

1.

- a. $P(\text{BuyJersey}) = 7/11$
 $P(\text{BuyJersey}) = 4/11$
- b. $P(\text{Weather} = \text{clear} \mid \text{BuyJersey} = \text{yes}) = 3/7$
 $P(\text{Weather} = \text{cloudy} \mid \text{BuyJersey} = \text{yes}) = 2/7$
 $P(\text{Weather} = \text{rainy} \mid \text{BuyJersey} = \text{yes}) = 2/7$
 $P(\text{Weather} = \text{clear} \mid \text{BuyJersey} = \text{no}) = 1/4$
 $P(\text{Weather} = \text{cloudy} \mid \text{BuyJersey} = \text{no}) = 1/4$
 $P(\text{Weather} = \text{rainy} \mid \text{BuyJersey} = \text{no}) = 2/4$
- c. $P(\text{Uniform} = \text{crimson} \mid \text{BuyJersey} = \text{yes}) = 6/7$
 $P(\text{Uniform} = \text{gray} \mid \text{BuyJersey} = \text{yes}) = 1/7$
 $P(\text{Uniform} = \text{crimson} \mid \text{BuyJersey} = \text{no}) = 0/4 \Rightarrow (0 + 1)/4 = 1/4$
 $P(\text{Uniform} = \text{gray} \mid \text{BuyJersey} = \text{no}) = 1$
- d. $P(\text{Win} = \text{yes} \mid \text{BuyJersey} = \text{yes}) = 4/7$
 $P(\text{Win} = \text{no} \mid \text{BuyJersey} = \text{yes}) = 3/7$
 $P(\text{Win} = \text{yes} \mid \text{BuyJersey} = \text{no}) = 1/4$
 $P(\text{Win} = \text{no} \mid \text{BuyJersey} = \text{no}) = 3/4$
- e. $P(\text{BuyJersey} = \text{yes} \mid \text{Weather} = \text{cloudy}, \text{Uniform} = \text{gray}, \text{Win} = \text{yes})$
 $= \alpha * P(\text{Weather} = \text{cloudy}, \text{Uniform} = \text{gray}, \text{Win} = \text{yes} \mid \text{BuyJersey} = \text{yes}) * P(\text{BuyJersey} = \text{yes})$
 $= \alpha * P(\text{Weather} = \text{cloudy} \mid \text{BuyJersey} = \text{yes}) * P(\text{Uniform} = \text{gray} \mid \text{BuyJersey} = \text{yes}) * P(\text{Win} = \text{yes} \mid \text{BuyJersey} = \text{yes}) * P(\text{BuyJersey} = \text{yes})$
 $= \alpha * \frac{2}{7} * \frac{1}{7} * \frac{4}{7} * \frac{7}{11}$
 $= \alpha(0.015) \text{ from } \alpha \text{ below} = 0.39$
 $P(\text{BuyJersey} = \text{no} \mid \text{Weather} = \text{cloudy}, \text{Uniform} = \text{gray}, \text{Win} = \text{yes})$
 $= \alpha * P(\text{Weather} = \text{cloudy}, \text{Uniform} = \text{gray}, \text{Win} = \text{yes} \mid \text{BuyJersey} = \text{no}) * P(\text{BuyJersey} = \text{no})$
 $= \alpha * P(\text{Weather} = \text{cloudy} \mid \text{BuyJersey} = \text{no}) * P(\text{Uniform} = \text{gray} \mid \text{BuyJersey} = \text{no}) * P(\text{Win} = \text{yes} \mid \text{BuyJersey} = \text{no}) * P(\text{BuyJersey} = \text{no})$
 $= \alpha * \frac{1}{4} * 1 * \frac{1}{4} * \frac{4}{11}$
 $= \alpha(0.023) \text{ from } \alpha \text{ below} = 0.61$
 $\alpha = 1/(0.015 + 0.023) = 26.32$

- f. Since $P(\text{BuyJersey} = \text{yes} \mid \text{Weather} = \text{cloudy}, \text{Uniform} = \text{gray}, \text{Win} = \text{yes}) < P(\text{BuyJersey} = \text{no} \mid \text{Weather} = \text{cloudy}, \text{Uniform} = \text{gray}, \text{Win} = \text{yes})$, Naïve Bayes would classify the new instance as $\text{BuyJersey} = \text{no}$.

