EE559

Mathematical Pattern Recognition— Homework 1

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Due: 02/05/2021

- a. For each of the two synthetic datasets
 - 1) Plot the training-set data plots, the resulting class means, decision boundaries, and decision regions.

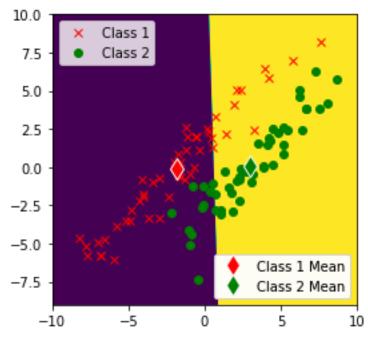
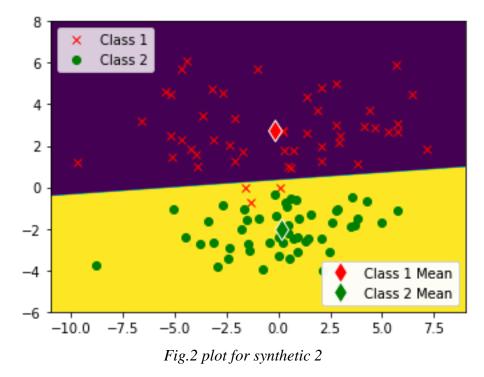


Fig.1 Plot for synthetic 1.



2) Give the classification error rate on the training set and test set.

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The error rate for training set in syn1=
0.21
The error rate for test set in syn1=
0.24
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Fig.3 results for synthetic 1

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The error rate for training set in syn2= 0.03
The error rate for test set in syn2= 0.04
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Fig.4 results for synthetic 2

b. Is there much difference in error rate between two synthetic datasets?

Yes, there is much difference.

The plot for synthetic1 shows that there are plenty of points (nearly one third) that are not classified as they are supposed to be.

But from the plot for synthetic2, it indicates that hardly had the points that are misclassified.

Maybe this classification method is quite suit for the dataset in synthetic2, and which is not the suitable method for synthetic1.

c. For the wine dataset, pick the first two features and repeat the procedure of part a.

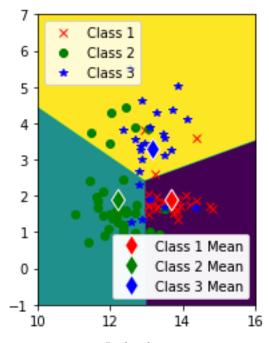


Fig.5 plot for wine

The error rate for training set in wine= 0.20224719101123595
The error rate for test set in wine= 0.2247191011235955

Fig.6 results for wine

d. Find the 2 features among 13 that achieve the minimum classification error on the training set.

Two FOR loop are used for finding the minimum classification error among 13 features (C^{13}_2 combinations).

The minimum training error rate is 0.07865168539325842 ,which appears at feature 1 and feature 12, meanwhile its testing error rate is 0.12359550561797752 The minimum testing error rate is 0.11235955056179775 ,which appears at feature 1 and feature 7, meanwhile its training error rate is 0.0898876404494382

Fig. 7 results for minimum error rate

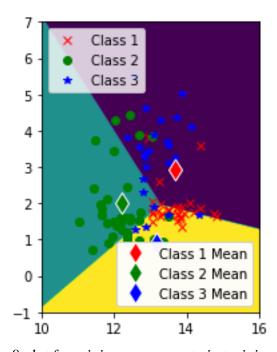


Fig.8 plot for minimum error rate in training set

The two features that could achieve the minimum classification error on the training set is feature 1 and feature 12.

e. Are there much differences in training-set error rate and testing-set error for different pairs of features?

The minimum training error rate is 0.07865168539325842 ,which appears at feature 1 and feature 12, meanwhile its testing error rate is 0.12359550561797752

The maximum training error rate is 0.5730337078651685 ,which appears at feature 2 and feature 5, meanwhile its testing error rate is 0.43820224719101125

Fig. 9 the comparison between the minimum and maximum error rate in training-set

The minimum testing error rate is 0.11235955056179775 ,which appears at feature 1 and feature 7, meanwhile its training error rate is 0.0898876404494382

The maximum testing error rate is 0.5056179775280899 ,which appears at feature 3 and feature 4, meanwhile its training error rate is 0.6067415730337079

Fig. 10 the comparison between the minimum and maximum error rate in testing-set

There are many differences for different feature pairs that can be read from the comparisons above. The training error rate is fluctuated from 0.124 to 0.438 and the testing error rate is fluctuated from 0.090 to 0.607.