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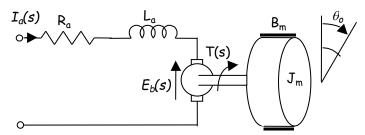
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Introduction

DC Motor

In our class, we studied a permanent magnet DC Motor.



Neglect the armature inductance for the present.

Figure 1: A permanent magnet d.c. motor

According to our class, we know The torque applied to a load and the moment of inertia of the load determine the load acceleration. The load speed is equivalent to the time integral of its

acceleration.

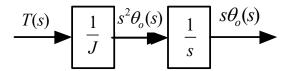


Figure 2: Calculation

As the load speeds up a viscous friction torque that opposes motion builds up and reduces the amount of torque available to accelerate the load.

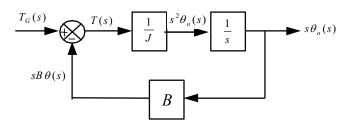


Figure3: Calculation

The current flowing in the armature circuit determines the amount of torque generated in the motor.

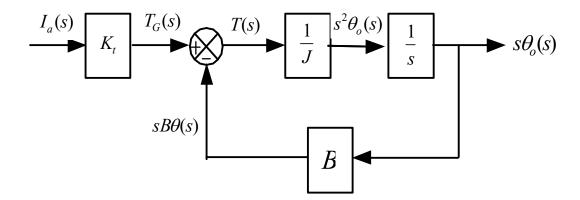


Figure 4: Calculation

The armature current in turn is determined by the difference between the applied input voltage and the back emf generated in the armature windings as they move in the magnetic field set up by the motor permanent magnet. The magnitude of the back emf is proportional to the speed of rotation of the armature and provides a feedback that limits the speed of the motor for any given input voltage.

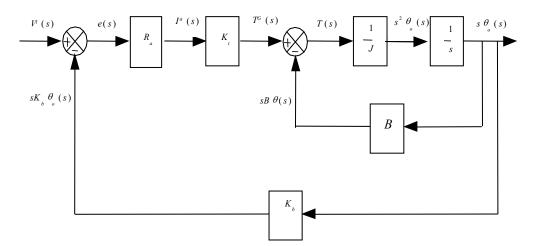


Figure 5: Calculation

Today, through study the permanent dc motor, we will design a 12V DC Motor include the effect of armature inductance La. We are investigating the effective usage of a PID controller, when used to control the speed of a DC 12 V motor.

PID Controller

A PID controller is an instrument used in industrial control applications to regulate temperature, flow, pressure, speed and other process variables. PID (proportional integral derivative) controllers use a control loop feedback mechanism to control process variables and are the most accurate and stable controller.

Mathematical form

The overall control function:

$$u(t) = K_p * e(t) + K_i * \int_0^t e(t) + K_d * \frac{de(t)}{dt}$$

Where $K_{p_i}K_i$ and K_d all non-negative, denote the coefficients for the proportional, integral, and derivative terms respectively (sometimes denoted P, I, and D).

Design 12V DC Motor

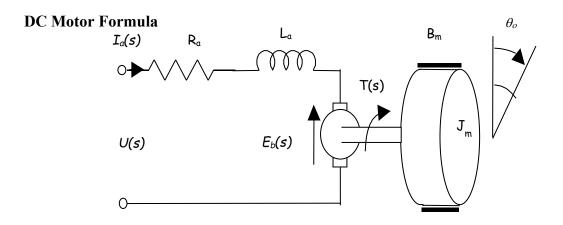


Figure 6: DC Motor Parameter

 T_e : Electromagnetic Torque

*T*_l: Load Torque

w: Angular Speed

K_t: Torque Constant

 J_m : Moment of Inertia

*K*_b: Back EMF constant

 B_m : Friction coefficient

 R_a : Electrical Resistance

 L_a : Electrical Inductance

$$U=E_b + I_{a^*}R_a + L_{a^*}\frac{di}{dt}$$

$$E_b=K_b^*w$$

$$T_e - T_l = J*\frac{dw}{dt}$$

$$T_l=B_m^*w$$

Formula Manipulation

$$U(s)=E_h(s) + I_a(s) * (R_a(s)+S*L_a(s))$$

$$E_b(\mathbf{s}) = K_b *_{\mathbf{w}}(\mathbf{s})$$

$$T_e(\mathbf{s}) - T_l(\mathbf{s}) = \mathbf{S} *_{J_m} *_{\mathbf{w}}(\mathbf{s})$$

