# Dealing with Sequences: Recurrent Neural Network (RNN) layer

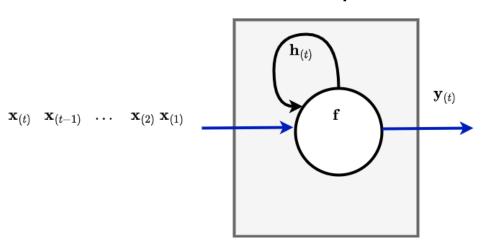
For a function that takes sequence  $\mathbf{x}^{(i)}$  as input and creates sequence  $\mathbf{y}$  as output we had two choices for implementing the function.

The RNN implements the function as a "loop"

- A function that taking **a single**  $\mathbf{x}_{(t)}$  as input a time
- Outputting  $\mathbf{y}_{(t)}$
- ullet Using a "latent state"  $\mathbf{h}_{(t)}$  to summarize the prefix  $\mathbf{x}_{(1\ldots t)}$
- Repeat in a loop over t

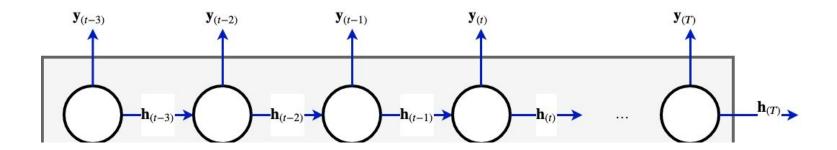
$$p(\mathbf{h}_{(t)}|\mathbf{x}_{(t)}, \mathbf{h}_{(t-1)})$$
 latent variable  $\mathbf{h}_{(t)}$  encodes  $[\mathbf{x}_{(1)} \dots \mathbf{x}_{(t)}]$   $p(\mathbf{y}_{(t)}|\mathbf{h}_{(t)})$  prediction contingent on latent variable

#### Loop with latent state



"Unrolling" the loop makes it equivalent to a multi-layer network

RNN unrolled

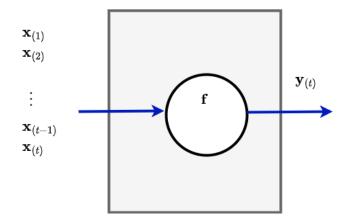


# **Transformer: Encoder-style**

The alternative to the loop was to create a "direct function"

- Taking a sequence  $\mathbf{x}_{(1\ldots t)}$  as input
- Outputting  $\mathbf{y}_{(t)}$

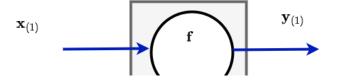
#### **Direct function**



In order to output the sequence  $\mathbf{y}_{(1)}\dots\mathbf{y}_{(T)}$  we create T copies of the function (one for each  $\mathbf{y}_{(t)}$ )

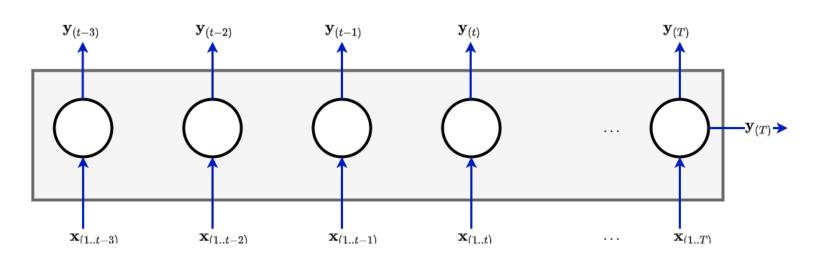
- computes each  $\mathbf{y}_{(t)}$  in **parallel**, not sequentially as in the loop

Direct function, in parallel (masked input)