2. Perception

- a. See the table below:

Weather	Uniform	Win	BuyJersey
0	0	1	1
0	0	0	1
0	1	1	1
0	1	0	0
1	0	1	1
1	0	0	1
1	1	0	0
2	0	1	1
2	0	0	1
2	1	1	0
2	1	0	0

- b. New instance $\langle \text{Weather}=\text{cloudy}, \text{Uniform}=\text{gray}, \text{Win}=\text{yes}, \text{BuyJersey}=\text{no} \rangle$

Weather	Uniform	Win	BuyJersey
1	1	1	0

before any training passes, new instance:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 * 1 + 1 * 1 + 1 * 1 + 1 * 1 = 4 > 0 \rightarrow 1 \text{ (incorrect)}$$

- c. Training.

Pass#1

Example1:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 + 0 + 0 + 1 = 2 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example2:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 + 0 + 0 + 0 = 1 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example3:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 + 0 + 1 + 1 = 3 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example4:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 + 0 + 1 + 0 = 2 \geq 0 \rightarrow 1 \text{ (incorrect)}$$

$$w_i = w_i + \eta(\text{correct} - \text{output})x_i$$

$$w_0 = 1 + 0.5 * (0 - 1) * 1 = 0.5$$

$$w_1 = 1 + 0.5 * (0 - 1) * 0 = 1$$

$$w_2 = 1 + 0.5 * (0 - 1) * 1 = 0.5$$

$$w_3 = 1 + 0.5 * (0 - 1) * 1 = 1$$

Example5:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 + 1 + 0 + 1 = 2.5 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example6:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 + 1 + 0 + 0 = 1.5 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example7:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 + 1 + 0.5 + 0 = 2 \geq 0 \rightarrow 1 \text{ (incorrect)}$$

$$w_i = w_i + \eta(\text{correct} - \text{output})x_i$$

$$w_0 = 0.5 + 0.5 * (0 - 1) * 1 = 0$$

$$w_1 = 1 + 0.5 * (0 - 1) * 1 = 0.5$$

$$w_2 = 0.5 + 0.5 * (0 - 1) * 1 = 0$$

$$w_3 = 1 + 0.5 * (0 - 1) * 0 = 1$$

Example8:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0 + 1 + 0 + 1 = 2 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example9:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0 + 1 + 0 + 0 = 1 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example10:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0 + 1 + 0 + 1 = 2 \geq 0 \rightarrow 1 \text{ (incorrect)}$$

$$w_i = w_i + \eta(\text{correct} - \text{output})x_i$$

$$w_0 = 0 + 0.5 * (0 - 1) * 1 = -0.5$$

$$w_1 = 0.5 + 0.5 * (0 - 1) * 2 = -0.5$$

$$w_2 = 0 + 0.5 * (0 - 1) * 1 = -0.5$$

$$w_3 = 1 + 0.5 * (0 - 1) * 1 = 0.5$$

Example11:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = -0.5 - 1 - 0.5 + 0 = -2 < 0 \rightarrow 0 \text{ (correct)}$$

d. new instance < Weather=cloudy, Uniform=gray, Win=yes >

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = -0.5 - 0.5 - 0.5 - 0.5 = -2 < 0 \rightarrow 0 \text{ (correct)}$$

