

Q. 2. Soln

From the pseudo code, we can say that there are two for loops that determine the running time of the algorithm. The first outer loop runs for n times and the inner loop runs for the W times. And, also it is the every case scenario, so has tight bound. Thus, the knapsack problem solution with dynamic programming gives us $\Theta(nW)$ running time complexity.

Q. 3. Soln

The knapsack problem can be solved in brute-force way by using some recursive strategy. In a naïve approach, the solution would look like -

$\text{maxVal} \leftarrow 0$

Algorithm $\text{KPSolution}(n, \text{currWeight}, \text{currVal})$

if $n \neq 0$ and $\text{currWeight} \leq W$ and $\text{currVal} > \text{maxVal}$
 $\text{maxVal} \leftarrow \text{currVal}$

if $n = 0$ return

$\text{KPSolution}(n-1, \text{currWeight}, \text{currVal})$

$\text{KPSolution}(n-1, \text{currWeight} + w[n], \text{currVal} + v[n])$

As, there are two recursive calls it has obviously $O(2^n)$ time complexity. So, DP has reduced the exponential time complexity to pseudo-polynomial time.