## 5 Model Training and Tuning

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# 5.1 Model Training and Parameter Tuning

The caret package has several functions that attempt to streamline the model building and evaluation process.

The train function can be used to

- evaluate, using resampling, the effect of model tuning parameters on performance
- choose the "optimal" model across these parameters
- estimate model performance from a training set

First, a specific model must be chosen. Currently, 237 are available using caret; see train Model List or train Models By Tag for details. On these pages, there are lists of tuning parameters that can potentially be optimized. User-defined models can also be created.

The first step in tuning the model (line 1 in the algorithm below) is to choose a set of parameters to evaluate. For example, if fitting a Partial Least Squares (PLS) model, the number of PLS components to evaluate must be specified.

```
1 Define sets of model parameter values to evaluate
2 for each parameter set do
      for each resampling iteration do
         Hold-out specific samples
4
         [Optional] Pre-process the data
5
         Fit the model on the remainder
6
         Predict the hold-out samples
7
8
      Calculate the average performance across hold—out predictions
9
10 end
11 Determine the optimal parameter set
12 Fit the final model to all the training data using the optimal parameter set
```

Once the model and tuning parameter values have been defined, the type of resampling should be also be specified. Currently, *k*-fold cross-validation (once or repeated), leave-one-out cross-validation and

bootstrap (simple estimation or the 632 rule) resampling methods can be used by train. After resampling, the process produces a profile of performance measures is available to guide the user as to which tuning parameter values should be chosen. By default, the function automatically chooses the tuning parameters associated with the best value, although different algorithms can be used (see details below).

## 5.2 An Example

The Sonar data are available in the mlbench package. Here, we load the data:

```
library(mlbench)
data(Sonar)
str(Sonar[, 1:10])
```

```
'data.frame':
                    208 obs. of 10 variables:
##
##
    $ V1 : num
                0.02 0.0453 0.0262 0.01 0.0762 0.0286 0.0317 0.05
##
    $ V2 : num
                0.0371 0.0523 0.0582 0.0171 0.0666 0.0453 0.0956
                0.0428 0.0843 0.1099 0.0623 0.0481 ...
##
    $ V3 : num
                0.0207 0.0689 0.1083 0.0205 0.0394 ...
##
    $ V4 : num
                0.0954 0.1183 0.0974 0.0205 0.059 ...
##
    $ V5 : num
##
   $ V6 : num
                0.0986 0.2583 0.228 0.0368 0.0649 ...
    $ V7 : num
##
                0.154 0.216 0.243 0.11 0.121 ...
                0.16 0.348 0.377 0.128 0.247 ...
##
    $ V8 : num
                0.3109 0.3337 0.5598 0.0598 0.3564 ...
##
    $ V9 : num
    $ V10: num
                0.211 0.287 0.619 0.126 0.446 ...
##
```

The function createDataPartition can be used to create a stratified random sample of the data into training and test sets:

```
library(caret) inTraining得到的是随机从208个数据总体中抽取的0.75training data 即157个索引值(排过序但不是连续数字)

inTraining <- createDataPartition(Sonar$Class, p = .75, list = FAI training <- Sonar[inTraining,]

testing <- Sonar[-inTraining,]
```

We will use these data illustrate functionality on this (and other) pages.

## 5.3 Basic Parameter Tuning

By default, simple bootstrap resampling is used for line 3 in the algorithm above. Others are available, such as repeated *K*-fold cross-validation, leave-one-out etc. The function trainControl can be used to specify the type of resampling:

```
fitControl <- trainControl(## 10-fold CV

    method = "repeatedcv",

    number = 10,

    ## repeated ten times

    repeats = 10)</pre>
```



More information about trainControl is given in a section below.

The first two arguments to train are the predictor and outcome data objects, respectively. The third argument, method, specifies the type of model (see train Model List or train Models By Tag). To illustrate, we will fit a boosted tree model via the gbm package. The basic syntax for fitting this model using repeated cross-validation is shown below:

```
## Stochastic Gradient Boosting
##
## 157 samples
                    157行60列的training data
                    class有两种
    60 predictor
##
      2 classes: 'M',
##
## No pre-processing
## Resampling: Cross-Validated (10 fold, repeated 10 times)
## Summary of sample sizes: 141, 141, 142, 141, 141, 142, ...
## Resampling results across tuning parameters:
    depth的1,2,3和n.trees的50,100,150是train默认值
                                            plot(abmFit1)
##
    吗?后面expand.grid赋值给了train(..., tuneGrid())
                                            可以观察的更明显, interaction=3, n.trees=150时
                                            accuracy最高
##
      interaction.depth
                            n.trees
                                        Accuracy
                                                     Kappa
                                                                 kappa计算结果为-1~1,但
                                                                 通常kappa是落在 0~1 间,
##
      1
                              50
                                        0.7876495
                                                     0.5712306
                                                                 可分为五组来表示不同级别
                                                                 的一致性: 0.0~0.20极低的
                             100
                                        0.7957794
##
      1
                                                     0.5867732
                                                                 一致性(slight)、0.21~0.40
                                                                  -般的一致性(fair)、
                                                                0.41~0.60 中等的一致性
##
      1
                             150
                                        0.8140441
                                                     0.6235694
                                                                 (moderate)、0.61~0.80 高
                                                                 度的一致性(substantial)和
      2
                                        0.8073676
##
                              50
                                                     0.6101031
                                                                 0.81~1几乎完全一致(almost
                                                                 perfect).
##
      2
                             100
                                        0.8158211
                                                     0.6263183
                                                                 kappa=(po-pe)/(1-pe)
                                                                 po是每一类正确分类的样本
      2
                             150
                                        0.8244608
                                                     0.6441406
##
                                                                 数量之和除以总样本数,也
                                                                 就是总体分类精度
                                                                 假设每一类的真实样本个数
##
      3
                              50
                                        0.8167843
                                                     0.6294107
                                                                 分别为a1,a2,...,aC
                                                                 而预测出来的每一类的样本
      3
                                        0.8251127
                                                     0.6458154
##
                             100
                                                                 个数分别为b1,b2,...,bC
                                                                 总样本个数为n
                                                     0.6522968
                                                                 则有:pe=a1 x b1+a2 x b2
##
      3
                             150
                                        0.8284510
                                                                 +...+aC × bC / n × n
##
```