3. Input .arff file:

@relation Pass

@attribute Weather{clear,cloudy,rainy}

@attribute Uniform{crimson,gray}

@attribute Win{yes,no}

@attribute BuyJersey{yes,no}

@data

clear,crimson,yes,yes

clear,crimson,no,yes

clear,gray,yes,yes

clear,gray,no,no

cloudy,crimson,yes,yes

cloudy,crimson,no,yes

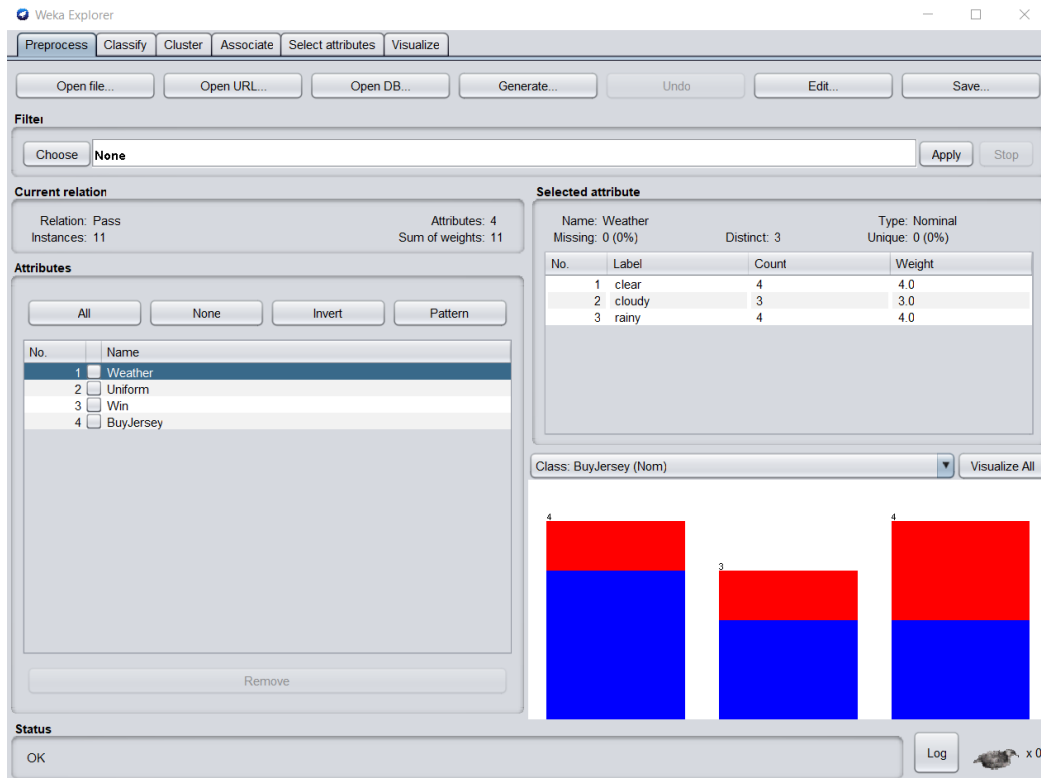
cloudy,gray,no,no

rainy,crimson,yes,yes

rainy,crimson,no,yes

rainy,gray,yes,no

rainy,gray,no,no



Output:

=== Run information ===

Scheme: weka.classifiers.bayes.NaiveBayes

Relation: Pass

Instances: 11

Attributes: 4

Weather

Uniform

Win

BuyJersey

Test mode: evaluate on training data

=== Classifier model (full training set) ===

Naive Bayes Classifier

Class

Attribute yes no

(0.62) (0.38)

=====

Weather		
clear	4.0	2.0
cloudy	3.0	2.0
rainy	3.0	3.0
[total]	10.0	7.0

Uniform		
crimson	7.0	1.0
gray	2.0	5.0
[total]	9.0	6.0

Win		
yes	5.0	2.0
no	4.0	4.0
[total]	9.0	6.0

Time taken to build model: 0 seconds

=== Evaluation on training set ===

Time taken to test model on training data: 0 seconds

=== Summary ===

Correctly Classified Instances	10	90.9091 %
Incorrectly Classified Instances	1	9.0909 %
Kappa statistic	0.8136	
Mean absolute error	0.2047	
Root mean squared error	0.2399	
Relative absolute error	43.6901 %	
Root relative squared error	49.8209 %	
Total Number of Instances	11	

