

COMP9334 Project Report

Server setup in data centres

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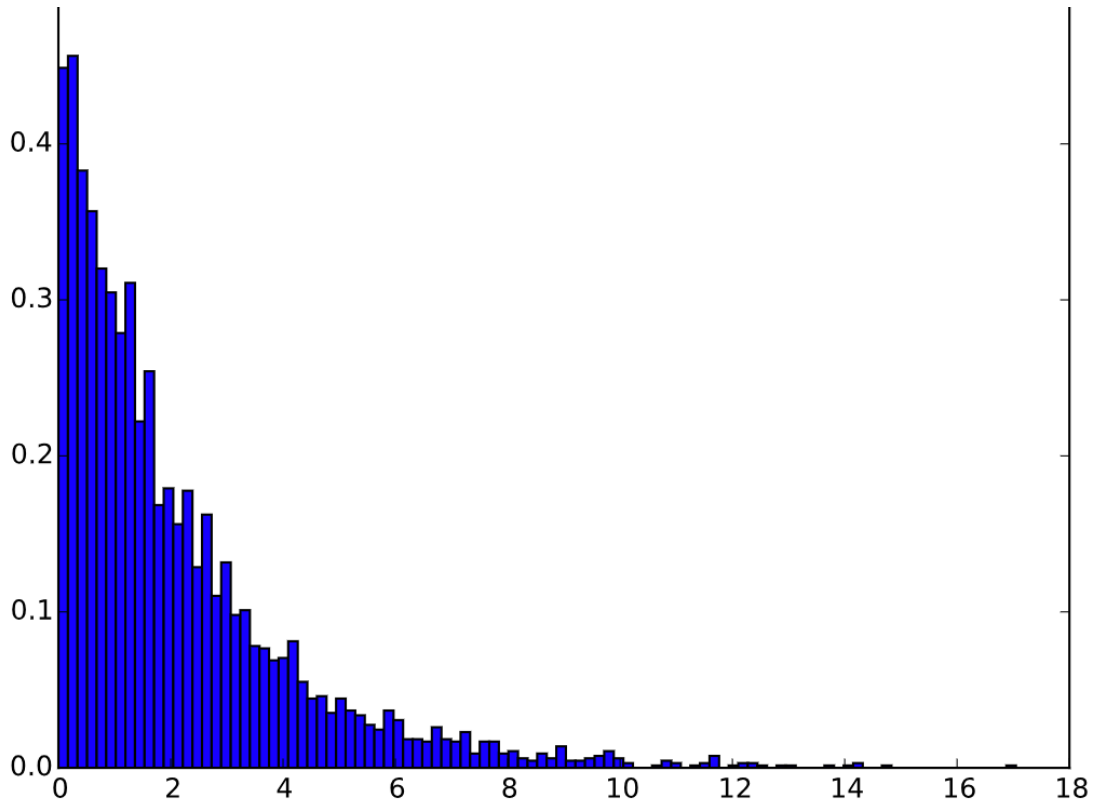
This project is designed to use simulation to perform the operation of the computer system. We need to handle arrivals and departures, then get the mean response time and departure time. And we need to choose the value of T_c for the improved system. This report will verify the following criteria.

1. The correctness of the inter-arrival probability distribution and service time distribution.

```
if mode == "random":
    lambda_value = float(read_value(arrival_name))
    mu_value = float(read_value(service_name))
    para = read_data(para_name)
    end_time = para[3]
    arrival = []
    service = []
    curr = 0
    flag = True
    inter_arrival = []
    while flag == True:
        inter = random.expovariate(lambda_value)
        curr += inter
        if curr < end_time:
            arrival.append(curr)
            inter_arrival.append(inter)
        else:
            flag = False
    job_number = len(arrival)
    for i in range(job_number):
        t = 0
        for j in range(3):
            t += random.expovariate(mu_value)
        service.append(t)
```

