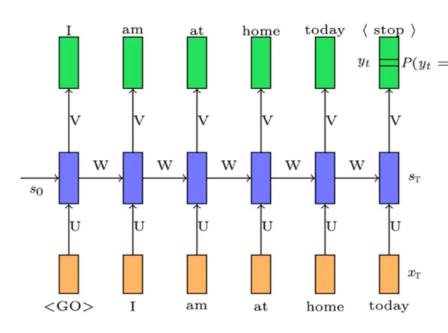




#### **Course Instructor:**

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• We are interested in

$$P(y_t = j | y_1^{t-1})$$
  $P(y_t = j | y_1, y_2...y_{t-1})$ 

where  $j \in V$  and V is the set of all vocabulary words

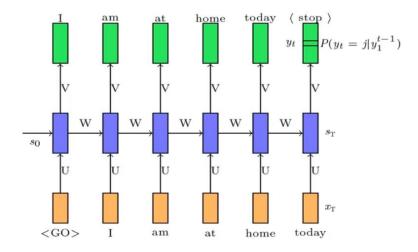
• Using an RNN we compute this as

$$P(y_t = j | y_1^{t-1}) = softmax(Vs_t + c)_j$$

• In other words we compute

$$P(y_t = j|y_1^{t-1}) = P(y_t = j|s_t)$$
  
=  $softmax(Vs_t + c)_j$ 

### Language Modelling



Data:

India, officially the Republic of India, is a country in South Asia. It is the seventh-largest country by area, .....

- Data: All sentences from any large corpus (say wikipedia)
- Model:

$$s_t = \sigma(Ws_{t-1} + Ux_t + b)$$

$$P(y_t = j|y_1^{t-1}) = softmax(Vs_t + c)_j$$

- Parameters: U, V, W, b, c
- Loss:

$$\mathcal{L}(\theta) = \sum_{t=1}^{T} \mathcal{L}_t(\theta)$$
$$\mathcal{L}_t(\theta) = -\log P(y_t = \ell_t | y_1^{t-1})$$

### Encoder Decoder Model

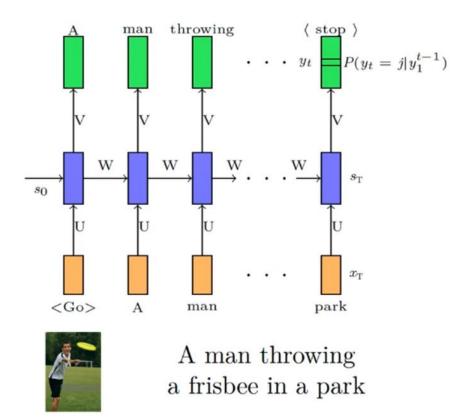
$$s_{t} = \sigma(U x_{t} + W s_{t-1} + b) \qquad \tilde{s}_{t} = \sigma(W(o_{t} \odot s_{t-1}) + U x_{t} + b) \qquad \tilde{s}_{t} = \sigma(W h_{t-1} + U x_{t} + b)$$

$$s_{t} = i_{t} \odot s_{t-1} + (1 - i_{t}) \odot \tilde{s}_{t} \qquad s_{t} = f_{t} \odot s_{t-1} + i_{t} \odot \tilde{s}_{t}$$

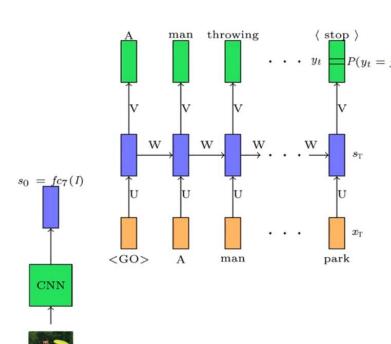
$$h_{t} = o_{t} \odot \sigma(s_{t})$$

$$s_t = \text{RNN}(s_{t-1}, x_t)$$
  $s_t = \text{GRU}(s_{t-1}, x_t)$   $h_t, s_t = \text{LSTM}(h_{t-1}, s_{t-1}, x_t)$ 

