

High Frequency Trading and Long-Term Investors: A View from the Buy-Side

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Outline & A Bit of History

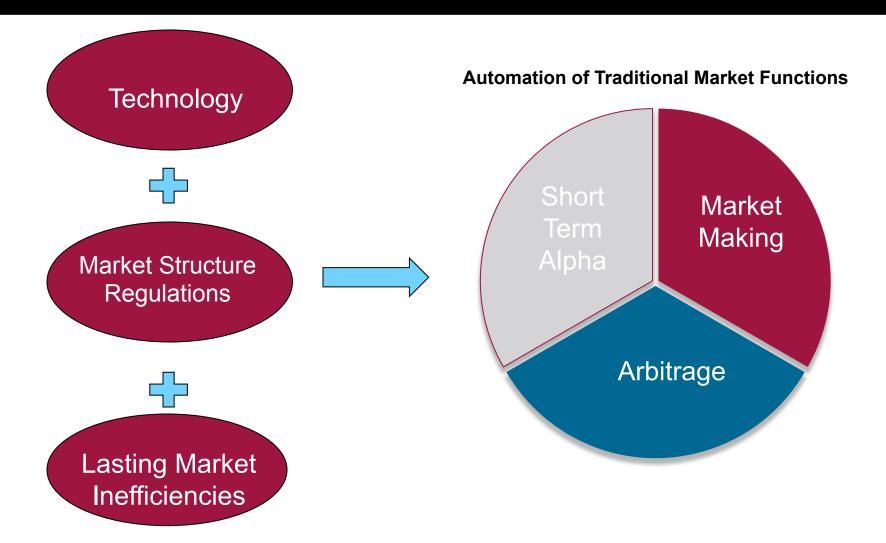
What is HFT really?

Reasons for Emergence of HFT?

Market Quality Impact

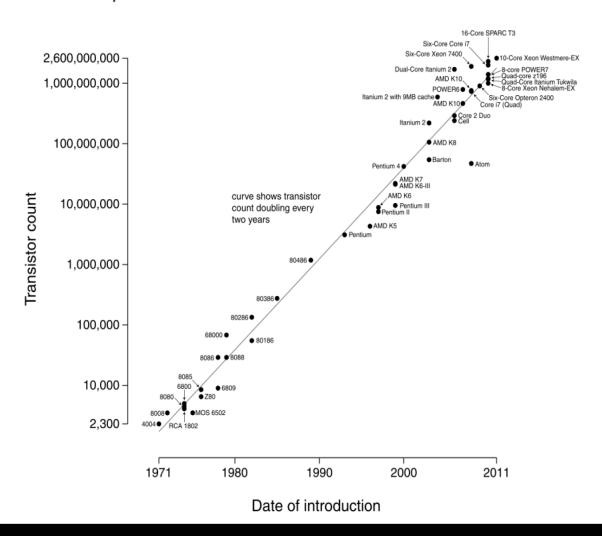
Size of HFT

The growth of High Frequency Trading



Moore's Law

Microprocessor Transistor Counts 1971-2011 & Moore's Law



Technology

Processing Power

- A. Moore's law: Transistor count has doubled every two years for decades
- B. Performance doubled every 18 months
- C. Cheap and easy to process market data for thousands of instruments in real time

Networking and Storage

- A. 10 Gigabit/sec Ethernet
- B. Connectivity across data centers
- C. Petabytes of fast, reliable data storage

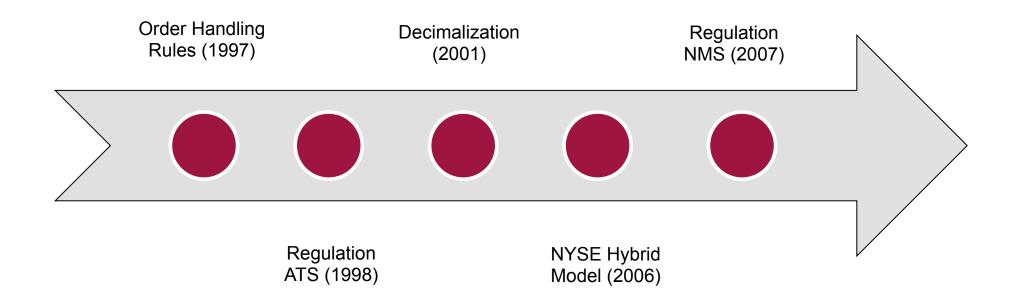
Software

- A. High level programming languages
- B. FIX and other standardized protocols

Algorithms

- A. Statistical techniques
- B. Optimal execution strategies

Market Structure Evolution



Early History

- National Market System: Securities Acts Amendments of 1975
 - A. Vision of unified national market for securities
 - B. Transparent pricing: the NBBO
 - C. Competitive execution landscape
- Order Handling Rules of 1997
 - A. Requires display of best customer price
- Regulation ATS of 1998
 - A. Formalized notion of alternative trading system
 - B. Encouraged proliferation of ECNs in early 2000s (INET, Island, BRUT, ARCA, etc)
 - C. Island introduced two major innovations
 - a) Direct book feeds with order update: ITCH
 - b) Maker-take pricing

Decimalization (2001)

- Definition: minimum price variant is the smallest increment in price in which an instruments can be quoted (or an order entered)
- Before 2001: MPV for stocks was 1/16 or 6.25 cents
- After 2001: MPV lowered to 1 cent
- Not just a cosmetic change. Implications for the market:
 - Ability to improve prices by economically smaller amount discourages posting large orders
 - B. Spread narrows for small orders, but it may be harder to do larger size
 - C. Market makers want to adjust their quotes faster in response

Regulation NMS

- Strengthened and formalized many aspects of existing market structure
 - A. Banned trade-through, so ability to set the NBBO became paramount
 - B. Capped access fees
 - C. Standardized minimum price variants at 0.01 for order above \$1
 - D. Some market data rules...
- Forced the hand of NYSE to adopt a more purely automated system
 - A. We will hear about its implications later

Upshot of all this regulation:

Universal Market Access Greater
Information
Symmetry

Competition among market centers for flow

Emergence of HFT

Reliance on Technology

New types of exploitable opportunities

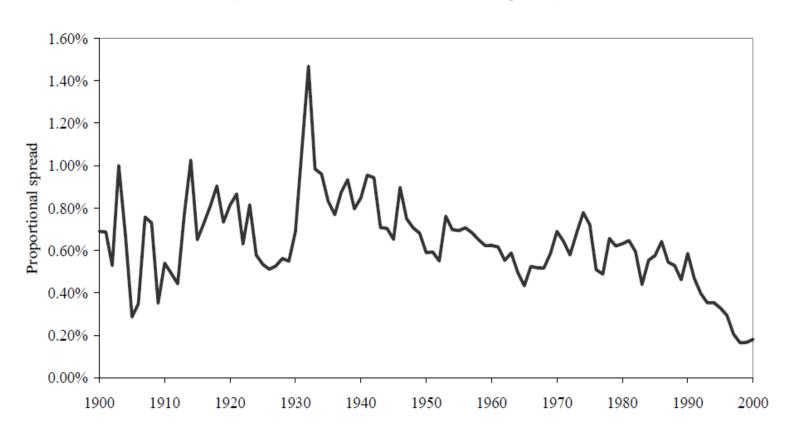
Emergence of new technologies (news feeds) with profound effect on mkt. vol.

Empirical Market Quality Measures

- Transaction costs
 - A. Bid-Ask spread
 - B. Implementation shortfall
- Volatility
- Specific Market Structure Changes

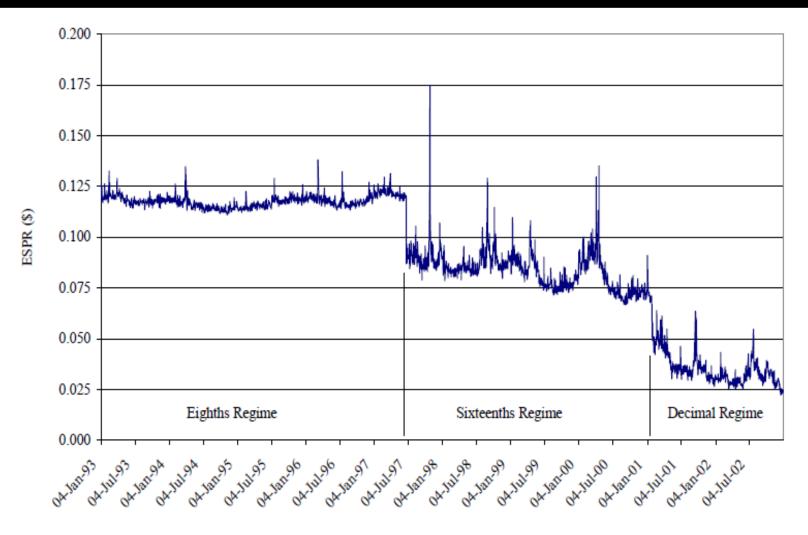
A History of Spreads

Figure 1. Bid-ask spreads on Dow Jones stocks (all DJ stocks 1900-1928, DJIA stocks 1929-present)



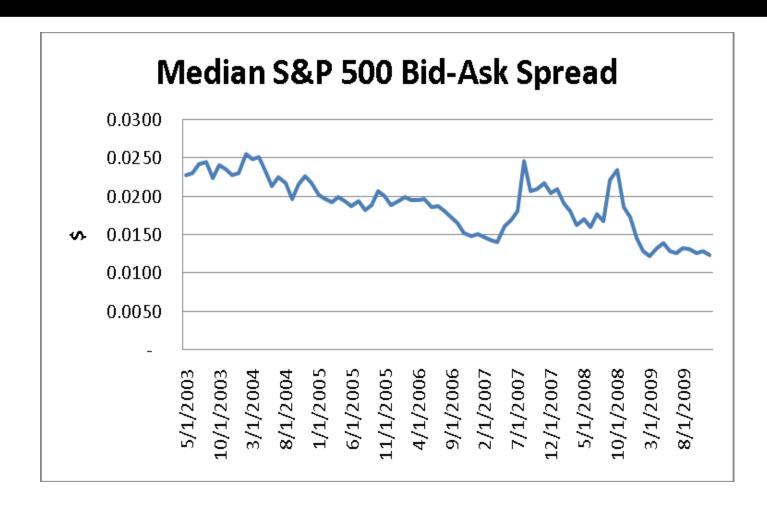
Source: Charles Jones (2002)

Spreads: Impact of MPV Regulation



Source: Chordia, Roll, Subrahmanyam (2008)

Recent Spreads: Impact of Technology

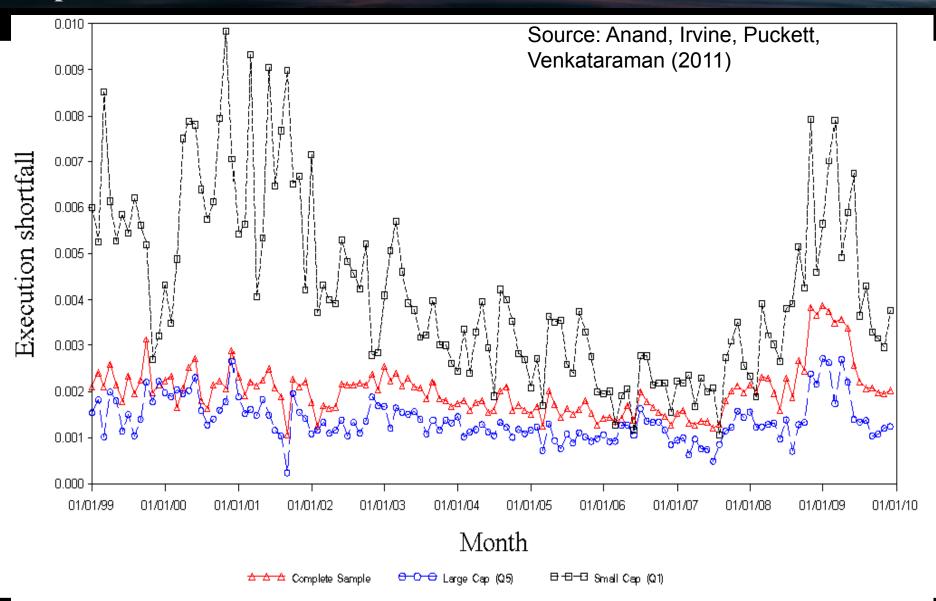


Source: Angel, Harris, Spatt (2010)

