- 1. (1 point) Give two examples why low-rank approximation of matrices is important for data science
- 2. (1 point) What is singular value decomposition?
- 3. (1 point) State one difference between the non-negative matrix factorization and singular value decomposition.
- 4. (1 point) What is biclustering?
- 5. (1 point) What is the similarity between histograms and kernel density estimation?
- 6. The following is an outcome of applying SVD on a small data set D of movie ratings of 7 people on 5 movies, to approximate D as  $U_k^*S_k^*V_k^T$ .

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- a) (1 point) What is the value of k in this example?
- b) (3 points) What can you conclude by looking at the first column of U and V? What can you conclude by looking at the second column?
- c) (1 point) How important is the third column of U and V?