### Compact way of writing functions computed using RNNs, GRU and LSTM

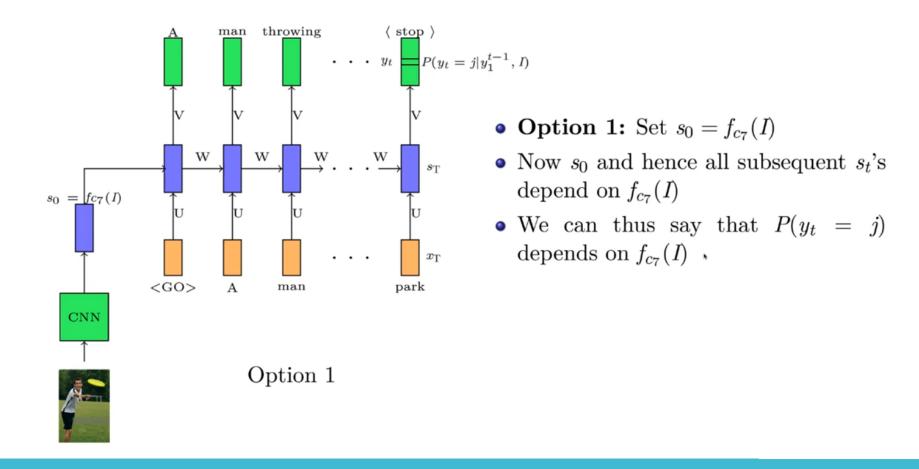


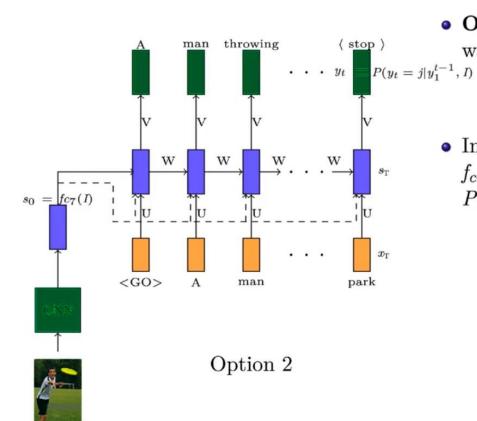
- So far we have seen how to model the conditional probability distribution  $P(y_t|y_1^{t-1})$
- More informally, we have seen how to generate a sentence given previous words
- What if we want to generate a sentence given an image?
- We are now interested in  $P(y_t|y_1^{t-1}, I)$  instead of  $P(y_t|y_1^{t-1})$  where I is an image
- Notice that  $P(y_t|y_1^{t-1}, I)$  is again a conditional distribution



• Earlier we modeled  $P(y_t|y_1^{t-1})$  as

- $P(y_t = j | y_1^{t-1}, I)$   $P(y_t | y_1^{t-1}) = P(y_t = j | s_t)$ 
  - Where  $s_t$  was a state capturing all the previous words
  - We could now model  $P(y_t = j | y_1^{t-1}, I)$  as  $P(y_t = j | s_t, f_{c_7}(I))$
  - where  $fc_7(I)$  is the representation obtained from the  $fc_7$  layer of an image

