

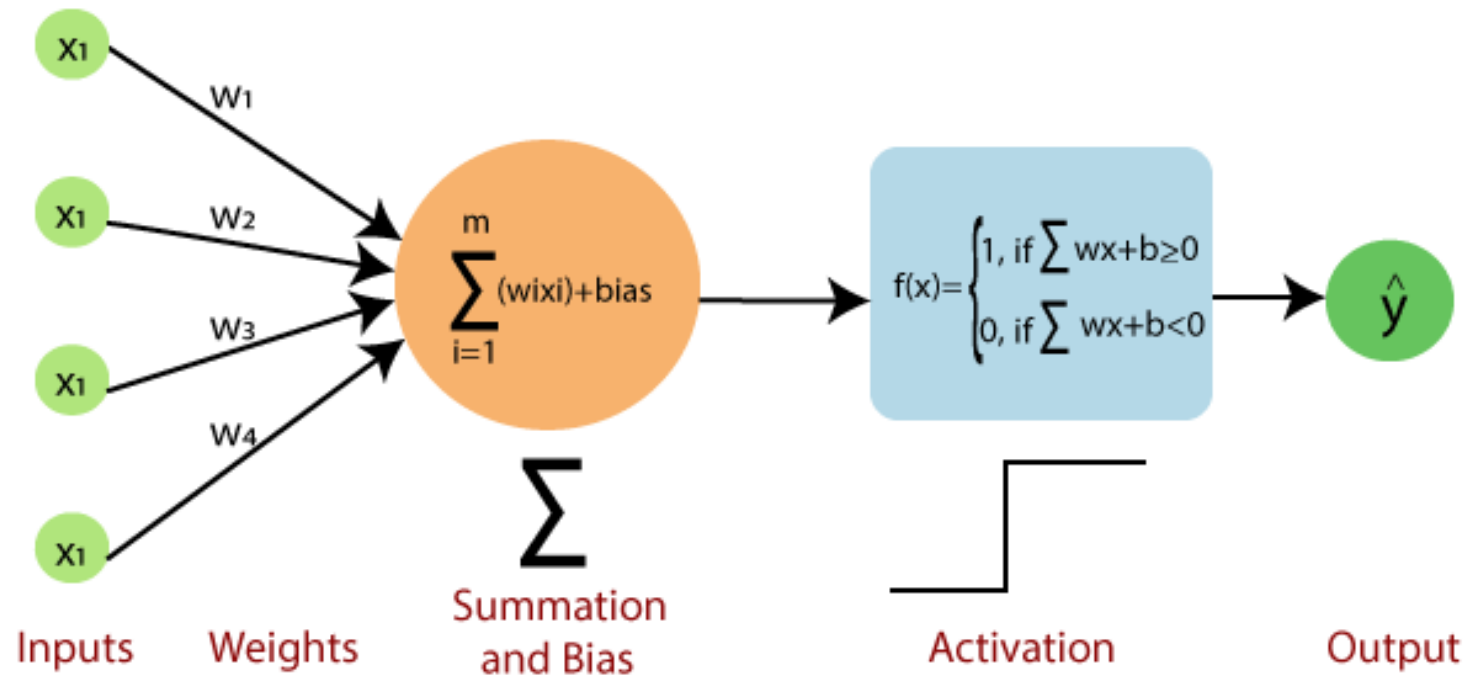
Deep Learning : Perceptron



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Perceptron



MP- Neuron (Recap)



$\{0, 1\}$



Boolean inputs



$$loss = \sum_i (y_i - \hat{y}_i)^2$$



Classification



Boolean output



Brute force



Only one parameter, b



Linear



$$Accuracy = \frac{\text{Number of correct predictions}}{\text{Total number of predictions}}$$

Perceptron



$\{0, 1\}$

😊 Real inputs



Classification

😞 Boolean output



😊 Weights for every input

😞 Linear



$$\text{loss} = \sum_i (y_i - \hat{y}_i)^2$$

😞 $\text{loss} = \sum_i \max(0, 1 - y_i * \hat{y}_i)$



😊 Our 1st learning algorithm



$$\text{Accuracy} = \frac{\text{Number of correct predictions}}{\text{Total number of predictions}}$$

Data (Real Inputs)

									
Launch (within 6 months)	0	1	1	0	0	1	0	1	1
Weight (g)	151	180	160	205	162	182	138	185	170
Screen size (inches)	5.8	6.18	5.84	6.2	5.9	6.26	4.7	6.41	5.5
dual sim	1	1	0	0	0	1	0	1	0
Internal memory (≥ 64 GB, 4GB RAM)	1	1	1	1	1	1	1	1	1
NFC	0	1	1	0	1	0	1	1	1
Radio	1	0	0	1	1	1	0	0	0
Battery(mAh)	3060	3500	3060	5000	3000	4000	1960	3700	3260
Price (INR)	15k	32k	25k	18k	14k	12k	35k	42k	44k
Like (y)	1	0	1	0	1	1	0	1	0

Each Feature will have different ranges.