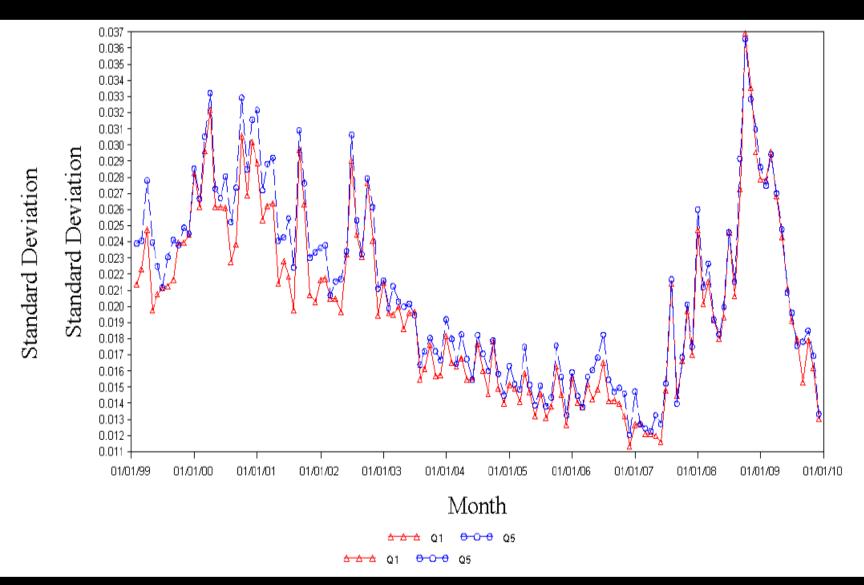
Implementation Shortfall: Institutional Flow Stats (Ancerno)

	Number of Institutions	Number of Stocks	Number of daily orders	Daily order Size	Daily order Size/Avg. daily volume (30 days)	Buy dollar volume/Total dollar volume
Panel A: Full sample						
•	955	8,514	43,293,870	16,165	2.9%	50.7%
			UP 244%	FLAT	DOWN 63%	
Panel B: By year			WF 4447			
1999	324	5,726	2,122,761	14,371	4.8%	51.3%
2000	322	5,502	2,509,332	16,189	3.9%	51.4%
2001	350	4,715	2,754,936	18,672	3.8%	52.0%
2002	380	4,383	3,456,098	19,984	3.7%	51.6%
2003	356	4,320	3,558,992	18,799	3.5%	50.6%
2004	367	4,485	4,497,585	18,658	3.5%	50.9%
2005	336	4,342	3,915,803	16,326	3.1%	50.5%
2006	359	4,321	4,933,460	14,668	2.5%	50.5%
2007	339	4,335	5,013,820	13,733	2.2%	50.0%
2008	296	4,052	5,347,082	14,636	1.8%	49.8%
2009	286	3,938	5,184,001	14,270	1.8%	49.8%
Panel C: Firm size (NYSE	market value quint	iles)				
Small	•	•	4,471,299	11,418	11.1%	53.5%
2			6,064,350	12,402	4.4%	52.9%
3			6,699,324	14,298	2.9%	52.2%
4			8,158,691	17,240	2.0%	50.6%
Large			16,556,470	19,398	0.7%	50.1%

Implementation Shortfall

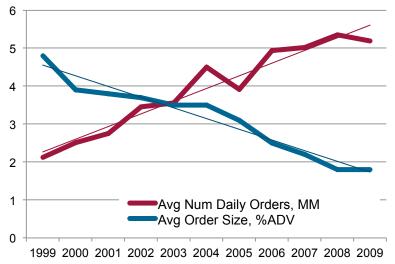


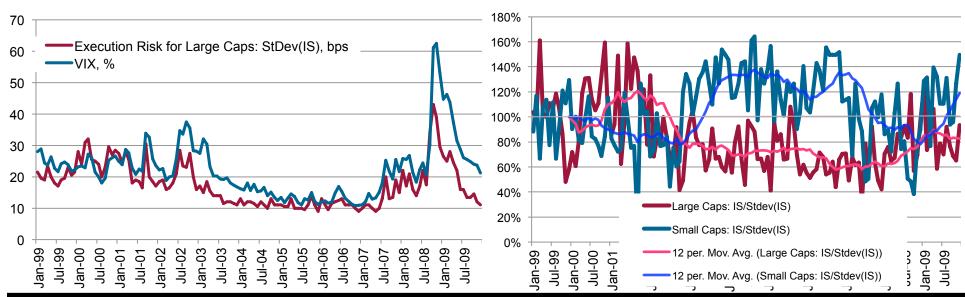
Implementation Shortfall Risk



Implementation Shortfall Normalized. Benefits of Increased Liquidity

- 1. (Institutional turnover) x (Order Size) ≈ Const.
- Buy-side trading is directional → proportional increase in market making. On top increased ETF volumes, which EMMs use as hedges
- Higher Turnover → higher Sharpe (at least in theory).
 Smaller orders → lower execution risk
- E(Cost)~σ√T, Stdev(IS)=σ√T. IS/Stdev(IS) is more or less flat for the last decade (1999-2009)





Impact HTF on Volatility

- 1. No impact on daily volatility HTF are flat by EOD, so this result is hardly surprising
- 2. HTF increase short-term volatility (up to 10 minutes). From our own study:
 - A. In UK short-term volatility is 30% higher for names most traded by HFT
 - B. In Japan from 1H'10 (Arrowhead implementation) to 1H'11 short-term volatility increased ~10% in the names most traded by HFT relative to names not popular with HFT

