | <5,6,3,5> |
| | <5,6,3,4,6,3,5> |
| | <5,6,3,4,6,(3,4,6)*,3,5> |
| † infeasible | |



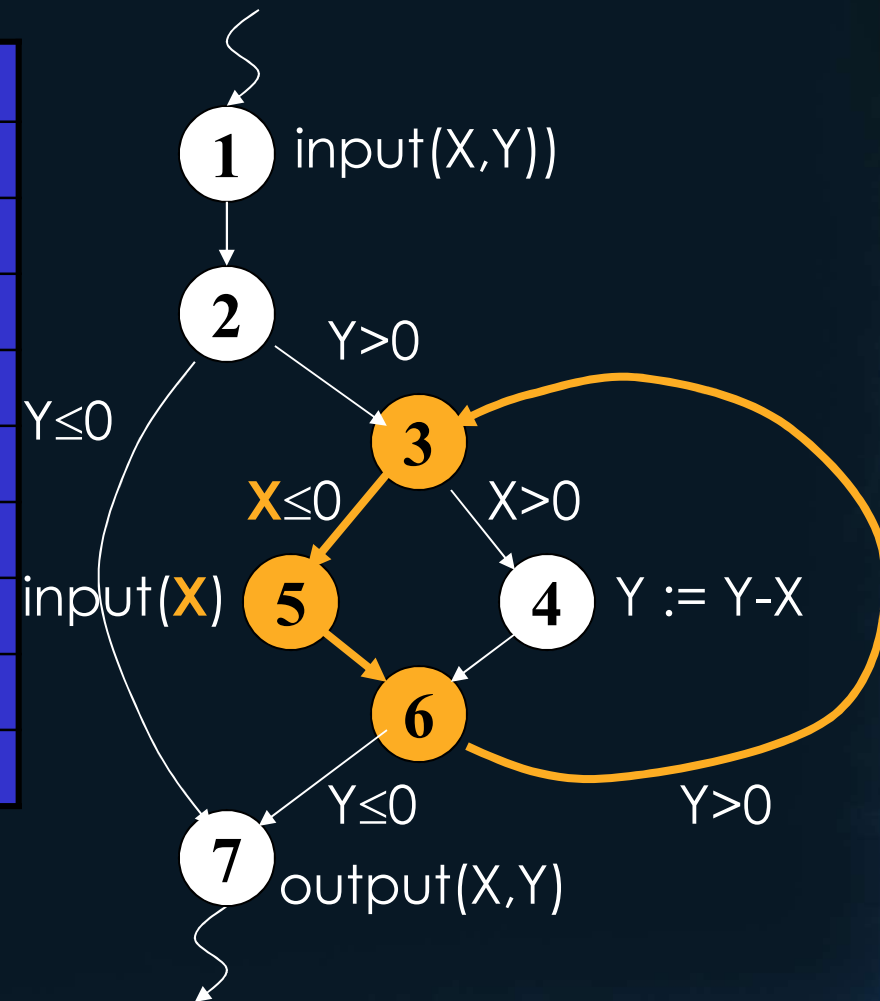
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|------------------------|---------------------------------|
| (5,7) | <5,6,7> † |
| | <5,6,3,4,6,7> |
| | <5,6,3,4,6,(3,4,6)*7> |
| (5,<3,4>) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |
| (5,<3,5>) | <5,6,3,5> |
| | <5,6,3,4,6,3,5> |
| | <5,6,3,4,6,(3,4,6)*,3,5> |
| † infeasible | |



