Before you turn this problem in, make sure everything runs as expected. First, **restart the kernel** (in the menubar, select Kernel \rightarrow Restart) and then **run all cells** (in the menubar, select Cell \rightarrow Run All).

Make sure you fill in any place that says YOUR CODE HERE or "YOUR ANSWER HERE", as well as your name and collaborators below:

```
In [1]: NAME = ""
COLLABORATORS = ""
```

Assignment: Using Machine Learning for Hedging

Welcome to the first assignment!

Problem description

We will solve a Regression task that is very common in Finance

• Given the return of "the market", predict the return of a particular stock

That is

• Given the return of a proxy for "the market" at time t, predict the return of, e.g., Apple at time t.

As we will explain, being able to predict the relationship between two financial instruments opens up possibilities

- Use one instrument to "hedge" or reduce the risk of holding the other
- Create strategies whose returns are independent of "the market"
 - Hopefully make a profit regardless of whether the market goes up or down

Goal

You will create models of increasing complexity in order to explain the return of Apple (ticker AAPL)

- ullet The first model will have a single feature: return of the market proxy, ticker SPY
- Subsequent models will add the return of other tickers as additional features

Learning Objectives

- Learn how to solve a Regression task
- Become facile in the sklearn toolkit for Machine Learning

How to report your answers

We will mix explanation of the topic with tasks that you must complete.

Look for the string "Question" to find a task that you must perform.

Most of the tasks will require you to create some code at the location indicated by

```
# YOUR CODE HERE
raise NotImplementedError()
```

• Replace raise NotImplementedError() with your own code

Standard imports

```
In [2]: | # Standard imports
        import numpy as np
         import pandas as pd
         import matplotlib.pyplot as plt
         import sklearn
         import os
         import math
        %matplotlib inline
In [3]: | from IPython.core.interactiveshell import InteractiveShell
         InteractiveShell.ast node interactivity = "all"
         # Reload all modules imported with %aimport
         %load ext autoreload
         %autoreload 1
         # Import nn helper module
         import helper
         %aimport helper
         helper = helper.HELPER()
```

Get The data

The first step in our Recipe is Get the Data.

The data are the daily prices of a number of individual equities and equity indices.

The prices are arranged in a series in ascending date order (a timeseries).

There are many . CSV files for equity or index in the directory DATA_DIR

API for students

We will define some utility routines to help you.

In this way, you can focus on the learning objectives rather than data manipulation.

This is not representative of the "real world"; you will need to complete data manipulation tasks in later assignments.

We provide a class HELPER

• Instantiated as

```
helper =
helper.HELPER()
```

With methods

- getData:
 - Get examples for a list of equity tickers and an index ticker.
 - Called as

```
data = helper.getData( tickers,
index_ticker, attrs)
```

- tickers is a list of tickers
- *index* is the ticker of the index
- attrs is a list of data attributes

Question:

- Create code to
 - $\,\blacksquare\,$ Get the adjusted close price of AAPL and SPY
 - Assign the result to variable data

Hint:

- Use the getData method from the helper class
 - The list of tickers contains just the single ticker AAPL
 - The index ticker is SPY
 - The list of attributes is the single attribute Adj Close

Have a look at the data

We will not go through all steps in the Recipe, nor in depth.

But here's a peek at the data you retrieved

```
In [ ]: data.head()
In [ ]: # Print the Start time and End time
    print("Start time: ", data.index.min())
    print("End time: ", data.index.max())
```

Create DataFrame of price levels for the training examples

The training examples will be stored in a DataFrame.

- The DataFrame should have two columns: the price level for the ticker and for the index
- The minimum date in the DataFrame should be the trading day before start_dt
 - That is: the latest date for which there is data and which is less than start_dt
 - For example, if start_dt is a Monday, the "day before" would be Friday, not Sunday.
 - Similarly for the case where the day before start_dt is a holiday
- The maximum date in the DataFrame should be end_dt

The reason we are adding one day prior to start dt

- We want to have returns (percent price changes) from start_dt onwards
- In order to compute a return for start_dt, we need the level from the prior day

Question:

- Complete the function getRange()
 - To return the subset of rows of our examples
 - Beginning on the trading day before date start_dt
 - Ending on date end_dt

```
In [ ]: | start dt = "2018-01-02"
        end dt = "2018-09-28"
        train data price = None
        # Set variable train data price to be a DataFrame with two columns
        ## AAPL Adj Close, SPY Adj Close
        ## with dates as the index
        ## Having minimum date equal to THE DAY BEFORE start dt
        ## Having maximum date equal to end dt
        def getRange(df, start dt, end dt):
            Return the the subset of rows of DataFrame df
             restricted to dates between start dt and end dt
             Parameters
            df: DataFrame
             - The data from which we will take a subset
             start dt: String
             - Start date
            end dt: String
             - End date
            # YOUR CODE HERE
             raise NotImplementedError()
        train data price = getRange(data, start dt, end dt)
        print(train data price.head())
```

As you can see, each row has two attributes for one date

- Price (adjusted close) of ticker AAPL
- Price (adjusted close) of the market proxy SPY

Create test set

We just created a set of training examples as a subset of the rows of data.

