

# Traveling Tournament Problem

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# Outline

- **Approach**
- Parameter Exploration
- Results

# Representation

- $i \times j$  matrix  $G$
- $i \dots$  round
- $j \dots$  team 1
- $g_{i,j} \in G \dots$  team 2
- $\text{sgn}(g_{i,j}) \dots$  negative away, positive home

# Approach

- Greedy Randomized Search Procedure (GRASP)
  - construct multiple initial solutions
  - multiple local searches
- Problem relaxation
  - soft / hard constraints + penalty

# Construction

- Randomized (iterated local search)
- Randomized with heuristic (GRASP)
  - Random Greedy

# GRASP Construction

- create “virtual schedule”
- real teams → virtual schedule (greedy)
  - count # of consecutive team-pairs
  - sort real teams by distance
  - assign closely located teams to high count

# GRASP Construction

continued

- create set of candidate pairs
  - team-pair with smallest distance
  - team-pairs  $<$  threshold
- choose randomly

# GRASP Construction

extended

- avoid known solutions
  - tabu list
- different virtual schedules
  - [AMHV06]
  - [GS07]



# Tabu Search

- recency based memory
- complete schedules stored
- no aspiration criteria
- union of multiple neighborhoods

# Neighborhoods

- Shift Round
- Swap Home-Visitor
- Swap Match Round
- Swap Matches
- 2-opt Swap Rounds
- 2-opt Swap Teams