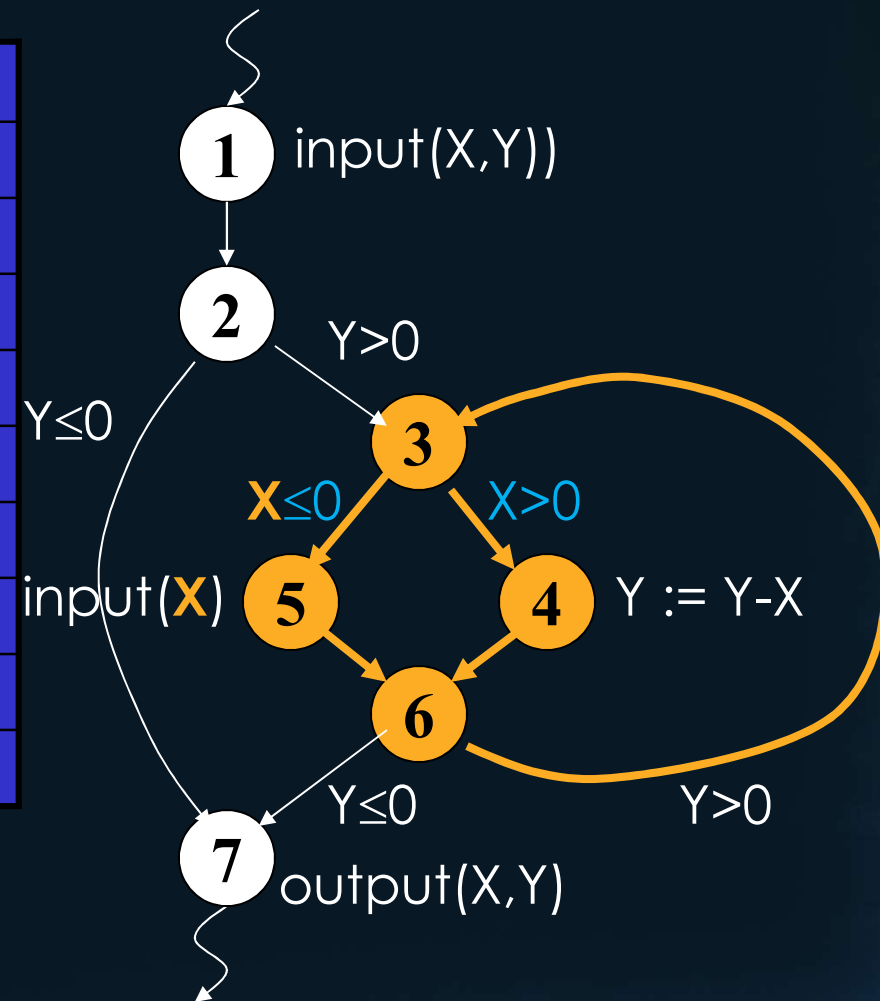
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|------------------------|--------------------------|
| (5,7) | <5,6,7> † |
| | <5,6,3,4,6,7> |
| | <5,6,3,4,6,(3,4,6)*7> |
| (5,<3,4>) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |
| (5,<3,5>) | <5,6,3,5> |
| | <5,6,3,4,6,3,5> |
| | <5,6,3,4,6,(3,4,6)*,3,5> |
| † infeasible | |