$$T_e(\mathbf{s}) = K_t *_{I_a}(\mathbf{s})$$

$$T_l = B_m *_{\mathbf{w}}(\mathbf{s})$$

DC Motor Math Function Model

Parameter	Value
Moment of inertia	$J_m = 0.000052 Kg.$
Friction coefficient	$B_m = 0.01 \ N.ms$
Back EMF constant	$K_b = 0.235 \frac{V}{ms}$
Torque constant	$K_t = 0.235 \frac{Nm}{A}$
Electric resistance	$R_a = 2 \text{ ohm}$
Electric inductance	$L_a = 0.23 H$
Gear ratio	gr
Load torque	$ au_L(t)$
Angular speed	$\omega_m \frac{rad}{}$
DC motor parameter and values	

According to the formula and parameter, we can get the model as follows:

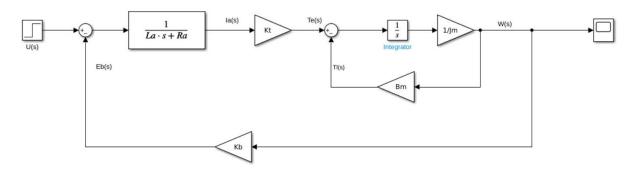


Figure6: DC Motor Model

Set Point	Setting Time	2	
Value	Termination Value	5	
	Stop Value	10	

Chart1: DC Motor Model Set Point Value

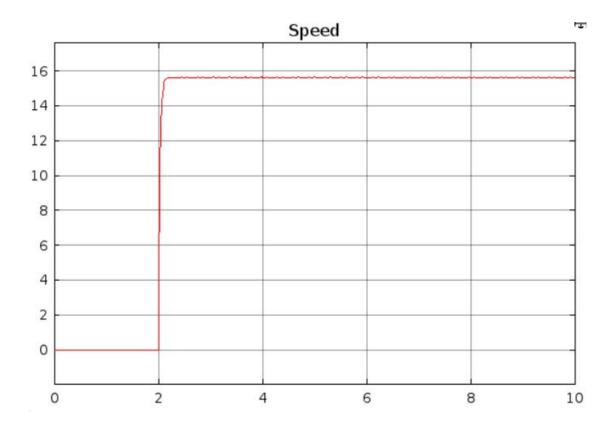


Figure 7: DC Motor Model Speed Display

From this picture, we can see the rise-time equal to our setting time, when time =2.3s, the speed arrive at termination, over set point. 15.6-5=10.6, it has large Steady State Error.

$$U(s) = E_b(s) + I_a(s) * (R_a(s) + S*L_a(s))$$

$$U(s) = K_b*w(s) + \frac{T_e(s)}{K_t} * (R_a(s) + S*L_a(s))$$

$$U(s) = K_b*w(s) + \frac{B_m*w(s) + S*J_m*w(s)}{K_t} * (R_a(s) + S*L_a(s))$$

$$U(s) = K_b*w(s) + \frac{(B_m + S*J_m)*w(s)}{K_t} * (R_a(s) + S*L_a(s))$$

$$U(s) = \frac{K_b*w(s)*K_t}{K_t} + \frac{(B_m + S*J_m)*w(s)}{K_t} * (R_a(s) + S*L_a(s))$$

$$\frac{w}{U(s)} = \frac{1}{K_b} + \frac{K_t}{(B_m + S*J_m)* (Ra(s) + S*La(s))}$$

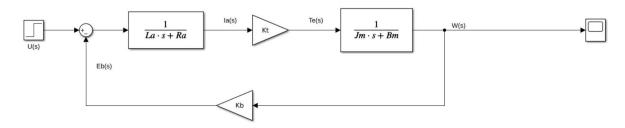


Figure8: DC Motor Transfer Function Model

Set Point	Setting Time	2
Value	Termination Value	10
	Stop Value	20

Chart2: DC Motor Transfer Function Model Set Point Value

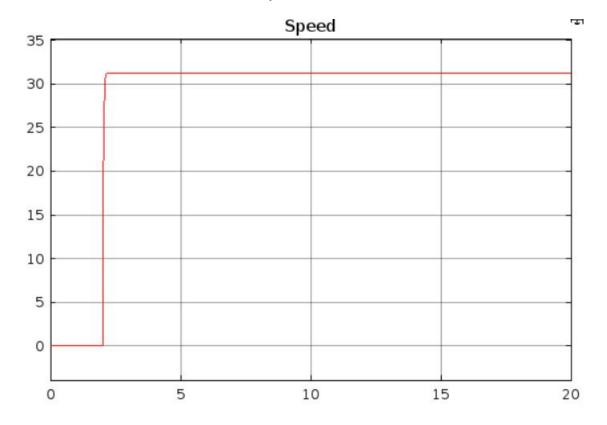


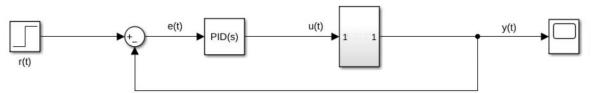
Figure 9: DC Motor Transfer Function Model Speed Display