Data Preparation: Standardize the input

Feature Scaling

- Normalization
- Standardization

Normalization & Standardization

- **Normalization** or **Min-Max Scaling** is used to transform features to be on a similar scale.
- It transforms data to fit within a specific range, typically `[0, 1]` or sometimes `[-1, 1]`. The formula for normalization is:

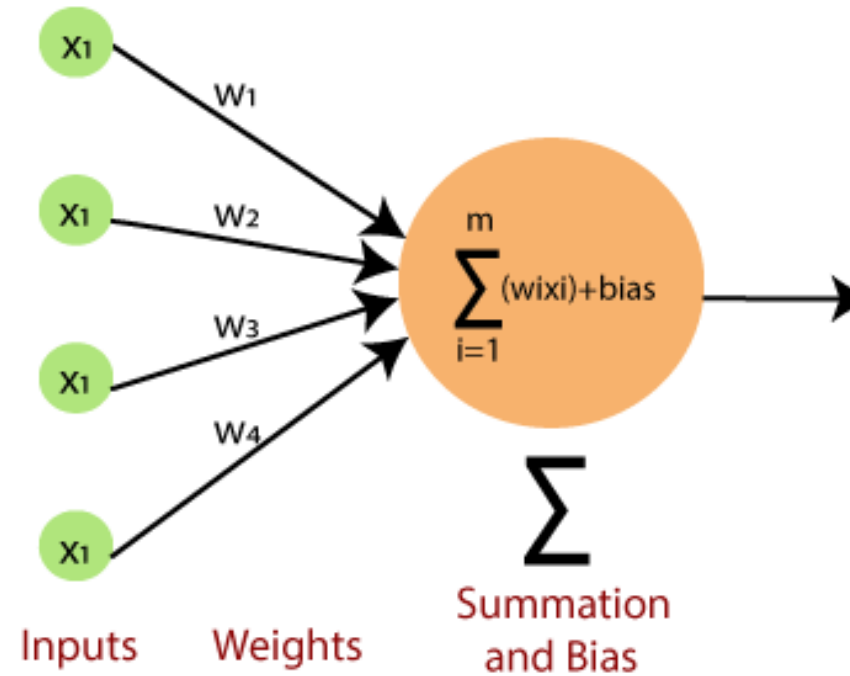
$$X_{\text{new}} = (X - X_{\text{min}}) / (X_{\text{max}} - X_{\text{min}})$$

- **Standardization** can be helpful in cases where the data follows a Gaussian distribution. However, this does not have to be necessarily true. Geometrically speaking, it translates the data to the mean vector of original data to the origin and squishes or expands the points if std is 1 respectively.

$$\text{New value} = (x - \mu) / \sigma$$

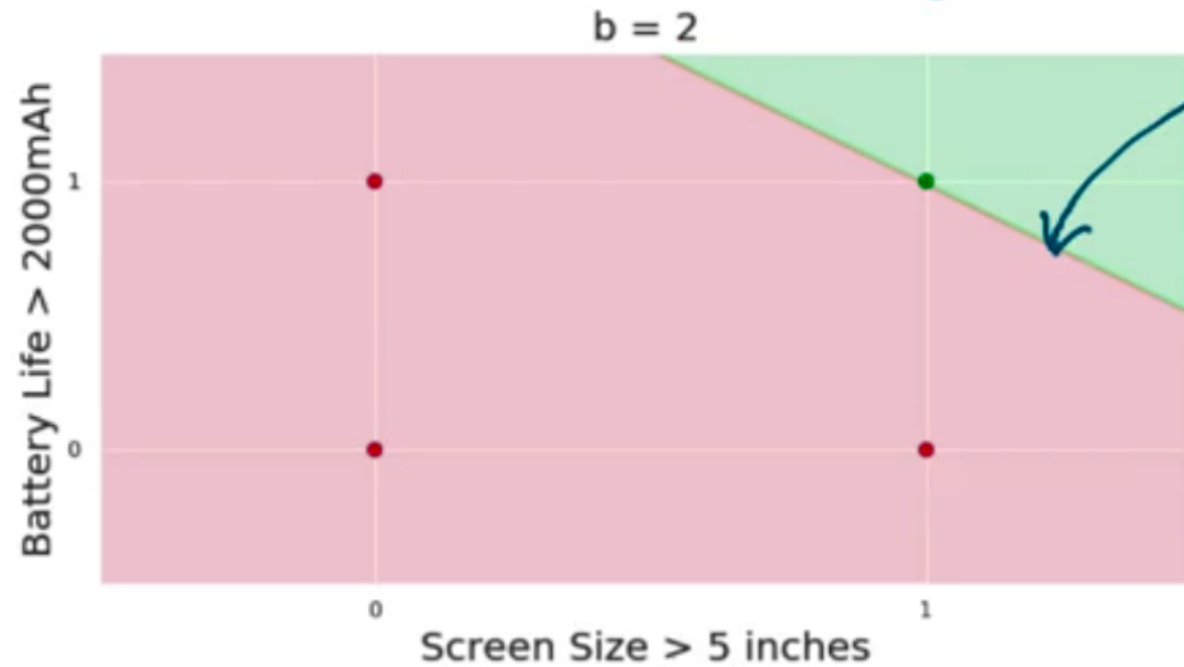
(This is also termed as **Z-Score Normalization**)