High Frequency Size and Profitability Estimates

1. Hendershott and Riordan (2011) + Brogaard (2011)

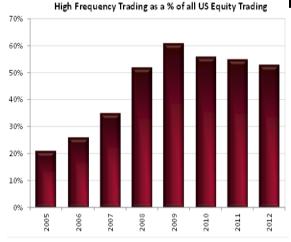
- A. Proprietary NASDAQ data set of 25 of the largest HF traders
- B. HF is 42% of (double counted) volume
- C. Collective profitability is 0.4 bps. Total revenue \$3 billion/year
- D. Not a small number, but far less than the specialist and market makers of mid 1990s (1999: Spear Leeds and Kellogg alone had revenue \$1.7B)

2. Other vague estimates

- A. Kearns et al 2010 assume "aggressive" HFTs have Oracular perfect predictive capability and bound profitability above by \$21 billion USD (probably a wild overestimate by their own admission)
- B. Tabb Group "guesstimate" \$8.5B

Flow Breakdown, US

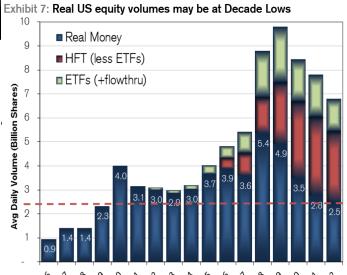
Exhibit 3: Tabb survey says HFT is shrinking faster than real money trading



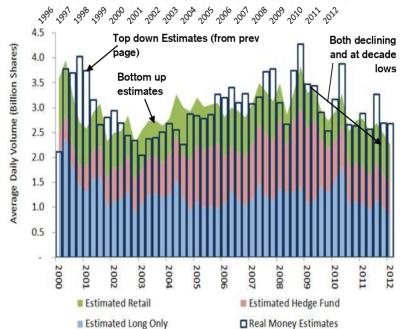
Source: Tabb

Exhibit 4: And all electronic trading has plateaued





Source: Credit Suisse



High Frequency Trading and Long-Term Investors

PROS & CONS OF HFT

- 1. The is no acceptable HFT definition. Yet there is an evidence that HFT is the largest market participant trading 50-60% of reported volumes in US, 40-55% in UK and 35-40% in Japan.
- 2. There is also an indication that top 5 HFT firms are originating majority of HFT volumes globally.
- 3. There is NO consensus on the impact of HFT on the market quality.

Proponents:

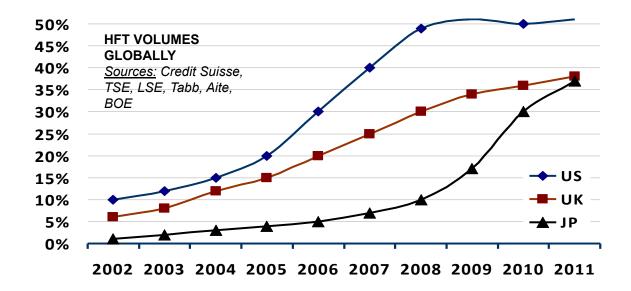
- HFT are EMMs + statarb = liquidity providers, can't be harmful
- They reduce volatility, compress bid-ask spreads = reduce T-Costs for LT and retail
- It is EMMs who are adversely selected by large orders originated by informed LT investors. EMM margins are razor thin (profits are \$2-5B annually, 0.3-0.8bps/trade, 5-15% spread), so have to be quick to re-price quotes

Critics:

- HFT generates most of the profits by front-running LT orders
- Provided liquidity is fictitious. This hurts confidence of slow-to-react LTs.
- HFT contribute to elevated intraday volatility and correlations
- Liquidity is being shifted toward smaller subset of investible universe (which works as self-fulfilling prophecy)

SO, IS THERE TRUTH IN ANY OF THESE STATEMENTS?

Scope



- 1. What are the characteristics of stocks that are actively and rarely traded by HFT?
- 2. How HFT daily volumes correlate with the market volumes and LT investor's volumes?
- 3. Is liquidity demand by LT truly matched by liquidity supply by HFT?
- 4. What are the factors driving daily volumes for HFTs?
- 5. How HFT affect trading costs for a traditional LT investor?

DATA SETS

- 1. AllianceBernstein's trades: orders executed by 5 regional buy-side desks, originated by ~80 PMs (both Value and Growth styles).
- 2. HFT & LT traded volumes for Nikkei 225 & BE500 (Bloomberg European 500), routed via a single broker between January June 2010
 - Europe: daily volumes
 - Japan: sided volumes split into 6 intraday intervals
 - HFTs are defined as users of ultra low latency infrastructure, LTs are users of DMA/DSA/ Crossing platform
- 3. We focus on UK (mature market) and post-Arrowhead Japan (evolving market with rapidly growing HFT presence).
- 4. Within each region we defined *HiVLM*, *LoVLM* subgroups roughly top and bottom tertiles by volume traded. *HiVLM* is validated by volume consistency
- 5. UK 140 names, 50 in *HiVLM*, 50 in *LoVLM*, Japan 225 names 75 & 75 names

TRADING UNIVERSE

HFT Most Traded: Higher Capitalization, Higher Liquidity Group

- 1. UK: HiVLM: share float 5B, LoVLM: 0.5B shares (note, LoVLM stocks are not illiquid, not small caps, far from it)
- 2. HiVLM stocks form the top of major country indices (which are cap-weighted)
- 3. HiVLM stocks have significantly tighter bid-ask spread

HiVLM - UK	Beta	Spread	MDV	HL
HIV LIM - UK	Бета	(bps)	(mln_shares)	(%)
Avg.	1.1	6.6	17.3	2.6
Median	1.0	6.3	5.8	2.1
Std. dev	0.4	2.3	36.6	1.5
LoVLM - UK				
Avg.	1.0	13.7	2.8	2.8
Median	1.0	11.2	1.3	2.3
Std. dev	0.3	7.4	4.1	1.6
<i>HiVLM -</i> JP	Beta	Spread	MDV	HL
HIV LWI - JF	Бета	(bps)	(mln. shares)	(%)
Avg.	1.1	13.1	8.3	2.2
Median	1.2	12.1	3.6	2.0
Std. dev	0.2	6.1	14.5	1.1
LoVLM - JP				
Avg.	1.1	27.1	4.1	2.2
Median	1.1	25.4	2.5	2.0
Std. dev	0.2	12.0	5.0	1.1