As the requirements said, the inter-arrival probability distribution is exponentially distributed with λ . So I use `random.expovariate(lambda)` to

generate the inter-arrival times and use *random.expovariate(mu)* to generate the random numbers and sum each three of them as service time. The numbers generated by *random.expovariate()* are obviously exponentially distributed. The plot graph for *random.expovariate* shows as:



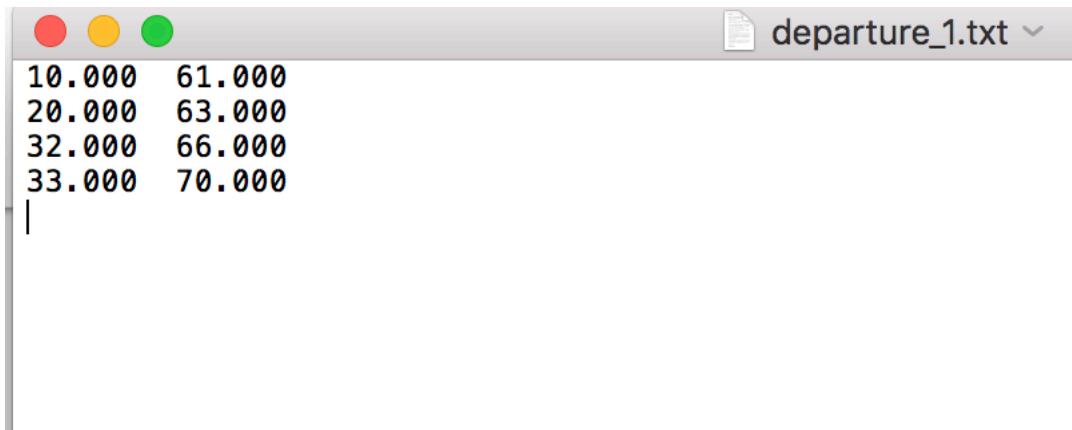
2. The correctness of my simulation code.

In “Trace” mode, I try to derive test cases in Section 3.2 to test my code. The arrival time and service time are in Table1.

Arrival time	Service time
10	1
20	2
30	3
33	4

Table 1: Example 1: Job arrival and service times.

After running my program, we get the *departure.txt*, which shows as:



```
10.000  61.000
20.000  63.000
32.000  66.000
33.000  70.000
|
```

These results have verified the Table 2 which shows the on-paper simulation with explanatory comments in example.

In “random” mode, I produce the inter-arrival time which then transforms to arrival time, as well as I produce service time, and store them in lists called ‘arrival’ and ‘service’.

```
if mode == "random":
    lambda_value = float(read_value(arrival_name))
    mu_value = float(read_value(service_name))
    para = read_data(para_name)
    end_time = para[3]
    arrival = []
    service = []
    curr = 0
    flag = True
    while flag == True:
        inter = random.expovariate(lambda_value)
        curr += inter
        if curr < end_time:
            arrival.append(curr)
        else:
            flag = False
    job_number = len(arrival)
    for i in range(job_number):
        t = 0
        for j in range(3):
            t += random.expovariate(mu_value)
        service.append(t)
    processing(arrival, service, para, number)
```

```
def processing(arrival, service, para, number):
```

Running the function processing() with these data, the departure.txt and mrt.txt produced. In this simulation, I choose seed = 1 to generate random numbers, so simulation experiments are reproducible.

```
def main(arrival_name, service_name, para_name, mode_name, number):
    mode = read_value(mode_name)
    random.seed(1)
```