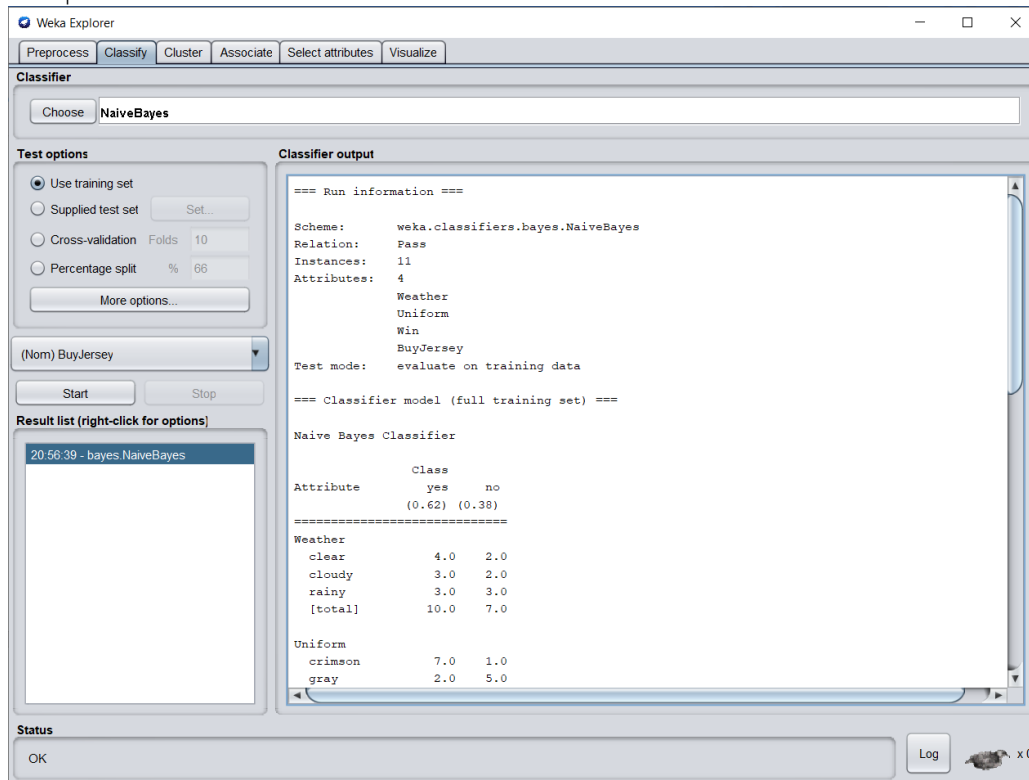
=== Detailed Accuracy By Class ===

	TP Rate	FP Rate	Precision	Recall	F-Measure	MCC	ROC Area	PRC
Area Class								
	0.857	0.000	1.000	0.857	0.923	0.828	1.000	yes
	1.000	0.143	0.800	1.000	0.889	0.828	1.000	no
Weighted Avg.	0.909	0.052	0.927	0.909	0.911	0.828	1.000	1.000

=== Confusion Matrix ===

a b <-- classified as

6 1 | a = yes
0 4 | b = no



4. Keep training

Pass#2

$$w_0 = -0.5, w_1 = -0.5, w_2 = -0.5, w_3 = 0.5$$

Example1:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = -0.5 + 0 + 0 + 0.5 = 0 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example2:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = -0.5 + 0 + 0 + 0 = -0.5 < 0 \rightarrow 0 \text{ (incorrect)}$$

$$w_i = w_i + \eta(\text{correct} - \text{output})x_i$$

$$w_0 = -0.5 + 0.5 * (1 - 0) * 1 = 0$$

$$w_1 = -0.5 + 0.5 * (1 - 0) * 0 = -0.5$$

$$w_2 = -0.5 + 0.5 * (1 - 0) * 0 = -0.5$$

$$w_3 = 0.5 + 0.5 * (1 - 0) * 0 = 0.5$$

Example3:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0 + 0 - 0.5 + 0.5 = 0 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example4:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0 + 0 - 0.5 + 0 = -0.5 < 0 \rightarrow 0 \text{ (correct)}$$

Example5:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0 - 0.5 + 0 + 0.5 = 0 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example6:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0 - 0.5 + 0 + 0 = -0.5 < 0 \rightarrow 0 \text{ (incorrect)}$$

$$w_i = w_i + \eta(\text{correct} - \text{output})x_i$$

$$\begin{aligned}
w_0 &= 0 + 0.5 * (1 - 0) * 1 = 0.5 \\
w_1 &= -0.5 + 0.5 * (1 - 0) * 1 = 0 \\
w_2 &= -0.5 + 0.5 * (1 - 0) * 0 = -0.5 \\
w_3 &= 0.5 + 0.5 * (1 - 0) * 0 = 0.5
\end{aligned}$$

Example7:

$$\begin{aligned}
w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 &= 0.5 + 0 - 0.5 + 0 = 0 \geq 0 \rightarrow 1 \text{ (incorrect)} \\
w_0 &= 0.5 + 0.5 * (0 - 1) * 1 = 0 \\
w_1 &= 0 + 0.5 * (0 - 1) * 1 = -0.5 \\
w_2 &= -0.5 + 0.5 * (0 - 1) * 1 = -1 \\
w_3 &= 0.5 + 0.5 * (0 - 1) * 0 = 0.5
\end{aligned}$$

Example8:

$$\begin{aligned}
w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 &= 0 - 1 + 0 + 0.5 = -0.5 < 0 \rightarrow 0 \text{ (incorrect)} \\
w_0 &= 0 + 0.5 * (1 - 0) * 1 = 0.5 \\
w_1 &= -0.5 + 0.5 * (1 - 0) * 2 = 0.5 \\
w_2 &= -1 + 0.5 * (1 - 0) * 0 = -1 \\
w_3 &= 0.5 + 0.5 * (1 - 0) * 1 = 1
\end{aligned}$$