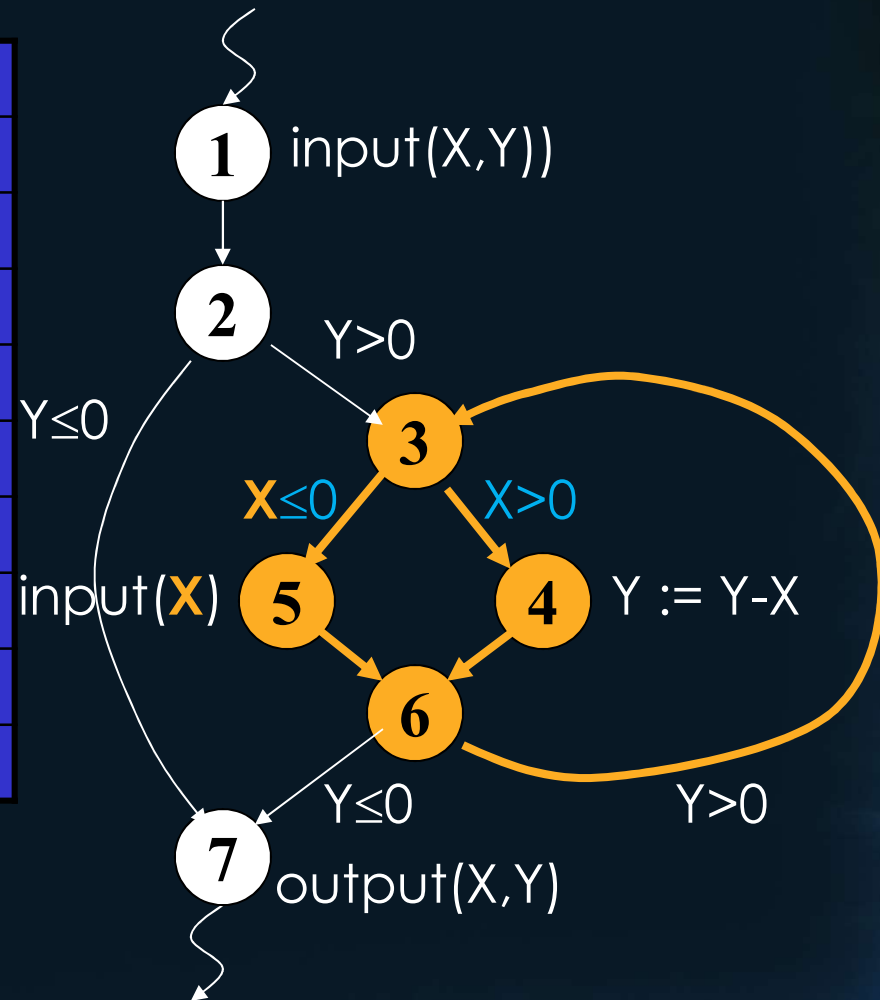
Identifying DU-Pairs – Variable X

| <u>du-pair</u> | <u>path(s)</u> |
|------------------------|--------------------------------|
| (5,7) | <5,6,7> † |
| | <5,6,3,4,6,7> |
| | <5,6,3,4,6,(3,4,6)*7> |
| (5,<3,4>) | <5,6,3,4> |
| | <5,6,3,4,(6,3,4)*> |
| (5,<3,5>) | <5,6,3,5> |
| | <5,6,3,4,6,3,5> † |
| | <5,6,3,4,6,(3,4,6)*,3,5> |
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| (5,<3,5>) | <5,6,3,5> |
| | <5,6,3,4,6,3,5> † |
| | <5,6,3,4,6,(3,4,6)*,3,5> † |
| † infeasible | |



More Dataflow Terms and Definitions

- A path (either partial or complete) is **simple** if all edges within the path are distinct (i.e., different).
- A path is **loop-free** if all nodes within the path are distinct (i.e., different).

Simple and Loop-Free Paths

| path | Simple? | Loop-free? |
|---------------------------------|---------|------------|
| $\langle 1, 3, 4, 2 \rangle$ | Yes | Yes |
| $\langle 1, 2, 3, 2 \rangle$ | Yes | No |
| $\langle 1, 2, 3, 1, 2 \rangle$ | No | No |
| $\langle 1, 2, 3, 2, 4 \rangle$ | Yes | No |

Simple and Loop-Free Paths (cont'd)

Which is *stronger*, **simple** or **loop-free**?

环路为1

无环路

More Dataflow Terms and Definitions

A path $\langle n_1, n_2, \dots, n_j, n_k \rangle$ is a **du-path** with respect to a variable v if v is defined at node n_1 and either:

1. there is a **c-use** of v at node n_k and $\langle n_1, n_2, \dots, n_j, n_k \rangle$ is a def-clear **simple** path,

or

1. there is a **p-use** of v at edge $\langle n_j, n_k \rangle$ and $\langle n_1, n_2, \dots, n_j \rangle$ is a def-clear **loop-free** path.

NOTE!