## Tuning parameter 'shrinkage' was held constant at a value of 0
##

## Tuning parameter 'n.minobsinnode' was held constant at a value ## Accuracy was used to select the optimal model using the larges.

```
## The final values used for the model were n.trees = 150,
## interaction.depth = 3, shrinkage = 0.1 and n.minobsinnode = 10
```

For a gradient boosting machine (GBM) model, there are three main tuning parameters:

- <u>number of iterations</u>, i.e. trees, (called <u>n.trees</u> in the gbm function)
- complexity of the tree, called <u>interaction.depth</u>
- learning rate: how quickly the algorithm adapts, called <a href="shrinkage">shrinkage</a>
- the minimum number of training set samples in a node to commence splitting ( n.minobsinnode )

The default values tested for this model are shown in the first two columns ( shrinkage and n.minobsinnode are not shown beause the grid set of candidate models all use a single value for these tuning parameters). The column labeled "Accuracy" is the overall agreement rate averaged over cross-validation iterations. The agreement standard deviation is also calculated from the cross-validation results. The column "Kappa" is Cohen's (unweighted) Kappa statistic averaged across the resampling results. <a href="train">train</a> works with specific models (see train Model List or train Models By Tag). For these models, train can automatically create a grid of tuning parameters. By default, if p is the number of tuning parameters, the grid size is 3^p. As another example, regularized discriminant analysis (RDA) models have two parameters ( gamma and lambda ), both of which lie between zero and one. The default training grid would produce nine combinations in this two-dimensional space.

There is additional functionality in train that is described in the next section.

## 5.4 Notes on Reproducibility

Many models utilize random numbers during the phase where parameters are estimated. Also, the resampling indices are chosen using random numbers. There are two main ways to control the randomness in order to assure reproducible results.

- There are two approaches to ensuring that the same <code>resamples</code> are used between calls to <code>train</code>. The first is to use <code>set.seed</code> just prior to calling <code>train</code>. The first use of random numbers is to create the resampling information. Alternatively, if you would like to use specific splits of the data, the <code>index</code> argument of the <code>trainControl</code> function can be used. This is briefly discussed below.

  Index a list with elements for each resampling iteration. Each list element is a vector of integers corresponding to the rows used for training at that iteration.
- When the models are created *inside of resampling*, the seeds can also be set. While setting the seed prior to calling train may guarantee that the same random numbers are used, this is unlikely to be the case when parallel processing is used (depending which technology is utilized). To set the model fitting seeds, trainControl has an additional argument called seeds that can be used. The value for this argument is a list of integer vectors that are used as seeds. The help page for trainControl describes the appropriate format for this option.

seeds an optional set of integers that will be used to set the seed at each resampling iteration. This is useful when the models are run in parallel. A value of NA will stop the seed from being set within the worker processes while a value of NULL will set the seeds using a random set of integers. Alternatively, a list can be used.

How random numbers are used is highly dependent on the package author. There are rare cases where the underlying model function does not control the random number seed, especially if the computations are conducted in C code. Also, please note that some packages load random numbers when loaded (directly or via namespace) and this may effect reproducibility.

# 5.5 Customizing the Tuning Process

There are a few ways to customize the process of selecting tuning/complexity parameters and building the final model.

## **5.5.1 Pre-Processing Options**

As previously mentioned, train can pre-process the data in various ways prior to model fitting. The function preprocess is automatically used. This function can be used for centering and scaling, imputation (see details below), applying the spatial sign transformation and feature extraction via principal component analysis or independent component analysis.

To specify what pre-processing should occur, the <u>train</u> <u>function has</u> <u>an argument called preProcess</u>. This argument takes a character string of methods that would normally be passed to the method

argument of the preProcess function. Additional options to the preProcess function can be passed via the trainControl function.

These processing steps would be applied during any predictions generated using <a href="mailto:predict.train">predict.train</a>, <a href="mailto:extractPrediction">extractPrediction</a> or <a href="mailto:extractProbs">extractProbs</a> (see details later in this document). The pre-processing would **not** be applied to predictions that directly use the object\$finalModel Object.

For imputation, there are three methods currently implemented:

- <u>k-nearest neighbors</u> takes a sample with missing values and finds the *k* closest samples in the training set. The average of the *k* training set values for that predictor are used as a substitute for the original data. When calculating the distances to the training set samples, the predictors used in the calculation are the ones with no missing values for that sample and no missing values in the training set.
- another approach is to fit a <u>bagged tree model</u> for each predictor using the training set samples. This is usually a fairly accurate model and can handle missing values. When a predictor for a sample requires imputation, the values for the other predictors are fed through the bagged tree and the prediction is used as the new value. This model can have significant computational cost.
- the <u>median</u> of the predictor's training set values can be used to estimate the missing data.

If there are missing values in the training set, PCA and ICA models only use complete samples.

## **5.5.2 Alternate Tuning Grids**

The tuning parameter grid can be specified by the user. The argument tuneGrid can take a data frame with columns for each tuning parameter. The column names should be the same as the fitting function's arguments. For the previously mentioned RDA example, the names would be gamma and lambda. train will tune the model over each combination of values in the rows.