### The parallel units constitute a *Transformer Encoder*

#### Transformer Encoder (causal masked input)



#### Compared to the unrolled RNN, the Transformer Decoder

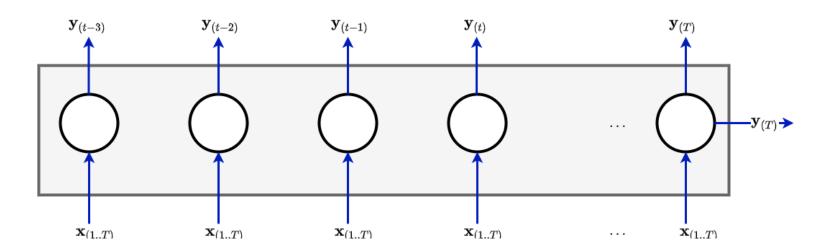
- Takes a **sequence**  $\mathbf{x}_{(1..t)}$  as input
  - Because  $\mathbf{y}_{(t)}$  is computed as a *direct* function of the prefix  $\mathbf{x}_{(1..t)}$  rather than recursively
- Has **no** latent state: output is a direct function of the input sequence
- ullet Has **no** data (e.g.,  ${f h}_{(t)}$ ) passing from the computation between time steps (e.g., from t to (t+1))
- Outputs generated in parallel, not sequentially
- No gradients flowing backward over time

With this architecture, we can compute more general functions than the RNN

• where each  $\mathbf{y}_{(t)}$  depends on the entire  $\mathbf{x}_{(1\dots T)}$  rather than a prefix  $\mathbf{x}_{(1\dots t)}$ 

Direct function, in parallel (un-masked input)

 $\mathbf{x}_{(1\dots T)}$   $\mathbf{y}_{(1)}$ 



An example of such a general function is the "meaning" of a word, in context.

#### Sentence Meaning of "it"

The animal didn't cross the street because **it** was too tired | the animal The animal didn't cross the street because **it** was too wide | the road

The meaning of the word "it" is determined by a word that follows it ("tired" or "wide")

So even though the Transformer output at each position is a function of the entire sequence  $\mathbf{x}_{(1\dots T)}$ 

ullet the output is different for each position t

We can control whether the input to Transformer element at position t is prefix  $\mathbf{x}_{(1\dots t)}$  or the entire sequence  $\mathbf{x}_{(1\dots T)}$  by **masking** the input to element t

- no masking: the entire sequence is visible
- ullet casual masking: only the prefix up to t is visible:  ${f x}_{(1\ldots t)}$

# Attention is all you need

The key to the Transformation is multiple uses of the Attention mechanism

- Self-attention
  - Both the Encoder and Decoder attend to their own inputs
  - Implementing the *direct function*, rather than "loop" approach
- Cross-attention
  - The Decoder attends to the intermediate representations of the Encoder

The queries used in attention lookup are  $\mathbf{h}_{(t)}, ar{\mathbf{h}}_{(t)}$ 

• as are the keys and values

We will use d (or  $d_{
m model}$  to denote the length of these values.

Moreover, all pathways in the Transformer will maintain the size d.

# **Technical clarifications**

# **Shared Transformer blocks across positions**

The transformer blocks ("circles" in the diagram)

- are **shared** across all positions
- that is: the same computation (with shared parameters) is performed in parallel
- ullet Thus, the number of parameters is **not** a function of sequence length T

# Identifying $\mathbf{y}_{(t)}$ with $\mathbf{h}_{(t)}$

When we introduced the RNN, at each step t of the loop, we defined two outputs  $\mathbf{h}_{(t)}$  and  $\mathbf{y}_{(t)}$ .

In general, we only need to output  $\mathbf{h}_{(t)}$ 

•  $\mathbf{y}_{(t)}$  can be defined as a further processing of  $\mathbf{h}_{(t)}$ 

Henceforth, we will assume the style of a single output  $\mathbf{h}_{(t)}$ 

The reason for doing this:

- We can "stack" N Transformer layers (just as we can stack RNN layers) The output of the non-top layer j is  $\mathbf{h}_{(t)}^{[j]}$ , not the final  $\mathbf{y}_{(t)}$
- ullet We identify  $\mathbf{y}_{(t)}$  as the output of the top layer  $\mathbf{h}_{(t)}^{[N]}$ 
  - perhaps after a further processing

#### Furthermore:

Since the Encoder part is no longer a "loop"