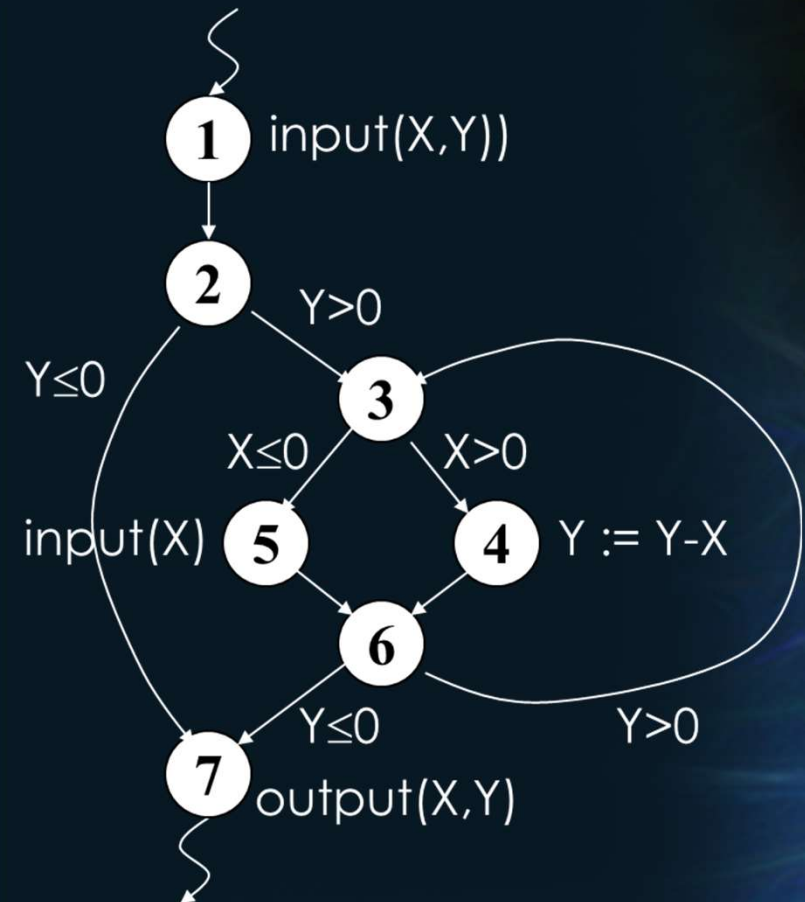


Identifying du-paths

c-use

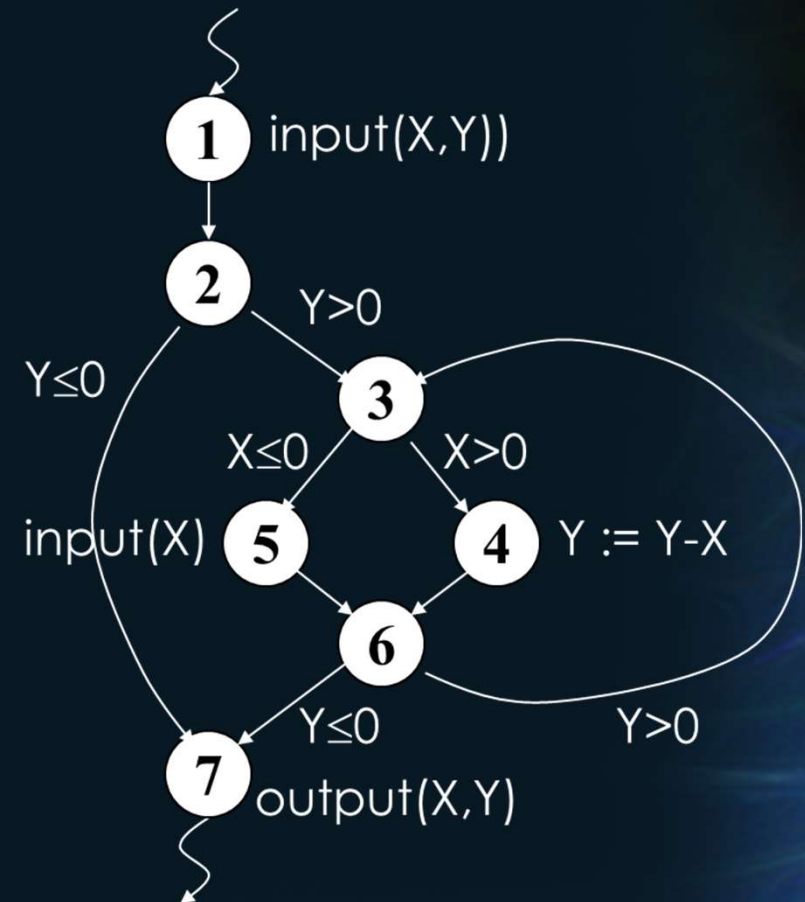
| <u>du-pair</u> | <u>path(s)</u> | <u>du-path?</u> |
|----------------|------------------------|-----------------|
| X: (1,4) | <1,2,3,4> | Yes |
| | <1,2,3,4,(6,3,4)*> | No |
| X: (1,7) | <1,2,7> | Yes |
| | <1,2,3,4,6,7> | Yes |
| | <1,2,3,4,6,(3,4,6)*,7> | No |
| X: (1,<3,4>) | <1,2,3,4> | Yes |
| | <1,2,3,4,(6,3,4)*> | No |
| X: (1,<3,5>) | <1,2,3,5> | Yes |
| X: (5,4) | <5,6,3,4> | Yes |
| | <5,6,3,4,(6,3,4)*> | No |

p-use



Identifying du-paths

| <u>du-pair</u> | <u>path(s)</u> | <u>du-path?</u> |
|----------------|----------------------------|-----------------|
| X: (5,7) | <5,6,7> † | Yes |
| simple | <5,6,3,4,6,7> | Yes |
| | <5,6,3,4,6,(3,4,6)*,7> | No |
| X: (5,<3,4>) | <5,6,3,4> | Yes |
| | <5,6,3,4,(6,3,4)*> | No |
| X: (5,<3,5>) | <5,6,3,5> | Yes |
| Loop free | <5,6,3,4,6,3,5> † | No |
| | <5,6,3,4,6,(3,4,6)*,3,5> † | No |
| † infeasible | | |



Another Dataflow Test Coverage Criterion

- ***All-DU-Paths:*** for every program variable v , **every** du-path from every definition of v to every c-use and every p-use of v must be covered.

