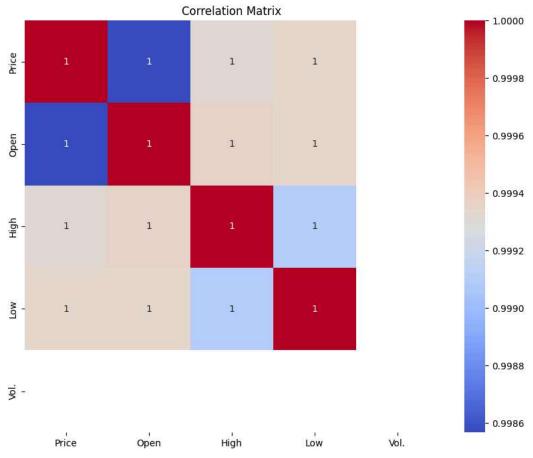
```
import pandas as pd
file_path = 'EUR_USD Historical Data.csv'
df = pd.read_csv(file_path)
print(df.head())
             Date Price Open
                                    High
                                             Low Vol. Change %
    0 28-06-2024 1.0713 1.0703 1.0726 1.0684
                                                         0.10%
                                                  NaN
    1 27-06-2024 1.0702 1.0680 1.0728 1.0677
                                                   NaN
                                                         0.22%
    2 26-06-2024 1.0679 1.0713 1.0719 1.0665
                                                   NaN
                                                         -0.32%
    3 25-06-2024 1.0713 1.0735 1.0745 1.0690
                                                        -0.18%
                                                   NaN
    4 24-06-2024 1.0732 1.0688 1.0747 1.0683
                                                   NaN
                                                         0.38%
print(df.dtypes)
df['Date'] = pd.to_datetime(df['Date'])
numerical_features = df.select_dtypes(include=['number'])
correlation_matrix = numerical_features.corr()
print(correlation_matrix)
import matplotlib.pyplot as plt
import seaborn as sns # Importing seaborn as well
# Visualize the correlation matrix
plt.figure(figsize=(10, 8))
sns.heatmap(correlation_matrix, annot=True, cmap='coolwarm')
plt.title('Correlation Matrix')
plt.show()
```

```
→ Date
                 object
    Price
                float64
    Open
                float64
    High
                float64
    Low
                float64
                float64
    Vol.
    Change %
                 object
    dtype: object
              Price
                         Open
                                  High
                                             Low
                                                  Vol.
    Price 1.000000 0.998568
                              0.999328 0.999342
                                                   NaN
    0pen
           0.998568 1.000000
                              0.999356
                                        0.999340
                                                   NaN
    High
           0.999328
                     0.999356
                               1.000000
                                        0.999088
                                                    NaN
           0.999342 0.999340
                              0.999088
                                        1.000000
                                                   NaN
    Low
    Vol.