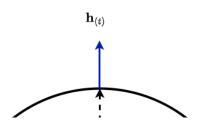
- ullet It is inaccurate to refer to the Encoder output  $ar{\mathbf{h}}_{(t)}$  as a "latent" state
- ullet However,  $ar{\mathbf{h}}_{(t)}$  is still a summary of the input sequence
  - lacksquare a summary of  $\mathbf{x}_{(1\ldots t)}$  when casual attention is used
  - lacksquare a summary of  $\mathbf{x}_{(1\dots ar{T})}$  otherwise
- Out of **bad habit** we may continue to erroneously refer to  $\bar{\mathbf{h}}$  and  $\mathbf{h}$  as "latent" states

# Inside the Transformer Encoder: Self Attention

If we look inside the box computing the direct function, we will find several layers

- An Attention layer
  - To influence which elements of the input sequence  $\mathbf{x}$  to attend/focus when outputting  $\mathbf{y}_{(t)}$
- A Feed Forward Network (FF) layer to compute the function

Transformer Layer (Encoder)



An Attention layer that attends/focus on its inputs implements what is called *Self-attention* 

• We will soon see the possibility of attending to other values

If the function for  $\mathbf{h}_{(t)}$  is restricted to prefix  $\mathbf{x}_{(1...t)}$  the Attention layer can use causal masking of the input sequence.

This is referred to as Masked Self-Attention.

The Feed Forward Network computes the function, given the elements of the input sequence that are being attend to.

# Advantages of a Transformer compared to an RNN

As we will demonstrate in detail below

- The Transformer's operations can be performed in parallel versus sequentially for the RNN
- Gradients less likely to vanish or explode

We can **leverage** these advantages in complexity by

- By making a Transformer model bigger (e.g., more stacked Transformer layers)
- Making the sequence lengths longer
- Increasing the number of examples of training data

So, for the same time "cost" as an RNN, we can use a bigger Transformer on more data

• Hence: we can learn more complex functions for similar time cost

The path length from the output to the input is constant in an Transformer, compared to *T* in the RNN.

• parallel computation: reduced wall time
• less likely for gradients to vanish/explode over shorter path
■ Transformer better ble to capture long-range dependencies than an RNN

But there are costs to pay for this (relative to an RNN), many due to Attention Lookup.

- higher memory
  - lacktriangledown the Q matrix is shape (T imes d); the K,V matrices are  $(ar{T} imes d)$

 $Q * K^T$ 

• intermediate matrices, e.g.

are of shape 
$$(T imes ar{T})$$

- the number of operations is greater
- the number of parameters is greater

We give the detailed math below.

# Number of sequential steps

The most obvious advantage of the "direct function" as opposed to the "loop" is that outputs are computed in parallel versus sequentially.

For an input sequence of length T:

- ullet The loop requires T steps
- The direct function requires 1 step

# Path length

The *Path length* is the distance that the Loss Gradient needs to travel backwards during Back Propagation.

At each step, the gradient is subject to being diminished or increased (Vanishing/Exploding gradients).

Since the Transformer operates in parallel across positions, this is  $\mathcal{O}\left(1\right)$ .

It is  $\mathcal{O}\left(T\right)$  for the RNN due to the sequential computation.

#### The constant path length is critical to the success of the Transformer

- The query used for the input at position t can access **all** prior positions  $t' \leq t$  at the same cost
  - Gradient not diminished
  - RNN
- $\circ$  Gradient signal diminished for position t' << t
- $\circ$  Truncated Back Propagation may kill the gradient flow from position t back to t' beyond truncation window

A key strength of the Transformer is that it enables learning long-range dependencies.

# **Number of parameters**

In the Transformer, the Q,K,V matrices are first projected through  $(d \times d)$  matrices,  $\mathbf{W}_k,\mathbf{W}_Q,\mathbf{W}_V$ 

$$K \mid = \mid K \mid \mid \boldsymbol{W}_{K} \mid V \mid = \mid V \mid \mid \boldsymbol{W}_{V} \mid (\bar{T} \times d) \mid \mid (\bar{T} \times d) \mid \mid (d \times d) \mid$$

Each of the matrices,  $\mathbf{W}_k, \mathbf{W}_Q, \mathbf{W}_V$ , is  $\mathcal{O}\left(d^2\right)$  parameters.