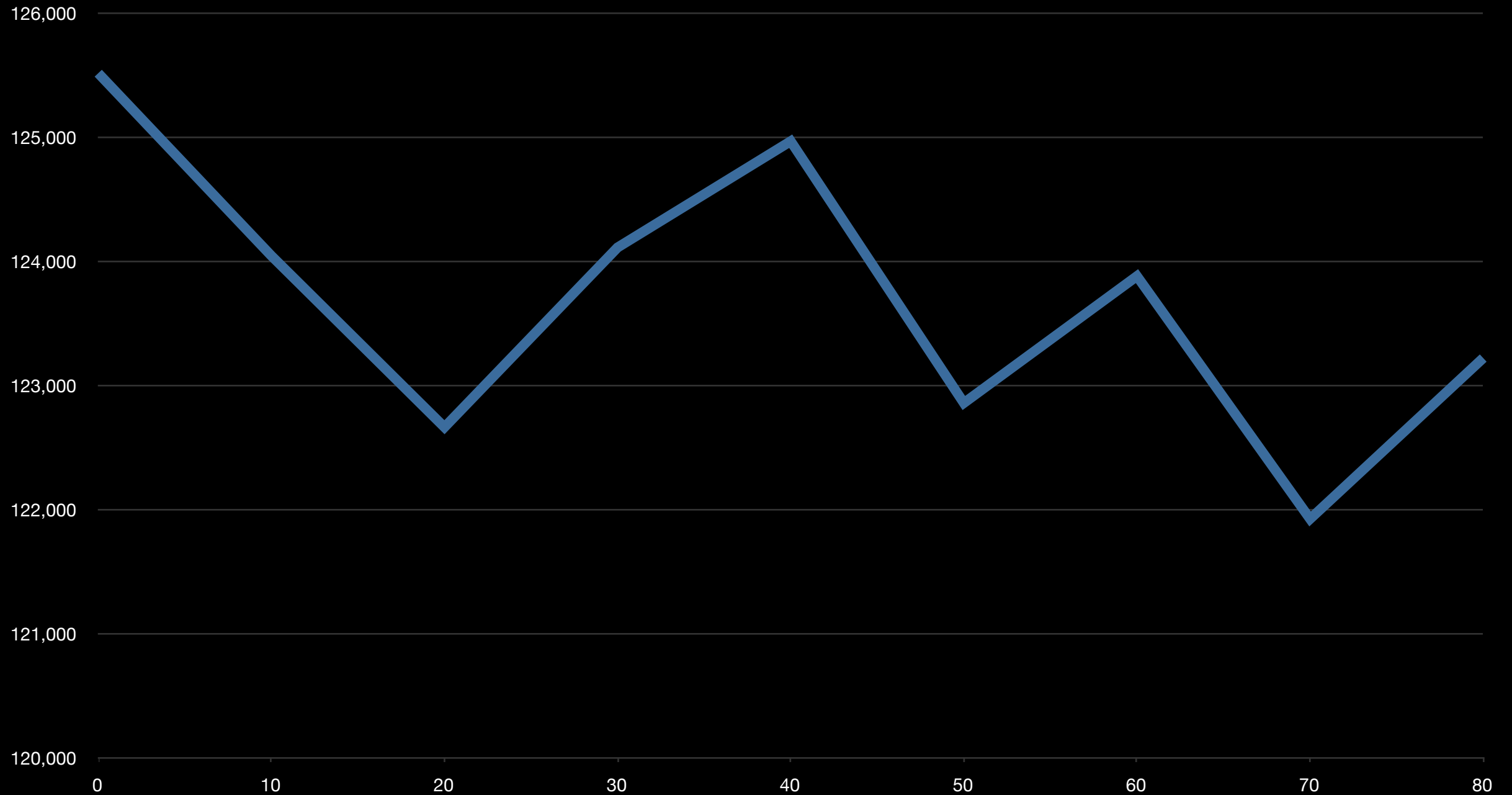
# Outline

- Approach
- **Parameter Exploration**
- Results

# Parameter Exploration

- use baseline, vary one parameter
- length of tabu list: 0, 10 ... **50** ... 80
- iterations: 100, 200 ... **500**, 600
- # of searches: 10, 20 ... **40** ... 80
- neighborhoods:  $2^{\{\text{neighborhoods}\}}$  -  $\emptyset$