We will do the same to create a set of test examples.

Question:

Set variable test_data_price

- To the subset of rows of our examples
- Beginning on the trading day before date test start dt
- Ending on date test_end_dt

Hint

• Use getRange with different arguments for the dates

```
In [ ]: test_start_dt = '2018-10-01'
    test_end_dt = '2018-12-31'

# YOUR CODE HERE
    raise NotImplementedError()
In [ ]:
```

Prepare the data

In Finance, it is very typical to work with *relative changes* (e.g., percent price change) rather than *absolute changes* (price change) or *levels* (prices).

Without going into too much detail

- Relative changes are more consistent over time than either absolute changes or levels
- The consistency can facilitate the use of data over a longer time period

For example, let's suppose that prices are given in units of USD (dollar)

- A price change of 1 USD is more likely for a stock with price level 100 than price level 10
 - lacksquare A relative change of 1/100=1 is more likely than a change of 1/10=10
 - So relative changes are less dependent on price level than either price changes or price levels

To compute the *return* (percent change in prices) for ticker AAPL (Apple) on date t

$$r_{ ext{AAPL}}^{(t)} = rac{p_{ ext{AAPL}}^{(t)}}{p_{ ext{AAPL}}^{(t-1)}} - 1$$

where

 $p_{ ext{AAPL}}^{(t)}$ denotes the price of ticker AAPL on date t $r_{ ext{AAPL}}^{(t)}$ denotes the return of ticker AAPL on date t

Transformations: transform the training data

Our first task is to transform the data from price levels (Adj Close) to Percent Price Changes.

Moreover, the date range for the training data is specified to be in the range from start_dt (start date) to end_dt, inclusive on both sides.

Note

We will need to apply **identical** transformations to both the training and test data examples.

In the cells that immediately follow, we will do this only for the training data

You will need to repeat these steps for the test data in a subsequent step.

You are well-advised to create subroutines or functions to accomplish these tasks!

- You will apply them first to transform training data
- You will apply them a second time to transform the test data

We will achieve this is several steps

Create DataFrame of returns for training examples

Create a new DataFrame with percent price changes of the columns, rather than the levels

Question:

- Complete function getReturns() to set variable train_data_ret to be a
 DataFrame with the same columns
 - But where the prices have been replaced by day over day percent changes
 - The column names of train_data_ret should be the same as the original columns names
 - We give you code to rename the columns to reflect the changed meaning of the data in the next step

Hint:

look up the Pandas pct_change() method

```
train_data_ret = None
        def getReturns(df):
            Return the day over day percent changes of adjusted price
             Parameters
             df: DataFrame
            # YOUR CODE HERE
             raise NotImplementedError()
        train data ret = getReturns(train data price)
         train data ret.head()
In [ ]:
```

Since the columns of train_data_ret are now returns, we will rename then for you.

Also, we will drop the earliest date

- There is now return for this date
- We included this row only so we could compute the return for the following trading date

Remove the target

The only feature is the return of the market proxy SPY.

Predicting the target given the target as a feature would be cheating!

So we will create X_train, y_train from train_data_ret

- X train has only features for the example
- y train is the target for the example

```
In [ ]: tickerAttr = ticker + "_Ret"

X_train, y_train = train_data_ret.drop(columns=[tickerAttr]), train_data_ret[[tickerAttr]]
```

Transformations: transform the test data

We have just performed some transformations of the training data.

Remember:

You need to perform identical transformations to the test data.

The test data will be returns from test_start_dt to test_end_dt inclusive.

We will apply identical transformations as we did to the training data, but with a different date range.

We obtained X_train, y_train via transformations to train_data_price.

We will now obtain X_{test} , y_{test} by identical transformations to test_data_price

Question:

Create the training data X_test, y_test

- Apply the same transformations to test_data_price as you did to train_data_price
- To create variable test_data_ret
- We will convert test_data_ret to X_test, y_test for you

Hints

Create test_data_ret in a manner analogous to the creation of train_data_ret

- Use getReturns to convert price levels to returns
- Use helper.renamePriceToRet to rename the columns to reflect the change in data from price to return
- Drop the first date from test_data_ret as it has an undefined return

```
In [ ]:
        test data price.head()
In [ ]: | test data ret = None
        X test = None
        y test = None
        # YOUR CODE HERE
         raise NotImplementedError()
        X test, y test = test data ret.drop(columns=[tickerAttr]), test data ret[[ tick
        erAttr 11
        print("test data length", test data ret.shape[0])
        print("X test length", X test.shape[0])
        print("y test length", y test.shape[0])
        test data ret.head()
In [ ]:
```