The Feed Forward Network is usually implemented by 2 Dense layers.

the first takes the length d attention output

- ullet and creates  $d_{
  m ffn}$  new features
- by custom:  $d_{\rm ffn} = 4*d$

The second takes the length  $d_{
m ffn}$  output of the first and creates the final length  $d_{
m model}$  output.

Thus, each Dense layer has  $\mathcal{O}\left(d^2\right)$  weights.

# **Number of operations**

What about the number of operations?

The Attention Lookup is computed via matrix multiplication

$$Q * K^T * V$$

 $Q*K^T$  has  $(T imes ar{T})$  elements, each the result of d multiplications.

Thus:  $\mathcal{O}\left(T^2*d\right)$  multiplications.

The Self Attention layer attend to (transformed) inputs

 $\bullet$  each element assumed size of d

The keys and values of the CSM implementing Attention are the size d input elements.

- ullet Each attention lookup (dot product of query with a key) requires d multiplications.
- There are T key/value pairs in the CSM
- ullet There are T attention units (one for each position, outputting  $\mathbf{h}_{(t)}$ )

Thus:  $\mathcal{O}\left(T^2*d\right)$  multiplications.

### **RNN** calculations

Let's examine the RNN's number of operations and weights.

The RNN inputs  $\mathbf{x}_{(t)}$  and outputs  $\mathbf{h}_{(t)}$  of size d (same as Transformer).

• In the RNN  $\mathbf{h}_{(t)}$  is also the latent state

Each step of the RNN updates the latent state  $\mathbf{h}_{(t)}$  via the equation

$$\mathbf{h}_{(t)} = \phi(\mathbf{W}_{xh}\mathbf{x}_{(t)} + \mathbf{W}_{hh}\mathbf{h}_{(t-1)} + \mathbf{b}_h)$$

The weight matrices

$$\mathbf{W}_{xh}$$
 and  $\mathbf{W}_{hh}$ 

are of size

$$\mathcal{O}\left(d imes d
ight)$$

ullet transforming length d vectors  $(\mathbf{x}_{(t)},\mathbf{h}_{(t-1)})$  into a length d vector  $\mathbf{h}_{(t)}$ 

The multiplication of (d imes d) weights matrices times a vector of length d

- requires d multiplications per element
- ullet there are d elements in  $\mathbf{h}_{(t)}$

Thus  $\mathcal{O}\left(d^2\right)$  operations per time step.

There are T sequential time-steps

- $\mathcal{O}\left(T*d^2\right)$  total operations
- ullet involving T sequential steps
  - steps are computed sequentially in the RNN, versus in parallel in the Transformer
- ullet path length T as gradient flows backward through each of the T time steps

# **Complexity: summary**

We also throw in a CNN for comparison

The detailed CNN math is given in a following section.

Туре	Parameters	Operations	Sequential steps	Path length
CNN	$\mathcal{O}\left(k*d^2 ight)$	$\mathcal{O}\left(T*k ight. + d^2 ight)$	$\mathcal{O}\left(T ight)$	$\mathcal{O}\left(T ight)$
RNN	$\mathcal{O}\left(d^2 ight)$	$\mathcal{O}\left(T*d^2 ight)$	$\mathcal{O}\left(T ight)$	$\mathcal{O}\left(T ight)$
Self-attention	$\mathcal{O}\left(d^2 ight)$	$\mathcal{O}\left(T^2*d\right)$	$\mathcal{O}\left(1 ight)$	$\mathcal{O}\left(1\right)$

#### Reference:

- <u>Transformer Scaling paper (https://arxiv.org/pdf/2001.08361.pdf#page=6)</u>
- Table 1 of Attention paper (https://arxiv.org/pdf/1706.03762.pdf#page=6)
- See <u>Stack overflow</u> (<a href="https://stackoverflow.com/questions/65703260/computational-complexity-of-self-attention-in-the-transformer-model">https://stackoverflow.com/questions/65703260/computational-complexity-of-self-attention-in-the-transformer-model</a>) for correction of the number Operations calculated in paper

Transformer main point of comparison to the RNN

- fewer Sequential Steps:  $\mathcal{O}\left(1\right)$  versus  $\mathcal{O}\left(T\right)$
- ullet operations:  $\mathcal{O}\left(T^2*d\right)$  versus  $\mathcal{O}\left(T*d^2\right)$ 
  - lacktriangledown more when sequences are long, i.e., T>d

