Theory and Practice of Algorithms Final Programming Assignment - Fall 2023 Due Dec 15 - 60 points

Remember at the start of the semester, you learned about NFAs and DFAs---as you saw in lecture 20 these are graphs, so now that you know about graphs, you can apply your knowledge of graph algorithms to solve problems on regular languages! We are going to solve one particular problem: are two regular expressions equivalent (do they accept the same set of strings) which turns out to combine several graph problems! We have broken this problem down into 3 steps. In each step you solve a different graph problem, and all of them together give you a program which tests two regular expressions for equality. Note that we **strongly** recommend that you test your code extensively in between in each step! We have given you code to help you with the testing.

1. Convert Regex, and Regex, to NFA, and NFA,

We have provided you code to parse regular expressions (parse re), which takes a regular expression string, and returns a Regex object. In regex.py you have classes Regex, ConcatRegex, StarRegex, OrRegex, SymRegex, and EpsilonRegex that build up a tree. Note that we picked & as a symbol for epsilon. To transform Regex to NFA you are going to recurse over this tree and build a graph (We have added a method called transformToNFA to all the classes in regex.py that you need to implement). transformToNFA should create a new object and return it. The ones that recurse will recurse on their children, then modify one of the returned results to return it. You should also complete the NFA class in nfa.py. NFA has three fields, states, is accepting and alphabet. State in state.py has two fields, id and transitions. We assume that NFA state ids always start from 0. The methods that you need to implement in nfa.py are addTransition, addStateFrom, and epsilonClose. You need addTransition, and addStateFrom for the transformation of ConcatRegex, and OrRegex to NFA. addTransition should add a transition from one state of the NFA to the other input state of the NFA. addStateFrom should add all the states from another NFA, and return a mapping of (state number in old NFA \rightarrow state number in this NFA) as a dictionary.

Write the method isStringInLanguage in NFA class. This method takes a string as input and returns True if the string is in the language of this NFA.

The order we recommend you implementing and testing is as follow:

a. Implement isStringInLanguage.

- b. Implement transformToNFA in EpsilonRegex and test it using testNFA('&','', True), etc.
- c. Implement transformToNFA in SymRegex and test it using testNFA.
- d. Implement transformToNFA in ConcatRegex which you need to also implement addTransition and addStateFrom and then test it using testNFA.
- e. Implement transformToNFA in StarRegex and test it.
- f. Implement transformToNFA in OrRegex and test it.
- g. Test on regular expressions that have the mixture of all subclasses of regex.
- 2. Next, we want to compute two NFAs: NFA₁ NFA₂ and NFA₂ NFA₁. If both of these are empty, the NFAs are equivalent. If either accepts any string, that string shows the difference between the two. We can compute NFA₁ NFA₂ and NFA₂ NFA₁ by

NFA1 U NFA2 and NFA1 U NFA2. Doing so requires conversion of the NFA to a DFA,

which is another graph algorithm. You use BFS for this conversion. As said in class you can change the goal of BFS according to the problem that you are using it for. You need to implement the nfaToDFA function in main.py.

You can review the NFA to DFA conversion algorithm in the book. Part of the algorithm is that you need to compute <u>epsilon closure</u> of a state which is <u>a set of states which are reachable from this state on epsilon transitions</u>. So you need to <u>implement the method</u> <u>epsilonClose in nfa.py</u>. It takes a state and returns the epsilon closure of it.

After you have the DFA you need to stop and test your conversion. So you need to implement the isStringInLanguage function in dfa.py and then from main in main.py call the function testDFA to test the correctness of your DFA (similar to the test that you did for NFAs). After you know that your NFA to DFA conversion is correct you can compute the complement of the DFA. You should complete the method called complement in your DFA class (dfa.py).

Test your complement functions. You can use testDFA again but this time pass the complemented DFA as input. After your complement function passes your tests then you can proceed.

Remember, it is easier to complement a DFA and it is easier to union two NFAs. So now that we can compute the complement of DFA₁ and DFA₂, we need to convert the complements to NFAs to do the union. Then convert the resulting NFA to DFA and complement it.

After every conversion you need to test the returned NFA or DFA.

3. As you saw in lecture 20, we can run BFS algorithm to find if any string is accepted by DFA. Here if any string is accepted by either $\overline{NFA1} \cup NFA2$ or $\overline{NFA1} \cup \overline{NFA2}$ (the results of the previous step) then it means that Regex₁ and Regex₂ are not equivalent. The last step to solve the regex equivalence problem is to implement the BFS algorithm to find out if any string is accepted.

You should implement shortestString in dfa.py. This function runs BFS on this DFA and returns the shortest string accepted by it. You can use isStringInLanguage function to double check if the returned string is in the language of the first regex or the second regex.

You should also complete the function equivalent in main.py. equivalent function gets two RegExes and then returns a boolean value; True if the two RegExes are equivalent and False if they are not. You need to call the functions that you implemented before such as transformToNFA, nfaToDFA, dfaToNFA, complement, union, shortestString.

On submission:

Submit all, and only the .py files provided in the starter kit. When submitting to gradescope, make sure the file names are not changed.

Names of functions and methods that are already in the <code>.py</code> files should not be changed. You could add new functions and methods as you please, but keep them in the given files.

Bonus/Hint (20 points):

In nfa.py you can find problematic method. This is, as the name suggests, a problematic implementation of isStringInLanguage method. You can get bonus points if:

- 1. You point out why the implementation is broken;
- You give an example of a type of languages that could cause the method to misbehave.