

STAR Analysis Note: psn0689  
Analysis Note for Hyperon Transverse Spin Transfer with  
run12 data

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# 1 Introduction

The spin structure of the proton is a hot topic in QCD. After many years' studies on the longitudinal spin structure, rich knowledge about it has been obtained but the transverse spin structure is still poorly known.  $\Lambda$  and other hyperons have been studied extensively in different aspects of spin physics, due to their self-analyzing weak decay.

In 1997, a significant spin transfer along the normal direction of the  $\Lambda$  production plane,  $D_{NN}$ , was observed by the E704 Collaboration at Fermilab [2].

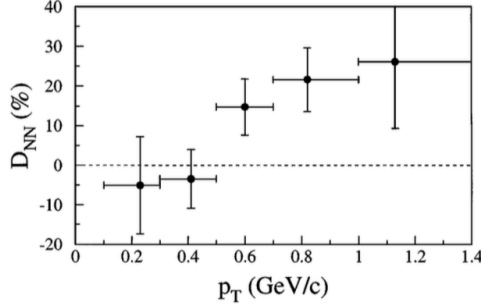


Figure 1.1: Depolarization  $D_{NN}$  data as a function of  $p_T$  in  $p^\uparrow + p \rightarrow \Lambda^0 + X$  at 200 GeV/c from Fermilab E704 Collaboration measurement. The errors shown are statistical only.

The transverse spin transfer,  $D_{TT}$ , of hyperons in  $pp$  collisions is defined in Eq. 1.1 as the asymmetry of the cross section of hyperons polarized parallel and anti-parallel to the incoming protons. It is the natural connection to the transversely polarized parton distribution and the transversely polarized fragmentation functions.

$$D_{TT}^\Lambda \equiv \frac{d\sigma(p^\uparrow p \rightarrow \Lambda^\uparrow X) - d\sigma(p^\uparrow p \rightarrow \Lambda^\downarrow X)}{d\sigma(p^\uparrow p \rightarrow \Lambda^\uparrow X) + d\sigma(p^\uparrow p \rightarrow \Lambda^\downarrow X)} = \frac{d\delta\sigma^\Lambda}{d\sigma^\Lambda}, \quad (1.1)$$

where  $\uparrow$  and  $\downarrow$  denote the positive and negative polarization directions correspondingly,  $\delta\sigma^\Lambda$  is the cross section of  $\Lambda$  when the initial state is transversely polarized and  $\sigma^\Lambda$  is the cross section of  $\Lambda$  when the initial state is unpolarized.  $\delta\sigma^\Lambda$  can be factorized into three parts shown as 1.2 [8]:

$$\frac{d\delta\sigma^\Lambda}{dp_T^\Lambda} = \sum_{abcd} \int dx_a dx_b dz \delta f_a(x_a) f_b(x_b) \delta\sigma^{(a^\uparrow b \rightarrow c^\uparrow d)} \delta D_c^\Lambda(z), \quad (1.2)$$

where,  $\delta D_c^H(z)$  and  $\delta f(x)$  are the polarized fragmentation function in the transversely polarized case and the transversity distribution function of the quarks or antiquarks. They can be studied experimentally in semi-inclusive deep inelastic lepton-nucleon scattering with transversely polarized nucleon or high- $p_T$  hyperon production in transversely polarized  $pp$  collisions by measuring the hyperon polarization in the final state. The partonic spin transfer factor for the elementary hard scattering process is denoted by  $\delta\sigma^{(a^\uparrow b \rightarrow c^\uparrow d)}$ , which is calculatable by pQCD [3].

We present the first measurement on transverse spin transfer of  $\Lambda$  and  $\bar{\Lambda}$  in transversely polarized  $pp$  collisions at  $\sqrt{s} = 200$  GeV with the STAR detector at RHIC. The measurement covers a kinematic range of  $|\eta| < 1.2$  in pseudo-rapidity and transverse momentum  $p_T$  from 1.0 GeV/c up to 8.0 GeV/c. The spin transfer,  $D_{TT}$ , is determined from the asymmetry of  $\Lambda$  counts with opposite beam polarization states, in which the detector acceptance mostly cancels.  $D_{TT}$  dependent on  $p_T$  is presented both in positive and negative pseudo-rapidity ranges.



## 2 Data Set

### 2.1 Trigger selection

The data used in this analysis is the transversely polarized  $pp$  collisions taken in 2012 at  $\sqrt{s} = 200$  GeV with STAR detector and was produced with library P12id. Four triggers are selected in the analysis:

- Jet-Patch 0 (JP0) trigger with id 370601.
- Jet-Patch 1 (JP1) trigger with id 370611.
- Jet-Patch 2 (JP2) trigger with id 370621.
- Adjacent Jet Patch (AJP) trigger with id 370641.

QA was applied for Jet-Patches samples for hyperon analysis and 573 runs left. The average values of some variables per event in each run are used to test the data quality. For each variable, the average value should be stable or have a regularity with the fill running. The run is removed if it is strongly deviated from the average line or regularity. The QA details can be found at:

[http://www.star.bnl.gov/protected/spin/jcmei/pp200trans\\_2012/htmlCode/pp200trans\\_2012\\_dataQA.html](http://www.star.bnl.gov/protected/spin/jcmei/pp200trans_2012/htmlCode/pp200trans_2012_dataQA.html)

The short runs whose running time is shorter than 3 mins or events are smaller than 5k are also removed. Considering that we need to make the correlation between  $\Lambda$  hyperons and reconstructed jets, the runs removed in J. Kevin Adkins' jet tree are also removed. The run number list can be found in Appendix.

The events with primary vertex of  $|V_z| < 60$  cm are selected to ensure uniform tracking efficiency.

The Jet-Patch (JP) trigger conditions in 2012 required a transverse energy deposit in a patch of towers of BEMC or EEMC to exceed the threshold. The BEMC or EEMC patch covers  $\Delta\eta \times \Delta\phi = 1 \times 1$  in pseudo-rapidity,  $\eta$  and azimuthal angle,  $\phi$ . The thresholds are  $E_T \sim 3.5$  GeV for JP0,  $E_T \sim 5.4$  GeV for JP1,  $E_T \sim 7.3$  GeV for JP2 and two adjacent patches to each exceed  $E_T \sim 3.5$  GeV for AJP. JP triggers are preferred to collecting  $pp$  events including scattering with high transverse momentum transfer. Consequently, the  $p_T$  of  $\Lambda$  ( $\bar{\Lambda}$ ) produced through the fragmentation of high transverse momentum parton is expected to be higher. However, JP triggers are not (necessarily) caused by  $\Lambda$  or  $\bar{\Lambda}$ . This implies that the trigger is biased in a way that is different for different classes of  $\Lambda$  or  $\bar{\Lambda}$ . The trigger bias effect on our measurement is considered as a systematic uncertainty and will be discussed in Section 6.

The overlap events were only taken into one (the one with lower threshold) of the fired triggers to avoid double counting. The ratio of the overlap events between each two triggers are shown in TABLE 2.1

The statistics of the data sample used in this analysis are 141.7M totally and for each trigger sample used are:

- 24.6 M JP0 events.

- 85.3 M JP1 events.
- 18.0 M JP2 events.
- 13.9 M AJP events.

The distributions of primary vertex z for each of the JP trigger samples are shown in Fig. 2.1. The distribution of primary vertex z for trigger-combined sample is shown in Fig. 2.2.

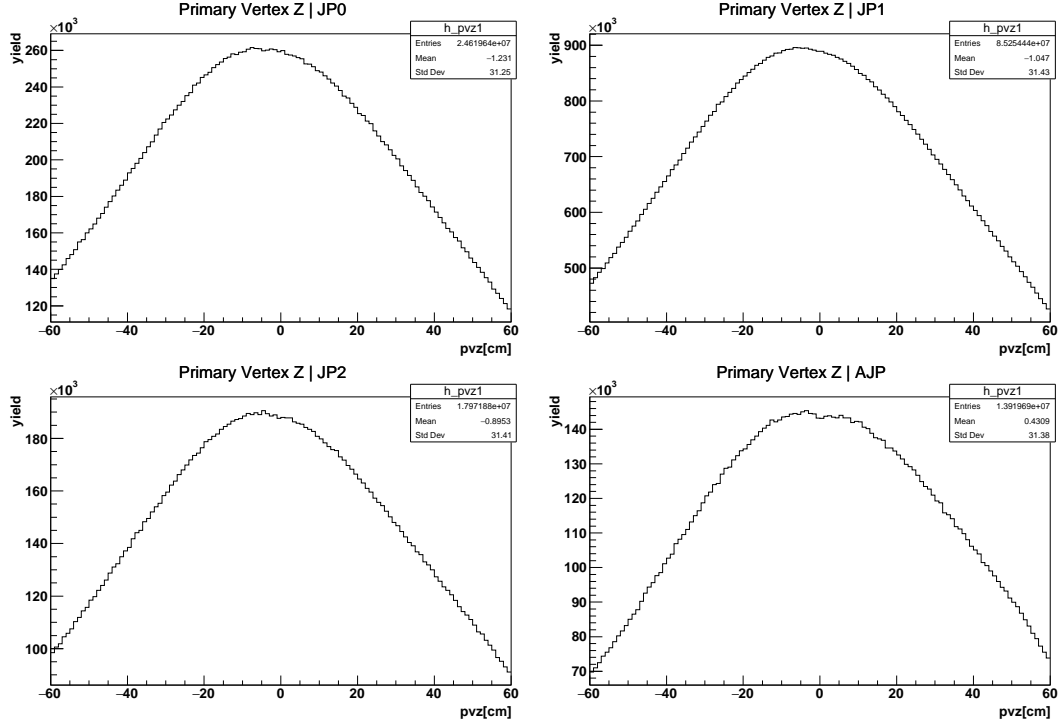


Figure 2.1: z of primary vertex for each of the JP trigger samples

Table 2.1: Ratio of the overlap events between each two triggers. The ratio is the number of events belonging to the trigger of the column and the one of the row together over the number of events belonging to the trigger of the column.

| Trigger Overlap | JP0     | JP1     | JP2     | AJP     |
|-----------------|---------|---------|---------|---------|
| JP0             | 100.00% | 1.01%   | 0.86%   | 0.85%   |
| JP1             | 8.64%   | 100.00% | 42.19%  | 14.53%  |
| JP2             | 2.97%   | 16.89%  | 100.00% | 8.40%   |
| AJP             | 1.33%   | 2.66%   | 3.84%   | 100.00% |

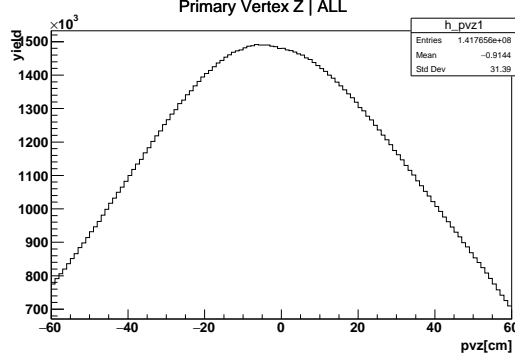


Figure 2.2: z of primary vertex combined four JP trigger samples

## 2.2 Beam polarization

Beam polarizations are average values over fills with run events used in the analysis weighted. The beam polarizations are 64.35% for blue beam and 58.38% for yellow beam.

We use measurements on the website: <http://www.phy.bnl.gov/cnipol/fills/?rp=12&fn=&ft=1&be=100&mode=1&sb=Select>

## 2.3 Relative luminosity

In this analysis, due to the lack of the scaler files for parts of the runs, the Jet-Patch events without  $\Lambda$  or  $\bar{\Lambda}$  candidates was used to estimate the relative luminosities. The relative luminosities of  $R_4$ ,  $R_5$  and  $R_6$  are defined as

$$R_4 = \frac{\mathcal{L}^{\uparrow\uparrow}}{\mathcal{L}^{\downarrow\downarrow}} = \frac{n^{\uparrow\uparrow}}{n^{\downarrow\downarrow}} \quad (2.1)$$

$$R_5 = \frac{\mathcal{L}^{\downarrow\uparrow}}{\mathcal{L}^{\downarrow\downarrow}} = \frac{n^{\downarrow\uparrow}}{n^{\downarrow\downarrow}} \quad (2.2)$$

$$R_6 = \frac{\mathcal{L}^{\uparrow\downarrow}}{\mathcal{L}^{\downarrow\downarrow}} = \frac{n^{\uparrow\downarrow}}{n^{\downarrow\downarrow}} \quad (2.3)$$

At first, the  $pp$  events without  $\Lambda$  or  $\bar{\Lambda}$  candidates were counted for the four spin states of crossing bunches. Then the relative luminosities obtained by using the Eq. 2.1-2.3. The three relative luminosities are shown in Fig. 2.3. The counts of the four spin states and three relative luminosities can be found in Appendix.

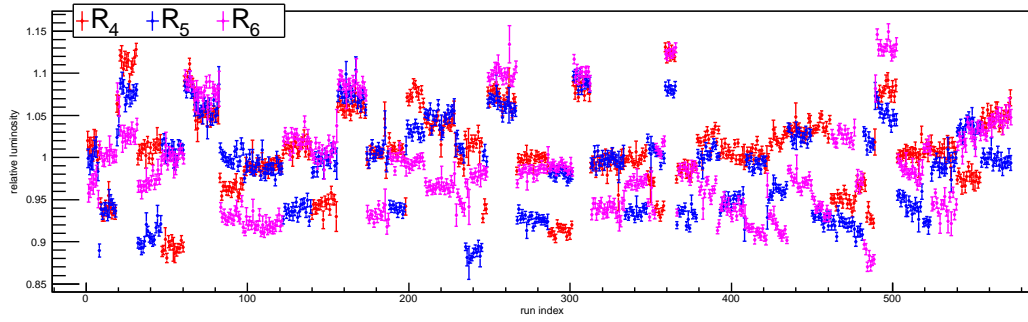


Figure 2.3: Relative luminosities calculated using the Jet-Patch events without  $\Lambda$  or  $\bar{\Lambda}$  candidates. They are used to form the single spin collision events.

### 3 $\Lambda$ ( $\bar{\Lambda}$ ) Reconstruction and Jet Correlation

#### 3.1 $\Lambda$ ( $\bar{\Lambda}$ ) Reconstruction

The reconstruction was done similarly with the previous longitudinal spin transfer analysis [5]. The candidates were identified from the topology of their dominant weak decay channels,  $\Lambda \rightarrow p\pi^-$  and  $\bar{\Lambda} \rightarrow \bar{p}\pi^+$  each having a branching ratio of 63.9%. A search was made in each event to find (anti-)proton and pion tracks of opposite curvatures with an identification cut on track's  $dE/dx$  measured in TPC. The tracks were paired to form  $\Lambda$  ( $\bar{\Lambda}$ ) candidates and then topological selections were applied to further reduce the background. The topological selections include criteria for the distance of closest approach between the paired tracks and the distance between the middle point of the closest approach and the beam collision vertex, and demanded that the momentum sum of the track pair pointed at the collision vertex. The criteria were tuned in each  $p_T$  bin to preserve signals in the mass window while reducing the background fraction to 10% or less. The cuts were summarized in TABLE. 3.1 for all the JP samples and the sketch picture Fig. 3.1.

Table 3.1: Summary of selection cuts for  $\Lambda$  ( $\bar{\Lambda}$ ) reconstruction for Jet-Patch trigger data sample. Here “DCA” denotes “distance of closest approach”, “PV” denotes “primary vertex”,  $\vec{r}$  denotes the vector from primary vertex to the V0 vertex and  $\vec{p}$  denotes the momentum vector of V0. Fig. 3.1 shows definitions of topological selection cuts as a reference.

| Cut \ $p_T$ [GeV/c]                     | (1, 2)  | (2, 3)  | (3, 4)  | (4, 5)  | (5, 6)  | (6, 8)  |
|---|---------|---------|---------|---------|---------|---------|
| N(hits) of daughter tracks              | > 14    | > 14    | > 14    | > 14    | > 14    | > 14    |
| N( $\sigma$ ) $dE/dx$ for daughters     | < 3     | < 3     | < 3     | < 3     | < 3     | < 3     |
| DCA of V0-daughters [cm]                | < 0.80  | < 0.70  | < 0.60  | < 0.50  | < 0.45  | < 0.45  |
| DCA of V0 to PV [cm]                    | < 1.0   | < 1.0   | < 1.0   | < 1.0   | < 1.0   | < 1.0   |
| $\cos(\vec{r}, \vec{p})$                | > 0.995 | > 0.995 | > 0.995 | > 0.995 | > 0.995 | > 0.995 |
| Decay Length [cm]                       | > 3.5   | > 4.0   | > 4.0   | > 4.5   | > 5.0   | > 5.0   |
| DCA of $p$ ( $\bar{p}$ ) to PV [cm]     | > 0.25  | > 0.20  | > 0.10  | > 0.05  | > 0.05  | > 0.05  |
| DCA of $\pi^-$ ( $\pi^+$ ) to PV [cm]   | > 0.60  | > 0.55  | > 0.50  | > 0.50  | > 0.50  | > 0.50  |
| Momentum of $\pi^-$ ( $\pi^+$ ) [GeV/c] | > 0.15  | > 0.15  | > 0.20  | > 0.25  | > 0.30  | > 0.40  |

The invariant mass distributions of  $\Lambda$  and  $\bar{\Lambda}$  candidates for the trigger-combined sample are shown in Fig. 3.2. The distributions of the invariant mass in each JP trigger samples could be found from the link:

[http://www.star.bnl.gov/protected/spin/jcmei/pp200trans\\_2012/htmlCode/pp200trans\\_2012\\_rec\\_step\\_all\\_cut\\_crp0995\\_J0.html](http://www.star.bnl.gov/protected/spin/jcmei/pp200trans_2012/htmlCode/pp200trans_2012_rec_step_all_cut_crp0995_J0.html)

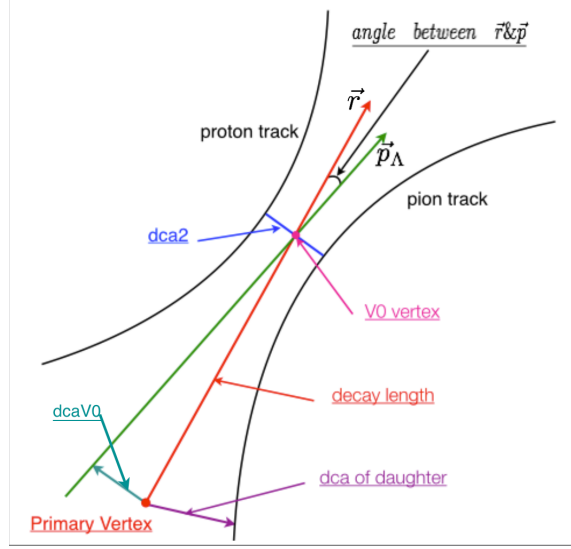


Figure 3.1: Sketch of topological cuts applied in the reconstruction of  $\Lambda$  and  $\bar{\Lambda}$ .

Table 3.2:  $\Lambda$  and  $\bar{\Lambda}$  candidate counts, residual background fractions and signal mass windows after topological selection.

| $p_T$ [GeV/c] | $\Lambda$ |            | $\bar{\Lambda}$ |            | mass window [GeV/c <sup>2</sup> ] |
|---------------|-----------|------------|-----------------|------------|-----------------------------------|
|               | counts    | bkg. frac. | counts          | bkg. frac. |                                   |
| (1, 2)        | 2378150   | 0.057      | 1827999         | 0.082      | (1.111, 1.119)                    |
| (2, 3)        | 833695    | 0.066      | 783074          | 0.075      | (1.111, 1.121)                    |
| (3, 4)        | 308065    | 0.066      | 290993          | 0.071      | (1.109, 1.123)                    |
| (4, 5)        | 108569    | 0.065      | 94996           | 0.066      | (1.108, 1.124)                    |
| (5, 6)        | 42417     | 0.073      | 32733           | 0.077      | (1.106, 1.126)                    |
| (6, 8)        | 26136     | 0.090      | 17187           | 0.107      | (1.104, 1.128)                    |

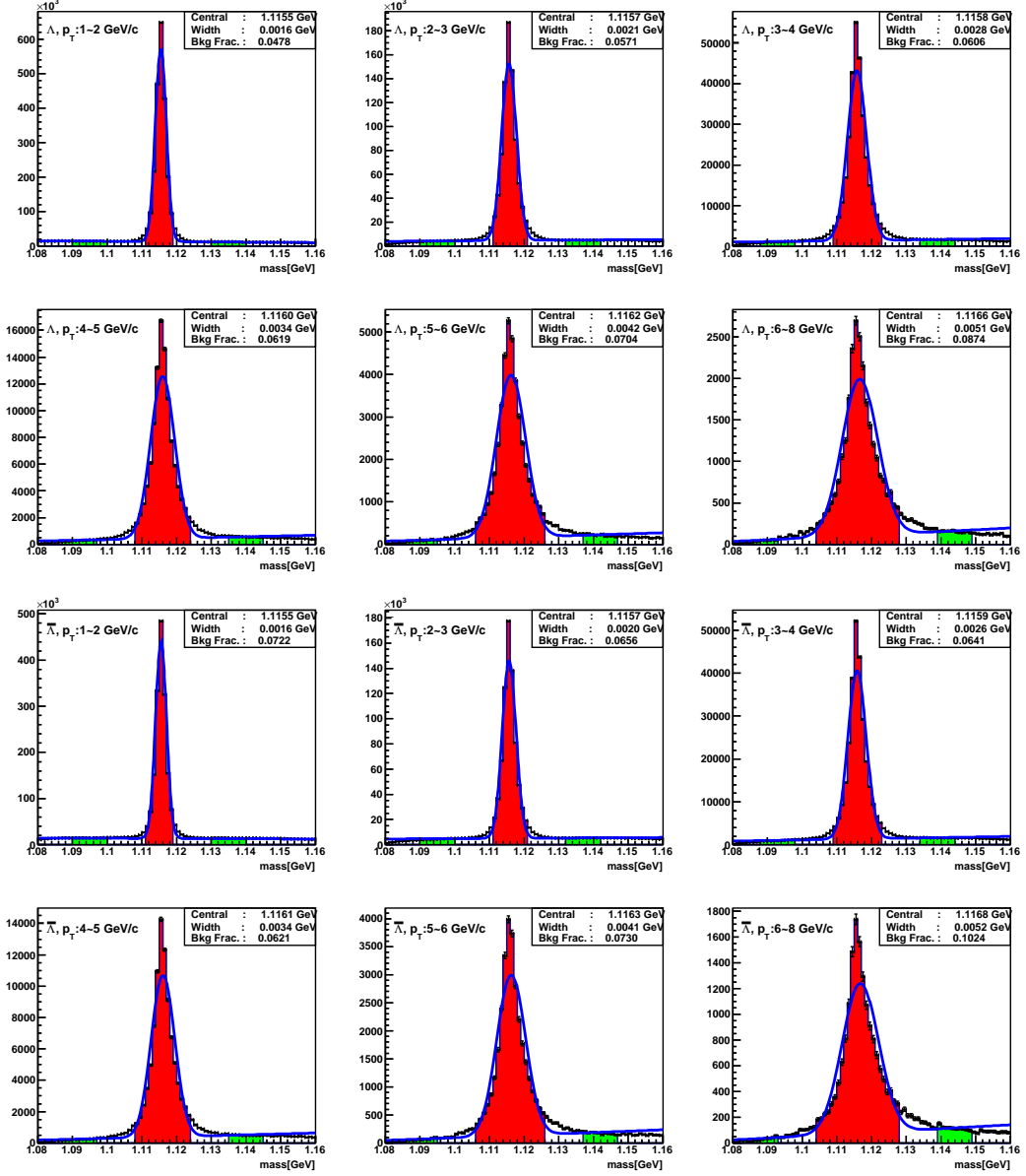


Figure 3.2: Invariant mass distributions of  $\Lambda$  and  $\bar{\Lambda}$  candidates after topological selections for the trigger-combined sample.

### 3.2 Jet Correlation

In our analysis, the outgoing quark momentum direction is used to determine the polarization direction of  $\Lambda(\bar{\Lambda})$ . In STAR experiment, the tracks in TPC and the energy deposits in EMC towers are used to reconstruct jets using the anti- $k_T$  algorithm with a resolution parameter  $R = 0.6$ . The jets used in this analysis is the public jet tree of pp200GeV\_2012 which was generated by J. Kevin Adkins. Fig. 3.3, 3.4 and 3.5 show the  $p_T$ ,  $\eta$  and  $\phi$  distribution of reconstructed jets.