Exercise

- Identify du pairs, all c-uses and p-uses for **variable Y** in Exercise.
- Identify whether or not each def-clear path is feasible, and whether or not it is a du-path.
- Finally, receive the test suite to satisfy **All-DU-Paths** of this program.

Recall

- **All-Defs:** for every program variable v , at least one def-clear path from every definition of v to at least one c-use or one p-use of v must be covered.
- **All-Uses:** for every program variable v , at least one def-clear path from every definition of v to every c-use and every p-use of v must be covered.
- **All-DU-Paths:** for every program variable v , every du-path from every definition of v to every c-use and every p-use of v must be covered.

Summary of White-Box Coverage Relationships





The Commission Problem

A rifle salesperson sells rifle locks, stocks, and barrels. Locks cost \$45, stocks cost \$30, and barrels cost \$25. The salesperson had to sell at least one complete rifle per month, and production limits were such that the most the salesperson could sell in a month was 70 locks, 80 stocks, and 90 barrels.

Suppose the commission is computed as follows: 10% on sales up to (and including) \$1000, 15% on the next \$800, and 20% on any sales in excess of \$1800.

The commission program produces a monthly sales report that gave the total number of locks, stocks, and barrels sold, the salesperson's total dollar sales, and, finally, the commission.

佣金程序的问题描述

- 步枪销售商在亚利桑那州境内销售制造商制造的步枪锁、准星和枪管
- 枪锁卖45美元，准星卖30美元，枪管卖25美元
- 销售商每月至少要售出一枝完整的步枪，生产限额考虑到大多数销售商在一个月內可销售70个枪锁、80个准星和90个枪管
- 销售商在每访问一个镇子之后，给制造商发出电报，说明在那个镇子中售出的枪锁、准星和枪管数量

佣金程序的问题描述（续）

- 到了月末，销售商要发出一封很短的电报，通知—1个枪锁被售出，以便制造商知道当月的销售情况
- 销售商的佣金为：销售额不到（含）1000美元的部分，为10%，1000（不含）到1800（含）美元的部分，为15%，超过1800美元的部分为20%
- 佣金程序生成月份销售报告，汇总售出的枪锁、准星和枪管总数，销售商的总销售额，以及佣金

```
1  Program Commission (INPUT,OUTPUT)

2      Dim locks,stocks,barrels As Integer
3      Dim lockPrice,stockPrice,barrelPrice As Real
4      Dim totalLocks,totalStocks,totalBarrels As Integer
5      Dim lockSales,stockSales,barrelSales As Real
6      Dim sales,commission As Real

7      lockPrice = 45.0
8      stockPrice = 30.0
9      barrelPrice = 25.0
10     totalLocks = 0
11     totalStocks = 0
12     totalBarrels = 0
```



```
13     Input(locks)
14     While NOT(locks = - 1)      'loop condition uses -1 to indicate end of
15         Input(stocks,barrels)
16         totalLocks = totalLocks + locks
17         totalStocks = totalStocks + stocks
18         totalBarrels = totalBarrels + barrels
19         Input(locks)
20     EndWhile

21     Output("Locks sold:",totalLocks)
22     Output("Stocks sold:",totalStocks)
23     Output("Barrels sold:",totalBarrels)
24     lockSales = lockPrice * totalLocks
25     stockSales = stockPrice * totalStocks
26     barrelSales = barrelPrice * totalBarrels
27     sales = lockSales + stockSales + barrelSales
28     Output("Total sales:",sales)
```

```
29   If(sales>1800.0)
30       Then
31           commission = 0.10 * 1000.0
32           commission = commission + 0.15 * 800.0
33           commission = commission + 0.20 * (sales - 1800.0)
34   Else If(sales>1000.0)
35       Then
36           commission = 0.10 * 1000.0
37           commission = commission + 0.15 * (sales - 1000.0)
38       Else commission = 0.10 * sales
39       EndIf
40   EndIf
41   Output("Commission is $",commission)
42   End Commission
```

Homework

- Draw control flow graph.
- For these variable: LockPrice, TotalStocks, Barrels, LockSales, Sales, Commission
 - List du-pairs and def-clear paths
 - Design test cases to satisfy all du-path coverage.