

$$Pr(u_i|\mathbf{y}) = \frac{\textcolor{red}{a}_i(u_i)g(y_i|u_i) \prod_{j \in S_i} \textcolor{blue}{p}_{ij}(u_i)}{L} \quad (1)$$

Anterior probability:

$$\begin{aligned} \textcolor{red}{a}(u_i) = & \sum_{u_m} \left\{ \textcolor{red}{a}_m(u_m)g(y_m|u_m) \prod_{k \in S_m, k \neq f} \textcolor{blue}{p}_{mk}(u_m) \right. \\ & \times \sum_{u_f} \left\{ \textcolor{red}{a}_f(u_f)g(y_f|u_f) \prod_{k \in S_f, k \neq m} \textcolor{blue}{p}_{fk}(u_f) \right. \\ & \times \textcolor{green}{tr}(u_i|u_m, u_f) \\ & \times \left. \prod_{s \in C_{mf}, s \neq i} \left[\sum_{u_s} \textcolor{green}{tr}(u_s|u_m, u_f)g(y_s|u_s) \prod_{k \in S_s} \textcolor{blue}{p}_{sk}(u_s) \right] \right\} \Big\} \end{aligned} \quad (2)$$

Posterior probability:

$$\begin{aligned} \textcolor{blue}{p}_{ij}(u_i) = & \sum_{u_j} \left\{ \textcolor{red}{a}_j(u_j)g(y_j|u_j) \prod_{k \in S_j, k \neq i} \textcolor{blue}{p}_{jk}(u_j) \right. \\ & \times \left. \prod_{o \in C_{ij}} \left[\sum_{u_o} \textcolor{green}{tr}(u_o|u_i, u_j)g(y_o|u_o) \prod_{k \in S_o} \textcolor{blue}{p}_{ok}(u_o) \right] \right\} \end{aligned} \quad (3)$$

Where:

- i : focal individual
- m, f : parents of i
- j : mate to i
- o : offspring of i
- $S_.$: Set of mates of 1 individual
- $C_{..}$: Set of offspring of 2 individuals

and

- $\textcolor{red}{a}(u_i)$ anterior probability: information from parents and full sibs
- $\textcolor{blue}{p}_{ij}(u_i)$ posterior probability: information from mates and progeny
- $g(y_i|u_i)$ penetrance value; information from self: conditional probability that i has phenotype (observed genotype) y_i given it has (actual) genotype u_i .
- $\textcolor{green}{tr}(u_i|u_m, u_f)$ Inheritance; conditional probability that i has genotype u_i , given that parents m and f have genotypes u_m and u_f .