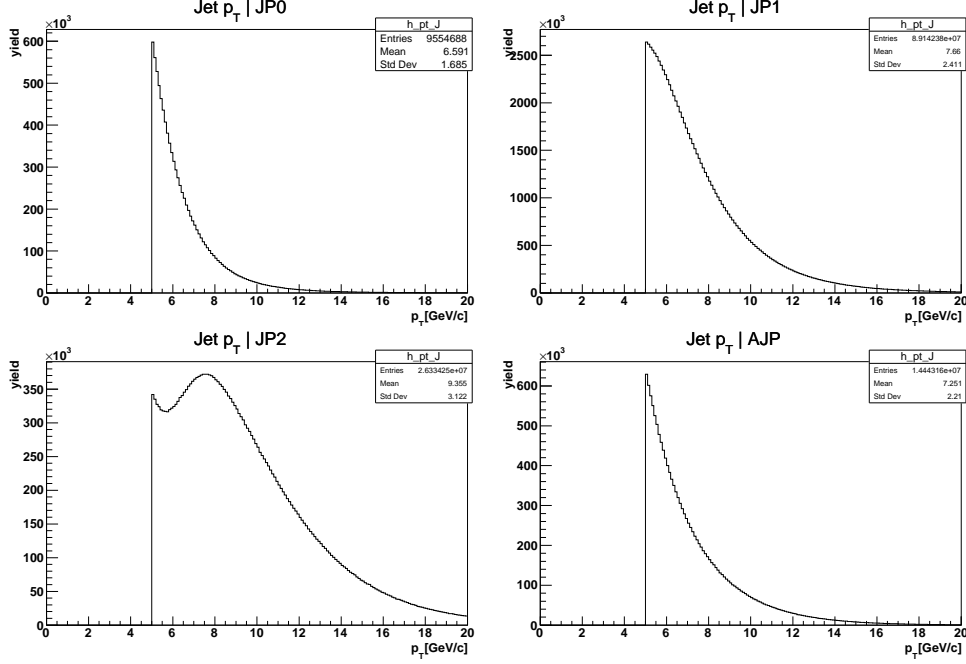


Figure 3.3:  $p_T$  distribution of reconstructed jets.

The selection cuts applied on jets include  $-0.7 < \eta < 0.9$ ,  $E_T > 5 \text{ GeV}$ ,  $0.1 < EMF < 0.95$ .  $EMF$  is the neutral energy fraction of jet, and it is defined as the ratio of BEMC and EEMC  $E_T$  sum over the jet  $E_T$ .

The correlation between  $\Lambda(\bar{\Lambda})$  candidates and the reconstructed jets is made by constraining the distance  $\Delta R (= \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2})$  between momentum directions of  $\Lambda(\bar{\Lambda})$  candidates and jets in  $\eta-\phi$  space. The  $\Delta R$  distributions of  $\Lambda(\bar{\Lambda})$  from JP1 sample are shown in Fig. 3.6 as an example.

The  $\Lambda(\bar{\Lambda})$  hyperons in the jet near-side ( $\Delta R < 0.6$ ) are used to measure  $D_{TT}$ . The fraction of jet near-side  $\Lambda(\bar{\Lambda})$  is increasing with  $p_T$  increasing. This is because  $\Lambda(\bar{\Lambda})$  with higher  $p_T$  is more likely from a jet. We note that jet reconstruction in STAR uses the sample of primary tracks in an event, which often includes the  $p(\bar{p})$  from  $\Lambda(\bar{\Lambda})$  decay but not the decay pion. In addition, the annihilation effect of  $\bar{p}$  in EMC, which provides additional energy to the JP trigger compared to  $\Lambda(p)$  case leads to an excess of  $\bar{\Lambda}$  counts to  $\Lambda$ 's in lower  $p_T$  range. With the increase of  $p_T$ , the fraction of the energy



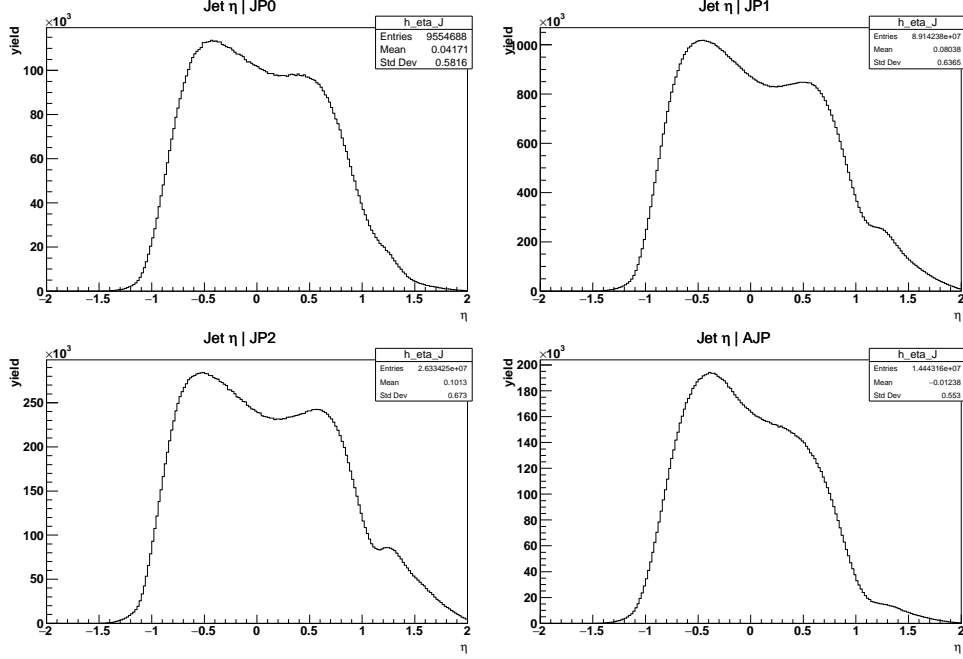


Figure 3.4:  $\eta$  distribution of reconstructed jets.

contributed from the annihilation effect of  $\bar{p}$  in the whole energy deposits in EMC is becoming smaller, so the counts of  $\Lambda$  becomes larger than  $\bar{\Lambda}$  in higher  $p_T$  range. No attempt was made to correct the jet or revise the jet finding and reconstruction for these effects. After such requirements, the invariant mass distributions of  $\Lambda$  and  $\bar{\Lambda}$  from all JP samples are shown in Fig. 3.7 and the sum number of  $\Lambda$  ( $\bar{\Lambda}$ ) candidates from all JP data with the residual background fractions in mass windows for each  $p_T$  bin is listed in Table 3.3. The fractions of  $\Lambda$  and  $\bar{\Lambda}$  hyperons falling in jet near-side cone is shown in TABLE 3.4.

The distributions of  $p_T$ ,  $\eta$  and  $\phi$  for the jet near-side  $\Lambda$  and  $\bar{\Lambda}$  candidates are shown in Fig. 3.8, 3.9 and 3.10.

The distributions in each JP trigger samples could be found from the link:  
[http://www.star.bnl.gov/protected/spin/jcmei/pp200trans\\_2012/htmlCode/pp200trans\\_2012\\_rec\\_step\\_all\\_cut\\_crp0995\\_J1.html](http://www.star.bnl.gov/protected/spin/jcmei/pp200trans_2012/htmlCode/pp200trans_2012_rec_step_all_cut_crp0995_J1.html)

### 3.3 Control sample: $K_S^0$

A null-measurement was performed of the spin transfer for the spinless  $K_S^0$  meson, which has a similar event topology with  $\Lambda$  hyperon. The decay channel

$$K_S^0 \rightarrow \pi^+ \pi^-$$

Table 3.3: Jet near-side  $\Lambda$  and  $\bar{\Lambda}$  candidate counts, residual background fractions and signal mass windows.

| $p_T$ [GeV/c] | $\Lambda$ |            | $\bar{\Lambda}$ |            | mass window [GeV/c <sup>2</sup> ] |
|---------------|-----------|------------|-----------------|------------|-----------------------------------|
|               | counts    | bkg. frac. | counts          | bkg. frac. |                                   |
| ( 1, 2 )      | 469681    | 0.065      | 502226          | 0.074      | ( 1.111, 1.119 )                  |
| ( 2, 3 )      | 318358    | 0.079      | 368042          | 0.077      | ( 1.111, 1.121 )                  |
| ( 3, 4 )      | 181550    | 0.071      | 193221          | 0.072      | ( 1.109, 1.123 )                  |
| ( 4, 5 )      | 77866     | 0.065      | 71833           | 0.066      | ( 1.108, 1.124 )                  |
| ( 5, 6 )      | 32441     | 0.070      | 25571           | 0.075      | ( 1.106, 1.126 )                  |
| ( 6, 8 )      | 20256     | 0.084      | 13486           | 0.102      | ( 1.104, 1.128 )                  |

Table 3.4: The fraction of hyperons falling in the jet near-side cone for  $\Lambda$  and  $\bar{\Lambda}$  in each  $p_T$  bin.

| $p_T$ [GeV/c]   | [1,2)  | [2,3)  | [3,4)  | [4,5)  | [5,6)  | [6,8)  |
|-----------------|--------|--------|--------|--------|--------|--------|
| $\Lambda$       | 19.75% | 38.19% | 58.93% | 71.72% | 76.48% | 77.50% |
| $\bar{\Lambda}$ | 27.47% | 47.00% | 66.40% | 75.62% | 78.12% | 78.47% |

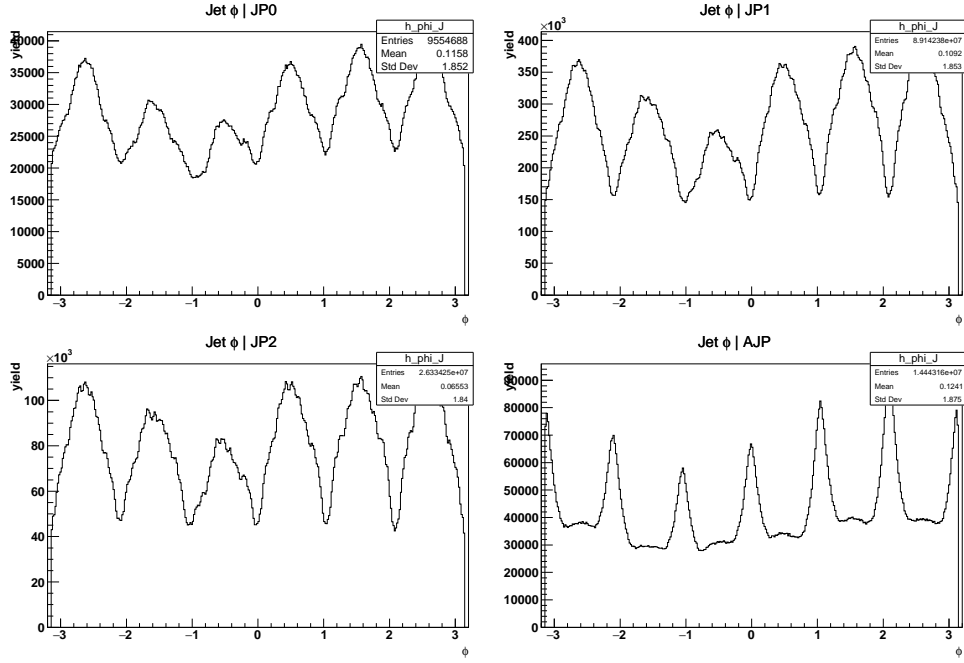


Figure 3.5:  $\phi$  distribution of reconstructed Jets.

with the branching ratio of 69.20%. The topological selection cuts applied on the reconstruction of the  $K_S^0$  are shown in Table 3.5.

The invariant mass distribution of  $K_S^0$  is shown in Fig. 3.11.

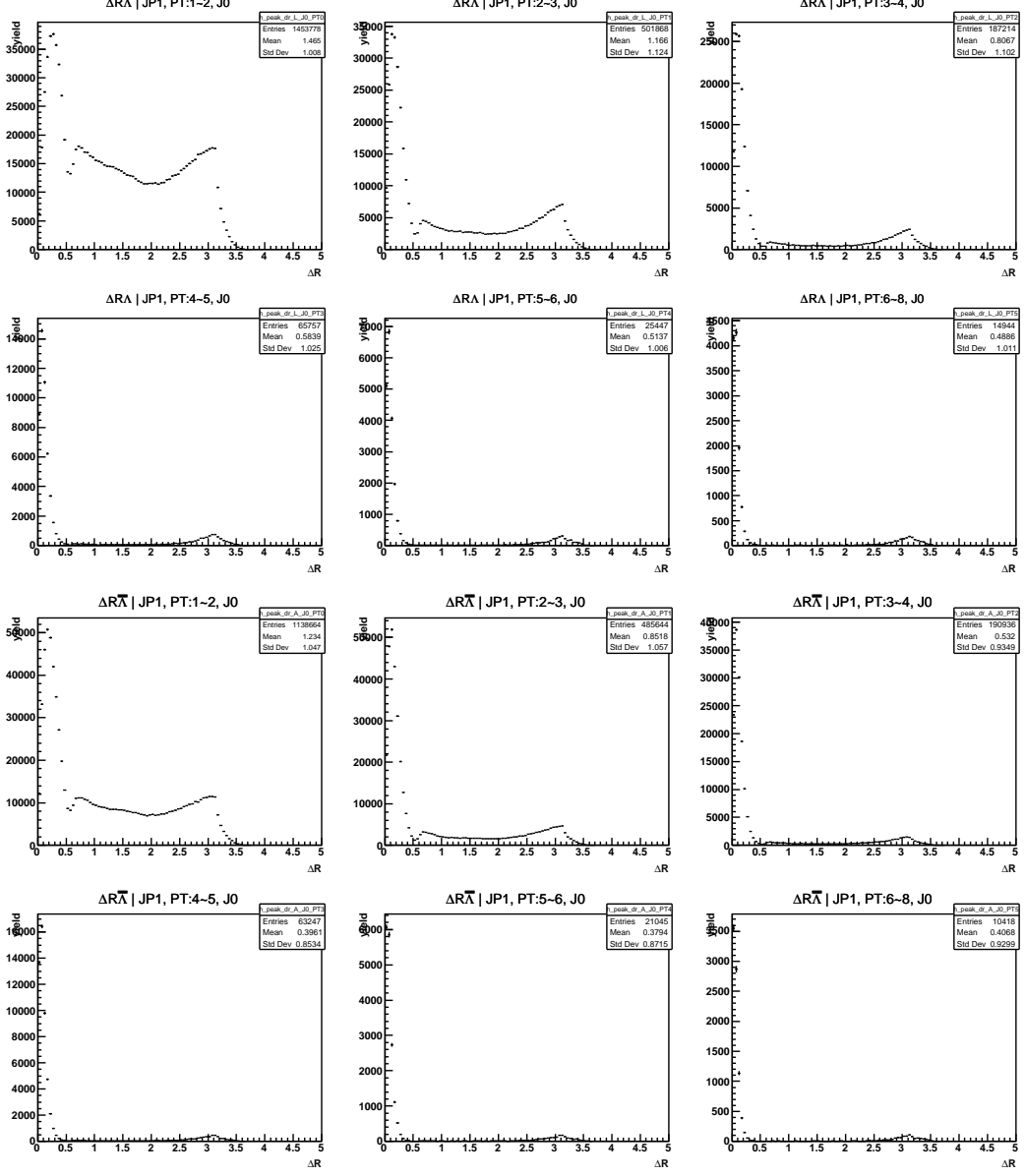


Figure 3.6:  $\Delta R$  distribution in the correlation between the reconstructed jet and  $\Lambda$  ( $\bar{\Lambda}$ ) from JP1 trigger sample as the example.

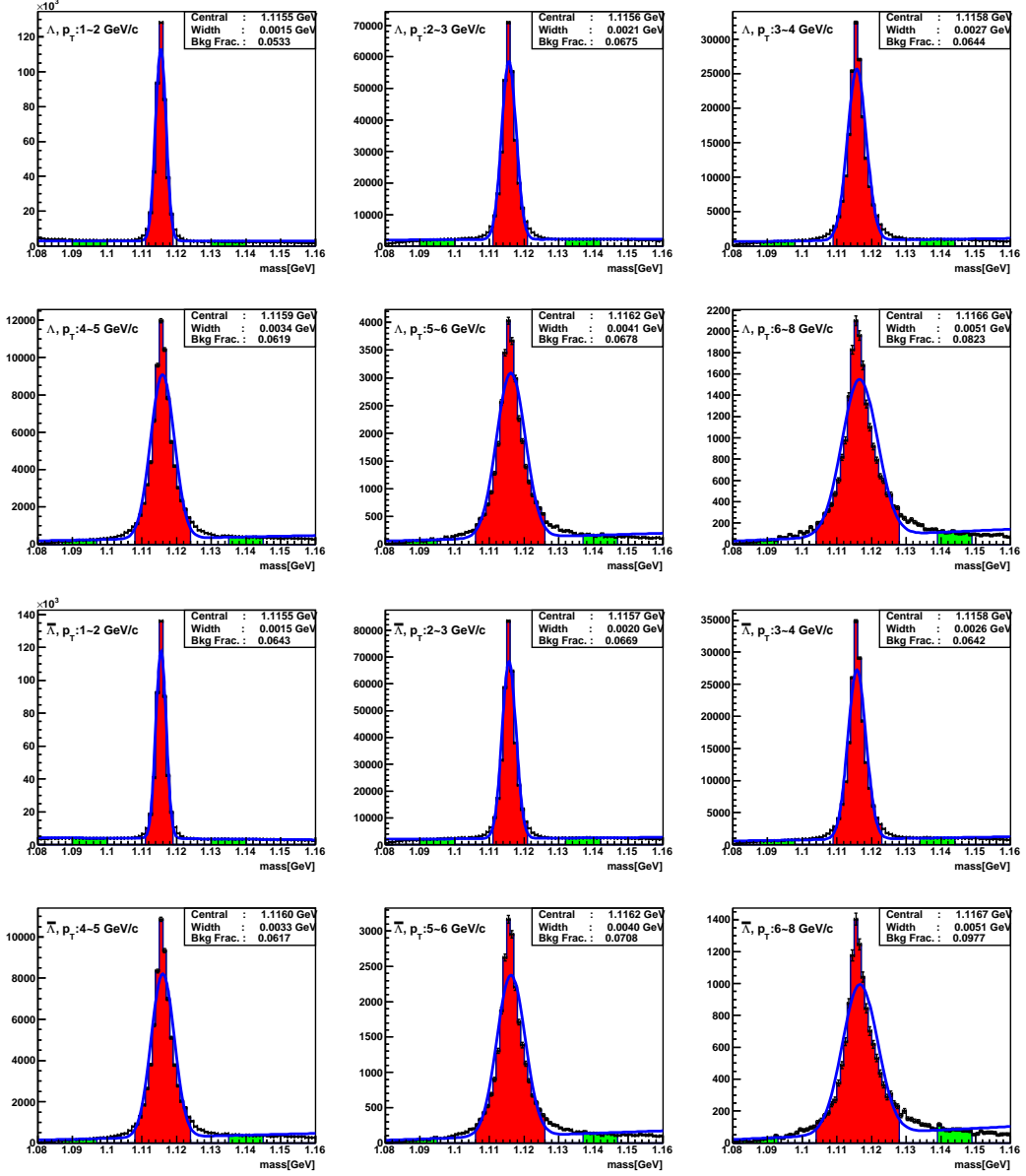


Figure 3.7: The invariant mass distributions of jet near-side  $\Lambda$  and  $\bar{\Lambda}$  candidates for the trigger-combined samples.

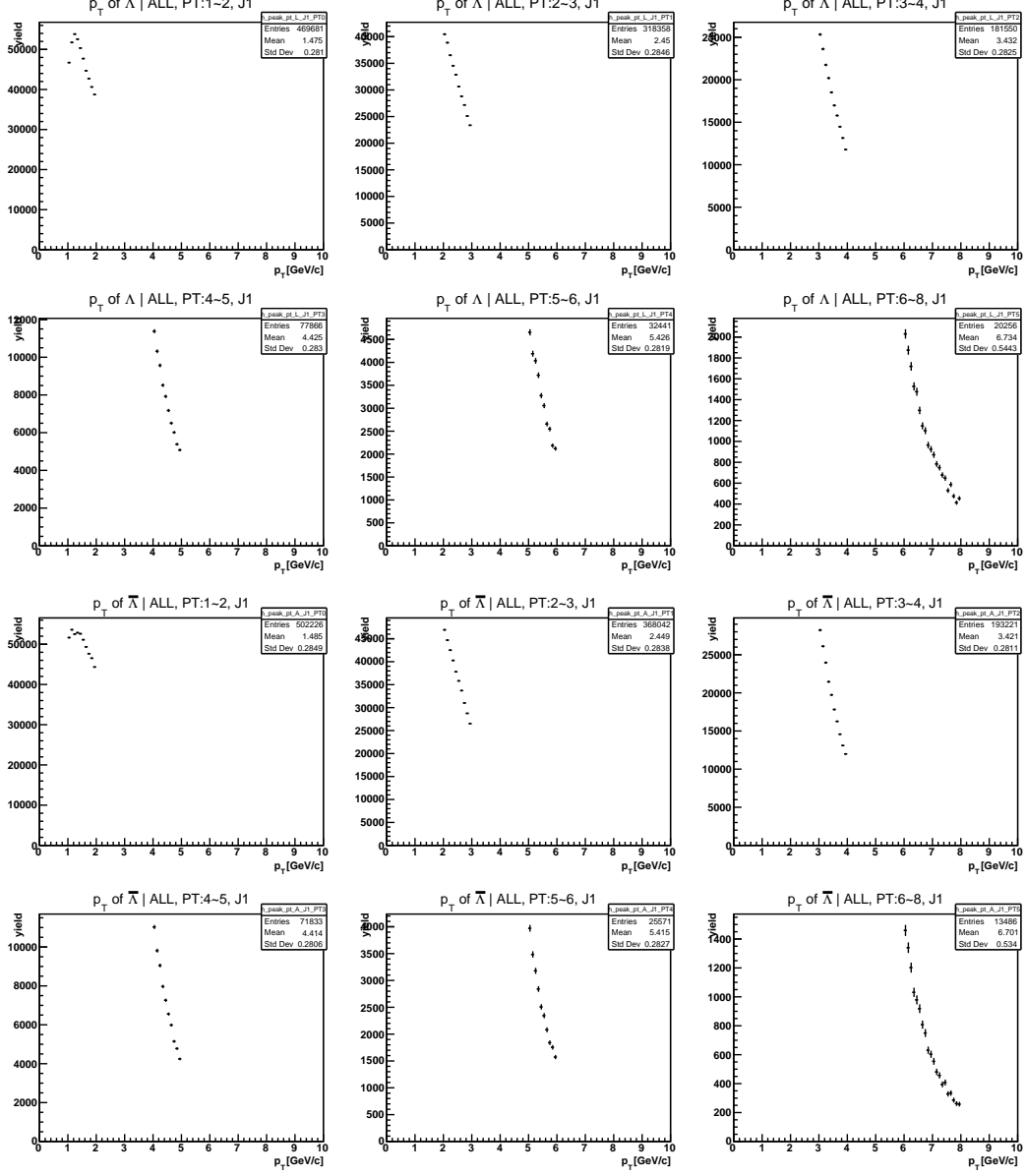


Figure 3.8: The  $p_T$  distributions of  $\Lambda$  and  $\bar{\Lambda}$  candidates in the jet near-side from the four JP trigger samples.

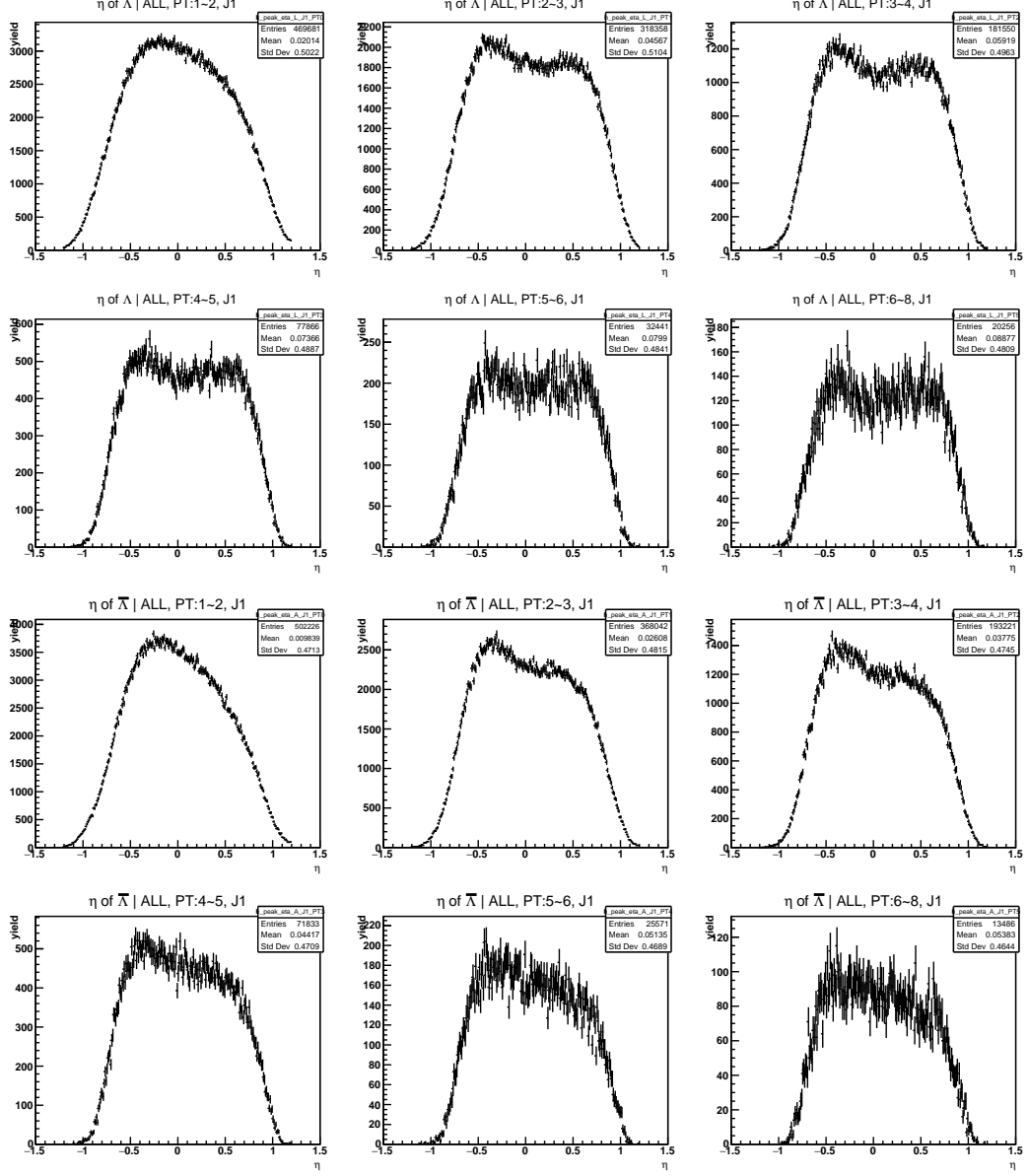


Figure 3.9: The  $\eta$  distributions of  $\Lambda$  and  $\bar{\Lambda}$  candidates in the jet near-side from the four JP trigger samples.

