

## Homework 4

0. To solve this problem, I modified the `mall` class by adding a hook before calling `_process_chunk` so that this class can record what chunks are put into this function.

When attacking, we should guess all possible key lengths, and for each guess, use length extension attack to generate new url, and see if we can get something meaningful from server by using this url, and if we do get something meaningful, that means we guessed the length right.

And, for a certain guessed key length, first use the modified `mall` class to generate `mall` hash value and get all the chunks produced, then append all the padding and length represented in bytes of the last chunk to the url (note, here if a byte can't be decoded by ascii or is an invalid char of url, we should use `%0xbyte`), finally, append the parameter string we want to url and generate new hash value according to the last hash value, the parameter string we appended, padding and total length.

1. (a) let's prove its converse proposition :

if  $H$  is not collision secure,

that is, we can find  $m_1$  and  $m_2$  such that  $H(m_1) = H(m_2)$  in reasonable time

then,  $(H_1(m_1), H_2(m_1)) = (H_1(m_2), H_2(m_2))$

then, we have  $H_1(m_1) = H_1(m_2)$  and  $H_2(m_1) = H_2(m_2)$

so if  $H$  is not collision secure, then neither  $H_1$  nor  $H_2$  is collision secure

(b) if we can find  $m_1, m_2$  such that  $H_2(m_1) = H_2(m_2)$

then  $H'(m_2) = H_1(H_2(m_2)) = H_1(H_2(m_1)) = H'(m_1)$

2.  $Enc_1$  is not safe, because attacker  $H_1$  don't have a key. Attacker can compute  $H_1(m)$  for all  $m$  and construct a table to map hash results of  $H_1$  to possible original messages, and guess what original message  $m$  is every time attacker gets a  $(e_k, h_1(m))$

$Enc_2$  does not provide authentication, because attacker can substitute  $e_k$  to  $e'_k$  and append  $H_2(e'_k)$  to it to generate a valid ciphertext. And the victim will receive some garbage if attacker randomly generates  $e'_k$