From this picture, we can see the rise-time equal to our setting time, when time =2.3s, the speed arrive at termination, over set point. 32-10=22, it has large Steady State Error.

Connect PID Controller

$$e(t)=|y(t)-r(t)|$$
Overshoot =
$$\frac{\textit{Max value} - \textit{Settling value}}{\textit{Settling value}} *100\%$$

$$u(t) = K_p * e(t) + K_i * \int_0^t e(t) + K_d * \frac{de(t)}{dt}$$



e(t): stable state error

y(t): actual output value

r(t): setpoint value

u(t): PID controller output

Figure 10: PID Controller control DC Motor Speed

The Effective of K_p Speed =5, K_p =1, K_i =0

1	Setting Time	2	Overshoot	7.89%
Actual	Termination Value	5	Rise-time	3.8
Value	Stop Value	20	Settling Time	2
VS Setting	K_p	1	-	
Value	K_i	0	Steady State Error	1.1
Value	K_d	0		

Chart3: PID Controller control DC Motor Speed Actual Value

$$e(t) = |y(t) - r(t)| = |3.9-5| = 1.1$$
Overshoot = $\frac{Max \ value - Settling \ value}{Settling \ value} * 100\%$
Overshoot = $\frac{4.1 - 3.8}{3.8} * 100\% = 7.89\%$

$$u(t) = K_p * e(t) + K_i * \int_0^t e(t) + K_d * \frac{de(t)}{dt}$$

 $u(t) = K_p * e(t) = 1.1$ (System intervention on speed)



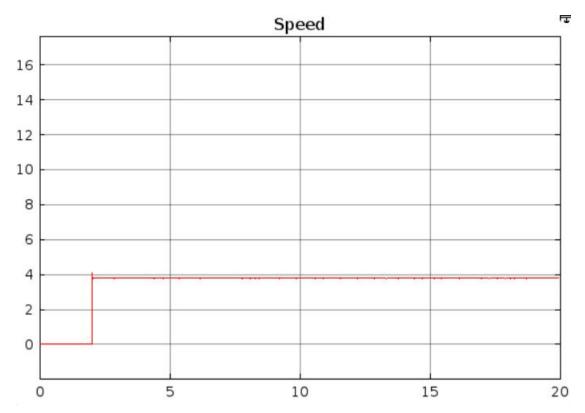


Figure 11: PID Controller control DC Motor Speed = 5 Display

Speed =5, $K_p = 2$, $K_i = 0$

1	Setting Time	2	Overshoot	18.6%
Actual	Termination Value	5	Rise-time	4.3
Value	Stop Value	20	Settling Time	2
VS Setting	K_p	2		
Value	K_i	0	Steady State Error	0.7
value	K_d	0		