But: because of the reduced number of sequential steps, Transformers

- ullet can stack many (i.e.,  $n_{
  m layers}$ ) blocks, each taking  $\mathcal{O}\left(1
  ight)$  time
  - $\mathcal{O}\left(n_{ ext{layers}}
    ight)$  Sequential Steps total
- ullet and still be less than the  $\mathcal{O}\left(T
  ight)$  Sequential Steps of an RNN
- ullet at the cost of increasing number of operations and parameters by  $\mathcal{O}\left(n_{ ext{layers}}
  ight)$

Transformers consume larger number of parameters and operations through this factor of  $n_{
m layers}$  blocks.

### **CNN** calculations

Here's the details of the math for the CNN

- ullet path length T
  - each kernel multiplication connects only k elements of  $\mathbf{x}$
  - lacktriangleright since kernels overlap inputs, can't parallelize, hence  $\mathcal{O}\left(T/k
    ight)$  path length
    - $\circ$  can reduce to  $\log(T)$  with tree structure
- Parameters
  - kernel size k
  - lacktriangle number of input channels = number of output channels = d
  - k\*d parameters for kernel of one channel
  - lacksquare  $\mathcal{O}\left(k*d^2\right)$  parameters for kernel for all d output channels
- Operations
  - for a single output channel: k per input channel
    - $\circ$  There are d input channels, so k\*d for each dot product of one output channel
    - There are d output channels, so  $k*d^2$  per time step
  - T time steps so  $\mathcal{O}\left(T*k*d^2\right)$  number of operations

## A free lunch? Almost!

Transformers sound almost too good to be true

- Faster compute (through reduced number of Sequential steps)
- Constant Path Length
  - Better able to capture long range dependencies

Is there really such a thing as a free lunch?

Almost.

In order to achieve the full benefit of reduced path length

- ullet the operations across all T positions must be computed in parallel
- this involves a tremendous amount of simultaneous compute power
  - very expensive in hardware and power costs

In addition, positional encoding needs to be preserved at each layer

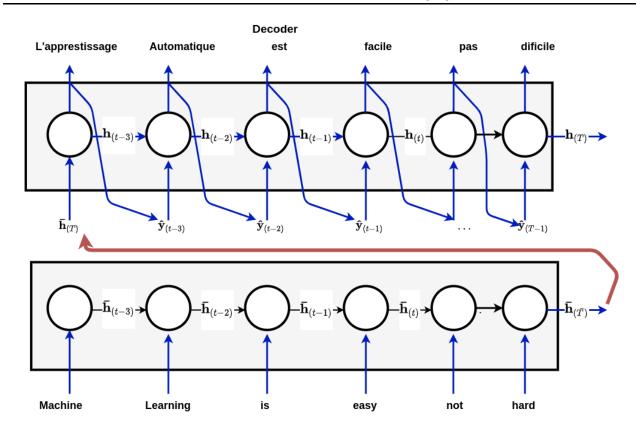
- to maintain relative ordering (e.g., for causal attention)
- more complicated than an RNN

# Transformer: Decoder style

It is common to use two Transformers in an Encoder-Decoder configuration.

Recall the Encoder-Decoder architecture (using RNN's rather than Transformers in the diagram)

**Encoder-Decoder for language translation** 



Encoder

The Decoder in the Encoder-Decoder architecture is generative

- Outputs  $\hat{\mathbf{y}}_{(t)}$  for a single t at a time
- ullet Appending output  $\hat{\mathbf{y}}_{(t)}$  to the input available to output the next  $\hat{\mathbf{y}}_{(t+1)}$

The Encoder in the Encoder-Decoder architecture creates a latent state  $\bar{\mathbf{h}}_{(t)}$  which summarizes the input prefix  $\mathbf{x}_{(1\dots t)}$ .

In the above diagram the Decoder only has access to  $ar{\mathbf{h}}_{(ar{T})}$ , the final latent state

• summarizing the entire input sequence

This is very restrictive, forcing  $ar{\mathbf{h}}_{(ar{T})}$  to encode a lot of information.