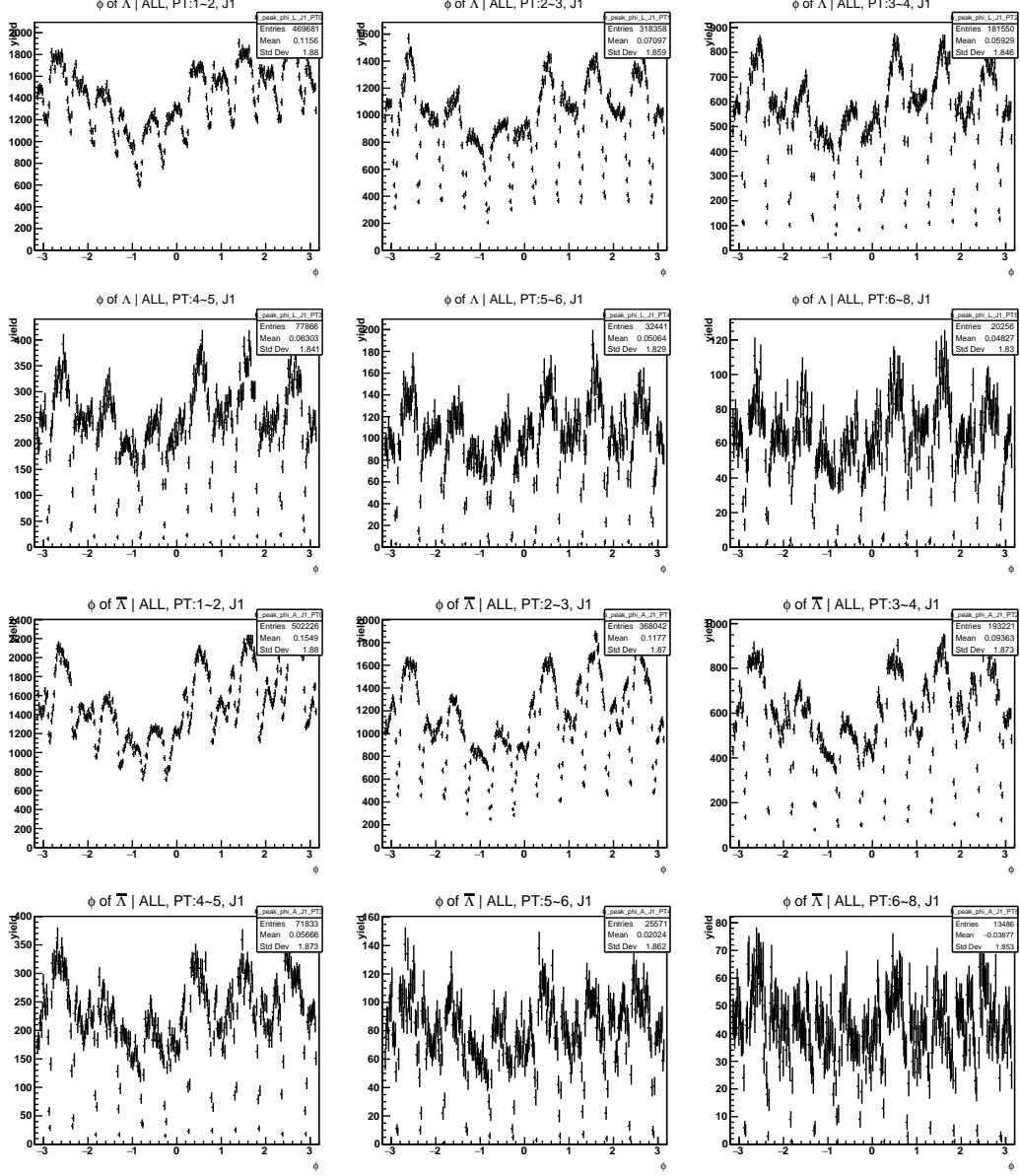


Figure 3.10: The  $\phi$  distributions of  $\Lambda$  and  $\bar{\Lambda}$  candidates in the jet near-side from the four JP trigger samples.



Table 3.5: Summary of selection cuts for  $K_S^0$  reconstruction for Jet-Patch trigger data sample. Here “DCA” denotes “distance of closest approach”, “PV” denotes “primary vertex”,  $\vec{r}$  denotes the vector from primary vertex to the V0 vertex and  $\vec{p}$  denotes the momentum vector of V0. Fig. 3.1 shows definitions of topological selection cuts as a reference.

| Cut \ $p_T$ [GeV/c]                     | (1, 2) | (2, 3) | (3, 4) | (4, 5) | (5, 6) | (6, 8) |
|---|--------|--------|--------|--------|--------|--------|
| N(hits) of daughter tracks              | > 14   | > 14   | > 14   | > 14   | > 14   | > 14   |
| N( $\sigma$ ) $dE/dx$ for daughters     | < 3    | < 3    | < 3    | < 3    | < 3    | < 3    |
| DCA of V0-daughters [cm]                | < 0.70 | < 0.65 | < 0.55 | < 0.45 | < 0.40 | < 0.35 |
| DCA of V0 to PV [cm]                    | < 0.60 | < 0.70 | < 0.80 | < 0.80 | < 0.80 | < 0.80 |
| $\cos(\vec{r}, \vec{p})$                | > 0.99 | > 0.99 | > 0.99 | > 0.99 | > 0.99 | > 0.99 |
| Decay Length [cm]                       | > 1.20 | > 1.40 | > 1.50 | > 1.60 | > 1.80 | > 2.00 |
| DCA of $\pi^-$ ( $\pi^+$ ) to PV [cm]   | > 0.60 | > 0.55 | > 0.50 | > 0.45 | > 0.40 | > 0.35 |
| Momentum of $\pi^-$ ( $\pi^+$ ) [GeV/c] | > 0.15 | > 0.15 | > 0.20 | > 0.25 | > 0.30 | > 0.40 |

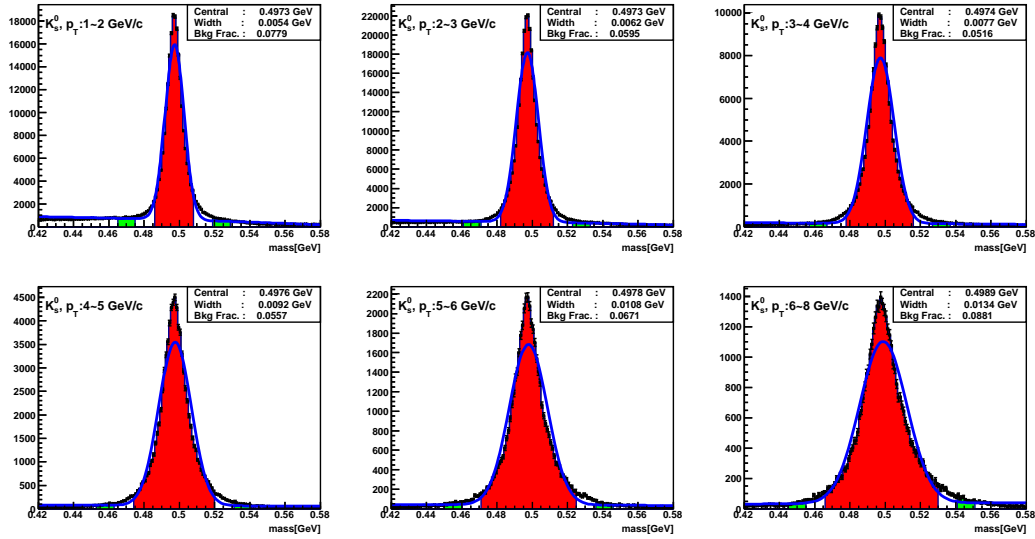


Figure 3.11: Invariant mass of  $K_S^0$  candidates for the trigger-combined sample.

## 4 Extraction of Transverse Spin Transfer

Usually, the polarization and spin transfer of  $\Lambda$  ( $\bar{\Lambda}$ ) can be measured via its weak decay channel  $\Lambda \rightarrow p\pi^-$  ( $\bar{\Lambda} \rightarrow \bar{p}\pi^+$ ) from the angular distribution of the final state,

$$\frac{dN}{d\cos\theta^*} = \frac{N_{\text{tot}}}{2} A(\cos\theta^*) (1 + \alpha_\Lambda P_\Lambda \cos\theta^*), \quad (4.1)$$

where  $N_{\text{tot}}$  is the total number of  $\Lambda$  produced in collisions,  $\alpha_\Lambda = -\alpha_{\bar{\Lambda}} = 0.642 \pm 0.013$  [4] is the decay parameter,  $\theta^*$  is the angle between the decay proton momentum in the  $\Lambda$ 's rest frame and the  $\Lambda$  polarization direction (Fig. 3.1) and  $A(\cos\theta^*)$  is the detector acceptance which may vary with  $\theta^*$  as well as other observables. The average of the detector acceptance shows as:

$$\langle A(P, \cos\theta^*) \rangle = \frac{\int A(\cos\theta^*) N(P, \cos\theta^*) d\cos\theta^*}{\int N(P, \cos\theta^*) d\cos\theta^*}, \quad (4.2)$$

where  $N(P, \cos\theta^*)$  is the number of  $\Lambda$  with beam polarization  $P$  and  $\cos\theta^*$ . The acceptance is expected to be a constant in a small  $\cos\theta^*$  interval  $[\theta_1^*, \theta_2^*]$  and the average of the acceptance is used, which is noted as  $\langle A(P, \cos\theta_1^*, \cos\theta_2^*) \rangle$ . Then the number of  $\Lambda$  with the inversed polarization in the small interval  $[\cos(\theta_1^*), \cos(\theta_2^*)]$  could be obtained

$$\begin{aligned} N(P) &= \langle A(P, \cos\theta_1^*, \cos\theta_2^*) \rangle N_{\text{tot}} (\cos\theta_2^* - \cos\theta_1^*) + \frac{\alpha}{2} P (\cos^2\theta_2^* - \cos^2\theta_1^*) \quad (4.3) \\ N(-P) &= \langle A(-P, \cos\theta_1^*, \cos\theta_2^*) \rangle N_{\text{tot}} (\cos\theta_2^* - \cos\theta_1^*) - \frac{\alpha}{2} P (\cos^2\theta_2^* - \cos^2\theta_1^*). \end{aligned}$$

Due to the symmetry of the detector geometry, the acceptances of the inversed polarizations should be the same, namely  $\langle A(P, \cos\theta_1^*, \cos\theta_2^*) \rangle = \langle A(-P, \cos\theta_1^*, \cos\theta_2^*) \rangle$ . Thus the asymmetry of inversed polarizations is

$$\frac{N(P) - N(-P)}{N(P) + N(-P)} = \alpha P_\Lambda \frac{\cos\theta_1^* + \cos\theta_2^*}{2}, \quad (4.4)$$

Further, the polarization of  $\Lambda$  can be expressed as:

$$P_\Lambda = \frac{1}{\alpha \langle \cos\theta^* \rangle} \frac{N(P) - N(-P)}{N(P) + N(-P)}, \quad (4.5)$$

where  $\langle \cos\theta^* \rangle$  is the average value of  $\cos\theta^*$  in a small interval  $[\theta_1^*, \theta_2^*]$ . In Eq. 4.5, the acceptance of the detector has been cancelled. In the  $pp$  collision, the polarization of  $\Lambda$  will be inversed with the polarization of incoming proton inversed, namely

$$P_\Lambda(p^\uparrow p \rightarrow \Lambda X) = -P_\Lambda(p^\downarrow p \rightarrow \Lambda X) \quad (4.6)$$

The  $\Lambda$  polarization in experiment is transferred from the beam polarization

$$P_\Lambda = D_{\text{TT}} P, \quad (4.7)$$

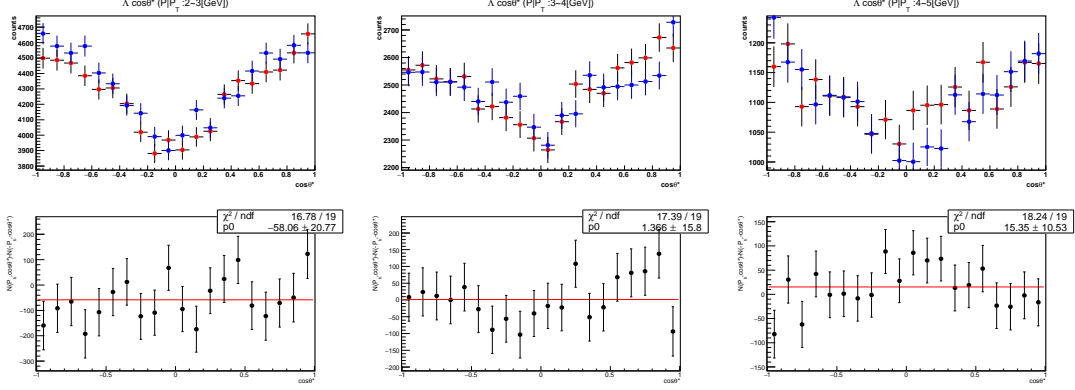


Figure 4.1: Symmetry test of  $\Lambda$  counts when both of the beam polarization and  $\cos\theta^*$  reverse.

where  $D_{\text{TT}}$  is actually the ratio of beam polarization transferred to  $\Lambda$  polarization.

To minimize the uncertainty associated with the detector acceptance effects,  $D_{\text{TT}}$  has been extracted through the asymmetry of  $\Lambda$  counts in small  $\cos\theta^*$  intervals with opposite beam polarization:

$$D_{\text{TT}} = \frac{1}{\alpha P \langle \cos\theta^* \rangle} \frac{N^\uparrow - RN^\downarrow}{N^\uparrow + RN^\downarrow}, \quad (4.8)$$

where  $\alpha$  is the decay parameter [4],  $P$  is the polarization of the beam,  $\langle \cos\theta^* \rangle$  is the average value in each small  $\cos\theta^*$  bin,  $N^\uparrow(N^\downarrow)$  are the counts of hyperons in a small  $\cos\theta^*$  interval when the beam is positively (negatively) polarized and  $R$  is the relative luminosity ratio for these two polarization states. The detector acceptance in this  $\cos\theta^*$  interval is largely canceled because the acceptance in a small  $\cos\theta^*$  interval is expected to be the same when flipping the beam spin.

In this analysis, the cross-ratio method is used to extract  $D_{\text{TT}}$  and thus the relative luminosity  $R$  Eq. 4.8 can be canceled. Based on the symmetry of the cross section of hyperon when both of beam polarization and  $\cos\theta^*$  reverse, namely

$$\sigma^\uparrow(\cos\theta^*) = \sigma^\downarrow(-\cos\theta^*), \quad \sigma^\downarrow(\cos\theta^*) = \sigma^\uparrow(-\cos\theta^*), \quad (4.9)$$

where  $\sigma$  is the cross section of hyperons and  $\uparrow(\downarrow)$  is the beam polarization direction. The symmetry can be tested using the hyperon counts distribution with  $\cos\theta^*$ . The symmetries are shown in Fig. 4.1 and Fig. 4.2 for  $\Lambda$  and  $\bar{\Lambda}$  correspondingly. The symmetries are good within the uncertainty. Then from the following equation Eq. 4.10 and Eq. 4.13, we could find that the relative luminosities are canceled when single beam is polarized.

$$\sigma^\uparrow = \frac{N^\uparrow}{\mathcal{L}^\uparrow}, \quad \sigma^\downarrow = \frac{N^\downarrow}{\mathcal{L}^\downarrow}, \quad (4.10)$$

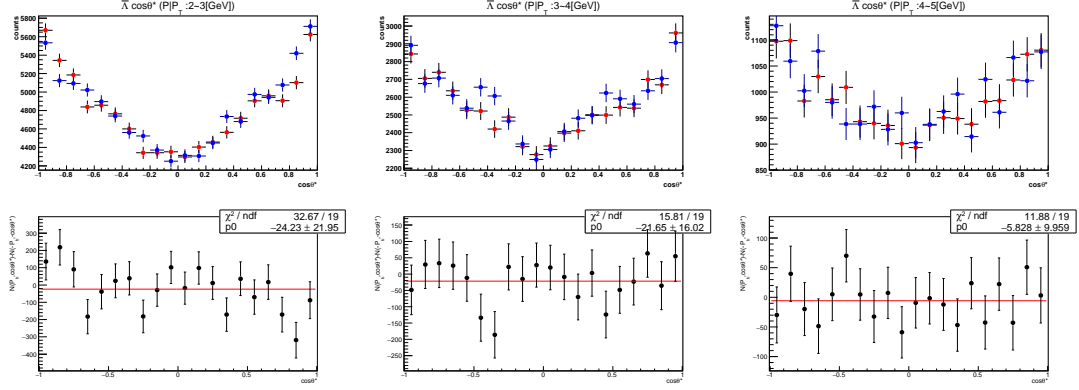


Figure 4.2: Symmetry test of  $\bar{\Lambda}$  counts when both of the beam polarization and  $\cos\theta^*$  reverse.

$$\frac{\sqrt{\sigma^\uparrow(\cos\theta^*)\sigma^\downarrow(-\cos\theta^*)} - \sqrt{\sigma^\uparrow(-\cos\theta^*)\sigma^\downarrow(\cos\theta^*)}}{\sqrt{\sigma^\uparrow(\cos\theta^*)\sigma^\downarrow(-\cos\theta^*)} + \sqrt{\sigma^\uparrow(-\cos\theta^*)\sigma^\downarrow(\cos\theta^*)}} \quad (4.11)$$

$$= \frac{\sqrt{\frac{N^\uparrow(\cos\theta^*)}{\mathcal{L}^\uparrow} \frac{N^\downarrow(-\cos\theta^*)}{\mathcal{L}^\downarrow}} - \sqrt{\frac{N^\uparrow(-\cos\theta^*)}{\mathcal{L}^\uparrow} \frac{N^\downarrow(\cos\theta^*)}{\mathcal{L}^\downarrow}}}{\sqrt{\frac{N^\uparrow(\cos\theta^*)}{\mathcal{L}^\uparrow} \frac{N^\downarrow(-\cos\theta^*)}{\mathcal{L}^\downarrow}} + \sqrt{\frac{N^\uparrow(-\cos\theta^*)}{\mathcal{L}^\uparrow} \frac{N^\downarrow(\cos\theta^*)}{\mathcal{L}^\downarrow}}} \quad (4.12)$$

$$= \frac{\sqrt{N^\uparrow(\cos\theta^*)N^\downarrow(-\cos\theta^*)} - \sqrt{N^\uparrow(-\cos\theta^*)N^\downarrow(\cos\theta^*)}}{\sqrt{N^\uparrow(\cos\theta^*)N^\downarrow(-\cos\theta^*)} + \sqrt{N^\uparrow(-\cos\theta^*)N^\downarrow(\cos\theta^*)}}, \quad (4.13)$$

At last, the equation used to extract  $D_{\text{TT}}$  is expressed as Eq. 4.14.

$$D_{\text{TT}} = \frac{1}{\alpha P_{\text{beam}} \langle \cos\theta^* \rangle} \frac{\sqrt{N^\uparrow(\cos\theta^*)N^\downarrow(-\cos\theta^*)} - \sqrt{N^\uparrow(-\cos\theta^*)N^\downarrow(\cos\theta^*)}}{\sqrt{N^\uparrow(\cos\theta^*)N^\downarrow(-\cos\theta^*)} + \sqrt{N^\uparrow(-\cos\theta^*)N^\downarrow(\cos\theta^*)}}, \quad (4.14)$$

Here the approximation

$$\mathcal{L}^{\uparrow\uparrow} \approx \mathcal{L}^{\uparrow\downarrow}, \quad \mathcal{L}^{\downarrow\downarrow} \approx \mathcal{L}^{\downarrow\uparrow}$$

are used here and actually the approximation is highly convinced which is shown in Fig. 4.3. The values of relative luminosities are really closed to each other and the residual polarized parts of the unpolarized beam expected are really small. The residual polarized parts are hardly affect the  $D_{\text{TT}}$  results especially in the positive  $\eta$  range.

To measure the transverse spin transfer,  $D_{\text{TT}}$ , the polarization direction of  $\Lambda$  needs to be determined first. Here, the polarization direction of  $\Lambda$  is considered as the same with the polarization direction of the outgoing quark which can be obtained via the rotation relationship with the polarization direction of the incoming quark [3]. At the experimental level, the polarization direction of the beam is substituted for that of the

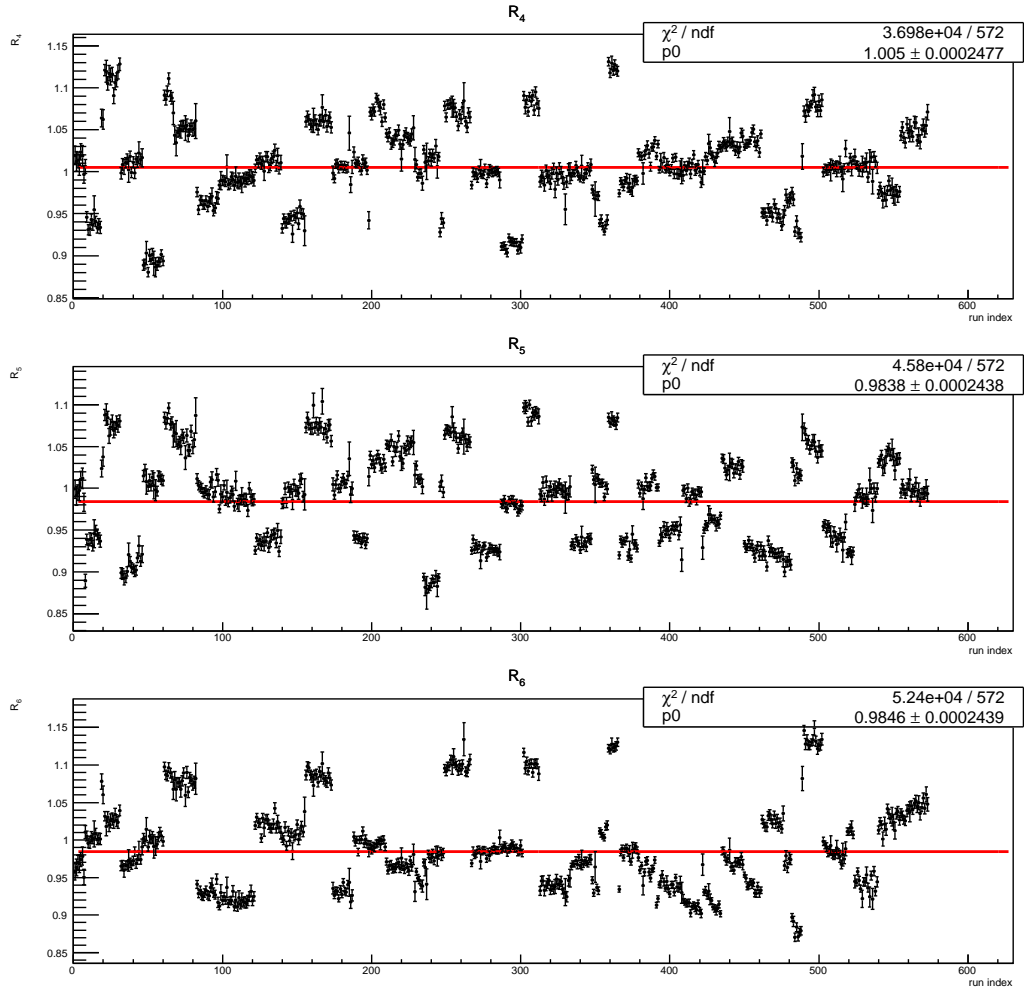


Figure 4.3: Average values of relative luminosities over runs.

incoming quark and the momentum direction of the jet reconstructed is substituted for that of the outgoing quark.