Chart4: PID Controller control DC Motor Speed Actual Value

$$e(t) = |y(t) - r(t)| = |4.3-5| = 0.7$$

$$Overshoot = \frac{Max \ value - Settling \ value}{Settling \ value} * 100\%$$

$$Overshoot = \frac{5.1 - 4.3}{4.3} * 100\% = 18.6\%$$

$$u(t) = K_p * e(t) + K_i * \int_0^t e(t) + K_d * \frac{de(t)}{dt}$$

$$u(t) = K_p * e(t) = 1.4 \text{(System intervention on speed)}$$

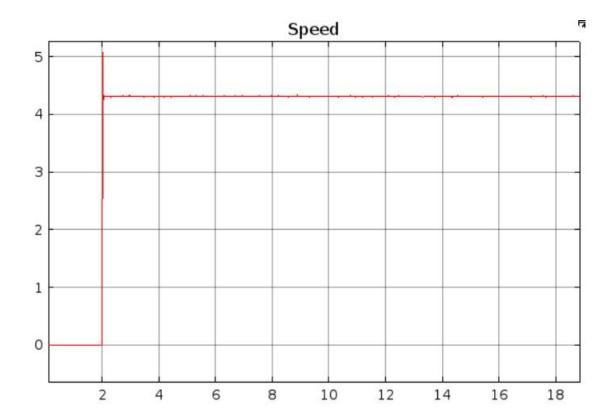


Figure 12: PID Controller control DC Motor Speed = 5 Display

Analysis Figure 11 and Figure 12, The proportional part speeds up the response speed of the system and reduces the steady state error of the system. The rise-time is increased. However, if the proportional coefficient is too large, the overshoot will increase, the number of oscillations will increase, the adjustment time will lengthen, and the dynamic performance will deteriorate. If the proportional coefficient is too large, the closed-loop system will become unstable.

Speed =5, $K_p = 1$, $K_i = 1$

1	Setting Time	2	Overshoot	0%
Actual	Termination Value	5	Rise-time	3.8
Value	Stop Value	20	Settling Time	12.5
VS Setting	K_p	1		
Value	K_i	1	Steady State Error	0
value	K_d	0		

Chart5: PID Controller control DC Motor Speed Actual Value

Speed = 5, $K_p = 1$, $K_i = 4$

1	Setting Time	2	Overshoot	0%
Actual	Termination Value	5	Rise-time	3.8
Value	Stop Value	20	Settling Time	4
VS Setting	K_p	1		
Value	K_i	4	Steady State Error	0
varue	K_d	0		

Chart6: PID Controller control DC Motor Speed Actual Value

$$e(t) = |y(t) - r(t)| = |5-5| = 0$$

$$Overshoot = \frac{Max \ value - Settling \ value}{Settling \ value} *100\%$$

$$Overshoot = \frac{5-5}{5} *100\% = 0\%$$

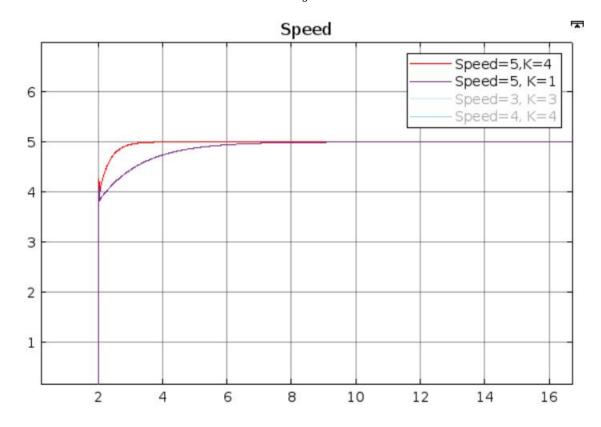


Figure 13: PID Controller control DC Motor Speed = 5 Display

Analysis Figure 13 and Figure 11. When adding K_i , the steady state error is reduced and the system is close the setpoint value. If K_i is too large, it maybe reduce the system stability. At the same time, the overshoot is reduced, but the settling time is increased. The rise-time is same. If K_i is increased, K_p is constant, the settling time is reduced.

Speed = 5, $K_p = 0$, $K_i = 1$

1	Setting Time	2	Overshoot	0%
Actual	Termination Value	5	Rise-time	2
Value	Stop Value	20	Settling Time	3.8
VS Setting	K_p	0		
Value	K_i	1	Steady State Error	0
value	K_d	0		

Chart7: PID Controller control DC Motor Speed Actual Value

	Setting Time	2	Overshoot	0%
Actual	Termination Value	5	Rise-time	2
Value	Stop Value	20	Settling Time	2.1
VS Setting	K_p	0		
Value	K_i	4	Steady State Error	0
v aruc	K_d	0		