Model (Binary Classification Task)

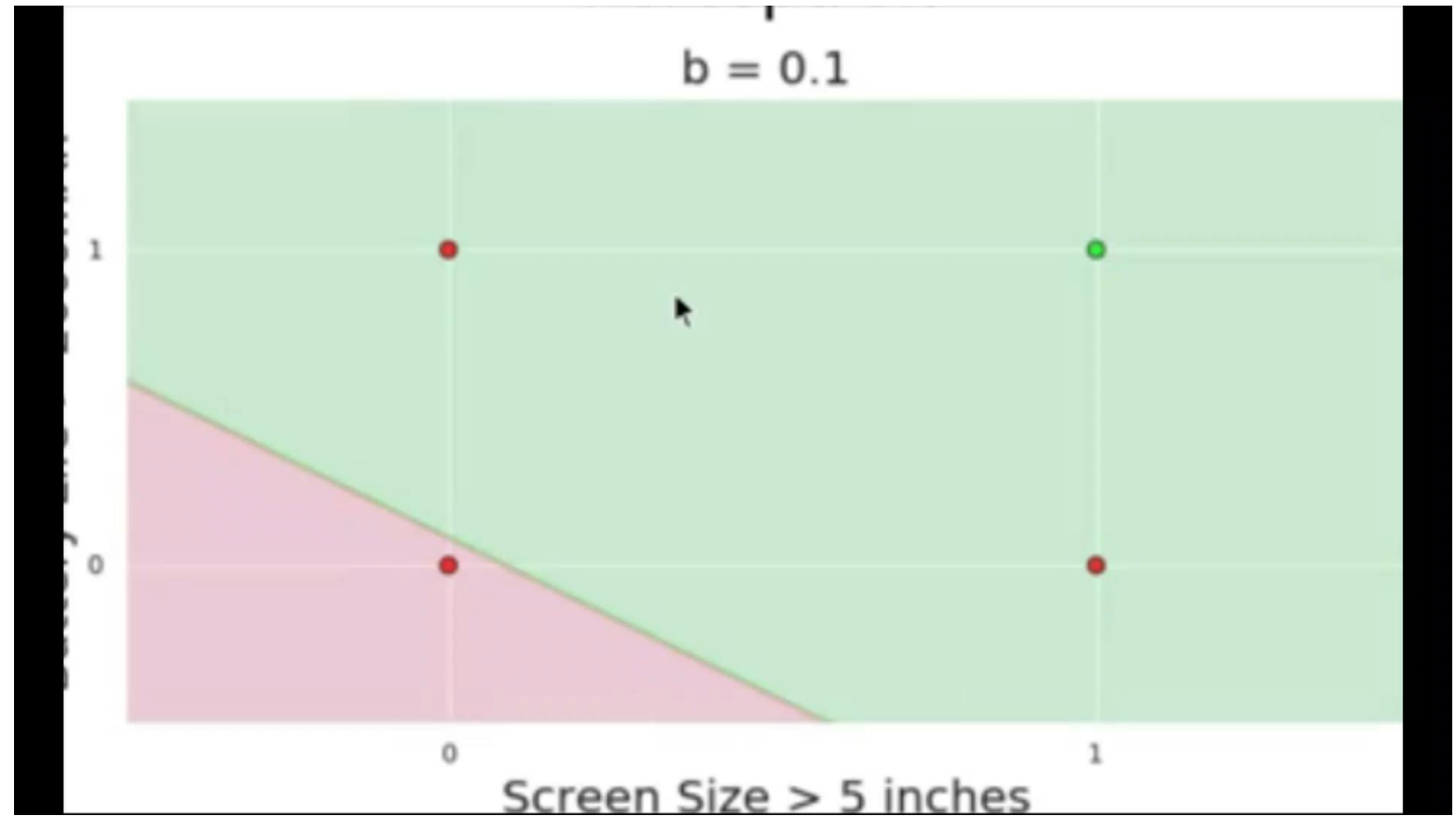


Why do we need weights?

