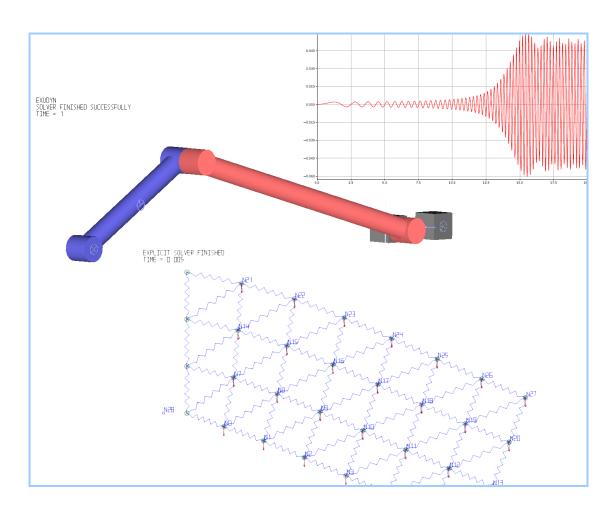
## Flexible Multibody Dynamics Systems with Python and C++

# **EXUDYN**

(flexible multibody dynamics)

## User documentation



EXUDYN version = 0.1.333

University of Innsbruck, Department of Mechatronics, May 17, 2020,

Johannes Gerstmayr

# **Contents**

1	Get	Getting Started			
	1.1	Gettir	ng started	1	
		1.1.1	What is EXUDYN?	1	
		1.1.2	Who is developing EXUDYN?	2	
		1.1.3	How to link EXUDYN with Python (recommended for beginners)?	2	
		1.1.4	How to install EXUDYN and using the C++ code (advanced)?	3	
		1.1.5	Goals of EXUDYN	3	
		1.1.6	Run a simple example in Spyder	4	
	1.2	FAQ -	- Frequently asked questions	5	
2	Ove	Overview on EXUDYN			
	2.1	Modu	ıle structure	9	
		2.1.1	Overview of modules	9	
		2.1.2	Conventions: items, indices, coordinates	10	
	2.2	Items	: Nodes, Objects, Loads, Markers, Sensors,	12	
		2.2.1	Nodes	12	
		2.2.2	Objects	12	
		2.2.3	Markers	13	
		2.2.4	Loads	13	
		2.2.5	Sensors	13	
		2.2.6	Reference coordinates and displacements	14	
	2.3	Exudy	yn Basics	14	
		2.3.1	Interaction with the EXUDYN module	14	
		2.3.2	Simulation settings	14	
		2.3.3	Visualization settings	15	
		2.3.4	Solver	16	
		2.3.5	Generating output and results	16	
		2.3.6	Graphics pipeline	19	
		2.3.7	Generating animations	21	
	2.4	C++ (	Code	22	
		2.4.1	Focus of the C++ code	22	
		242	C++ Code structure	23	

		2.4.3	C++ Code: Modules	23		
		2.4.4	Code style and conventions	24		
		2.4.5	Notation conventions	25		
		2.4.6	No-abbreviations-rule	25		
	2.5	Chang	ges	26		
3	Tuto	orial		29		
4	Pyth	non-C+	+ command interface	35		
	4.1	EXUD	OYN	36		
	4.2	Systen	mContainer	37		
	4.3	MainS	System	38		
		4.3.1	MainSystem: Node	40		
		4.3.2	MainSystem: Object	41		
		4.3.3	MainSystem: Marker	42		
		4.3.4	MainSystem: Load	43		
		4.3.5	MainSystem: Sensor	44		
	4.4	Systen	mData	45		
		4.4.1	SystemData: Access coordinates	46		
		4.4.2	SystemData: Get object local-to-global (LTG) coordinate mappings	47		
	4.5	Type o	definitions	48		
		4.5.1	OutputVariableType	48		
		4.5.2	ConfigurationType	49		
		4.5.3	LinearSolverType	50		
5	Objects, nodes, markers, loads and sensors reference manual 5					
	5.1	Notati	ion for item equations	51		
		5.1.1	Reference and current coordinates	53		
		5.1.2	Coordinate Systems	53		
	5.2	Nodes	3	54		
		5.2.1	NodePoint	54		
		5.2.2	NodePoint2D	56		
		5.2.3	NodeRigidBodyEP	58		
		5.2.4	NodeRigidBodyRxyz	60		
		5.2.5	NodeRigidBodyRotVecLG	62		
		5.2.6	NodeRigidBody2D	64		
		5.2.7	NodePoint2DSlope1	66		
		5.2.8	NodeGenericODE2	68		
		5.2.9	NodeGenericData	69		
		5.2.10	NodePointGround	70		
	5.3	Object	ts	71		
		531	ObjectMassPoint (1997)	71		

	5.3.2	ObjectMassPoint2D	73
	5.3.3	ObjectRigidBody	75
	5.3.4	ObjectRigidBody2D	77
	5.3.5	ObjectGenericODE2	80
	5.3.6	ObjectFFRF	83
	5.3.7	ObjectFFRFreducedOrder	87
	5.3.8	ObjectANCFCable2D	91
	5.3.9	ObjectALEANCFCable2D	93
	5.3.10	ObjectGround	95
	5.3.11	ObjectConnectorSpringDamper	96
	5.3.12	ObjectConnectorCartesianSpringDamper	99
	5.3.13	ObjectConnectorRigidBodySpringDamper	102
	5.3.14	ObjectConnectorCoordinateSpringDamper	105
	5.3.15	ObjectConnectorDistance	108
	5.3.16	ObjectConnectorCoordinate	110
	5.3.17	ObjectContactCoordinate	113
	5.3.18	ObjectContactCircleCable2D	114
		ObjectContactFrictionCircleCable2D	116
	5.3.20	ObjectJointGeneric	118
	5.3.21	ObjectJointSpherical	122
	5.3.22	ObjectJointRevolute2D	124
	5.3.23	ObjectJointPrismatic2D	125
	5.3.24	ObjectJointSliding2D	127
	5.3.25	ObjectJointALEMoving2D	131
5.4	Marke	ers	135
	5.4.1	MarkerBodyMass	135
	5.4.2	MarkerBodyPosition	136
	5.4.3	MarkerBodyRigid	137
	5.4.4	MarkerNodePosition	138
	5.4.5	MarkerNodeRigid	139
	5.4.6	MarkerNodeCoordinate	140
	5.4.7	MarkerSuperElementPosition	141
	5.4.8	MarkerBodyCable2DShape	142
	5.4.9	MarkerBodyCable2DCoordinates	143
5.5	Loads		144
	5.5.1	LoadForceVector	144
	5.5.2	LoadTorqueVector	145
	5.5.3	LoadMassProportional	146
	5.5.4	LoadCoordinate	147
5.6	Sensor	°S	148
		SensorNode	148

		5.6.2	SensorObject	149
		5.6.3	SensorBody	150
		5.6.4	SensorSuperElement	151
		5.6.5	SensorLoad	152
	5.7	Graph	icsData	153
6	EXU	JDYN S	ettings	155
	6.1	Simula	ation settings	155
		6.1.1	SolutionSettings	155
		6.1.2	NumericalDifferentiationSettings	156
		6.1.3	NewtonSettings	
		6.1.4	GeneralizedAlphaSettings	159
		6.1.5	TimeIntegrationSettings	159
		6.1.6	StaticSolverSettings	160
		6.1.7	SimulationSettings	162
	6.2	Visual	ization settings	162
		6.2.1	VSettingsGeneral	162
		6.2.2	VSettingsWindow	163
		6.2.3	VSettingsOpenGL	164
		6.2.4	VSettingsContour	
		6.2.5	VSettingsExportImages	166
		6.2.6	VSettingsNodes	166
		6.2.7	VSettingsBeams	167
		6.2.8	VSettingsBodies	167
		6.2.9	VSettingsConnectors	168
		6.2.10	VSettingsMarkers	168
		6.2.11	VSettingsLoads	169
		6.2.12	VSettingsSensors	169
		6.2.13	VisualizationSettings	170
	6.3		substructures	
		6.3.1	CSolverTimer	170
		6.3.2	SolverLocalData	171
		6.3.3	SolverIterationData	172
		6.3.4	SolverConvergenceData	173
		6.3.5	SolverOutputData	174
		6.3.6	MainSolverStatic	174
		6.3.7	MainSolverImplicitSecondOrder	177
7	3D (	Graphic	es Visualization	183
	7.1	-	e input	183
	7.2		ard input	183

8	Solver				
	8.1	Jacobian computation	185		
	8.2	Implicit trapezoidal rule solver	186		
	8.3	Representation of coordinates and equations of motion	186		
	8.4	Newmark method	187		
9	9 References		189		
10 License			191		

## Chapter 1

# **Getting Started**

The documentation for EXUDYN is split into this introductory section, including a quick start up, code structure and important hints, as well as a couple of sections containing references to the available Python interfaces to interact with EXUDYN and finally some information on theory (e.g., 'Solver').

EXUDYN is hosted on GitHub:

• web: https://github.com/jgerstmayr/EXUDYN/wiki

For any comments, requests, issues, bug reports, send an email to:

• email: reply.exudyn@gmail.com

Thanks for your contribution!

## 1.1 Getting started

This section will show:

- 1. What is EXUDYN?
- 2. Who is developing EXUDYN?
- 3. How to install EXUDYN
- 4. How to link EXUDYN and Python
- 5. Goals of EXUDYN
- 6. Run a simple example in Spyder
- 7. FAQ Frequently asked questions

#### 1.1.1 What is EXUDYN?

EXUDYN is a C++ based Python library for efficient simulation of flexible multibody dynamics systems. It is designed to easily set up complex multibody models, consisting of rigid and flexible bodies with joints, loads and other components.

The formulation is mostly based on redundant coordinates. This means that computational objects (rigid bodies, flexible bodies, ...) are added as independent bodies to the system. Hereafter,

connectors (e.g., springs or constraints) are used to interconnect the bodies. The connectors are using Markers on the bodies as interfaces, in order to transfer forces and displacements. For details on the interaction of nodes, objects, markers and loads see Section 2.2.

### 1.1.2 Who is developing EXUDYN?

EXUDYN is currently (5-2020) developed at the University of Innsbruck. In the first phase most of the core code has been (and still is) written by Johannes Gerstmayr, implementing ideas of earlier developments of HOTINT. 15 years of development led to a lot of lessions learned.

Some specific codes regarding pybind interface and parallelization have been written by Stefan Holzinger, who also supports the upload to GitLab. Important discussions with researchers from the community where important for the design and development of EXUDYN, where we like to mention Joachim Schöberl from TU-Vienna who influenced the design of the code. During a Comet-K2 cooperation project, several discussions with the TMECH/LCM group in Linz influenced the code development.

The cooperation and funding within the EU H2020-MSCA-ITN project 'Joint Training on Numerical Modelling of Highly Flexible Structures for Industrial Applications' will support the further development of the code.

### 1.1.3 How to link EXUDYN with Python (recommended for beginners)?

In order to run EXUDYN, you need an appropriate Python installation. We recommend to use

- Anaconda, 32bit, Python 3.6.5 (alternatively 64bit)<sup>1</sup>
- Spyder 3.2.8 with Python 3.6.5 32 bit (alternatively 64bit), which is included in the Anaconda installation<sup>2</sup>

If you plan to use 64bit and newer Python versions, we recommend to use VS2019 to compile your code, which offers Python 3.7 compatibility. However, you should know that Python versions and the version of the module must be identical (e.g., Python 3.6 32 **both** in the exudyn module and in Spyder).

The simplest way to start is, to copy the files (and possibly further files that are needed)

- exudynUtilities.py
- itemInterface.py
- exudyn.pyd

<sup>&</sup>lt;sup>1</sup>Anaconda 32/64bit with Python3.6 can be downloaded via the repository archive https://repo.anaconda.com/archive/ choosing Anaconda3-5.2.0-Windows-x86.exe or Anaconda3-5.2.0-Windows-x86\_64.exe for 64bit.

<sup>&</sup>lt;sup>2</sup>It is important that Spyder, python and exudyn are **either** 32bit **or** 64bit. There will be a strange .DLL error, if you mix up 32/64bit. It is possible to install both, Anaconda 32bit and Anacondo 64bit – then you should follow the recommendations of paths as suggested by Anaconda installer

to your working directory and directly import the modules as described in tutorials and examples. The second way (**recommended**) is to use Python's sys module to link to your WorkingRelease directory, for example:

```
import sys
sys.path.append('C:/DATA/cpp/EXUDYN_git/main/bin/WorkingRelease')
```

The path C:/DATA/cpp/EXUDYN\_git/main/bin/WorkingRelease needs to be adapted to the location of your WorkingRelease where the exudyn.pyd files are located. In case of 64bit, it must be changed to .... /bin/WorkingRelease64.

In the future, there will also be a possibility to install the module using pip commands – we are happy, if somebody could do this!

## 1.1.4 How to install EXUDYN and using the C++ code (advanced)?

EXUDYN is still under intensive development of core modules. There are several ways to using the code, but you **cannot** install EXUDYN as compared to other executable programs and apps.

In order to make full usage of the C++ code and extending it, you can use:

- Windows / Microsoft Visual Studio 2017 and above:
  - get the files from git
  - put them into a local directory (recommended: C:/DATA/cpp/EXUDYN\_git)
  - start main\_sln.sln with Visual Studio
  - compile the code and run main/pythonDev/pytest.py example code
  - adapt pytest.py for your applications
  - extend the C++ source code
  - link it to your own code
  - NOTE: on some systems, you might need to replace '/' with '\'
- Linux, etc.: not fully supported yet; however, all external libraries are Linux-compatible and thus should run with minimum adaptation efforts.

#### 1.1.5 Goals of EXUDYN

After the first development phase (planned in Q4/2021), it will

- be a small multibody library, which can be easily linked to other projects,
- allow to efficiently simulate small scale systems (compute 100000s time steps per second for systems with  $n_{DOF} < 10$ ),
- safe and widely accessible module for Python,
- allow to add user defined objects in C++,
- allow to add user defined solvers in Python).

#### Listing 1.1: My first example

```
from itemInterface import *
                                #conversion of data to exudyn dictionaries
import exudyn as exu
                               #C++ EXUDYN library
SC = exu.SystemContainer()
                                 #container of systems
mbs = SC.AddSystem()
                                #add a new system to work with
nMP = mbs.AddNode(NodePoint2D(referenceCoordinates=[0,0]))
mbs.AddObject(ObjectMassPoint2D(physicsMass=10, nodeNumber=nMP ))
mMP = mbs.AddMarker(MarkerNodePosition(nodeNumber = nMP))
mbs.AddLoad(Force(markerNumber = mMP, loadVector=[0.001,0,0]))
mbs.Assemble()
                                #assemble system and solve
simulationSettings = exu.SimulationSettings()
SC. TimeIntegrationSolve (mbs, 'GeneralizedAlpha', simulationSettings)
```

### 1.1.6 Run a simple example in Spyder

After performing the steps of the previous section, this section shows a simplistic model which helps you to check if EXUDYN runs on your computer.

In order to start, run the python interpreter Spyder. For the following example, either

- open Spyder and copy the example provided in Listing 1.1 into a new file, or
- open myFirstExample.py from your WorkingRelease directory

Hereafter, press the play button or F5 in Spyder.

If successful, the IPython Console of Spyder will print something like:

If you check your current directory (where myFirstExample.py lies), you will find a new file coordinatesSolution.txt, which contains the results of your computation (with default values for time integration). The beginning and end of the file should look like:

```
#number of time steps (planned) = 100
#

0,0,0,0,0,0.0001,0
0.02,2e-08,0,2e-06,0,0.0001,0
0.03,4.5e-08,0,3e-06,0,0.0001,0
0.04,8e-08,0,4e-06,0,0.0001,0
0.05,1.25e-07,0,5e-06,0,0.0001,0
...

0.96,4.608e-05,0,9.6e-05,0,0.0001,0
0.97,4.7045e-05,0,9.7e-05,0,0.0001,0
0.98,4.802e-05,0,9.8e-05,0,0.0001,0
0.99,4.9005e-05,0,9.9e-05,0,0.0001,0
1,5e-05,0,0.0001,0,0.0001,0
#simulation finished=2019-11-14,20:35:12
#Solver Info: errorOccurred=0,converged=1,solutionDiverged=0,total time steps=100,total
Newton iterations=100,total Newton jacobians=100
```

Within this file, the first column shows the simulation time and the following columns provide solution of coordinates, their derivatives and Lagrange multipliers on system level. As expected, the x-coordinate of the point mass has constant acceleration a = f/m = 0.001/10 = 0.0001, the velocity grows up to 0.0001 after 1 second and the point mass moves 0.00005 along the x-axis.

## 1.2 FAQ - Frequently asked questions

- 1. Where do I find the '.exe' file?
  - → EXUDYN is only available via the python interface as exudyn.pyd library, which is located in folder: main/bin/WorkingRelease. This means that you need to run python (best: Spyder) and import the EXUDYN module.
- 2. Why does type auto completion does not work for mbs (Main system)?
  - → most python environments only have information up to the first sub-structure, e.g., SC=exu. SystemContai provides full access to SC in the type completion, but mbs=SC.AddSystem() is at the second sub-structure of the module and is not accessible.
    WORKAROUND: type mbs=MainSystem() before the mbs=SC.AddSystem() command and the interpreter will know what type mbs is. This also works for settings, e.g., simulation settings 'Newton'.
- 3. How to add graphics?
  - → Graphics (lines, text, 3D triangular / STL mesh) can be added to all BodyGraphicsData items in objects. Graphics objects which are fixed with the background can be attached to a ObjectGround object. Moving objects must be attached to the BodyGraphicsData of a moving body. Other moving bodies can be realized, e.g., by adding a ObjectGround and changing its reference with time.

- 4. What is the difference between MarkerBodyPosition and MarkerBodyRigid?
  - → Position markers (and nodes) do not have information on the orientation (rotation). For that reason, there is a difference between position based and rigid-body based markers. In case of a rigid body attached to ground with a SpringDamper, you can use both, MarkerBodyPosition or MarkerBodyRigid, markers. For a prismatic joint, you will need a MarkerBodyRigid.
- 5. I do not understand the python errors how can I find the reason of the error or crash?
  - → First, you should read all error messages and warnings: from the very first to the last message. Very often, there is a definite line number which shows the error. Note, that if you are executing a string (or module) as a python code, the line numbers refer to the local line number inside the script or module.
  - → If everything fails, try to execute only part of the code to find out where the first error occurs. By omiting parts of the code, you should find the according source of the error.
  - → If you think, it is a bug: send an email with a representative code snippet, version, etc. to reply.exudyn@gmail.com
- 6. I get an error in SC.TimeIntegrationSolve(mbs, 'GeneralizedAlpha', simulationSettings) but no further information how can I solve it?
  - → Typical time integration errors may look like:

model.

- File "C:/DATA/cpp/EXUDYN\_git/main/pythonDev/...<file name>", line XXX, in <module>
  SC.TimeIntegrationSolve(mbs, 'GeneralizedAlpha', simulationSettings)
  SystemError: <built-in method TimeIntegrationSolve of PyCapsule object at 0x0CC63590> returned
- a result with an error set

  → The prechecks, which are performed to enable a crash-free simulation are insufficient for your
- → Very likely, you are using python user functions inside EXUDYN: They lead to an internal python error, which is not catched by EXUDYN. However, you can just check all your user functions, if they will run without EXUDYN. E.g., a load user function UFload(t,load), which tries to access load[4] will fail internally.
- → Use the print(...) command in python at many places to find a possible error in user functions (e.g., put print("Start user function XYZ") at the beginning of every user function.
- → It is also possible, that you are using inconsistent data, which leads to the crash. In that case, you should try to change your model: omit parts and find out which part is causing your error
- $\rightarrow$  see also I do not understand the python errors how can I find the cause?
- 7. Why can't I get the focus of the simulation window on startup (render window hidden)?
  - → Starting EXUDYN out of Spyder might not bring the simulation window to front, because of specific settings in Spyder(version 3.2.8), e.g., Tools→Preferences→Editor→Advanced settings: uncheck 'Maintain focus in the Editor after running cells or selections'; Alternatively, set SC.visualizationSettings.window.alwaysOnTop=True before starting the renderer with exu.StartRenderer()

8. When importing EXUDYN in python (windows) I get the error (or similar):

```
Traceback (most recent call last):
   File "C:\DATA\cpp\EXUDYN_git\main\pythonDev\pytest.py", line 18, in <module>
    import exudyn as exu
ImportError: DLL load failed: %1 is no valid Win32 application.
```

→ probably this is a 32/64bit problem. Your Python installation and EXUDYN need to be **BOTH** either 64bit OR 32bit (Check in your python help; exudyn in WorkingRelease64 is the 64bit version, in WorkingRelease it is the 32bit version) and the Python installation and EXUDYN need to have **BOTH** the same version and 1st subversion number (e.g., 3.6.5 should be compatible with 3.6.2).

## **Chapter 2**

## Overview on EXUDYN

#### 2.1 Module structure

This section will show:

- Overview of modules
- Conventions: dimension of nodes, objects and vectors
- Coordinates: reference coordinates and displacements
- Nodes, Objects, Markers and Loads

#### 2.1.1 Overview of modules

Currently, the module structure is simple:

- Python parts:
  - itemInterface: contains the interface, which transfers python classes (e.g., of a NodePoint)
     to dictionaries that can be understood by the C++ module
  - exudynUtilities: constains helper classes in Python, which allows simpler working with EXUDYN
- C++ parts, see Figs. 2.1 and 2.2:
  - exudyn<sup>1</sup>: on this level, there are just very few functions: SystemContainer(), StartRenderer(),
     StopRenderer()
  - SystemContainer: contains the systems (most important), solvers (static, dynamics, ...), visualization settings
  - mbs: system created with mbs = SC.AddSystem(), this structure contains everything that defines a solvable multibody system; a large set of nodes, objects, markers, loads can added to the system, see Section 5;

¹note that there is a second module, called exudynFast, which deactivates all range-, index- or memory allocation checks at the gain of higher speed (probably 30 percent in regular cases and up to 100 percent in the 64 bit version). This module is included by import exudynFast as exu and can be used same as exudyn. To check the version, just type exu.\_\_doc\_\_ and you will see a note on 'exudynFast' in the exudynFast module.

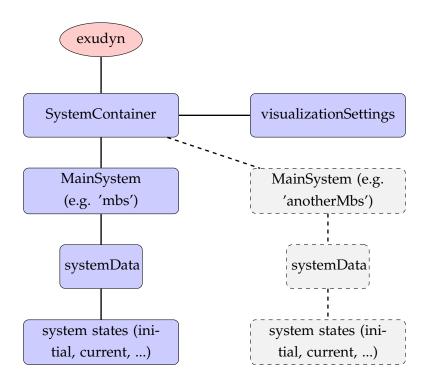


Figure 2.1: Overview of exudyn module.

 mbs.systemData: contains the initial, current, visualization, ... states of the system and holds the items, see Fig. 2.2

#### 2.1.2 Conventions: items, indices, coordinates

In this documentation, we will use the term **item** to identify nodes, objects, markers and loads:

$$item \in \{node, object, marker, load\}$$
 (2.1)

#### Indices: arrays and vector starting with 0:

As known from Python, all **indices** of arrays, vectors, etc. are starting with 0. This means that the first component of the vector v=[1,2,3] is accessed with v[0] in Python (and also in the C++ part of EXUDYN). The range is usually defined as range(0,3), in which '3' marks the index after the last valid component of an array or vector.

## Dimensionality of objects and vectors:

As a convention, quantities in EXUDYN are 3D, such as nodes, objects, markers, loads, measured quantities, etc. For that reason, we denote planar nodes, objects, etc. with the suffix '2D', but 3D objects do not get this suffix.

Output and input to objects, markers, loads, etc. is usually given by 3D vectors (or matrices), such as (local) position, force, torque, rotation, etc. However, initial and reference values for nodes depend on their dimensionality. As an example, consider a NodePoint2D:

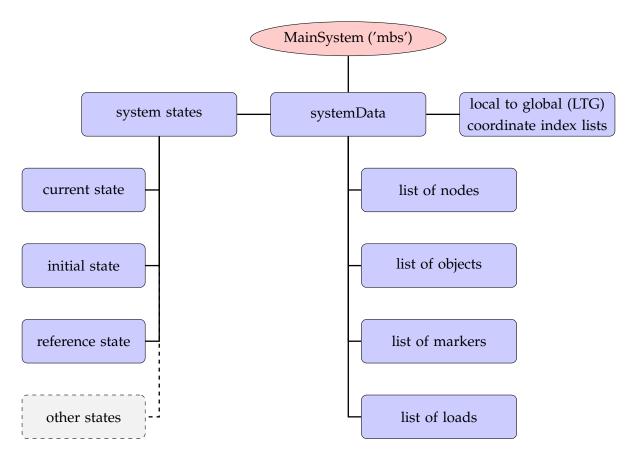


Figure 2.2: Overview of systemData, which connects items and states. Note that access to items is provided via functions in system.

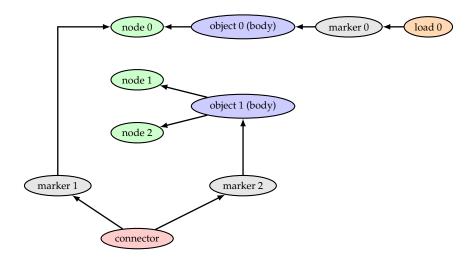


Figure 2.3: Typical interaction of items in a multibody system. Note that both, bodies and connectors/constraints are (computational) objects. The arrows indicate, that, e.g., object 1 has node 1 and node 2 (indices) and that marker 0 is attached to object 0, while load 0 uses marker 0 to apply the load. Sensors could additionally be attached to certain items.

- referenceCoordinates is a 2D vector (but could be any dimension in general nodes)
- measuring the current position of NodePoint2D gives a 3D vector
- when attaching a MarkerNodePosition and a LoadForceVector, the force will be still a 3D vector

Furthermore, the local position in 2D objects is provided by a 3D vector. Usually, the dimensionality is given in the reference manual. User errors in the dimensionality will be usually detected either by the python interface (i.e., at the time the item is created) or by the system-preprocessor

## 2.2 Items: Nodes, Objects, Loads, Markers, Sensors, ...

In this section, the most important part of EXUDYN are provided. An overview of the interaction of the items is given in Fig. 2.3

#### 2.2.1 **Nodes**

Nodes provide the coordinates (and the degrees of freedom) to the system. They have no mass, stiffness or whatsoever assigned. Without nodes, the system has no unknown coordinates. Adding a node provides (for the system unknown) coordinates. In addition we also need equations for every nodal coordinate – otherwise the system cannot be computed (NOTE: this is currently not checked by the preprocessor).

#### 2.2.2 Objects

Objects are 'computational objects' and they provide equations to your system. Objects additionally often provide derivatives and have measurable quantities (e.g. displacement) and they provide access, which can be used to apply, e.g., forces.

Objects can be a:

- general object (e.g. a controller, user defined object, ...; no example yet)
- body: has a mass or mass distribution; markers can be placed on bodies; loads can be applied; constraints can be attached via markers; bodies can be:
  - ground object: has no nodes
  - simple body: has one node (e.g. mass point, rigid body)
  - finite element and more complicated body (e.g. FFRF-object): has more than one node
- connector: uses markers to connect nodes and/or bodies; adds additional terms to system equations either based on stiffness/damping or with constraints (and Lagrange multipliers). Possible connectors:
  - algebraic constraint (e.g. constrain two coordinates:  $q_1 = q_2$ )
  - classical joint
  - spring-damper or penalty constraint

#### 2.2.3 Markers

Markers are interfaces between objects/nodes and constraints/loads. A constraint (which is also an object) or load cannot act directly on a node or object without a marker. As a benefit, the constraint or load does not need to know whether it is applied, e.g., to a node or to a local position of a body.

Typical situations are:

- Node Marker Load
- Node Marker Constraint (object)
- Body(object) Marker Load
- Body1 Marker1 Joint(object) Marker2 Body2

#### **2.2.4** Loads

Loads are used to apply forces and torques to the system. The load values are static values. However, you can use Python functionality to modify loads either by linearly increasing them during static computation or by using the 'preStepPyExecute' structure in order to modify loads in every integration step depending on time or on measured quantities (thus, creating a controller).