Specu 3, Np 0, N₁ 4

Chart8: PID Controller control DC Motor Speed Actual Value

$$e(t) = |y(t) - r(t)| = |5-5| = 0$$

$$Overshoot = \frac{Max \ value - Settling \ value}{Settling \ value} *100\%$$

$$Overshoot = \frac{5-5}{5} *100\% = 0\%$$

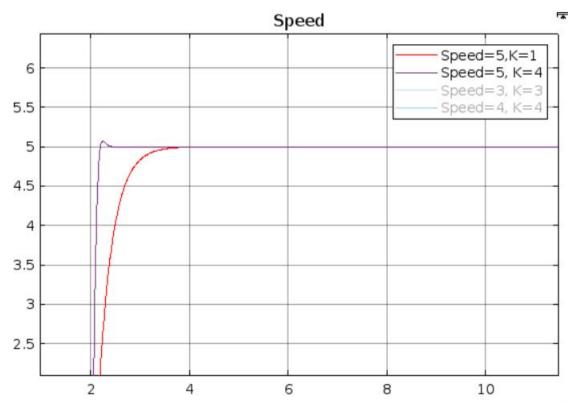


Figure 14: PID Controller control DC Motor Speed = 5 Display

Analysis Figure 14. When adding K_i , the steady state error is reduced and the system is close the setpoint value. If K_i is too large, it maybe reduce the system stability. At the same time, the overshoot is reduced, If K_i is increased, K_p is constant, the settling time is reduced.

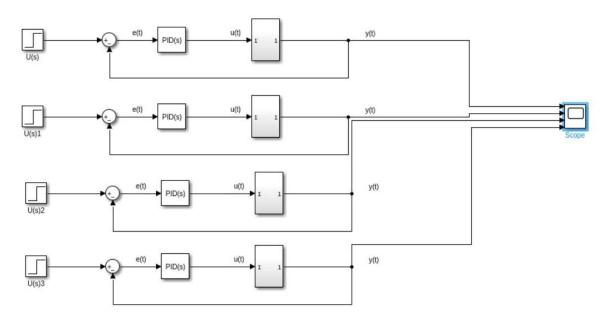


Figure 15: PID Controller control DC Motor Speed=5

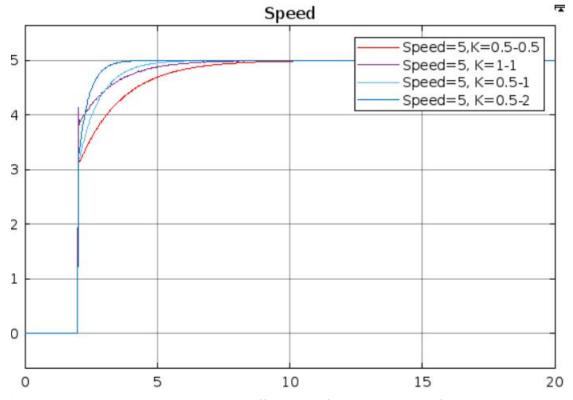


Figure 16: PID Controller control DC Motor Speed = 5

Analysis Figure 11-16, we investigate different K_i and K_p , then we contrast the overshoot, rise-time, steady state error and settling time, we observe when $K_i = 0.5$ and $K_p = 2$, the speed is close to the setpoint desired value. This is because the response speed is fastest, the overshoot is minimum, the steady stable error is minimum.

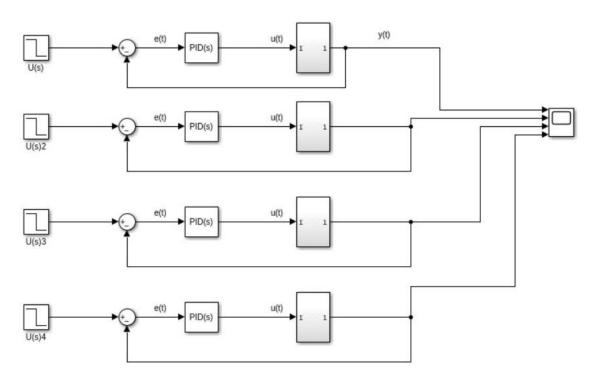


Figure 17: PID Controller control DC Motor Speed=-3

Speed = -3, $K_p = 2$, $K_i = 0$

1	Setting Time	2	Overshoot	18.2%
Actual	Termination Value	-3	Rise-time	2.58
Value	Stop Value	20	Settling Time	2
VS Setting	K_p	2		
Value	K_i	0	Steady State Error	0.42
varue	K_d	0		

Chart9: PID Controller control DC Motor Speed Actual Value

$$e(t) = |y(t) - r(t)| = |2.58-3| = 0.42$$

$$Overshoot = \frac{Max \ value - Settling \ value}{Settling \ value} *100\%$$

$$Overshoot = \frac{-3.05 - (-2.58)}{-2.58} *100\% = 18.2\%$$

Speed = -3, $K_p = 3$, $K_i = 0$

	Setting Time	2	Overshoot	25.5%
Actual	Termination Value	-3	Rise-time	2.71
Value	Stop Value	20	Settling Time	2
VS Setting	K_p	3		
Value	K_i	0	Steady State Error	0
value	K_d	0		