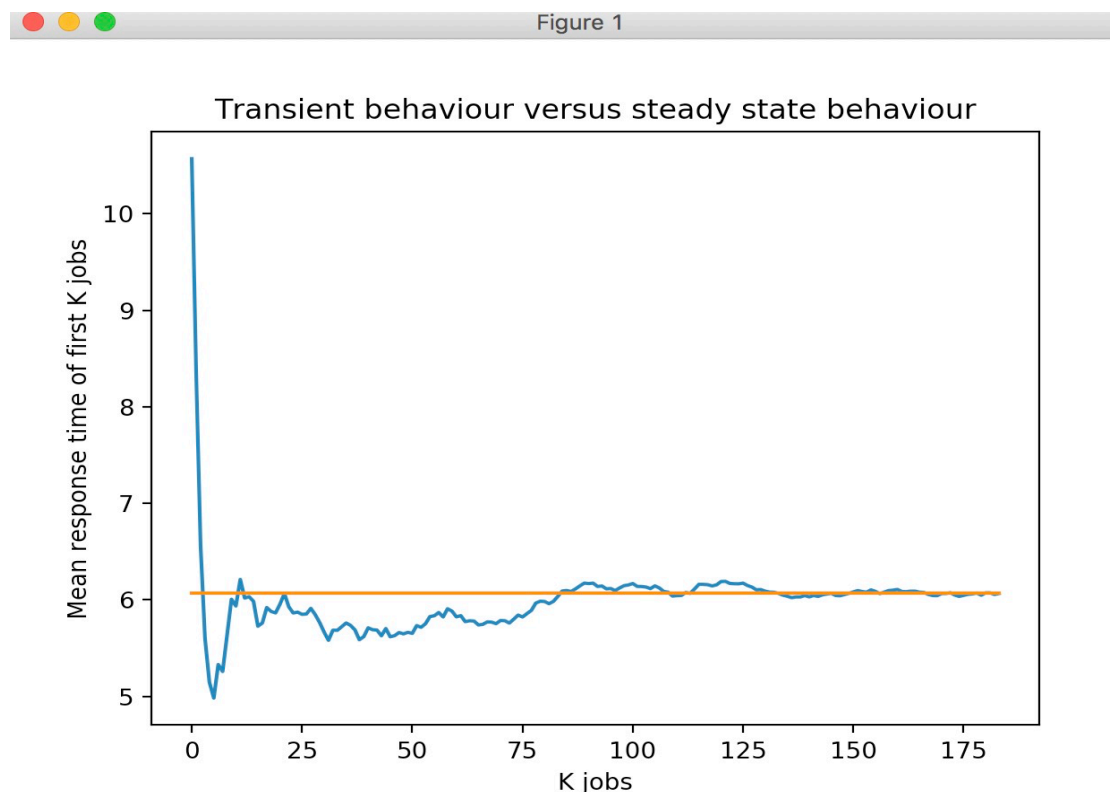
I used a sample para.txt with the following parameter values: the number of servers is 5, setup time is 5, $\lambda = 0.35$, $\mu = 1$, $T_c = 0.1$, and endtime = 500, the partial results are showed below:

departure_3.txt	
0.412	10.982
5.784	11.915
9.907	12.886
10.748	13.473
12.703	16.025
14.408	18.567
17.421	24.837
21.862	26.613
22.226	30.827
22.144	31.544
29.007	34.238
27.387	36.622
33.112	36.817
33.118	39.336
34.802	40.108
39.197	41.059
38.455	44.750
47.498	56.137
54.118	59.272
54.281	59.856
54.207	61.962
56.508	64.909
64.506	67.392
65.878	70.273
66.575	72.655
68.226	73.508
68.942	74.889
68.142	75.629
72.545	76.547
73.303	76.699