For the boosted tree model, we can fix the learning rate and evaluate more than three values of n.trees:

```
gbmGrid <- expand.grid(interaction.depth = c(1, 5, 9),</pre>
                           n.trees = (1:30)*50,
                           shrinkage = 0.1,
                           n.minobsinnode = 20)
nrow(gbmGrid)
set.seed(825)
                                                        扩大interaction depth & n trees 用于
                                                        cross validation 看 accuracy &
gbmFit2 <- train(Class ~ ., data = training,</pre>
                                                        kappa取最大
                   method = "gbm",
                   trControl = fitControl,
                   verbose = FALSE,
                   ## Now specify the exact models
                   ## to evaluate:
                   tuneGrid = gbmGrid)
```

gbmFit2

```
## Stochastic Gradient Boosting
##
## 157 samples
    60 predictor
##
    2 classes: 'M', 'R'
##
##
## No pre-processing
## Resampling: Cross-Validated (10 fold, repeated 10 times)
## Summary of sample sizes: 141, 141, 142, 141, 141, 142, ...
## Resampling results across tuning parameters:
##
     interaction.depth n.trees Accuracy Kappa
##
                           50
                                  0.77
                                             0.54
##
     1
                                  0.80
     1
                          100
                                             0.59
##
                                  0.81
                                             0.62
##
     1
                          150
                                  0.82
     1
                          200
                                             0.64
##
                          250
                                  0.82
                                             0.64
##
     1
     1
                          300
                                  0.82
                                             0.64
##
##
                                  •
                                             •
     :
                          :
     9
                         1350
                                  0.84
                                             0.68
##
                                  0.84
##
     9
                         1400
                                             0.68
     9
                                  0.84
                                             0.68
##
                         1450
##
     9
                         1500
                                  0.84
                                             0.68
##
## Tuning parameter 'shrinkage' was held constant at a value of 0
##
```

## Tuning parameter 'n.minobsinnode' was held constant at a value

```
## Accuracy was used to select the optimal model using the larges
## The final values used for the model were n.trees = 350,
## interaction.depth = 9, shrinkage = 0.1 and n.minobsinnode = 20
```

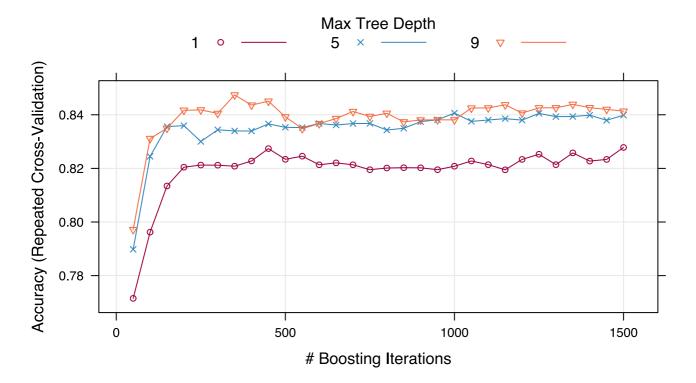
Another option is to use a random sample of possible tuning parameter combinations, i.e. "random search" (pdf). This functionality is described on this page.

To use a random search, use the option search = "random" in the call to trainControl. In this situation, the tuneLength parameter defines the total number of parameter combinations that will be evaluated.

## 5.5.3 Plotting the Resampling Profile

The plot function can be used to examine the relationship between the estimates of performance and the tuning parameters. For example, a simple invokation of the function shows the results for the first performance measure:

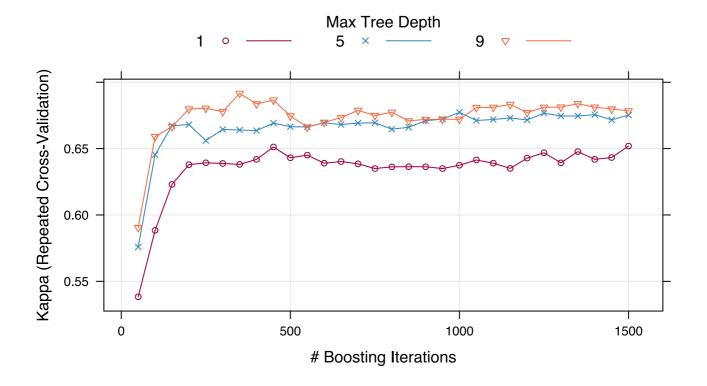
```
trellis.par.set(caretTheme())
plot(gbmFit2)
```



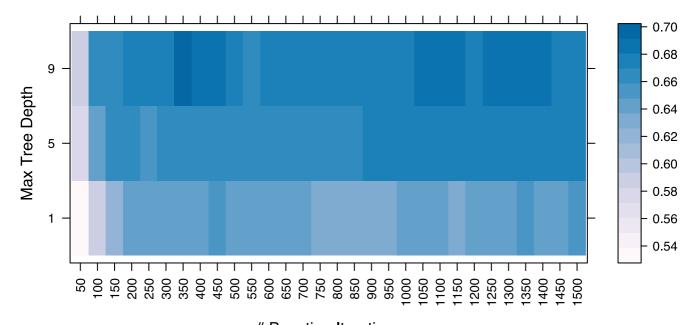
### Other performance metrics can be shown using the metric option:

```
trellis.par.set(caretTheme())
plot(gbmFit2, metric = "Kappa")

默认metric=accuracy
```



Other types of plot are also available. See <code>?plot.train</code> for more details. The code below shows a heatmap of the results:

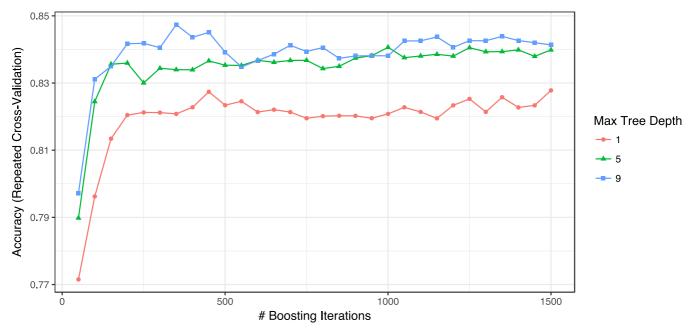


# Boosting Iterations
Kappa (Repeated Cross-Validation)

A ggplot method can also be used:

ggplot(gbmFit2)





There are also plot functions that show more detailed representations of the resampled estimates. See ?xyplot.train for more details.

From these plots, a different set of tuning parameters may be desired. To change the final values without starting the whole process again, the update.train can be used to refit the final model. See ?

update.train

update allows a user to over-ride the tuning parameter selection process by specifying a set of tuning parameters or to update the model object to the latest version of this package. d=

#### trainControl Function 5.5.4 The

update(object, param = NULL, ...)