TRADING UNIVERSE

HIVLM TRADE CONSISTENTLY, LOVLM TRADE OPPORTUNISTICALLY

<i>HiVLM</i> - UK	Market	HFT	LT
Market			
HFT	(0.40)	1	
LT	0.50	0.28	1

<u>LoVLM - UK</u>	Market	HFT	LT
Market			
HFT	(0.25)	1	
LT	0.37	0.21	1

HiVLM - JP	Market	HFT	LT
Market			
HFT	(0.39)	1	
LT	0.31	0.27	1

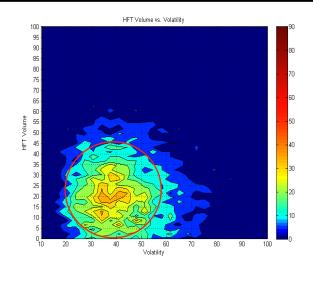
<i>HiVLM</i> - JP	Market	HFT	LT
Market	1		
HFT	0.28	1	
LT	0.22	0.10	1

HiVLM names show much higher correlation of HFT & LT volumes with overall market volume:

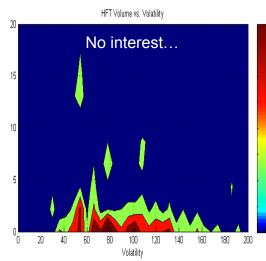
- Underscores consistency of HiVLM flow from both HFT and LT,
- Opportunistic nature of *LoVLM* flow,
- Higher dispersion of *LoVLM* flow among brokers
- Relative to UK, Japan market shows more opportunistic nature of LT flows, but similar consistency for HTF's (similar models?)

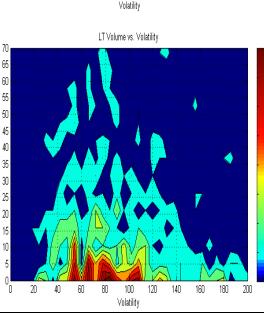
LT VS. HTF: MISMATCHED DEMAND-SUPPLY

JAPANESE MARKET



LT Volume vs. Volatility





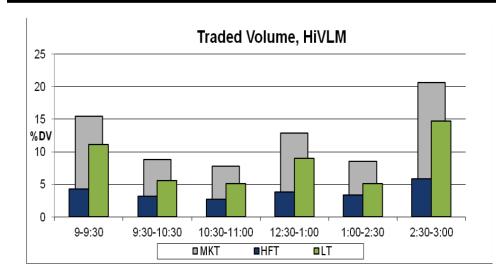
- HiVLM: HFT trade the same range %DV if volatility stays within their comfort zone
- LoVLM: HFT are not there. Period.
- LT: Trade at 5% every day (rebalances). Occasionally trade a lot more. Averse to volatility.

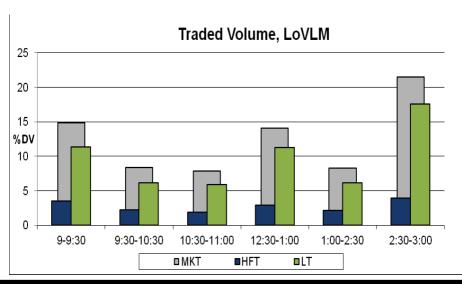
Triggers for LT and HFT volumes:

- LT: driven by fundamentals (such as earnings)
- LT trade less as implied volatility increase
- HFT not driven by fundamentals, but positively correlated with implied volatility
- Both LT and HFT volumes are highly correlated with each other in <u>HiVLM</u> (liquidity begets liquidity)

LT vs. HTF: MISMATCHED VOLUME PROFILES

JAPANESE MARKET





- LT volume profiles are strongly W-shaped:
 - Two price discovery windows
 - High-volume closing session
- HFT's volume profiles are <u>significantly</u> flatter

This means:

- HFT doesn't aim to maximize liquidity provisioning: risk controls take prevalence, informed flow at the open of both sessions is avoided and positions are flat by EOD
- LT may not realize how expensive it is to trade around the open given pronounced one-sidedness of the market.

TRADE "SIDEDNESS"

JAPANESE MARKET - LT TRADE IS CROWDED, HFT TRADES ON BOTH SIDES

<u>HiVLM</u>	HFT BUY	HFT SELL	LT BUY	LT SELL
HFT BUY	1			
HFT SELL	(0.93)	1		
LT BUY	0.21	0.23	1	
LT SELL	0.26	0.25	0.28	1

LoVLM	HFT BUY	HFT SELL	LT BUY	LT SELL
HFT BUY	1			
HFT SELL	(0.79)	1		
LT BUY	0.03	0.04	1	
LT SELL	0.05	0.04	0.16	1

	HiVLM, HFT	<i>HiVLM</i> , LT	LoVLM, HFT	LoVLM, LT
Avg.	(11.08)	52.97	28.58	66.13
Median	7.50	53.76	19.64	74.21
Std. dev	11.96	30.43	26.05	31.51

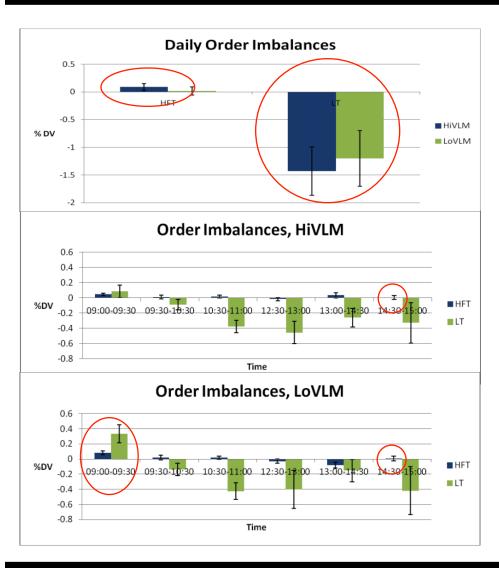
$$Im balance = \frac{Abs(Buy - Sell)}{(Buy + Sell)}$$

$$10\% \approx \frac{|1.2x - x|}{(1.2x + x)} \quad 66\% = \frac{|5x - x|}{(5x + x)}$$