#### 2.2.5 Sensors

Sensors are only used to measure output variables (values) in order to simpler generate the requested output quantities. They have a very weak influence on the system, because they are only evaluated after certain solver steps as requested by the user.

### 2.2.6 Reference coordinates and displacements

Nodes usually have separated reference and initial quantities. Here, referenceCoordinates are the coordinates for which the system is defined upon creation. Reference coordinates are needed, e.g., for definition of joints and for the reference configuration of finite elements. In many cases it marks the undeformed configuration (e.g., with finite elements), but not, e.g., for ObjectConnectorSpringDamper, which has its own reference length.

Initial displacement (or rotation) values are provided separately, in order to start a system from a configuration different from the reference configuration. As an example, the initial configuration of a NodePoint is given by referenceCoordinates + initialCoordinates, while the initial state of a dynamic system additionally needs initialVelocities.

## 2.3 Exudyn Basics

This section will show:

- Interaction with the EXUDYN module
- Simulation settings
- Visualization settings
- Generating output and results
- Graphics pipeline
- Generating animations

#### 2.3.1 Interaction with the EXUDYN module

It is important that the EXUDYN module is basically a state machine, where you create items on the C++ side using the Python interface. This helps you to easily set up models using many other Python modules (numpy, sympy, matplotlib, ...) while the computation will be performed in the end on the C++ side in a very efficient manner.

#### Where do objects live?

Whenever a system container is created with SC = exu.SystemContainer(), the structure SC lives in C++ and will be modified via the python interface. Usually, the system container will hold at least one system, usually called mbs. Commands such as mbs.AddNode(...) add objects to the system mbs. The system will be prepared for simulation by mbs.Assemble() and can be solved (e.g., using SC.TimeIntegrationSolve(...)) and evaluated hereafter using the results files. Using mbs.Reset() will clear the system and allows to set up a new system. Items can be modified (ModifyObject(...)) after first initialization, even during simulation.

### 2.3.2 Simulation settings

The simulation settings consists of a couple of substructures, e.g., for solutionSettings, staticSolver, timeIntegration as well as a couple of general options – for details see Sections 6.1.1 - 6.1.7.

Simulation settings are needed for every solver. They contain solver-specific parameters (e.g., the way how load steps are applied), information on how solution files are written, and very specific control parameters, e.g., for the Newton solver.

The simulation settings structure is created with

```
simulationSettings = exu.SimulationSettings()
```

Hereafter, values of the structure can be modified, e.g.,

```
#10 seconds of simulation time:
simulationSettings.timeIntegration.endTime = 10
    #1000 steps for time integration:
simulationSettings.timeIntegration.numberOfSteps = 1000
    #assigns a new tolerance for Newton's method:
simulationSettings.timeIntegration.newton.relativeTolerance = 1e-9
    #write some output while the solver is active (SLOWER):
simulationSettings.timeIntegration.verboseMode = 2
    #write solution every 0.1 seconds:
simulationSettings.solutionSettings.solutionWritePeriod = 0.1
    #use sparse matrix storage and solver (package Eigen):
    simulationSettings.linearSolverType = exu.LinearSolverType.EigenSparse
```

### 2.3.3 Visualization settings

Visualization settings are used for user interaction with the model. E.g., the nodes, markers, loads, etc., can be visualized for every model. There are default values, e.g., for the size of nodes, which may be inappropriate for your model. Therefore, you can adjust those parameters. In some cases, huge models require simpler graphics representation, in order not to slow down performance – e.g., the number of faces to represent a cylinder should be small if there are 10000s of cylinders drawn. Even computation performance can be slowed down, if visualization takes lots of CPU power. However, visualization is performed in a separate thread, which usually does not influence the computation exhaustively. Details on visualization settings and its substructures are provided in Sections 6.2.1 – 6.2.13.

The visualization settings structure can be accessed in the system container SC (access per reference, no copying!), accessing every value or structure directly, e.g.,

```
SC.visualizationSettings.nodes.defaultSize = 0.001 #draw nodes very small
#change openGL parameters; current values can be obtained from SC.GetRenderState()
#change zoom factor:
SC.visualizationSettings.openGL.initialZoom = 0.2
#set the center point of the scene (can be attached to moving object):
SC.visualizationSettings.openGL.initialCenterPoint = [0.192, -0.0039, -0.075]
```



Figure 2.4: Basic solver flow chart for SolveSystem(). This flow chart is the same for static solver and for time integration.

```
#turn of auto-fit:
SC.visualizationSettings.general.autoFitScene = False

#change smoothness of a cylinder:
SC.visualizationSettings.general.cylinderTiling = 100

#make round objects flat:
SC.visualizationSettings.openGL.shadeModelSmooth = False

#turn on coloured plot, using y-component of displacements:
SC.visualizationSettings.contour.outputVariable = exu.OutputVariableType.
    Displacement
SC.visualizationSettings.contour.outputVariableComponent = 1 #0=x, 1=y, 2=z
```

#### 2.3.4 Solver

Both in the static as well as in the dynamic case, the solver runs in a loop to solve a nonlinear system of (differential and/or algebraic) equations over a given time or load interval. For the time integration (dynamic solver), Fig. 2.4 shows the basic loops for the solution process. The inner loops are shown in Fig. 2.6 and Fig. 2.7. The static solver behaves very similar, while no velocities or accelerations need to be solved and time is replaced by load steps.

Settings for the solver substructures, like timer, output, iterations, etc. are described in Sections 6.3.1 - 6.3.5. The description of interfaces for solvers starts in Section 6.3.6.

#### 2.3.5 Generating output and results

The solvers provide a number of options in solutionSettings to generate a solution file. As a default, exporting solution to the solution file is activated with a writing period of 0.01 seconds.

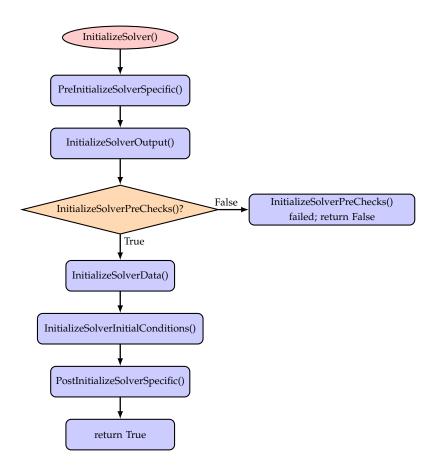


Figure 2.5: Basic solver flow chart for function InitializeSolver().

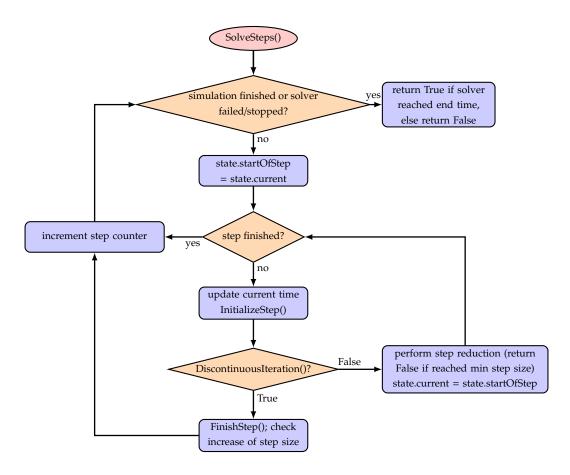


Figure 2.6: Solver flow chart for SolveSteps(), which is the inner loop of the solver.

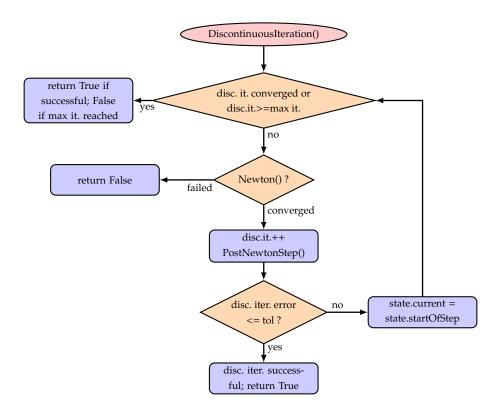


Figure 2.7: Solver flow chart for DiscontinuousIteration(), which is run for every solved step inside the static/dynamic solvers. If the DiscontinuousIteration() returns False, SolveSteps() will try to reduce the step size.

#### Typical output settings are:

```
#create a new simulationSettings structure:
simulationSettings = exu.SimulationSettings()

#activate writing to solution file:
simulationSettings.solutionSettings.writeSolutionToFile = True
#write results every 1ms:
simulationSettings.solutionSettings.solutionWritePeriod = 0.001

#assign new filename to solution file
simulationSettings.solutionSettings.coordinatesSolutionFileName= "myOutput.txt"

#do not export certain coordinates:
simulationSettings.solutionSettings.exportDataCoordinates = False
```

## 2.3.6 Graphics pipeline

The user cannot interact with the visualization part for now. There are basically two loops during simulation, which feed the graphics pipeline. The solver runs a loop:

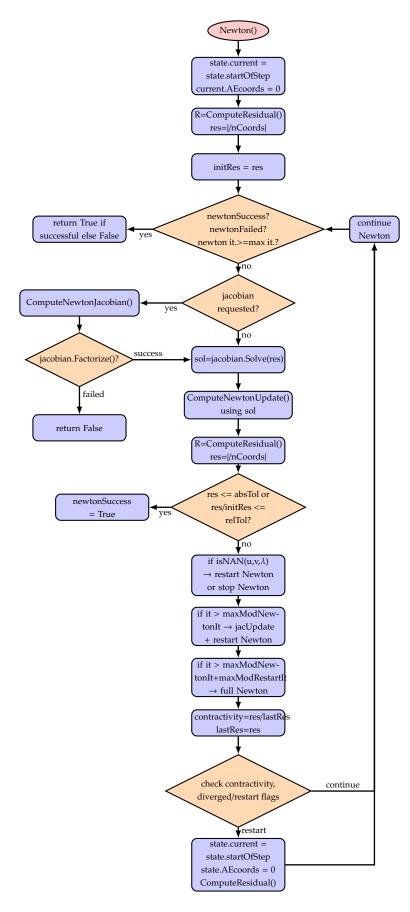


Figure 2.8: Solver flow chart for Newton(), which is run inside the DiscontinuousIteration(). The shown case is valid for newtonResidualMode = 0.

- compute new step
- finish computation step; results are in current state
- copy current state to visualization state (thread safe)
- signal graphics pipeline that new visualization data is available

The openGL graphics thread runs the following loop:

- render openGL scene with a given graphicsData structure (containing lines, faces, text, ...)
- go idle for some milliseconds
- check if openGL rendering needs an update (e.g. due to user interaction)
  - → if update is needed, the visualization of all items is updated stored in a graphicsData structure)
- check if new visualization data is available and the time since last update is larger than a presribed value, the graphicsData structure is updated with the new visualization state

#### 2.3.7 Generating animations

In many dynamics simulations, it is very helpful to create animations in order to better understand the motion of bodies. Specifically, the animation can be used to visualize the model much slower or faster than the model is computed.

Animations are created based on a series of images (frames, snapshots) taken during simulation. It is important, that the current view is used to record these images – this means that the view should not be changed during the recording of images. To turn on recording of images during solving, set the following flag to a positive value

• simulationSettings.solutionSettings.recordImagesInterval = 0.01

which means, that after every 0.01 seconds of simulation time, an image of the current view is taken and stored in the directory and filename (without filename ending) specified by

• SC.visualizationSettings.exportImages.saveImageFileName = "myFolder/frame"

By default, a consecutive numbering is generated for the image, e.g., 'frame0000.tga, frame0001.tga,...'. Note that '.tga' files contain raw image data and therefore can become very large.

To create animation files, an external tool FFMPEG is used to efficiently convert a series of images into an animation. In windows, simple DOS batch files can do the job to convert frames given in the local directory to animations, e.g.:

```
echo off

REM 2019-12-23, Johannes Gerstmayr

REM helper file for EXUDYN to convert all frame00000.tga, frame00001.tga, ... files to a video

REM for higher quality use crf option (standard: -crf 23, range: 0-51, lower crf value means higher quality)

IF EXIST animation.mp4 (
```

```
echo "animation.mp4 already exists! rename the file"

) ELSE (

"C:\Program Files (x86)\FFMPEG\bin\ffmpeg.exe" -r 25 -start_number 0 -i frame%%05d.

tga -c:v libx264 -vf "fps=25,format=yuv420p" animation.mp4

)
```

After the video has been created, you should delete the single images:

```
REM 2019-12-23, Johannes Gerstmayr
REM helper file for EXUDYN
REM delete all .tga images of current directory
del *.tga
```

#### 2.4 C++ Code

This section covers some information on the C++ code. For more information see the Open source code and use doxygen.

Exudyn was developed for the efficient simulation of flexible multi-body systems. Exudyn was designed for rapid implementation and testing of new formulations and algorithms in multibody systems, whereby these algorithms can be easily implemented in efficient C++ code. The code is applied to industry-related research projects and applications.

#### 2.4.1 Focus of the C++ code

#### Four principles:

- 1. developer-friendly
- 2. error minimization
- 3. efficiency
- 4. user-friendliness

The focus is therefore on:

- A developer-friendly basic structure regarding the C++ class library and the possibility to add new components.
- The basic libraries are slim, but extensively tested; only the necessary components are available
- Complete unit tests are added to new program parts during development; for more complex processes, tests are available in Python
- In order to implement the sometimes difficult formulations and algorithms without errors, error avoidance is always prioritized.

- To generate efficient code, classes for parallelization (vectorization and multithreading) are provided. We live the principle that parallelization takes place on multi-core processors with a central main memory, and thus an increase in efficiency through parallelization is only possible with small systems, as long as the program runs largely in the cache of the processor cores. Vectorization is tailored to SIMD commands as they have Intel processors, but could also be extended to GPGPUs in the future.
- The user interface (Python) provides a 1:1 image of the system and the processes running in it, which can be controlled with the extensive possibilities of Python.

#### 2.4.2 C++ Code structure

The functionality of the code is based on systems (MainSystem/CSystem) representing the multibody system or similar physical systems to be simulated. Parts of the core structure of Exudyn are:

- CSystem / MainSystem: a multibody system which consists of nodes, objects, markers, loads, etc.
- SystemContainer: holds a set of systems; connects to visualization (container)
- node: used to hold coordinates (unknowns)
- (computational) object: leads to equations, using nodes
- marker: defines a consistent interface to objects (bodies) and nodes; write access ('AccessFunction')
   provides jacobian and read access ('OutputVariable')
- load: acts on an object or node via a marker
- computational objects: efficient objects for computation = bodies, connectors, connectors, loads, nodes, ...
- visualization objects: interface between computational objects and 3D graphics
- main (manager) objects: do all tasks (e.g. interface to visualization objects, GUI, python, ...) which are not needed during computation
- static solver, kinematic solver, time integration
- python interface via pybind11; items are accessed with a dictionary interface; system structures and settings read/written by direct access to the structure (e.g. SimulationSettings, Visualization-Settings)
- interfaces to linear solvers; future: optimizer, eigenvalue solver, ... (mostly external or in python)

#### 2.4.3 C++ Code: Modules

The following internal modules are used, which are represented by directories in main/src:

- Autogenerated: item (nodes, objects, markers and loads) classes split into main (management, python connection), visualization and computation
- Graphics: a general data structure for 2D and 3D graphical objects and a tiny openGL visualization; linkage to GLFW

- Linalg: Linear algebra with vectors and matrices; separate classes for small vectors (SlimVector), large vectors (Vector and ResizableVector), vectors without copying data (LinkedDataVector), and vectors with constant size (ConstVector)
- Main: mainly contains SystemContainer, System and ObjectFactory
- Objects: contains the implementation part of the autogenerated items
- Pymodules: manually created libraries for linkage to python via pybind; remaining linking to python is located in autogenerated folder
- pythonGenerator: contains python files for automatic generation of C++ interfaces and python interfaces of items;
- Solver: contains all solvers for solving a CSystem
- System: contains core item files (e.g., MainNode, CNode, MainObject, CObject, ...)
- Tests: files for testing of internal linalg (vector/matrix), data structure libraries (array, etc.) and functions
- Utilities: array structures for administrative/managing tasks (indices of objects ... bodies, forces, connectors, ...); basic classes with templates and definitions

The following main external libraries are linked to Exudyn:

- LEST: for testing of internal functions (e.g. linalg)
- GLFW: 3D graphics with openGL; cross-platform capabilities
- Eigen: linear algebra for large matrices, linear solvers, sparse matrices and link to special solvers
- pybind11: linking of C++ to python

#### 2.4.4 Code style and conventions

This section provides general coding rules and conventions, partly applicable to the C++ and python parts of the code. Many rules follow common conventions (e.g., google code style, but not always – see notation):

- write simple code (no complicated structures or uncommon coding)
- write readable code (e.g., variables and functions with names that represent the content or functionality; AVOID abbreviations)
- put a header in every file, according to Doxygen format
- put a comment to every (global) function, member function, data member, template parameter
- ALWAYS USE curly brackets for single statements in 'if', 'for', etc.; example: if (i<n)  $\{i += 1;\}$
- use Doxygen-style comments (use '//!' Qt style and '@ date' with '@' instead of 'for commands)
- use Doxygen (with preceeding '@') 'test' for tests, 'todo' for todos and 'bug' for bugs
- USE 4-spaces-tab
- use C++11 standards when appropriate, but not exhaustively
- ONE class ONE file rule (except for some collectors of single implementation functions)
- add complete unit test to every function (every file has link to LEST library)

- avoid large classes (>30 member functions; > 15 data members)
- split up god classes (>60 member functions)
- mark changed code with your name and date
- REPLACE tabs by spaces: Extras->Options->C/C++->Tabstopps: tab stopp size = 4 (=standard)
   KEEP SPACES=YES

#### 2.4.5 Notation conventions

The following notation conventions are applied (**no exceptions!**):

- use lowerCamelCase for names of variables (including class member variables), consts, c-define variables, ...; EXCEPTION: for algorithms following formulas, e.g.,  $f = M * q_t t + K * q$ , GBar, ...
- use UpperCamelCase for functions, classes, structs, ...
- Special cases for CamelCase: write 'ODEsystem', BUT: 'ODE1Equations'
- '[...]Init' ... in arguments, for initialization of variables; e.g. 'valueInit' for initialization of member variable 'value'
- use American English troughout: Visualization, etc.
- for (abbreviations) in captial letters, e.g. ODE, use a lower case letter afterwards:
- do not use consecutive capitalized words, e.g. DO NOT WRITE 'ODEAE'
- for functions use ODEComputeCoords(), for variables avoid 'ODE' at beginning: use nODE or write odeCoords
- do not use '\_' within variable or function names; exception: derivatives
- use name which exactly describes the function/variable: 'numberOfItems' instead of 'size' or 'l'
- examples for variable names: secondOrderSize, massMatrix, mThetaTheta
- examples for function/class names: SecondOrderSize, EvaluateMassMatrix, Position(const Vector3D& localPosition)
- use the Get/Set...() convention if data is retrieved from a class (Get) or something is set in a class (Set); Use const T& Get()/T& Get if direct access to variables is needed; Use Get/Set for pybind11
- (Set); Use const T& Get()/T& Get if direct access to variables is needed; Use Get/Set for pybind11
   example Get/Set: Real\* GetDataPointer(), Vector::SetAll(Real), GetTransposed(), SetRotationalParameters
- use 'Real' instead of double or float: for compatibility, also for AVX with SP/DP
- use 'Index' for array/vector size and index instead of size\_t or int
- item: object, node, marker, load: anything handled within the computational/visualization systems

#### 2.4.6 No-abbreviations-rule

SetColor(...), ...

The code uses a **minimum set of abbreviations**; however, the following abbreviation rules are used throughout: In general: DO NOT ABBREVIATE function, class or variable names: GetDataPointer() instead of GetPtr(); exception: cnt, i, j, k, x or v in cases where it is really clear (5-line member functions).

Exceptions to the NO-ABBREVIATIONS-RULE:

- ODE ... ordinary differential equations;
- ODE2 ... marks parts related to second order differential equations (SOS2, EvalF2 in HOTINT)
- ODE1 ... marks parts related to first order differential equations (ES, EvalF in HOTINT)
- AE ... algebraic equations (IS, EvalG in HOTINT); write 'AEcoordinates' for 'algebraicEquation-sCoordinates'
- 'C[...]' ... Computational, e.g. for ComputationalNode ==> use 'CNode'
- min, max ... minimum and maximum
- write time derivatives with underscore: \_t, \_tt; example: Position\_t, Position\_tt, ...
- write space-wise derivatives ith underscore: \_x, \_xx, \_y, ...
- if a scalar, write coordinate derivative with underscore: \_q, \_v (derivative w.r.t. velocity coordinates)
- for components, elements or entries of vectors, arrays, matrices: use 'item' throughout
- '[...]Init' ... in arguments, for initialization of variables; e.g. 'valueInit' for initialization of member variable 'value'

## 2.5 Changes

The following list covers changes in the python interface and functionality:

#### • Version $0.1.288 \rightarrow \text{Version } 0.1.289$

Changes in the python interface (ESSENTIAL!):

Added time 't' as additional first argument in user functions: ObjectCoordinateSpringD
 ObjectConnectorCoordinateSpringDamper, ObjectConnectorCartesianSpringDamper

#### • Version 0.1.287 → Version 0.1.288

Changes in the python interface (ESSENTIAL!):

- changed the name of initialDisplacements to initialCoordinates in all Nodes for consisten reasons with rotation parameters!

#### • Version 0.1.282 → Version 0.1.284

Changes in the python interface:

 all bodyFixed parameters in MarkerRigidBody, which were inactive so far, have been eliminated

#### • Version 0.1.260 → Version 0.1.263

Changes in the python interface:

- mbs.systemData.GetCurrentTime() → mbs.systemData.GetTime()
- mbs.systemData.GetVisualizationTime() → mbs.systemData.GetTime(configurationType=exu.C

#### • Version 0.1.244 → Version 0.1.245

Changes in the implementation / solver (LEADS TO DIFFERENT RESULTS):

- **Solvers updated**: static solver and time integration have been updated; old solvers are still available with the 'OldSolver' extension

Changes in the python interface (new functions / interface to call the old solvers):

- SC.SolveStaticOldSolver(...)
- SC.TimeIntegrationSolve(mbs, 'GeneralizedAlphaOldSolver', simulationSettings)

#### • Version 0.1.243 → Version 0.1.244

Changes in the python interface:

- simulationSettings.staticSolver.pauseAfterEachStep
  - → simulationSettings.pauseAfterEachStep (merged with timeIntegration.pauseAfterEachStep

#### • Version $0.1.238 \rightarrow \text{Version } 0.1.240$

Changes in the implementation / solver (LEADS TO DIFFERENT RESULTS):

- generalizedAlpha: corrected initialization of algorithmic acceleration for discontinuous iteration
- time integration: corrected time t for evaluation of RHS from beginning to end of time step (improves accuracy for time-dependent loads significantly)

Changes in the python interface:

- simulationSettings.timeIntegration.pauseAfterEachStep
  - → simulationSettings.pauseAfterEachStep
- ADDED: simulationSettings.timeIntegration.verboseModeFile
- ADDED: simulationSettings.staticSolver.verboseModeFile

## Chapter 3

## **Tutorial**

This section will show:

- A basic tutorial for a 1D mass and spring-damper with initial displacements, shortest possible model with practically no special settings
- A more advanced 2D rigid-body model (coming soon)
- Links to examples section

The python source code of this section can be found in the file:

```
main/pythonDev/Examples/springDamperTutorial.py
```

This tutorial will set up a mass point and a spring damper, dynamically compute the solution and evaluate the reference solution.

To start up, we set the system path to the directory of the library (needs to be adjusted; can be relative or absolute path):

```
import sys
sys.path.append('../../bin/WorkingRelease') #chose path of WorkingRelease!!!
```

We import the exudyn library and the interface for all nodes, objects, markers, loads and sensors:

```
import exudyn as exu
from itemInterface import *
import numpy as np #for postprocessing
```

Next, we need a SystemContainer, which contains all computable systems and add a new system. Per default, you always should name your system 'mbs' (multibody system), in order to copy/paste code parts from other examples, tutorials and other projects:

```
SC = exu.SystemContainer()
mbs = SC.AddSystem()
```

In order to check, which version you are using, you can printout the current EXUDYN version. This version is in line with the issue tracker and marks the number of open/closed issues added to EXUDYN:

```
print('EXUDYN version='+exu.__version__)
```

Using the powerful Python language, we can define some variables for our problem, which will also be used for the analytical solution:

```
L=0.5 #reference position of mass

mass = 1.6 #mass in kg

spring = 4000 #stiffness of spring—damper in N/m

damper = 8 #damping constant in N/(m/s)

f =80 #force on mass
```

For the simple spring-mass-damper system, we need initial displacements and velocities:

```
u0=-0.08  #initial displacement
v0=1  #initial velocity
x0=f/spring  #static displacement
print('resonance frequency = '+str(np.sqrt(spring/mass)))
print('static displacement = '+str(x0))
```

We first need to add nodes, which provide the coordinates (and the degrees of freedom) to the system. The following line adds a 3D node for 3D mass point<sup>1</sup>:

Here, Point (=NodePoint) is a Python class, which takes a number of arguments defined in the reference manual. The arguments here are referenceCoordinates, which are the coordinates for which the system is defined. The initial configuration is given by referenceCoordinates + initialCoordinates, while the initial state additionally gets initialVelocities.

While Point adds 3 unknown coordinates to the system, which need to be solved, we also can add ground nodes, which can be used similar to nodes, but they do not have unknown coordinates – and therefore also have no initial displacements or velocities. The advantage of ground nodes (and ground bodies) is that no constraints are needed to fix these nodes. Such a ground node is added via:

```
nGround=mbs.AddNode(NodePointGround(referenceCoordinates = [0,0,0]))
```

In the next step, we add an object<sup>2</sup>, which provides equations for coordinates. The MassPoint needs at least a mass (kg) and a node number to which the mass point is attached. Additionally, graphical objects could be attached:

```
massPoint = mbs.AddObject(MassPoint(physicsMass = mass, nodeNumber = n1))
```

<sup>&</sup>lt;sup>1</sup>Note: Point is an abbreviation for NodePoint, defined in itemInterface.py.

<sup>&</sup>lt;sup>2</sup>For the moment, we just need to know that objects either depend on one or more nodes, which are usually bodies and finite elements, or they can be connectors, which connect (the coordinates of) objects via markers, see Section 2.1.

In order to apply constraints and loads, we need markers. These markers are used as local positions (and frames), where we can attach a constraint lateron. In this example, we work on the coordinate level, both for forces as well as for constraints. Markers are attached to the according ground and regular node number, additionally using a coordinate number (0 ... first coordinate):

This means that loads can be applied to the first coordinate of node n1 via marker with number nodeMarker.

Now we add a spring-damper to the markers with numbers groundMarker and the nodeMarker, providing stiffness and damping parameters:

A load is added to marker nodeMarker, with a scalar load with value f:

Finally, a sensor is added to the coordinate constraint object nC, requesting the output variable Force:

Note that sensors can be attached, e.g., to nodes, bodies, objects (constraints) or loads. As our system is fully set, we can print the overall information and assemble the system to make it ready for simulation:

```
print(mbs)
mbs.Assemble()
```

We will use time integration and therefore define a number of steps (fixed step size; must be provided) and the total time span for the simulation:

```
steps = 1000 #number of steps to show solution
tEnd = 1 #end time of simulation
```

All settings for simulation, see according reference section, can be provided in a structure given from exu.SimulationSettings(). Note that this structure will contain all default values, and only non-default values need to be provided:

```
simulationSettings = exu.SimulationSettings()
```

```
simulationSettings.solutionSettings.solutionWritePeriod = 5e-3 #output interval
    general
simulationSettings.solutionSettings.sensorsWritePeriod = 5e-3 #output interval of
    sensors
simulationSettings.timeIntegration.numberOfSteps = steps
simulationSettings.timeIntegration.endTime = tEnd
```

We are using a generalized alpha solver, where numerical damping is needed for index 3 constraints. As we have only spring-dampers, we can set the spectral radius to 1, meaning no numerical damping:

```
simulationSettings.timeIntegration.generalizedAlpha.spectralRadius = 1
```

In order to visualize the results online, a renderer can be started. As our computation will be very fast, it is a good idea to wait for the user to press SPACE, before starting the simulation (uncomment second line):

As the simulation is still very fast, we will not see the motion of our node. Using e.g. steps=10000000 in the lines above allows you online visualize the resulting oscillations.