The function trainControl generates parameters that further control how models are created, with possible values:

method : The resampling method: "boot" , "cv" , "LOOCV" , "LGOCV", "repeatedcv", "timeslice", "none" and "oob". The last value, out-of-bag estimates, can only be used by random forest, bagged trees, bagged earth, bagged flexible discriminant analysis, or conditional tree forest models. GBM models are not included (the gbm package maintainer has indicated that it would

not be a good idea to choose tuning parameter values based on the model OOB error estimates with boosted trees). Also, for leave-one-out cross-validation, no uncertainty estimates are given for the resampled performance measures.

- number and repeats: number controls with the number of folds in K-fold cross-validation or number of resampling iterations for bootstrapping and leave-group-out cross-validation. repeats applied only to repeated K-fold cross-validation. Suppose that method = "repeatedcv", number = 10 and repeats = 3, then three separate 10-fold cross-validations are used as the resampling scheme.
- verboseIter: A logical for printing a training log.
- returnData: A logical for saving the data into a slot called trainingData.
- p : For leave-group out cross-validation: the training percentage
- For method = "timeslice", trainControl has options
   initialWindow, horizon and fixedWindow that govern how
   cross-validation can be used for time series data.
- classProbs : a logical value determining whether class probabilities should be computed for held-out samples during resample.
- index and indexOut : optional lists with elements for each resampling iteration. Each list element is the sample rows used for training at that iteration or should be held-out. When these values are not specified, train will generate them.
- summaryFunction: a function to computed alternate performance summaries.

• selectionFunction: a function to choose the optimal tuning parameters, and examples.

- PCAthresh, ICAcomp and k: these are all options to pass to the preProcess function (when used).
- returnResamp: a character string containing one of the following values: "all", "final" or "none". This specifies how much of the resampled performance measures to save.
- allowParallel: a logical that governs whether train should use parallel processing (if availible).

There are several other options not discussed here.

### 5.5.5 Alternate Performance Metrics

The user can change the metric used to determine the best settings. By default, RMSE, R<sup>2</sup>, and the mean absolute error (MAE) are computed for regression while accuracy and Kappa are computed for classification. Also by default, the parameter values are chosen using RMSE and accuracy, respectively for regression and classification. The metric argument of the train function allows the user to control which the optimality criterion is used. For example, in problems where there are a low percentage of samples in one class, using metric = "Kappa" can improve quality of the final model.

If none of these parameters are satisfactory, the user can also compute custom performance metrics. The trainControl function has a argument called summaryFunction that specifies a function for computing performance. The function should have these arguments:

data is a reference for a data frame or matrix with columns called obs and pred for the observed and predicted outcome values (either numeric data for regression or character values for classification). Currently, class probabilities are not passed to the function. The values in data are the held-out predictions (and their associated reference values) for a single combination of tuning parameters. If the classProbs argument of the trainControl object is set to TRUE, additional columns in data will be present that contains the class probabilities. The names of these columns are the same as the class levels. Also, if weights were specified in the call to train, a column called weights will also be in the data set. Additionally, if the recipe method for train was used (see this section of documentation), other variables not used in the model will also be included. This can be accomplished by adding a role in the recipe of "performance var". An example is given in the recipe section of this site.

- lev is a character string that has the outcome factor levels taken from the training data. For regression, a value of NULL is passed into the function.
- model is a character string for the model being used (i.e. the value passed to the method argument of train).

The output to the function should be a vector of numeric summary metrics with non-null names. By default, train evaluate classification models in terms of the predicted classes. Optionally, class probabilities can also be used to measure performance. To obtain predicted class probabilities within the resampling process, the argument classProbs in trainControl must be set to TRUE. This

merges columns of probabilities into the predictions generated from each resample (there is a column per class and the column names are the class names).

As shown in the last section, custom functions can be used to calculate performance scores that are averaged over the resamples. Another built-in function, <a href="twoClassSummary">twoClassSummary</a>, will <a href="compute the">compute the</a> sensitivity, specificity and area under the ROC curve:

```
head(twoClassSummary)

##

## 1 function (data, lev = NULL, model = NULL)

## 2 {

## 3    lvls <- levels(data$obs)

## 4    if (length(lvls) > 2)

## 5        stop(paste("Your outcome has", length(lvls), "levels

## 6    requireNamespaceQuietStop("ModelMetrics")
```

To rebuild the boosted tree model using this criterion, we can see the relationship between the tuning parameters and the area under the ROC curve using the following code:

```
fitControl <- trainControl(method = "repeatedcv",</pre>
                            number = 10,
                            repeats = 10,
                            ## Estimate class probabilities
                            classProbs = TRUE,
                            ## Evaluate performance using
                            ## the following function
                            summaryFunction = twoClassSummary)
set.seed(825)
gbmFit3 <- train(Class ~ ., data = training,</pre>
                 method = "gbm",
                 trControl = fitControl,
                  verbose = FALSE,
                  tuneGrid = gbmGrid,
                 ## Specify which metric to optimize
                 metric = "ROC")
gbmFit3
```

```
## Stochastic Gradient Boosting
##
## 157 samples
   60 predictor
##
    2 classes: 'M', 'R'
##
##
## No pre-processing
## Resampling: Cross-Validated (10 fold, repeated 10 times)
## Summary of sample sizes: 141, 141, 142, 141, 141, 142, ...
## Resampling results across tuning parameters:
##
     interaction.depth n.trees ROC
##
                                      Sens
                                            Spec
                                0.87 0.83
##
     1
                          50
                                            0.71
     1
                         100
                                0.88 0.85 0.74
##
                                0.89 0.85 0.77
##
     1
                         150
     1
                         200
                                0.89 0.85
                                           0.78
##
                         250
                                0.89 0.86 0.78
##
     1
     1
                         300
                                0.89 0.86
                                           0.78
##
##
                                 •
                                     . .
     :
                         :
     9
                        1350
                                0.91 0.89 0.79
##
                                0.91 0.89
##
     9
                        1400
                                           0.79
                                0.91 0.89 0.79
##
     9
                        1450
##
     9
                        1500
                                0.91 0.89 0.79
##
## Tuning parameter 'shrinkage' was held constant at a value of 0
##
## Tuning parameter 'n.minobsinnode' was held constant at a value
```

```
## ROC was used to select the optimal model using the largest val
## The final values used for the model were n.trees = 250,
## interaction.depth = 9, shrinkage = 0.1 and n.minobsinnode = 20
```

In this case, the average area under the ROC curve associated with the optimal tuning parameters was 0.914 across the 100 resamples.