                NaN
                         NaN
                                   NaN
                                             NaN
                                                   NaN
```

<ipython-input-38-6e97200ae6af>:5: UserWarning: Parsing dates in %d-%m-%Y format when dayfirst=False (the default) was specified. Pass `
 df['Date'] = pd.to\_datetime(df['Date'])

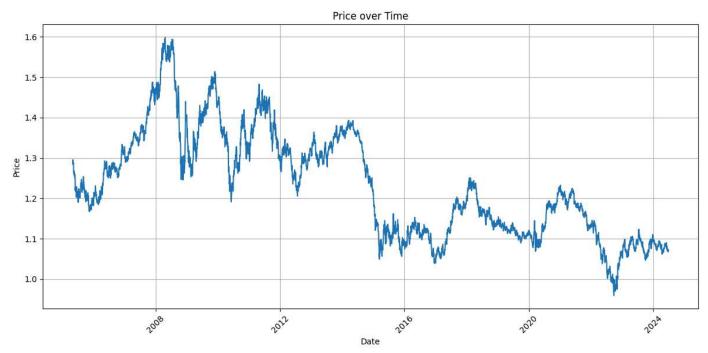


```
import matplotlib.pyplot as plt

# Assuming 'Price' is the column name containing the prices
# and 'Date' is the column name containing the dates

plt.figure(figsize=(12, 6))
plt.plot(df['Date'], df['Price'])
plt.xlabel('Date')
plt.xlabel('Date')
plt.ylabel('Price')
plt.title('Price over Time')
plt.grid(True)
plt.xticks(rotation=45)  # Rotate x-axis labels for better readability
plt.tight_layout()  # Adjust layout to prevent labels from overlapping
plt.show()
```

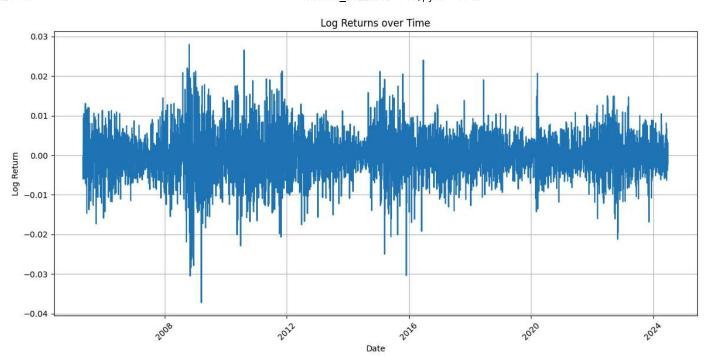




```
import pandas as pd
import matplotlib.pyplot as plt
import numpy as np

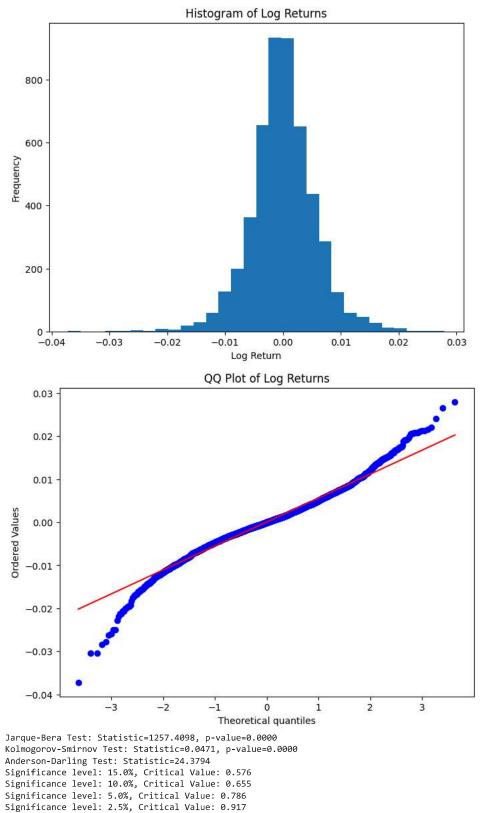
# Calculate log returns
df['Log_Return'] = np.log(df['Price'] / df['Price'].shift(1))

# Plot log returns
plt.figure(figsize=(12, 6))
plt.plot(df['Date'], df['Log_Return'])
plt.xlabel('Date')
plt.ylabel('Log Return')
plt.title('Log Returns over Time')
plt.grid(True)
plt.xticks(rotation=45)
plt.tight_layout()
plt.show()
```



```
import matplotlib.pyplot as plt
import scipy.stats as stats
import statsmodels.api as sm
df = df.dropna(subset=['Log_Return'])
plt.figure(figsize=(8, 6))
plt.hist(df['Log_Return'], bins=30)
plt.xlabel('Log Return')
plt.ylabel('Frequency')
plt.title('Histogram of Log Returns')
plt.show()
# QQ-Plot
plt.figure(figsize=(8, 6))
stats.probplot(df['Log_Return'], dist="norm", plot=plt)
plt.title('QQ Plot of Log Returns')
plt.show()
# Jarque-Bera test
jarque_bera = stats.jarque_bera(df['Log_Return'])
print(f"Jarque-Bera\ Test:\ Statistic=\{jarque\_bera[0]:.4f\},\ p-value=\{jarque\_bera[1]:.4f\}")
# Kolmogorov-Smirnov test
ks\_test = stats.kstest(df['Log\_Return'], 'norm', args=(df['Log\_Return'].mean(), df['Log\_Return'].std()))
print(f"Kolmogorov-Smirnov Test: Statistic={ks_test[0]:.4f}, p-value={ks_test[1]:.4f}")
# Anderson-Darling test
anderson_test = stats.anderson(df['Log_Return'], dist='norm')
