

# Optimization for Engineers

## 2. Lab Exercise

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### Assignment 1: Conjugate Gradient Algorithm - 5 Credits

Complete the conjugate gradient algorithm in the template *conjugateGradient.m*, for solving  $Ax_s = b$

- a) Input:  $A \in \mathbb{R}^{n \times n}$ ;  $b, x_0 \in \mathbb{R}^n$ ;  $\varepsilon > 0$ .
- b) Set  $x_k \leftarrow x_0$ ,  $r_k \leftarrow Ax_k - b$  and  $d_k \leftarrow -r_k$ .
- c) While  $\|r_k\| > \varepsilon$  do
  - i) Set  $\rho_k \leftarrow d_k^\top Ad_k$ .
  - ii) Set  $t_k \leftarrow -\frac{r_k^\top d_k}{\rho_k}$ .
  - iii) Set  $x_k \leftarrow x_k + t_k d_k$ .
  - iv) Set  $r_k \leftarrow r_k + t_k Ad_k$ .
  - v) Set  $\beta_k \leftarrow \frac{r_k^\top Ad_k}{\rho_k}$ .
  - vi) Set  $d_k \leftarrow -r_k + \beta_k d_k$ .
- d) Return  $x_s \leftarrow x_k$ .

**Hint:** Use `norm(x)` for  $\|x\|$ .

Test the algorithm with the command `sheet02Script(1);`

### Assignment 2: Newton's Method - 5 Credits

Complete Newton's method in the template *newtonsMethod.m*, for minimizing  $f : \mathbb{R}^n \rightarrow \mathbb{R}$  with Hessian evaluation:

- a) Input:  $f \in \mathcal{C}^2$ ;  $x_0 \in \mathbb{R}^n$ ;  $\varepsilon > 0$ .
- b) Set  $x_k \leftarrow x_0$ .
- c) While  $\|\nabla f(x_k)\| > \varepsilon$  do:
  - i) Solve  $\nabla^2 f(x_k)d_k = -\nabla f(x_k)$  for  $d_k$  using `conjugateGradient.m`.
  - ii) If  $d_k$  is a descent direction compute  $t_k$  by calling `backtrackingLineSearch.m` for  $f$  at  $x_k$  along  $d_k$ .
  - iii) Else throw a warning, set  $d_k$  to steepest descent and use `bisectionLineSearch.m` for  $t_k$ .
  - iv) Set  $x_k \leftarrow x_k + t_k d_k$ .
- d) Return  $x_s \leftarrow x_k$ .

#### Hints:

- a) Use `getHessian(f_handle,x_k)` to get the Hessian matrix at  $x_k$ .
- b) For the `conjugateGradient` call only provide  $A$  and  $b$ .
- c) Throw a warning with `warning('yourPersonalWarningMessage');`
- d) Test the algorithm with the command `sheet02Script(2);`

### Evaluation and Upload

Hand in the following files (unzipped) to StudOn using the **Exercises** object again:

- a) `conjugateGradient.m`
- b) `newtonsMethod.m`