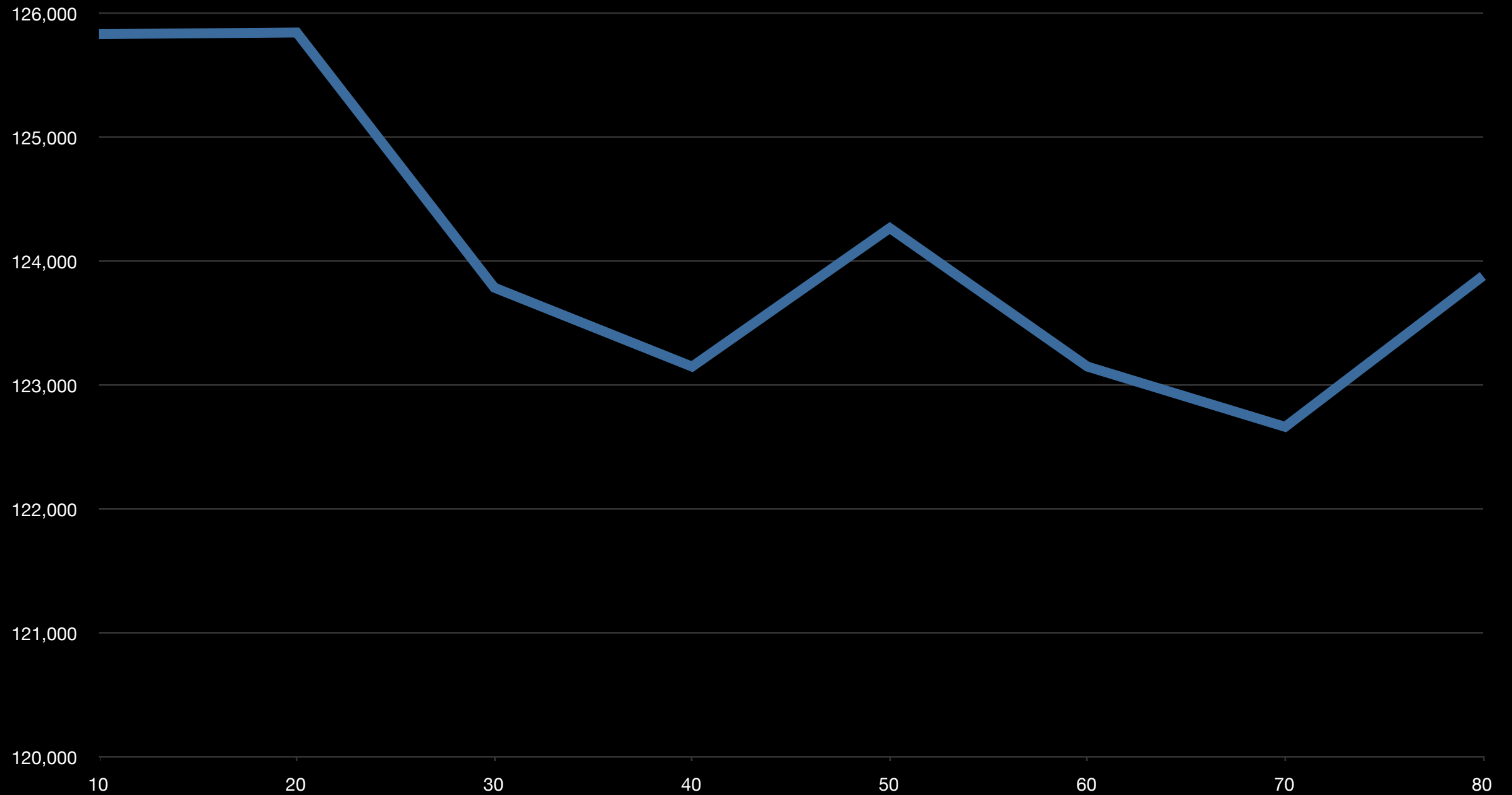
# Tabu List Length - Cost



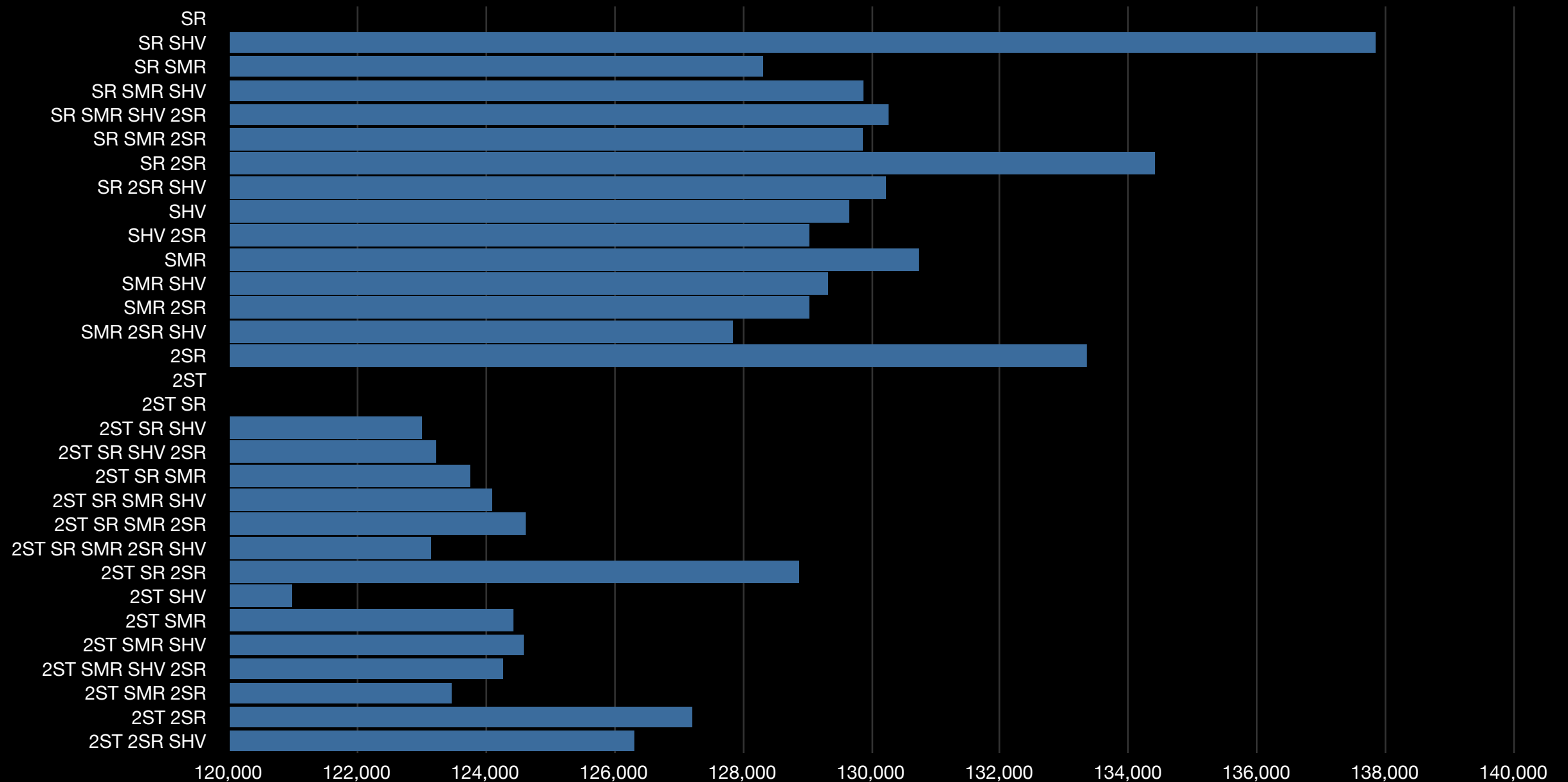
# # Iterations - Cost



# # Searches - Cost



# Neighborhoods - Cost





# Outline

- Approach
- Parameter Exploration
- **Results**

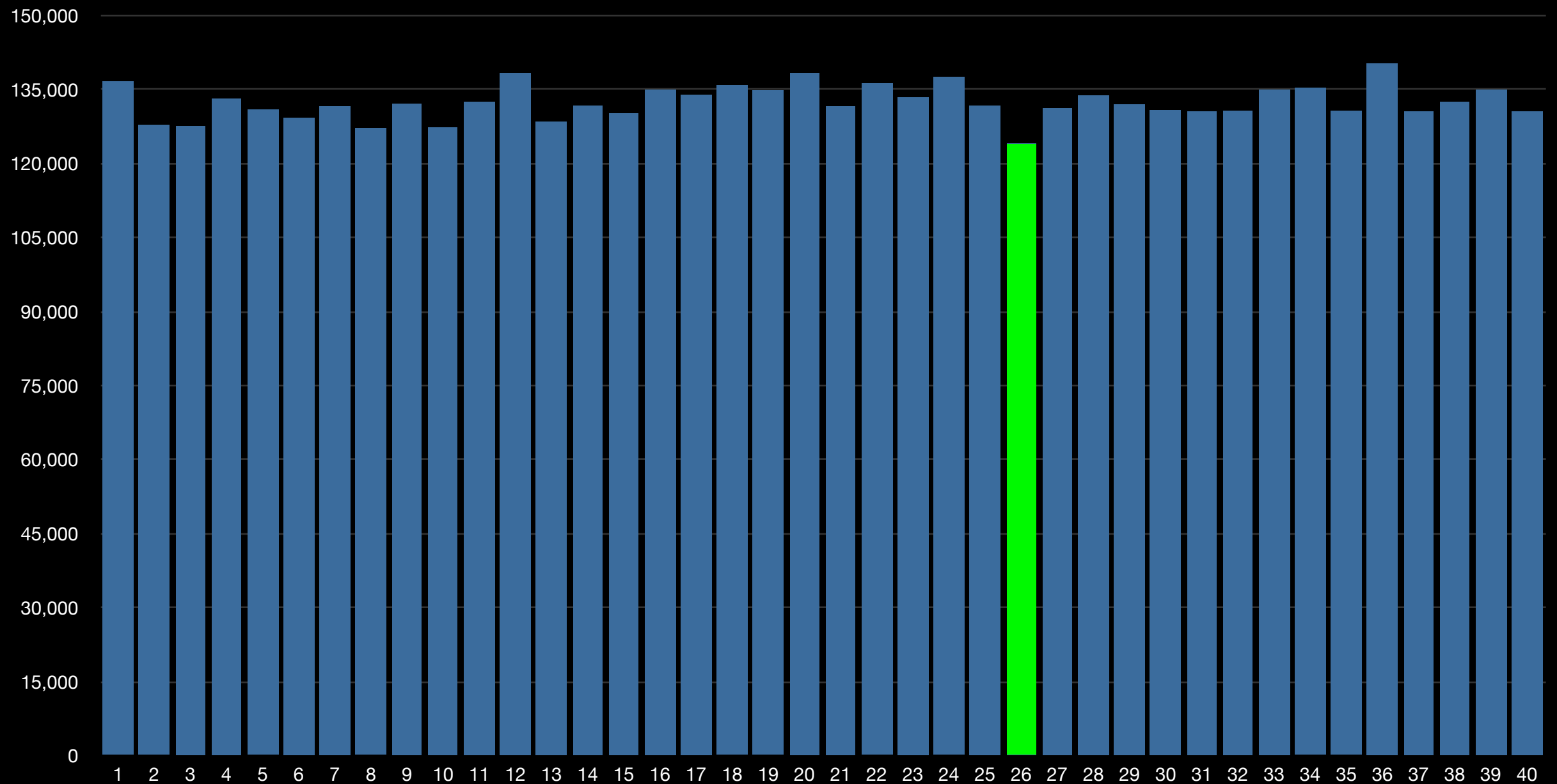
# NLx Parameters

- Method: GRASP
- Construction Heuristic: GRASP, threshold 0.4
- Tabu-List Length: 70
- # Iterations: 10,000
- # Searches: 40
- Neighborhoods: all