print(f"Anderson-Darling Test: Statistic={anderson_test.statistic:.4f}")
for i in range(len(anderson_test.critical_values)):
    sl, cv = anderson_test.significance_level[i], anderson_test.critical_values[i]
    print(f"Significance level: {sl}%, Critical Value: {cv}")
```





```
import numpy as np
# Calculate historical volatility (standard deviation of log returns)
historical_volatility = np.std(df['Log_Return']) * np.sqrt(252) # Annualized volatility (252 trading days)
print(f"Historical Volatility: {historical_volatility:.4f}")
```

→ Historical Volatility: 0.0893

```
eur_3month_treasury_rate = 0.03
risk_free_rate_usd = usd_3month_treasury_rate
risk_free_rate_eur = eur_3month_treasury_rate
print(f"Risk-free rate for usd (3-month treasury rate): {risk_free_rate_usd:.4f}")
print(f"Risk-free rate for eur (3-month treasury rate): {risk_free_rate_eur:.4f}")
Risk-free rate for CAD (3-month treasury rate): 0.0200
     Risk-free rate for INR (3-month treasury rate): 0.0500
import pandas as pd
import matplotlib.pyplot as plt
\verb"import numpy as np"
import scipy.stats as stats
import statsmodels.api as sm
import seaborn as sns
file_path = 'EUR_USD Historical Data.csv'
df = pd.read_csv(file_path)
# Calculate log returns
df['Log_Return'] = np.log(df['Price'] / df['Price'].shift(1))
df = df.dropna(subset=['Log_Return'])
# Autocorrelation and Partial Autocorrelation Functions (ACF and PACF)
from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
fig, axes = plt.subplots(1, 2, figsize=(15, 5))
plot_acf(df['Log_Return'], lags=20, ax=axes[0])
axes[0].set_title('Autocorrelation Function (ACF)')
plot_pacf(df['Log_Return'], lags=20, ax=axes[1])
axes[1].set_title('Partial Autocorrelation Function (PACF)')
plt.tight_layout()
plt.show()
# Ljung-Box test for autocorrelation
from statsmodels.stats.diagnostic import acorr_ljungbox
lb_test = acorr_ljungbox(df['Log_Return'], lags=20) # Test up to 20 lags
print(lb_test)
print("\nLjung-Box Test:")
for lag, p_value in zip(lb_test.index, lb_test['lb_pvalue']):
 print(f"Lag {lag}: p-value = {p_value:.4f}")
# Interpretation of the tests
# ACF and PACF plots: Significant spikes at certain lags (outside the confidence bands) suggest autocorrelation.
# Ljung-Box test: A small p-value indicates evidence against the null hypothesis of no autocorrelation. If the p-value is less than your si