After the reconstruction and jet correlation, the  $\Lambda(\bar{\Lambda})$  sample was obtained. The  $\cos\theta^*$  for each  $\Lambda(\bar{\Lambda})$  candidate was calculated with the blue and yellow beam as the polarized beam separately. The spin 4-bit sorted distributions were combined using the relative luminosities as the weight to form the distribution sorted by beam polarization. The  $\cos\theta^*$  vs. invariant mass distributions and  $\cos\theta^*$  distributions of  $\Lambda$  and  $\bar{\Lambda}$  for inversed beam polarizations with  $\eta$  of  $0 \sim 1.2$ ,  $p_T$  of  $2 \sim 3$  GeV/c and BLUE beam as the polarized beam from JP1 sample are shown in Fig. 4.4 and Fig. 4.5 are used as examples. The distributions from all  $\Lambda$   $p_T$  and all JP trigger samples bins could be found from the link:

[http://www.star.bnl.gov/protected/spin/jcmei/pp200trans\\_2012/htmlCode/pp200trans\\_2012\\_dttExtraction\\_1.html](http://www.star.bnl.gov/protected/spin/jcmei/pp200trans_2012/htmlCode/pp200trans_2012_dttExtraction_1.html)

The distributions of  $\cos\theta^*$  versus invariant mass could be found from the link, too. The drop in the middle range ( $\cos\theta^* \sim 0$ ) is due to the missing of the daughter particle with small  $p_T$ .

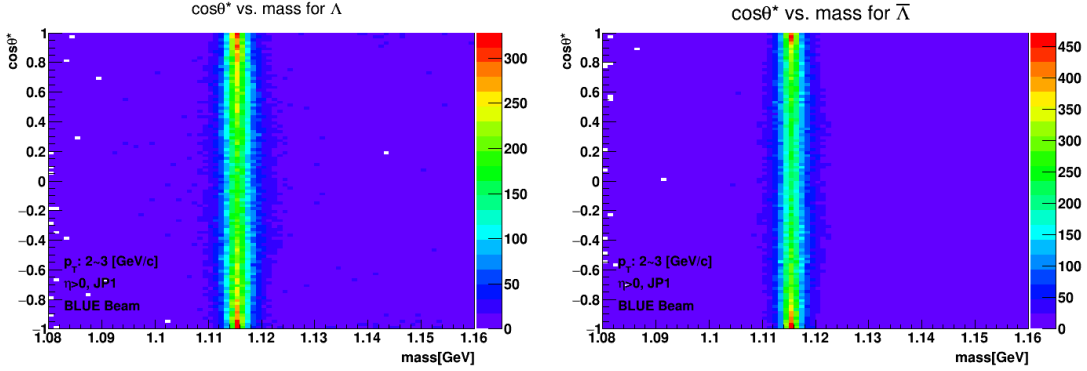


Figure 4.4:  $\cos\theta^*$  vs. invariant mass distribution for  $\Lambda$ (left) and  $\bar{\Lambda}$ (right) with  $2 < p_T < 3$  GeV/c and  $0 < \eta < 1.2$  from JP1 sample with the BLUE beam as the polarized beam.

$D_{TT}$  in each small  $\cos\theta^*$  interval were obtained using Eq. 4.8 and shown in Fig. 4.6. Here the results are from JP1 sample and with the  $\Lambda$   $p_T$  of  $2 \sim 3$  GeV/c.

Then  $D_{TT}$  in each  $\cos\theta^*$  interval are fitted using a constant in each  $p_T$  bin and the fitted result is used as the  $D_{TT}$  for the  $p_T$  bin. Fig. 4.7 shows the  $D_{TT}$  of  $\Lambda(\bar{\Lambda})$  for JP triggers.

#### 4.1 Trigger Combined $D_{TT}$

$D_{TT}$  values for each of the JP trigger samples are consistent with each other within the statistical uncertainty and the  $\chi^2$  test for the results of each two trigger samples are shown in TABLE 4.1 so we combined the events from each of the trigger samples into one data sample.

The  $D_{TT}$  for  $\Lambda(\bar{\Lambda})$  and  $\delta_{TT}$  for  $K_S^0$  vs.  $\cos\theta^*$  in each  $p_T$  bin are shown in Fig. 4.8.

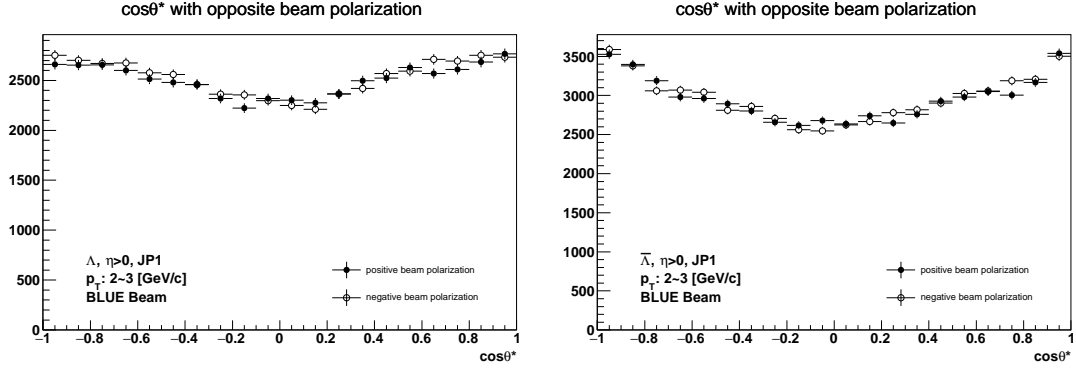


Figure 4.5:  $\cos\theta^*$  distribution for (a)  $\Lambda$  and (b)  $\bar{\Lambda}$  from JP1 sample. The solid circle denotes the positive beam polarization and the open circle denotes the negative beam polarization.

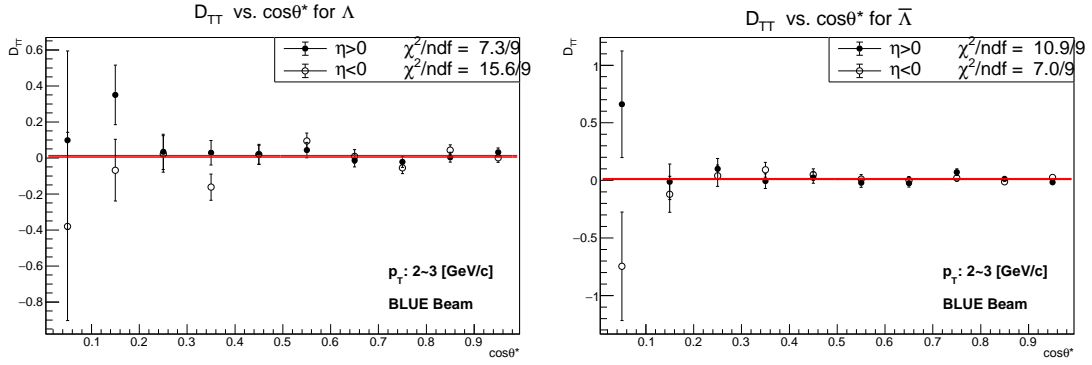


Figure 4.6:  $D_{TT}$  vs.  $\cos\theta^*$  for  $\Lambda$ (left) and  $\bar{\Lambda}$ (right) with  $p_T$  of  $2 \sim 3$  GeV/c using JP1 data.

Table 4.1:  $\chi^2/\text{ndf}$  testing between the results of each two trigger samples

| Trigger   | $\Lambda$        |                   | $\bar{\Lambda}$  |                   |
|-----------|------------------|-------------------|------------------|-------------------|
|           | $0 < \eta < 1.2$ | $-1.2 < \eta < 0$ | $0 < \eta < 1.2$ | $-1.2 < \eta < 0$ |
| JP0 : JP1 | 6.47/6           | 2.58/6            | 3.84/6           | 5.94/6            |
| JP0 : JP2 | 6.09/6           | 2.48/6            | 5.85/6           | 3.09/6            |
| JP0 : AJP | 5.02/6           | 2.97/6            | 6.10/6           | 3.47/6            |
| JP1 : JP2 | 6.68/6           | 2.60/6            | 10.45/6          | 3.27/6            |
| JP1 : AJP | 2.70/6           | 2.86/6            | 7.84/6           | 4.62/6            |
| JP2 : AJP | 6.57/6           | 3.80/6            | 12.56/6          | 4.23/6            |

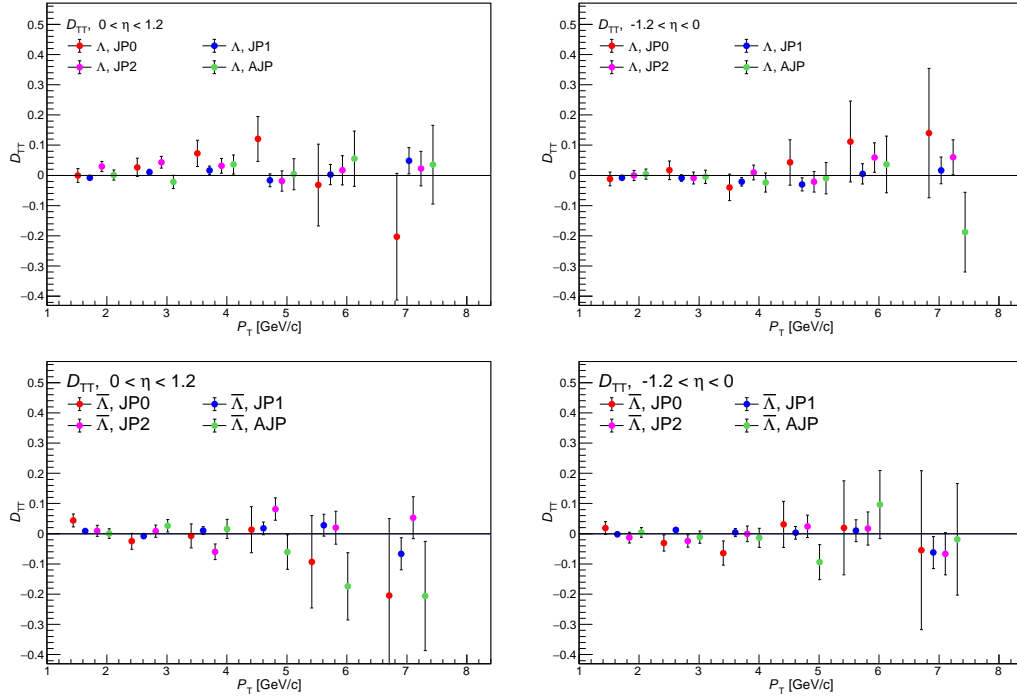


Figure 4.7:  $D_{TT}$  for the 4 JP trigger samples. The upper panel is for  $\Lambda$  and the lower is for  $\bar{\Lambda}$ . The  $\eta$  range is  $0 \sim 1.2$  in the left and  $-1.2 \sim 0$  in the right.



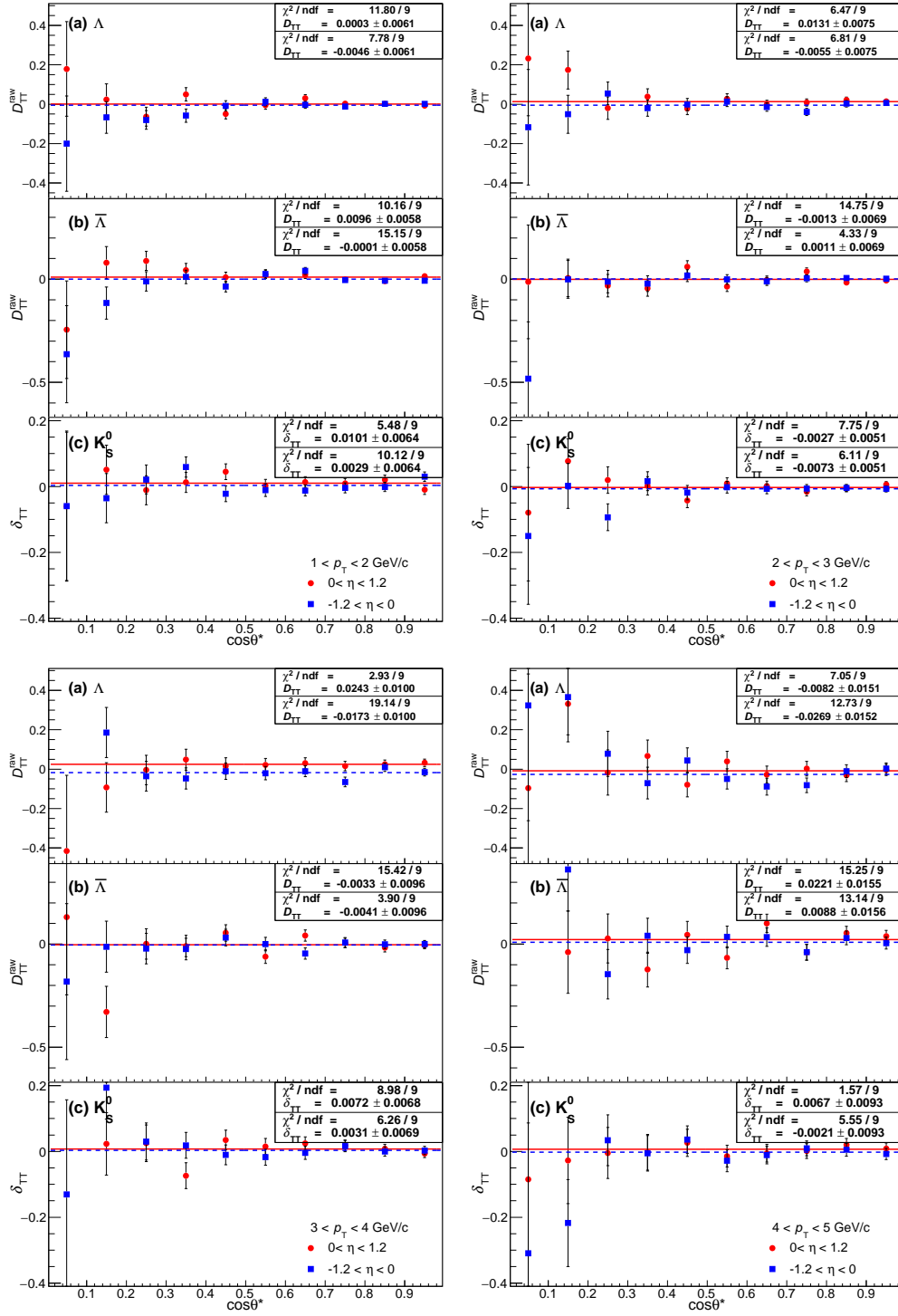


Figure 4.8:  $D_{\text{TT}}$  for  $\Lambda$  ( $\bar{\Lambda}$ ) and  $\delta_{\text{TT}}$  for  $K_S^0$  vs.  $\cos\theta^*$  in each  $p_{\text{T}}$  bin from the trigger-combined data sample.

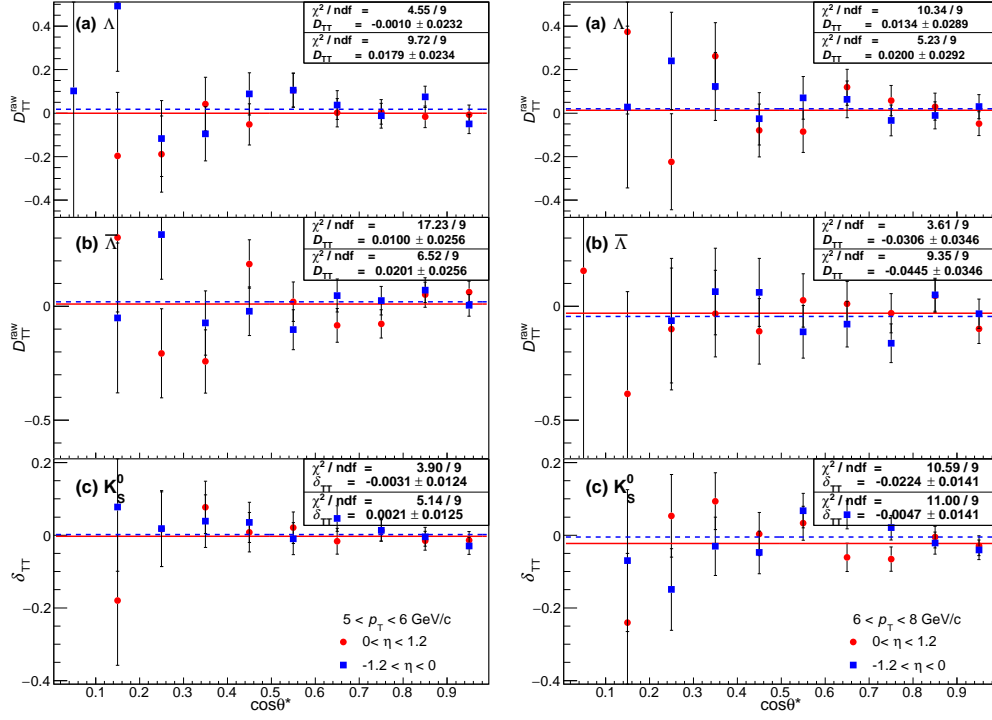


Figure 4.8:  $D_{\text{TT}}$  for  $\Lambda$  ( $\bar{\Lambda}$ ) and  $\delta_{\text{TT}}$  for  $K_S^0$  vs.  $\cos\theta^*$  in each  $p_{\text{T}}$  bin from the trigger-combined data sample.

$D_{\text{TT}}$  extracted from the JP trigger-combined data sample are shown in Fig. 4.9.

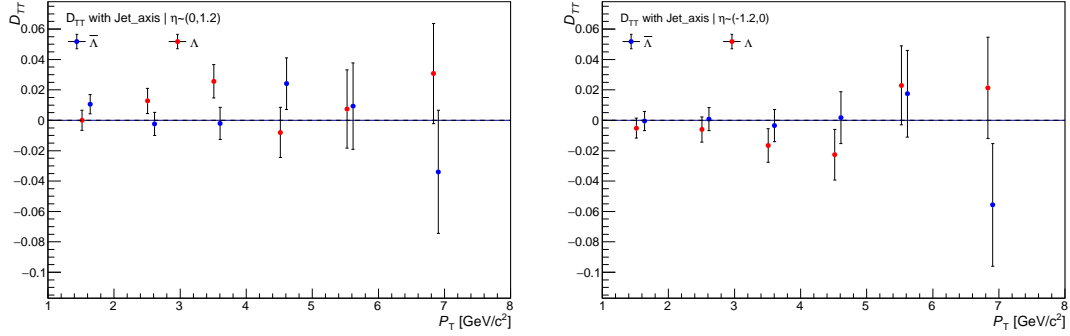


Figure 4.9:  $D_{\text{TT}}$  for the trigger-combined sample. The left and right plots are for  $0 < \eta < 1.2$  and  $-1.2 < \eta < 0$ , correspondingly.

$K_S^0$  was reconstructed in our analysis which is used to do the cross check. We constructed the so-called "spin asymmetry",  $\delta_{\text{TT}}$ , of  $K_S^0$  using the same structure with  $D_{\text{TT}}$  of  $\Lambda$  shown in Eq. 4.15 where the  $N$  is the number of  $K_S^0$  reconstructed and  $\alpha_{K_S^0}$  is assumed as 1 which used as the decay parameter of  $\Lambda$ .

$$\delta_{\text{TT}} = \frac{1}{\alpha_{K_S^0} P \langle \cos \theta^* \rangle} \frac{\sqrt{N^\uparrow(\cos \theta^*) N^\downarrow(-\cos \theta^*)} - \sqrt{N^\uparrow(-\cos \theta^*) N^\downarrow(\cos \theta^*)}}{\sqrt{N^\uparrow(\cos \theta^*) N^\downarrow(-\cos \theta^*)} + \sqrt{N^\uparrow(-\cos \theta^*) N^\downarrow(\cos \theta^*)}} \quad (4.15)$$

Higher statistics and lower background fraction make  $K_S^0$  a good choice to do the check. The results of  $\delta_{\text{TT}}$  versus  $p_T$  from trigger combined sample are shown in bottom panels in Fig. 4.8.

## 4.2 Cross check of $D_{\text{TT}}$ measurement method

The main results were extracted via the Cross-Ratio method. We also used the relative luminosity method to extract  $D_{\text{TT}}$  as the cross check. In the relative luminosity method,  $D_{\text{TT}}$  in a small  $\cos \theta^*$  interval is extracted via the equation following,

$$D_{\text{TT}} = \frac{1}{\alpha P_{\text{beam}} \langle \cos \theta^* \rangle} \frac{\left( \frac{N^{\uparrow\uparrow}}{R_4} + \frac{N^{\uparrow\downarrow}}{R_6} \right) - \left( N^{\downarrow\downarrow} + \frac{N^{\downarrow\uparrow}}{R_5} \right)}{\left( \frac{N^{\uparrow\uparrow}}{R_4} + \frac{N^{\uparrow\downarrow}}{R_6} \right) + \left( N^{\downarrow\downarrow} + \frac{N^{\downarrow\uparrow}}{R_5} \right)}. \quad (4.16)$$

The comparison between the results corresponding to the two methods is shown in Fig. 4.10. The result comparison between the two methods are consistent to each other. This is a good proof to the stability of our measurement method.

In the main results extraction, we used the jet axis as the substitute of the quark axis. The results extracted by using the hyperon axis as the substitute of the quark axis are shown in Fig 4.11 for the cross check and a good agreement is observed in the comparison.

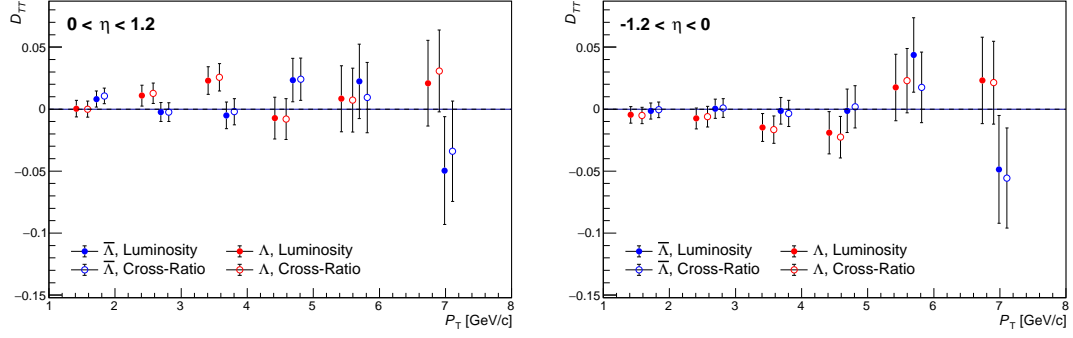


Figure 4.10: The comparison between the results extracted via Cross-Ratio method and Relative Luminosity method. The left and right plots are for  $0 < \eta < 1.2$  and  $-1.2 < \eta < 0$ , correspondingly.

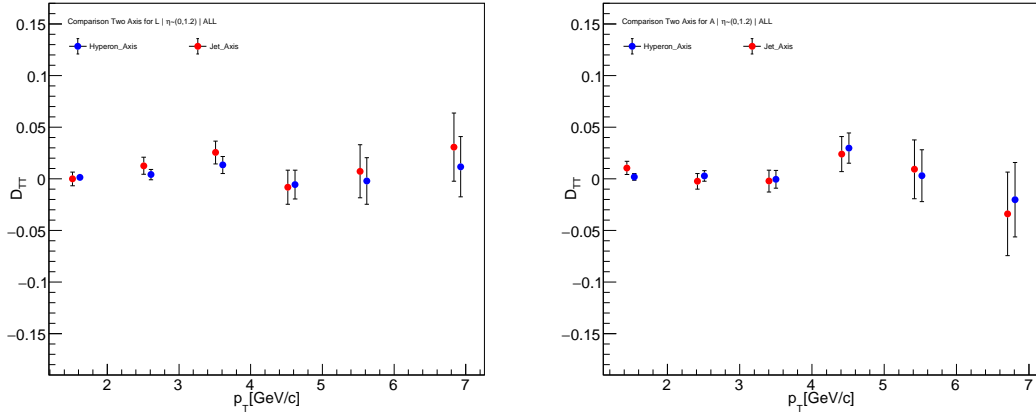


Figure 4.11: The comparison between the results extracted by using the hyperon axis and the jet axis as the substitute of the quark axis, separately.

## 5 MC Production and Data Comparison

### 5.1 MC Production

Private MC sample was generated to compare with data and further do the study of trigger bias. The MC sample was generated using pure pythia of version 6.4.28 [6] with Perugia 2012 tune [7] and GEANT-based simulation framework. The sample was generated in each  $\Lambda p_T$  and hard  $p_T$  interval separately and then combined with weight of hard  $p_T$  in each  $\Lambda p_T$  interval. The hard  $p_T$  distributions for each  $\Lambda p_T$  are shown in Fig. 5.1.

The hard  $p_T$  does not comply with exponential distribution perfectly. This is because that only  $\Lambda (\bar{\Lambda})$  events were stored by using  $\Lambda$  filter. The  $\Lambda$  filter was used in order to improve the generation efficiency and save disk space. The filter is based on the StMCfilter and requests at least one  $\Lambda$  or  $\bar{\Lambda}$  in a pythia event. In the generation, we set  $\text{PARP}(90)=0.213$  which is consistent with Embedding production of jet  $A_{LL}$  analysis by Kevin and  $K\_factor = 2$  which makes the  $p_T$  spectrum of  $\Lambda$  hyperons better consistent with data.