Finally, we start the solver, by telling which system to be solved, solver type and the simulation settings:

```
SC. TimeIntegrationSolve(mbs, 'GeneralizedAlpha', simulationSettings)
```

After simulation, our renderer needs to be stopped (otherwise it would stay in background and prohibit further simulations). Sometimes you would like to wait until closing the render window, using WaitForRenderEngineStopFlag():

```
#SC.WaitForRenderEngineStopFlag()#wait for pressing 'Q' to quit
exu.StopRenderer() #safely close rendering window!
```

There are several ways to evaluate results, see the reference pages. In the following we take the final value of node n1 and read its 3D position vector:

```
#evaluate final (=current) output values
u = mbs.GetNodeOutput(n1, exu.OutputVariableType.Position)
print('displacement=',u)
```

The following code generates a reference (exact) solution for our example:

```
import matplotlib.pyplot as plt
import matplotlib.ticker as ticker

omega0 = np.sqrt(spring/mass) #eigen frequency of undamped system
dRel = damper/(2*np.sqrt(spring*mass)) #dimensionless damping
omega = omega0*np.sqrt(1-dRel**2) #eigen freq of damped system
```

```
C1 = u0-x0 #static solution needs to be considered!
C2 = (v0+omega0*dRel*C1) / omega #C1, C2 are coeffs for solution

refSol = np.zeros((steps+1,2))

for i in range(0, steps+1):
    t = tEnd*i/steps
    refSol[i,0] = t
    refSol[i,1] = np.exp(-omega0*dRel*t)*(C1*np.cos(omega*t)+C2*np.sin(omega*t))+x0

plt.plot(refSol[:,0], refSol[:,1], 'r-', label='displacement (m); exact solution')
```

Now we can load our results from the default solution file coordinatesSolution.txt, which is in the same directory as your python tutorial file. For convenient reading the file containing commented lines, we use a numpy feature and finally plot the displacement of coordinate 0 or our mass point<sup>3</sup>:

```
data = np.loadtxt('coordinatesSolution.txt', comments='#', delimiter=',')
plt.plot(data[:,0], data[:,1], 'b-', label='displacement (m); numerical solution')
```

The sensor result can be loaded in the same way. The sensor output format contains time in the first column and sensor values in the remaining columns. The number of columns depends on the sensor and the output quantity (scalar, vector, ...):

```
data = np.loadtxt('groundForce.txt', comments='#', delimiter=',')
plt.plot(data[:,0], data[:,1]*1e-3, 'g-', label='force (kN)')
```

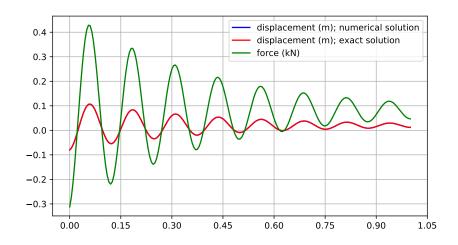
In order to get a nice plot within Spyder, the following options can be used<sup>4</sup>:

```
ax=plt.gca() # get current axes
ax.grid(True, 'major', 'both')
ax.xaxis.set_major_locator(ticker.MaxNLocator(10))
ax.yaxis.set_major_locator(ticker.MaxNLocator(10))
plt.legend() #show labels as legend
plt.tight_layout()
plt.show()
```

The matplotlib output should look like this:

<sup>&</sup>lt;sup>3</sup>data[:,0] contains the simulation time, data[:,1] contains displacement of (global) coordinate 0, data[:,2] contains displacement of (global) coordinate 1, ...)

<sup>&</sup>lt;sup>4</sup>note, in some environments you need finally the command plt.show()



Further examples can be found in your copy of exudyn:

main/pythonDev/Examples
main/pythonDev/TestModels

## Chapter 4

# Python-C++ command interface

This section lists the basic interface functions which can be used to set up a EXUDYN model in Python.

To import the module, just include the EXUDYN module in Python (for compatibility with examples and other users, we recommend to use the 'exu' abbreviation throughout)<sup>1</sup>:

```
import exudyn as exu
```

The exudyn module will usually hold one SystemContainer, which is a class that is initialized by assigning a system container to a variable, usually denoted as 'SC':

```
SC = exu.SystemContainer()
```

Furthermore, there are a couple of commands available directly in the EXUDYN module, given in the following subsections. Regarding the **(basic) module access**, functions are related to the 'exudyn = exu' module, see these examples:

```
import exudyn as exu

SC = exu.SystemContainer()
exu.InfoStat()
exu.Go()
nInvalid = exu.InvalidIndex()
```

Understanding the usage of functions for python object 'SystemContainer' provided by EXUDYN, the following examples might help:

```
import exudyn as exu
SC = exu.SystemContainer()
mbs = SC.AddSystem()
nSys = SC.NumberOfSystems()
print(nSys)
SC.Reset()
```

<sup>&</sup>lt;sup>1</sup>note that there is a second module, called exudynFast, which does deactivates all range-, index- or memory allocation checks at the gain of higher speed (probably 30 percent in regular cases). To check which version you have, just type exu.\_\_doc\_\_ and you will see a note on 'exudynFast' in the exudynFast module.

Understanding the usage of functions for the 'MainSystem' provided by SystemContainer, the following examples might help:

```
import exudyn as exu

SC = exu.SystemContainer()

mbs = SC.AddSystem()

mbs.Reset()

mbs.WaitForUserToContinue()
```

## 4.1 EXUDYN

These are the access functions to the EXUDYN module.

function/structure name	description
Go()	Creates a SystemContainer SC and a main system mbs
InfoStat()	Print some global (debug) information: linear algebra,
	memory allocation, threads, computational efficiency, etc.
StartRenderer(verbose = false)	Start OpenGL rendering engine (in separate thread); use
	verbose=True to output information during OpenGL win-
	dow creation
StopRenderer()	Stop OpenGL rendering engine
SetOutputPrecision(numberOfDigits)	Set the precision (integer) for floating point numbers writ-
	ten to console (reset when simulation is started!)
SetLinalgOutputFormatPython(flagPythonFormat)	true: use python format for output of vectors and matrices;
	false: use matlab format
InvalidIndex()	This function provides the invalid index, which depends
	on the kind of 32-bit, 64-bit signed or unsigned integer;
	e.g. node index or item index in list
SetWriteToConsole(flag)	set flag to write (true) or not write to console; default =
	true
SetWriteToFile(filename, flagWriteToFile = true, flagAp-	set flag to write (true) or not write to console; default
pend = false)	value of flagWriteToFile = false; flagAppend appends
	output to file, if set true; in order to finalize the file, write
	exu.SetWriteToFile(", False) to close the output file
	EXAMPLE:
	exu.SetWriteToConsole(False) #no output to console
	exu.SetWriteToFile(filename='testOutput.log', flag-
	WriteToFile=True, flagAppend=False)
	exu.Print('print this to file')
	exu.SetWriteToFile(", False) #terminate writing to file
	which closes the file
Set Print Delay Milli Seconds (delay Milli Seconds)	add some delay (in milliSeconds) to printing to console,
	in order to let Spyder process the output; default = 0

Print()	this allows printing via exudyn with similar syntax as
	in python print(args) except for keyword arguments:
	print('test=',42); allows to redirect all output to file
	given by SetWriteToFile(); does not output in case that
	SetWriteToConsole is set to false
variables	this dictionary may be used by the user to store exudyn-
	wide data in order to avoid global python variables; usage:
	exu.variables["myvar"] = 42
sys	this dictionary is used by the system, e.g. for testsuite or
	solvers to store exudyn-wide data in order to avoid global
	python variables

## 4.2 SystemContainer

The SystemContainer is the top level of structures in EXUDYN. The container holds all systems, solvers and all other data structures for computation. Currently, only one container shall be used. In future, multiple containers might be usable at the same time.

#### Example:

import exudyn as exu
SC = exu.SystemContainer()
mbs = SC.AddSystem()

function/structure name	description
AddSystem()	add a new computational system
Reset()	delete all systems and reset SystemContainer (including
	graphics)
NumberOfSystems()	obtain number of systems available in system container
GetSystem(systemNumber)	obtain systems with index from system container
WaitForRenderEngineStopFlag()	Wait for user to stop render engine (Press 'Q' or Escape-
	key)
RenderEngineZoomAll()	Send zoom all signal, which will perform zoom all at next
	redraw request
GetRenderState()	Get dictionary with current render state (openGL zoom,
	modelview, etc.)
	EXAMPLE:
	SC = exu.SystemContainer()
	renderState = SC.GetRenderState()
	print(renderState['zoom'])
SetRenderState(renderState)	Set current render state (openGL zoom, modelview, etc.)
	with given dictionary; usually, this dictionary has been
	obtained with GetRenderState
	EXAMPLE:
	SC = exu.SystemContainer()
	SC.GetRenderState(renderState)

RedrawAndSaveImage()	Redraw openGL scene and save image (command waits
<b>.</b>	until process is finished)
TimeIntegrationSolve(mainSystem, solverName, simula-	Call time integration solver for given system with
tionSettings)	solverName ('RungeKutta1'explicit solver, 'General-
	izedAlpha'implicit solver); use simulationSettings to
	individually configure the solver
	EXAMPLE:
	simSettings = exu.SimulationSettings()
	simSettings.timeIntegration.numberOfSteps = 1000
	simSettings.timeIntegration.endTime = 2
	simSettings.timeIntegration.verboseMode = 1
	SC.TimeIntegrationSolve(mbs,'GeneralizedAlpha',simSetti
StaticSolve(mainSystem, simulationSettings)	Call solver to compute a static solution of the system, con-
	sidering acceleration and velocity coordinates to be zero
	(initial velocities may be considered by certain objects)
	EXAMPLE:
	simSettings = exu.SimulationSettings()
	simSettings.staticSolver.newton.relativeTolerance = 1e-6
	SC.StaticSolve(mbs, simSettings)
visualizationSettings	this structure is read/writeable and contains visualization
	settings, which are immediately applied to the rendering
	window.
	EXAMPLE:
	SC = exu.SystemContainer()
	SC.visualizationSettings.autoFitScene=False

## 4.3 MainSystem

This is the structure which defines a (multibody) system. In C++, there is a MainSystem (links to python) and a System (computational part). For that reason, the name is MainSystem on the python side, but it is often just called 'system'. It can be created, visualized and computed. Use the following functions for system manipulation.

#### Usage:

```
import exudyn as exu
SC = exu.SystemContainer()
mbs = SC.AddSystem()
```

function/structure name	description
Assemble()	assemble items (nodes, bodies, markers, loads,);
	Calls CheckSystemIntegrity(), AssembleCoordinates(),
	AssembleLTGLists(), and AssembleInitializeSystemCoor-
	dinates()

AssembleCoordinates()	assemble coordinates: assign computational coordinates to nodes and constraints (algebraic variables)
AssembleLTGLists()	build local-to-global (ltg) coordinate lists for objects (used to build global ODE2RHS, MassMatrix, etc. vectors and matrices)
AssembleInitializeSystemCoordinates()	initialize all system-wide coordinates based on initial values given in nodes
Reset()	reset all lists of items (nodes, bodies, markers, loads,) and temporary vectors; deallocate memory
WaitForUserToContinue()	interrupt further computation until user input -> 'pause' function
SendRedrawSignal()	this function is used to send a signal to the renderer that the scene shall be redrawn because the visualization state has been updated
GetRenderEngineStopFlag()	get the current stop simulation flag; true=user wants to stop simulation
SetRenderEngineStopFlag()	set the current stop simulation flag; set to false, in order to continue a previously user-interrupted simulation
repr()	return the representation of the system, which can be, e.g., printed EXAMPLE: print(mbs)
systemIsConsistent	this flag is used by solvers to decide, whether the system is in a solvable state; this flag is set to false as long as Assemble() has not been called; any modification to the system, such as Add(), Modify(), etc. will set the flag to false again; this flag can be modified (set to true), if a change of e.g. an object (change of stiffness) or load (change of force) keeps the system consistent, but would normally lead to systemIsConsistent=False
interactiveMode	set this flag to true in order to invoke a Assemble() command in every system modification, e.g. AddNode, AddObject, ModifyNode,; this helps that the system can be visualized in interactive mode.
variables	this dictionary may be used by the user to store model- specific data, in order to avoid global python variables in complex models; mbs.variables["myvar"] = 42
sys	this dictionary is used by exudyn python libraries, e.g., solvers, to avoid global python variables
solverSignalJacobianUpdate	this flag is used by solvers to decide, whether the jacobian should be updated; at beginning of simulation and after jacobian computation, this flag is set automatically to False; use this flag to indicate system changes, e.g. during time integration
systemData	Access to SystemData structure; enables access to number of nodes, objects, and to (current, initial, reference,) state variables (ODE2, AE, Data,)

#### 4.3.1 MainSystem: Node

This section provides functions for adding, reading and modifying nodes. Nodes are used to define coordinates (unknowns to the static system and degrees of freedom if constraints are not present). Nodes can provide various types of coordinates for second/first order differential equations (ODE2/ODE1), algebraic equations (AE) and for data (history) variables – which are not providing unknowns in the nonlinear solver but will be solved in an additional nonlinear iteration for e.g. contact, friction or plasticity.

function/structure name	description
AddNode(pyObject)	add a node with nodeDefinition from Python node class;
	returns (global) node number of newly added node
	EXAMPLE:
	item = Rigid2D( referenceCoordinates= [1,0.5,0], initialVe-
	locities= [10,0,0])
	mbs.AddNode(item)
	nodeDict = {'nodeType': 'Point',
	'referenceCoordinates': [1.0, 0.0, 0.0],
	'initialCoordinates': [0.0, 2.0, 0.0],
	'name': 'example node'}
	mbs.AddNode(nodeDict)
GetNodeNumber(nodeName)	get node's number by name (string)
	EXAMPLE:
	n = mbs.GetNodeNumber('example node')
GetNode(nodeNumber)	get node's dictionary by index
	EXAMPLE:
	nodeDict = mbs.GetNode(0)
ModifyNode(nodeNumber, nodeDict)	modify node's dictionary by index
	EXAMPLE:
	mbs.ModifyNode(nodeNumber, nodeDict)
GetNodeDefaults(typeName)	get node's default values for a certain nodeType as (dic-
	tionary)
	EXAMPLE:
	nodeType = 'Point'
	nodeDict = mbs.GetNodeDefaults(nodeType)
GetNodeOutput(nodeNumber, variableType, configura-	get the ouput of the node specified with the OutputVari-
tion = ConfigurationType.Current)	ableType; default configuration = 'current'; output may
	be scalar or array (e.g. displacement vector)
	EXAMPLE:
	mbs.GetNodeOutput(nodeNumber=0, variable-
	Type='exu.OutputVariable.Displacement')
GetNodeODE2Index(nodeNumber)	get index in the global ODE2 coordinate vector for the first
	node coordinate of the specified node
	EXAMPLE:
	mbs.GetNodeODE2Index(nodeNumber=0)
GetNodeParameter(nodeNumber, parameterName)	get nodes's parameter from nodeNumber and parame-
	terName; parameter names can be found for the specific
	items in the reference manual

SetNodeParameter(nodeNumber,	parameterName,	set parameter 'parameterName' of node with nodeNum-
value)		ber to value; parameter names can be found for the specific
		items in the reference manual

#### 4.3.2 MainSystem: Object

This section provides functions for adding, reading and modifying objects, which can be bodies (mass point, rigid body, finite element, ...), connectors (spring-damper or joint) or general objects. Objects provided terms to the residual of equations resulting from every coordinate given by the nodes. Single-noded objects (e.g. mass point) provides exactly residual terms for its nodal coordinates. Connectors constrain or penalize two markers, which can be, e.g., position, rigid or coordinate markers. Thus, the dependence of objects is either on the coordinates of the marker-objects/nodes or on nodes which the objects possess themselves.

function/structure name	description
AddObject(pyObject)	add a object with objectDefinition from Python object
	class; returns (global) object number of newly added ob-
	ject
	EXAMPLE:
	<pre>item = MassPoint(name='heavy object', nodeNumber=0,</pre>
	physicsMass=100)
	mbs.AddObject(item)
	objectDict = {'objectType': 'MassPoint',
	'physicsMass': 10,
	'nodeNumber': 0,
	'name': 'example object'}
	mbs.AddObject(objectDict)
GetObjectNumber(objectName)	get object's number by name (string)
	EXAMPLE:
	n = mbs.GetObjectNumber('heavy object')
GetObject(objectNumber)	get object's dictionary by index
	EXAMPLE:
	objectDict = mbs.GetObject(0)
ModifyObject(objectNumber, objectDict)	modify object's dictionary by index
	EXAMPLE:
	mbs.ModifyObject(objectNumber, objectDict)
GetObjectDefaults(typeName)	get object's default values for a certain objectType as (dic-
	tionary)
	EXAMPLE:
	objectType = 'MassPoint'
	objectDict = mbs.GetObjectDefaults(objectType)
GetObjectOutput(objectNumber, variableType)	get object's current output variable from objectNum-
	ber and OutputVariableType; can only be computed for
	exu.ConfigurationType.Current configuration!

GetObjectOutputBody(objectNumber, variableType, lo-	get body's output variable from objectNumber and
calPosition, configuration = ConfigurationType.Current)	OutputVariableType
	EXAMPLE:
	u = mbs.GetObjectOutputBody(objectNumber = 1,
	variableType = exu.OutputVariableType.Position,
	localPosition=[1,0,0], configuration =
	exu.ConfigurationType.Initial)
GetObjectOutputSuperElement(objectNumber, variable-	get output variable from mesh node number of object
Type, meshNodeNumber, configuration = Configura-	with type SuperElement (GenericODE2, FFRF, FFRFre-
tionType.Current)	duced - CMS) with specific OutputVariableType; the
	meshNodeNumber is the object's local node number, not
	the global node number!
	EXAMPLE:
	u = mbs.GetObjectOutputSuperElement(objectNumber =
	1, variableType = exu.OutputVariableType.Position,
	meshNodeNumber = 12, configuration =
	exu.ConfigurationType.Initial)
GetObjectParameter(objectNumber, parameterName)	get objects's parameter from objectNumber and parame-
	terName; parameter names can be found for the specific
	items in the reference manual
SetObjectParameter(objectNumber, parameterName,	set parameter 'parameterName' of object with objectNum-
value)	ber to value; parameter names can be found for the specific
	items in the reference manual

## 4.3.3 MainSystem: Marker

This section provides functions for adding, reading and modifying markers. Markers define how to measure primal kinematical quantities on objects or nodes (e.g., position, orientation or coordinates themselves), and how to act on the quantities which are dual to the kinematical quantities (e.g., force, torque and generalized forces). Markers provide unique interfaces for loads, sensors and constraints in order to address these quantities independently of the structure of the object or node (e.g., rigid or flexible body).

function/structure name	description
AddMarker(pyObject)	add a marker with markerDefinition from Python marker
	class; returns (global) marker number of newly added
	marker
	EXAMPLE:
	item = MarkerNodePosition(name='my
	marker',nodeNumber=1)
	mbs.AddMarker(item)
	markerDict = {'markerType': 'NodePosition',
	'nodeNumber': 0,
	'name': 'position0'}
	mbs.AddMarker(markerDict)

GetMarkerNumber(markerName)	get marker's number by name (string)
	EXAMPLE:
	n = mbs.GetMarkerNumber('my marker')
GetMarker(markerNumber)	get marker's dictionary by index
	EXAMPLE:
	markerDict = mbs.GetMarker(0)
ModifyMarker(markerNumber, markerDict)	modify marker's dictionary by index
	EXAMPLE:
	mbs.ModifyMarker(markerNumber, markerDict)
GetMarkerDefaults(typeName)	get marker's default values for a certain markerType as
	(dictionary)
	EXAMPLE:
	markerType = 'NodePosition'
	markerDict = mbs.GetMarkerDefaults(markerType)
GetMarkerParameter(markerNumber, parameterName)	get markers's parameter from markerNumber and param-
	eterName; parameter names can be found for the specific
	items in the reference manual
SetMarkerParameter(markerNumber, parameterName,	set parameter 'parameterName' of marker with marker-
value)	Number to value; parameter names can be found for the
	specific items in the reference manual

## 4.3.4 MainSystem: Load

This section provides functions for adding, reading and modifying operating loads. Loads are used to act on the quantities which are dual to the primal kinematic quantities, such as displacement and rotation. Loads represent, e.g., forces, torques or generalized forces.

function/structure name	description
AddLoad(pyObject)	add a load with loadDefinition from Python load class;
	returns (global) load number of newly added load
	EXAMPLE:
	item = mbs. AddLoad(LoadForceVector(loadVector = [1,0,0],
	markerNumber=0, name='heavy load'))
	mbs.AddLoad(item)
	loadDict = {'loadType': 'ForceVector',
	'markerNumber': 0,
	'loadVector': [1.0, 0.0, 0.0],
	'name': 'heavy load'}
	mbs.AddLoad(loadDict)
GetLoadNumber(loadName)	get load's number by name (string)
	EXAMPLE:
	n = mbs.GetLoadNumber('heavy load')
GetLoad(loadNumber)	get load's dictionary by index
	EXAMPLE:
	loadDict = mbs.GetLoad(0)

ModifyLoad(loadNumber, loadDict)	modify load's dictionary by index
	EXAMPLE:
	mbs.ModifyLoad(loadNumber, loadDict)
GetLoadDefaults(typeName)	get load's default values for a certain loadType as (dictio-
	nary)
	EXAMPLE:
	loadType = 'ForceVector'
	loadDict = mbs.GetLoadDefaults(loadType)
GetLoadValues(loadNumber)	Get current load values, specifically if user-defined loads
	are used; can be scalar or vector-valued return value
GetLoadParameter(loadNumber, parameterName)	get loads's parameter from loadNumber and parameter-
	Name; parameter names can be found for the specific
	items in the reference manual
SetLoadParameter(loadNumber, parameterName, value)	set parameter 'parameterName' of load with loadNumber
	to value; parameter names can be found for the specific
	items in the reference manual

## 4.3.5 MainSystem: Sensor

This section provides functions for adding, reading and modifying operating sensors. Sensors are used to measure information in nodes, objects, markers, and loads for output in a file.

function/structure name	description
AddSensor(pyObject)	add a sensor with sensor definition from Python sensor
	class; returns (global) sensor number of newly added
	sensor
	EXAMPLE:
	item = mbs.AddSensor(SensorNode(sensorType=
	exu.SensorType.Node, nodeNumber=0, name='test
	sensor'))
	mbs.AddSensor(item)
	<pre>sensorDict = {'sensorType': 'Node',</pre>
	'nodeNumber': 0,
	'fileName': 'sensor.txt',
	'name': 'test sensor'}
	mbs.AddSensor(sensorDict)
GetSensorNumber(sensorName)	get sensor's number by name (string)
	EXAMPLE:
	<pre>n = mbs.GetSensorNumber('test sensor')</pre>
GetSensor(sensorNumber)	get sensor's dictionary by index
	EXAMPLE:
	sensorDict = mbs.GetSensor(0)
ModifySensor(sensorNumber, sensorDict)	modify sensor's dictionary by index
	EXAMPLE:
	mbs.ModifySensor(sensorNumber, sensorDict)

GetSensorDefaults(typeName)	get sensor's default values for a certain sensorType as
	(dictionary)
	EXAMPLE:
	sensorType = 'Node'
	sensorDict = mbs.GetSensorDefaults(sensorType)
GetSensorValues(sensorNumber, configuration = Config-	get sensors's values for configuration; can be a scalar or
urationType.Current)	vector-valued return value!
GetSensorParameter(sensorNumber, parameterName)	get sensors's parameter from sensorNumber and param-
	eterName; parameter names can be found for the specific
	items in the reference manual
SetSensorParameter(sensorNumber, parameterName,	set parameter 'parameterName' of sensor with sensor-
value)	Number to value; parameter names can be found for the
	specific items in the reference manual

## 4.4 SystemData

This is the data structure of a system which contains Objects (bodies/constraints/...), Nodes, Markers and Loads. The SystemData structure allows advanced access to this data, which HAS TO BE USED WITH CARE, as unexpected results and system crash might happen.