Chart 10: PID Controller control DC Motor Speed Actual Value

$$e(t)=|y(t)-r(t)|=|2.58-3|=0.42$$

$$Overshoot = \frac{\textit{Max value} - \textit{Settling value}}{\textit{Settling value}} *100\%$$

Overshoot =
$$\frac{-3.4 - (-2.71)}{-2.71} *100\% = 25.5\%$$

Speed = -3, $K_p = 0.5$, $K_i = 1$

	Setting Time	2	Overshoot	0%
Actual	Termination Value	-3	Rise-time	1.8
Value	Stop Value	20	Settling Time	6.3
VS Setting	K_p	0.5		
Value	K_i	1	Steady State Error	0
Value	K_d	0		

Chart11: PID Controller control DC Motor Speed Actual Value

$$e(t) = |y(t) - r(t)| = |3-3| = 0$$

$$Overshoot = \frac{Max \ value - Settling \ value}{Settling \ value} * 100\%$$

$$Overshoot = \frac{-3 - (-3)}{-3} * 100\% = 0\%$$

Speed = -3, $K_p = 0.5$, $K_i = 2$

	Setting Time	2	Overshoot	0%
Actual	Termination Value	-3	Rise-time	1.9
Value	Stop Value	20	Settling Time	4
VS Setting	K_p	0.5		
Value	K_i	2	Steady State Error	0
varue	K_d	0		

Chart12: PID Controller control DC Motor Speed Actual Value

$$e(t) = |y(t) - r(t)| = |3-3| = 0$$
Overshoot =
$$\frac{Max \ value - Settling \ value}{Settling \ value} *100\%$$
Overshoot =
$$\frac{3-3}{3} *100\% = 0\%$$

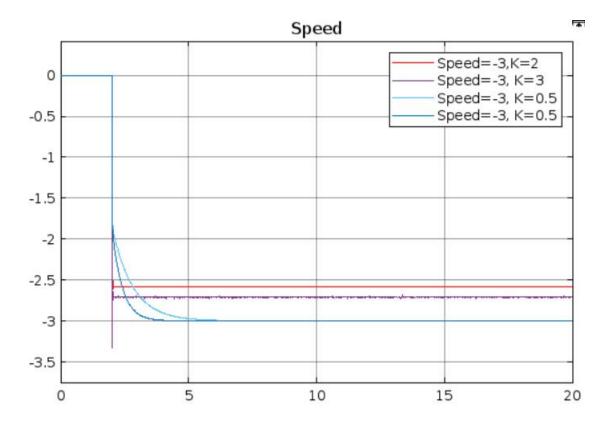


Figure 18: PID Controller control DC Motor Speed =-3 Display

Analysis Figure 18, we investigate negative speed, we have 4 table to explain these situation. When speed is constant, we change K_p, when K_p is increased, it increased the response of system and close to setpoint value, the overshoot is increased, it maybe cause system instability, the steady stable error is reduced. From this picture, when K_p is increased, K_p=3 it caused oscillate.

When speed and K_p are constant, we change K_t, when K_t is increased, the overshoot is reduced, the steady stable error is reduced. From this picture, when K_t is increased, the settling time is reduced and we can see that when $K_t = 2$, $K_p = 0.5$, the speed is close to setpoint desired value.

Speed	l =0,	$K_p = 1$	1, K _i	_! =1
-------	-------	-----------	-------------------	-----------------

1	Setting Time	2	Overshoot	0
Actual	Termination Value	0	Rise-time	0
Value	Stop Value	20	Settling Time	0
VS Setting	K_p	1		
Value	K_i	1	Steady State Error	0
Value	K_d	0		

Chart 13: PID Controller control DC Motor Speed Actual Value

$$e(t)=|y(t)-r(t)|=|0-0|=0$$

$$Overshoot = \frac{\textit{Max value} - \textit{Settling value}}{\textit{Settling value}} *100\%$$

$$Overshoot = 0$$

$$u(t) = K_p * e(t) + K_i * \int_0^t e(t) + K_d * \frac{de(t)}{dt}$$
$$u(t) = K_p * e(t) = 0$$

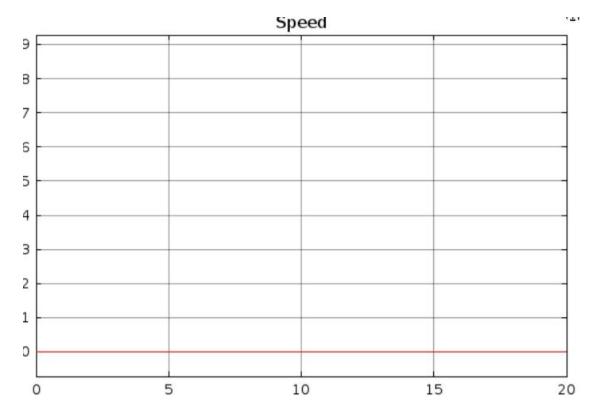


Figure 19: PID Controller control DC Motor Speed=0 Display

When speed setpoint current equal 0, all value change 0.

