

# CSC 212: Data Structures and Abstractions

## Basic Sorting Algorithms

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# Announcements

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- Programming #2
  - ✓ posted
  - ✓ Gradescope active
  - ✓ focus on classes and dynamic arrays (`std::vector`)
- If programming is still a **significant** issue ...
  - ✓ consider taking this class next semester and focus on addressing the issue

# Looking for internships / jobs?

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<https://careers.google.com/how-we-hire/interview/>

[https://www.amazon.jobs/en/landing\\_pages/software-development-topics](https://www.amazon.jobs/en/landing_pages/software-development-topics)

<https://www.facebook.com/careers/life/preparing-for-your-software-engineering-interview-at-facebook/>

Worst-case, Average-case,  
Best-case

# Warming up: Analyze this code

```
unsigned int argmin(const std::vector<int> &values) {  
    unsigned int length = values.size();  
    assert(length > 0);  
    unsigned int idx = 0;  
    int current = values[0];  
    for (unsigned int i = 1 ; i < length ; i ++) {  
        if (values[i] < current) {  
            current = values[i];  
            idx = i;  
        }  
    }  
    return idx;  
}
```

$T(n) = ?$   
based on number of comparisons

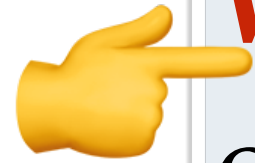
# Warming up: Analyze this code

```
bool argk(const std::vector<int> &values, int k, unsigned int &idx) {  
    unsigned int length = values.size();  
    for (unsigned int i = 0 ; i < length ; i ++ ) {  
        if (values[i] == k) {  
            idx = i;  
            return true;  
        }  
    }  
    return false;  
}
```

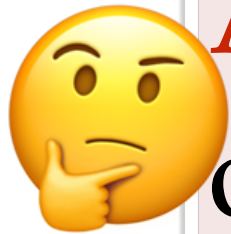
$T(n) = ?$   
based on number of comparisons

# Different types of analysis

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**Worst-case:** maximum time of algorithm on any input



**Average-case:** expected time of algorithm over all inputs



**Best-case:** minimum time of algorithm on some (optimal) input

# Different types of analysis

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- While **asymptotic analysis** describes  $T(n)$  as  $n$  approaches infinity ...
  - ✓ asymptotic notation: big O, big Omega, big Theta
- **Case analysis** looks into the different input types
  - ✓ best-case, worst-case, average-case

Both analysis types are orthogonal  
to each other



# Worst-case, Average-case, Best-case

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- Ex: factorial of a number (iterative algorithm)
- Ex: sequential search (return first occurrence)
- Ex: sequential search (return last occurrence)

# Basic Sorting Algorithms

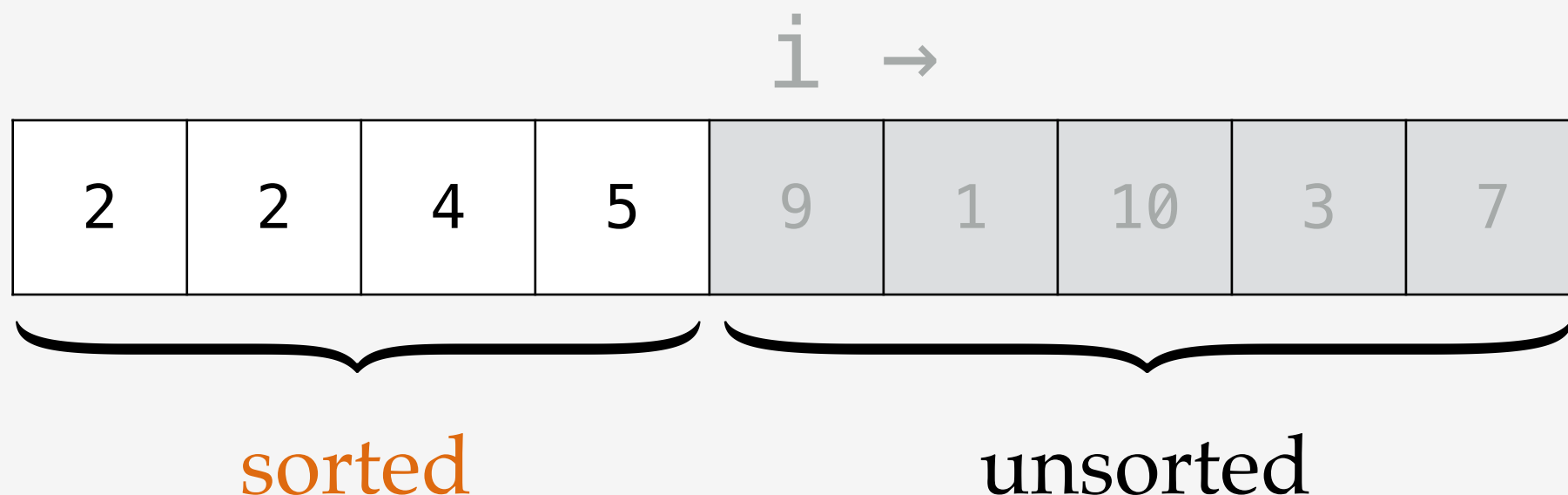
# Sorting

- Given **n** elements that can be compared according to a **total order** relation
  - ✓ we want to rearrange them in non-increasing / non-decreasing order
  - ✓ for example (non-decreasing):
    - **input:** sequence of items  $A = [k_0, k_1, \dots, k_{n-1}]$
    - **output:** permutation of A  $B \mid B[0] \leq B[1] \leq \dots B[n-1]$