Usage:

#obtain current ODE2 system vector (e.g. after static simulation finished):

u = mbs.systemData.GetODE2Coordinates()

#set initial ODE2 vector for next simulation:

mbs.systemData.SetODE2Coordinates(coordinates=u,configurationType=exu.ConfigurationType.Initial)

function/structure name	description
NumberOfLoads()	return number of loads in system
	EXAMPLE:
	print(mbs.systemData.NumberOfLoads())
NumberOfMarkers()	return number of markers in system
	EXAMPLE:
	print(mbs.systemData.NumberOfMarkers())
NumberOfNodes()	return number of nodes in system
	EXAMPLE:
	print(mbs.systemData.NumberOfNodes())
NumberOfObjects()	return number of objects in system
	EXAMPLE:
	print(mbs.systemData.NumberOfObjects())
GetTime(configurationType =	get configuration dependent time.
exu.ConfigurationType.Current)	EXAMPLE:
	mbs.systemData.GetTime(exu.ConfigurationType.Initial)
SetTime(newTime, configurationType =	set configuration dependent time; use this access with
exu.ConfigurationType.Current)	care, e.g. in user-defined solvers.
	EXAMPLE:
	mbs.systemData.SetTime(10.,
	exu.ConfigurationType.Initial)

GetCurrentTime()	DEPRICATED; get current (simulation) time; time is up-
	dated in time integration solvers and in static solver;
	use this function e.g. during simulation to define time-
	dependent loads
	EXAMPLE:
	mbs.systemData.GetCurrentTime()
SetVisualizationTime()	DEPRICATED; set time for render window (visualization)
	EXAMPLE:
	mbs.systemData.SetVisualizationTime(1.3)
Info()	print detailed system information for every item; for short
	information use print(mbs)
	EXAMPLE:
	mbs.systemData.Info()

## 4.4.1 SystemData: Access coordinates

This section provides access functions to global coordinate vectors. Assigning invalid values or using wrong vector size might lead to system crash and unexpected results.

function/structure name		description
GetODE2Coordinates(configuration	=	get ODE2 system coordinates (displacements) for given
exu.ConfigurationType.Current)		configuration (default: exu.Configuration.Current)
		EXAMPLE:
		uCurrent = mbs.systemData.GetODE2Coordinates()
SetODE2Coordinates(coordinates, configurat	tion =	set ODE2 system coordinates (displacements) for given
exu.ConfigurationType.Current)		configuration (default: exu.Configuration.Current); in-
		valid vector size may lead to system crash!
		EXAMPLE:
		mbs.systemData.SetODE2Coordinates(uCurrent)
GetODE2Coordinates_t(configuration	=	get ODE2 system coordinates (velocities) for given config-
exu.ConfigurationType.Current)		uration (default: exu.Configuration.Current)
		EXAMPLE:
		$vCurrent = mbs.systemData.GetODE2Coordinates\_t()$
SetODE2Coordinates_t(coordinates, configura	ition =	set ODE2 system coordinates (velocities) for given con-
exu.ConfigurationType.Current)		figuration (default: exu.Configuration.Current); invalid
		vector size may lead to system crash!
		EXAMPLE:
		$mbs.systemData.SetODE2Coordinates\_t(vCurrent)$
GetODE1Coordinates(configuration	=	get ODE1 system coordinates (displacements) for given
exu.ConfigurationType.Current)		configuration (default: exu.Configuration.Current)
		EXAMPLE:
		qCurrent = mbs.systemData.GetODE1Coordinates()
SetODE1Coordinates(coordinates, configurat	tion =	set ODE1 system coordinates (displacements) for given
exu.ConfigurationType.Current)		configuration (default: exu.Configuration.Current); in-
		valid vector size may lead to system crash!
		EXAMPLE:
		mbs.systemData.SetODE1Coordinates(qCurrent)

GetAECoordinates(configuration		=	get algebraic equations (AE) system coordinates for given
exu.ConfigurationType.Current)			configuration (default: exu.Configuration.Current)
			EXAMPLE:
			lambdaCurrent = mbs.systemData.GetAECoordinates()
SetAECoordinates(coordinates,	configuration	=	set algebraic equations (AE) system coordinates for given
exu.ConfigurationType.Current)			configuration (default: exu.Configuration.Current); in-
			valid vector size may lead to system crash!
			EXAMPLE:
			mbs. system Data. Set AE Coordinates (lambda Current)
GetDataCoordinates(configuration		=	get system data coordinates for given configuration (de-
exu.ConfigurationType.Current)			fault: exu.Configuration.Current)
			EXAMPLE:
			dataCurrent = mbs.systemData.GetDataCoordinates()
SetDataCoordinates(coordinates,	configuration	=	set system data coordinates for given configuration (de-
exu.ConfigurationType.Current)			fault: exu.Configuration.Current); invalid vector size may
			lead to system crash!
			EXAMPLE:
			mbs.systemData.SetDataCoordinates(dataCurrent)
GetSystemState(configuration		=	get system state for given configuration (default:
exu.ConfigurationType.Current)			exu.Configuration.Current); state vectors do not include
			the non-state derivatives ODE1_t and ODE2_tt and the
			time; function is copying data - not highly efficient; format
			of pyList: [ODE2Coords, ODE2Coords_t, ODE1Coords,
			AEcoords, dataCoords]
			EXAMPLE:
			sysStateList = mbs.systemData.GetSystemState()
SetSystemState(systemStateList,	configuration	=	set system data coordinates for given configuration (de-
exu.ConfigurationType.Current)			fault: exu.Configuration.Current); invalid list of vectors
			/ vector size may lead to system crash; write access to
			state vectors (but not the non-state derivatives ODE1_t
			and ODE2_tt and the time); function is copying data
			- not highly efficient; format of pyList: [ODE2Coords,
			ODE2Coords_t, ODE1Coords, AEcoords, dataCoords]
			EXAMPLE:
			mbs.systemData.SetDataCoordinates(sysStateList, con-
			figurationType = exu.ConfigurationType.Initial)

## 4.4.2 SystemData: Get object local-to-global (LTG) coordinate mappings

This section provides access functions the LTG-lists for every object (body, constraint, ...) in the system.

function/structure name	description
GetObjectLTGODE2(objectNumber)	get local-to-global coordinate mapping (list of global coor-
	dinate indices) for ODE2 coordinates; only available after
	Assemble()
	EXAMPLE:
	ltgObject4 = mbs.systemData.GetObjectLTGODE2(4)

GetObjectLTGODE1(objectNumber)	get local-to-global coordinate mapping (list of global coor-
	dinate indices) for ODE1 coordinates; only available after
	Assemble()
	EXAMPLE:
	ltgObject4 = mbs.systemData.GetObjectLTGODE1(4)
GetObjectLTGAE(objectNumber)	get local-to-global coordinate mapping (list of global coor-
	dinate indices) for algebraic equations (AE) coordinates;
	only available after Assemble()
	EXAMPLE:
	ltgObject4 = mbs.systemData.GetObjectLTGODE2(4)
GetObjectLTGData(objectNumber)	get local-to-global coordinate mapping (list of global co-
	ordinate indices) for data coordinates; only available after
	Assemble()
	EXAMPLE:
	ltgObject4 = mbs.systemData.GetObjectLTGData(4)

## 4.5 Type definitions

This section defines a couple of structures, which are used to select, e.g., a configuration type or a variable type. In the background, these types are integer numbers, but for safety, the types should be used as type variables. Conversion to integer is possible:

x = int(exu.OutputVariableType.Displacement)

and also conversion from integer:

varType = exu.OutputVariableType(8)

#### 4.5.1 OutputVariableType

This section shows the OutputVariableType structure, which is used for selecting output values, e.g. for GetObjectOutput(...) or for selecting variables for contour plot.

Available output variables and the interpreation of the output variable can be found at the object definitions. The Output VariableType does not provide information about the size of the output variable, which can be either scalar or a list (vector). For vector output quantities, the contour plot option offers an additional parameter for selection of the component of the OutputVariableType.

function/structure name	description
_None	no value; used, e.g., to select no output variable in contour
	plot
Distance	e.g., measure distance in spring damper connector
Position	measure 3D position, e.g., of node or body
Displacement	measure displacement; usually difference between current
	position and reference position
Velocity	measure (translational) velocity of node or object
Acceleration	measure (translational) acceleration of node or object
RotationMatrix	measure rotation matrix of rigid body node or object

AngularVelocity	measure angular velocity of node or object
AngularVelocityLocal	measure local (body-fixed) angular velocity of node or object
AngularAcceleration	measure angular acceleration of node or object
Rotation	measure, e.g., scalar rotation of 2D body, Euler angles of a 3D object or rotation within a joint
Coordinates	measure the coordinates of a node or object; coordinates usually just contain displacements, but not the position values
Coordinates_t	measure the time derivative of coordinates (= velocity coordinates) of a node or object
SlidingCoordinate	measure sliding coordinate in sliding joint
Director1	measure a director (e.g. of a rigid body frame), or a slope vector in local 1 or x-direction
Director2	measure a director (e.g. of a rigid body frame), or a slope vector in local 2 or y-direction
Director3	measure a director (e.g. of a rigid body frame), or a slope vector in local 3 or z-direction
Force	measure force, e.g., in joint or beam (resultant force)
Torque	measure torque, e.g., in joint or beam (resultant couple/moment)
Strain	measure strain, e.g., axial strain in beam
Stress	measure stress, e.g., axial stress in beam
Curvature	measure curvature; may be scalar or vectorial: twist and curvature
DisplacementLocal	measure local displacement, e.g. in local joint coordinates
VelocityLocal	measure local (translational) velocity, , e.g. in local joint coordinates
ForceLocal	measure local force, e.g., in joint or beam (resultant force)
TorqueLocal	measure local torque, e.g., in joint or beam (resultant couple/moment)
ConstraintEquation	evaluates constraint equation (=current deviation or drift of constraint equation)
EndOfEnumList	this marks the end of the list, usually not important to the user

## 4.5.2 ConfigurationType

This section shows the ConfigurationType structure, which is used for selecting a configuration for reading or writing information to the module. Specifically, the ConfigurationType.Current configuration is usually used at the end of a solution process, to obtain result values, or the ConfigurationType.Initial is used to set initial values for a solution process.

function/structure name	description	
_None	no configuration; usually not valid, but may be used, e.g	
	if no configurationType is required	

Initial	initial configuration prior to static or dynamic solver,		
	is computed during mbs.Assemble() or AssembleInitial-		
	izeSystemCoordinates()		
Current	current configuration during and at the end of the com-		
	putation of a step (static or dynamic)		
Reference	configuration used to define deformable bodies (reference		
	configuration for finite elements) or joints (configuration		
	for which some joints are defined)		
StartOfStep	during computation, this refers to the solution at the start		
	of the step = end of last step, to which the solver falls back		
	if convergence fails		
Visualization	this is a state completely de-coupled from computation,		
	used for visualization		
EndOfEnumList	this marks the end of the list, usually not important to the		
	user		

## 4.5.3 LinearSolverType

This section shows the LinearSolverType structure, which is used for selecting output values, e.g. for GetObjectOutput(...) or for selecting variables for contour plot.

function/structure name	description	
_None	no value; used, e.g., if no solver is selected	
EXUdense	use dense matrices and according solvers for densly popu-	
	lated matrices (usually the CPU time grows cubically with	
	the number of unknowns)	
EigenSparse	use sparse matrices and according solvers; additional	
	overhead for very small systems; specifically, memory al-	
	location is performed during a factorization process	

# **Chapter 5**

# Objects, nodes, markers, loads and sensors reference manual

This chapter includes the reference manual for all objects (bodies/constraints), nodes, markers, loads and sensors.

## 5.1 Notation for item equations

The following subscripts are used to define configurations of a quantity, e.g., x:

- $x_{config} \dots x$  in any configuration
- $\mathbf{x}_{\text{ref}} \dots \mathbf{x}$  in reference configuration, e.g., reference coordinates:  $\mathbf{c}_{\text{ref}}$
- $\mathbf{x}_{\text{ini}} \dots \mathbf{x}$  in initial configuration, e.g., initial displacements:  $\mathbf{u}_{\text{ini}}$
- $x_{cur} \dots x$  in current configuration
- $x_{vis} \dots x$  in visualization configuration
- $x_{\text{start of step}} \dots x$  in start of step configuration

As written in the introduction, the coordinates can have the types:

- ODE2 ... second order differential equations coordinates
- ODE1 ... first order differential equations coordinates; CURRENTLY NOT AVAILABLE
- AE ... algebraic equations coordinates
- Data ... data coordinates (history variables)

Finally, time is defined as 'time' or *t*.

The following table contains the common notation:

python name (or description)	symbol	description
displacement coordinates	$\mathbf{q} = [q_0, \ldots, q_n]^{\mathrm{T}}$	vector of <i>n</i> displacement based coordinates
		in any configuration
rotation coordinates	$\boldsymbol{\psi} = [\psi_0, \ldots, \psi_{\eta}]^{\mathrm{T}}$	vector of $\eta$ rotation based coordinates
		in any configuration; this coordinates are
		added to reference rotation parameters to
		provide the current rotation parameters
algebraic coordinates	$\mathbf{z} = [z_0, \ldots, z_m]^{\mathrm{T}}$	vector of <i>m</i> algebraic coordinates if not La-
		grange multipliers in any configuration

Lagrange multipliers	$\lambda = [\lambda_0, \ldots, \lambda_m]^{\mathrm{T}}$	vector of <i>m</i> Lagrange multipliers (=alge-
		braic coordinates) in any configuration
data coordinates	$\mathbf{x} = [x_0, \dots, x_l]^{\mathrm{T}}$	vector of <i>l</i> data coordinates in any configu-
		ration
python name: OutputVariable	symbol	description
Coordinate	$\mathbf{c} = [c_0, \ldots, c_n]^{\mathrm{T}}$	coordinate vector with <i>n</i> generalized coor-
		dinates $c_i$ in any configuration
Coordinate_t	$\dot{\mathbf{c}} = [c_0, \ldots, c_n]^{\mathrm{T}}$	time derivative of coordinate vector
Displacement	$\dot{\mathbf{c}} = [c_0, \dots, c_n]^{\mathrm{T}}$ ${}^{0}\mathbf{u} = [u_0, u_1, u_2]^{\mathrm{T}}$	global displacement vector with 3 displace-
•		ment coordinates $u_i$ in any configuration; in
		1D or 2D objects, some of there coordinates
		may be zero
Rotation	$\boldsymbol{\theta} = [\theta_0, \ldots, \theta_n]^{\mathrm{T}}$	vector of rotation parameters (e.g., Euler
		parameters, Tait Bryan angles,) with <i>n</i>
		coordinates $\theta_i$ in any configuration
	$\begin{bmatrix} A_{00} & A_{01} & A_{02} \end{bmatrix}$	, ,
RotationMatrix	$  {}^{0b}\mathbf{A} =   A_{10}  A_{11}  A_{12}  $	a 3D rotation matrix, which transforms local
	${}^{0b}\mathbf{A} = \begin{bmatrix} A_{00} & A_{01} & A_{02} \\ A_{10} & A_{11} & A_{12} \\ A_{20} & A_{21} & A_{22} \end{bmatrix}$	(e.g., body <i>b</i> ) to global coordinates (0): ${}^{0}\mathbf{x} =$
		<sup>0b</sup> <b>A</b> <sup>b</sup> <b>x</b>
Position	${}^{0}\mathbf{p} = [p_0, p_1, p_2]^{\mathrm{T}}$	global position vector with 3 position coor-
		dinates $p_i$ in any configuration
Velocity	$^{0}\mathbf{v} = ^{0}\dot{\mathbf{u}} = [v_0, v_1, v_2]^{\mathrm{T}}$	global velocity vector with 3 displacement
		coordinates $v_i$ in any configuration
AngularVelocity	$^{0}\boldsymbol{\omega} = [\omega_0, \ldots, \omega_2]^{\mathrm{T}}$	global angular velocity vector with 3 coor-
		dinates $\omega_i$ in any configuration
VelocityLocal	${}^b\mathbf{v} = [v_0, v_1, v_2]^{\mathrm{T}}$	local (body-fixed) velocity vector with 3 dis-
		placement coordinates $v_i$ in any configura-
		tion
AngularVelocityLocal	${}^{b}\boldsymbol{\omega} = [\omega_0, \ldots, \omega_2]^{\mathrm{T}}$	local (body-fixed) angular velocity vector
		with 3 coordinates $\omega_i$ in any configuration
Force	$^{0}\mathbf{f} = [f_0, \ldots, f_2]^{\mathrm{T}}$	vector of 3 force components in global co-
		ordinates
Torque	$^{0}\tau = [\tau_0, \ldots, \tau_2]^{\mathrm{T}}$	vector of 3 torque components in global co-
		ordinates
python name: input to nodes,	symbol	description
markers, etc.		_
referenceCoordinates	$\mathbf{c}_{\text{ref}} = [c_0, \dots, c_n]_{\text{ref}}^{\text{T}} =$	n coordinates of reference configuration
	$[c_{\text{Ref},0},\ldots,c_{\text{Ref},n}]_{\text{ref}}^{\text{T}}$	(can usually be set at initialization of nodes)
initialCoordinates	c <sub>ini</sub>	initial coordinates with generalized or
		mixed displacement/rotation quantities
		(can usually be set at initialization of nodes)
localPosition	${}^b\mathbf{p} = [{}^bp_0, {}^bp_1, {}^bp_2]^{\mathrm{T}}$	local (body-fixed) position vector with 3 po-
		sition coordinates $p_i$ in any configuration;
		used for local position of markers, sensors,
		etc.
		·

#### 5.1.1 Reference and current coordinates

An important fact on the coordinates is upon the splitting of quantities (e.g. position, rotation parameters, etc.) into reference and current (initial/visualization/...) coordinates. For the current position of a point node we have, e.g.,

$$\mathbf{p}_{\rm cur} = \mathbf{p}_{\rm ref} + \mathbf{u}_{\rm cur} \tag{5.1}$$

The same holds, e.g., for rotation parameters,

$$\theta_{\rm cur} = \theta_{\rm ref} + \psi_{\rm cur} \tag{5.2}$$

#### 5.1.2 Coordinate Systems

The left indices provide information about the coordinate system, e.g.,

$$^{0}\mathbf{u}$$
 (5.3)

is the displacement vector in the global (inertial) coordinate systme 0, while

$$^{m1}\mathbf{u}$$
 (5.4)

represents the displacement vector in marker 1 (m1) coordinates. Typical coordinate systems:

- ullet  $^0\mathbf{u}$  ... global coordinates
- <sup>b</sup>**u** ... body-fixed, local coordinates
- $^{m0}$ **u** ... local coordinates of (the body or node of) marker m0
- $^{m1}$ **u** ... local coordinates of (the body or node of) marker m1

To transform the local coordinates  ${}^{m0}\mathbf{u}$  of marker 0 into global coordinates  ${}^{0}\mathbf{x}$ , we use

$${}^{0}\mathbf{u} = {}^{0,m0}\mathbf{A} \, {}^{m0}\mathbf{u} \tag{5.5}$$

in which  $^{0,m0}$ **A** is the transformation matrix of (the body or node of) the underlying marker 0.

#### 5.2 Nodes

#### 5.2.1 NodePoint

A 3D point node for point masses or solid finite elements which has 3 displacement degrees of freedom for second order differential equations (ODE2).

#### Additional information for NodePoint:

- The Node has the following types = Position
- **Short name** for Python = **Point**

#### The item **NodePoint** with type = 'Point' has the following parameters:

Name	type	size	default value	description
name	String		"	node's unique name
referenceCoordinates	Vector3D	3	[0.,0.,0.]	reference coordinates of node, e.g. ref. co- ordinates for finite elements; global posi-
				tion of node without displacement
initialCoordinates	Vector3D	3	[0.,0.,0.]	initial displacement coordinate
initialVelocities	Vector3D	3	[0.,0.,0.]	initial velocity coordinate
visualization	VNodePoint			parameters for visualization of item

#### The item VNodePoint has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size (diameter, dimensions of un-
				derlying cube, etc.) for item; size == -1.f
				means that default size is used
color	Float4	4	[-1.,-1.,-1.]	Default RGBA color for nodes; 4th value
				is alpha-transparency; R=-1.f means, that
				default color is used

#### **Detailed information on NodePoint:**

input parameter	symbol	description see tables above
referenceCoordinates	$\mathbf{q}_{\text{ref}} = [q_0, q_1, q_2]_{\text{ref}}^{\text{T}} = \mathbf{p}_{\text{ref}} =$	
	$[r_0, r_1, r_2]^{\mathrm{T}}$	
initialCoordinates	$\mathbf{q}_{\text{ini}} = [q_0, q_1, q_2]_{\text{ini}}^{\text{T}} = \mathbf{u}_{\text{ini}} =$	
	$[u_0, u_1, u_2]_{\text{ini}}^{\text{T}}$	
initialVelocities	$\dot{\mathbf{q}}_{\text{ini}} = \mathbf{v}_{\text{ini}} = [\dot{q}_0,  \dot{q}_1,  \dot{q}_2]_{\text{ini}}^{\text{T}}$	

#### The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Position	$\mathbf{p}_{\text{config}} = [p_0, p_1, p_2]_{\text{config}}^{\text{T}} = \mathbf{u}_{\text{config}} +$	global 3D position vector of node; $\mathbf{u}_{ref} = 0$
	$\mathbf{p}_{\mathrm{ref}}$	
Displacement	$\mathbf{u}_{\text{config}} = [q_0, q_1, q_2]_{\text{config}}^{\text{T}}$	global 3D displacement vector of node

Velocity	$\mathbf{v}_{\text{config}} = [\dot{q}_0,  \dot{q}_1,  \dot{q}_2]_{\text{config}}^{\text{T}}$	global 3D velocity vector of node
Coordinates	$\mathbf{c}_{\text{config}} = \mathbf{u}_{\text{config}} = [q_0, q_1, q_2]_{\text{config}}^{\text{T}}$	coordinate vector of node
Coordinates_t	$\dot{\mathbf{c}}_{\text{config}} = \mathbf{v}_{\text{config}} = [\dot{q}_0,  \dot{q}_1,  \dot{q}_2]_{\text{config}}^{\text{T}}$	velocity coordinates vector of node

**Description of Item**: The node provides  $n_c = 3$  displacement coordinates. Equations of motion need to be provided by an according object (e.g., MassPoint, finite elements, ...). Usually, the nodal coordinates are provided in the global frame. However, the coordinate system is defined by the object (e.g. MassPoint uses global coordinates, but floating frame of reference objects use local frames). Note that for this very simple node, coordinates are identical to the nodal displacements, same for time derivatives. This is not the case, e.g. for nodes with orientation.

Example for NodePoint: see ObjectMassPoint

#### 5.2.2 NodePoint2D

A 2D point node for point masses or solid finite elements which has 2 displacement degrees of freedom for second order differential equations.

#### Additional information for NodePoint2D:

- The Node has the following types = Position2D, Position
- **Short name** for Python = **Point2D**

The item **NodePoint2D** with type = 'Point2D' has the following parameters:

Name	type	size	default value	description
name	String		"	node's unique name
referenceCoordinates	Vector2D	2	[0.,0.]	reference coordinates of node ==> e.g. ref.
				coordinates for finite elements; global posi-
				tion of node without displacement
initialCoordinates	Vector2D	2	[0.,0.]	initial displacement coordinate
initialVelocities	Vector2D	2	[0.,0.]	initial velocity coordinate
visualization	VNodePoint2D			parameters for visualization of item

The item VNodePoint2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size (diameter, dimensions of un-
				derlying cube, etc.) for item; size == -1.f
				means that default size is used
color	Float4	4	[-1.,-1.,-1.]	Default RGBA color for nodes; 4th value
				is alpha-transparency; R=-1.f means, that
				default color is used

#### Detailed information on NodePoint2D:

input parameter	symbol	description see tables above
referenceCoordinates	$\mathbf{q}_{\text{ref}} = [q_0, q_1]_{\text{ref}}^{\text{T}} = \mathbf{p}_{\text{ref}} = [r_0, r_1]^{\text{T}}$	
initialCoordinates	$\mathbf{q}_{\text{ini}} = [q_0, q_1]_{\text{ini}}^{\text{T}} = [u_0, u_1]_{\text{ini}}^{\text{T}}$	
initialVelocities	$\dot{\mathbf{q}}_{\mathrm{ini}} = \mathbf{v}_{\mathrm{ini}} = [\dot{q}_0,  \dot{q}_1]_{\mathrm{ini}}^{\mathrm{T}}$	

#### The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Position	$\mathbf{p}_{\text{config}} = [p_0, p_1, 0]_{\text{config}}^{\text{T}} = \mathbf{u}_{\text{config}} + \mathbf{p}_{\text{ref}}$	global 3D position vector of node; $\mathbf{u}_{ref} = 0$
Displacement	$\mathbf{u}_{\text{config}} = [q_0, q_1, 0]_{\text{config}}^{\text{T}}$	global 3D displacement vector of node
Velocity	$\mathbf{v}_{\text{config}} = [\dot{q}_0,  \dot{q}_1,  0]_{\text{config}}^{\text{T}}$	global 3D velocity vector of node
Coordinates	$\mathbf{c}_{\text{config}} = [q_0, q_1]_{\text{config}}^{\text{T}}$	coordinate vector of node
Coordinates_t	$\dot{\mathbf{c}}_{\text{config}} = [\dot{q}_0,  \dot{q}_1]_{\text{config}}^{\text{T}}$	velocity coordinates vector of node

#### **Description of Item:**

The node provides  $n_c = 2$  displacement coordinates. Equations of motion need to be provided by an according object (e.g., MassPoint2D). Coordinates are identical to the nodal displacements, except for the third coordinate  $u_2$ , which is zero, because  $q_2$  does not exist.

Note that for this very simple node, coordinates are identical to the nodal displacements, same for time derivatives. This is not the case, e.g. for nodes with orientation.

**Example** for NodePoint: see ObjectMassPoint2D

#### 5.2.3 NodeRigidBodyEP

A 3D rigid body node based on Euler parameters for rigid bodies or beams; the node has 3 displacement coordinates (displacements of center of mass - COM: ux,uy,uz) and four rotation coordinates (Euler parameters = quaternions).

#### Additional information for NodeRigidBodyEP:

- The Node has the following types = Position, Orientation, RigidBody, RotationEulerParameters
- **Short name** for Python = **RigidEP**

The item **NodeRigidBodyEP** with type = 'RigidBodyEP' has the following parameters:

Name	type	size	default value	description
name	String		"	node's unique name
referenceCoordinates	Vector7D	7	[0.,0.,0., 0.,0.,0.,0.]	reference coordinates (3 position coordi-
				nates and 4 Euler parameters) of node ==>
				e.g. ref. coordinates for finite elements or
				reference position of rigid body (e.g. for
				definition of joints)
initialCoordinates	Vector7D	7	[0.,0.,0., 0.,0.,0.,0.]	initial displacement coordinates and 4 Euler
				parameters relative to reference coordinates
initialVelocities	Vector7D	7	[0.,0.,0., 0.,0.,0.,0.]	initial velocity coordinates: time deriva-
				tives of initial displacements and Euler pa-
				rameters
visualization	VNodeRigidBodyE	P		parameters for visualization of item

#### The item VNodeRigidBodyEP has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size (diameter, dimensions of un-
				derlying cube, etc.) for item; size == -1.f
				means that default size is used
color	Float4	4	[-1.,-1.,-1.]	Default RGBA color for nodes; 4th value
				is alpha-transparency; R=-1.f means, that
				default color is used

#### Detailed information on NodeRigidBodyEP:

input parameter	symbol	description see tables above
referenceCoordinates	$\mathbf{q}_{\text{ref}} = [q_0, q_1, q_2, \psi_0, \psi_1, \psi_2, \psi_3]_{\text{ref}}^{\text{T}} =$	
	$[oldsymbol{p}_{ ext{ref}}^{ ext{T}},oldsymbol{\psi}_{ ext{ref}}^{ ext{T}}]^{ ext{T}}$	
initialCoordinates	$\mathbf{q}_{\text{ini}} = [q_0, q_1, q_2, \psi_0, \psi_1, \psi_2, \psi_3]_{\text{ini}}^{\text{T}} =$	
	$[\mathbf{u}_{ ext{ini}}^{ ext{T}}, oldsymbol{\psi}_{ ext{ini}}^{ ext{T}}]^{ ext{T}}$	
initialVelocities	$\dot{\mathbf{q}}_{\text{ini}} = [\dot{q}_0, \dot{q}_1, \dot{q}_2, \dot{\psi}_0, \dot{\psi}_1, \dot{\psi}_2, \dot{\psi}_3]_{\text{ini}}^{\text{T}} =$	
	$[\dot{f u}_{ m ini}^{ m T},\dot{m \psi}_{ m ini}^{ m T}]^{ m T}$	

The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Position	${}^{0}\mathbf{p}_{\text{config}} = {}^{0}[p_0, p_1, p_2]_{\text{config}}^{\mathrm{T}} =$	global 3D position vector of node; $\mathbf{u}_{ref} = 0$
	$^{0}$ <b>u</b> config + $^{0}$ <b>p</b> ref	
Displacement	$^{0}\mathbf{u}_{\text{config}} = [q_0, q_1, q_2]_{\text{config}}^{\text{T}}$	global 3D displacement vector of node
Velocity	$^{0}\mathbf{v}_{\text{config}} = [\dot{q}_0,  \dot{q}_1,  \dot{q}_2]_{\text{config}}^{\text{T}}$	global 3D velocity vector of node
Coordinates	c <sub>config</sub> =	coordinate vector of node, having 3 dis-
	$[q_0, q_1, q_2, \psi_0, \psi_1, \psi_2, \psi_3]_{\text{config}}^{\text{T}}$	placement coordinates and 4 Euler param-
	· ·	eters
Coordinates_t	$\dot{\mathbf{c}}_{\mathrm{config}}$ =	velocity coordinates vector of node
	$[\dot{q}_0, \dot{q}_1, \dot{q}_2, \dot{\psi}_0, \dot{\psi}_1, \dot{\psi}_2, \dot{\psi}_3]_{\text{config}}^{\text{T}}$	
RotationMatrix	$[A_{00}, A_{01}, A_{02}, A_{10}, \dots, A_{21}, A_{22}]_{\text{config}}^{\text{T}}$	vector with 9 components of the rotation
		matrix $^{0b}$ <b>A</b> config in row-major format, in any
		configuration; the rotation matrix trans-
		forms local (b) to global (0) coordinates
Rotation	$[\varphi_0, \varphi_1, \varphi_2]_{\text{config}}^{\text{T}}$	vector with 3 components of the Euler an-
		gles in xyz-sequence ( $^{0b}$ <b>A</b> config =: <b>A</b> <sub>0</sub> ( $\varphi_0$ ) ·
		$\mathbf{A}_1(\varphi_1) \cdot \mathbf{A}_2(\varphi_2)$ ), recomputed from rotation
		matrix
AngularVelocity	$^{0}\boldsymbol{\omega}_{\text{config}} = ^{0}[\omega_{0},  \omega_{1},  \omega_{2}]_{\text{config}}^{T}$	global 3D angular velocity vector of node
AngularVelocityLocal	${}^{b}\boldsymbol{\omega}_{\text{config}} = {}^{b}[\omega_0,  \omega_1,  \omega_2]_{\text{config}}^{\text{T}}$	local (body-fixed) 3D angular velocity vec-
		tor of node

**Description of Item**: All coordinates  $\mathbf{c}_{\text{config}}$  lead to second order differential equations, but there is one additional constraint equation for the quaternions. The additional constraint equation, which needs to be provided by the object, reads

$$1 - \sum_{i=0}^{3} \theta_i^2 = 0. {(5.6)}$$

The rotation matrix  ${}^{0b}\mathbf{A}_{\text{config}}$  transforms local (body-fixed) 3D positions  ${}^{b}\mathbf{p} = {}^{b}[p_0, p_1, p_2]^{\mathrm{T}}$  to global 3D positions,

$${}^{0}\mathbf{p}_{\text{config}} = {}^{0b}\mathbf{A}_{\text{config}} {}^{b}\mathbf{p} \tag{5.7}$$

Note that the Euler parameters  $\theta_{cur}$  are computed as sum of current coordinates plus reference coordinates,

$$\theta_{\rm cur} = \psi_{\rm cur} + \psi_{\rm ref}. \tag{5.8}$$

The rotation matrix is defined as function of the rotation parameters  $\theta = [\theta_0, \theta_1, \theta_2, \theta_3]^T$ 

$${}^{0b}\mathbf{A} = \begin{bmatrix} -2\theta_3^2 - 2\theta_2^2 + 1 & -2\theta_3\theta_0 + 2\theta_2\theta_1 & 2*\theta_3\theta_1 + 2*\theta_2\theta_0 \\ 2\theta_3\theta_0 + 2\theta_2\theta_1 & -2\theta_3^2 - 2\theta_1^2 + 1 & 2\theta_3\theta_2 - 2\theta_1\theta_0 \\ -2\theta_2\theta_0 + 2\theta_3\theta_1 & 2\theta_3\theta_2 + 2\theta_1\theta_0 & -2\theta_2^2 - 2\theta_1^2 + 1 \end{bmatrix}$$
(5.9)

The derivatives of the angular velocity vectors w.r.t. the rotation velocity coordinates  $\dot{\theta} = [\dot{\theta}_0, \dot{\theta}_1, \dot{\theta}_2, \dot{\theta}_3]^T$  lead to the **G** matrices, as used in the equations of motion for rigid bodies,

$${}^{0}\omega = {}^{0}\mathbf{G}\,\dot{\boldsymbol{\theta}},\tag{5.10}$$

$${}^{b}\omega = {}^{b}\mathbf{G}\,\dot{\boldsymbol{\theta}}.\tag{5.11}$$

#### 5.2.4 NodeRigidBodyRxyz

A 3D rigid body node based on Euler / Tait-Bryan angles for rigid bodies or beams; all coordinates lead to second order differential equations; NOTE that this node has a singularity if the second rotation parameter reaches  $\psi_1 = (2k-1)\pi/2$ , with  $k \in \mathbb{N}$  or  $-k \in \mathbb{N}$ .