# you'd reject the null and conclude there is significant autocorrelation.
```

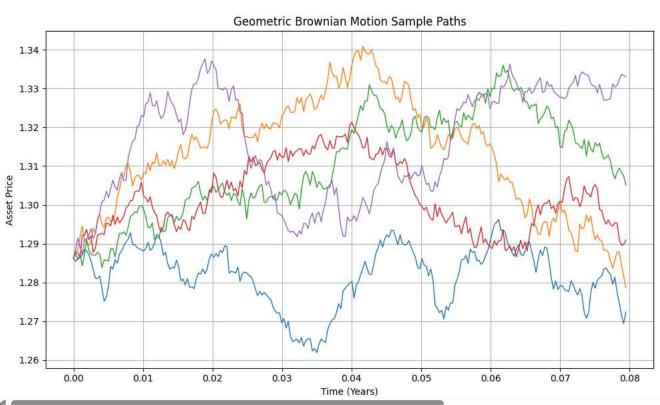
```
Jitender_2022MCB1318.ipynb - Colab
₹
                              Autocorrelation Function (ACF)
                                                                                                 Partial Autocorrelation Function (PACF)
      1.00
                                                                            1.00
                                                                            0.75
      0.75
      0.50
                                                                            0.50
      0.25
                                                                            0.25
      0.00
                                                                            0.00
     -0.25
                                                                           -0.25
     -0.50
     -0.75
                                                                           -0.75
     -1.00
                                                                           -1.00
                                                       15
                                                                                                              10
                                                                                                                            15
                                        10
                                                                    20
                                                                                                                                           20
          lb_stat lb_pvalue
          0.017290
                     0.895385
    2
         0.674072
                     0.713883
         3.366513
    3
                     0.338492
    4
         5.064462
                     0.280747
                     0.401309
         5.120860
                     0.368133
    6
         6.514020
    7
         6.660274
                     0.465088
    8
          7.612778
                     0.472179
         9.568714
                     0.386514
    10 11.302805
                     0.334418
    11
        13.464591
                     0.264047
    12 13.483688
                     0.334885
    13
       14,544356
                     0.336654
    14
        14.606254
                     0.405588
    15 14.911847
                     0.457786
    16 15.245821
                     0.506713
    17
        15.387961
                     0.567559
    18 15.497750
                     0.627554
    19
        15.834690
                     0.668278
    20 16.778227
                     0.667324
    Ljung-Box Test:
    Lag 1: p-value = 0.8954
    Lag 2: p-value = 0.7139
    Lag 3: p-value = 0.3385
    Lag 4: p-value = 0.2807
    Lag 5: p-value = 0.4013
    Lag 6: p-value = 0.3681
    Lag 7: p-value = 0.4651
    Lag 8: p-value = 0.4722
    Lag 9: p-value = 0.3865
    Lag 10: p-value = 0.3344
    Lag 11: p-value = 0.2640
    Lag 12: p-value = 0.3349
    Lag 13: p-value = 0.3367
    Lag 14: p-value = 0.4056
    Lag 15: p-value = 0.4578
    Lag 16: p-value = 0.5067
    Lag 17: p-value = 0.5676
    Lag 18: p-value = 0.6276
    Lag 19: p-value = 0.6683
    Lag 20: p-value = 0.6673
```

```
import numpy as np
# Calculate historical volatility (standard deviation of log returns)
historical_volatility = np.std(df['Log_Return']) * np.sqrt(252) # Annualized volatility (252 trading days)