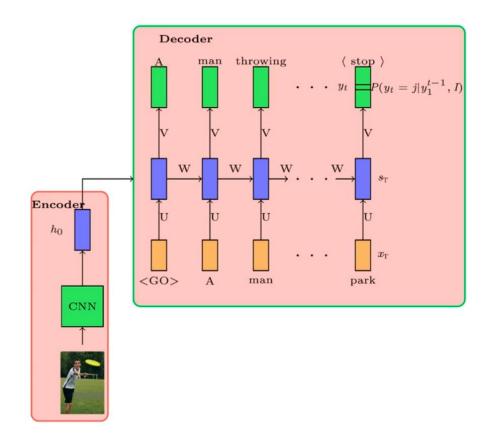




• Option 2: Another more explicit way of doing this is to compute

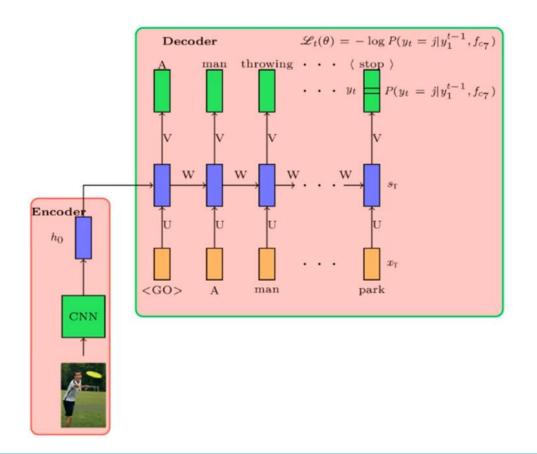
$$s_t = RNN(s_{t-1}, [x_t, f_{c_7}(I))]$$

• In other words we are explicitly using  $f_{c_7}(I)$  to compute  $s_t$  and hence  $P(y_t = j)$ 



- A CNN is first used to **encode** the image
- A RNN is then used to decode (generate) a sentence from the encoding
- This is a typical **encoder** decoder architecture
- Both the encoder and decoder use a neural network
- Alternatively, the encoder's output can be fed to every step of the decoder

#### Encoder – Decoder Architecture



• Task: Image captioning

• Data:  $\{x_i = image_i, y_i = caption_i\}_{i=1}^N$ 

• Model:

• Encoder:

$$s_0 = CNN(x_i)$$

• Decoder:

$$s_t = RNN(s_{t-1}, e(\hat{y}_{t-1}))$$
$$P(y_t|y_1^{t-1}, I) = softmax(Vs_t + b)$$

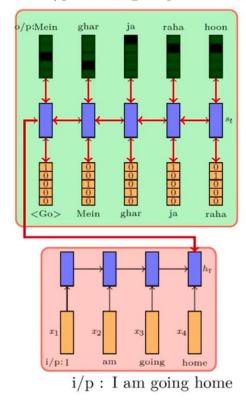
- Parameters:  $U_{dec}$ , V,  $W_{dec}$ ,  $W_{conv}$ , b
- Loss:

$$\mathscr{L}( heta) = \sum_{i=1}^T \mathscr{L}_t( heta) \quad = -\sum_{t=1}^T \log P(y_t = \ell_t | y_1^{t-1}, I)$$

• Algorithm: Gradient descent with backpropagation

### Encoder – Decoder Architecture

o/p: Mein ghar ja raha hoon



• Task: Image captioning

• Data:  $\{x_i = image_i, y_i = caption_i\}_{i=1}^N$ 

• Model:

• Encoder:

$$s_0 = CNN(x_i)$$

• Decoder:

$$s_t = RNN(s_{t-1}, e(\hat{y}_{t-1}))$$
$$P(y_t|y_1^{t-1}, I) = softmax(Vs_t + b)$$

• Parameters:  $U_{dec}$ , V,  $W_{dec}$ ,  $W_{conv}$ , b

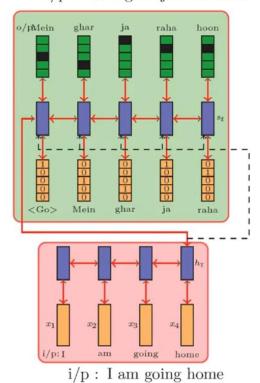
Loss:

$$\mathscr{L}(\theta) = \sum_{i=1}^{T} \mathscr{L}_t(\theta) = -\sum_{t=1}^{T} \log P(y_t = \ell_t | y_1^{t-1}, I)$$

• Algorithm: Gradient descent with backpropagation

## Encoder – Decoder Architecture – Option 1 (Machine Translation)

o/p: Mein ghar ja raha hoon



• Task: Machine translation

• Data:  $\{x_i = source_i, y_i = target_i\}_{i=1}^N$ 

• Model (Option 2):