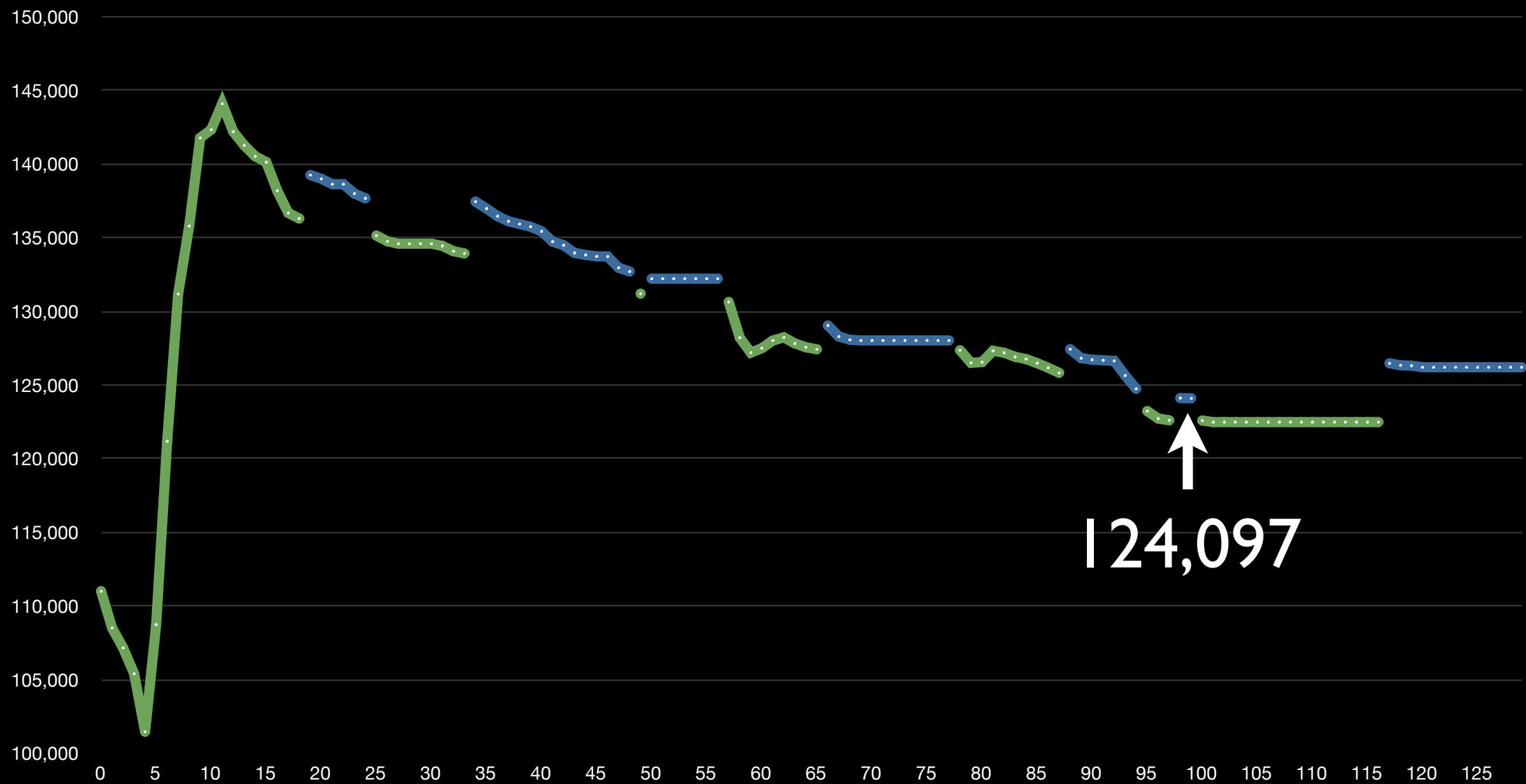
# NLx Results

	<b>min</b>	<b>max</b>	<b>avg</b>	<b>median</b>
<b>4</b>	8,276	8,276	8,276.0	8,276.0
<b>6</b>	23,916	24,073	23,931.7	23,916.0
<b>8</b>	40,806	41,833	41,024.2	40,929.0
<b>10</b>	63,660	64,948	64,311.5	64,463.0
<b>12</b>	124,097	127,639	125,374.8	124,725.5

# GRASP Run (NLI2)



# Tabu Search Run (NLI2)



thanks for your attention

questions?

# References

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- [CKB07] P.-C. Chen, G. Kendall, and G. Vanden Berghe. **An ant based hyper-heuristic for the travelling tournament problem.** In Proceedings of 2007 IEEE Symposium of Computational Intelligence in Scheduling (CISched 2007), pages 19–26. Hawaii, 2007.
- [GS07] Luca Di Gaspero and Andrea Schaerf. **A composite-neighborhood tabu search approach to the travelling tournament problem.** Journal of Heuristics, 13:189–207, 2007.
- [HV06] Pascal Van Hentenryck and Yannis Vergados. **Traveling tournament scheduling: A systematic evaluation of simulated annealing.** In CPAIOR, pages 228–243, 2006.
- [RBK08] F. Ryckbosch, G. Vanden Berghe, and G. Kendall. **A heuristic approach for the travelling tournament problem using optimal travelling salesman tours.** In PATAT 2008, 18-22 August 2008, Montreal, Canada 2008.
- [RU04] Celso C. Ribeiro and Sebastan Urrutia. **Heuristics for the mirrored traveling tournament problem.** European Journal of Operational Research, pages 323–342, 2004.