## 5.6 Choosing the Final Model

Another method for customizing the tuning process is to modify the algorithm that is used to select the "best" parameter values, given the performance numbers. By default, the train function chooses the model with the largest performance value (or smallest, for mean squared error in regression models). Other schemes for selecting model can be used. Breiman et al (1984) suggested the "one standard error rule" for simple tree-based models. In this case, the model with the best performance value is identified and, using resampling, we can estimate the standard error of performance. The final model used was the simplest model within one standard error of the (empirically) best model. With simple trees this makes sense, since these models will start to over-fit as they become more and more specific to the training data.

train allows the user to specify alternate rules for selecting the final model. The argument <u>selectionFunction</u> <u>can be used to supply a function to algorithmically determine the final model</u>. There are three existing functions in the package: <u>best</u> is chooses the

largest/smallest value, oneSE attempts to capture the spirit of Breiman et al (1984) and tolerance selects the least complex model within some percent tolerance of the best value. See ?best for more details.

User-defined functions can be used, as long as they have the following arguments:

- x is a data frame containing the tune parameters and their associated performance metrics. Each row corresponds to a different tuning parameter combination.
- metric a character string indicating which performance metric should be optimized (this is passed in directly from the metric argument of train.
- maximize is a single logical value indicating whether larger values
  of the performance metric are better (this is also directly passed
  from the call to train).

The function should output a single integer indicating which row in x is chosen.

As an example, if we chose the previous boosted tree model on the basis of overall accuracy, we would choose: n.trees = 250, interaction.depth = 9, shrinkage = 0.1, n.minobsinnode = 20. However, the scale in this plots is fairly tight, with accuracy values ranging from 0.872 to 0.914. A less complex model (e.g. fewer, more shallow trees) might also yield acceptable accuracy.

The tolerance function could be used to find a less complex model based on  $(x-x_{best})/x_{best}x$  100, which is the percent difference. For example, to select parameter values based on a 2% loss of

performance:

之前expand.grid得到的是90种参数(90行)的gbmfit3, whichiTwoPct经过tolerance返回一个值5, 作为下面 gbmFit3\$results第五行的索引

问题是为什么只返回一个5呢?tolerance只筛选一个model吗?满足tolerance筛选要求的model?tolerance返 |回行索引?

whichTwoPct <- tolerance(gbmFit3\$results, metric = "ROC",</pre>

tol = 2, maximize = TRUE)

cat("best model within 2 pct of best:\n")



## best model within 2 pct of best:

tolerance takes the simplest model that is within a percent tolerance of the empirically optimal model. For example, if the largest Kappa value is 0.5 and a simpler model within 3 percent is acceptable, we score the other models using (x -0.5)/0.5 \* 100. The simplest model whose score is not less than 3 is chosen (in this case, a model with a Kappa value of 0.35 is acceptable).

#### gbmFit3\$results[whichTwoPct,1:6]

取tolerance选取的那行和前6列 这个拿来做什么?model吗?

gbmFit3不是数据阿是evaluation的值,选model时应该索引gbmFit3吧?

shrinkage interaction.depth n.minobsinnode n.trees ##

ROC

## 32

0.1

5

20

100 0.901255

This indicates that we can get a less complex model with an area under the ROC curve of 0.901 (compared to the "pick the best" value of 0.914).

The main issue with these functions is related to ordering the models from simplest to complex. In some cases, this is easy (e.g. simple trees, partial least squares), but in cases such as this model, the ordering of models is subjective. For example, is a boosted tree model using 100 iterations and a tree depth of 2 more complex than

one with 50 iterations and a depth of 8? The package makes some choices regarding the orderings. In the case of boosted trees, the package assumes that increasing the number of iterations adds complexity at a faster rate than increasing the tree depth, so models are ordered on the number of iterations then ordered with depth. See ?best for more examples for specific models.

# 5.7 Extracting Predictions and Class Probabilities

As previously mentioned, objects produced by the train function contain the "optimized" model in the finalModel sub-object. Predictions can be made from these objects as usual. In some cases, such as pls or gbm objects, additional parameters from the optimized fit may need to be specified. In these cases, the train objects uses the results of the parameter optimization to predict new samples. For example, if predictions were created using predict.gbm, the user would have to specify the number of trees directly (there is no default). Also, for binary classification, the predictions from this function take the form of the probability of one of the classes, so extra steps are required to convert this to a factor vector. predict.train automatically handles these details for this (and for other models).

Also, there are very few standard syntaxes for model predictions in R. For example, to get class probabilities, many predict methods have an argument called type that is used to specify whether the classes

or probabilities should be generated. Different packages use different values of type, such as "prob", "posterior", "response", "probability" or "raw". In other cases, completely different syntax is used.

| default of type is type = "raw" |

For predict.train, the type options are standardized to be "class" and "prob" (the underlying code matches these to the appropriate choices for each model. For example:

```
predict(gbmFit3, newdata = head(testing))
## [1] R R R R M M
## Levels: M R
predict(gbmFit3, newdata = head(testing), type = "prob")
##
                Μ
                           R
## 1 0.2600273005 0.73997270
## 2 0.0113631254 0.98863687
## 3 0.0003797417 0.99962026
## 4 0.1532818480 0.84671815
## 5 0.9879809255 0.01201907
## 6 0.6342884390 0.36571156
```

# 5.8 Exploring and Comparing Resampling Distributions

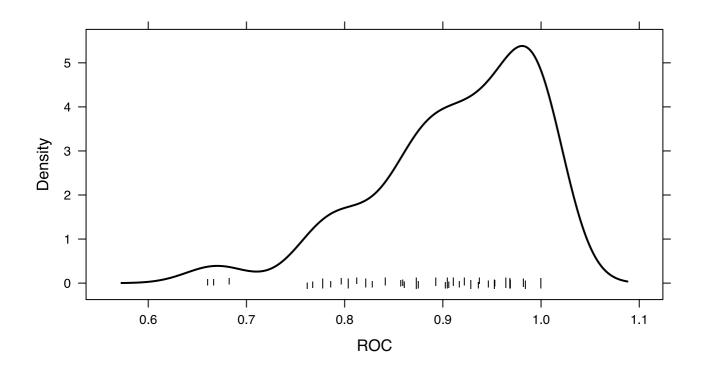
### 5.8.1 Within-Model

There are several lattice functions than can be used to explore relationships between tuning parameters and the resampling results for a specific model:

- xyplot and stripplot can be used to plot resampling statistics against (numeric) tuning parameters.
- histogram and densityplot can also be used to look at distributions of the tuning parameters across tuning parameters.