#### Additional information for NodeRigidBodyRxyz:

- The Node has the following types = Position, Orientation, RigidBody, RotationRxyz
- **Short name** for Python = **RigidRxyz**

The item **NodeRigidBodyRxyz** with type = 'RigidBodyRxyz' has the following parameters:

Name	type	size	default value	description
name	String		"	node's unique name
referenceCoordinates	Vector6D	6	[0.,0.,0., 0.,0.,0.]	reference coordinates (3 position and 3 xyz
				Euler angles) of node ==> e.g. ref. coor-
				dinates for finite elements or reference po-
				sition of rigid body (e.g. for definition of
				joints)
initialCoordinates	Vector6D	6	[0.,0.,0., 0.,0.,0.]	initial displacement coordinates: ux,uy,uz
				and 3 Euler angles (xyz) relative to reference
				coordinates
initialVelocities	Vector6D	6	[0.,0.,0., 0.,0.,0.]	initial velocity coordinate: time derivatives
				of ux,uy,uz and of 3 Euler angles (xyz)
visualization	VNodeRigidBodyR	xyz		parameters for visualization of item

The item VNodeRigidBodyRxyz has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size (diameter, dimensions of un-
				derlying cube, etc.) for item; size == -1.f
				means that default size is used
color	Float4	4	[-1.,-1.,-1.]	Default RGBA color for nodes; 4th value
				is alpha-transparency; R=-1.f means, that
				default color is used

#### Detailed information on NodeRigidBodyRxyz:

input parameter	symbol	description see tables above
referenceCoordinates	$\mathbf{q}_{\text{ref}} = [q_0, q_1, q_2, \psi_0, \psi_1, \psi_2]_{\text{ref}}^{\text{T}} =$	
	$[\mathbf{p}_{ ext{ref}}^{ ext{T}}, oldsymbol{\psi}_{ ext{ref}}^{ ext{T}}]^{ ext{T}}$	
initialCoordinates	$\mathbf{q}_{\text{ini}} = [q_0, q_1, q_2, \psi_0, \psi_1, \psi_2]_{\text{ini}}^{\text{T}} =$	
	$[\mathbf{u}_{ ext{ini}}^{ ext{T}}, oldsymbol{\psi}_{ ext{ini}}^{ ext{T}}]^{ ext{T}}$	
initialVelocities	$\dot{\mathbf{q}}_{\text{ini}} = [\dot{q}_0, \dot{q}_1, \dot{q}_2, \dot{\psi}_0, \dot{\psi}_1, \dot{\psi}_2]_{\text{ini}}^{\text{T}} =$	
	$\left[ \left[ \dot{\mathbf{u}}_{ ext{ini}}^{ ext{T}}, \dot{oldsymbol{\psi}}_{ ext{ini}}^{ ext{T}}  ight]^{ ext{T}}$	

The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Position	${}^{0}\mathbf{p}_{\text{config}} = {}^{0}[p_0, p_1, p_2]_{\text{config}}^{\mathrm{T}} =$	global 3D position vector of node; $\mathbf{u}_{ref} = 0$
	$^{0}$ u config + $^{0}$ p ref	
Displacement	$^{0}\mathbf{u}_{\text{config}} = [q_0, q_1, q_2]_{\text{config}}^{\text{T}}$	global 3D displacement vector of node
Velocity	$^{0}\mathbf{v}_{\text{config}} = [\dot{q}_{0},  \dot{q}_{1},  \dot{q}_{2}]_{\text{config}}^{\text{T}}$	global 3D velocity vector of node
Coordinates	$\mathbf{c}_{\text{config}} = [q_0, q_1, q_2, \psi_0, \psi_1, \psi_2]_{\text{config}}^{\text{T}}$	coordinate vector of node, having 3 dis-
		placement coordinates and 3 Euler angles
Coordinates_t	$\dot{\mathbf{c}}_{\text{config}} = [\dot{q}_0, \dot{q}_1, \dot{q}_2, \dot{\psi}_0, \dot{\psi}_1, \dot{\psi}_2]_{\text{config}}^{\text{T}}$	velocity coordinates vector of node
RotationMatrix	$[A_{00}, A_{01}, A_{02}, A_{10}, \dots, A_{21}, A_{22}]_{\text{config}}^{\text{T}}$	vector with 9 components of the rotation
		matrix $^{0b}$ <b>A</b> <sub>config</sub> in row-major format, in any
		configuration; the rotation matrix trans-
		forms local (b) to global (0) coordinates
Rotation	$[\varphi_0, \varphi_1, \varphi_2]_{\text{config}}^{\text{T}} = [\psi_0, \psi_1, \psi_2]_{\text{ref}}^{\text{T}} +$	vector with 3 components of the Euler / Tait-
	$[\psi_0, \psi_1, \psi_2]_{\text{config}}^{\text{T}}$	Bryan angles in xyz-sequence ( ${}^{0b}$ <b>A</b> config =:
		$\mathbf{A}_0(\varphi_0) \cdot \mathbf{A}_1(\varphi_1) \cdot \mathbf{A}_2(\varphi_2)$ ), recomputed from
		rotation matrix
AngularVelocity	$^{0}\boldsymbol{\omega}_{\text{config}} = ^{0}[\omega_{0},  \omega_{1},  \omega_{2}]_{\text{config}}^{T}$	global 3D angular velocity vector of node
AngularVelocityLocal	${}^{b}\boldsymbol{\omega}_{\text{config}} = {}^{b}[\omega_0,  \omega_1,  \omega_2]_{\text{config}}^{\text{T}}$	local (body-fixed) 3D angular velocity vec-
		tor of node

**Description of Item**: The node has 3 displacement coordinates  $[q_0, q_1, q_2]^T$  and 3 rotation coordinates  $[\psi_0, \psi_1, \psi_2]^T$  for consecutive rotations around the 0, 1 and 2-axis (x, y and z). All coordinates  $\mathbf{c}_{\text{config}}$  lead to second order differential equations. The rotation matrix  ${}^{0b}\mathbf{A}_{\text{config}}$  transforms local (body-fixed) 3D positions  ${}^b\mathbf{p} = {}^b[p_0, p_1, p_2]^T$  to global 3D positions,

$${}^{0}\mathbf{p}_{\text{config}} = {}^{0b}\mathbf{A}_{\text{config}} {}^{b}\mathbf{p}$$
 (5.12)

Note that the Euler angles  $\theta_{cur}$  are computed as sum of current coordinates plus reference coordinates,

$$\theta_{\rm cur} = \psi_{\rm cur} + \psi_{\rm ref}. \tag{5.13}$$

The rotation matrix is defined as function of the rotation parameters  $\theta = [\theta_0, \theta_1, \theta_2]^T$ 

$$^{0b}\mathbf{A} = \mathbf{A}_0(\theta_0)\mathbf{A}_1(\theta_1)\mathbf{A}_2(\theta_2) \tag{5.14}$$

The derivatives of the angular velocity vectors w.r.t. the rotation velocity coordinates  $\dot{\theta} = [\dot{\theta}_0, \dot{\theta}_1, \dot{\theta}_2, \dot{\theta}_3]^T$  lead to the **G** matrices, as used in the equations of motion for rigid bodies,

$${}^{0}\boldsymbol{\omega} = {}^{0}\mathbf{G}\,\dot{\boldsymbol{\theta}},\tag{5.15}$$

$${}^{b}\omega = {}^{b}\mathbf{G}\,\dot{\boldsymbol{\theta}}.\tag{5.16}$$

#### 5.2.5 NodeRigidBodyRotVecLG

A 3D rigid body node based on rotation vector and Lie group methods for rigid bodies or beams; the node has 3 displacement coordinates and three rotation coordinates.

#### Additional information for NodeRigidBodyRotVecLG:

- $\bullet \ \ The \ Node \ has \ the \ following \ types = \textbf{Position}, \textbf{Orientation}, \textbf{RigidBody}, \textbf{RotationRotationVector}, \textbf{RotationLieGroup}, \textbf{Soliton}, \textbf{Constitution Position Pos$
- Short name for Python = RigidRotVecLG

The item **NodeRigidBodyRotVecLG** with type = 'RigidBodyRotVecLG' has the following parameters:

Name	type	size	default value	description
name	String		"	node's unique name
referenceCoordinates	Vector6D	3	[0.,0.,0., 0.,0.,0.]	reference coordinates (position and rotation
				vector $\nu$ ) of node ==> e.g. ref. coordinates
				for finite elements or reference position of
				rigid body (e.g. for definition of joints)
initialCoordinates	Vector6D	3	[0.,0.,0., 0.,0.,0.]	initial displacement coordinates <b>u</b> and ro-
				tation vector $\nu$ relative to reference coordi-
				nates
initialVelocities	Vector6D	3	[0.,0.,0., 0.,0.,0.]	initial velocity coordinate: time derivatives
				of displacement and angular velocity vector
visualization	VNodeRigidBodyR	otVecI	.G	parameters for visualization of item

The item VNodeRigidBodyRotVecLG has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size (diameter, dimensions of un-
				derlying cube, etc.) for item; size == -1.f
				means that default size is used
color	Float4	4	[-1.,-1.,-1.]	Default RGBA color for nodes; 4th value
				is alpha-transparency; R=-1.f means, that
				default color is used

#### Detailed information on NodeRigidBodyRotVecLG:

input parameter	symbol	description see tables above
referenceCoordinates	$\mathbf{q}_{\text{ref}} = [q_0, q_1, q_2, \nu_0, \nu_1, \nu_2]_{\text{ref}}^{\text{T}} =$	
	$[\mathbf{p}_{ ext{ref}}^{ ext{T}}, \mathbf{ u}_{ ext{ref}}^{ ext{T}}]^{ ext{T}}$	
initialCoordinates	$\mathbf{q}_{\text{ini}} = [q_0, q_1, q_2, \nu_0, \nu_1, \nu_2]_{\text{ini}}^{\text{T}} =$	
	$[\mathbf{u}_{ ext{ini}}^{ ext{T}}, \mathbf{ u}_{ ext{ini}}^{ ext{T}}]^{ ext{T}}$	
initialVelocities	$\dot{\mathbf{q}}_{\text{ini}} = [\dot{q}_0, \dot{q}_1, \dot{q}_2, \dot{v}_0, \dot{v}_1, \dot{v}_2]_{\text{ini}}^{\text{T}} =$	
	$[\dot{f u}_{ m ini}^{ m T},\dot{m  u}_{ m ini}^{ m T}]^{ m T}$	

The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Position	${}^{0}\mathbf{p}_{\text{config}} = {}^{0}[p_0, p_1, p_2]_{\text{config}}^{\mathrm{T}} =$	global 3D position vector of node; $\mathbf{u}_{ref} = 0$
	$^{0}$ <b>u</b> config + $^{0}$ <b>p</b> ref	
Displacement	$^{0}\mathbf{u}_{\text{config}} = [q_0, q_1, q_2]_{\text{config}}^{\text{T}}$	global 3D displacement vector of node
Velocity	$^{0}\mathbf{v}_{\text{config}} = [\dot{q}_{0},  \dot{q}_{1},  \dot{q}_{2}]_{\text{config}}^{\text{T}}$	global 3D velocity vector of node
Coordinates	$\mathbf{c}_{\text{config}} = [q_0, q_1, q_2, \nu_0, \nu_1, \nu_2]_{\text{config}}^{\text{T}}$	coordinate vector of node, having 3 dis-
		placement coordinates and 3 Euler angles
Coordinates_t	$\dot{\mathbf{c}}_{\text{config}} = [\dot{q}_0,  \dot{q}_1,  \dot{q}_2,  \dot{v}_0,  \dot{v}_1,  \dot{v}_2]_{\text{config}}^{\text{T}}$	velocity coordinates vector of node
RotationMatrix	$[A_{00}, A_{01}, A_{02}, A_{10}, \dots, A_{21}, A_{22}]_{\text{config}}^{\text{T}}$	vector with 9 components of the rotation
		matrix $^{0b}$ <b>A</b> config in row-major format, in any
		configuration; the rotation matrix trans-
		forms local (b) to global (0) coordinates
Rotation	$[\varphi_0, \varphi_1, \varphi_2]_{\text{config}}^{\text{T}}$	vector with 3 components of the Euler / Tait-
		Bryan angles in xyz-sequence ( $^{0b}$ <b>A</b> config =:
		$\mathbf{A}_0(\varphi_0) \cdot \mathbf{A}_1(\varphi_1) \cdot \mathbf{A}_2(\varphi_2)$ ), recomputed from
		rotation matrix
AngularVelocity	$^{0}\boldsymbol{\omega}_{\text{config}} = ^{0}[\omega_{0},  \omega_{1},  \omega_{2}]_{\text{config}}^{T}$	global 3D angular velocity vector of node
AngularVelocityLocal	${}^{b}\boldsymbol{\omega}_{\text{config}} = {}^{b}[\omega_{0},  \omega_{1},  \omega_{2}]_{\text{config}}^{T}$	local (body-fixed) 3D angular velocity vec-
		tor of node

**Description of Item**: The node has 3 displacement coordinates  $[q_0, q_1, q_2]^T$  and three rotation coordinates, which is the rotation vector

$$\mathbf{v} = \varphi \mathbf{n} = \mathbf{v}_{\text{config}} + \mathbf{v}_{\text{ref}},\tag{5.17}$$

with the rotation angle  $\varphi$  and the rotation axis  $\mathbf{n}$ . All coordinates  $\mathbf{c}_{\text{config}}$  lead to second order differential equations, however the rotation vector cannot be used as a conventional parameterization. It must be computed within a nonlinear update, using appropriate Lie group methods.

The rotation matrix  ${}^{0b}\mathbf{A}_{\text{config}}$  transforms local (body-fixed) 3D positions  ${}^{b}\mathbf{p} = {}^{b}[p_0, p_1, p_2]^{\mathrm{T}}$  to global 3D positions,

$${}^{0}\mathbf{p}_{\text{config}} = {}^{0b}\mathbf{A}_{\text{config}} {}^{b}\mathbf{p} \tag{5.18}$$

Note that the rotation vector  $v_{cur}$  are computed as sum of current coordinates plus reference coordinates,

$$\theta_{\rm cur} = \nu_{\rm cur} + \nu_{\rm ref}$$
 with. (5.19)

The derivatives of the angular velocity vectors w.r.t. the rotation velocity coordinates  $\dot{\theta} = [\dot{\theta}_0, \dot{\theta}_1, \dot{\theta}_2, \dot{\theta}_3]^T$  lead to the **G** matrices, as used in the equations of motion for rigid bodies,

$${}^{0}\omega = {}^{0}\mathbf{G}\,\dot{\boldsymbol{\theta}},\tag{5.20}$$

$${}^{b}\omega = {}^{b}\mathbf{G}\,\dot{\boldsymbol{\theta}}.\tag{5.21}$$

#### 5.2.6 NodeRigidBody2D

A 2D rigid body node for rigid bodies or beams; the node has 2 displacement degrees of freedom and one rotation coordinate (rotation around z-axis: uphi). All coordinates are ODE2, used for second order differential equations.

#### Additional information for NodeRigidBody2D:

- The Node has the following types = Position2D, Orientation2D, Position, Orientation
- **Short name** for Python = **Rigid2D**

The item **NodeRigidBody2D** with type = 'RigidBody2D' has the following parameters:

Name	type	size	default value	description
name	String		"	node's unique name
referenceCoordinates	Vector3D	3	[0.,0.,0.]	reference coordinates (x-pos,y-pos and ro-
				tation) of node ==> e.g. ref. coordinates
				for finite elements; global position of node
				without displacement
initialCoordinates	Vector3D	3	[0.,0.,0.]	initial displacement coordinates and angle
				(relative to reference coordinates)
initialVelocities	Vector3D	3	[0.,0.,0.]	initial velocity coordinates
visualization	VNodeRigidBod	y2D		parameters for visualization of item

#### The item VNodeRigidBody2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size (diameter, dimensions of un-
				derlying cube, etc.) for item; size == -1.f
				means that default size is used
color	Float4	4	[-1.,-1.,-1.]	Default RGBA color for nodes; 4th value
				is alpha-transparency; R=-1.f means, that
				default color is used

#### Detailed information on NodeRigidBody2D:

input parameter	symbol	description see tables above
referenceCoordinates	$\mathbf{q}_{\text{ref}} = [q_0, q_1, \psi_0]_{\text{ref}}^{\text{T}}$	
initialCoordinates	$\mathbf{q}_{\text{ini}} = [q_0, q_1, \psi_0]_{\text{ini}}^{\text{T}}$	
initialVelocities	$\dot{\mathbf{q}}_{\text{ini}} = [\dot{q}_0,  \dot{q}_1,  \dot{\psi}_0]_{\text{ini}}^{\text{T}} = [v_0,  v_1,  \omega_2]_{\text{ini}}^{\text{T}}$	

#### The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Position	${}^{0}\mathbf{p}_{\text{config}} = {}^{0}[p_0, p_1, 0]_{\text{config}}^{\text{T}} = {}^{0}\mathbf{u}_{\text{config}} +$	global 3D position vector of node; $\mathbf{u}_{ref} = 0$
	$^{0}\mathbf{p}_{\mathrm{ref}}$	
Displacement	$^{0}\mathbf{u}_{\text{config}} = [q_0, q_1, 0]_{\text{config}}^{\text{T}}$	global 3D displacement vector of node
Velocity	${}^{0}\mathbf{v}_{\text{config}} = [\dot{q}_{0},  \dot{q}_{1},  0]_{\text{config}}^{\text{T}}$	global 3D velocity vector of node

Coordinates	$\mathbf{c}_{\text{config}} = [q_0, q_1, \psi_0]_{\text{config}}^{\text{T}}$	coordinate vector of node, having 2 dis-
	Coming	placement coordinates and 1 angle
Coordinates_t	$\dot{\mathbf{c}}_{\text{config}} = [\dot{q}_0,  \dot{q}_1,  \dot{\psi}_0]_{\text{config}}^{\text{T}}$	velocity coordinates vector of node
RotationMatrix	$[A_{00}, A_{01}, A_{02}, A_{10}, \ldots, A_{21}, A_{22}]_{\text{config}}^{\text{T}}$	vector with 9 components of the rotation
		matrix $^{0b}$ <b>A</b> config in row-major format, in any
		configuration; the rotation matrix trans-
		forms local (b) to global (0) coordinates
Rotation	$[\theta_0]_{\text{config}}^{\text{T}} = [\psi_0]_{\text{ref}}^{\text{T}} + [\psi_0]_{\text{config}}^{\text{T}}$	vector with 1 angle around out of plane axix
AngularVelocity	$^{0}\boldsymbol{\omega}_{\text{config}} = ^{0}[\omega_{0}, 0, 0]_{\text{config}}^{\text{T}}$	global 3D angular velocity vector of node
AngularVelocityLocal	${}^{b}\boldsymbol{\omega}_{\text{config}} = {}^{b}[\omega_0, 0, 0]_{\text{config}}^{\text{T}}$	local (body-fixed) 3D angular velocity vec-
		tor of node

**Description of Item**: The node provides 2 displacement coordinates (displacement of center of mass, COM,  $(q_0, q_1)$ ) and 1 rotation parameter  $(\theta_0)$ . According equations need to be provided by an according object (e.g., RigidBody2D). Using the rotation parameter  $\theta_{0\text{config}} = \psi_{0ref} + \psi_{0\text{config}}$ , the rotation matrix is defined as

$${}^{0b}\mathbf{A}_{\text{config}} = \begin{bmatrix} \cos(\theta_0) & -\sin(\theta_0) & 0\\ \sin(\theta_0) & \cos(\theta_0) & 0\\ 0 & 0 & 1 \end{bmatrix}_{\text{config}}$$

$$(5.22)$$

Example for NodeRigidBody2D: see ObjectRigidBody2D

# 5.2.7 NodePoint2DSlope1

A 2D point/slope vector node for planar Bernoulli-Euler ANCF (absolute nodal coordinate formulation) beam elements; the node has 4 displacement degrees of freedom (2 for displacement of point node and 2 for the slope vector 'slopex'); all coordinates lead to second order differential equations; the slope vector defines the directional derivative w.r.t the local axial (x) coordinate, denoted as ()'; in straight configuration aligned at the global x-axis, the slope vector reads  $\mathbf{r}' = [r'_x \ r'_y]^T = [1 \ 0]^T$ .

#### Additional information for NodePoint2DSlope1:

- The Node has the following types = Position2D, Orientation2D, Point2DSlope1, Position, Orientation
- **Short name** for Python = **Point2DS1**

The item **NodePoint2DSlope1** with type = 'Point2DSlope1' has the following parameters:

Name	type	size	default value	description
name	String		"	node's unique name
referenceCoordinates	Vector4D	4	[0.,0.,1.,0.]	reference coordinates (x-pos,y-pos; x-
				slopex, y-slopex) of node; global position
				of node without displacement
initialCoordinates	Vector4D	4	[0.,0.,0.,0.]	initial displacement coordinates: ux, uy
				and x/y 'displacements' of slopex
initialVelocities	Vector4D	4	[0.,0.,0.,0.]	initial velocity coordinates
visualization	VNodePoint2DSlop	e1		parameters for visualization of item

The item VNodePoint2DSlope1 has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size (diameter, dimensions of un-
				derlying cube, etc.) for item; size == -1.f
				means that default size is used
color	Float4	4	[-1.,-1.,-1.]	Default RGBA color for nodes; 4th value
				is alpha-transparency; R=-1.f means, that
				default color is used

# Detailed information on NodePoint2DSlope1: The following output parameters are available as Output-VariableType in sensors and other functions:

output parameter	symbol	description
Position		global 3D position vector of node (=dis-
		placement+reference position)
Displacement		global 3D displacement vector of node
Velocity		global 3D velocity vector of node
Coordinates		coordinates vector of node (2 displacement
		coordinates + 2 slope vector coordinates)

Coordinates_t	velocity coordinates vector of node (deriva-
	tive of the 2 displacement coordinates + 2
	slope vector coordinates)

# 5.2.8 NodeGenericODE2

A node containing a number of ODE2 variables; use e.g. for scalar dynamic equations (Mass1D) or for the ALECable element.

#### Additional information for NodeGenericODE2:

• The Node has the following types = GenericODE2

The item **NodeGenericODE2** with type = 'GenericODE2' has the following parameters:

Name	type	size	default value	description
name	String		"	node's unique name
referenceCoordinates	Vector		[]	generic reference coordinates of node;
				must be consistent with numberO-
				fODE2Coordinates
initialCoordinates	Vector		[]	initial displacement coordinates;
				must be consistent with numberO-
				fODE2Coordinates
initialCoordinates_t	Vector		[]	initial velocity coordinates; must be consis-
				tent with numberOfODE2Coordinates
numberOfODE2Coordinates	Index		0	number of generic ODE2 coordinates
visualization	VNodeGenericODE	2		parameters for visualization of item

# The item VNodeGenericODE2 has the following parameters:

Name	type	size	default value	description
show	bool		False	set true, if item is shown in visualization
				and false if it is not shown

#### Detailed information on NodeGenericODE2:

input parameter	symbol	description see tables above
referenceCoordinates	$\mathbf{q}_{\mathrm{ref}} = [q_0, \ldots, q_{nc}]_{\mathrm{ref}}^{\mathrm{T}}$	
initialCoordinates	$\mathbf{q}_{\text{ini}} = [q_0, \ldots, q_{nc}]_{\text{ini}}^{\text{T}}$	
initialCoordinates_t	$\dot{\mathbf{q}}_{\mathrm{ini}} = [\dot{q}_0, \ldots, \dot{q}_{n_c}]_{\mathrm{ini}}^{\mathrm{T}}$	
numberOfODE2Coordinates	$n_c$	

output parameter	symbol	description
Coordinates	$\mathbf{q}_{\text{config}} = [q_0, \dots, q_{nc}]_{\text{config}}^{\text{T}}$	coordinates vector of node
Coordinates_t	$\dot{\mathbf{q}}_{\text{config}} = [\dot{q}_0, \dots, \dot{q}_{nc}]_{\text{config}}^{\text{T}}$	velocity coordinates vector of node

#### 5.2.9 NodeGenericData

A node containing a number of data (history) variables; use e.g. for contact (active set), friction or plasticity (history variable).

#### Additional information for NodeGenericData:

• The Node has the following types = GenericData

The item **NodeGenericData** with type = 'GenericData' has the following parameters:

Name	type	size	default value	description
name	String		"	node's unique name
initialCoordinates	Vector		[]	initial data coordinates
numberOfDataCoordinates	Index		0	number of generic data coordinates (history
				variables)
visualization	VNodeGenericData	ı		parameters for visualization of item

# The item VNodeGenericData has the following parameters:

Name	type	size	default value	description
show	bool		False	set true, if item is shown in visualization
				and false if it is not shown

#### Detailed information on NodeGenericData:

input parameter	symbol	description see tables above
initialCoordinates	$\mathbf{x}_{\text{ini}} = [x_0, \ldots, x_{n_c}]_{\text{ini}}^{\text{T}}$	
numberOfDataCoordinates	$n_c$	

output parameter	symbol	description
Coordinates	$\mathbf{x}_{\text{config}} = [x_0, \dots, x_{nc}]_{\text{config}}^{\text{T}}$	data coordinates (history variables) vector
		of node

#### 5.2.10 NodePointGround

A 3D point node fixed to ground. The node can be used as NodePoint, but it does not generate coordinates. Applied or reaction forces do not have any effect.

