

**You are all very smart** - being able to solve all lab problems. Here are some challenges from TAs. **Solve them to get more credits.**

**Problem 1 (Medium - 1 credit):**

Design an recursive algorithm to calculate Fibonacci numbers that takes only  $O(n)$  (Instead of exponential time as being proved in our class).

(Hint: Using memoization)

**Problem 2 (Medium - 1 credit):**

Design an iterative algorithm to calculate Fibonacci numbers that takes  $O(n)$  time, and  $O(1)$  space complexity. Use it to calculate the 10,000,000 Fibonacci number. If the result is too large, give it in modulo of 1,000,000,007.

**Problem 3 (Hard - 1 credit):**

Design an  $O(\log n)$  algorithm to calculate Fibonacci numbers.