Train a model (Regression)

Use Linear Regression to predict the return of a ticker from the return of the market proxy SPY. For example, for ticker AAPL

$$r_{ ext{AAPL}}^{(t)} = eta_0 + eta_{ ext{AAPL,SPY}} * r_{ ext{SPY}}^{(t)} + \epsilon_{ ext{AAPL}}^{(t)}$$

Each example corresponds to one day (time t)

- has features
 - constant 1, corresponding to the intercept parameter
 - return of the market proxy SPY

$$\mathbf{x}^{(t)} = \left(egin{array}{c} 1 \ r_{\mathrm{SPY}}^{(t)} \end{array}
ight)$$

- has target
 - return of the ticker

$$\mathbf{y}^{(t)} = r_{ ext{AAPL}}^{(t)}$$

You will use Linear Regression to solve for parameters eta_0 , $eta_{\mathrm{AAPL,SPY}}$

- In the lectures we used the symbol Θ to denote the parameter vector; here we use β
- In Finance the symbol β is often used to denote the relationship between returns.
- Rather than explicitly creating a constant 1 feature
 - you may invoke the model object with the option including an intercept
 - if you do so, the feature vector you pass will be

$$\mathbf{x}^{(t)} = \left(\, r_{ ext{SPY}}^{(t)} \,
ight)$$

- Use the entire training set
- Do not use cross-validation

Question:

Train your model to estimate the parameters beta_0 and beta_SPY

- Complete the function createModel () to build your linear regression model. The detailed description is in the function below.
- Complete the function regress () to perform the regression and return two item: the intercept and coefficients. The detailed description is in the function below.
 - beta_0 is the regression parameter for the constant;
 - beta_SPY is the regression parameter for the return of SPY.
 - We will test if the parameters of your regression are correct. We have initialized them to be 0.

Hints:

- The input model of your function regress () should be the model you get from function createModel ()
- Before you input your X_train and y_train into your sklearn model, you need to convert them from type DataFrame into type ndarray.
 - You can convert a DataFrame into an ndarray with the values attribute, e.g., X_train.values

```
In [ ]: | from sklearn import datasets, linear_model
        beta 0 = 0 # The regression parameter for the constant
        beta SPY = 0 # The regression parameter for the return of SPY
        ticker = "AAPL"
        def createModel():
            Build your linear regression model using sklearn
            Returns
            An sklearn model object implementing Linear Regression
            # YOUR CODE HERE
             raise NotImplementedError()
        def regress(model, X, y):
            Do regression using returns of your ticker and index
             Parameters
            model: model object implementing Linear Regression
            X: DataFrame
             - Index returns
            y: DataFrame
             - Ticker returns
            Returns
             Tuple (beta_0, beta SPY)
             where,
```

```
beta 0: Scalar number
        - Parameter for the constant
        beta_SPY: Scalar number
        - Parameter for the return of SPY
    111
    # YOUR CODE HERE
    raise NotImplementedError()
# Assign to answer variables
regr = createModel()
beta 0, beta SPY = regress(regr, X train, y train)
print("\{t:s\}: beta 0=\{b0:3.3f\}, beta SPY=\{b1:3.3f\}".format(t=ticker, b0=beta 0,
b1=beta SPY))
```

Your expected outputs should be:

```
beta_0 0.001
beta_SPY 1.071
```

```
In [ ]:
```

Train the model using Cross validation

Since we only have one test set, we want to use 5-fold cross validation to assess model performance.

Question:

- Complete the function compute_cross_val_avg() to compute the average score of 5-fold cross validation
 - Set cross_val_avg as your average score of k-fold results
 - Set k = 5 as the number of folds

Hint:

You can use the cross_val_score in sklearn.model_selection

```
In [ ]: | from sklearn.model selection import cross val score
        cross val avg = 0 # average score of cross validation
        k = 5
                           # 5-fold cross validation
        def compute cross val avg(model, X, y, k):
             Compute the average score of k-fold cross validation
             Parameters
            model: An sklearn model
            X: DataFrame
             - Index returns
            y: DataFrame
             - Ticker returns
             k: Scalar number
             - k-fold cross validation
             Returns
             The average, across the k iterations, of the score
            # YOUR CODE HERE
             raise NotImplementedError()
        cross val avg = compute cross val avg(regr, X train, y train, 5)
        print("{t:s}: Avg cross val score = {sc:3.2f}".format(t=ticker, sc=cross val av
        g) )
```

Evaluate Loss (in sample RMSE) and Performance (Out of sample RMSE)

To see how well your model performs, we can check the in-sample loss and out-of-sample performance.

Question:

- Complete the function computeRMSE() to compute the Root of Mean Square Error (RMSE)
 - Set rmse_in_sample to be in-sample loss
 - Set rmse_out_sample to be out-of-sample performance