#### Additional information for NodePointGround:

- The Node has the following types = Ground, Position2D, Position, GenericODE2
- **Short name** for Python = **PointGround**

The item **NodePointGround** with type = 'PointGround' has the following parameters:

Name	type	size	default value	description
name	String		"	node's unique name
referenceCoordinates	Vector3D	3	[0.,0.,0.]	reference coordinates of node ==> e.g. ref.
				coordinates for finite elements; global posi-
				tion of node without displacement
visualization	VNodePointGround	d		parameters for visualization of item

# The item VNodePointGround has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size (diameter, dimensions of un-
				derlying cube, etc.) for item; size == -1.f
				means that default size is used
color	Float4	4	[-1.,-1.,-1.]	Default RGBA color for nodes; 4th value
				is alpha-transparency; R=-1.f means, that
				default color is used

#### Detailed information on NodePointGround:

input parameter	symbol	description see tables above
referenceCoordinates	$\mathbf{q}_{\text{ref}} = [q_0, q_1, q_2]_{\text{ref}}^{\text{T}} = \mathbf{p}_{\text{ref}} = \begin{bmatrix} r_0, r_1, r_2 \end{bmatrix}^{\text{T}}$	

output parameter	symbol	description
Position	$\mathbf{p}_{\text{config}} = [p_0, p_1, p_2]_{\text{config}}^{\text{T}} = \mathbf{p}_{\text{ref}}$	global 3D position vector of node (=refer-
		ence position)
Displacement	$\mathbf{u}_{\text{config}} = [0, 0, 0]_{\text{config}}^{\text{T}}$	zero 3D vector
Velocity	$\mathbf{v}_{\text{config}} = [0, 0, 0]_{\text{config}}^{\text{T}}$	zero 3D vector
Coordinates	$\mathbf{c}_{\mathrm{config}} = []$	vector of length zero
Coordinates_t	$\dot{\mathbf{c}}_{\mathrm{config}} = []$	vector of length zero

# 5.3 Objects

# 5.3.1 ObjectMassPoint

A 3D mass point which is attached to a position-based node, usually NodePoint.

# Additional information for ObjectMassPoint:

- The Object has the following types = Body, SingleNoded
- Requested node type = Position
- **Short name** for Python = **MassPoint**

# The item **ObjectMassPoint** with type = 'MassPoint' has the following parameters:

Name	type	size	default value	description
name	String		"	objects's unique name
physicsMass	UReal		0.	mass [SI:kg] of mass point
nodeNumber	Index		MAXINT	node number for mass point
visualization	VObjectMassPoint			parameters for visualization of item

#### The item VObjectMassPoint has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
graphicsData	BodyGraphicsData			Structure contains data for body visualiza-
				tion; data is defined in special list / dictio-
				nary structure

#### Detailed information on ObjectMassPoint:

input parameter	symbol	description see tables above
physicsMass	m	
nodeNumber	$n_0$	

#### The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Position	${}^{0}\mathbf{p}_{\text{config}}({}^{b}\mathbf{p}) = {}^{0}\mathbf{u}_{\text{config}} + {}^{0}\mathbf{p}_{\text{ref}} + {}^{0b}\mathbf{A} {}^{b}\mathbf{p}$	global position vector of translated local
		position; local (body) coordinate system =
		global coordinate system
Displacement	$^{0}\mathbf{u}_{\text{config}} = [q_0, q_1, q_2]_{\text{config}}^{\text{T}}$	global displacement vector of mass point
Velocity	$^{0}\mathbf{v}_{\text{config}} = ^{0}\mathbf{\dot{u}}_{\text{config}} = [\dot{q}_{0}, \dot{q}_{1}, \dot{q}_{2}]_{\text{config}}^{\text{T}}$	global velocity vector of mass point

#### **Description of Item:**

intermediate variables	symbol	description
node position	$^{0}$ <b>p</b> config = $^{0}$ <b>p</b> $(n_{0})$ config	position of mass point which is provided by
		node $n_0$ in any configuration

node displacement	$^{0}$ <b>u</b> config = $[q]$	g <sub>0</sub> , g <sub>1</sub> ,	$q_2$ ] $_{\text{config}}^{\text{T}}$	=	displacement of mass point which is pro-
	$^{0}$ <b>u</b> $(n_{0})_{\text{config}}$				vided by node $n_0$ in any configuration
node velocity	$^{0}\mathbf{v}_{\text{config}} = [\dot{q}$	jo, ġ <sub>1</sub> ,	$\dot{q}_2]_{\rm config}^{\rm T}$	=	velocity of mass point which is provided by
	$^{0}\mathbf{v}\left( n_{0}\right) _{\mathrm{config}}$		Ü		node $n_0$ in any configuration
transformation matrix	$^{0b}\mathbf{A} = \mathbf{I}^{3\times3}$				transformation of local body (b) coordinates
					to global (0) coordinates; this is the constant
					unit matrix, because local = global coordi-
					nates for the mass point
residual forces	${}^{0}\mathbf{f} = [f_{0}, f_{1}, f_{2}]$	] <sup>T</sup>			residual of all forces on mass point
applied forces	${}^{0}\mathbf{f}_{a} = [f_{0}, f_{1}, f_{2}]$	$[2]^{T}$			applied forces (loads, connectors, joint re-
					action forces,)

# **Equations of motion:**

$$\begin{bmatrix} m & 0 & 0 \\ 0 & m & 0 \\ 0 & 0 & m \end{bmatrix} \begin{bmatrix} \ddot{q}_0 \\ \ddot{q}_1 \\ \ddot{q}_2 \end{bmatrix} = \begin{bmatrix} f_0 \\ f_1 \\ f_2 \end{bmatrix}. \tag{5.23}$$

For example, a LoadCoordinate on coordinate 1 of the node would add a term in  $f_1$  on the RHS. Position-based markers can measure position  $\mathbf{p}_{\text{config}}$ . The **position jacobian** 

$$\mathbf{J}_{pos} = \partial \mathbf{p}_{cur} / \partial \mathbf{c}_{cur} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$
 (5.24)

transforms the action of global applied forces  ${}^{0}\mathbf{f}_{a}$  of position-based markers on the coordinates  $\mathbf{c}$ 

$$\mathbf{Q} = \mathbf{J}_{vos}^{\phantom{vos}0} \mathbf{f}_{a}. \tag{5.25}$$

#### **Example** for ObjectMassPoint:

# 5.3.2 ObjectMassPoint2D

A 2D mass point which is attached to a position-based 2D node.

#### Additional information for ObjectMassPoint2D:

- The Object has the following types = Body, SingleNoded
- Requested node type = Position2D + Position
- **Short name** for Python = **MassPoint2D**

# The item **ObjectMassPoint2D** with type = 'MassPoint2D' has the following parameters:

Name	type	size	default value	description
name	String		"	objects's unique name
physicsMass	UReal		0.	mass [SI:kg] of mass point
nodeNumber	Index		MAXINT	node number for mass point
visualization	VObjectMassPoint2	D		parameters for visualization of item

# The item VObjectMassPoint2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
graphicsData	BodyGraphicsData			Structure contains data for body visualiza-
				tion; data is defined in special list / dictio-
				nary structure

# Detailed information on ObjectMassPoint2D:

input parameter	symbol	description see tables above
physicsMass	m	
nodeNumber	<i>n</i> 0	

# The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Position	$0 \mathbf{p}_{\text{config}}(b \mathbf{p}) = 0 \mathbf{u}_{\text{config}} + 0 \mathbf{p}_{\text{ref}} + 0 b \mathbf{A} b \mathbf{p}$	global position vector of translated local
		position; local (body) coordinate system =
		global coordinate system
Displacement	$^{0}\mathbf{u}_{\text{config}} = [q_0, q_1, 0]_{\text{config}}^{\text{T}}$	global displacement vector of mass point
Velocity	${}^{0}\mathbf{v}_{\text{config}} = {}^{0}\dot{\mathbf{u}}_{\text{config}} = [\dot{q}_{0}, \ \dot{q}_{1}, \ 0]_{\text{config}}^{\text{T}}$	global velocity vector of mass point

#### **Description of Item:**

intermediate variables	symbol	description
node position	$^{0}$ <b>p</b> config = $^{0}$ <b>p</b> $(n_{0})$ config	position of mass point which is provided by
		node $n_0$ in any configuration
node displacement	${}^{0}\mathbf{u}_{\mathrm{config}} = [q_{0}, q_{1}, 0]_{\mathrm{config}}^{\mathrm{T}} =$	displacement of mass point which is pro-
	$^{0}\mathbf{u}(n_{0})_{\mathrm{config}}$	vided by node $n_0$ in any configuration

node velocity	$0$ <b>v</b> <sub>config</sub> = $[\dot{q}_0, \dot{q}_1, 0]_{\text{config}}^{\text{T}}$ =	velocity of mass point which is provided by
	$^{0}\mathbf{v}\left( n_{0}\right) _{\mathrm{config}}$	node $n_0$ in any configuration
transformation matrix	$^{0b}\mathbf{A} = \mathbf{I}^{3\times3}$	transformation of local body (b) coordinates
		to global (0) coordinates; this is the constant
		unit matrix, because local = global coordi-
		nates for the mass point
residual forces	$^{0}\mathbf{f}=[f_{0},\ f_{1}]^{\mathrm{T}}$	residual of all forces on mass point
applied forces	${}^{0}\mathbf{f}_{a} = [f_{0}, f_{1}, f_{2}]^{\mathrm{T}}$	applied forces (loads, connectors, joint re-
		action forces,)

#### Equations of motion:

$$\begin{bmatrix} m & 0 \\ 0 & m \end{bmatrix} \begin{bmatrix} \ddot{q}_0 \\ \ddot{q}_1 \end{bmatrix} = \begin{bmatrix} f_0 \\ f_1 \end{bmatrix}. \tag{5.26}$$

For example, a LoadCoordinate on coordinate 1 of the node would add a term in  $f_1$  on the RHS. Position-based markers can measure position  $\mathbf{p}_{\text{config}}$ . The **position jacobian** 

$$\mathbf{J}_{pos} = \partial \mathbf{p}_{cur} / \partial \mathbf{c}_{cur} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}$$
 (5.27)

transforms the action of global applied forces  ${}^0\mathbf{f}_a$  of position-based markers on the coordinates  $\mathbf{c}$ 

$$\mathbf{Q} = \mathbf{J}_{pos}^{0} \mathbf{f}_{a}. \tag{5.28}$$

#### Example for ObjectMassPoint2D:

# 5.3.3 ObjectRigidBody

A 3D rigid body which is attached to a 3D rigid body node. Equations of motion with the displacements  $[u_x \ u_y \ u_z]^T$  of the center of mass and the rotation parameters (Euler parameters) **q**, the mass m, inertia  $\mathbf{J} = [J_{xx}, J_{xy}, J_{xz}; J_{yx}, J_{yy}, J_{yz}; J_{zx}, J_{zy}, J_{zz}]$  and the residual of all forces and moments  $[R_x \ R_y \ R_z \ R_{q0} \ R_{q1} \ R_{q2} \ R_{q3}]^T$  are given as ...; REMARK: Use the class RigidBodyInertia and AddRigidBody(...) of exudynRigidBodyUtilities.py to handle inertia, COM and mass.

#### Additional information for ObjectRigidBody:

- The Object has the following types = Body, SingleNoded
- Requested node type = Position + Orientation + RigidBody
- **Short name** for Python = **RigidBody**

# The item **ObjectRigidBody** with type = 'RigidBody' has the following parameters:

Name	type	size	default value	description
name	String		"	objects's unique name
physicsMass	UReal		0.	mass [SI:kg] of rigid body
physicsInertia	Vector6D		[0.,0.,0., 0.,0.,0.]	inertia components [SI:kgm <sup>2</sup> ]:
				$[J_{xx}, J_{yy}, J_{zz}, J_{yz}, J_{xz}, J_{xy}]$ of rigid body w.r.t.
				to the reference point of the body, NOT
				w.r.t. to center of mass; use the class
				RigidBodyInertia and AddRigidBody()
				of exudynRigidBodyUtilities.py to handle
				inertia, COM and mass
physicsCenterOfMass	Vector3D	3	[0.,0.,0.]	local position of center of mass (COM); if
				the vector of the COM is [0,0,0], the com-
				putation will not consider additional terms
				for the COM and it is faster
nodeNumber	Index		MAXINT	node number for rigid body node
visualization	VObjectRigidBody			parameters for visualization of item

#### The item VObjectRigidBody has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
graphicsData	BodyGraphicsData			Structure contains data for body visualiza-
				tion; data is defined in special list / dictio-
				nary structure

# Detailed information on ObjectRigidBody:

input parameter	symbol	description see tables above
physicsMass	m	
physicsInertia	J	
physicsCenterOfMass	<sup>b</sup> <b>р</b> сом	
nodeNumber	n0	

output parameter	symbol	description
Position		global position vector of rotated and trans-
		lated local position
Displacement		global displacement vector of local position
RotationMatrix		vector with 9 components of the rotation
		matrix (row-major format)
Rotation		vector with 3 components of the Euler an-
		gles in xyz-sequence (R=Rx*Ry*Rz), recom-
		puted from rotation matrix
Velocity		global velocity vector of local position
AngularVelocity		angular velocity of body
AngularVelocityLocal		local (body-fixed) 3D velocity vector of
		node

# 5.3.4 ObjectRigidBody2D

A 2D rigid body which is attached to a rigid body 2D node. The body obtains coordinates, position, velocity, etc. from the underlying 2D node

# Additional information for ObjectRigidBody2D:

- The Object has the following types = Body, SingleNoded
- Requested node type = Position2D + Orientation2D + Position + Orientation
- Short name for Python = RigidBody2D

The item **ObjectRigidBody2D** with type = 'RigidBody2D' has the following parameters:

Name	type	size	default value	description
name	String		"	objects's unique name
physicsMass	UReal		0.	mass [SI:kg] of rigid body
physicsInertia	UReal		0.	inertia [SI:kgm²] of rigid body w.r.t. center
				of mass
nodeNumber	Index		MAXINT	node number for 2D rigid body node
visualization	VObjectRigidBody2	D		parameters for visualization of item

The item VObjectRigidBody2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
graphicsData	BodyGraphicsData			Structure contains data for body visualiza-
				tion; data is defined in special list / dictio-
				nary structure

#### Detailed information on ObjectRigidBody2D:

input parameter	symbol	description see tables above
physicsMass	m	
physicsInertia	J	
nodeNumber	$n_0$	

output parameter	symbol	description
Position	${}^{0}\mathbf{p}_{\text{config}}({}^{b}\mathbf{p}) = {}^{0}\mathbf{u}_{\text{config}} + {}^{0}\mathbf{p}_{\text{ref}} + {}^{0b}\mathbf{A} {}^{b}\mathbf{p}$	global position vector of body-fixed point
		given by local position vector
Displacement	$^{0}$ <b>u</b> config + $^{0b}$ <b>A</b> $^{b}$ <b>p</b>	global displacement vector of body-fixed
		point given by local position vector
Velocity	${}^{0}\mathbf{v}_{\text{config}} = {}^{0}\dot{\mathbf{u}}_{\text{config}} + {}^{0b}\mathbf{A} ({}^{b}\boldsymbol{\omega} \times {}^{b}\mathbf{p}_{\text{config}})$	global velocity vector of body-fixed point
		given by local position vector
Rotation	$ heta_{0 ext{config}}$	scalar rotation angle of body
AngularVelocity	$\omega_{0 m config}$	angular velocity of body
RotationMatrix	$\operatorname{vec}(^{0b}\mathbf{A}) =$	rotation matrix in vector form (stored in
	$[A_{00}, A_{01}, A_{02}, A_{10}, \dots, A_{21}, A_{22}]_{\text{config}}^{\text{T}}$	row-major order)

#### Description of Item:

intermediate variables	symbol	description
COM position	$^{0}\mathbf{p}_{\text{config}} = ^{0}\mathbf{p}(n_{0})_{\text{config}}$	position of center of mass (COM) which is
		provided by node $n_0$ in any configuration
COM displacement	$\begin{bmatrix} {}^{0}\mathbf{u}_{\mathrm{config}} & = & [q_0, q_1, 0]_{\mathrm{config}}^{\mathrm{T}} & = & \end{bmatrix}$	displacement of center of mass which is pro-
	$^{0}\mathbf{u}\left( n_{0}\right) _{\mathrm{config}}$	vided by node $n_0$ in any configuration
COM velocity	${}^{0}\mathbf{v}_{\text{config}} = [\dot{q}_{0}, \dot{q}_{1}, 0]_{\text{config}}^{\mathrm{T}} =$	velocity of center of mass which is provided
	$^{0}\mathbf{v}\left( n_{0} ight) _{\mathrm{config}}$	by node $n_0$ in any configuration
body rotation	$^{0}\theta_{0\text{config}} = \theta_{0}(n_{0})_{\text{config}} = \psi_{0}(n_{0})_{\text{ref}} +$	rotation of body as provided by node $n_0$ in
	$\psi_0(n_0)_{ m config}$	any configuration
body rotation matrix	$^{0b}$ <b>A</b> config = $^{0b}$ <b>A</b> $(n_0)$ config	rotation matrix which transforms local to
		global coordinates as given by node
local position	${}^{b}\mathbf{p} = [{}^{b}p_{0}, {}^{b}p_{1}, 0]^{T}$ ${}^{0}\boldsymbol{\omega}_{\text{config}} = {}^{0}[\boldsymbol{\omega}_{0}(n_{0}), 0, 0]^{T}_{\text{config}}$	local position as used by markers or sensors
body angular velocity	${}^{0}\boldsymbol{\omega}_{\text{config}} = {}^{0}[\omega_{0}(n_{0}), 0, 0]^{\text{T}}_{\text{config}}$	rotation of body as provided by node $n_0$ in
		any configuration
(generalized) coordinates	$\mathbf{c}_{\text{config}} = [q_0, q_1, \ \psi_0]^{\text{T}}$	generalized coordinates of body (= coordi-
		nates of node)
generalized forces	$^{0}\mathbf{f}=[f_{0},\ f_{1},\ \tau_{2}]^{\mathrm{T}}$	generalized forces applied to body
applied forces	${}^{0}\mathbf{f}_{a} = [f_{0}, f_{1}, 0]^{\mathrm{T}}$	applied forces (loads, connectors, joint re-
		action forces,)
applied torques	${}^{0}\boldsymbol{\tau}_{a}=[0,\ 0,\ \tau_{2}]^{\mathrm{T}}$	applied torques (loads, connectors, joint re-
		action forces,)

#### **Equations of motion:**

$$\begin{bmatrix} m & 0 & 0 \\ 0 & m & 0 \\ 0 & 0 & I \end{bmatrix} \begin{bmatrix} \ddot{q}_0 \\ \ddot{q}_1 \\ \ddot{\psi}_0 \end{bmatrix} = \begin{bmatrix} f_0 \\ f_1 \\ \tau_2 \end{bmatrix} = \mathbf{f}.$$
 (5.29)

For example, a LoadCoordinate on coordinate 2 of the node would add a torque  $\tau_2$  on the RHS.

Position-based markers can measure position  $\mathbf{p}_{\text{config}}$  depending on the local position  ${}^b\mathbf{p}$ . The **position jacobian** depends on the local position  ${}^b\mathbf{p}$  and is defined as,

$$\mathbf{J}_{pos} = \partial \mathbf{p}_{cur} / \partial \mathbf{c}_{cur} = \begin{bmatrix} 1 & 0 & -\sin(\theta)^{b} p_{0} - \cos(\theta)^{b} p_{1} \\ 0 & 1 & \cos(\theta)^{b} p_{0} - \sin(\theta)^{b} p_{1} \\ 0 & 0 & 0 \end{bmatrix}$$
(5.30)

which transforms the action of global forces <sup>0</sup>**f** of position-based markers on the coordinates **c**,

$$\mathbf{Q} = \mathbf{J}_{pos}^{0} \mathbf{f}_{a} \tag{5.31}$$

The rotation jacobian

$$\mathbf{J}_{rot} = \partial \mathbf{p}_{cur} / \partial \mathbf{c}_{cur} = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$
 (5.32)

transforms the action of global torques  $^{0}\tau$  of orientation-based markers on the coordinates c,

$$\mathbf{Q} = \mathbf{J}_{rot}^{0} \mathbf{\tau}_{a} \tag{5.33}$$

**Example** for ObjectRigidBody2D:

# 5.3.5 ObjectGenericODE2

A system of n second order ordinary differential equations (ODE2), having a mass matrix, damping/gyroscopic matrix, stiffness matrix and generalized forces. It can combine generic nodes, or node points. User functions can be used to compute mass matrix and generalized forces depending on given coordinates. NOTE that all matrices, vectors, etc. must have the same dimensions n or  $(n \times n)$ , or they must be empty  $(0 \times 0)$ , except for the mass matrix which always needs to have dimensions  $(n \times n)$ .

# Additional information for ObjectGenericODE2:

- The Object has the following types = Body, MultiNoded, SuperElement
- Requested node type: read detailed information of item

The item **ObjectGenericODE2** with type = 'GenericODE2' has the following parameters:

Name	type	size	default value	description
name	String		"	objects's unique name
nodeNumbers	ArrayIndex		[]	node numbers which provide the coordi-
				nates for the object (consecutively as pro-
				vided in this list)
massMatrix	NumpyMatrix		Matrix[]	mass matrix of object in python numpy for-
				mat
stiffnessMatrix	NumpyMatrix		Matrix[]	stiffness matrix of object in python numpy
				format
dampingMatrix	NumpyMatrix		Matrix[]	damping matrix of object in python numpy
				format
forceVector	NumpyVector		[]	generalized force vector added to RHS
forceUserFunction	PyFunctionVectorS	Scalar2\	/ector	A python user function which computes
	-		0	the generalized user force vector for the
				ODE2 equations; The function takes the
				time, coordinates q (without reference val-
				ues) and coordinate velocities q_t; Example
				for python function with numpy stiffness
				matrix K: $def f(t, q, q_t)$ : return np. $dot(K, q)$
massMatrixUserFunction	PyFunctionMatrix	Scalar2	Vector	A python user function which computes the
			0	mass matrix instead of the constant mass
				matrix; The function takes the time, coordi-
				nates q (without reference values) and co-
				ordinate velocities q_t; Example (academic)
				for python function with numpy stiffness
				matrix M: def $f(t, q, q_t)$ : return $(q[0]+1)*M$
coordinateIndexPerNode	ArrayIndex			this list contains the local coordinate index
				for every node, which is needed, e.g., for
				markers; the list is generated automatically
				every time parameters have been changed
use First Node As Reference Frame	bool		False	set true, if first node $(n_0)$ is used as floating
				reference frame; all other nodes are inter-
				preted relative to the reference frame; used
				to implement FFRF (floating frame of refer-
				ence formulation); NOTE that in this case,
				nodes $[n_1, \ldots, n_n]^T$ are still drawn without
				the reference frame

visualization	VObjectGenericODE2		parameters for visualization of item
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# The item VObjectGenericODE2 has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
color	Float4	4	[-1.,-1.,-1.]	RGBA color for object; 4th value is alpha-
				transparency; R=-1.f means, that default
				color is used
triangleMesh	NumpyMatrixI		MatrixI[]	a matrix, containg node number triples in
				every row, referring to the node numbers
				of the GenericODE2 object; the mesh uses
				the nodes to visualize the underlying object;
				contour plot colors are still computed in the
				local frame!
showNodes	bool		False	set true, nodes are drawn uniquely via the
				mesh, eventually using the floating refer-
				ence frame, even in the visualization of
				the node is show=False; node numbers are
				shown with indicator 'NF'

# Detailed information on ObjectGenericODE2:

input parameter	symbol	description see tables above
nodeNumbers	$\mathbf{n}_n = [n_0, \ldots, n_n]^{\mathrm{T}}$	
massMatrix	$\mathbf{M} \in \mathbb{R}^{n \times n}$	
stiffnessMatrix	$\mathbf{K} \in \mathbb{R}^{n \times n}$	
dampingMatrix	$\mathbf{D} \in \mathbb{R}^{n \times n}$	
forceVector	$\mathbf{f} \in \mathbb{R}^n$	
forceUserFunction	$\mathbf{f}_{user} \in \mathbb{R}^n$	
massMatrixUserFunction	$\mathbf{M}_{user} \in \mathbb{R}^{n \times n}$	

# The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Coordinates		all ODE2 coordinates
Coordinates_t		all ODE2 velocity coordinates
Force		generalized forces for all coordinates (resid-
		ual of all forces except mass*accleration;
		corresponds to ComputeODE2RHS)

**Description of Item**: An object with node numbers  $[n_0, ..., n_n]$  and according numbers of nodal coordinates  $[n_{c_0}, ..., n_{c_n}]$ , the total number of equations (=coordinates) of the object is

$$n = \sum_{i} n_{c_i}. \tag{5.34}$$

**Equations of motion:** 

$$\mathbf{M}\ddot{\mathbf{q}} + \mathbf{D}\dot{\mathbf{q}} + \mathbf{K}\mathbf{q} = \mathbf{f} + \mathbf{f}_{user}(t, \mathbf{q}, \dot{\mathbf{q}})$$
 (5.35)

Note that the user function  $\mathbf{f}_{user}(t, \mathbf{q}, \dot{\mathbf{q}})$  may be empty (=0).

In case that a user mass matrix is specified, Eq. (5.35) is replaced with

$$\mathbf{M}_{user}(t, \mathbf{q}, \dot{\mathbf{q}})\ddot{\mathbf{q}} + \mathbf{D}\dot{\mathbf{q}} + \mathbf{K}\mathbf{q} = \mathbf{f} + \mathbf{f}_{user}(t, \mathbf{q}, \dot{\mathbf{q}})$$
(5.36)

CoordinateLoads are integrated for each ODE2 coordinate on the RHS of the latter equation.

# 5.3.6 ObjectFFRF

This object is used to represent equations modelled by the floating frame of reference formulation (FFRF). It contains a RigidBodyNode (always node 0) and a list of other nodes representing the finite element nodes used in the FFRF.