But we motivated Attention by suggesting that the Decoder have access to each  $\bar{\mathbf{h}}_{(t)}$  for  $1 \leq t \leq \bar{T}$ .

- and use the Attention mechanism to decide which  $\bar{\mathbf{h}}_{(t)}$  to focus on when generating  $\hat{\mathbf{y}}_{(t)}$ 

**Decoder: Attention** 

Decoder

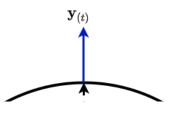
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#### The Decoder Transformer

- is similar to the Encoder Transformer in that both use Self-Attention to their own inputs
- differs in that it can also attend to the output of the Encoder.

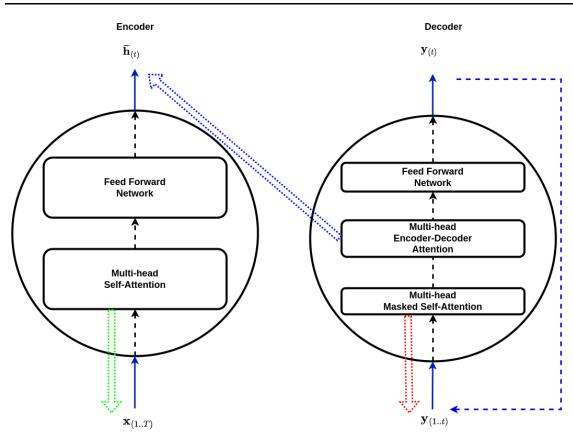
Attending to the output of another model (e.g., Decoder attending to Encoder output) is called *Cross Attention* (Encoder-Decoder Attention).

Transformer Layer (Decoder)
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### The combinded Encoder-Decoder Transformer diagram looks like this

#### Transformer Layer (Encoder/Decoder)



#### **Explanation of diagram**

- The Encoder uses Self-attention (wide Green arrow) to attend to input sequence
   x
- The Decoder uses Masked Self-attention (wide Red arrow) to attend to its input
  - It's input is the prefix of the output sequence y
  - Limited to prefix of length t by masking
- The Decoder uses Cross Attention (between Encoder and Decoder) (wide Blue arrow)
  - lacksquare To enable Decoder to focus on which Encoder latent state  $ar{\mathbf{h}}_{(t)}$  to atttend to
- The dotted (thin Blue arrow) indicates that the output  $\hat{\mathbf{y}}_{(t)}$  is appended to the input that is available when generating  $\hat{\mathbf{y}}_{(t+1)}$

Note that the Decoder is recurrent (generative)

- it generates a single output at a time
- unlike the Encoder, which generates all outputs (i.e., "encodings") in parallel

## Functional versus Sequential architecture

The architecture diagram is more complex than we have seen thus far.

In particular: data no longer strictly flows forward in a layer-wise arrangement!

- There are two independent sub-networks (Encoder and Decoder)
- Connection from the Encoder output to the middle of the Decoder (Cross-Attention)

Each of the Encoder and Decoder is an independent Functional model.

• not our familiar Sequential modles

The Encoder-Decoder pair combination is also constructed as a Functional model.

Since we have not yet addressed Functional Models, you may not be prepared to completely grasp the totality.

But hopefully you can absorb the concepts even without fully understanding the details.

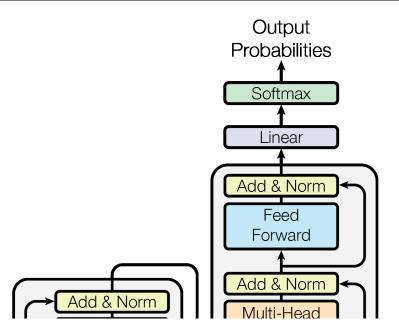
### **Detailed Encoder-Decoder Transformer architecture**

There are other components of the Encoder and Decoder that we have yet to describe.

We will do so briefly.

(The Transformer was introduced in the paper <u>Attention is all you Need</u> (<u>https://arxiv.org/pdf/1706.03762.pdf</u>)

Transformer (Encoder/Decoder)



### **Embedding layers**

We will motivate and describe Embeddings in the NLP module.