print(f"Historical Volatility: {historical_volatility:.4f}")
→ Historical Volatility: 0.0893
valuation_date = date(2025, 5, 2)
maturity_date = date(2025, 5, 31)
T = (maturity_date - valuation_date).days / 365 \# \approx 0.079 years
```

```
sigma = historical_volatility # Replace with your actual volatility
n steps = 100
# ATM setup
S = df['Price'].iloc[-1] # Current spot price (ATM)
K = S # ATM Strike
r = 0.03 # Risk-free rate (annual)
import numpy as np
import matplotlib.pyplot as plt
def simulate_gbm_paths(S0, T, r, sigma, steps=252, paths=5):
    dt = T / steps
    time_grid = np.linspace(0, T, steps + 1)
    prices = np.zeros((paths, steps + 1))
    prices[:, 0] = S0
    for i in range(paths):
        for t in range(1, steps + 1):
            z = np.random.normal()
            prices[i, t] = prices[i, t-1] * np.exp((r - 0.5 * sigma**2) * dt + sigma * np.sqrt(dt) * z)
    return time_grid, prices
# Parameters
S0 = S # Spot price
num paths = 5
num_steps = 252  # Daily steps
\label{time_grid}  \mbox{ time\_grid, gbm\_paths} = \mbox{simulate\_gbm\_paths} (\mbox{S0, T, r, sigma, steps=num\_steps, paths=num\_paths}) \\
# Plot
plt.figure(figsize=(10, 6))
for i in range(num_paths):
    plt.plot(time_grid, gbm_paths[i], lw=1)
plt.title('Geometric Brownian Motion Sample Paths')
plt.xlabel('Time (Years)')
plt.ylabel('Asset Price')
plt.grid(True)
plt.tight_layout()
plt.show()
```



 $\overline{\pm}$ 



def binomial\_option\_price(S, K, T, r, sigma, n, option\_type="call", american=False):  $dt = T \ / \ n$ 

```
u = np.exp(sigma * np.sqrt(dt)) # up factor
    d = 1 / u
                                    # down factor
    p = (np.exp(r * dt) - d) / (u - d) # risk-neutral probability
    # Initialize asset prices at maturity
    asset_prices = np.array([S * (u ** j) * (d ** (n - j)) for j in range(n + 1)])
    # Option values at maturity
    if option type == "call":
       option_values = np.maximum(0, asset_prices - K)
    else:
        option values = np.maximum(0, K - asset prices)
    # Backward induction
    for i in range(n - 1, -1, -1):
        for j in range(i + 1):
            early_exercise = 0
            asset_price = S * (u ** j) * (d ** (i - j))
            if option_type == "call":
               early_exercise = max(0, asset_price - K)
            else:
                early_exercise = max(0, K - asset_price)
            option_values[j] = np.exp(-r * dt) * (p * option_values[j + 1] + (1 - p) * option_values[j])
                option_values[j] = max(option_values[j], early_exercise)
    return option_values[0]
# Binomial Model
call_binom = binomial_option_price(S, K, T, r, sigma, n_steps, option_type="call", american=False)
put_binom = binomial_option_price(S, K, T, r, sigma, n_steps, option_type="put", american=False)
# CRR Model (Reusing same from before)
call_crr = crr_option_price(S, K, T, r, sigma, n_steps, option_type="call")
put_crr = crr_option_price(S, K, T, r, sigma, n_steps, option_type="put")
print("Binomial Call Price:", call_binom)
print("Binomial Put Price:", put binom)
print("CRR Call Price:", call_crr)
print("CRR Put Price:", put_crr)
→ Binomial Call Price: 0.01445764882713232
     Binomial Put Price: 0.011395562626176367
     CRR Call Price: 0.01445764882713232
     CRR Put Price: 0.011395562626176367
import numpy as np
import pandas as pd
from scipy.stats import norm
from datetime import date
# Parameters
spot_price = 1.10 # ATM, so strike = spot
strike_price = 1.10
valuation_date = date(2025, 5, 2)
maturity_date = date(2025, 5, 31)
T = (maturity_date - valuation_date).days / 365 # ≈ 0.079