Example9:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 + 1 + 0 + 0 = 1.5 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example10:

$$\begin{aligned}
w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 &= 0.5 + 1 - 1 + 1 = 1.5 \geq 0 \rightarrow 1 \text{ (incorrect)} \\
w_i &= w_i + \eta(\text{correct} - \text{output})x_i \\
w_0 &= 0.5 + 0.5 * (0 - 1) * 1 = 0 \\
w_1 &= 0.5 + 0.5 * (0 - 1) * 2 = -0.5 \\
w_2 &= -1 + 0.5 * (0 - 1) * 1 = -1.5 \\
w_3 &= 1 + 0.5 * (0 - 1) * 1 = 0.5
\end{aligned}$$

Example11:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0 - 1 - 1.5 + 0 = -2.5 < 0 \rightarrow 0 \text{ (correct)}$$

Pass#3

$$w_0 = 0, w_1 = -0.5, w_2 = -1.5, w_3 = 0.5$$

Example1:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0 + 0 + 0 + 0.5 = 0.5 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example2:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0 + 0 + 0 + 0 = 0 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example3:

$$\begin{aligned}
w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 &= 0 + 0 - 1.5 + 0.5 = -1 < 0 \rightarrow 0 \text{ (incorrect)} \\
w_0 &= 0 + 0.5 * (1 - 0) * 1 = 0.5 \\
w_1 &= -0.5 + 0.5 * (1 - 0) * 0 = -0.5 \\
w_2 &= -1.5 + 0.5 * (1 - 0) * 1 = -1 \\
w_3 &= 0.5 + 0.5 * (1 - 0) * 1 = 1
\end{aligned}$$

Example4:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 + 0 - 1 + 0 = -0.5 < 0 \rightarrow 0 \text{ (correct)}$$

Example5:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 0.5 + 0 + 1 = 1 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example6:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 0.5 + 0 + 0 = 0 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example7:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 0.5 - 1 + 0 = -1 < 0 \rightarrow 0 \text{ (correct)}$$

Example8:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 1 + 0 + 1 = 0.5 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example9:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 1 + 0 + 0 = -0.5 < 0 \rightarrow 0 \text{ (incorrect)}$$

$$w_0 = 0.5 + 0.5 * (1 - 0) * 1 = 1$$

$$w_1 = -0.5 + 0.5 * (1 - 0) * 2 = 0.5$$

$$w_2 = -1 + 0.5 * (1 - 0) * 0 = -1$$

$$w_3 = 1 + 0.5 * (1 - 0) * 0 = 1$$

Example10:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 + 1 - 1 + 1 = 2 \geq 0 \rightarrow 1 \text{ (incorrect)}$$

$$w_i = w_i + \eta(\text{correct} - \text{output})x_i$$

$$w_0 = 1 + 0.5 * (0 - 1) * 1 = 0.5$$

$$w_1 = 0.5 + 0.5 * (0 - 1) * 2 = -0.5$$

$$w_2 = -1 + 0.5 * (0 - 1) * 1 = -1.5$$

$$w_3 = 1 + 0.5 * (0 - 1) * 1 = 0.5$$

Example11:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 1 - 1.5 + 0 = -2 < 0 \rightarrow 0 \text{ (correct)}$$

Pass#4

$$w_0 = 0.5, w_1 = -0.5, w_2 = -1.5, w_3 = 0.5$$

Example1:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 + 0 + 0 + 0.5 = 1 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example2:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 + 0 + 0 + 0 = 0.5 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example3:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 + 0 - 1.5 + 0.5 = -0.5 < 0 \rightarrow 0 \text{ (incorrect)}$$

$$w_0 = 0.5 + 0.5 * (1 - 0) * 1 = 1$$

$$w_1 = -0.5 + 0.5 * (1 - 0) * 0 = -0.5$$

$$w_2 = -1.5 + 0.5 * (1 - 0) * 1 = -1$$

$$w_3 = 0.5 + 0.5 * (1 - 0) * 1 = 1$$

Example4:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 + 0 - 1 + 0 = 0 \geq 0 \rightarrow 1 \text{ (incorrect)}$$

$$w_0 = 1 + 0.5 * (0 - 1) * 1 = 0.5$$

$$w_1 = -0.5 + 0.5 * (0 - 1) * 0 = -0.5$$

$$w_2 = -1 + 0.5 * (0 - 1) * 1 = -1.5$$

$$w_3 = 1 + 0.5 * (0 - 1) * 0 = 1$$

Example5:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 0.5 + 0 + 1 = 1 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example6:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 0.5 + 0 + 0 = 0 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example7:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 0.5 - 1.5 + 0 = -1.5 < 0 \rightarrow 0 \text{ (correct)}$$

