



$$\boxed{v_4 = v_3 = v_5}$$

$$\begin{cases} v_4 (sC + G_1 + G_2) = v_5 G_2 + v_i sC \\ 2v_3 = v_o + v_2 \Rightarrow \boxed{v_2 = 2v_3 - v_o} \quad (2) \\ (sC + G) v_5 = v_i G + v_o sC \Rightarrow v_5 = v_i \frac{G}{sC + G} + v_o \frac{sC}{sC + G} \end{cases}$$

(1) & (2) & (3)

$$\begin{cases} v_5 (sC + G_1 + G_2) = 2v_3 G_2 - v_o G_2 + v_i sC \\ v_i \left(\frac{G}{sC + G} \right) + v_o \left(\frac{sC}{sC + G} \right) (sC + G_1 + G_2) = G_2 (2v_3 - v_o) + v_i sC \end{cases}$$

↓

$$v_o \left(\frac{s^2 C^2 + sC(G_1 + G_2)}{sC + G} + G_2 - \frac{sC G_2}{sC + G} \right) = v_i \left(\frac{2G G_2}{(sC + G)} + sC - \frac{sC(G_1 + G_2)}{(sC + G)} \right)$$

$$v_o \left(\frac{s^2 C^2 + sC(G_1 + sC G_2 + sC G_2 + G G_2 - sC G_2)}{(sC + G)} \right) = v_i \frac{2G G_2 + s^2 C^2 + sC G_2 - sC(G_1 + G_2)}{(sC + G)}$$

$$\frac{v_o}{v_i} = \frac{s^2 C^2 + (G G_2 - G G_1 - G G_2)}{s^2 C^2 + sC G_1 + sC G_2 + G G_2}$$

$$\frac{V_o}{V_i} = \frac{s^2 + \left(\frac{G G_2}{C^2} - \frac{G G_1}{C^2} \right)}{s^2 + s \left(\frac{G_1}{C} + \frac{G_2}{C} \right) + \frac{G G_2}{C^2}}$$

$$\frac{V_o}{V_i} = \frac{s^2 + \left(\frac{1}{R R_2 C^2} - \frac{1}{R R_1 C^2} \right)}{s^2 + s \left(\frac{1}{R_1 C} + \frac{1}{R_2 C} \right) + \frac{1}{R R_2 C^2}}$$

$$\omega_o^2 = \frac{1}{R R_2 C^2}$$

$$\frac{\omega_o}{Q} = \left(\frac{1}{R_1 C} + \frac{1}{R_2 C} \right)$$

$$\omega_N = \frac{1}{R R_2 C^2} - \frac{1}{R R_1 C^2}$$

$$\left(\omega_N = \omega_o^2 - \frac{1}{R R_1 C^2} \right)$$

$$\omega_N = \omega_o^2 \left(1 - \frac{1}{R R_1 C^2} \right)$$