For example, the following statements create a density plot:

```
trellis.par.set(caretTheme())
densityplot(gbmFit3, pch = "|")
```



Note that if you are interested in <u>plotting the resampling results across</u>

<u>multiple tuning parameters, the option resamples = "all"</u> should be used in the control object.

### 5.8.2 Between-Models

The caret package also includes functions to characterize the differences between models (generated using train, sbf or rfe) via their resampling distributions. These functions are based on the work of Hothorn et al. (2005) and Eugster et al (2008).

First, a support vector machine model is fit to the Sonar data. The data are centered and scaled using the <a href="preProc">preProc</a> argument. Note that the same random number seed is set prior to the model that is identical to the seed used for the boosted tree model. This ensures that the same resampling sets are used, which will come in handy when we compare the resampling profiles between models.

```
## Support Vector Machines with Radial Basis Function Kernel
##
## 157 samples
    60 predictor
##
     2 classes: 'M', 'R'
##
##
## Pre-processing: centered (60), scaled (60)
## Resampling: Cross-Validated (10 fold, repeated 10 times)
## Summary of sample sizes: 141, 141, 142, 141, 141, 142, ...
## Resampling results across tuning parameters:
##
            ROC
                       Sens
##
     \mathbf{C}
                                  Spec
##
      0.25
            0.8700471
                       0.7572222
                                  0.7539286
      0.50
           0.9102133 0.8587500
##
                                  0.7819643
      1.00
##
           0.9344767 0.8809722
                                  0.7807143
      2.00
           0.9346230 0.8870833
##
                                  0.7878571
      4.00
           0.9455828 0.8979167
##
                                  0.8192857
      8.00
           0.9486012 0.9002778
##
                                  0.8162500
     16.00
##
           0.9491146 0.9050000
                                  0.8216071
     32.00 0.9491146 0.9119444
                                  0.8164286
##
##
## Tuning parameter 'sigma' was held constant at a value of 0.013
## ROC was used to select the optimal model using the largest value
## The final values used for the model were sigma = 0.01334808 and
```

### Also, a regularized discriminant analysis model was fit.

```
set.seed(825)

rdaFit <- train(Class ~ ., data = training,

method = "rda",

trControl = fitControl,

tuneLength = 4,

metric = "ROC")
```

```
## Regularized Discriminant Analysis
##
## 157 samples
    60 predictor
##
##
     2 classes: 'M', 'R'
##
## No pre-processing
## Resampling: Cross-Validated (10 fold, repeated 10 times)
## Summary of sample sizes: 141, 141, 142, 141, 141, 142, ...
## Resampling results across tuning parameters:
##
                                       Sens
                lambda
                           ROC
                                                  Spec
##
     gamma
##
     0.0000000
                0.0000000
                           0.6677145
                                       0.9052778
                                                  0.3998214
##
     0.0000000
                0.3333333
                           0.8516543
                                       0.8425000
                                                  0.7564286
##
     0.0000000
                0.6666667
                           0.8697941
                                       0.8212500
                                                  0.7969643
     0.0000000
                1.0000000
                           0.8560193
                                       0.7772222
                                                  0.7898214
##
     0.3333333
                0.0000000
                           0.9069866
                                       0.8884722
                                                  0.7630357
##
                0.3333333
##
     0.3333333
                           0.9247817
                                       0.9201389
                                                  0.7942857
     0.3333333
                0.6666667
                           0.9247148
                                       0.9251389
                                                  0.7830357
##
##
     0.3333333
                1.0000000
                           0.8782242
                                       0.8462500
                                                  0.7817857
     0.6666667
                0.0000000
                           0.9015352
                                       0.8804167
                                                  0.7557143
##
##
     0.6666667
                0.3333333
                           0.9100471
                                       0.9044444
                                                  0.7607143
##
     0.6666667
                0.6666667
                           0.9033209
                                       0.9013889
                                                  0.7687500
     0.6666667
                1.0000000
                           0.8704638
                                       0.8077778
                                                  0.7883929
##
##
     1.0000000
                0.0000000
                           0.7283631
                                       0.6652778
                                                  0.6507143
     1.0000000
                0.3333333
                           0.7308557
                                       0.6676389
                                                  0.6564286
##
##
     1.0000000
                0.6666667
                           0.7322222
                                       0.6770833
                                                  0.6633929
```

```
## 1.0000000 1.0000000 0.7342832 0.6745833 0.6607143

##

## ROC was used to select the optimal model using the largest valuable

## The final values used for the model were gamma = 0.3333333 and

## = 0.33333333.
```

Given these models, can we make statistical statements about their performance <u>differences</u>? To do this, we first <u>collect the resampling</u> results using <u>resamples</u>.

```
resamps <- resamples(list(GBM = gbmFit3,</pre>
                                SVM = svmFit,
                                RDA = rdaFit))
                  resamples(list())
resamps
                  These functions provide methods for collection, analyzing
                  and visualizing a set of resampling results from a common
                  data set.
##
## Call:
## resamples.default(x = list(GBM = gbmFit3, SVM = svmFit, RDA = |
##
## Models: GBM, SVM, RDA
## Number of resamples: 100
## Performance metrics: ROC, Sens, Spec
## Time estimates for: everything, final model fit
```