r = 0.02 # Annualized risk-free rate
# Define or load your historical volatility here
volatility = historical_volatility # Replace with your actual calculated volatility
def black_scholes_price(S, K, T, r, sigma):
    d1 = (np.log(S / K) + (r + 0.5 * sigma ** 2) * T) / (sigma * np.sqrt(T))
    d2 = d1 - sigma * np.sqrt(T)
    call = S * norm.cdf(d1) - K * np.exp(-r * T) * norm.cdf(d2)
    put = K * np.exp(-r * T) * norm.cdf(-d2) - S * norm.cdf(-d1)
    return call, put
call_bs, put_bs = black_scholes_price(spot_price, strike_price, T, r, volatility)
print("Black-Scholes Call Price:", call_bs)
```

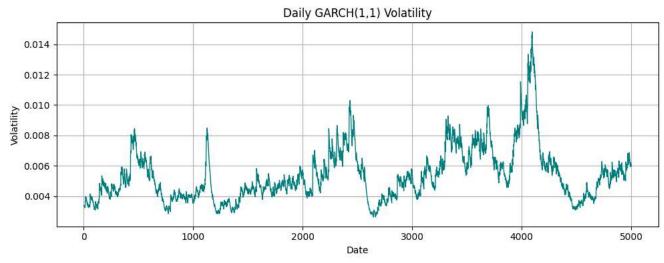
```
print("Black-Scholes Put Price:", put_bs)
→ Black-Scholes Call Price: 0.011933144504276516
     Black-Scholes Put Price: 0.01018658734186284
def crr_option_price(S, K, T, r, sigma, n, option_type="call"):
    dt = T / n
    u = np.exp(sigma * np.sqrt(dt))
    d = 1 / u
    p = (np.exp(r * dt) - d) / (u - d)
    # Stock prices at maturity
    ST = np.array([S * (u**j) * (d**(n - j)) for j in range(n + 1)])
    # Option values at maturity
    if option_type == "call":
       option_values = np.maximum(0, ST - K)
    else:
        option_values = np.maximum(0, K - ST)
    # Backward induction
    for i in range(n - 1, -1, -1):
        option values = np.exp(-r * dt) * (p * option values[1:] + (1 - p) * option values[:-1])
    return option_values[0]
steps = 100
call_crr = crr_option_price(spot_price, strike_price, T, r, volatility, steps, option_type="call")
put_crr = crr_option_price(spot_price, strike_price, T, r, volatility, steps, option_type="put")
print("CRR Call Price:", call_crr)
print("CRR Put Price:", put_crr)
Fr CRR Call Price: 0.011905529989514049
     CRR Put Price: 0.010158972827109505
def simulate_gbm(S, T, r, sigma, simulations, steps):
    dt = T / steps
    prices = np.zeros((simulations, steps + 1))
    prices[:, 0] = S
    for i in range(simulations):
        for j in range(1, steps + 1):
            z = np.random.standard normal()
            prices[i, j] = prices[i, j - 1] * np.exp((r - 0.5 * sigma **2) * dt + sigma * np.sqrt(dt) * z)
    return prices
def monte_carlo_option_price(prices, K, T, r, option_type="call"):
    if option_type == "call":
       payoffs = np.maximum(0, prices[:, -1] - K)
    else:
       payoffs = np.maximum(0, K - prices[:, -1])
    return np.exp(-r * T) * np.mean(payoffs)
simulations = 10000
steps = 252
sim_prices = simulate_gbm(spot_price, T, r, volatility, simulations, steps)
call_sim = monte_carlo_option_price(sim_prices, strike_price, T, r, "call")
put_sim = monte_carlo_option_price(sim_prices, strike_price, T, r, "put")
print("Monte Carlo Call Price:", call_sim)
print("Monte Carlo Put Price:", put_sim)
→ Monte Carlo Call Price: 0.011842481123189573
     Monte Carlo Put Price: 0.010235224744715665
comparison = pd.DataFrame({
    "Method": ["Black-Scholes", "CRR", "Simulation"],
    "Call Price": [call_bs, call_crr, call_sim],
    "Put Price": [put_bs, put_crr, put_sim]
})
```

print(comparison)

```
₹
               Method Call Price Put Price
     0 Black-Scholes
                       0.011933 0.010187
                        0.011906 0.010159
     1
                 CRR
     2
           Simulation
                        0.011842 0.010235
import numpy as np
import matplotlib.pyplot as plt
from arch import arch_model
# Assuming df['Price'] contains your price series (e.g., FX rates)
prices = df['Price']
log_ret = np.log(prices / prices.shift(1)).dropna() * 100 # log returns in percent