Speed =1, $K_p = 1$, $K_i = 1$

1	Setting Time	2	Overshoot	0%
Actual	Termination Value	1	Rise-time	0.75
Value	Stop Value	20	Settling Time	10
VS Setting	K_p	1		
Value	K_i	1	Steady State Error	0
Value	K_d	0		

Chart14: PID Controller control DC Motor Speed Actual Value

Speed =2, $K_p = 1$, $K_i = 1$

Actual	Setting Time	2	Overshoot	0%
Value	Termination Value	2	Rise-time	1.6
VS	Stop Value	20	Settling Time	10
Setting	K_p	1	Steady State Error	0

Value	K_i	1
	K_d	0

Chart15: PID Controller control DC Motor Speed Actual Value

Speed =3, $K_p = 1$, $K_i = 1$

1	Setting Time	2	Overshoot	0%
Actual	Termination Value	3	Rise-time	2.4
Value	Stop Value	20	Settling Time	10
VS Setting	K_p	1		
Value	K_i	1	Steady State Error	0
v aruc	K_d	0		

Chart16: PID Controller control DC Motor Speed Actual Value

Speed =4, $K_p = 1$, $K_i = 1$

1	Setting Time	2	Overshoot	0%
Actual	Termination Value	4	Rise-time	3.4
Value	Stop Value	20	Settling Time	10
VS Setting	K_p	1		
Value	K_i	1	Steady State Error	0
value	K_d	0		

Chart17: PID Controller control DC Motor Speed Actual Value

$$e(t) = |y(t) - r(t)| = |1 - 1| = 0$$

$$Overshoot = \frac{Max \ value - Settling \ value}{Settling \ value} * 100\%$$

$$Overshoot = \frac{1 - 1}{1} * 100\% = 0\%$$

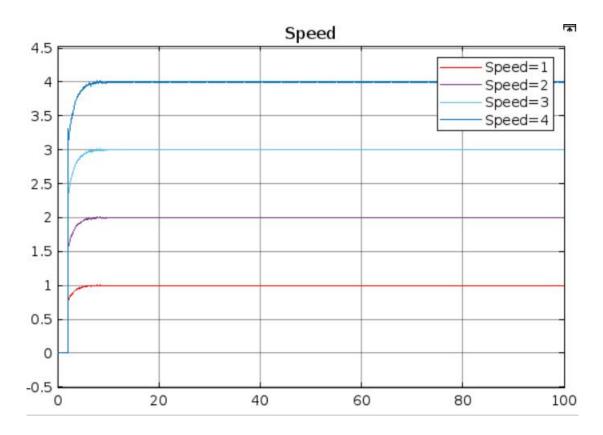


Figure 20: PID Controller control DC Motor Positive Speed Display

Analysis Figure 20, when K_p and K_i are constant, we change the speed and observe that except rise-time, other factors have no influence. The rise-time is increased, this is because rise-time and speed are related, the speed is greater, the rise-time is longer and the response speed is lower.

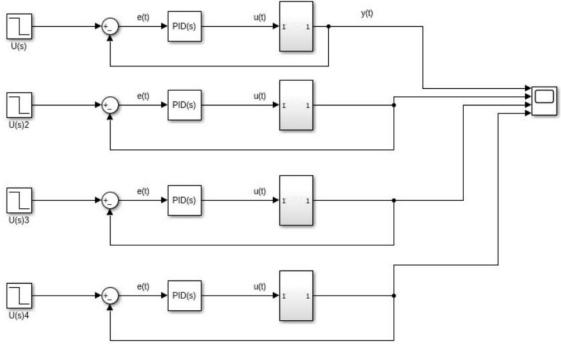


Figure 21: PID Controller control DC Motor Negative Speed

Speed =-2, $K_p = 0.5, K_i = 1$

1	Setting Time	2	Overshoot	0%
Actual	Termination Value	-2	Rise-time	1.28
Value	Stop Value	20	Settling Time	10
VS Setting	K_p	0.5		
Value	K_i	1	Steady State Error	0
value	K_d	0		