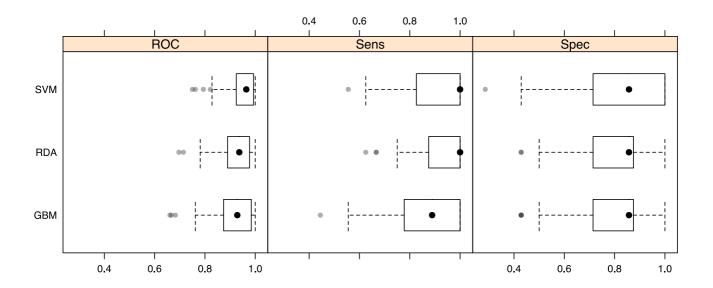
```
summary(resamps)
```

```
##
## Call:
## summary.resamples(object = resamps)
##
## Models: GBM, SVM, RDA
## Number of resamples: 100
##
## ROC
##
            Min.
                   1st Ou.
                               Median
                                                   3rd Ou. Max. NA':
                                           Mean
## GBM 0.6607143 0.8745040 0.9285714 0.9139534 0.9841890
                                                              1
                                                                   (
## SVM 0.7500000 0.9265873 0.9642857 0.9491146 0.9895833
                                                              1
                                                                   (
## RDA 0.6964286 0.8901910 0.9365079 0.9247817 0.9747024
                                                              1
##
## Sens
            Min.
                               Median
##
                   1st Qu.
                                           Mean 3rd Qu. Max. NA's
## GBM 0.4444444 0.7777778 0.8888889 0.8818056
                                                       1
                                                            1
                                                                 0
## SVM 0.5555556 0.8506944 1.0000000 0.9050000
                                                            1
                                                                 0
                                                       1
## RDA 0.6250000 0.8750000 1.0000000 0.9201389
                                                       1
                                                            1
                                                                 0
##
## Spec
##
            Min.
                    1st Qu.
                               Median
                                           Mean 3rd Qu. Max. NA's
## GBM 0.4285714 0.7142857 0.8571429 0.7966071
                                                            1
                                                   0.875
                                                                 0
## SVM 0.2857143 0.7142857 0.8571429 0.8216071
                                                   1.000
                                                            1
                                                                 0
## RDA 0.4285714 0.7142857 0.8571429 0.7942857
                                                   0.875
                                                            1
                                                                 0
```

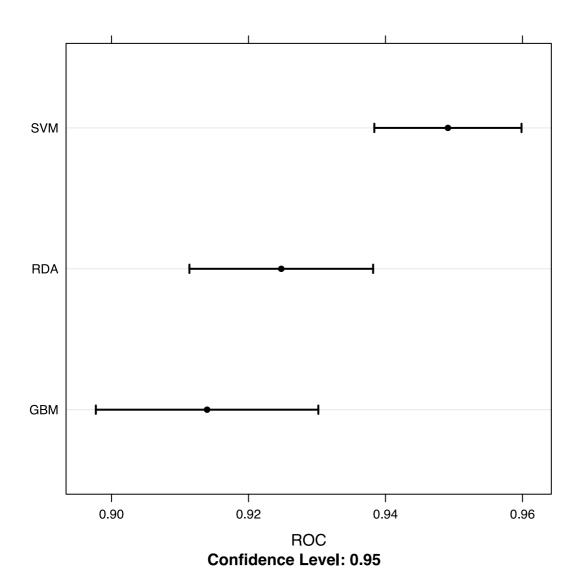
Note that, in this case, the option resamples = "final" should be user-defined in the control objects.

There are several lattice plot methods that can be used to visualize the resampling distributions: density plots, box-whisker plots, scatterplot matrices and scatterplots of summary statistics. For example:

```
theme1 <- trellis.par.get()
theme1$plot.symbol$col = rgb(.2, .2, .2, .4)
theme1$plot.symbol$pch = 16
theme1$plot.line$col = rgb(1, 0, 0, .7)
theme1$plot.line$lwd <- 2
trellis.par.set(theme1)
bwplot(resamps, layout = c(3, 1))</pre>
```

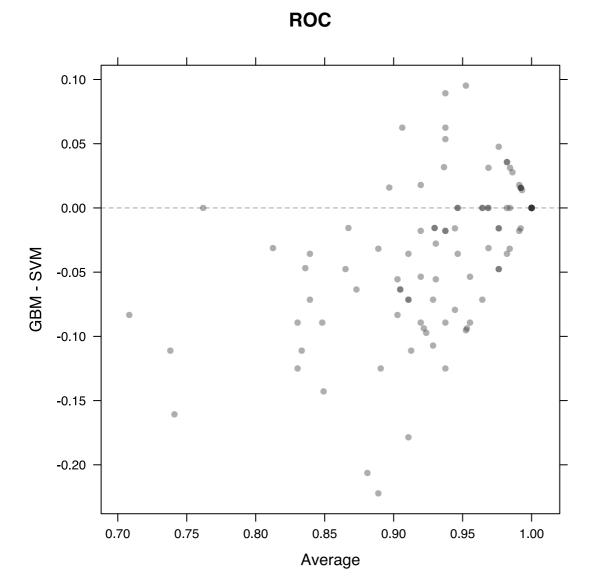


```
trellis.par.set(caretTheme())
dotplot(resamps, metric = "ROC")
```

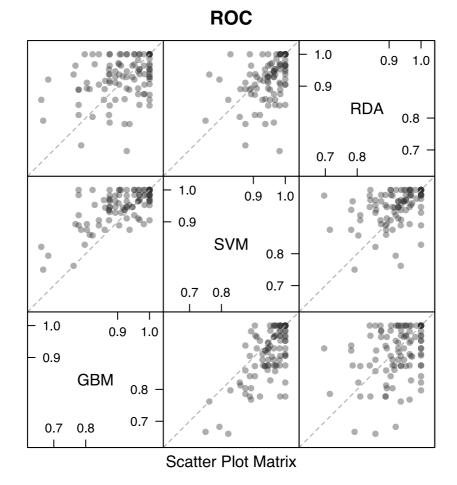


trellis.par.set(theme1)

xyplot(resamps, what = "BlandAltman")



splom(resamps)



Other visualizations are availible in densityplot.resamples and parallel.resamples

Since models are fit on the same versions of the training data, it makes sense to make inferences on the differences between models. In this way we reduce the within-resample correlation that may exist. We can compute the differences, then use a simple *t*-test to evaluate the null hypothesis that there is no difference between models.