Jet Patch trigger conditions are applied using the standard STAR trigger simulator. Particle identification of  $p$ ,  $\pi$  and  $\Lambda$  are implemented via StAssociateMaker in MC events then the same selection cuts are applied on except  $dE/dx$ . The efficiency of the track association is about 70% for single track and thus the efficiency of finding a  $\Lambda$  into  $p\pi$  is only 50%, which is an obstacle to generate MC sample with enough statistics. Jets are reconstructed with anti- $K_T$  algorithm with  $R = 0.6$  which is same with data.

### 5.2 Data and MC Comparison

The comparisons between data and MC were made. The  $\Lambda (\bar{\Lambda})$  with  $p_T$  of  $3 \sim 4 \text{ GeV}/c$  from JP1 sample are used as the example shown in the following figures.

The comparison of primary vertex  $z$  after reweighting between data and simulation is shown in Fig. 5.2. The reweighting is made for each trigger sample separately. They are consistent with each other as the expected.

The comparisons of reconstructed variables for jet near-side  $\Lambda$  and  $\bar{\Lambda}$  between data and simulation are shown in the following plots. The JP1 sample is used here for example and the others could be found from the link:

[http://www.star.bnl.gov/protected/spin/jcmei/pp200trans\\_2012/htmlCode/pp200trans\\_2012\\_MCDataComparison\\_J1.html](http://www.star.bnl.gov/protected/spin/jcmei/pp200trans_2012/htmlCode/pp200trans_2012_MCDataComparison_J1.html)

Fig. 5.3 and Fig. 5.4 show the comparisons of the invariant mass,  $p_T$ ,  $\eta$ ,  $\phi$  for jet near-side  $\Lambda$  and  $\bar{\Lambda}$ . In  $\eta$  comparison, data lower than simulation at the mid-rapidity is related to the efficiency drop in data from pileup. The MC sample was produced using pure pythia and pileup is not involved in.

Fig. 5.5 and Fig. 5.6 show the comparison of  $p_T$ ,  $\eta$ ,  $\phi$  for  $p$  and  $\pi$  from jet near-side  $\bar{\Lambda}$  and  $\Lambda$ . The similar behaviour can be found in  $\eta$  distribution.

The comparisons of selection cuts are shown in the following plots.

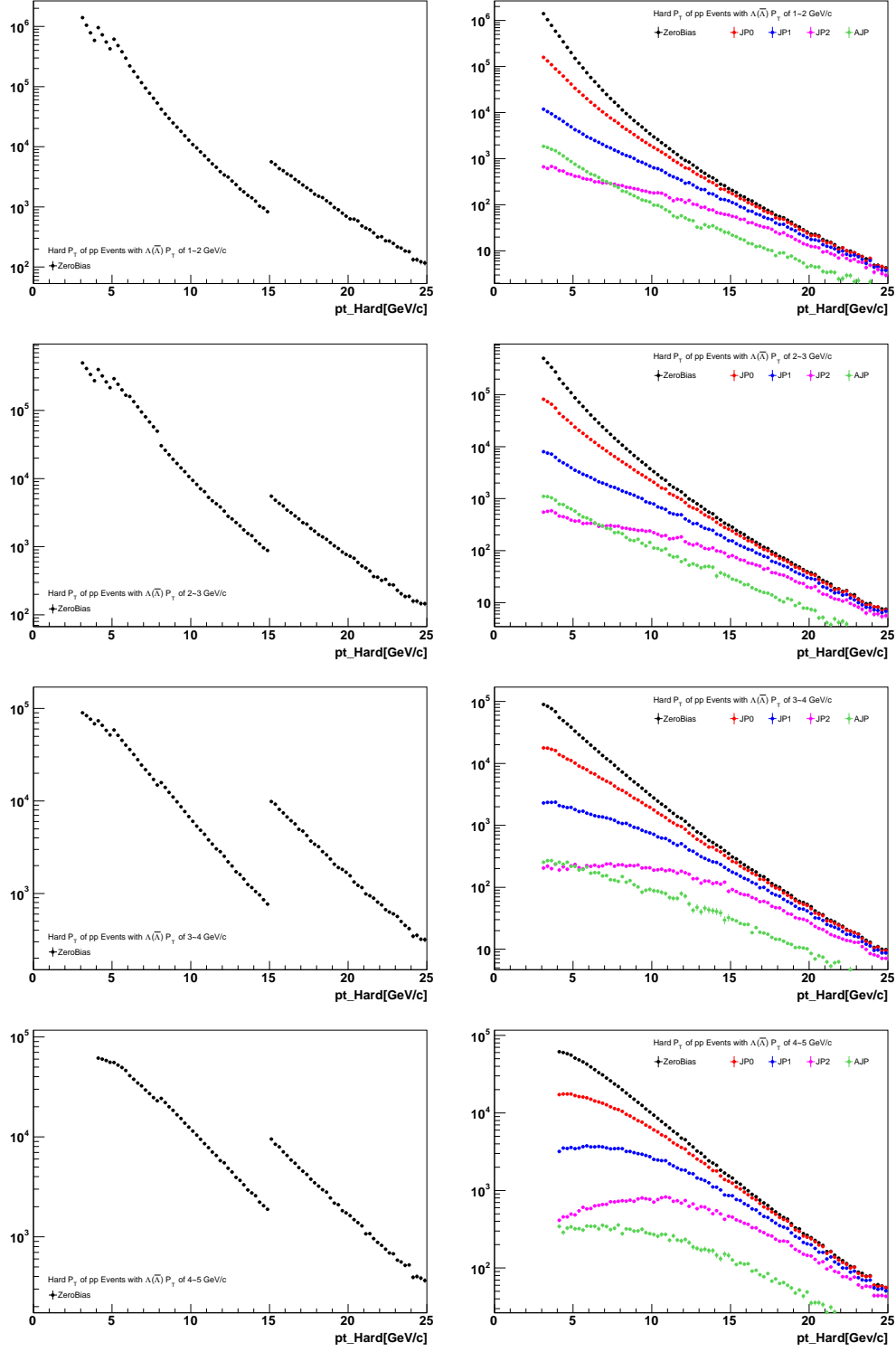


Figure 5.1: Hard Hard  $p_T$  distributions before (left) and after (right) weighting for each of  $\Lambda$   $p_T$  bins.

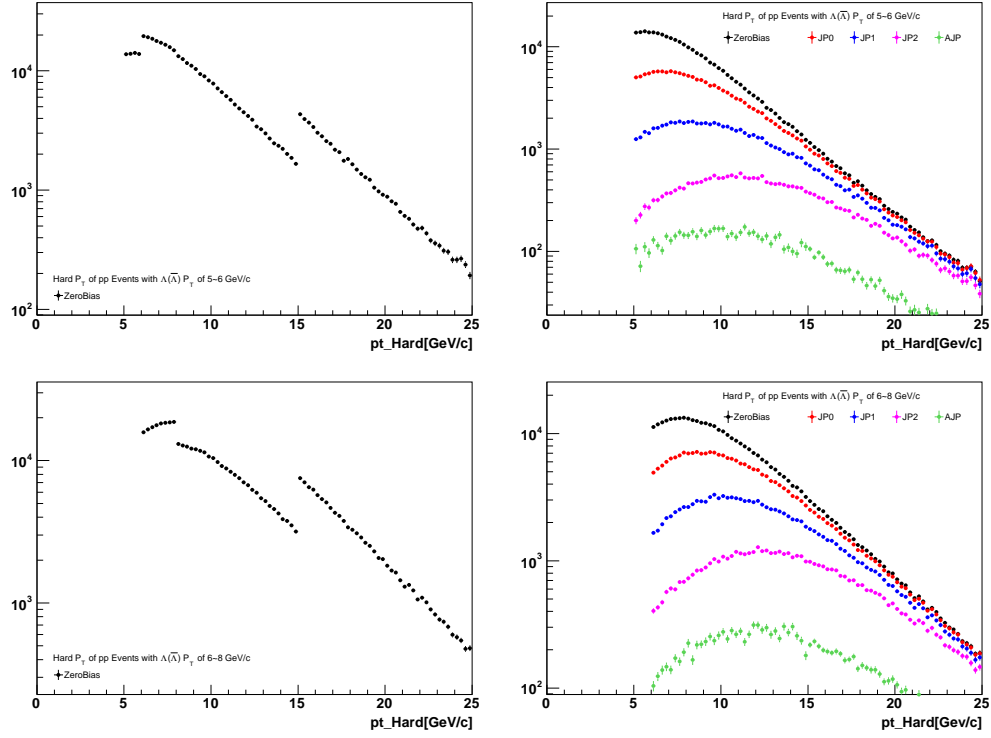


Figure 5.1: Hard  $p_T$  distribution before (left) and after (right) weighting for each of  $\Lambda$   $p_T$  bins.

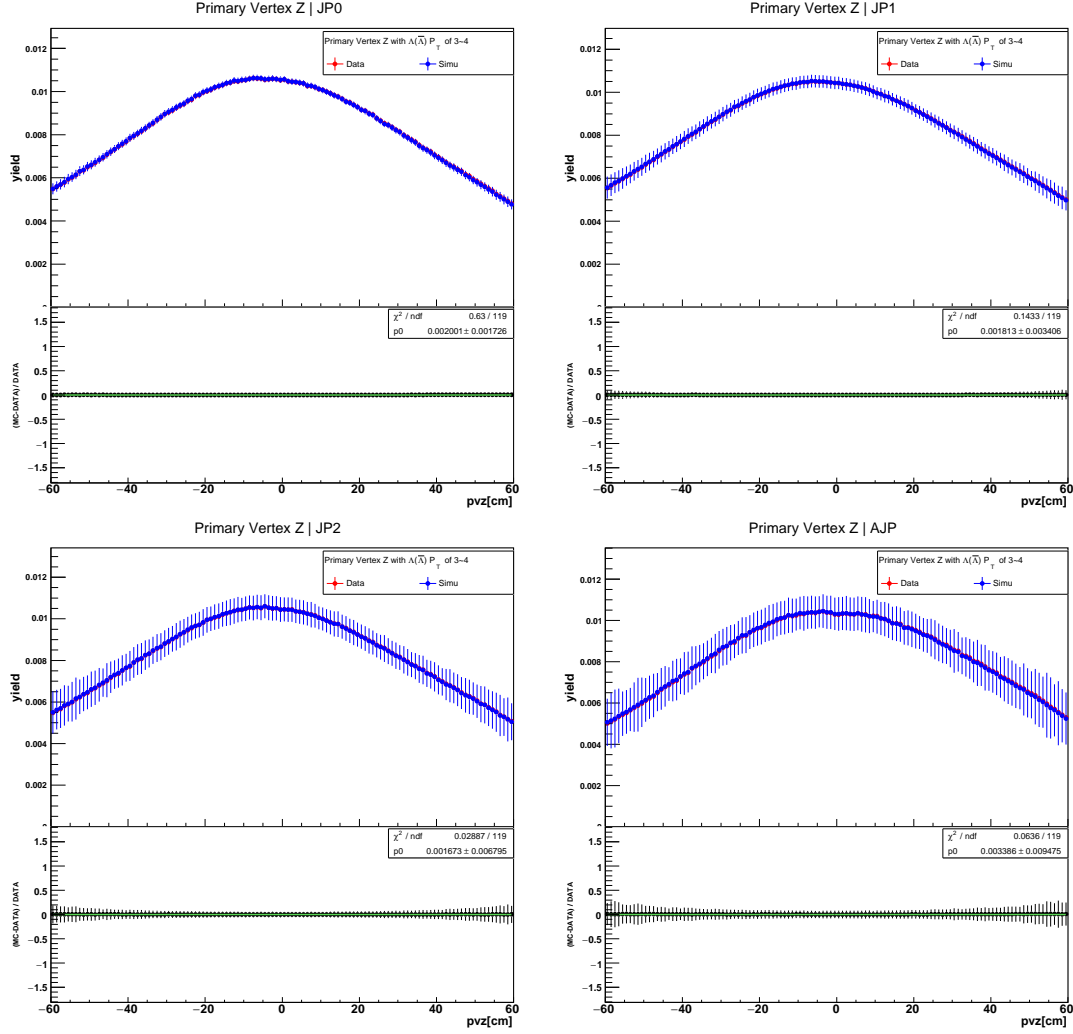


Figure 5.2: Comparison of primary vertex z after reweighting. The plots are for JP0, JP1, JP2, AJP trigger conditions from left to right in sequence.



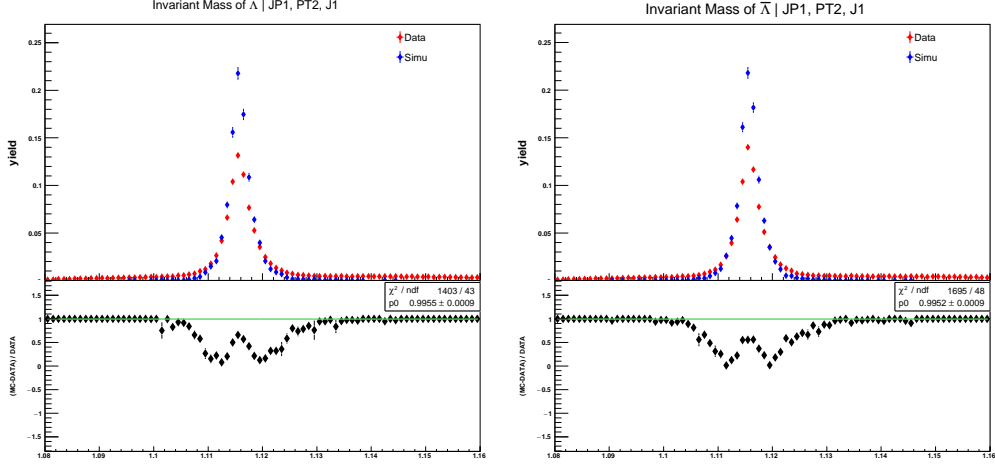


Figure 5.3: Comparison of reconstructed variables of  $p(\bar{p})$  from jet near-side  $\Lambda(\bar{\Lambda})$ . The invariant mass of  $\bar{\Lambda}$  are shown in the left panel and the right one is for  $\Lambda$ .

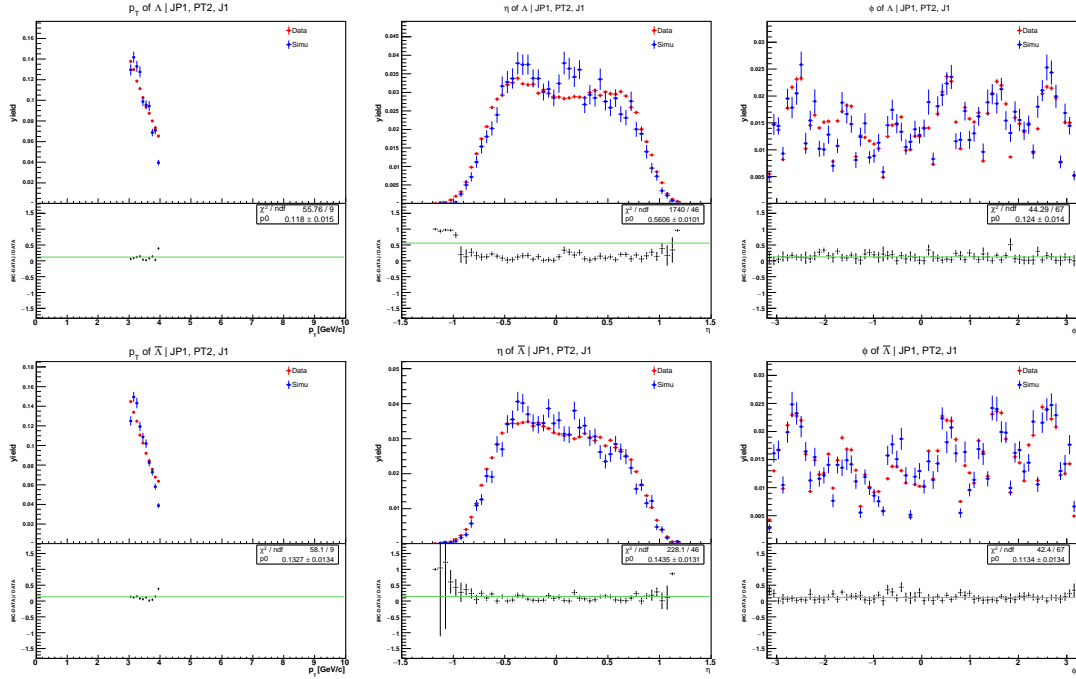


Figure 5.4: Comparison of reconstructed variables for jet near-side  $\Lambda$  and  $\bar{\Lambda}$ . The  $p_T$ ,  $\eta$ ,  $\phi$  comparisons for  $\Lambda$  are shown in the upper panel and the lower panel is for  $\bar{\Lambda}$ .

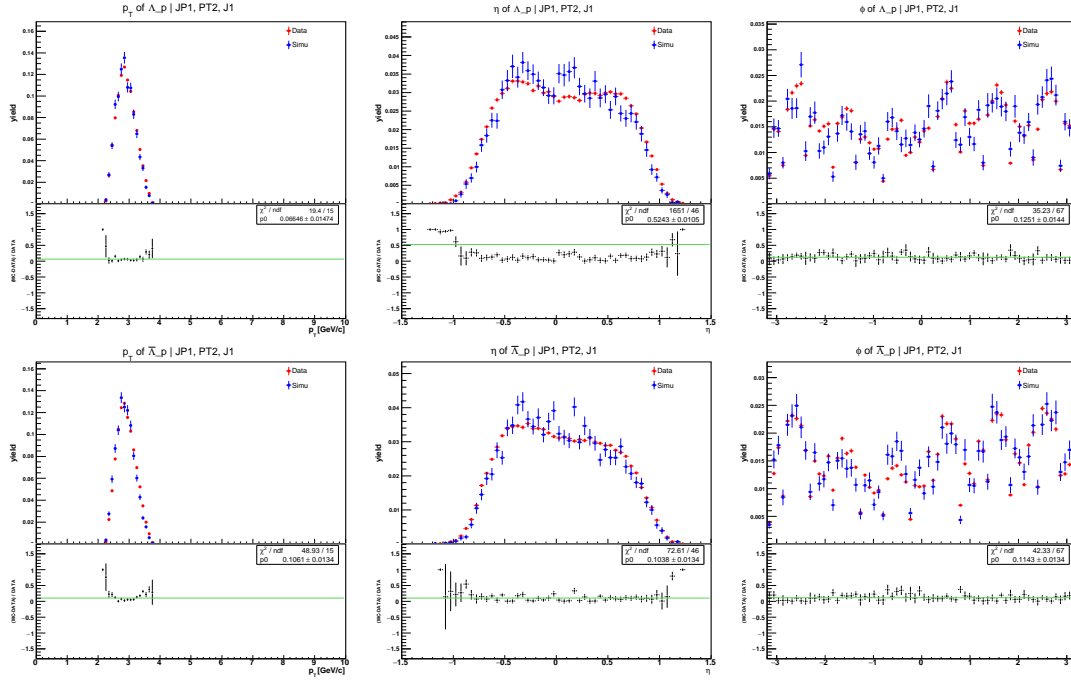


Figure 5.5: Comparisons of reconstructed variables of  $p$  ( $\bar{p}$ ) from jet near-side  $\Lambda$  ( $\bar{\Lambda}$ ). The  $p_T$ ,  $\eta$ ,  $\phi$  comparisons for  $p$  from  $\Lambda$  are shown in the upper panel and the lower panel is for  $\bar{p}$  from  $\bar{\Lambda}$ .

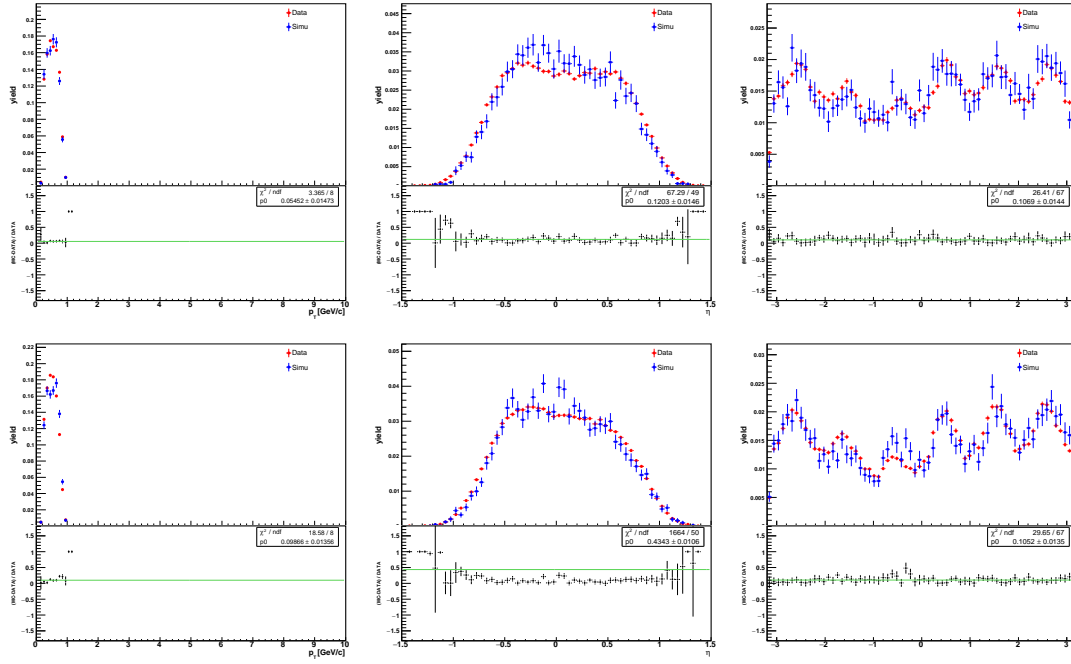


Figure 5.6: Comparisons of reconstructed variables for  $\pi^-$  ( $\pi^+$ ) decay from jet near-side  $\Lambda$  ( $\bar{\Lambda}$ ). The  $p_T$ ,  $\eta$ ,  $\phi$  comparisons for  $\pi^-$  from  $\Lambda$  are shown in the upper panel and the lower panel is for  $\pi^+$  from  $\bar{\Lambda}$ .

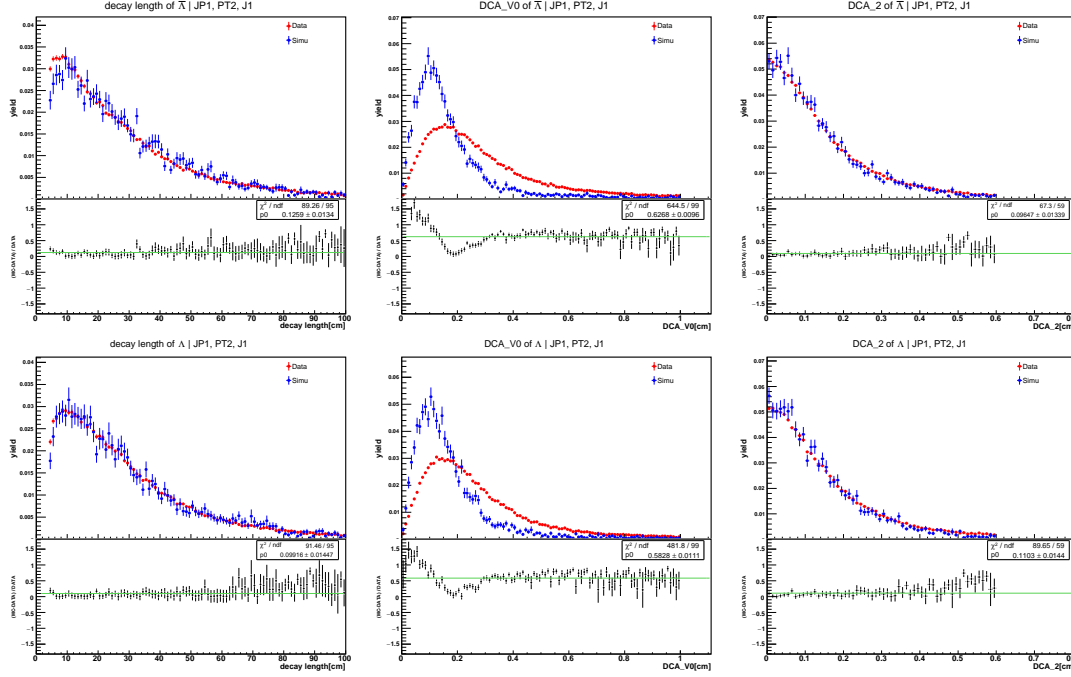


Figure 5.7: Comparisons of selection cuts for jet near-side  $\Lambda$  and  $\bar{\Lambda}$ . The decay length, DCA\_V0, DCA\_2 comparisons for  $\Lambda$  are shown in the upper panel and the lower panel is for  $\bar{\Lambda}$ .

Decay length, DCA\_V0 and DCA\_2 comparisons are shown in Fig. 5.7. Significant difference can be observed in DCA\_V0 comparison. This is because the resolution of primary vertex in simulation is better than in data.

The comparisons of DCA\_p and DCA\_π are shown in Fig. 5.8.

The comparisons between data and simulation is generally consistent with each other.