- HFT buy and sell volumes are highly correlated, even in *LoVLM* category
- HFT absolute daily imbalances are very tight in *HiVLM*, much less so in *LoVLM* (different strategies? low trading volumes?)
- This confirms that HFT make markets in select group of highly liquid names.
- Note: This data doesn't preclude the possibility of front-running (it only indicates that HFT are typically flat by EOD)
- As expected, LT trades are one-sided: daily imbalances are high in *HiVLM* names and even higher in *LoVLM* names a source of adverse selection for market-makers.

INTRADAY TRADE IMBALANCE

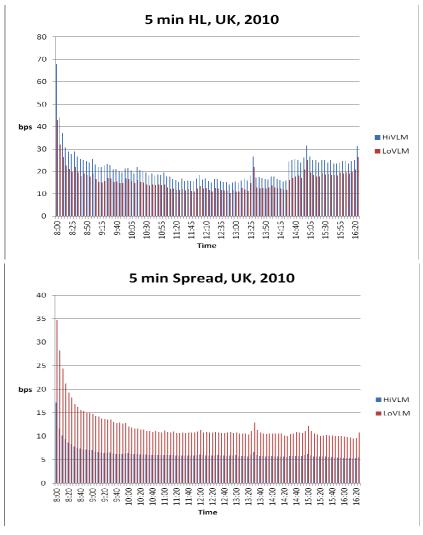
JAPANESE MARKET - HFT FLAT INTRADAY, LT IS NOT



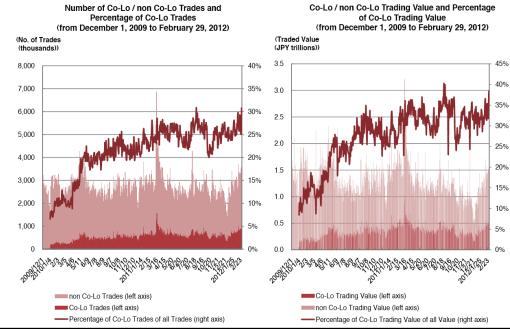
- LT were net-sellers during the 1H 2010 (outflows from Equities, from the region)
- HFT supplied liquidity in *HiVLM* (offsetting LT imbalance, perhaps hedged with futures).
- HFT keeps intraday positions flat (per ticker, making front-running of large orders difficult)
- HFT trade imbalance especially tight around the close positions are flatten before that.
- HFT trade on the same side in the morning (front-running?), although they are late to unwind (stat-arb strategies may still be profitable)

HOW HFT AFFECTS MARKET QUALITY?

UK MARKET - HFT CREATES HIGHER ST VOLATILITY & LOWER SPREADS



- 5-minute HL volatility is 30% higher in HiVLM.
- Bid-ask spread is twice lower.
- These levels are observed with HFT at 40-55% of the market. What is the dynamics in Japan? (HFT grew from 10% in 2010 to



HOW HFT AFFECTS MARKET QUALITY?

JAPANESE MARKET – HFT CREATES HIGHER ST VOLATILITY & LOWER SPREADS

Stock Price, ¥	Tick Size ¥, Before Revision	Tick Size ¥, After Revision
Up to 2,000	1	1
2,000-3,000	5	1
3,000-5,000	10	5
5,000-30,000	10	10
30,000-50,000	50	50
50,000-300,000	100	100
300,000-500,000	1,000	500
500,000-3,000,000	1,000	1,000
3,000,000-5,000,000	10,000	5,000
5,000,000-20,000,000	10,000	10,000
20,000,000-30,000,000	50,000	10,000
30,000,000-50,000,000	100,000	50,000
Over 50,000,000	100,000	100,000

Price Category <=2000 ¥

% Change	Mean	Std. Err.	T-statistics
HL5	9.48	0.28	33.57
HL10	1.79	0.31	5.79
HL30	1.47	0.41	3.59
HL	1.24	1.17	1.06
СО	4.19	3.18	1.32
Quoted spread	-3.33	0.34	-9.76
Quoted spread improvement over tick size	-28.11	0.78	-36.18

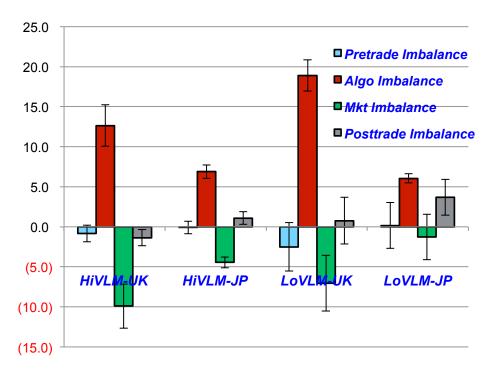
Price Category 2000-5000 ¥

% Change	Mean	Std. Err.	T-statistics
HL5	7.83	0.43	18.08
HL10	1.20	0.45	2.67
HL30	-0.23	0.57	-0.41
HL	0.03	1.10	0.02
CO	1.00	2.76	0.36
Quoted spread	-11.55	0.68	-16.96
Quoted spread improvement over tick size	-26.48	0.60	-44.06

- Market in flux: Arrowhead implementation, colocation facilities, minimum tick size reduction
- Same plots for UK don't work: tick size in LoVLM created artificially high ST-σ (bid-ask bounce) above fundamentals
- Employed DID (difference-in-difference) method: volatility in *LoVLM* is control variable, volatility in *HiVLM* is dependent variable
- 5- & 10-minute σ is up, daily volatility didn't change, quoted spread is down, quotes adjust much faster (less time spread > 1 tick)
- 8-9% increase is the slope (change in ST-σ over 1 year). In UK the difference in ST-σ is 30% between *HiVLM* and *LoVLM*

HFT: Liquidity Provision? Front-Running?