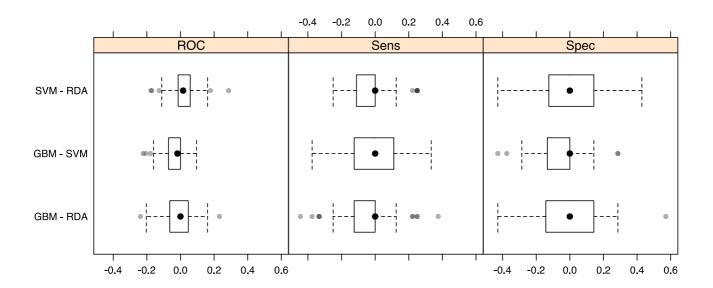
```
difValues <- diff(resamps)
difValues</pre>
```

```
##
## Call:
## diff.resamples(x = resamps)
##
## Models: GBM, SVM, RDA
## Metrics: ROC, Sens, Spec
## Number of differences: 3
## p-value adjustment: bonferroni
```

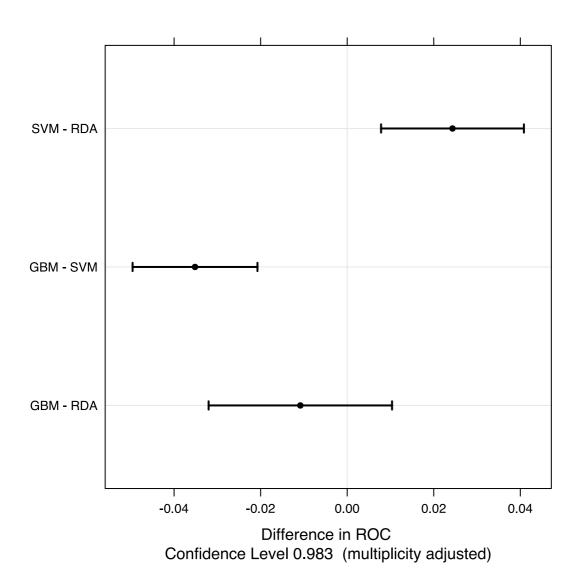
summary(difValues)

```
##
## Call:
## summary.diff.resamples(object = difValues)
##
## p-value adjustment: bonferroni
## Upper diagonal: estimates of the difference
## Lower diagonal: p-value for H0: difference = 0
##
## ROC
      GBM SVM RDA
##
## GBM
              -0.03516 -0.01083
## SVM 1.304e-07
                         0.02433
## RDA 0.649032 0.001546
##
## Sens
      GBM SVM
##
                      RDA
## GBM
              -0.02319 -0.03833
## SVM 0.36881
                      -0.01514
## RDA 0.02684 0.60884
##
## Spec
   GBM
             SVM
                      RDA
## GBM
      -0.025000 0.002321
## SVM 0.1235
                      0.027321
## RDA 1.0000 0.2994
```

trellis.par.set(theme1)
bwplot(difValues, layout = c(3, 1))



trellis.par.set(caretTheme())
dotplot(difValues)



# 5.9 Fitting Models Without Parameter Tuning

In cases where the model tuning values are known, train can be used to fit the model to the entire training set without any resampling or parameter tuning. <u>Using the method = "none" option in trainControl</u> can be used. For example:

```
fitControl <- trainControl(method = "none", classProbs = TRUE)</pre>
set.seed(825)
gbmFit4 <- train(Class ~ ., data = training,</pre>
                 method = "gbm",
                 trControl = fitControl,
                  verbose = FALSE,
                 ## Only a single model can be passed to the
                 ## function when no resampling is used:
                  tuneGrid = data.frame(interaction.depth = 4,
                                        n.trees = 100,
                                         shrinkage = .1,
                                         n.minobsinnode = 20),
                  metric = "ROC")
gbmFit4
## Stochastic Gradient Boosting
##
## 157 samples
   60 predictor
##
     2 classes: 'M', 'R'
##
##
## No pre-processing
## Resampling: None
```

```
Note that plot.train, resamples, confusionMatrix.train and several other functions will not work with this object but predict.train and others will:
```

```
predict(gbmFit4, newdata = head(testing))
## [1] R R R R M M
## Levels: M R
predict(gbmFit4, newdata = head(testing), type = "prob")
                                          Ch5
                                          1.dataset
                                          inTraining<-createDataPartition(p=)
                                          training<-data[inTraining, ]
##
                      Μ
                                          testing<-data[-inTraining,]
## 1 0.129181487 0.87081851
                                          2.tuning parameter
## 2 0.039369722 0.96063028
                                          if tune parameter(选择较大的ROC Sens Spec时的参数(比如method=gbm
                                          时的参数是n.trees, interaction.depth, shrinkage, n.minobsinnode))
## 3 0.002722481 0.99727752
                                          fitControl<- trainControl(method=gbm,number=,repeats=,classProbs =
                                          TRUE, summaryFunction = twoClassSummary)
## 4 0.076762607 0.92323739
                                          Grid <- expand.grid (interaction.depth =, n.trees = ,
                                          shrinkage= ,n.minobsinnode = )
## 5 0.959529367 0.04047063
                                          set.seed(1)
                                          Fit<-train(..., data=,method=很多, verbose = FALSE, trControl = fitControl,
## 6 0.622319826 0.37768017
                                          tuneGrid=Grid, metric = "ROC"...)
                                          if no parameter tuning
                                          trainControl(method = "none")
                                          3.choose final model(经过tolerance或oneSE筛选过的最优的predictor)
                                          whichTwoPct <- tolerance()
                                          Fit[whichTwoPct,]
                                          4.prediction
                                          predict(model,newdata,type=)
```

5.compare

summary(diff())

resamps<-resamples(list())
xyplot(),splom(),bwplot(),dotplot()

1)plot(Fit): between tuning parameters and the resampling results

method都可以做不同的model,然后通过plot比较)

2)Between-Models(可以用preProc 来center和scale一下training data ,或改变