In order to make sure whether the annihilation effect of  $\bar{p}$  is simulated in the MC production, the ratio of  $\bar{\Lambda}/\Lambda$  is studied in both simulation and data and the ratios for different classes of production are shown in Fig. 5.9. The natural yield of  $\bar{\Lambda}$  should be lower than  $\Lambda$  in  $pp$  collisions and the ratio is about 88% varying with  $p_T$  [1]. The ratios shown in Fig. 5.9 indicate that more  $\bar{\Lambda}$  than  $\Lambda$  are reconstructed relatively in lower  $p_T$  bins. This is caused by the annihilation effect of  $\bar{p}$  which makes it easier to pass the trigger threshold for the event including  $\bar{\Lambda}$ . With the increasing of  $p_T$ , the energy contributed from the annihilation of  $\bar{p}$  is no longer the main fraction making the trigger fired so the ratio is going down.

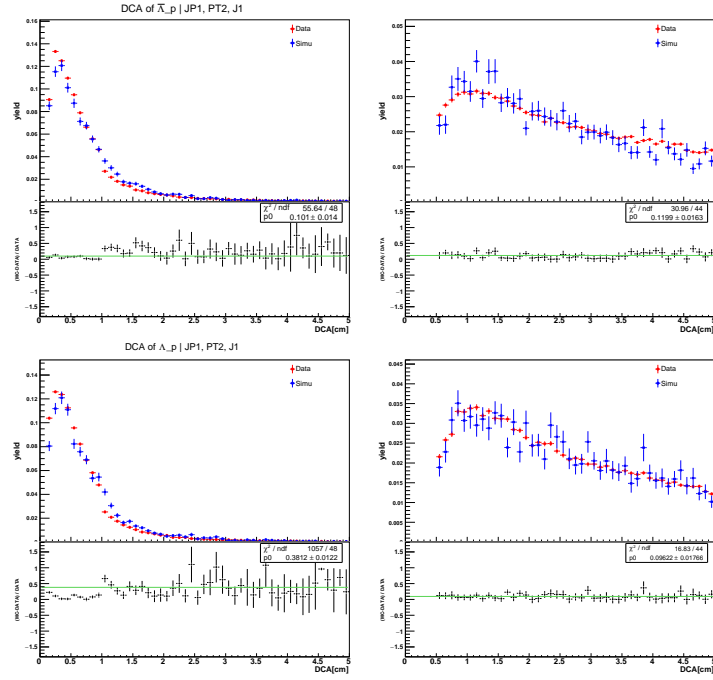


Figure 5.8: DCA of  $p$ ,  $\pi$  from jet near-side  $\Lambda$  and  $\bar{\Lambda}$ . The upper panel is for  $\Lambda$  and the lower panel is for  $\bar{\Lambda}$ .

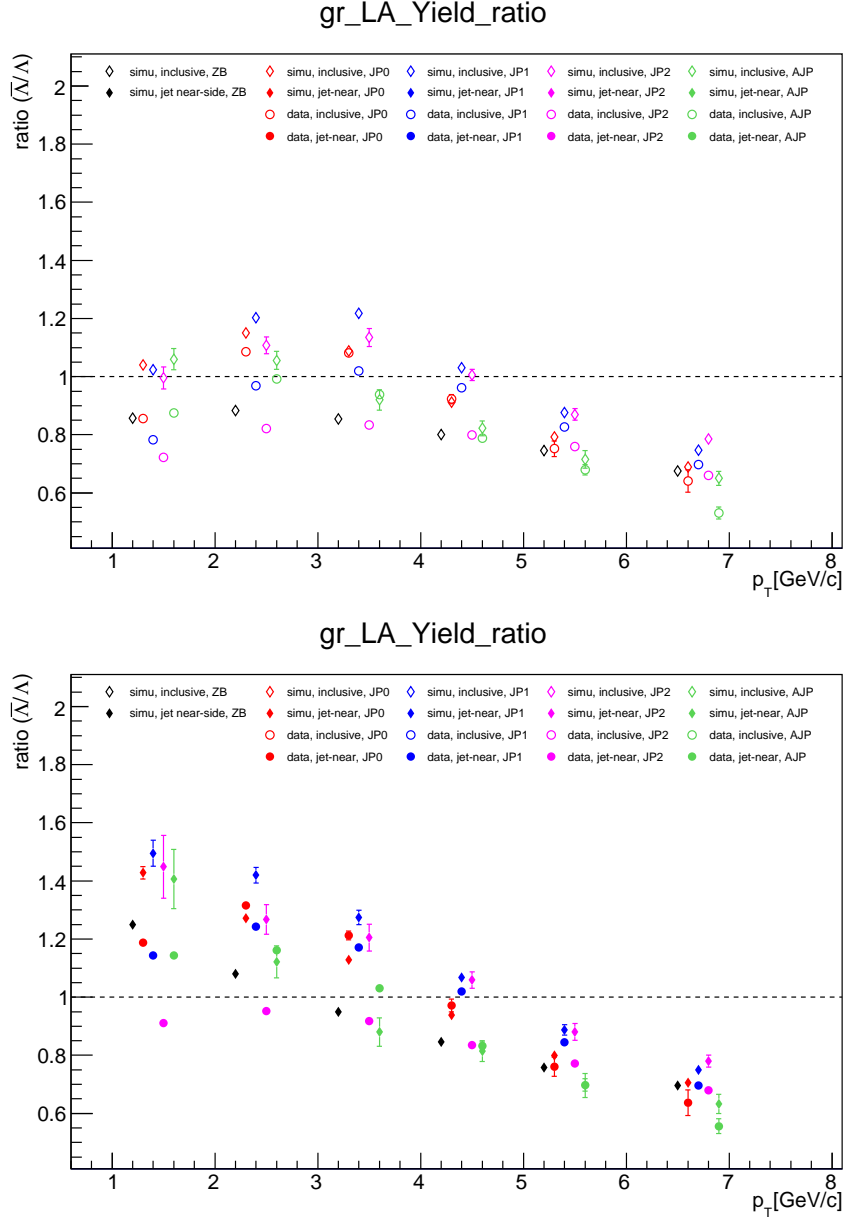


Figure 5.9: The ratio of  $\bar{\Lambda}/\Lambda$  yield in different states. The left plot is for inclusive  $\Lambda$  and  $\bar{\Lambda}$  and the right one is for the jet near-side  $\Lambda$  and  $\bar{\Lambda}$ .

## 6 Evaluation of Systematic Uncertainty

The systematic uncertainties in this analysis are stated in this section. Uncertainty sources we have considered include:

- the decay parameter,
- the measurement of beam polarization,
- the pileup effect,
- the estimation of residual background fraction,
- the trigger bias.

The systematic uncertainty caused by the trigger bias for the results of the combination sample was combined with weights determined by the point-by-point inverse statistical variance (as in an ordinary weighted average). The systematic scale uncertainties were reevaluated for the  $D_{\text{TT}}$  value of the combined sample. The systematic uncertainties from the estimation of the residual background fraction and pileup were reevaluated using the trigger combined sample.

### 6.1 Uncertainty from Decay parameter

The decay parameter  $\alpha$  is taken from external measurements. We use the PDG value,  $0.0642 \pm 0.013$  [4]. This 2% scale uncertainty is common to the JP trigger samples.

### 6.2 Uncertainty from Beam polarization

The magnitude of the beam polarizations is measured by the RHIC polarimetry group and has a 3.4% scale uncertainty for Run12  $\sqrt{s} = 100$  GeV data.

The beam polarization and its uncertainty are evaluated using the present data. The details of the measurement could be found from the link:

<http://public.bnl.gov/docs/cad/Documents/RHIC%20polarization%20for%20Runs%209-12.pdf> The uncertainty of this part is estimated via the scale multiply the  $D_{\text{TT}}$  mean value of the trigger-combined data sample.

### 6.3 Uncertainty from Estimation of Residual Background Fraction

The transverse spin transfer  $D_{\text{TT}}$  is extracted using Eq. 6.1 considering the background subtraction.

$$D_{\text{TT}} = \frac{D_{\text{TT}}^{\text{raw}} - r D_{\text{TT}}^{\text{bkg}}}{1 - r}, \quad (6.1)$$

where  $D_{\text{TT}}^{\text{raw}}$  is the  $D_{\text{TT}}$  value using the  $\Lambda$  candidates in the signal mass window containing residual backgrounds. The uncertainty in the residual background fraction is taken into account as a systematic uncertainty of  $D_{\text{TT}}$ . The background fraction used in the main results is evaluated by counting events in the side-bands, interpolating them to the signal region, and comparing them with the observed counts in the signal region.

In order to estimate the systematic uncertainty caused by the background estimation, the background fraction was estimated also from a linear fit to the background and

Gaussian to describe the signal. The difference of the resulting  $D_{\text{TT}}$  values for these two methods is taken as the systematic uncertainty in  $r$ . The results are listed in TABLE.6.1 with  $p_T$  for trigger combined data sample.

Table 6.1: Uncertainty to  $D_{\text{TT}}$  from estimation of residual background fraction for  $\Lambda$  and  $\bar{\Lambda}$

|               | $0 < \eta < 1.2$ |                 | $-1.2 < \eta < 0$ |                 |
|---------------|------------------|-----------------|-------------------|-----------------|
| $p_T$ [GeV/c] | $\Lambda$        | $\bar{\Lambda}$ | $\Lambda$         | $\bar{\Lambda}$ |
| 1 $\sim$ 2    | 0.0000           | 0.0000          | 0.0000            | 0.0000          |
| 2 $\sim$ 3    | 0.0000           | 0.0000          | 0.0000            | 0.0000          |
| 3 $\sim$ 4    | 0.0000           | 0.0000          | 0.0000            | 0.0000          |
| 4 $\sim$ 5    | 0.0000           | 0.0001          | 0.0002            | 0.0004          |
| 5 $\sim$ 6    | 0.0009           | 0.0001          | 0.0005            | 0.0003          |
| 6 $\sim$ 8    | 0.0028           | 0.0002          | 0.0002            | 0.0007          |

#### 6.4 Uncertainty from Pileup

The effect of event-overlap was studied by hyperon data sample and examining the hyperon yield per STAR event versus collision rate. The ratio is expected to be constant in the absence of pile-up when the collision rate was 20 kHz. Constant and linear extrapolation to small collision rate, where pileup logically vanishes, was used to assess this systematic uncertainty contribution. The factor of pileup effect was estimated using the 4 JP samples and separately for the spin 4-bit sorted sample. Fig.6.1 and Fig.6.2 show the distribution for  $\Lambda$  and  $\bar{\Lambda}$  of JP trigger combined sample.

The values are tabulated in TABLE.6.2.

The systematic uncertainty propagation on  $D_{\text{TT}}$  due to pileup is calculated by determining the difference between the extracted  $D_{\text{TT}}$  sample and the pileup corrected  $D_{\text{TT}}$  for each spin 4-bit configuration,

$$(\delta D_{\text{TT}}^{\text{sys.pileup}})^2 = \sum_{k=++,+-,+-,--} [D_{\text{TT}}(n^k) - D_{\text{TT}}((1 - u^k)n^k)]^2, \quad (6.2)$$

where  $n^{++}$ ,  $n^{-+}$ ,  $n^{+-}$ , and  $n^{--}$  are the spin 4-bit sorted hyperons counts and  $u^{++}$ ,  $u^{-+}$ ,  $u^{+-}$ , and  $u^{--}$  are the spin 4-bit sorted pileup contributions. The uncertainty values from pileup for trigger combined data sample are tabulated in TABLE.6.3.

Table 6.2: Factors of pileup contribution for  $\Lambda$  and  $\bar{\Lambda}$  for each spin configuration.

| spin bit        | 5                 | 6                 | 9                 | 10                |
|-----------------|-------------------|-------------------|-------------------|-------------------|
| $\Lambda$       | $0.087 \pm 0.010$ | $0.104 \pm 0.011$ | $0.084 \pm 0.010$ | $0.097 \pm 0.011$ |
| $\bar{\Lambda}$ | $0.093 \pm 0.010$ | $0.076 \pm 0.010$ | $0.092 \pm 0.010$ | $0.088 \pm 0.010$ |



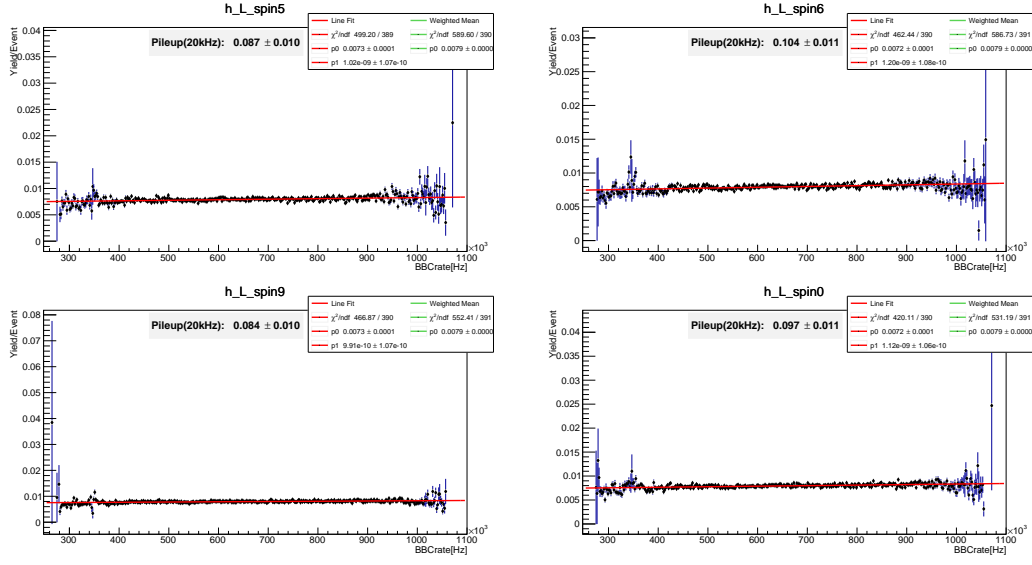


Figure 6.1: Hyperon yield vs. collision rate in spin 4-bit configurations of  $\Lambda$  for JP trigger combination. The upper-left graph is for spinbit-5, the upper right graph is for spinbit-6, the low left one is for spinbit-9 and the low right one is for spinbit-10.

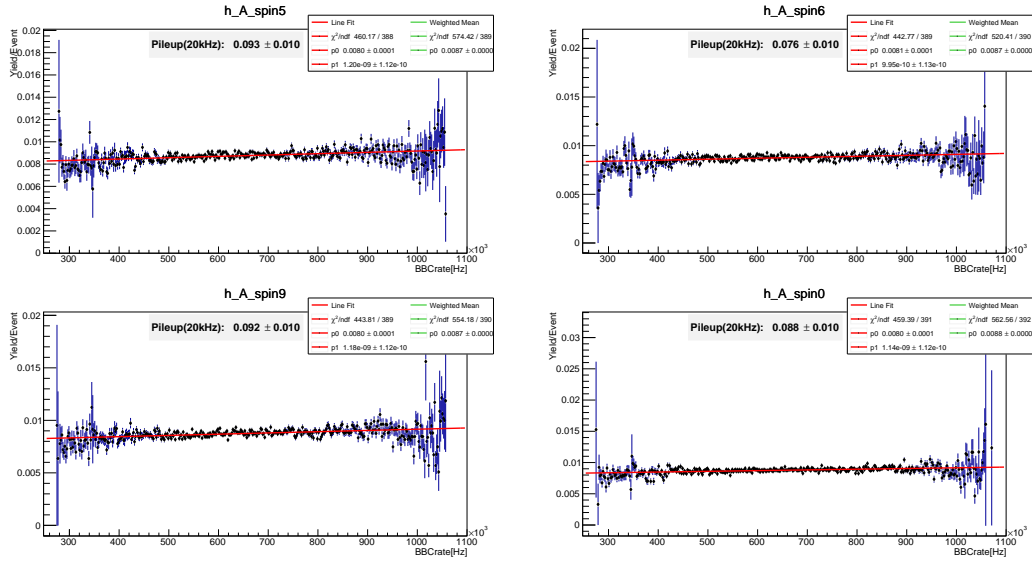


Figure 6.2: Hyperon yield vs. collision rate in spin 4-bit configurations of  $\bar{\Lambda}$  for JP trigger combination. The upper-left graph is for spinbit-5, the upper right graph is for spinbit-6, the low left one is for spinbit-9 and the low right one is for spinbit-10.

Table 6.3: Uncertainty to  $D_{\text{TT}}$  from pileup for  $\Lambda$  and  $\bar{\Lambda}$

| $p_{\text{T}}$ [GeV/c] | $0 < \eta < 1.2$ |                 | $-1.2 < \eta < 0$ |                 |
|------------------------|------------------|-----------------|-------------------|-----------------|
|                        | $\Lambda$        | $\bar{\Lambda}$ | $\Lambda$         | $\bar{\Lambda}$ |
| 1 $\sim$ 2             | 0.0005           | 0.0001          | 0.0006            | 0.0003          |
| 2 $\sim$ 3             | 0.0002           | 0.0005          | 0.0007            | 0.0003          |
| 3 $\sim$ 4             | 0.0002           | 0.0007          | 0.0002            | 0.0011          |
| 4 $\sim$ 5             | 0.0017           | 0.0012          | 0.0014            | 0.0007          |
| 5 $\sim$ 6             | 0.0013           | 0.0016          | 0.0013            | 0.0012          |
| 6 $\sim$ 8             | 0.0009           | 0.0022          | 0.0017            | 0.0031          |

## 6.5 Uncertainty from Trigger Bias

The data samples in this analysis are triggered for energy deposits in BEMC and EEMC, but not directly on the  $\Lambda$  and  $\bar{\Lambda}$ . The trigger condition may thus introduce a bias that needs to be taken into account in either the measurement or the phenomenological interpretation of the data. We choose to account for the possible size of this effect in a systematic uncertainty in the measurements and have considered three main manifestations:

- changes in the fractional momentum  $z$  of the produced  $\Lambda$  and  $\bar{\Lambda}$  within the associated jet,
- changes in the relative contributions from different hard sub-processes and fragmenting partons with different flavors in the production.
- possible differences in the fraction of feed-down contributions,

The uncertainty caused by each of the three items is estimated in each of the JP trigger data samples separately, then combined using ratios of each of the JP trigger data samples extracted in data as weights. For the trigger combined data sample, the uncertainties of the three items are added in quadrature.

These possible changes are examined in MC simulation before and after applying the Jet Patch trigger conditions using the standard STAR trigger simulator and GEANT-based simulation framework. Events were produced using PYTHIA version 6.4.28 [6] with Perugia 2012 tune [7].

Theoretical model [8] is used to evaluate the uncertainty into  $D_{\text{TT}}$  from trigger bias. The polarization of hyperons is separated into two parts as shown in Eq. 6.3.

$$P_{H_i} = \sum_f t_{H_i,f}^F P_f R_{H_i,f} + \sum_j t_{H_i,H_j}^D P_{H_j} R_{H_i,H_j}, \quad (6.3)$$

The polarization of  $H_i$  hyperon is the sum of the polarization of  $H_i$  produced directly from the fragmenting parton and produced from other particle ( $H_j$ ) decay. The first part shows the polarization of hyperons produced directly from fragmenting parton, where  $t_{H_i,f}^F$  is the transfer of polarization from the fragmenting parton to final state

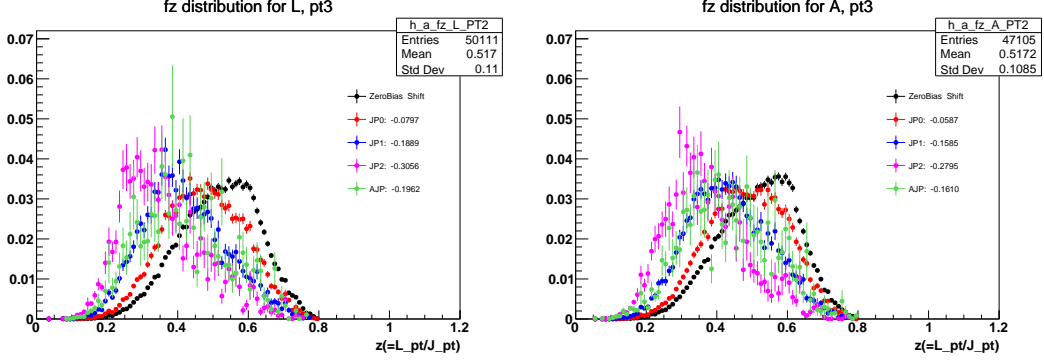


Figure 6.3:  $z$  distribution for  $\Lambda$  (in the left) and  $\bar{\Lambda}$  (in the right) with  $p_T$  of  $3 \sim 4$  GeV/ $c$ . X axis shows  $z$  and Y axis shows the yield after normalized. The shifts of the mean values related to the mean value of zero bias sample are shown in the legend.

hyperons directly,  $P_f$  is the polarization of the fragmenting parton and  $R_{H_i,f}$  is the relative fraction of  $H_i$  produced directly from fragmenting parton; The second part is about the polarization of  $H_i$  produced from other hyperons decay and  $t_{H_i,H_j}^D$  is the transfer of polarization from other polarized hyperons.

### 6.5.1 Fractional momentum $z$

The fractional momentum  $z$  is defined as the ratio of  $p_T^\Lambda$  over  $p_T^{jet.asso}$ , namely

$$z = \frac{p_T^\Lambda}{p_T^{jet.associated}} \quad (6.4)$$

It can be changed with JP trigger condition applied and the  $D_{TT}$  is dependent on  $z$  based on the model calculation.  $z$  are extracted from the MC sample before and after applying JP trigger conditions and shown in Fig. 6.3.

The  $z$ -dependent  $D_{TT}$  for  $\Lambda$  and  $\bar{\Lambda}$  calculated using the model are shown in Fig. 6.4.

The  $D_{TT}$  values are corresponding to  $z$  for each trigger are obtained using Eq. 6.5,

$$D_{TT} = \frac{\sum_i D_{TT}^i n^i}{\sum_i n^i}, \quad (6.5)$$

where  $n^i$  and  $D_{TT}^i$  are the number of  $\Lambda$  or  $\bar{\Lambda}$  offered by the MC sample and the value of  $D_{TT}$  calculated using the model in the  $i$ th bin along  $z$ . We assigned the  $D_{TT}$  value of the last bin in the  $D_{TT}$  versus  $z$  to the bins with  $z > 0.85$  and the events in the bins with  $z > 1.0$  are excluded in the calculation.

The differences of  $D_{TT}$  between before and after applying the trigger conditions are used as the systematic uncertainty to  $D_{TT}$  from  $z$  shift. The uncertainty is shown in TABLE. 6.4

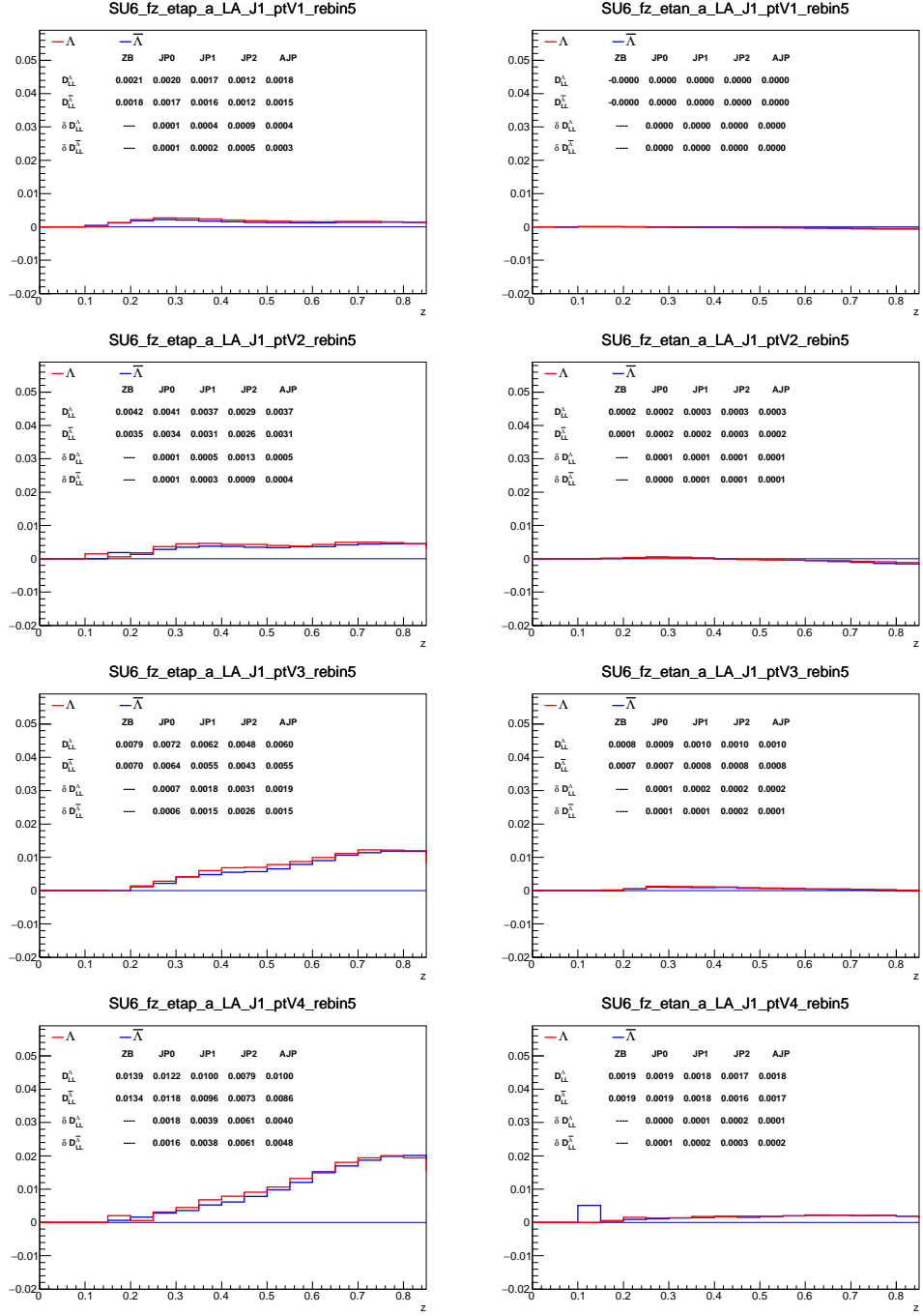


Figure 6.4:  $D_{TT}$  for  $\Lambda$  and  $\bar{\Lambda}$  versus  $z$  calculated using the model in different  $p_T$  bins with positive  $\eta$  (left) and negative  $\eta$  (right).