# Additional information for ObjectFFRF:

- The Object has the following types = Body, MultiNoded, SuperElement
- Requested node type: read detailed information of item

The item **ObjectFFRF** with type = 'FFRF' has the following parameters:

Name	type	size	default value	description
name	String		"	objects's unique name
nodeNumbers	ArrayIndex		[]	node numbers which provide the coordi-
				nates for the object (consecutively as pro-
				vided in this list); the $(n_f + 1)$ nodes repre-
				sent the nodes of the FE mesh (except for
				node 0); the global nodal position needs to
				be reconstructed from the rigid-body mo-
				tion of the reference frame
massMatrixFF	PyMatrixContainer		PyMatrixContainer	[]body-fixed and ONLY flexible coordinates
				part of mass matrix of object given in
				python numpy format (sparse (CSR) or
				dense, converted to sparse matrix); inter-
				nally data is stored in triplet format
stiffnessMatrixFF	PyMatrixContainer		PyMatrixContainer	[]body-fixed and ONLY flexible coordinates
				part of stiffness matrix of object in python
				numpy format (sparse (CSR) or dense, con-
				verted to sparse matrix); internally data is
				stored in triplet format
dampingMatrixFF	PyMatrixContainer		PyMatrixContainer	[]body-fixed and ONLY flexible coordinates
				part of damping matrix of object in python
				numpy format (sparse (CSR) or dense, con-
				verted to sparse matrix); internally data is
				stored in triplet format
forceVector	NumpyVector		[]	generalized, global force vector added to
				RHS; the rigid body part $\mathbf{f}_r$ is directly ap-
				plied to rigid body coordinates while the
				flexible part $\mathbf{f}_{ff}$ is transformed from global
				to local coordinates
forceUserFunction	PyFunctionVectorSe	calar2\	ector	A python user function which computes
			0	the generalized user force vector for the
				ODE2 equations; The function takes the
				time, coordinates q (without reference val-
				ues) and coordinate velocities q_t; Example
				for python function with numpy matrix K:
				def f(t, q, q_t): return np.dot(K, q)

massMatrixUserFunction	PyFunctionMatri	xScalar2	2Vector		A python user function which computes
			0		the TOTAL mass matrix (including refer-
					ence node) and adds the local constant mass
					matrix; this function takes the time, coordi-
					nates q (without reference values) and co-
					ordinate velocities q_t; Example (academic)
					for python function with numpy matrix M:
					def f(t, q, q_t): return (q[0]+1)*M
computeFFRFterms	bool		True		flag decides whether the standard FFRF
					terms are computed; use this flag for user-
					defined definition of FFRF terms in mass
					matrix and quadratic velocity vector
coordinateIndexPerNode	ArrayIndex		[]		this list contains the local coordinate index
					for every node, which is needed, e.g., for
					markers; the list is generated automatically
					every time parameters have been changed
objectIsInitialized	bool		False		flag used to correctly initialize all FFRF ma-
					trices; as soon as this flag is set false, FFRF
					matrices and terms are recomputed
physicsMass	UReal		0.		total mass [SI:kg] of FFRF object, auto-
					computed from mass matrix <b>M</b>
physicsInertia	Matrix3D		[[1,0,0],	[0,1,0],	inertia tensor [SI:kgm²] of rigid body w.r.t.
			[0,0,1]]		to the reference point of the body, auto-
					computed from the mass matrix $\mathbf{M}_{ff}$
physicsCenterOfMass	Vector3D	3	[0.,0.,0.]		local position of center of mass (COM);
					auto-computed from mass matrix M
PHItTM	NumpyMatrix		Matrix[]		projector matrix; may be removed in future
referencePositions	NumpyVector		[]		vector containing the reference positions of
					all flexible nodes
tempVector	NumpyVector		[]		temporary vector
tempCoordinates	NumpyVector		[]		temporary vector containing coordinates
tempCoordinates_t	NumpyVector		[]		temporary vector containing velocity coor-
					dinates
tempRefPosSkew	NumpyMatrix		Matrix[]		matrix with skew symmetric local (de-
					formed) node positions
tempVelSkew	NumpyMatrix		Matrix[]		matrix with skew symmetric local node ve-
					locities
visualization	VObjectFFRF				parameters for visualization of item

# The item VObjectFFRF has the following parameters:

Name	type	size	default value	description
show	bool	5126	True	set true, if item is shown in visualization and false if it is not shown; use visualizationSettings.bodies.deformationScaleFactor to draw scaled (local) deformations; the reference frame node is shown with additional
				letters RF

color	Float4	4	[-1.,-1.,-1.]	RGBA color for object; 4th value is alpha-
				transparency; R=-1.f means, that default
				color is used
triangleMesh	NumpyMatrixI		MatrixI[]	a matrix, containg node number triples in
				every row, referring to the node numbers
				of the GenericODE2 object; the mesh uses
				the nodes to visualize the underlying object;
				contour plot colors are still computed in the
				local frame!
showNodes	bool		False	set true, nodes are drawn uniquely via the
				mesh, eventually using the floating refer-
				ence frame, even in the visualization of
				the node is show=False; node numbers are
				shown with indicator 'NF'

# Detailed information on ObjectFFRF:

input parameter	symbol	description see tables above
nodeNumbers	$\mathbf{n}_n = [n_0, \ldots, n_{n_f}]^{\mathrm{T}}$	
massMatrixFF	$\mathbf{M}_{ff} \in \mathbb{R}^{n_{c_f} \times n_{c_f}}$	
stiffnessMatrixFF	$\mathbf{K}_{ff} \in \mathbb{R}^{n_{c_f} \times n_{c_f}}$	
dampingMatrixFF	$\mathbf{D}_{ff} \in \mathbb{R}^{n_{c_f} \times n_{c_f}}$	
forceVector	$\mathbf{f} \in \mathbb{R}^{n_c}$	
forceUserFunction	$\mathbf{f}_{user} \in \mathbb{R}^{n_c}$	
massMatrixUserFunction	$\mathbf{M}_{user} \in \mathbb{R}^{n_c \times n_c}$	
physicsMass	m	
physicsInertia	$J_r \in \mathbb{R}^{3 \times 3}$	
physicsCenterOfMass	<sup>b</sup> <b>р</b> сом	
PHItTM	$\Phi_t^{\mathrm{T}} \in \mathbb{R}^{n_{c_f} \times 3}$	
referencePositions	$\mathbf{x}_f \in \mathbb{R}^{n_f}$	
tempVector	$\mathbf{v}_{temp} \in \mathbb{R}^{n_f}$	
tempCoordinates	$\mathbf{c}_{temp} \in \mathbb{R}^{n_f}$	
tempCoordinates_t	$\dot{\mathbf{c}}_{temp} \in \mathbb{R}^{n_f}$	
tempRefPosSkew	$\tilde{\mathbf{p}}_f \in \mathbb{R}^{n_{c_f} \times 3}$	
tempVelSkew	$\dot{\tilde{\mathbf{c}}}_f \in \mathbb{R}^{n_{c_f} \times 3}$	

# The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Coordinates		all ODE2 coordinates
Coordinates_t		all ODE2 velocity coordinates
Force		generalized forces for all coordinates (resid-
		ual of all forces except mass*accleration;
		corresponds to ComputeODE2RHS)

# **Description of Item:**

intermediate variables	symbol	description
------------------------	--------	-------------

flexible coordinates transformation	$^{0b}\mathbf{A}_{bd} = \operatorname{diag}([^{0b}\mathbf{A}, \ldots, ^{0b}\mathbf{A})$	block diagonal transformation matrix,
matrix		which transforms all flexible coordinates
		from local to global coordinates

Consider an object with  $n = 1 + n_f$  nodes,  $n_f$  being the 'flexible' nodes. It has node numbers  $[n_0, \ldots, n_{n_f}]$  and according numbers of nodal coordinates  $[n_c, \ldots, n_{c_n}]$ . This gives  $n_c$  total nodal coordinates,

$$n_c = \sum_{i=0}^{n_f} n_{c_i}. (5.37)$$

whereof

$$n_{c_f} = \sum_{i=1}^{n_f} n_{c_i}. (5.38)$$

The total number of equations (=coordinates) of the object is  $n_c$ . The first node  $n_0$  represents the rigid body motion of the underlying reference frame with  $n_{c_r} = n_{c_0}$  coordinates (e.g.,  $n_{c_r} = 6$  coordinates for Euler angles and  $n_{c_r} = 7$  coordinates in case of Euler parameters).

**Equations of motion**, in case that computeFFRFterms = True (NEEDS TO BE UPDATED):

$$\begin{pmatrix}
\mathbf{M}_{user}(t, \mathbf{q}, \dot{\mathbf{q}}) + \begin{bmatrix}
\mathbf{M}_{tt} & \mathbf{M}_{tr} & \mathbf{M}_{tf} \\
\mathbf{M}_{rr} & \mathbf{M}_{rf} \\
\text{sym.} & \mathbf{M}_{ff}
\end{bmatrix} \dot{\mathbf{q}} + \begin{bmatrix}
0 & 0 & 0 \\
0 & 0 & 0 \\
0 & 0 & \mathbf{D}_{ff}
\end{bmatrix} \dot{\mathbf{q}} + \begin{bmatrix}
0 & 0 & 0 \\
0 & 0 & 0 \\
0 & 0 & \mathbf{K}_{ff}
\end{bmatrix} \mathbf{q} = \mathbf{f}_{Q}(\mathbf{q}, \dot{\mathbf{q}}) + \begin{bmatrix}\mathbf{f}_{r} \\ 0 b \mathbf{A}_{bd}^{T} \mathbf{f}_{ff}
\end{bmatrix} + \mathbf{f}_{user}(t, \mathbf{q}, \dot{\mathbf{q}})$$
(5.39)

In case that computeFFRFterms = False, the mass terms  $\mathbf{M}_{tt} \dots \mathbf{M}_{ff}$  are zero (not computed) and the quadratic velocity vector  $\mathbf{f}_Q = \mathbf{0}$ . Note that the user functions  $\mathbf{f}_{user}(t, \mathbf{q}, \dot{\mathbf{q}})$  and  $\mathbf{M}_{user}(t, \mathbf{q}, \dot{\mathbf{q}})$  may be empty (=0).

CoordinateLoads are integrated for each ODE2 coordinate on the RHS of the latter equation.

# 5.3.7 ObjectFFRFreducedOrder

This object is used to represent modally reduced flexible bodies using the floating frame of reference formulation (FFRF) and the component mode synthesis. It contains a RigidBodyNode (always node 0) and a NodeGenericODE2 representing the modal coordinates.

# ${\bf Additional\ information\ for\ Object FFR} \\ {\bf Freduced Order} \\ :$

- The Object has the following types = Body, MultiNoded, SuperElement
- Requested node type: read detailed information of item

The item **ObjectFFRFreducedOrder** with type = 'FFRFreducedOrder' has the following parameters:

Name	type	size	default value	description
name	String		"	objects's unique name
nodeNumbers	ArrayIndex		[]	node numbers of rigid body node and
				NodeGenericODE2 for modal coordinates;
				the global nodal position needs to be recon-
				structed from the rigid-body motion of the
				reference frame, the modal coordinates and
				the mode basis
massMatrixReduced	PyMatrixContainer		PyMatrixContaine	r[]body-fixed and ONLY flexible coordinates
				part of reduced mass matrix; provided as
				MatrixContainer(sparse/dense matrix)
stiffnessMatrixReduced	PyMatrixContainer		PyMatrixContaine	r[]body-fixed and ONLY flexible coordinates
				part of reduced stiffness matrix; provided
				as MatrixContainer(sparse/dense matrix)
dampingMatrixReduced	PyMatrixContainer		PyMatrixContaine	r[]body-fixed and ONLY flexible coordinates
				part of reduced damping matrix; provided
				as MatrixContainer(sparse/dense matrix)
forceUserFunction	PyFunctionVectorSo	calar2\	ector	A python user function which computes
			0	the generalized user force vector for the
				ODE2 equations; The function takes the
				time, coordinates q (without reference val-
				ues) and coordinate velocities q_t; Example
				for python function with numpy matrix K:
				$def f(t, q, q_t)$ : return np.dot(K, q)
massMatrixUserFunction	PyFunctionMatrixS	calar2	Vector	A python user function which computes
			0	the TOTAL mass matrix (including refer-
				ence node) and adds the local constant mass
				matrix; this function takes the time, coordi-
				nates q (without reference values) and co-
				ordinate velocities q_t; Example (academic)
				for python function with numpy matrix M:
				def f(t, q, q_t): return (q[0]+1)*M
computeFFRFterms	bool		True	flag decides whether the standard FFR-
				F/CMS terms are computed; use this flag
				for user-defined definition of FFRF terms in
				mass matrix and quadratic velocity vector

modeBasis	NumpyMatrix		Matrix[]		mode basis, which transforms re-
					duced coordinates to (full) nodal co-
					ordinates, written as a single vector
					$[u_{x,n_0}, u_{y,n_0}, u_{z,n_0}, \ldots, u_{x,n_n}, u_{y,n_n}, u_{z,n_n}]^{\mathrm{T}}$
referencePositions	NumpyVector		[]		vector containing the reference positions of
					all flexible nodes, needed for graphics
physicsMass	UReal		0.		total mass [SI:kg] of FFRF object, auto-
					computed from mass matrix M
physicsInertia	Matrix3D		[[1,0,0],	[0,1,0],	inertia tensor [SI:kgm²] of rigid body w.r.t.
			[0,0,1]]		to the reference point of the body, auto-
					computed from the mass matrix $\mathbf{M}_{ff}$
physicsCenterOfMass	Vector3D	3	[0.,0.,0.]		local position of center of mass (COM);
					auto-computed from mass matrix <b>M</b>
PHItTM	NumpyMatrix		Matrix[]		projector matrix; may be removed in future
tempUserFunctionForce	NumpyVector		[]		temporary vector for UF force
tempRefPosSkew	NumpyMatrix		Matrix[]		matrix with skew symmetric local (de-
					formed) node positions
tempVelSkew	NumpyMatrix		Matrix[]		matrix with skew symmetric local node ve-
					locities
visualization	VObjectFFRFreduc	edOrd	er		parameters for visualization of item

# The item VObjectFFRFreducedOrder has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in
				visualization and false if it is
				not shown; use visualizationSet-
				tings.bodies.deformationScaleFactor to
				draw scaled (local) deformations; the refer-
				ence frame node is shown with additional
				letters RF
color	Float4	4	[-1.,-1.,-1.]	RGBA color for object; 4th value is alpha-
				transparency; R=-1.f means, that default
				color is used
triangleMesh	NumpyMatrixI		MatrixI[]	a matrix, containg node number triples in
				every row, referring to the node numbers
				of the GenericODE2 object; the mesh uses
				the nodes to visualize the underlying object;
				contour plot colors are still computed in the
				local frame!
showNodes	bool		False	set true, nodes are drawn uniquely via the
				mesh, eventually using the floating refer-
				ence frame, even in the visualization of
				the node is show=False; node numbers are
				shown with indicator 'NF'

# $Detailed\ information\ on\ Object FRF reduced Order:$

input parameter	symbol	description see tables above
nodeNumbers	$\mathbf{n} = [n_0, n_1]^{\mathrm{T}}$	
massMatrixReduced	$\mathbf{M}_{red} \in \mathbb{R}^{n_{c_f} \times n_{c_f}}$	
stiffnessMatrixReduced	$\mathbf{K}_{red} \in \mathbb{R}^{n_{c_f} \times n_{c_f}}$	
dampingMatrixReduced	$\mathbf{D}_{red} \in \mathbb{R}^{n_{c_f} \times n_{c_f}}$	
forceUserFunction	$\mathbf{f}_{user} \in \mathbb{R}^{n_c}$	
massMatrixUserFunction	$\mathbf{M}_{user} \in \mathbb{R}^{n_c \times n_c}$	
modeBasis	$\mathbf{\Phi} \in \mathbb{R}^{n_{c_f} \times n_m}$	
referencePositions	$\mathbf{x}_f \in \mathbb{R}^{n_f}$	
physicsMass	m	
physicsInertia	$J_r \in \mathbb{R}^{3 \times 3}$	
physicsCenterOfMass	<sup>b</sup> <b>р</b> сом	
PHItTM	$\Phi_t^{\mathrm{T}} \in \mathbb{R}^{n_{c_f} \times 3}$	
tempUserFunctionForce	$\mathbf{v}_{temp} \in \mathbb{R}^{n_c}$	
tempRefPosSkew	$\tilde{\mathbf{p}}_f \in \mathbb{R}^{n_{c_f} \times 3}$	
tempVelSkew	$\mathbf{\tilde{c}}_f \in \mathbb{R}^{n_{c_f} \times 3}$	

#### The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Coordinates		all ODE2 coordinates
Coordinates_t		all ODE2 velocity coordinates
Force		generalized forces for all coordinates (resid-
		ual of all forces except mass*accleration;
		corresponds to ComputeODE2RHS)

#### **Description of Item:**

intermediate variables	symbol	description
flexible coordinates transformation	$^{0b}\mathbf{A}_{bd} = \operatorname{diag}([^{0b}\mathbf{A}, \ldots, ^{0b}\mathbf{A})$	block diagonal transformation matrix,
matrix		which transforms all flexible coordinates
		from local to global coordinates

#### Quantities:

- object has two nodes
- $n_n$  ... number of mesh nodes
- $n_c = 3n_n$  ... number of mesh coordinates
- $n_{rigid}$  ... number of rigid body node coordinates: 6 in case of Euler angles and 7 in case of Euler parameters
- $n_{ODE2} = n_c + n_{rigid}$  ... total number of object coordinates
- $n_m$  ... number of modal coordinates; computed from number of columns in modeBasis
- $\bullet$   $\Phi$ ... mode basis, containing eigenmodes and static modes
- $\mathbf{x}_f$  ... node reference coordinates for mesh nodes

**Equations of motion**, in case that computeFFRFterms = True (NEEDS TO BE UPDATED FOR FFRF!!!!):

$$\begin{pmatrix}
\mathbf{M}_{user}(t, \mathbf{q}, \dot{\mathbf{q}}) + \begin{bmatrix}
\mathbf{M}_{tt} & \mathbf{M}_{tr} & \mathbf{M}_{tf} \\
\mathbf{M}_{rr} & \mathbf{M}_{rf} \\
\text{sym.} & \mathbf{M}_{ff}
\end{bmatrix} \dot{\mathbf{q}} + \begin{bmatrix}
0 & 0 & 0 \\
0 & 0 & 0 \\
0 & 0 & \mathbf{D}_{ff}
\end{bmatrix} \dot{\mathbf{q}} + \begin{bmatrix}
0 & 0 & 0 \\
0 & 0 & 0 \\
0 & 0 & \mathbf{K}_{ff}
\end{bmatrix} \mathbf{q} = \mathbf{f}_{Q}(\mathbf{q}, \dot{\mathbf{q}}) + \mathbf{f}_{user}(t, \mathbf{q}, \dot{\mathbf{q}}) \qquad (5.40)$$

In case that computeFFRFterms = False, the mass terms  $\mathbf{M}_{tt} \dots \mathbf{M}_{ff}$  are zero (not computed) and the quadratic velocity vector  $\mathbf{f}_Q = \mathbf{0}$ . Note that the user functions  $\mathbf{f}_{user}(t, \mathbf{q}, \dot{\mathbf{q}})$  and  $\mathbf{M}_{user}(t, \mathbf{q}, \dot{\mathbf{q}})$  may be empty (=0).

 $Coordinate Loads \ are \ integrated \ for \ each \ ODE2 \ coordinate \ on \ the \ RHS \ of \ the \ latter \ equation.$ 

# 5.3.8 ObjectANCFCable2D

A 2D cable finite element using 2 nodes of type NodePoint2DSlope1; the element has 8 coordinates and uses cubic polynomials for position interpolation; the Bernoulli-Euler beam is capable of large deformation as it employs the material measure of curvature for the bending.

#### Additional information for ObjectANCFCable2D:

- Requested node type = Position2D + Orientation2D + Point2DSlope1 + Position + Orientation
- **Short name** for Python = **Cable2D**

The item **ObjectANCFCable2D** with type = 'ANCFCable2D' has the following parameters:

Name	type	size	default value	description
name	String		"	objects's unique name
physicsLength	UReal		0.	reference length L [SI:m] of beam; such that
				the total volume (e.g. for volume load)
				gives $\rho AL$
physicsMassPerLength	UReal		0.	mass $\rho A$ [SI:kg/m <sup>2</sup> ] of beam
physicsBendingStiffness	UReal		0.	bending stiffness EI [SI:Nm <sup>2</sup> ] of beam; the
				bending moment is $m = EI(\kappa - \kappa_0)$ , in which
				$\kappa$ is the material measure of curvature
physicsAxialStiffness	UReal		0.	axial stiffness EA [SI:N] of beam; the axial
				force is $f_{ax} = EA(\varepsilon - \varepsilon_0)$ , in which $\varepsilon =  \mathbf{r}'  - 1$
				is the axial strain
physicsBendingDamping	UReal		0.	bending damping $d_{EI}$ [SI:Nm <sup>2</sup> /s] of beam;
				the additional virtual work due to damping
				is $\delta W_{\dot{\kappa}} = \int_0^L \dot{\kappa} \delta \kappa dx$
physicsAxialDamping	UReal		0.	axial stiffness $d_{EA}$ [SI:N/s] of beam; the ad-
				ditional virtual work due to damping is
				$\delta W_{\dot{\varepsilon}} = \int_0^L \dot{\varepsilon} \delta \varepsilon dx$
physicsReferenceAxialStrain	UReal		0.	reference axial strain of beam (pre-
				deformation) $\varepsilon_0$ [SI:1] of beam; without ex-
				ternal loading the beam will statically keep
				the reference axial strain value
physicsReferenceCurvature	UReal		0.	reference curvature of beam (pre-
				deformation) $\kappa_0$ [SI:1/m] of beam; without
				external loading the beam will statically
				keep the reference curvature value
nodeNumbers	Index2		[MAXINT, MAX-	two node numbers ANCF cable element
			INT]	
useReducedOrderIntegration	Bool		False	false: use Gauss order 9 integration for vir-
				tual work of axial forces, order 5 for virtual
				work of bending moments; true: use Gauss
				order 7 integration for virtual work of axial
				forces, order 3 for virtual work of bending
				moments
visualization	VObjectANCFCable2	2D		parameters for visualization of item

The item VObjectANCFCable2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawHeight	float		0.	if beam is drawn with rectangular shape,
				this is the drawing height
color	Float4		[-1.,-1.,-1.]	RGBA color of the object; if R==-1, use de-
				fault color

# Detailed information on ObjectANCFCable2D: The following output parameters are available as Output-VariableType in sensors and other functions:

output parameter	symbol	description
Position		global position vector of local axis (1) and
		cross section (2) position
Displacement		global displacement vector of local axis (1)
		and cross section (2) position
Velocity		global velocity vector of local axis (1) and
		cross section (2) position
Director1		(axial) slope vector of local axis position
Strain		axial strain (scalar)
Curvature		axial strain (scalar)
Force		(local) section normal force (scalar)
Torque		(local) bending moment (scalar)

# 5.3.9 ObjectALEANCFCable2D

A 2D cable finite element using 2 nodes of type NodePoint2DSlope1 and a axially moving coordinate of type NodeGenericODE2; the element has 8+1 coordinates and uses cubic polynomials for position interpolation; the element in addition to ANCFCable2D adds an Eulerian axial velocity by the GenericODE2 coordinate

# Additional information for ObjectALEANCFCable2D:

- Requested node type: read detailed information of item
- **Short name** for Python = **ALECable2D**

The item **ObjectALEANCFCable2D** with type = 'ALEANCFCable2D' has the following parameters:

Name	type	size	default value	description
name	String		"	objects's unique name
physicsLength	UReal		0.	reference length $L$ [SI:m] of beam; such that the total volume (e.g. for volume load) gives $\rho AL$
physicsMassPerLength	UReal		0.	mass $\rho A$ [SI:kg/m <sup>2</sup> ] of beam
physicsMovingMassFactor	UReal		1.	this factor denotes the amount of $\rho A$ which is moving; physicsMovingMassFactor=1 means, that all mass is moving; physicsMovingMassFactor=0 means, that no mass is moving; factor can be used to simulate e.g. pipe conveying fluid, in which $\rho A$ is the mass of the pipe+fluid, while $physicsMovingMassFactor \cdot \rho A$ is the mass per unit length of the fluid
physicsBendingStiffness	UReal		0.	bending stiffness $EI$ [SI:Nm <sup>2</sup> ] of beam; the bending moment is $m = EI(\kappa - \kappa_0)$ , in which $\kappa$ is the material measure of curvature
physicsAxialStiffness	UReal		0.	axial stiffness $EA$ [SI:N] of beam; the axial force is $f_{ax} = EA(\varepsilon - \varepsilon_0)$ , in which $\varepsilon =  \mathbf{r}'  - 1$ is the axial strain
physicsBendingDamping	UReal		0.	bending damping $d_{EI}$ [SI:Nm <sup>2</sup> /s] of beam; the additional virtual work due to damping is $\delta W_{\dot{\kappa}} = \int_0^L \dot{\kappa} \delta \kappa dx$
physicsAxialDamping	UReal		0.	axial stiffness $d_{EA}$ [SI:N/s] of beam; the additional virtual work due to damping is $\delta W_{\hat{\varepsilon}} = \int_0^L \dot{\varepsilon} \delta \varepsilon dx$
physicsReferenceAxialStrain	UReal		0.	reference axial strain of beam (pre- deformation) $\varepsilon_0$ [SI:1] of beam; without ex- ternal loading the beam will statically keep the reference axial strain value
physicsReferenceCurvature	UReal		0.	reference curvature of beam (pre- deformation) $\kappa_0$ [SI:1/m] of beam; without external loading the beam will statically keep the reference curvature value

physicsUseCouplingTerms	bool		True	true: correct case, where all coupling terms
				due to moving mass are respected; false:
				only include constant mass for ALE node
				coordinate, but deactivate other coupling
				terms (behaves like ANCFCable2D then)
nodeNumbers	Index3		[MAXINT, MAX-	two node numbers ANCF cable element,
			INT, MAXINT]	third node=ALE GenericODE2 node
useReducedOrderIntegration	Bool		False	false: use Gauss order 9 integration for vir-
				tual work of axial forces, order 5 for virtual
				work of bending moments; true: use Gauss
				order 7 integration for virtual work of axial
				forces, order 3 for virtual work of bending
				moments
visualization	VObjectALEANCF	Cable2	D	parameters for visualization of item

# The item VObjectALEANCFCable2D has the following parameters:

*		0 1		
Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawHeight	float		0.	if beam is drawn with rectangular shape,
				this is the drawing height
color	Float4		[-1.,-1.,-1.]	RGBA color of the object; if R==-1, use de-
				fault color

# Detailed information on ObjectALEANCFCable2D: The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Position		global position vector of local axis (1) and
		cross section (2) position
Displacement		global displacement vector of local axis (1)
		and cross section (2) position
Velocity		global velocity vector of local axis (1) and
		cross section (2) position
Director1		(axial) slope vector of local axis position
Strain		axial strain (scalar)
Curvature		axial strain (scalar)
Force		(local) section normal force (scalar)
Torque		(local) bending moment (scalar)

# 5.3.10 ObjectGround

A ground object behaving like a rigid body, but having no degrees of freedom; used to attach body-connectors without an action. For examples see spring dampers and joints.

# Additional information for ObjectGround:

• The Object has the following types = Ground, Body

The item **ObjectGround** with type = 'Ground' has the following parameters:

Name	type	size	default value	description
name	String		"	objects's unique name
referencePosition	Vector3D	3	[0.,0.,0.]	reference position for ground object; local position is added on top of reference position for a ground object
visualization	VObjectGround			parameters for visualization of item

#### The item VObjectGround has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
color	Float4		[-1.,-1.,-1.]	RGB node color; if R==-1, use default color
graphicsData	BodyGraphicsData			Structure contains data for body visualiza-
				tion; data is defined in special list / dictio-
				nary structure

# Detailed information on ObjectGround: The following output parameters are available as OutputVariable-Type in sensors and other functions:

output parameter	symbol	description
Position		global position vector of rotated and trans-
		lated local position
Displacement		global displacement vector of local position
Velocity		global velocity vector of local position
AngularVelocity		angular velocity of body
RotationMatrix		rotation matrix in vector form (stored in
		row-major order)

# 5.3.11 ObjectConnectorSpringDamper

An simple spring-damper element with additional force; connects to position-based markers.

# Additional information for ObjectConnectorSpringDamper:

- The Object has the following types = Connector
- Requested marker type = Position
- **Short name** for Python = **SpringDamper**

The item **ObjectConnectorSpringDamper** with type = 'ConnectorSpringDamper' has the following parameters:

Name	type	size	default value	description
name	String		"	connector's unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX- INT ]	list of markers used in connector
referenceLength	UReal		0.	reference length [SI:m] of spring
stiffness	UReal		0.	stiffness [SI:N/m] of spring; acts against (length-initialLength)
damping	UReal		0.	damping [SI:N/(m s)] of damper; acts against d/dt(length)
force	UReal		0.	added constant force [SI:N] of spring; scalar force; $f=1$ is equivalent to reducing initial- Length by 1/stiffness; $f > 0$ : tension; $f < 0$ : compression
activeConnector	bool		True	flag, which determines, if the connector is active; used to deactivate (temorarily) a connector or constraint
springForceUserFunction	PyFunctionScalar6		0	A python function which defines the spring force with parameters (time, deltaL, deltaL_t, Real stiffness, Real damping, Real springForce); the parameters are provided to the function using the current values of the SpringDamper object; The python function will only be evaluated, if activeConnector is true, otherwise the SpringDamper is inactive; Example for python function: def f(t, u, v, k, d, F0): return k*u + d*v + F0
visualization	VObjectConnectorS	pringl	Damper	parameters for visualization of item

The item VObjectConnectorSpringDamper has the following parameters:

,	1 0 1		01	
Name	type	size	default value	description
show	Bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = diameter of spring; size == -
				1.f means that default connector size is used
color	Float4		[-1.,-1.,-1.]	RGBA connector color; if R==-1, use default
				color

# Detailed information on ObjectConnectorSpringDamper: The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Distance		distance between both points
Displacement		relative displacement between both points
Velocity		relative velocity between both points
Force		spring-damper force

#### **Description of Item:**

#### Definition of quantities:

input parameter	symbol	description
referenceLength	$L_0$	
stiffness	k	
damping	d	
force	$f_a$	additional force (e.g., actuator force)
markerNumbers[0]	m0	global marker number m0
markerNumbers[1]	<i>m</i> 1	global marker number m1

intermediate variables	symbol	description
marker m0 position	$^{0}\mathbf{p}_{m0}$	current global position which is provided
		by marker m0
marker m1 position	<sup>0</sup> <b>p</b> <sub>m1</sub>	
marker m0 velocity	<sup>0</sup> <b>v</b> <sub>m0</sub>	current global velocity which is provided
		by marker m0
marker m1 velocity	$^{0}\mathbf{v}_{m1}$	

output variables	symbol	formula
Distance	L	$ \Delta^0 \mathbf{p} $
Displacement	$\Delta^0 \mathbf{p}$	$^{0}\mathbf{p}_{m1} - ^{0}\mathbf{p}_{m0}$
Velocity	$\Delta^0 {f v}$	${}^{0}\mathbf{v}_{m1} - {}^{0}\mathbf{v}_{m0}$
Force	f	see below

**Connector equations**: The unit vector in force direction reads (raises SysError if L = 0),

$$\mathbf{v}_f = \frac{1}{L} \Delta^0 \mathbf{p} \tag{5.41}$$

If activeConnector = True, the scalar spring force is computed as

$$f_{SD} = k \cdot (L - L_0) + d \cdot \Delta^0 \mathbf{v}^{\mathrm{T}} \mathbf{v}_f + f_a$$
(5.42)

If the springForceUserFunction UF is defined, **f** instead becomes (*t* is current time)

$$f_{SD} = \mathrm{UF}(t, L - L_0, \Delta^0 \mathbf{v}^{\mathrm{T}} \mathbf{v}_f, k, d, f_a)$$

$$(5.43)$$

if activeConnector = False,  $f_{SD}$  is set to zero.: The vector of the spring force applied at both markers finally reads

$$\mathbf{f} = f_{SD}\mathbf{v}_f \tag{5.44}$$

**Example** for ObjectConnectorSpringDamper:

# 5.3.12 ObjectConnectorCartesianSpringDamper

An 3D spring-damper element acting accordingly in three (global) directions (x,y,z) which connects to position-based markers.