Central problem in computer science

# Insertion Sort

- Array is divided into **sorted** and **unsorted** parts
  - ✓ algorithm scans array from **left to right**
- Invariants
  - ✓ elements in **sorted** are in ascending order
  - ✓ elements in **unsorted** have not been seen



# Insertion Sort Demo

```

void insertionsort(int *A, unsigned int n) {
    int temp;
    unsigned int i, j;
    // grows the left part (sorted)
    for (i = 0 ; i < n ; i++) {
        // inserts A[j] in sorted part
        for (j = i ; j > 0 ; j--) {
            if (A[j] < A[j-1]) {
                temp = A[j];
                A[j] = A[j-1];
                A[j-1] = temp;
            }
            else
                break;
        }
    }
}

```

Number of comparisons?      Number of exchanges?

# Analysis — Insertion Sort (comparisons)

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- Running time depends on the input
- Worst-case?
  - ✓ input reverse sorted
- Best-case?
  - ✓ input already sorted
- Average-case?
  - ✓ expect every element to move  $O(n/2)$  times

# Partially sorted arrays

- An **inversion** is a pair of keys that are out of order

1	3	4	5	2	6	10	15	7
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“array is **partially sorted** if the number of pairs that are out-of-order is  $O(n)$ ”

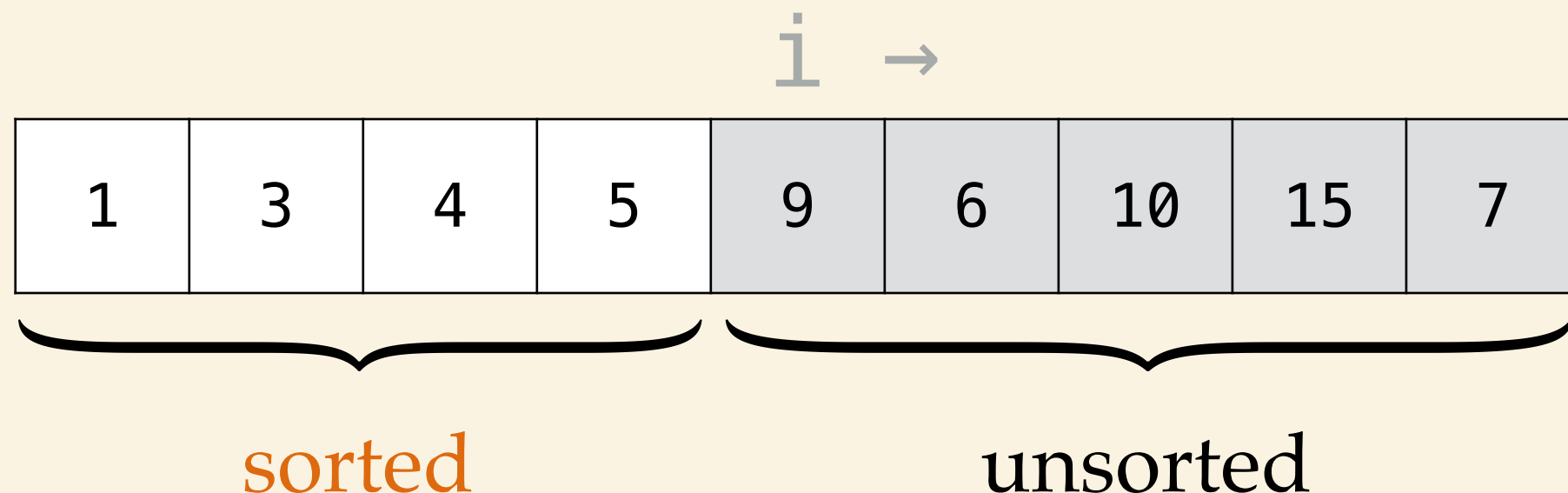
For partially-sorted arrays, insertion sort runs in **linear time**.

$$\Theta(n)$$



# Selection Sort

- Array is divided into **sorted** and **unsorted** parts
  - ✓ algorithm scans array from **left to right**
- Invariants
  - ✓ elements in **sorted** are **fixed** and in ascending order
  - ✓ no element in **unsorted** is smaller than any element in **sorted**



# Selection Sort Demo

```

void selectionsort(int *A, unsigned int n) {
    int temp;
    unsigned int i, j, min;
    // grows the left part (sorted)
    for (i = 0 ; i < n ; i++) {
        min = i;
        // find min in unsorted part
        for (j = i+1 ; j < n ; j++) {
            if (A[j] < A[min]) {
                min = j;
            }
        }
        // swap A[i] and A[min]
        temp = A[i];
        A[i] = A[min];
        A[min] = temp;
    }
}

```

Number of comparisons?      Number of exchanges?

# Summary

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	Best-Case	Average-Case	Worst-Case
Selection Sort	$\theta(n^2)$	$\theta(n^2)$	$\theta(n^2)$
Insertion Sort	$\theta(n)$	$\theta(n^2)$	$\theta(n^2)$