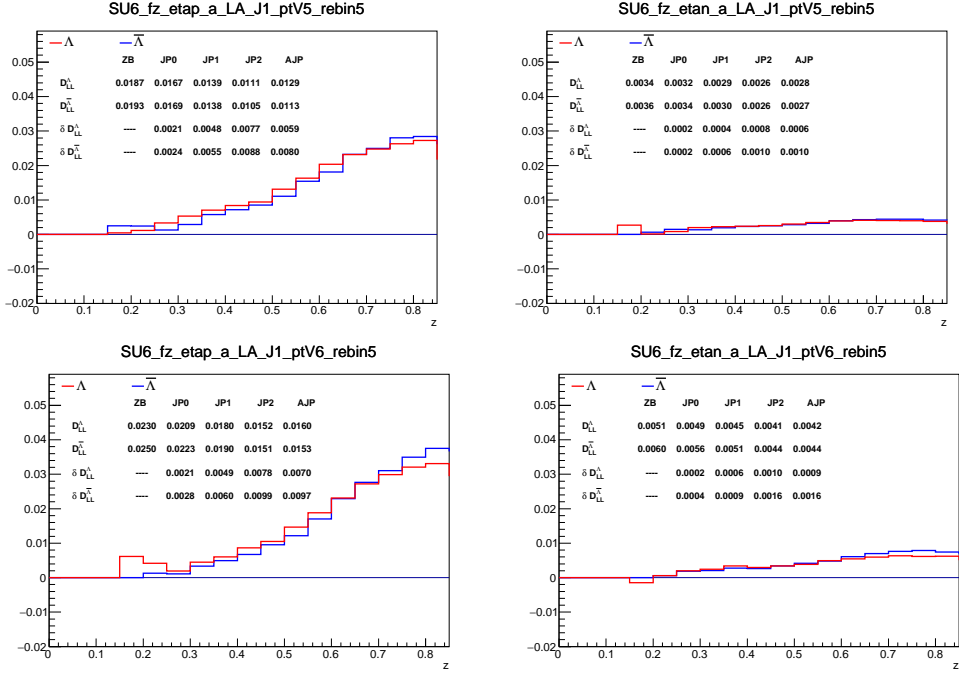


Figure 6.4:  $D_{TT}$  for  $\Lambda$  and  $\bar{\Lambda}$  versus  $z$  calculated using the model in different  $p_T$  bins with positive  $\eta$  (left) and negative  $\eta$  (right).

Table 6.4: Uncertainty to  $D_{TT}$  from  $z$  shift for  $\Lambda$  and  $\bar{\Lambda}$

| $0 < \eta < 1.2$  |           |                 |           |                 |           |                 |           |                 |           |                 |
|-------------------|-----------|-----------------|-----------|-----------------|-----------|-----------------|-----------|-----------------|-----------|-----------------|
|                   | JP0       |                 | JP1       |                 | JP2       |                 | AJP       |                 | Combined  |                 |
| $p_T$             | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ |
| $1 \sim 2$        | 0.0001    | 0.0001          | 0.0004    | 0.0002          | 0.0009    | 0.0005          | 0.0004    | 0.0003          | 0.0005    | 0.0003          |
| $2 \sim 3$        | 0.0001    | 0.0001          | 0.0005    | 0.0003          | 0.0013    | 0.0009          | 0.0005    | 0.0004          | 0.0007    | 0.0004          |
| $3 \sim 4$        | 0.0007    | 0.0006          | 0.0018    | 0.0015          | 0.0031    | 0.0026          | 0.0019    | 0.0015          | 0.0021    | 0.0017          |
| $4 \sim 5$        | 0.0018    | 0.0016          | 0.0039    | 0.0038          | 0.0061    | 0.0061          | 0.0040    | 0.0048          | 0.0045    | 0.0044          |
| $5 \sim 6$        | 0.0021    | 0.0024          | 0.0048    | 0.0055          | 0.0077    | 0.0088          | 0.0059    | 0.0080          | 0.0058    | 0.0067          |
| $6 \sim 8$        | 0.0021    | 0.0028          | 0.0049    | 0.0060          | 0.0078    | 0.0099          | 0.0070    | 0.0097          | 0.0061    | 0.0077          |
| $-1.2 < \eta < 0$ |           |                 |           |                 |           |                 |           |                 |           |                 |
|                   | JP0       |                 | JP1       |                 | JP2       |                 | AJP       |                 | Combined  |                 |
| $p_T$             | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ |
| $1 \sim 2$        | 0.0000    | 0.0000          | 0.0000    | 0.0000          | 0.0000    | 0.0000          | 0.0000    | 0.0000          | 0.0000    | 0.0000          |
| $2 \sim 3$        | 0.0001    | 0.0000          | 0.0001    | 0.0001          | 0.0001    | 0.0001          | 0.0001    | 0.0001          | 0.0001    | 0.0001          |
| $3 \sim 4$        | 0.0001    | 0.0001          | 0.0002    | 0.0001          | 0.0002    | 0.0002          | 0.0002    | 0.0001          | 0.0002    | 0.0001          |
| $4 \sim 5$        | 0.0000    | 0.0001          | 0.0001    | 0.0002          | 0.0002    | 0.0003          | 0.0001    | 0.0002          | 0.0001    | 0.0002          |
| $5 \sim 6$        | 0.0002    | 0.0002          | 0.0004    | 0.0006          | 0.0008    | 0.0010          | 0.0006    | 0.0010          | 0.0006    | 0.0008          |
| $6 \sim 8$        | 0.0002    | 0.0004          | 0.0006    | 0.0009          | 0.0010    | 0.0016          | 0.0009    | 0.0016          | 0.0008    | 0.0012          |

### 6.5.2 Subprocess & flavor of fragmenting parton

The polarization of the fragmenting parton is transferred from the incoming parton which can be expressed as

$$P_f = \frac{\delta f}{f} D_T^{a^\uparrow b \rightarrow c^\uparrow d}, \quad (6.6)$$

where  $P_c$  is the polarization of the fragmenting parton  $c$ ,  $\delta f$  is the transversely polarized partonic distribution function and  $f$  is the unpolarized partonic distribution function and  $D_T^{a^\uparrow b \rightarrow c^\uparrow d}$  is the partonic spin transfer for the subprocess  $a^\uparrow b \rightarrow c^\uparrow d$ . The JP trigger conditions could change the relative fractions of different subprocess and thus the relative fractions of the fragmenting partons with different flavor. The relative fractions of the subprocess are obtained from the MC sample and the example of  $p_T$  of  $3 \sim 4 \text{ GeV}/c$  is shown in Fig. 6.5. The main subprocesses are  $q_a q_b \rightarrow q_a q_b$ ,  $q_a g \rightarrow q_a g$  and  $g g \rightarrow g g$ .

The relative fractions for all  $p_T$  bins are summarized in Fig. 6.6. The relative fractions of  $q q \rightarrow q q$  and  $q g \rightarrow q g$  are increasing and the relative fraction of  $g g \rightarrow g g$  is decreasing with the trigger threshold increasing and hyperon  $p_T$  increasing.

The relative fractions of the fragmenting partons with different flavors changed with the different trigger conditions applied. The relative fractions are extracted from the MC sample. Fig. 6.7 shows the original fragmenting parton flavors for  $\Lambda$  ( $\bar{\Lambda}$ ) with  $p_T$  of  $3 \sim 4 \text{ GeV}/c$  as an example. The fraction distribution indicates that gluon is the main part in the fragmenting partons for both of  $\Lambda$  and  $\bar{\Lambda}$  and  $d$  and  $u$  quarks are following. The  $\bar{s}$  quark is obviously a main source for  $\bar{\Lambda}$  than  $\Lambda$ . This is also the reason why we expect  $\bar{\Lambda}$  is able to provide information for the polarization of strange sea quark.

The relative fractions for all  $p_T$  bins are summarized in Fig. 6.8. The relative fraction of gluon is decreasing while the relative fractions of quarks are increasing with hyperon  $p_T$  increasing. With trigger threshold increasing, the relative fraction of  $s$  ( $\bar{s}$ ) is decreasing while the relative fractions of gluon,  $d$  ( $\bar{d}$ ) and  $u$  ( $\bar{u}$ ) are increasing.

The relative fraction changes of subprocess and fragmenting parton with different flavor is combined to each other strongly. In the model calculation, the relative fraction of fragmenting parton with different flavor is used as the input to calculate the  $D_{TT}$  for each trigger. Based on the model calculation and the relative fractions of fragmenting parton with different flavor, the trigger-dependent  $D_{TT}$  was obtained. The difference of  $D_{TT}$  between before and after applying the trigger conditions is used as the systematic uncertainty to  $D_{TT}$  from the changes of subprocess and fragmenting parton flavor. The uncertainty from this part is tabulated in TABLE. 6.5.

### 6.5.3 Feed-down contributions

The possible effect from differences in the feed-down contribution on  $\Lambda$  and  $\bar{\Lambda}$  production were studied in simulation. The relative fractions of  $\Lambda$  ( $\bar{\Lambda}$ )'s mother particles can be obtained from the MC data samples.

The relative fractions for all  $p_T$  bins are summarized in Fig. 6.9. The solid circle is representative of the hyperon produced directly from the fragmenting parton and this part is decreasing with trigger threshold increasing. The relative fractions of hyperons

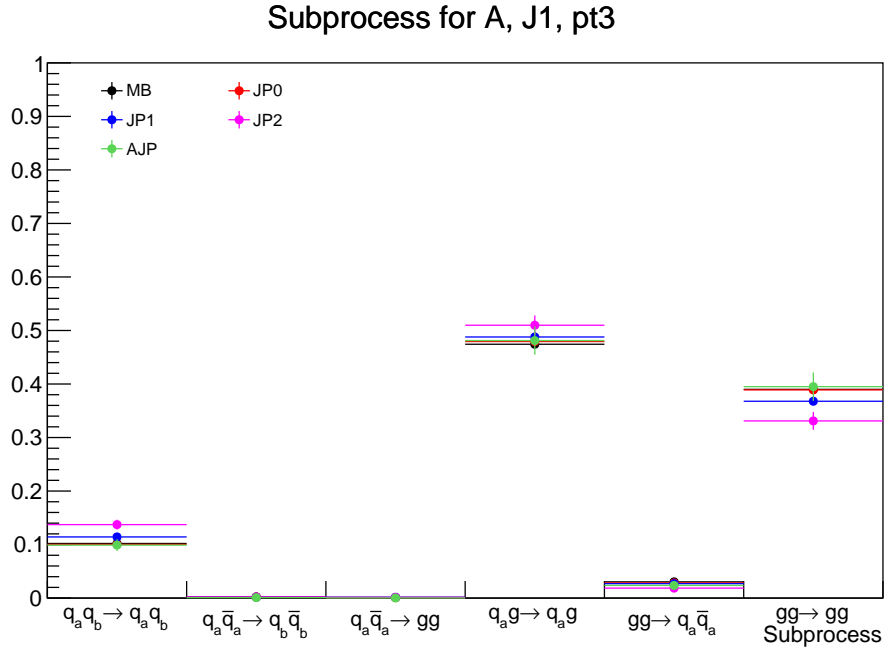
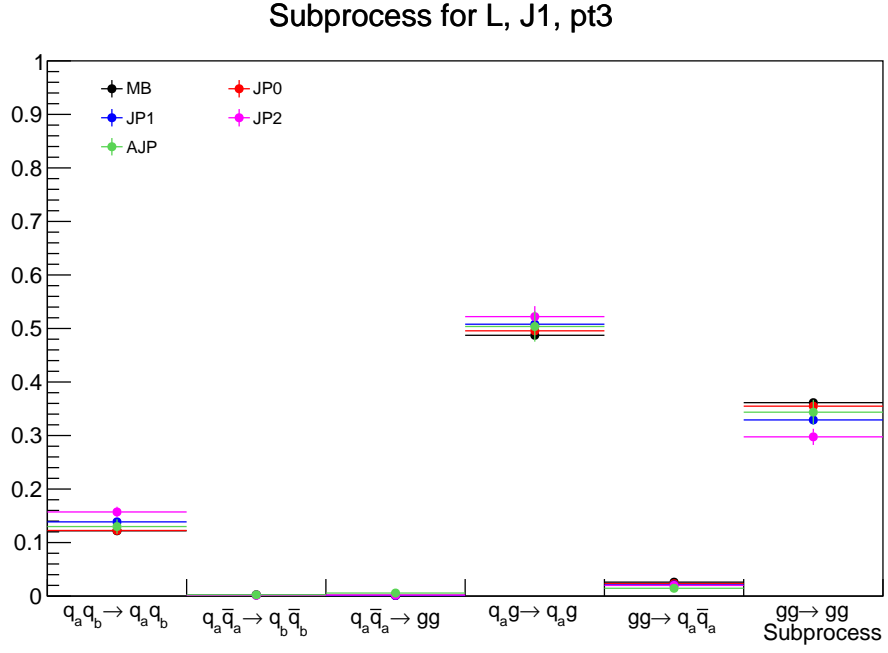


Figure 6.5: The relative fractions of subprocess for  $\Lambda$  (upper panel) and  $\bar{\Lambda}$  (lower panel) with  $p_T$  of  $3 \sim 4 \text{ GeV}/c$ .

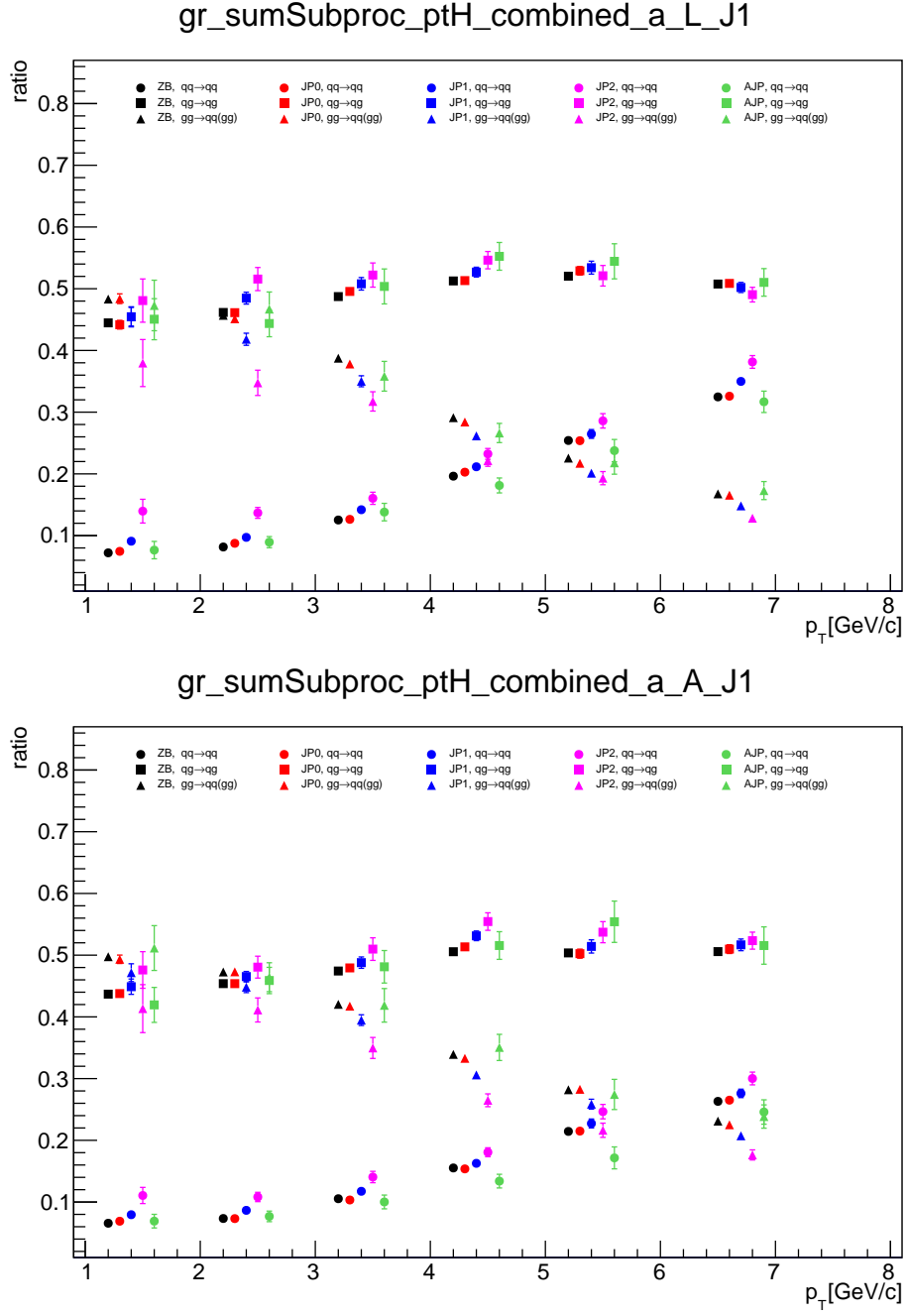


Figure 6.6: The relative fractions of subprocess for  $\Lambda$  (upper panel) and  $\bar{\Lambda}$  (lower panel) in all  $p_T$  bins.



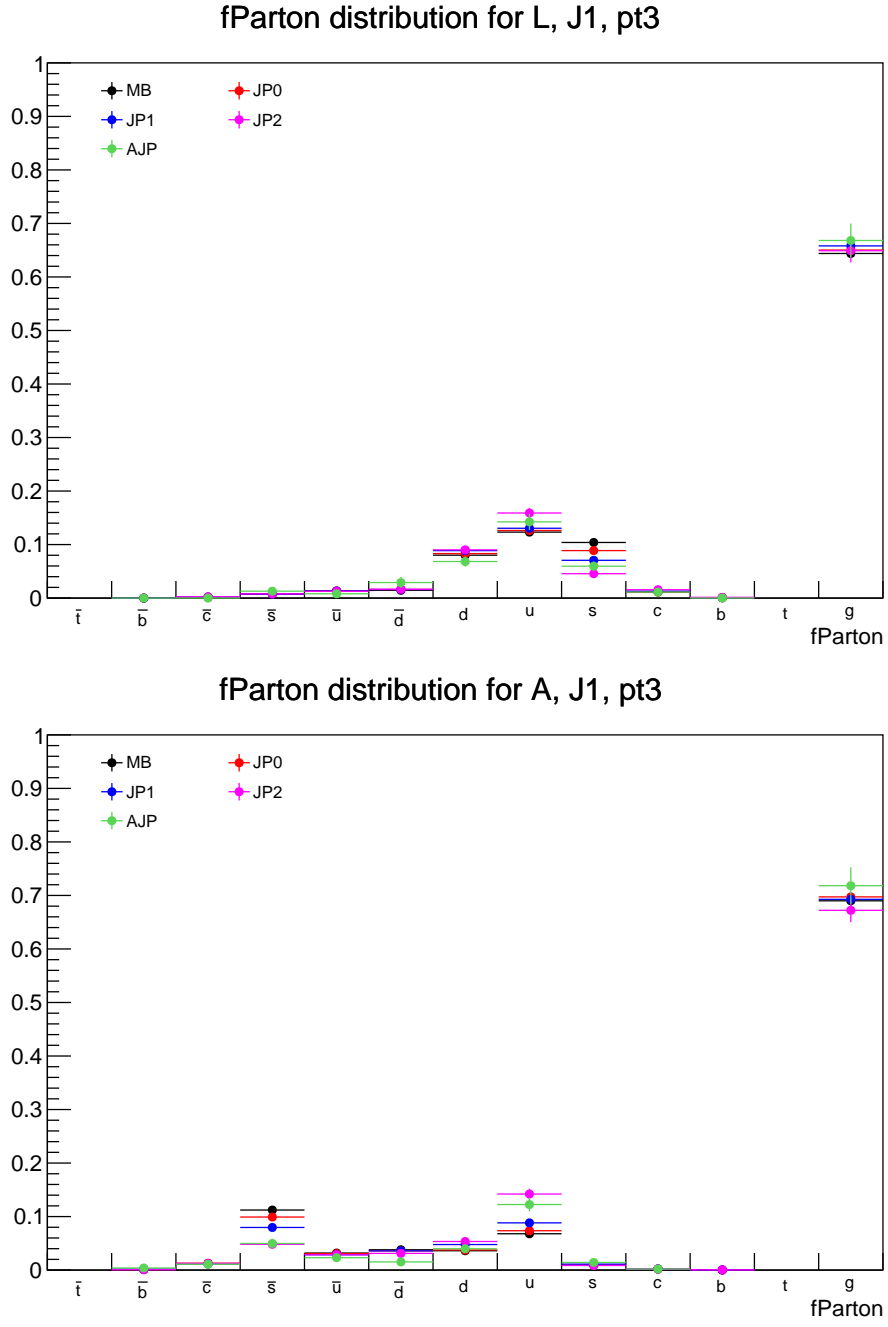


Figure 6.7: The relative fractions of fragmenting parton flavors for  $\Lambda$  (upper panel) and  $\bar{\Lambda}$  (lower panel) with  $p_T$  of 3  $\sim$  4 GeV/c.

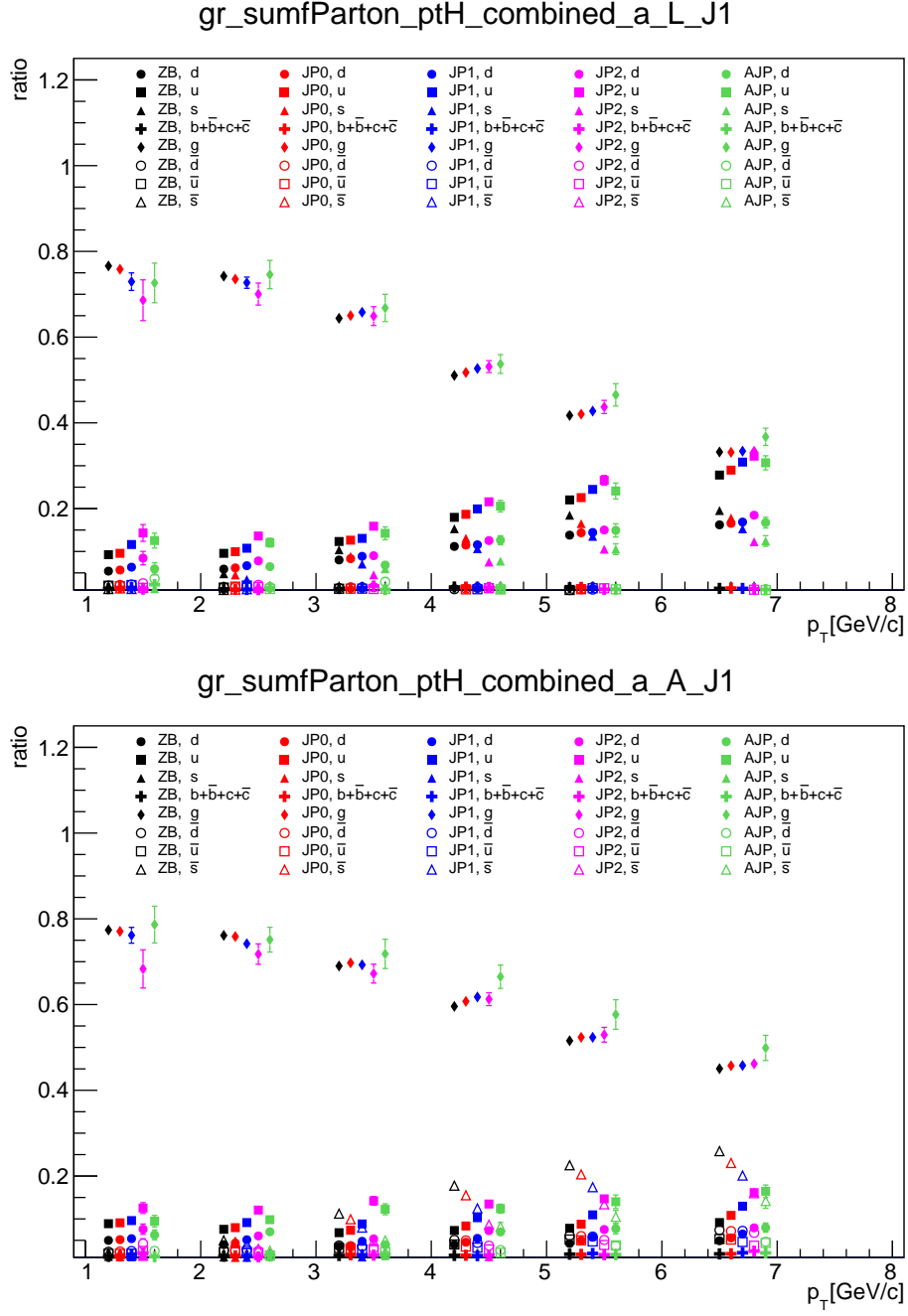


Figure 6.8: The relative fractions of fragmentin parton flavors for  $\Lambda$  (upper panel) and  $\bar{\Lambda}$  (lower panel) in all  $p_T$  bins.