• Encoder:

$$h_t = RNN(h_{t-1}, x_{it})$$

• Decoder:

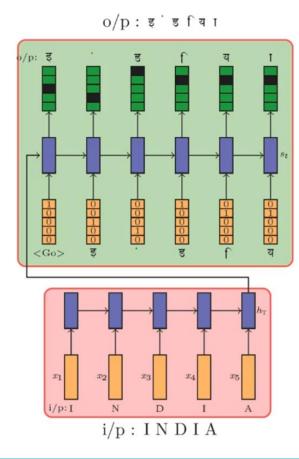
$$s_0 = h_T \quad (T \text{ is length of input})$$
 
$$s_t = RNN(s_{t-1}, [h_T, e(\hat{y}_{t-1})])$$
 
$$P(y_t|y_1^{t-1}, x) = softmax(Vs_t + b)$$

- Parameters:  $U_{dec}$ , V,  $W_{dec}$ ,  $U_{enc}$ ,  $W_{enc}$ , b
- Loss:

$$\mathscr{L}(\theta) = \sum_{i=1}^{T} \mathscr{L}_{t}(\theta) = -\sum_{t=1}^{T} \log P(y_{t} = \ell_{t} | y_{1}^{t-1}, x)$$

• Algorithm: Gradient descent with backpropagation

## Encoder – Decoder Architecture – Option 2 (Machine Translation)



- Task: Transliteration
- Data:  $\{x_i = srcword_i, y_i = tgtword_i\}_{i=1}^N$
- Model (Option 1):
  - Encoder:

$$h_t = RNN(h_{t-1}, x_{it})$$

• Decoder:

$$s_0 = h_T \quad (T \text{ is length of input})$$

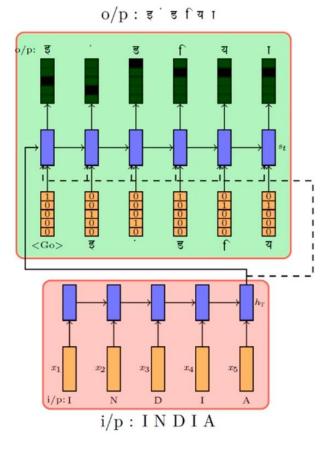
$$s_t = RNN(s_{t-1}, e(\hat{y}_{t-1}))$$

$$P(y_t|y_1^{t-1}, x) = softmax(Vs_t + b)$$

- Parameters:  $U_{dec}$ , V,  $W_{dec}$ ,  $U_{enc}$ ,  $W_{enc}$ , b
- Loss:

$$\mathcal{L}(\theta) = \sum_{i=1}^{T} \mathcal{L}_{t}(\theta) = -\sum_{t=1}^{T} \log P(y_{t} = \ell_{t} | y_{1}^{t-1}, x)$$

## Encoder – Decoder Architecture – Option 1 (Transliteration)



- Task: Transliteration
- Data:  $\{x_i = srcword_i, y_i = tgtword_i\}_{i=1}^N$
- Model (Option 2):
  - Encoder:

$$h_t = RNN(h_{t-1}, x_{it})$$

• Decoder:

$$s_0 = h_T \quad (T \text{ is length of input})$$

$$s_t = RNN(s_{t-1}, [e(\hat{y}_{t-1}), h_T])$$

$$P(y_t|y_1^{t-1}, x) = softmax(Vs_t + b)$$

- Parameters:  $U_{dec}$ , V,  $W_{dec}$ ,  $U_{enc}$ ,  $W_{enc}$ , b
- Loss:

$$\mathscr{L}(\theta) = \sum_{i=1}^{T} \mathscr{L}_t(\theta) = -\sum_{t=1}^{T} \log P(y_t = \ell_t | y_1^{t-1}, x)$$

• Algorithm: Gradient descent with backpropagation

# Encoder – Decoder Architecture – Option 2 (Transliteration)