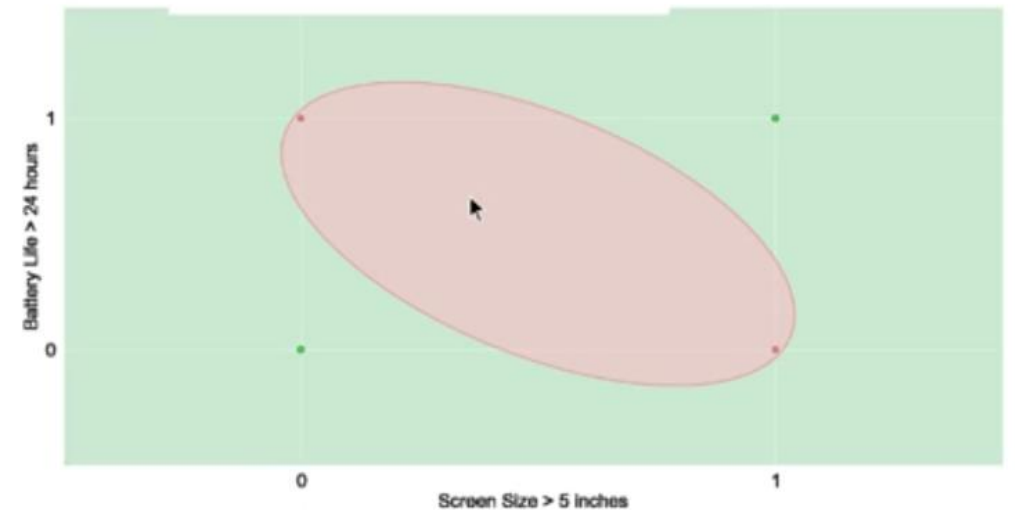
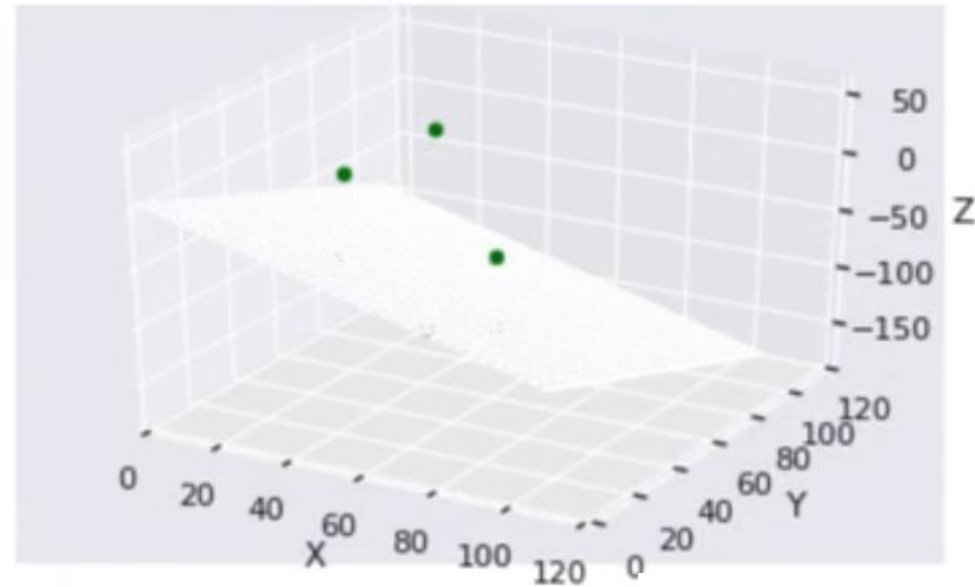
Geometric Representation of MP-Neuron



Geometric Representation of Perceptron



Do we need
more freedom
for modelling
the input?



☹️ We want even more freedom

Loss Function

i.) Perceptron Loss

ii.) Squared Error Loss

Weight	Screen Size	Like (y)	\hat{y}	Perceptron Loss	Squared Error Loss
0.19	0.64	1	1	0	0
0.63	0.87	1	0	1	1
0.33	0.67	0	1	1	1
1	0.88	0	0	0	0

$$L = 0, \text{ if } y = \hat{y} \\ = 1, \text{ otherwise}$$

When Output is Boolean; squared error loss is same as perceptron loss.

$$L = \mathbf{1}_{(y \neq \hat{y})}$$

$$\text{Squared Error loss} = (y - \hat{y})^2$$