Table 6.5: Uncertainty to  $D_{\text{TT}}$  from subprocess & fragmenting parton flavor for  $\Lambda$  and  $\bar{\Lambda}$

| $0 < \eta < 1.2$ |           |                 |           |                 |           |                 |           |                 |           |                 |
|------------------|-----------|-----------------|-----------|-----------------|-----------|-----------------|-----------|-----------------|-----------|-----------------|
|                  | JP0       |                 | JP1       |                 | JP2       |                 | AJP       |                 | Combined  |                 |
| $p_{\text{T}}$   | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ |
| 1 $\sim$ 2       | 0.0000    | 0.0001          | 0.0002    | 0.0001          | 0.0003    | 0.0004          | 0.0003    | 0.0004          | 0.0002    | 0.0002          |
| 2 $\sim$ 3       | 0.0001    | 0.0001          | 0.0005    | 0.0003          | 0.0011    | 0.0007          | 0.0009    | 0.0001          | 0.0007    | 0.0004          |
| 3 $\sim$ 4       | 0.0005    | 0.0002          | 0.0013    | 0.0006          | 0.0023    | 0.0017          | 0.0014    | 0.0005          | 0.0015    | 0.0009          |
| 4 $\sim$ 5       | 0.0011    | 0.0003          | 0.0024    | 0.0009          | 0.0043    | 0.0021          | 0.0041    | 0.0007          | 0.0031    | 0.0012          |
| 5 $\sim$ 6       | 0.0011    | 0.0005          | 0.0029    | 0.0013          | 0.0048    | 0.0019          | 0.0046    | 0.0023          | 0.0037    | 0.0016          |
| 6 $\sim$ 8       | 0.0011    | 0.0006          | 0.0026    | 0.0013          | 0.0048    | 0.0022          | 0.0041    | 0.0019          | 0.0036    | 0.0017          |

| $-1.2 < \eta < 0$ |           |                 |           |                 |           |                 |           |                 |           |                 |
|-------------------|-----------|-----------------|-----------|-----------------|-----------|-----------------|-----------|-----------------|-----------|-----------------|
|                   | JP0       |                 | JP1       |                 | JP2       |                 | AJP       |                 | Combined  |                 |
| $p_{\text{T}}$    | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ |
| 1 $\sim$ 2        | 0.0000    | 0.0000          | 0.0000    | 0.0000          | 0.0000    | 0.0000          | 0.0000    | 0.0000          | 0.0000    | 0.0000          |
| 2 $\sim$ 3        | 0.0000    | 0.0000          | 0.0000    | 0.0001          | 0.0000    | 0.0001          | 0.0000    | 0.0000          | 0.0000    | 0.0001          |
| 3 $\sim$ 4        | 0.0000    | 0.0000          | 0.0001    | 0.0000          | 0.0002    | 0.0001          | 0.0001    | 0.0000          | 0.0001    | 0.0000          |
| 4 $\sim$ 5        | 0.0001    | 0.0001          | 0.0003    | 0.0002          | 0.0005    | 0.0003          | 0.0005    | 0.0001          | 0.0004    | 0.0002          |
| 5 $\sim$ 6        | 0.0002    | 0.0001          | 0.0006    | 0.0003          | 0.0009    | 0.0004          | 0.0009    | 0.0005          | 0.0007    | 0.0003          |
| 6 $\sim$ 8        | 0.0003    | 0.0002          | 0.0007    | 0.0004          | 0.0012    | 0.0006          | 0.0011    | 0.0006          | 0.0009    | 0.0005          |

produced from  $\Sigma^0$ ,  $\Sigma^{*0}$  and  $\Xi^0$  decay are increasing with the trigger threshold increasing. This is because that  $\pi^0$  or  $\gamma$  is produced simultaneously in the decay, which provides more energy to make the trigger fired easier.

Based on the model calculation and the relative fractions of feed-down sources for each trigger condition, the trigger-dependent  $D_{\text{TT}}$  was obtained. The difference of  $D_{\text{TT}}$  between before and after applying the trigger conditions is used as the systematic uncertainty to  $D_{\text{TT}}$  from the changes of the feed-down sources. TABLE.6.6 shows the values of the uncertainty.

## 6.6 Total Systematic Uncertainty

The total systematic uncertainty was estimated by adding the above contributions in quadrature for each  $p_{\text{T}}$  interval in the analysis. This was done separately for the  $\Lambda$  and  $\bar{\Lambda}$  samples with positive and negative  $\eta$  ranges. The values are shown in TABLE.6.7.

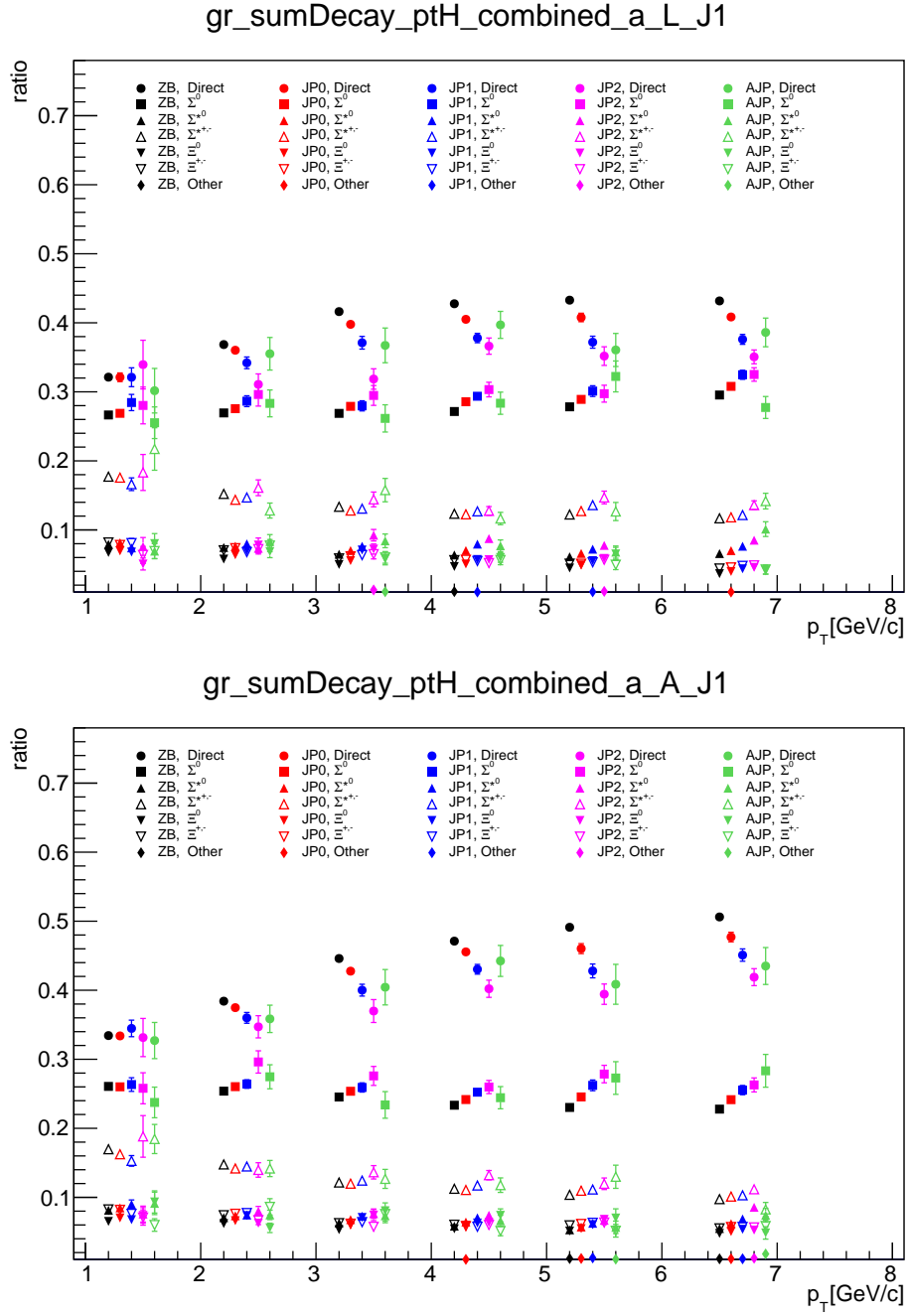


Figure 6.9: The feed-down fractions for  $\Lambda$  (upper panel) and  $\bar{\Lambda}$  (lower panel) in all  $p_T$  bins.

Table 6.6: Uncertainty to  $D_{\text{TT}}$  from feed-down for  $\Lambda$  and  $\bar{\Lambda}$ 

| $0 < \eta < 1.2$ |           |                 |           |                 |           |                 |           |                 |           |                 |
|------------------|-----------|-----------------|-----------|-----------------|-----------|-----------------|-----------|-----------------|-----------|-----------------|
|                  | JP0       |                 | JP1       |                 | JP2       |                 | AJP       |                 | Combined  |                 |
| $p_{\text{T}}$   | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ |
| 1 $\sim$ 2       | 0.0000    | 0.0001          | 0.0001    | 0.0001          | 0.0000    | 0.0001          | 0.0003    | 0.0001          | 0.0001    | 0.0001          |
| 2 $\sim$ 3       | 0.0002    | 0.0000          | 0.0004    | 0.0001          | 0.0004    | 0.0003          | 0.0001    | 0.0000          | 0.0004    | 0.0001          |
| 3 $\sim$ 4       | 0.0004    | 0.0002          | 0.0003    | 0.0003          | 0.0014    | 0.0008          | 0.0002    | 0.0004          | 0.0007    | 0.0004          |
| 4 $\sim$ 5       | 0.0007    | 0.0003          | 0.0013    | 0.0007          | 0.0020    | 0.0013          | 0.0016    | 0.0005          | 0.0015    | 0.0008          |
| 5 $\sim$ 6       | 0.0007    | 0.0008          | 0.0013    | 0.0014          | 0.0009    | 0.0024          | 0.0013    | 0.0030          | 0.0012    | 0.0018          |
| 6 $\sim$ 8       | 0.0006    | 0.0010          | 0.0019    | 0.0019          | 0.0024    | 0.0028          | 0.0008    | 0.0020          | 0.0020    | 0.0022          |

| $-1.2 < \eta < 0$ |           |                 |           |                 |           |                 |           |                 |           |                 |
|-------------------|-----------|-----------------|-----------|-----------------|-----------|-----------------|-----------|-----------------|-----------|-----------------|
|                   | JP0       |                 | JP1       |                 | JP2       |                 | AJP       |                 | Combined  |                 |
| $p_{\text{T}}$    | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ | $\Lambda$ | $\bar{\Lambda}$ |
| 1 $\sim$ 2        | 0.0000    | 0.0000          | 0.0000    | 0.0000          | 0.0000    | 0.0000          | 0.0001    | 0.0000          | 0.0000    | 0.0000          |
| 2 $\sim$ 3        | 0.0000    | 0.0000          | 0.0000    | 0.0001          | 0.0001    | 0.0001          | 0.0001    | 0.0001          | 0.0001    | 0.0001          |
| 3 $\sim$ 4        | 0.0001    | 0.0000          | 0.0001    | 0.0000          | 0.0001    | 0.0000          | 0.0002    | 0.0000          | 0.0001    | 0.0000          |
| 4 $\sim$ 5        | 0.0001    | 0.0001          | 0.0001    | 0.0001          | 0.0001    | 0.0001          | 0.0000    | 0.0001          | 0.0001    | 0.0001          |
| 5 $\sim$ 6        | 0.0001    | 0.0001          | 0.0003    | 0.0003          | 0.0004    | 0.0004          | 0.0006    | 0.0002          | 0.0004    | 0.0003          |
| 6 $\sim$ 8        | 0.0003    | 0.0002          | 0.0006    | 0.0003          | 0.0006    | 0.0005          | 0.0002    | 0.0006          | 0.0006    | 0.0004          |

Table 6.7: Total Systematic Uncertainty

| $p_{\text{T}} [\text{GeV}/c]$ | $0 < \eta < 1.2$ |                 | $-1.2 < \eta < 0$ |                 |
|-------------------------------|------------------|-----------------|-------------------|-----------------|
|                               | $\Lambda$        | $\bar{\Lambda}$ | $\Lambda$         | $\bar{\Lambda}$ |
| 1 $\sim$ 2                    | 0.0008           | 0.0006          | 0.0000            | 0.0003          |
| 2 $\sim$ 3                    | 0.0012           | 0.0008          | 0.0001            | 0.0003          |
| 3 $\sim$ 4                    | 0.0029           | 0.0021          | 0.0003            | 0.0011          |
| 4 $\sim$ 5                    | 0.0059           | 0.0049          | 0.0004            | 0.0009          |
| 5 $\sim$ 6                    | 0.0071           | 0.0073          | 0.0010            | 0.0017          |
| 6 $\sim$ 8                    | 0.0080           | 0.0086          | 0.0013            | 0.0041          |

## 7 Final Results

Events that satisfy the JP trigger conditions were analyzed as separate samples. Events that satisfy two or more conditions were analyzed only as part of one of the JP samples to avoid double-counting (or correlation). The  $D_{\text{TT}}$  results are consistent with each other within uncertainty. The  $D_{\text{TT}}$  results using the combined sample were also extracted.

The final results are shown in Fig. 7.1 including statistical uncertainty (black lines) and the systematic uncertainty (grey bands). The values are listed in TABLE. 7.1.

Table 7.1: Values of  $D_{\text{TT}}$  extracted from trigger combined sample

| $0 < \eta < 1.2$              |                 |       |       |                 |       |       |
|-------------------------------|-----------------|-------|-------|-----------------|-------|-------|
| $p_{\text{T}} [\text{GeV}/c]$ | $\Lambda$       |       |       | $\bar{\Lambda}$ |       |       |
|                               | $D_{\text{TT}}$ | stat. | sys.  | $D_{\text{TT}}$ | stat. | sys.  |
| 1 $\sim$ 2                    | 0.000           | 0.007 | 0.001 | 0.011           | 0.006 | 0.001 |
| 2 $\sim$ 3                    | 0.013           | 0.008 | 0.001 | -0.002          | 0.008 | 0.001 |
| 3 $\sim$ 4                    | 0.026           | 0.011 | 0.003 | -0.002          | 0.011 | 0.002 |
| 4 $\sim$ 5                    | -0.008          | 0.017 | 0.006 | 0.024           | 0.017 | 0.005 |
| 5 $\sim$ 6                    | 0.007           | 0.026 | 0.007 | 0.009           | 0.028 | 0.007 |
| 6 $\sim$ 8                    | 0.031           | 0.033 | 0.008 | -0.034          | 0.040 | 0.009 |
| $-1.2 < \eta < 0$             |                 |       |       |                 |       |       |
| $p_{\text{T}} [\text{GeV}/c]$ | $\Lambda$       |       |       | $\bar{\Lambda}$ |       |       |
|                               | $D_{\text{TT}}$ | stat. | sys.  | $D_{\text{TT}}$ | stat. | sys.  |
| 1 $\sim$ 2                    | -0.005          | 0.007 | 0.001 | -0.001          | 0.006 | 0.000 |
| 2 $\sim$ 3                    | -0.006          | 0.008 | 0.001 | 0.001           | 0.008 | 0.000 |
| 3 $\sim$ 4                    | -0.017          | 0.011 | 0.001 | -0.004          | 0.011 | 0.001 |
| 4 $\sim$ 5                    | -0.023          | 0.017 | 0.002 | 0.002           | 0.017 | 0.001 |
| 5 $\sim$ 6                    | 0.023           | 0.026 | 0.002 | 0.017           | 0.028 | 0.002 |
| 6 $\sim$ 8                    | 0.021           | 0.033 | 0.002 | -0.056          | 0.040 | 0.004 |

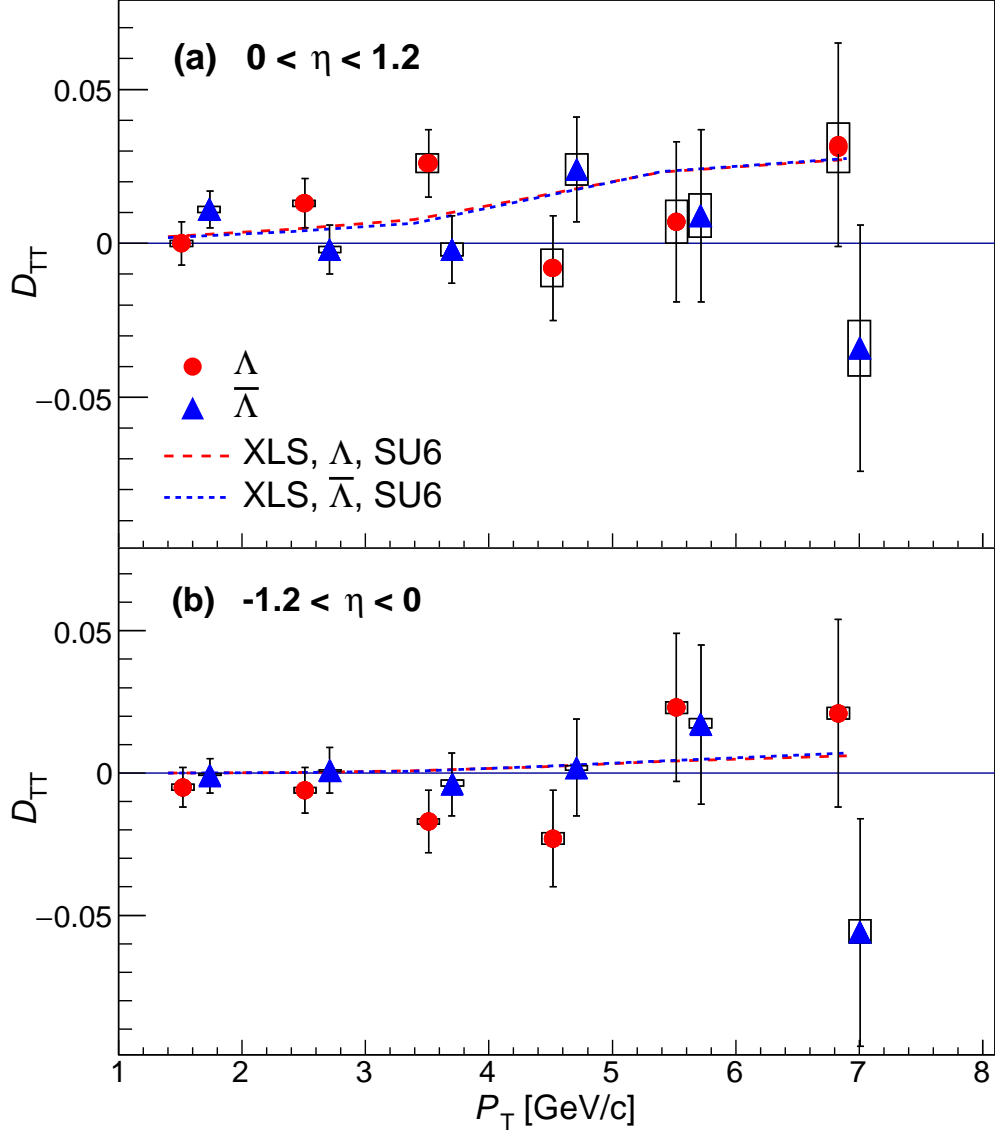


Figure 7.1:  $D_{TT}$  extracted from the trigger combined sample for  $\Lambda$  and  $\bar{\Lambda}$ . The left graph is with positive  $\eta$  with respect to the polarized beam and the right one is with negative  $\eta$  with respect to the polarized beam.

## 8 Main Code

The top directory for the code is

pp200trans\_2012

and the more details and updated introduction of the analysis code can be found in CVS directories.

### 8.1 Data Analysis: from MuDsts to $D_{TT}$

Currently, the muDst files for run12\_200GeV are not available on RCF disk any longer. For test, one can always download a small number of muDst files from HPSS. The full file list can be accessed via catalog:

```
get_file_list.pl -keys path,filename \\
-cond production=P12id,trgsetupname~pp200_production_2012, \\
filetype=daq_reco_MuDst,filename~st_physics,\\
tpx=1,emc=1,eemc=1,sanity=1,storage=hpss -limit 0
```

For reading the MuDst files (when the data is on the disk), you can just go inside directory LamRec, compile, and run the executable file Run job.csh, after which the analysis jobs will be submitted. The output files – the Lambda trees can be found in the scratch directory.

More detail steps are shown following:

In LamRec:

Lambda reconstruction from MuDst root files.

1. The code compiled with SL16b Library initially but the Library seems to be removed. starpro should be OK.
2. Execute the following commands:  
starpro  
cons  
Run\_jobs.csh start\_runIndex end\_runIndex
3. The output files will be stored in the Tree directory.

In JetRec:

Jet Tree are simplified here for Lambda and jet correlation.

1. Retrieve origin jet tree from HPSS to JetTree directory.  
The jet tree files are located in:  
/home/jcmei/JetTree\_run12/JetRec\_Kevin/
2. Make file lists in each one of the runs with the whole path.  
MakeList.csh



3. Submit jobs to simplify jet trees:  
Run\_simpleJet\_jobs.csh start\_runIndex end\_runIndex
4. The output files will be stored in the simpleJetTree directory.

In JetMatch:

Make the correlation between Lambda and jets.

1. Make file list.  
makeList.csh
2. Submit jobs to make the correlation.  
Run\_job.csh start\_runIndex end\_runIndex
3. Obtain root files by run.  
mergeBYrun.csh
4. cd dataBYrun  
lss | grep root > file.lis

In Ana directory:

The data is further selected and dealt with to obtain the final results.

1. Go to Select
2. Run\_jobs.csh
3. cd data  
lss | grep root > file.lis
4. Go to fillHist
5. Run\_job.csh
6. Go to imFit/code/
7. invariant mass fit and background estimation  
excute\_imFit.C
8. To Ana/fiilHist  
Run\_job\_2cos.csh
9. cd data/cos  
cd sig  
hadd merged\_ALL.cos.root ALL/\*\_ALL.cos.root  
cd ../bkg  
hadd merged\_ALL.cos.root ALL/\*\_ALL.cos.root
10. Extract D\_TT  
To Ana/result

```
cos2dtt_crossRatio.csh
textDtt.csh
```

11. Make Money plots  
To Ana/imFit/code

```
python paperPlot_im.py
python paperPlot_imcos.py
python paperPlot_dttcos.py
python paperPlot_result.py
```

The plots will be in the output directory.

## 8.2 MC production

Generation MC data sample:

```
cd mcProduction/Gen/
Run_gen.csh par1 par2 par3
```

Here par1, par2 and par3 are the low and high edges of the hard pT and the circle number of the generation.

Jets and Hyperons reconstruction of MC data sample:

```
cd pp200trans_2012/mcProduction/Rec/
Run_job.csh
```

PTV(hyperon pT) and PTH(hard pT) are needed to specify in the macro.  
Make histograms of MC data sample:

```
cd pp200trans_2012/mcProduction/Ana/
cd merge
Run_job.csh
```

```
cd ../toHist
Run_job.csh
```

PTV(hyperon pT) and PTH(hard pT) are also needed to specify in the macro.

## 8.3 Notes

As usual, the .csh and .xml scripts should be appropriately modified as needed (path and directory) and corresponding file lists are needed in some steps. In the code collection directory, the README file should be more updated. Now, all the needed histograms are produced. The trigger bias can be extracted by using a few short macros. In

```
pp200trans_2012/mcProduction/tBias
```

directory, the macros used in this analysis can be taken as reference. Overall, this codes mentioned in this section are not professional enough. If any confusion are met, please feel free to contact Jincheng Mei (jcmei@rcf.rhic.bnl.gov).

## A Run List

Here is the run list we used in the final results:

|          |          |          |          |          |          |          |          |
|----------|----------|----------|----------|----------|----------|----------|----------|
| 13044126 | 13045001 | 13045005 | 13045006 | 13045007 | 13045012 | 13045029 | 13045056 |
| 13045133 | 13045134 | 13045135 | 13045138 | 13045145 | 13045146 | 13045164 | 13046001 |
| 13046003 | 13046004 | 13046121 | 13047003 | 13047023 | 13047024 | 13047026 | 13047027 |
| 13047028 | 13047029 | 13047030 | 13047031 | 13047032 | 13047034 | 13047035 | 13047122 |
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