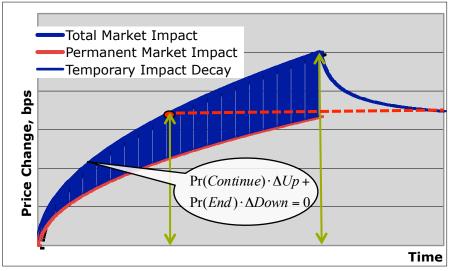
AB TRADED UNIVERSE

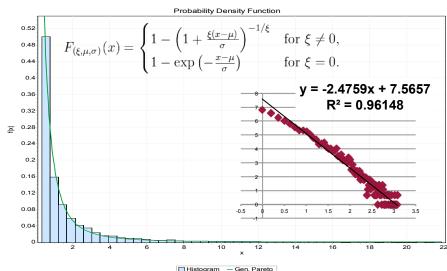


- Front-running: expecting same-side imbalance pre- or in-trade (first 5 min), reversal right after the trade. Observe:
- No pre-trade imbalance
- Offsetting in-trade imbalance in *HiVLM*, less so in *LoVLM*
- No post-trade imbalance
- On aggregate open-to-close return is flat (non-toxic flow) more profitable to provide liquidity
- In general, on average LT flow is non-toxic. (ITG, AbelNoser). Intuitively: annual <u>relative</u> out performance in top quartile is 2-3%. Median is 0 to mildly negative (T-costs). LT tend to trade aggressively as traders are not compensated to take risk.

HFT: LIQUIDITY PROVISION? FRONT-RUNNING?

MARKET MAKING MODELS





- On average LT flow is non-toxic. (ITG, AbelNoser). Intuitively: annual <u>relative</u> out performance in top quartile is 2-3%. Median is 0 to mildly negative (T-costs).
- Despite low alpha, LT orders are traded aggressively (average rate 10-20%), as traders are not compensated to take risk, which causes significant temporary impact.
- Vast majorly of institutional parent orders are small, market impact ~ bid-ask spread
- EMMs don't have risk appetite to carry open positions long enough to profit from front-running more then they would have profited scalping. EMMs do profit trading the reversion (which is fast ~5-10 minutes on daily orders)

HFT IMPACT ON TRADING COSTS

AB TRADED UNIVERSE

UK	Shortfall	Pretrade	Market Return	Daily Average 5 min HL	VX2	HFT	Time of Day
Shortfall	1						
Pretrade: E(Cost)	0.08	1					
Market Return	0.26	-0.02	1				
Daily average 5 min HL volatility	0.05	0.15	0.00	1			
VX2	-0.01	0.19	-0.01	0.30	1		
HFT	-0.03	-0.25	0.00	0.11	0.02	1	
Time of Day	0.03	-0.15	0.01	-0.03	-0.08	0.01	1

JP	Shortfall	Pretrade	Market Return	Daily Average 5 min HL	VXJ	HFT
Shortfall	1					
Pretrade: E(Cost)	0.10	1				
Market Return	0.19	-0.03	1			
Daily average 5 min HL volatility	0.03	0.30	-0.01	1		
VXJ	-0.02	0.02	-0.01	0.33	1	
HFT	-0.04	-0.31	-0.02	0.32	0.02	1

Variable	Coefficient	Std. Err.	T-statistics	95%	· CI
Pretrade: E(Cost)	0.0890	0.0158	5.62	0.0573	0.1208
HFT presence	-0.0755	0.0169	-4.45	-0.1094	-0.0415
Market Return	0.2933	0.0108	26.94	0.2715	0.0315
Daily average 5 min HL volatility	0.0230	0.0278	0.82	-0.0326	0.0786
Constant term	0.0193	0.0213	0.91	-0.0224	0.0610

Variable	Coefficient	Std. Err.	T-statistics	95% CI
Pretrade: E(Cost)	0.0783	0.0117	6.66	0.0550 0.1015
HFT presence	-0.1023	0.0126	-8.07	-0.1274 0.0771
Market Return	0.2328	0.0163	14.24	0.2004 0.2652
Daily average 5 min HL volatility	-0.0354	0.0203	-1.74	-0.0757 0.0047
Constant term	-0.0558	0.0147	3.78	0.0269 0.0847

- How HFT presence and ST-σ affect [IS-E(cost)], adjusted by broad market momentum?
- Side-adjusted market return is the largest factor positively correlated with [IS-E(cost)]
- HFT presence is negatively correlated with [IS-E(cost)] reducing T-costs through compressed realized spread and reduction of relative price dislocations.
- ST-σ adversely affects [IS-E(cost)] in UK. On our sample its impact is not statistically significant

CONCLUSION

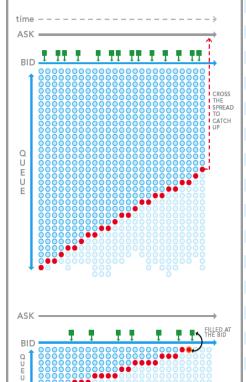
■ HFT activity is concentrated in a subset of liquid mega-cap names. This creates a self-fulfilling prophecy:

JP, \$10M positions (\$0.5-1B portfolio). Tracking to Topix/Nikkei ~4-5%			UK, \$10M pc	sitions (\$0.	5-1B port	folio). Trackin	g to FTSE10	0/250 ~4%			
	Cost	Risk	RiskAdjCost	Risk Bid	%ADV		Cost	Risk	RiskAdjCost	Risk Bid	%ADV
HiVLM	48	91	. 96	97	20	HiVLM	18	63	51	72	12
LoVLM	101	146	178	158	79	LoVLM	42	178	135	114	74
delta	53		81	61		delta	24		84	42	
JP, \$50M positions (\$2.5-5B portfolio). Tracking to Topix/Nikkei ~4-5%											
JP, \$50M p	ositions (\$2	2.5-5B por	rtfolio). Tracki	ng to Topix/I	Nikkei ~4-5%	UK, \$50M pc	ositions (\$2.	5-5B port	folio). Trackin	g to FTSE10	0/250 ~4%
JP, \$50M p	oositions (\$2 Cost	2 .5-5B por Risk	r tfolio). Tracki RiskAdjCost	ng to Topix/I Risk Bid	Nikkei ~4-5% %ADV	UK, \$50M pc	ositions (\$2. Cost	5-5B port Risk	folio). Trackin RiskAdjCost	g to FTSE10 Risk Bid	0/250 ~4% %ADV
JP, \$50M p	• •	•	RiskAdjCost			UK, \$50M pc <i>HiVLM</i>	••	•	RiskAdjCost	Ū	•
	Cost	Risk	RiskAdjCost 237	Risk Bid	%ADV		Cost	Risk	RiskAdjCost 96	Risk Bid	%ADV

- HFT is predominantly involved in market making. We didn't find any evidence of front-running.
- HFT is not serving liquidity on LT terms: mismatch between liquidity demand and supply.
- Smaller players are displaced by a few large EMMs. HTF liquidity is not additive there is only so much LT: (1H'10-1H'12: TSE volumes down 17-20%, inline with 15% weight drop of Japan in MSCI)
- This environment heightens liquidity risk for LT. Leads to compressed bid-ask spreads/higher ST-volatility. Net outcome for T-cost depends on the type of the flow.
- Our own trades: net cost reduction due to liquidity provisioning. This should be the outcome for majority of LT, although certain strategies are disadvantaged: Value orders, larger high-alpha orders. Retail benefits.
- How LT should adopt? Align order sizing and aggressiveness with underlying alpha. Optimize interaction with uncorrelated (non-EMM) liquidity. Be flexible in less liquid names.

Passive Trading in Mega-Liquid names

This schematic shows a limit order's journey through the time priority queue of a limit order book, and how longer queues can interfere with passive trading.



MARKET ORDER FROM OPPOSING SIDE

O POSTED ORDER AHEAD OF ALGO ORDER

ORDERS POSTED BEHIND ALGO ORDER

TICKER	ADV (MSHARES)	QUEUE LENGTH (SHARES)	SPREAD (CENTS)	15-MIN VOLATILITY (%)	QUEUE DEPLETION TIME (S)
BAC	190.3	558,925	1.0	0.41	138
SPY	161.1	30,237	1.0	0.12	9
XLF	89.6	2,574,847	1.0	0.19	1345
FB	74.5	22,296	1.3	0.91	14
EEM	60.9	82,727	1.0	0.16	64
JPM	56.8	13,250	1.0	0.30	11
VXX	56.4	11,852	1.0	0.57	10
SIRI	53.8	1,021,571	1.0	0.45	920
ggg	50.2	63,295	1.0	0.15	59
IWM	48.7	15,158	1.0	0.19	15
csco	47.3	84,527	1.0	0.23	85
MSFT	45.6	40,857	1.0	0.20	42
F	43.8	132,213	1.0	0.31	141 96
GE S	43.8 43.5	89,467 422,473	1.0	0.20 0.58	456
C	41.9	14,347	1.0	0.37	16
снк	38.6	10,778	1.0	0.52	13
INTC	36.9	35,485	1.0	0.22	45
NOK	32.2	430,861	1.0	0.37	627
PFE	30.9	58,008	1.0	0.19	88
мѕ	29.7	24,323	1.0	0.43	38
WFC	29.4	14,728	1.0	0.26	23
ORCL	29.3	22,414	1.0	0.26	36
MU	27.9	94,524	1.0	0.52	159
ZNGA	25.7	16,315	1.0	0.82	30
Т	25.4	33,937	1.0	0.14	63
DELL	23.6	53,863	1.0	0.26	107
vwo	22.8	43,736	1.0	0.15	90
VALE	21.9	23,396	1.0	0.31	50
TZA	21.8	11,200	1.1	0.56	24
EFA	21.8	34,171	1.0	0.14	73
EMC	21.7	23,829	1.0	0.25	52
SDS	21.0	316,091	1.0	0.24	706
AA HPQ	21.0 20.7	100,122	1.0	0.32 0.27	224 46
GDX	20.7	20,302 4,984	1.1	0.27	11
EWZ	20.3	5,748	1.0	0.32	13
RF	20.2	134,203	1.0	0.45	311
LOW	20.0	11,869	1.0	0.26	28
FAZ	19.3	7,236	1.1	0.50	18
FXI	19.2	22,049	1.0	0.17	54
үноо	18.9	36,246	1.0	0.29	90
XLI	17.7	169,464	1.0	0.16	447
NWSA	17.5	26,692	1.0	0.24	71
AAPL	17.5	416	14.3	0.25	1

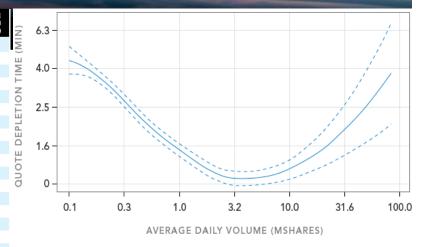


FIGURE 2
Average queue depletion time versus ADV*.

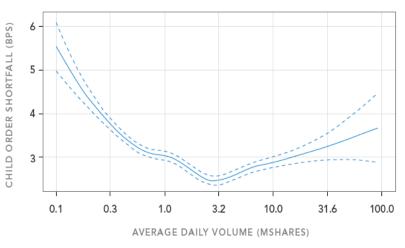


FIGURE 3

Average child order shortfall versus ADV*.

Source: PragmaTrading (Dr. Eran Fisher)

POSTED ALGO ORDER

Literature

Good Overview of Existing Literature:

Charles M Jones "What do we know about high-frequency trading" http://papers.ssrn.com/sol3/papers.cfm?abstract_id=2236201

Interesting Recent Paper:

Johannes Breckenfelder "Competition of High-Frequency Market Makers and Market Quality" http://people.stern.nyu.edu/jhasbrou/SternMicroMtg2013/Papers/CompetHFMktMkrs.pdf