Example8:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 1 + 0 + 1 = 0.5 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example9:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 1 + 0 + 0 = -0.5 < 0 \rightarrow 0 \text{ (incorrect)}$$

$$w_0 = 0.5 + 0.5 * (1 - 0) * 1 = 1$$

$$w_1 = -0.5 + 0.5 * (1 - 0) * 2 = 0.5$$

$$w_2 = -1.5 + 0.5 * (1 - 0) * 0 = -1.5$$

$$w_3 = 1 + 0.5 * (1 - 0) * 0 = 1$$

Example10:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 + 1 - 1.5 + 1 = 1.5 \geq 0 \rightarrow 1 \text{ (incorrect)}$$

$$w_i = w_i + \eta(\text{correct} - \text{output})x_i$$

$$w_0 = 1 + 0.5 * (0 - 1) * 1 = 0.5$$

$$w_1 = 0.5 + 0.5 * (0 - 1) * 2 = -0.5$$

$$w_2 = -1.5 + 0.5 * (0 - 1) * 1 = -2$$

$$w_3 = 1 + 0.5 * (0 - 1) * 1 = 0.5$$

Example11:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 1 - 2 + 0 = -2.5 < 0 \rightarrow 0 \text{ (correct)}$$

Pass#5

$$w_0 = 0.5, w_1 = -0.5, w_2 = -2, w_3 = 0.5$$

Example1:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 + 0 + 0 + 0.5 = 1 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example2:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 + 0 + 0 + 0 = 0.5 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example3:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 + 0 - 2 + 0.5 = -1 < 0 \rightarrow 0 \text{ (incorrect)}$$

$$w_0 = 0.5 + 0.5 * (1 - 0) * 1 = 1$$

$$w_1 = -0.5 + 0.5 * (1 - 0) * 0 = -0.5$$

$$w_2 = -2 + 0.5 * (1 - 0) * 1 = -1.5$$

$$w_3 = 0.5 + 0.5 * (1 - 0) * 1 = 1$$

Example4:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 + 0 - 1.5 + 0 = -0.5 < 0 \rightarrow 0 \text{ (correct)}$$

Example5:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 - 0.5 + 0 + 1 = 1.5 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example6:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 0.5 + 0 + 0 = 0 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example7:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 0.5 - 1.5 + 0 = -1.5 < 0 \rightarrow 0 \text{ (correct)}$$

Example8:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 1 + 0 + 1 = 0.5 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example9:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 - 1 + 0 + 0 = 0 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example10:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 - 1 - 1.5 + 1 = -0.5 < 0 \rightarrow 0 \text{ (correct)}$$

Example11:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 1 - 2 + 0 = -2.5 < 0 \rightarrow 0 \text{ (correct)}$$

Pass#6

$$w_0 = 1, w_1 = -0.5, w_2 = -1.5, w_3 = 1$$

Example1:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 + 0 + 0 + 1 = 2 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example2:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 + 0 + 0 + 0 = 1 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example3:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 + 0 - 1.5 + 1 = 0.5 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example4:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 + 0 - 1.5 + 0 = -0.5 < 0 \rightarrow 0 \text{ (correct)}$$

Example5:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 - 0.5 + 0 + 1 = 1.5 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example6:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 0.5 + 0 + 0 = 0 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example7:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 0.5 - 1.5 + 0 = -1.5 < 0 \rightarrow 0 \text{ (correct)}$$

Example8:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 1 + 0 + 1 = 0.5 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example9:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 - 1 + 0 + 0 = 0 \geq 0 \rightarrow 1 \text{ (correct)}$$

Example10:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 1 - 1 - 1.5 + 1 = -0.5 < 0 \rightarrow 0 \text{ (correct)}$$

Example11:

$$w_0x_0 + w_1x_1 + w_2x_2 + w_3x_3 = 0.5 - 1 - 2 + 0 = -2.5 < 0 \rightarrow 0 \text{ (correct)}$$

Thus, the final perceptron weights are:

$$w_0 = 1, w_1 = -0.5, w_2 = -1.5, w_3 = 1$$