

A standard basis $\{\vec{e}_1, \vec{e}_2, \dots, \vec{e}_n\}$, the elements of \vec{e}_i are all zero except for i^{th} element, which is one.

$$\vec{m} = \begin{bmatrix} \alpha_1 \\ \vdots \\ \alpha_n \end{bmatrix} = \alpha_1 \vec{e}_1 + \alpha_2 \vec{e}_2 + \dots + \alpha_n \vec{e}_n$$

$$= \sum_{i=1}^n \alpha_i \vec{e}_i$$

$$G(\vec{m}) = G\left(\sum_{i=1}^n \alpha_i \vec{e}_i\right) = \sum_{i=1}^n \alpha_i G(\vec{e}_i)$$

$$= [G(\vec{e}_1) \dots G(\vec{e}_n)] \begin{bmatrix} \alpha_1 \\ \vdots \\ \alpha_n \end{bmatrix}$$

$$= [G(\vec{e}_1) \dots G(\vec{e}_n)] \vec{m}$$

$$= \overline{\overline{I}} \vec{m}$$

So, $\overline{\overline{I}} = [G(\vec{e}_1) \dots G(\vec{e}_n)],$

and its size is $m \times n$