# GARCH(1,1) model
model = arch_model(log_ret, mean='Zero', vol='GARCH', p=1, q=1)
fitted = model.fit(disp='off')
# Summary of model fit
print(fitted.summary())
# Daily conditional volatility (converted from % to decimal)
daily_vol = fitted.conditional_volatility / 100
# Plot daily volatility
plt.figure(figsize=(10, 4))
plt.plot(daily_vol, color='teal', linewidth=1)
plt.title('Daily GARCH(1,1) Volatility')
plt.xlabel('Date')
plt.ylabel('Volatility')
plt.grid(True)
plt.tight_layout()
plt.show()
# Annualize the most recent volatility estimate
most_recent = daily_vol.iloc[-1]
annual_g_vol = most_recent * np.sqrt(252)
print(f"Most recent daily vol:
                                 {most_recent:.4%}")
print(f"Annualized GARCH(1,1) vol: {annual_g_vol:.4%}")
```

```
Zero Mean - GARCH Model Results
Den. Variable:
                     Price R-squared:
                                                  0.000
Mean Model:
                   Zero Mean
                           Adj. R-squared:
                                                  0.000
Vol Model:
                     GARCH
                          Log-Likelihood:
                                               -3739.06
Distribution:
                     Normal
                           AIC:
                                                7484.12
Method:
            Maximum Likelihood
                           BTC:
                                                7503.67
                           No. Observations:
                                                  4998
              Fri, May 02 2025
                           Df Residuals:
Date:
                                                  4998
                   11:56:47 Df Model:
Time:
                                                    0
                    Volatility Model
_____
          coef std err
                         t P>|t| 95.0% Conf. Int.
______
       1.3970e-03 4.421e-04 3.160 1.577e-03 [5.306e-04,2.263e-03]
omega
                          8.763 1.907e-18 [3.479e-02,5.484e-02]
alpha[1]
        0.0448 5.115e-03
beta[1]
          0.9514 5.130e-03
                       185.446
                                 0.000
                                        [ 0.941, 0.961]
```

Covariance estimator: robust



```
Most recent daily vol: 0.6018%
```

```
# Dates
valuation_date = date(2025, 5, 2)
maturity_date = date(2025, 5, 31)
T = (maturity_date - valuation_date).days / 365 # ≈ 0.079 years
# ATM setup
S = df['Price'].iloc[-1] # Current spot price (ATM)
K = S # ATM Strike
r = 0.03 # Risk-free rate (annual)
import numpy as np
import matplotlib.pyplot as plt
def simulate_gbm_paths(S0, T, r, sigma, steps=252, paths=5):
    dt = T / steps
    time grid = np.linspace(0, T, steps + 1)
    prices = np.zeros((paths, steps + 1))
    prices[:, 0] = S0
    for i in range(paths):
        for t in range(1, steps + 1):
            z = np.random.normal()
            prices[i, t] = prices[i, t-1] * np.exp((r - 0.5 * sigma**2) * dt + sigma * np.sqrt(dt) * z)
    return time_grid, prices
# Parameters
S0 = S # Spot price
num_paths = 5
num_steps = 252  # Daily steps
time_grid, gbm_paths = simulate_gbm_paths(S0, T, r, sigma, steps=num_steps, paths=num_paths)
```

```
# Plot
plt.figure(figsize=(10, 6))
for i in range(num_paths):
    plt.plot(time_grid, gbm_paths[i], lw=1)
plt.title('Geometric Brownian Motion Sample Paths')
plt.xlabel('Time (Years)')
plt.ylabel('Asset Price')
plt.grid(True)
plt.tight_layout()
plt.show()
```