For now:

• an embedding is an encoding of a categorical value that is shorter than OHE

It is used in the Transformer to

- encode the input sequence of words
- encode the output sequence of words

### **Positional Encoding**

The inputs are ordered (i.e., sequences) and thus describe a relative ordering relationship between elements.

But inputs to most layer types (e.g., Fully Connected) are unordered.

The Positional Encoding is a way of encoding the the relative ordering of elements.

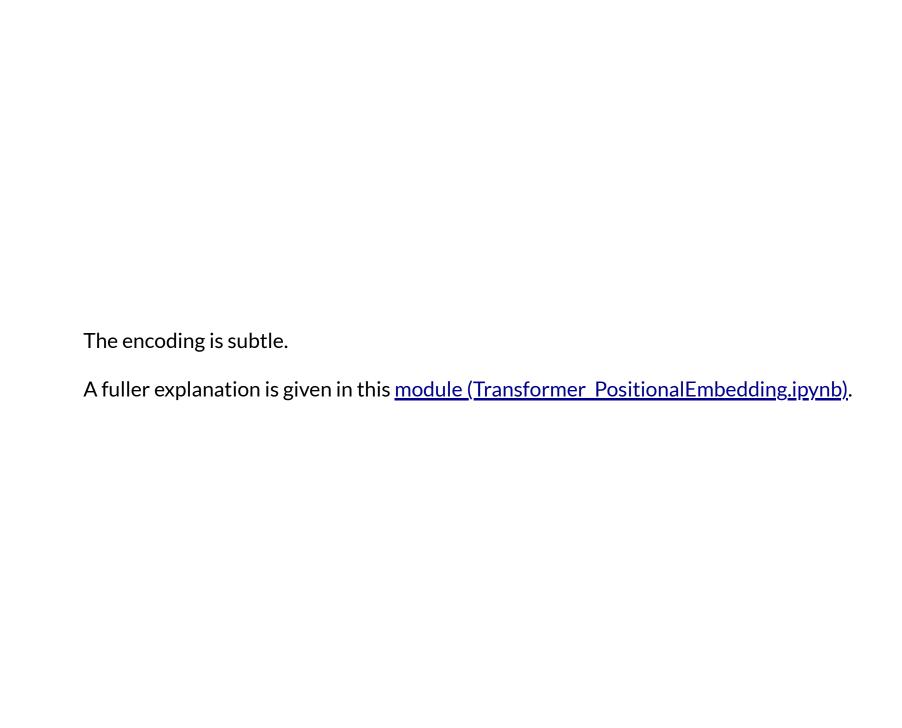
To represent the relative position of each element in the sequence,

• we can pair the input element with an encoding of its position in the sequence.  $\langle \mathbf{x}_{(t)}, \operatorname{encode}(t) \rangle$ 

The box labeled "Positional Encoding" creates encode(t).

The "+" concatenates the Input Embedding and Positional Encoding to create  $\langle \mathbf{x}_{(t)}, \operatorname{encode}(t) \rangle$ .

If relative position is important, the NN can learn the values of  $\mathrm{encode}(t)$ .



### **Self Attention layers (Encoder and Decoder)**

The 3 arrows flowing into the Multi-Head Attention box

- are identical
- are the inputs (after being Embedded and having Positional Encoding added)

The Self-Attention layers for the Encoder and Decoder

- differ in that the Decoder uses Causal Masking versus no-masking for the Encoder
- ullet Decoder can't "look ahead" at output  $\mathbf{y}_{t'}$  for  $t' \geq t$ 
  - lacktriangle it hasn't been generated yet at test time step t
  - it **is** available at training time (via Teacher Forcing)
    - but shouldn't look at it during training time, in order for training to be similar to test time

### **Cross Attention layer (Decoder)**

The two arrows flowing from the Encoder output are the keys and values of the CSM

The arrow flowing from the Self Attention layer is the query

• The output of the Self Attention layer is the **query** used in Cross Attention

#### Add and Norm

We have seen each of these layer types before

- Norm: Batch (or other) Normalization layers
- Add: the part of the residual network that joins outputs of multiple previous layers

The diagram shows an Encoder-Decoder pair.

You will notice that each element of the pair is different.

- It is possible to use each element independently as well.
- But first we need to understand the source of the differences and their implications.