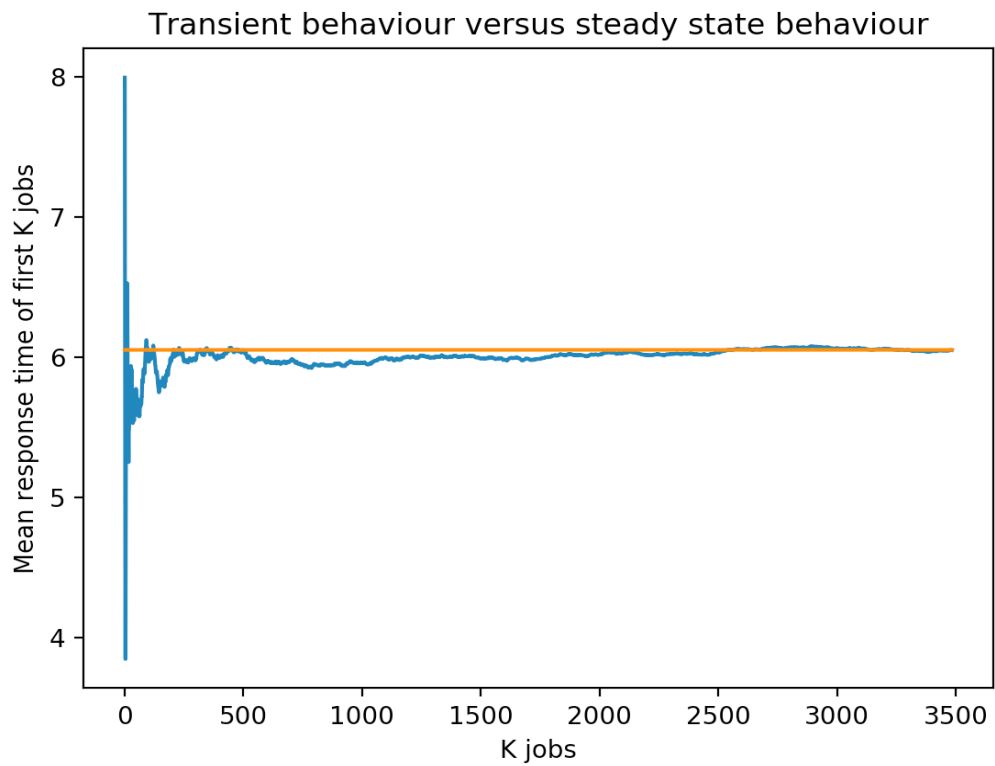
departure_3.txt	
397.531	401.251
400.770	403.145
403.018	411.632
403.730	412.324
414.339	421.075
418.906	426.218
424.692	427.380
421.705	427.483
420.983	427.942
426.127	432.199
429.685	434.066
428.578	434.135
432.533	435.204
433.719	437.783
432.706	438.529
443.545	453.343
450.544	456.680
449.499	457.034
456.131	457.917
457.193	460.793
465.198	473.085
469.089	477.117
471.482	478.284
470.626	478.289
477.620	479.674
471.457	481.975
477.509	483.559
482.510	485.429
491.868	499.776

3. Transient removal

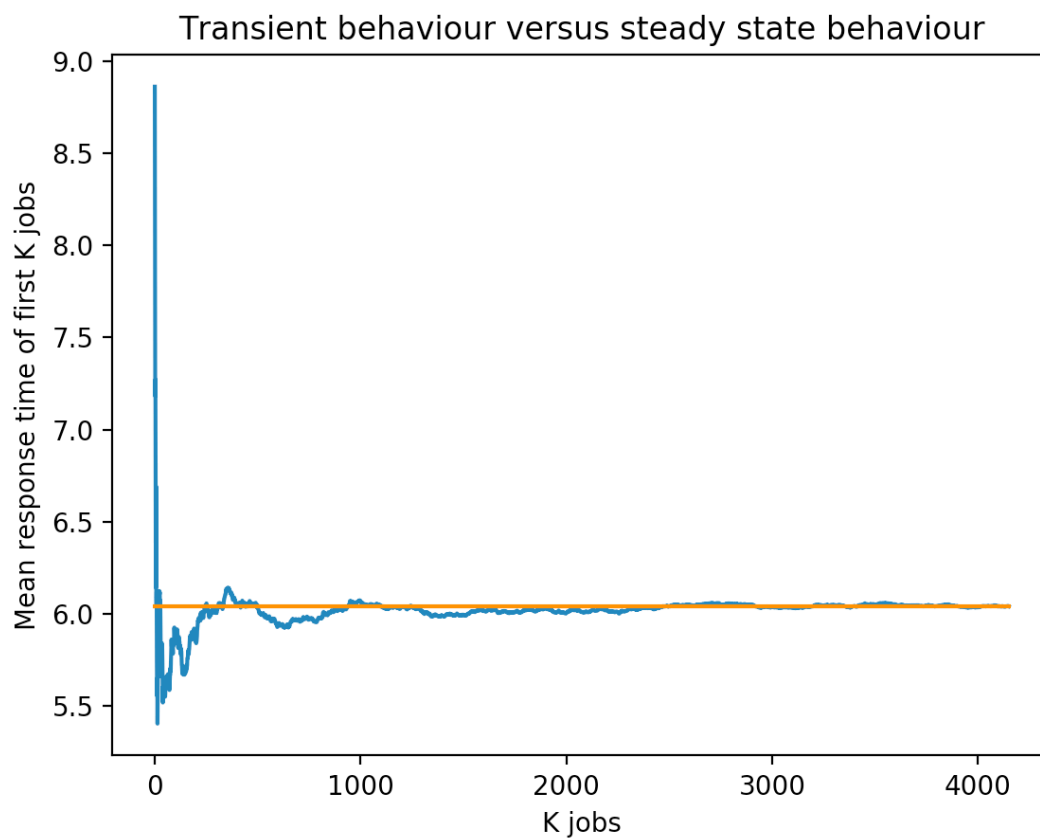
Response time continuously changes over time, in order to see a steady state, I compute the running mean by python file 'graph.py'. The graph produced as:



For further test, I try to run the simulation long enough so that I have a good number of jobs in the steady state part. I used a sample para.txt with the following parameter values: the number of servers is 5, setup time is 5, $\lambda = 0.35$, $\mu = 1$, $T_c = 0.1$ and **endtime = 10000**. The graph shows as:



In this simulation, the length of steady state is not longer than the transient.
So, I change the endtime into **12000**. The result shows as:



By observation, we can find that after 1600 jobs, the response time seems that it keeps in a steady state value. I get steady mean response time from file graph.py, the value is almost 6.0559541.

4. Determining a suitable value of T_c

In previous simulations, our baseline system uses the following parameter values: the number of servers is 5, setup time is 5, $\lambda = 0.35$, $\mu = 1$, $T_c = 0.1$ and endtime = 12000. This baseline system will give a poor response time because the servers have to be powered up again frequently.

In order to design an improved system, firstly, I have run some simulations with different T_c . And I get following data:

T_c	Steady mean response time
0.1	6.0559541
1	5.6779984
5	4.6295243
7	4.2951698
8	4.1490463
9	4.0593085
9.5	4.0112207

The improved system's response time must be 2 units less than that of the baseline system, so we can consider that the suitable value of T_c is around a value of 9. (The confidence interval produces by [caculate.py](#).)

Now we start with 5 replications by using **baseline system** (choose seed from 1 to N):

Number of replications	True mean response time	Confidence interval
5	6.0514517681548	(6.007814333636493, 6.095089202673107)
10	6.0478623482776	(5.941889661081383, 6.153835035474007)
20	6.0631314161020	(5.958067528253906, 6.168195303950132)

Then we start with 5 replications by using $T_c = 9$ (We will call this System1):

Number of replications	True mean response time	Confidence interval
5	4.0649336846382	(3.98223876453532, 4.147628604741029)
10	4.0707949466168	(3.96356652532867, 4.178023367904941)

It obviously shows that, if $[p,q]$ stands for 95% Confidence interval of EMRT System 1 - EMRT System baseline, p and q both less than 0. It means that System 1 is better than baseline system.

For getting better T_c which satisfy the requirement, I need to compare System 1 with others. We start with 5 replications by using $T_c = 9.5$ (We will call this System2):

Number of replications	True mean response time	Confidence interval
5	4.0291085530387	(3.9515833779643, 4.1066337281131355)
10	4.0335103841728	(3.9354054145918, 4.1316153537538485)

Comparing System2 with System1:

Independent replications	95% Confidence interval of EMRT System 2 - EMRT System1
5	(-0.03065538657101996, -0.04099487662789336)
10	(-0.02816111073677119, -0.0464080141510923)

Hence, System2 is better than System1.

Repeating the above comparison and increasing the number of replications, we can get better system. In this case, $T_c = 9.5$ meet expectations.