## Geometric Brownian Motion Sample Paths 1.32 1.30 Asset Price 1.28 1.26 1.24 0.00 0.01 0.02 0.03 0.04 0.05 0.06 0.07 0.08 Time (Years)

```
def black_scholes(S, K, T, r, sigma):
   d1 = (np.log(S / K) + (r + 0.5 * sigma**2) * T) / (sigma * np.sqrt(T))
   d2 = d1 - sigma * np.sqrt(T)
   call = S * norm.cdf(d1) - K * np.exp(-r * T) * norm.cdf(d2)
   put = K * np.exp(-r * T) * norm.cdf(-d2) - S * norm.cdf(-d1)
   return call, put
call_bs, put_bs = black_scholes(S, K, T, r, sigma)
print("Black-Scholes Call Price:", call_bs)
print("Black-Scholes Put Price:", put_bs)
    Black-Scholes Call Price: 0.014490004338463147
     Black-Scholes Put Price: 0.011427918137507098
def crr_binomial(S, K, T, r, sigma, n=100):
   dt = T / n
   u = np.exp(sigma * np.sqrt(dt))
   d = 1 / u
   p = (np.exp(r * dt) - d) / (u - d)
   # Terminal payoff
   prices = np.array([S * u**j * d**(n - j) for j in range(n + 1)])
   call = np.maximum(0, prices - K)
   put = np.maximum(0, K - prices)
   # Backward induction
   for i in range(n - 1, -1, -1):
        for j in range(i + 1):
           call[j] = np.exp(-r * dt) * (p * call[j + 1] + (1 - p) * call[j])
           put[j] = np.exp(-r * dt) * (p * put[j + 1] + (1 - p) * put[j])
```

```
return call[0], put[0]
call_crr, put_crr = crr_binomial(S, K, T, r, sigma, n=100)
print("CRR Call Price:", call_crr)
print("CRR Put Price:", put_crr)
→ CRR Call Price: 0.01445764882713232
     CRR Put Price: 0.011395562626176367
def simulate_gbm(S, T, r, sigma, simulations=10000, steps=252):
    dt = T / steps
    prices = np.zeros((simulations, steps + 1))
    prices[:, 0] = S
    for i in range(simulations):
        for j in range(1, steps + 1):
           z = np.random.standard_normal()
           prices[i, j] = prices[i, j - 1] * np.exp((r - 0.5 * sigma**2) * dt + sigma * np.sqrt(dt) * z)
    return prices
def monte_carlo_option(prices, K, T, r):
    call_payoffs = np.maximum(prices[:, -1] - K, 0)
    put_payoffs = np.maximum(K - prices[:, -1], 0)
    call = np.exp(-r * T) * np.mean(call_payoffs)
    put = np.exp(-r * T) * np.mean(put_payoffs)
    return call, put
sim_prices = simulate_gbm(S, T, r, sigma)
call_mc, put_mc = monte_carlo_option(sim_prices, K, T, r)
print("Monte Carlo Call Price:", call_mc)
print("Monte Carlo Put Price:", put_mc)
→ Monte Carlo Call Price: 0.014673166001064783
     Monte Carlo Put Price: 0.011335983974096006
import matplotlib.pyplot as plt
models = ["Black-Scholes", "CRR Binomial", "Monte Carlo"]
call_prices = [call_bs, call_crr, call_mc]
put_prices = [put_bs, put_crr, put_mc]
# Create DataFrame
results = pd.DataFrame({
    'Model': models,
    'Call Price': call_prices,
    'Put Price': put_prices
})
print(results)
# Plot
x = np.arange(len(models))
width = 0.35
fig, ax = plt.subplots(figsize=(10, 6))
bar1 = ax.bar(x - width/2, call_prices, width, label='Call Price', color='lightblue')
bar2 = ax.bar(x + width/2, put_prices, width, label='Put Price', color='salmon')
ax.set_ylabel('Option Price')
ax.set_title('ATM European Option Prices Using GARCH(1,1) Volatility')
ax.set_xticks(x)
ax.set_xticklabels(models)
ax.legend()
# Add labels
for bar in bar1 + bar2:
    height = bar.get_height()
    ax.annotate(f'{height:.4f}', xy=(bar.get x() + bar.get width() / 2, height),
                xytext=(0, 3), textcoords="offset points", ha='center', fontsize=8)
plt.tight_layout()
plt.show()
```

Model Call Price Put Price
0 Black-Scholes 0.014490 0.011428
1 CRR Binomial 0.014458 0.011396
2 Monte Carlo 0.014673 0.011336

## ATM European Option Prices Using GARCH(1,1) Volatility