Chart18: PID Controller control DC Motor Speed Actual Value

Speed =-4, $K_p = 0.5$, $K_i = 1$

	Setting Time	2	Overshoot	0%
Actual	Termination Value	-4	Rise-time	2.6
Value	Stop Value	20	Settling Time	10
VS Setting	K_p	0.5		
Value	K_i	1	Steady State Error	0
Value	K_d	0		

Chart19: PID Controller control DC Motor Speed Actual Value

Speed =-6, $K_p = 0.5$, $K_i = 1$

Actual Value VS Setting Value	Setting Time	2	Overshoot	0%
	Termination Value	-6	Rise-time	3.85
	Stop Value	20	Settling Time	10
	K_p	0.5		0
	K_i	1	Steady State Error	
	K_d	0		

Chart20: PID Controller control DC Motor Speed Actual Value

Speed =-8, $K_p = 0.5$, $K_i = 1$

Actual Value VS Setting Value	Setting Time	2	Overshoot	0%
	Termination Value	-8	Rise-time	4
	Stop Value	20	Settling Time	10
	K_p	0.5		0
	K_i	1	Steady State Error	
	K_d	0		

Chart21: PID Controller control DC Motor Speed Actual Value

$$e(t) = |y(t) - r(t)| = |2-2| = 0$$

$$Overshoot = \frac{Max \ value - Settling \ value}{Settling \ value} *100\%$$

$$Overshoot = \frac{-2 - (-2)}{-2} *100\% = 0\%$$

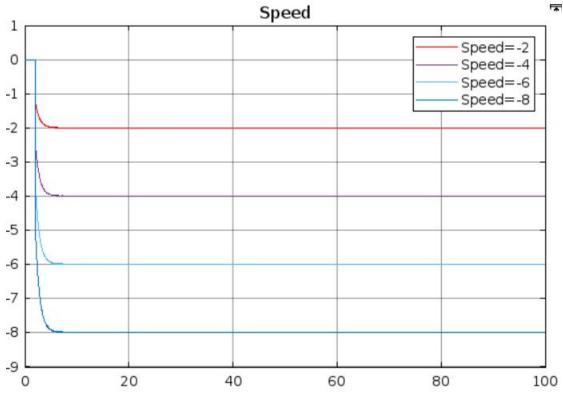


Figure 22: PID Controller control DC Motor Negative Speed Display

Analysis Figure 22, when K_p and K_i are constant, we change the negative speed and observe that except rise-time, other factors have no influence. The rise-time is increased, this is because rise-time and speed are related, the speed is greater, the rise-time is longer and the response speed is lower.

Conclusion

This report we are using Matlab Simulink design a DC motor, and connect the PID controller, we change the speed, K_p and K_i , then get the desired speed of the motor.

We investigate, demonstrate and explain in detail the observed effects of changes in controller gain, such as: Overshoot, Rise-time, Settling Time and Steady State Error.

Parameter	Oscillate	Overshoot	Rise-time	Settling Time	Steady State Error
Speed	/	/	Increase	/	/
K_p	Too large	Depend on situation	Depend on situation	Depend on situation	Reduce
K_i	Too large	Reduce	Reduce	Reduce	Reduce

Chart 22: PID Controller Parameter Influence

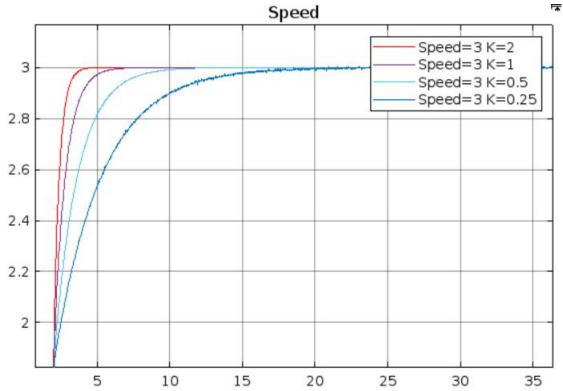


Figure 23: PID Controller control DC Motor Speed = 3 Display

Through this report, we can find that when K_p and K_i are too large, the system will have oscillate, it will effect the stability of the system, so we change different K_p and K_i, finally when $K_p = 0.5$ and $K_i = 2$, this close to setpoint value.

Reference

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