## How is the direct function computed?

The Encoder uses self-attention

 $\bullet\,$  So the keys and values of the CSM are derived directly from input sequence  $x_{(1\dots T)}$ 

During training, the Encoder

- learns a query, derived from input sequence  $\mathbf{x}_{(1\dots T)}$
- learns weights for the Feed Forward Network

The Attention output

- is equal to a weighted combination of CSM values
  - i.e., weighted sum of input elements

The Feed Forward Network transforms the Attention output into Encoder output  $ar{\mathbf{h}}_{(t)}$ .

Similarly for the Decoder.

The Self-Attention layer CSM has keys and values that are incrementally constructed from the outputs  $\mathbf{y}_{(1...,t)}$  that have been created from the first t steps.

The Cross-Attention layer CSM has keys and values that are outputs  $ar{\mathbf{h}}_{(t)}$  of the Encoder.

During training, the Self-Attention layer outputs **the query** that is used for Cross Attention.

The query is created by self-attention to the inputs.

The Decoder learns (from training)

- the Self-Attention query
- the Cross Attention query
- the weights of the Feed Forward Network

### **Stacked Transformer**

Just as with many other layer types (e.g., RNN), we may stack Transformer layers.

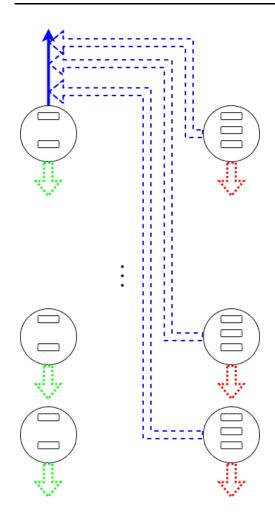
• Each layer creating alternate representations of the input of increasing complexity

In fact, stacking N>1 Transformer layers is typical.

N=6 was the choice of the original paper.

Note that this is still an Encoder-Decoder

• so the *final* output of the Encoder is attended to by *each* layer of the Decoder.



## **Uses of an Encoder-style Transformer**

The Transformer for the Encoder and Decoder of an Encoder-Decoder Transformer are slightly different.

They can also be used individually as well as in pairs.

It's important to understand the differences in order to know when to use each individually.

The Encoder side of the pair **does not** restrict the order in which it's inputs are accessed.

• Self-attention without causal masking

So the Encoder is appropriate for tasks that require a context-sensitive representation of each input element.

For example: the meaning of the word "it" changes with a small change to a subsequent word in the following sentences:

- "The animal didn't cross the road because it was too tired"
- "The animal didn't cross the road because it was too wide"

#### Some tasks with this characteristic are

- Sentiment
- Masked Language Modeling: fill-in the masked word
- Semantic Search
  - compare a summary of the sequence that is the context-sensitive representation of
    - query sentence
    - document sentences
  - Each summary is a kind of sentence embedding
  - Summary
    - pooling over each word
    - o final token

## **Uses of a Decoder-style Transformer**

One notable aspect of the Decoder is its recurrent (generative) architecture

- Output  $\mathbf{y}_{(t-1)}$  is appended to the Decoder inputs available at step t.
  - $\blacksquare$  The Decoder inputs are  $\mathbf{y}_{(1..T)}$  , where T is the full length of the Decoder output
  - But Causal Masking ensures that only  $\mathbf{y}_{(1..t)}$  is available at step t.

Thus, the Decoder is appropriate for generative tasks

- Text generation
- Predict the next word in a sentence

### Conclusion

The Transformer architecture has come to dominate tasks with long sequences (e.g., NLP).

The operations of a Transformer occur in parallel for each position.

This allows us to leverage the compute time

- Use many stacked Transformer layers
- At time cost still less than a sequential RNN layer

Moreover, the constant path length means the gradients are less likely to vanish/explode for long sequences
<ul> <li>No need to truncate Back Propagation as in an RNN</li> <li>Long term dependencies between positions become feasible.</li> </ul>

We pay for these advantages in terms of increasing

- number of operations
  - but they occur in parallel, so no increase in elapsed time
- number of weights

Thus, Transformer training is both compute and memory intensive.

• This limits the number of individuals/organizations able to train very large models.

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Done