# Additional information for ObjectConnectorCartesianSpringDamper:

- The Object has the following types = Connector
- Requested marker type = Position
- Short name for Python = CartesianSpringDamper

The item  ${\bf ObjectConnectorCartesianSpringDamper}$  with type = 'ConnectorCartesianSpringDamper' has the following parameters:

Name	type	size	default value	description
name	String		"	connector's unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	list of markers used in connector
			INT]	
stiffness	Vector3D		[0.,0.,0.]	stiffness [SI:N/m] of springs; act against rel-
				ative displacements in 0, 1, and 2-direction
damping	Vector3D		[0.,0.,0.]	damping [SI:N/(m s)] of dampers; act
				against relative velocities in 0, 1, and 2-
				direction
offset	Vector3D		[0.,0.,0.]	offset between two springs
springForceUserFunction	PyFunctionVector3	DScala	r5Vector3D	A python function which computes the
			0	3D force vector between the two marker
				points, if activeConnector=True; The func-
				tion takes the relative displacement (3D)
				vector (m1.position-m0.position, etc.) and
				the relative velocity vector (3D), the spring
				striffness vector 3D, damping and offset pa-
				rameter vectors (3D): f(time, displacement,
				velocity, stiffness, damping, offset); Exam-
				ple for python function: def f(t, u, v, k, d, off-
				set): return [u[0]*k[0],u[1]*k[1],u[2]*k[2]]
activeConnector	bool		True	flag, which determines, if the connector
				is active; used to deactivate (temorarily) a
				connector or constraint
visualization	VObjectConnectorO	Cartesia	anSpringDamper	parameters for visualization of item

The item VObjectConnectorCartesianSpringDamper has the following parameters:

Name	type	size	default value	description
show	Bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = diameter of spring; size == -
				1.f means that default connector size is used
color	Float4		[-1.,-1.,-1.]	RGBA connector color; if R==-1, use default
				color

#### Detailed information on ObjectConnectorCartesianSpringDamper:

input parameter	symbol	description see tables above
markerNumbers	$[m0, m1]^{T}$	
stiffness	k	
damping	d	
offset	V <sub>off</sub>	

#### The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Displacement	$\Delta^0 \mathbf{p} = {}^0 \mathbf{p}_{m1} - {}^0 \mathbf{p}_{m0}$	relative displacement in global coordinates
Distance	$L =  \Delta^0 \mathbf{p} $	scalar distance between both marker points
Velocity	$\Delta^0 \mathbf{v} = {}^0 \mathbf{v}_{m1} - {}^0 \mathbf{v}_{m0}$	relative translational velocity in global co-
		ordinates
Force	$\mathbf{f}_{SD}$	joint force in global coordinates, see equa-
		tions

# **Description of Item:**

#### Definition of quantities:

intermediate variables	symbol	description
marker m0 position	$^{0}$ <b>p</b> $_{m0}$	current global position which is provided
		by marker m0
marker m1 position	$^{0}$ p $_{m1}$	
marker m0 velocity	$^{0}\mathbf{v}_{m0}$	current global velocity which is provided
		by marker m0
marker m1 velocity	$^{0}\mathbf{v}_{m1}$	

Connector equations: Displacement between marker m0 to marker m1 positions,

$$\Delta^{0} \mathbf{p} = {}^{0} \mathbf{p}_{m1} - {}^{0} \mathbf{p}_{m0} \tag{5.45}$$

and relative velocity,

$$\Delta^0 \mathbf{v} = {}^0 \mathbf{v}_{m1} - {}^0 \mathbf{v}_{m0} \tag{5.46}$$

If activeConnector = True, the spring force vector is computed as

$$\mathbf{f}_{SD} = \left(\mathbf{k} \cdot (\Delta^0 \mathbf{p} - \mathbf{v}_{\text{off}}) + \mathbf{d}\Delta^0 \mathbf{v}\right)$$
 (5.47)

If the springForceUserFunction UF is defined,  $f_{SD}$  instead becomes (t is current time)

$$\mathbf{f}_{SD} = \mathrm{UF}(t, \Delta^0 \mathbf{p}, \Delta^0 \mathbf{v}, \mathbf{k}, \mathbf{d}, \mathbf{v}_{\mathrm{off}})$$
 (5.48)

if activeConnector = False,  $f_{SD}$  is set to zero. **Example** for ObjectConnectorCartesianSpringDamper:

```
#example with mass at [1,1,0], 5kg under load 5N in -y direction
k=5000
nMass = mbs.AddNode(NodePoint(referenceCoordinates=[1,1,0]))
oMass = mbs.AddObject(MassPoint(physicsMass = 5, nodeNumber = nMass))
mMass = mbs.AddMarker(MarkerNodePosition(nodeNumber=nMass))
```

# 5.3.13 ObjectConnectorRigidBodySpringDamper

An 3D spring-damper element acting on relative displacements and relative rotations of two rigid body (position+orientation) markers; connects to (position+orientation)-based markers and represents a penalty-based rigid joint (or prismatic, revolute, etc.)

#### Additional information for ObjectConnectorRigidBodySpringDamper:

- The Object has the following types = Connector
- Requested marker type = Position + Orientation
- **Short name** for Python = **RigidBodySpringDamper**

The item **ObjectConnectorRigidBodySpringDamper** with type = 'ConnectorRigidBodySpringDamper' has the following parameters:

Name	type	size	default value	description
name	String		"	connector's unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-INT ]	list of markers used in connector
stiffness	Matrix6D		np.zeros([6,6])	stiffness [SI:N/m or Nm/rad] of translational, torsional and coupled springs; act against relative displacements in x, y, and z-direction as well as the relative angles (calculated as Euler angles); in the simplest case, the first 3 diagonal values correspond to the local stiffness in x,y,z direction and the last 3 diagonal values correspond to the rotational stiffness around x,y and z axis
damping	Matrix6D		np.zeros([6,6])	damping [SI:N/(m/s) or Nm/(rad/s)] of translational, torsional and coupled dampers; very similar to stiffness, however, the rotational velocity is computed from the angular velocity vector
rotationMarker()	Matrix3D		[[1,0,0], [0,1,0], [0,0,1]]	local rotation matrix for marker 0; stiff- ness, damping, etc. components are mea- sured in local coordinates relative to rota- tionMarker0
rotationMarker1	Matrix3D		[[1,0,0], [0,1,0], [0,0,1]]	local rotation matrix for marker 1; stiff- ness, damping, etc. components are mea- sured in local coordinates relative to rota- tionMarker1
offset	Vector6D		[0.,0.,0.,0.,0.]	translational and rotational offset considered in the spring force calculation
activeConnector	bool		True	flag, which determines, if the connector is active; used to deactivate (temorarily) a connector or constraint
visualization	VObjectConnect	torRigidB	dySpringDamper	parameters for visualization of item

 $The\ item\ VObject Connector Rigid Body Spring Damper\ has\ the\ following\ parameters:$ 

Name	type	size	default value	description
show	Bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = diameter of spring; size == -
				1.f means that default connector size is used
color	Float4		[-1.,-1.,-1.]	RGBA connector color; if R==-1, use default
				color

# Detailed information on ObjectConnectorRigidBodySpringDamper: The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
DisplacementLocal	$^{J0}\Delta\mathbf{p}$	relative displacement in local joint0 coordi-
		nates
VelocityLocal	$^{J0}\Delta {f v}$	relative translational velocity in local joint0
		coordinates
Rotation	$J^0 \boldsymbol{\theta} = [\theta_0, \theta_1, \theta_2]^{\mathrm{T}}$	relative rotation parameters (Tait Bryan
		Rxyz); these are the angles used for calcula-
		tion of joint torques (e.g. if cX is the diago-
		nal rotational stiffness, the moment for axis
		X reads mX=cX*phiX, etc.)
AngularVelocityLocal	$^{J0}\Delta\omega$	relative angular velocity in local joint0 co-
		ordinates
ForceLocal	<sup>J0</sup> <b>f</b>	joint force in local joint0 coordinates
TorqueLocal	<sup>J0</sup> <b>m</b>	joint torque in in local joint0 coordinates

# Description of Item:

# **Definition of quantities:**

input parameter	symbol	description
stiffness	$\mathbf{k} \in \mathbb{R}^{6 \times 6}$	stiffness in J0 coordinates
damping	$\mathbf{d} \in \mathbb{R}^{6 \times 6}$	damping in J0 coordinates
offset	$J^0\mathbf{v}_{\mathrm{off}} \in \mathbb{R}^6$	offset in J0 coordinates
rotationMarker0	$^{m0,J0}\mathbf{A}$	rotation matrix which transforms from joint
		0 into marker 0 coordinates
rotationMarker1	$^{m1,J1}\mathbf{A}$	rotation matrix which transforms from joint
		1 into marker 1 coordinates
markerNumbers[0]	<i>m</i> 0	global marker number m0
markerNumbers[1]	m1	global marker number m1

intermediate variables	symbol	description
marker m0 position	$^{0}\mathbf{p}_{m0}$	current global position which is provided
		by marker m0
marker m0 orientation	$^{0,m0}\mathbf{A}$	current rotation matrix provided by marker
		m0
marker m1 position	<sup>0</sup> <b>p</b> <sub>m1</sub>	accordingly
marker m1 orientation	$^{0,m1}\mathbf{A}$	current rotation matrix provided by marker
		m1

marker m0 velocity	$^{0}\mathbf{v}_{m0}$	current global velocity which is provided
		by marker m0
marker m1 velocity	$^{0}\mathbf{v}_{m1}$	accordingly
marker m0 velocity	$^{b}\omega_{m0}$	current local angular velocity vector pro-
		vided by marker m0
marker m1 velocity	$^{b}\omega_{m1}$	current local angular velocity vector pro-
		vided by marker m1
Displacement	$^{0}\Delta\mathbf{p}$	${}^{0}\mathbf{p}_{m1} - {}^{0}\mathbf{p}_{m0}$
Velocity	$^{0}\Delta\mathbf{v}$	${}^{0}\mathbf{v}_{m1} - {}^{0}\mathbf{v}_{m0}$
DisplacementLocal	$^{J0}\Delta\mathbf{p}$	$\left({}^{0,m0}\mathbf{A}\right.^{m0,f0}\mathbf{A}\left.\right)^{\mathrm{T}}{}^{0}\Delta\mathbf{p}$
VelocityLocal	$^{J0}\Delta {f v}$	$\left(^{0,m0}\mathbf{A}\right.^{m0,f0}\mathbf{A}\left)^{\mathrm{T}}{}^{0}\Delta\mathbf{v}$
AngularVelocityLocal	$^{J0}\Delta\omega$	$\left( {^{0,m0}}\mathbf{A}^{\ m0,l0}\mathbf{A} \right)^{\mathrm{T}} \left( {^{0,m1}}\mathbf{A}^{\ m1}\boldsymbol{\omega} - {^{0,m0}}\mathbf{A}^{\ m0}\boldsymbol{\omega} \right)$

**Connector equations**: If activeConnector = True, the vector spring force is computed as

$$\begin{bmatrix} {}^{J0}\mathbf{f}_{SD} \\ {}^{J0}\mathbf{m}_{SD} \end{bmatrix} = \mathbf{k} \left( \begin{bmatrix} {}^{J0}\Delta\mathbf{p} \\ {}^{J0}\boldsymbol{\theta} \end{bmatrix} - {}^{J0}\mathbf{v}_{off} \right) + \mathbf{d} \begin{bmatrix} {}^{J0}\Delta\mathbf{v} \\ {}^{J0}\Delta\omega \end{bmatrix}$$
(5.49)

For the application of joint forces to markers,  $[^{J0}\mathbf{f}_{SD}, ^{J0}\mathbf{m}_{SD}]^{T}$  is transformed into global coordinates. if activeConnector = False,  $^{J0}\mathbf{f}_{SD}$  and  $^{J0}\mathbf{m}_{SD}$  are set to zero.

# 5.3.14 ObjectConnectorCoordinateSpringDamper

A 1D (scalar) spring-damper element acting on single ODE2 coordinates; connects to coordinate-based markers; NOTE that the coordinate markers only measure the coordinate (=displacement), but the reference position is not included as compared to position-based markers!; the spring-damper can also act on rotational coordinates.

### Additional information for ObjectConnectorCoordinateSpringDamper:

- The Object has the following types = Connector
- Requested marker type = Coordinate
- **Short name** for Python = **CoordinateSpringDamper**

The item **ObjectConnectorCoordinateSpringDamper** with type = 'ConnectorCoordinateSpringDamper' has the following parameters:

Name	type	size	default value	description
name	String		"	connector's unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	list of markers used in connector
			INT]	
stiffness	Real		0.	stiffness [SI:N/m] of spring; acts against rel-
				ative value of coordinates
damping	Real		0.	damping [SI:N/(m s)] of damper; acts
				against relative velocity of coordinates
offset	Real		0.	offset between two coordinates (reference
				length of springs), see equation
dryFriction	Real		0.	dry friction force [SI:N] against relative ve-
				locity; assuming a normal force $f_N$ , the fric-
				tion force can be interpreted as $f_{\mu} = \mu f_N$
dryFrictionProportionalZone	Real		0.	limit velocity [m/s] up to which the friction
				is proportional to velocity (for regulariza-
				tion / avoid numerical oscillations)
activeConnector	bool		True	flag, which determines, if the connector
				is active; used to deactivate (temorarily) a
				connector or constraint
springForceUserFunction	PyFunctionScalar8		0	A python function which defines the spring
				force with 8 parameters, see equations sec-
				tion; Example for python function: def f(t,
				u, v, k, d, offset, frictionForce, frictionPro-
				portionalZone): return $k^*(u\text{-offset}) + d^*v$
visualization	VObjectConnector(	oordii	nateSpringDamper	parameters for visualization of item

The item VObjectConnectorCoordinateSpringDamper has the following parameters:

Name	type	size	default value	description
show	Bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = diameter of spring; size == -
				1.f means that default connector size is used
color	Float4		[-1.,-1.,-1.]	RGBA connector color; if R==-1, use default
				color

### Detailed information on ObjectConnectorCoordinateSpringDamper:

input parameter	symbol	description see tables above
stiffness	k	
damping	d	
offset	$l_{ m off}$	
dryFriction	$f_{\mu}$	
dryFrictionProportionalZone	$v_{\mu}$	

### The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Displacement	Δq	relative scalar displacement of marker co-
		ordinates
Velocity	$\Delta v$	difference of scalar marker velocity coordi-
		nates
Force	$f_{SD}$	scalar spring force

### **Description of Item:**

#### Definition of quantities:

intermediate variables	symbol	description
marker m0 coordinate	$q_{m0}$	current displacement coordinate which is
		provided by marker m0; does NOT include
		reference coordinate!
marker m1 coordinate	$q_{m1}$	
marker m0 velocity coordinate	$v_{m0}$	current velocity coordinate which is pro-
		vided by marker m0
marker m1 velocity coordinate	$v_{m1}$	

**Connector equations**: Displacement between marker m0 to marker m1 coordinates (does NOT include reference coordinates),

$$\Delta q = q_{m1} - q_{m0} \tag{5.50}$$

and relative velocity,

$$\Delta v = v_{m1} - v_{m0} \tag{5.51}$$

If  $f_{\mu}$  > 0, the friction force is computed as

$$f_{\text{friction}} = \begin{cases} \operatorname{Sgn}(\Delta v) \cdot f_{\mu} & \text{if} \quad |\Delta v| \ge v_{\mu} \\ \frac{\Delta v}{v_{\mu}} f_{\mu} & \text{if} \quad |\Delta v| < v_{\mu} \end{cases}$$
 (5.52)

If activeConnector = True, the scalar spring force vector is computed as

$$f_{SD} = k(\Delta q - l_{\text{off}}) + d \cdot \Delta v + f_{\text{friction}}$$
(5.53)

If the springForceUserFunction UF is defined,  $f_{SD}$  instead becomes (t is current time)

$$f_{SD} = \text{UF}(t, \Delta q, \Delta v, k, d, l_{\text{off}}, f_{\mu}, v_{\mu})$$
(5.54)

 $if \ {\tt activeConnector} \ = \ {\tt False}, f_{SD} \ is \ {\tt set} \ to \ {\tt zero}. \ {\tt Example} \ for \ ObjectConnectorCoordinateSpringDamper:$ 

```
def springForce(t, u, v, k, d, offset, frictionForce, frictionProportionalZone):
    return 0.1*k*u+k*u**3+v*d
nMass=mbs.AddNode(Point(referenceCoordinates = [2,0,0]))
massPoint = mbs.AddObject(MassPoint(physicsMass = 5, nodeNumber = nMass))
groundMarker=mbs.AddMarker(MarkerNodeCoordinate(nodeNumber= nGround, coordinate = 0))
nodeMarker =mbs.AddMarker(MarkerNodeCoordinate(nodeNumber= nMass, coordinate = 0))
#Spring-Damper between two marker coordinates
mbs.AddObject(CoordinateSpringDamper(markerNumbers = [groundMarker, nodeMarker],
                                     stiffness = 5000, damping = 80,
                                         springForceUserFunction = springForce))
loadCoord = mbs.AddLoad(LoadCoordinate(markerNumber = nodeMarker, load = 1)) #static
   linear solution:0.002
#assemble and solve system for default parameters
mbs.Assemble()
SC.TimeIntegrationSolve(mbs, 'GeneralizedAlpha', exu.SimulationSettings())
#check result at default integration time
testError = mbs.GetNodeOutput(nMass, exu.OutputVariableType.Displacement)[0] -
   0.0019995158325691875
```

### 5.3.15 ObjectConnectorDistance

Connector which enforces constant or prescribed distance between two bodies/nodes.

### Additional information for ObjectConnectorDistance:

- The Object has the following types = Connector, Constraint
- Requested marker type = Position
- **Short name** for Python = **DistanceConstraint**

The item **ObjectConnectorDistance** with type = 'ConnectorDistance' has the following parameters:

Name	type	size	default value	description
name	String		"	constraints's unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	list of markers used in connector
			INT]	
distance	UReal		0.	prescribed distance [SI:m] of the used mark-
				ers
activeConnector	bool		True	flag, which determines, if the connector
				is active; used to deactivate (temorarily) a
				connector or constraint
visualization	VObjectConnecto	orDistano	e	parameters for visualization of item

### The item VObjectConnectorDistance has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = link size; size == -1.f means
				that default connector size is used
color	Float4		[-1.,-1.,-1.]	RGBA connector color; if R==-1, use default
				color

### Detailed information on ObjectConnectorDistance:

input parameter	symbol	description see tables above
markerNumbers	$[m0, m1]^{\mathrm{T}}$	
distance	$d_0$	

### The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Displacement	$^{0}\Delta p$	relative displacement in global coordinates
Velocity	$^{0}\Delta \mathbf{v}$	relative translational velocity in global co-
		ordinates
Distance	$   ^0 \Delta \mathbf{p}  $	distance between markers (should stay con-
		stant; shows constraint deviation)
Force	$\lambda_0$	joint force in global coordinates

### **Description of Item: Definition of quantities:**

intermediate variables	symbol	description
marker m0 position	$^{0}\mathbf{p}_{m0}$	current global position which is provided
		by marker m0
marker m1 position	$^{0}$ <b>p</b> $_{m1}$	accordingly
marker m0 velocity	0 <b>v</b> m0	current global velocity which is provided
		by marker m0
marker m1 velocity	$^{0}\mathbf{v}_{m1}$	accordingly
relative displacement	$^{0}\Delta \mathbf{p}$	$^{0}\mathbf{p}_{m1} - ^{0}\mathbf{p}_{m0}$
relative velocity	$^0\Delta {f v}$	${}^{0}\mathbf{v}_{m1} - {}^{0}\mathbf{v}_{m0}$
algebraicVariable	$\lambda_0$	Lagrange multiplier = force in constraint

Algebraic constraint equations: If activeConnector = True, the index 3 algebraic equation reads

$$\left| {}^{0}\Delta \mathbf{p} \right| - d_0 = 0 \tag{5.55}$$

The index 2 (velocity level) algebraic equation reads

$$\left(\frac{{}^{0}\Delta\mathbf{p}}{\left|{}^{0}\Delta\mathbf{p}\right|}\right)^{T}\Delta\mathbf{v} = 0$$
(5.56)

if activeConnector = False, the algebraic equation reads

$$\lambda_0 = 0 \tag{5.57}$$

#### **Example** for ObjectConnectorDistance:

```
#example with 1m pendulum, 50kg under gravity
nMass = mbs.AddNode(NodePoint2D(referenceCoordinates=[1,0]))
oMass = mbs.AddObject(MassPoint2D(physicsMass = 50, nodeNumber = nMass))
mMass = mbs.AddMarker(MarkerNodePosition(nodeNumber=nMass))
mGround = mbs.AddMarker(MarkerBodyPosition(bodyNumber=oGround, localPosition =
   [0,0,0]))
oDistance = mbs.AddObject(DistanceConstraint(markerNumbers = [mGround, mMass],
   distance = 1))
mbs.AddLoad(Force(markerNumber = mMass, loadVector = [0, -50*9.81, 0]))
#assemble and solve system for default parameters
mbs.Assemble()
sims=exu.SimulationSettings()
sims.timeIntegration.generalizedAlpha.spectralRadius=0.7
SC. TimeIntegrationSolve(mbs, 'GeneralizedAlpha', sims)
#check result at default integration time
testError = mbs.GetNodeOutput(nMass, exu.OutputVariableType.Position)[0] -
   (-0.9845225086606828)
```

### 5.3.16 ObjectConnectorCoordinate

A coordinate constraint which constrains two (scalar) coordinates of Marker[Node|Body]Coordinates attached to nodes or bodies. The constraint acts directly on coordinates, but does not include reference values, e.g., of nodal values.

### Additional information for ObjectConnectorCoordinate:

- The Object has the following types = Connector, Constraint
- Requested marker type = Coordinate
- Short name for Python = CoordinateConstraint

### The item **ObjectConnectorCoordinate** with type = 'ConnectorCoordinate' has the following parameters:

Name	type	size	default value	description
name	String		"	constraints's unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX- INT ]	list of markers used in connector
offset	UReal		0.	An offset between the two values
factorValue1	UReal		1.	An additional factor multiplied with value1
				used in algebraic equation
velocityLevel	bool		False	If true: connector constrains velocities (only
				works for ODE2 coordinates!); offset is used
				between velocities; in this case, the off-
				setUserFunction_t is considered and offse-
			_	tUserFunction is ignored
offsetUserFunction	PyFunctionScalar2		0	A python function which defines the time-
				dependent offset; it is highly RECOM-
				MENDED to use sufficiently smooth func-
				tions, having consistent initial offsets with
				initial configuration of bodies, zero or
				compatible initial offset-velocity, and no
				accelerations; Example for python func-
				tion: def UF(t, l_offset): return l_offset*(1-
				np.cos(t*10*2*np.pi))
offsetUserFunction_t	PyFunctionScalar2		0	time derivative of offsetUserFunction;
				needed for 'velocityLevel=True', or for in-
				dex2 time integration and for computation
				of initial accelerations in SecondOrderIm-
				plicit integrators
activeConnector	bool		True	flag, which determines, if the connector
				is active; used to deactivate (temorarily) a
				connector or constraint
visualization	VObjectConnectorC	oordi	nate	parameters for visualization of item

### The item VObjectConnectorCoordinate has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

drawSize	float	-1.	drawing size = link size; size == -1.f means
			that default connector size is used
color	Float4	[-1.,-1.,-1.]	RGBA connector color; if R==-1, use default
			color

### Detailed information on ObjectConnectorCoordinate:

input parameter	symbol	description see tables above
markerNumbers	$[m0, m1]^{\mathrm{T}}$	
offset	$l_{ m off}$	
factorValue1	$k_{m1}$	
offsetUserFunction	$\mathrm{UF}(t,l_{\mathrm{off}})$	
offsetUserFunction_t	$\mathrm{UF}_t(t,l_{\mathrm{off}})$	

### The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Displacement	$\Delta q$	relative scalar displacement of marker co-
		ordinates, not including factorValue1
Velocity	$\Delta v$	difference of scalar marker velocity coordi-
		nates, not including factorValue1
ConstraintEquation	С	(residuum of) constraint equation
Force	$\lambda_0$	scalar constraint force (Lagrange multi-
		plier)

### Description of Item: Definition of quantities:

intermediate variables	symbol	description
marker m0 coordinate	$q_{m0}$	current displacement coordinate which is
		provided by marker m0; does NOT include
		reference coordinate!
marker m1 coordinate	$q_{m1}$	
marker m0 velocity coordinate	$v_{m0}$	current velocity coordinate which is pro-
		vided by marker m0
marker m1 velocity coordinate	$v_{m1}$	
difference of coordinates	$\Delta q = q_{m1} - q_{m0}$	Displacement between marker m0 to
		marker m1 coordinates (does NOT include
		reference coordinates)
difference of velocity coordinates	$\Delta v = v_{m1} - v_{m0}$	

**Algebraic constraint equations**: If activeConnector = True, the index 3 algebraic equation reads

$$\mathbf{c}(q_{m0}, q_{m1}) = k_{m1} \cdot q_{m1} - q_{m0} - l_{\text{off}} = 0$$
(5.58)

If the offsetUserFunction UF is defined, **c** instead becomes (*t* is current time)

$$\mathbf{c}(q_{m0}, q_{m1}) = k_{m1} \cdot q_{m1} - q_{m0} - \mathbf{UF}(t, l_{\text{off}}) = 0$$
(5.59)

The activeConnector = True, index 2 (velocity level) algebraic equation reads

$$\dot{\mathbf{c}}(\dot{q}_{m0}, \dot{q}_{m1}) = k_{m1} \cdot \dot{q}_{m1} - \dot{q}_{m0} - d = 0 \tag{5.60}$$

The factor d in velocity level equations is zero, or if parameters.velocityLevel = True,  $d = l_{\text{off}}$ . If velocity level constraints are active and the velocity level offsetUserFunction\_t UF<sub>t</sub> is defined,  $\dot{\mathbf{c}}$  instead becomes (t is current time)

$$\dot{\mathbf{c}}(\dot{q}_{m0}, \dot{q}_{m1}) = k_{m1} \cdot \dot{q}_{m1} - \dot{q}_{m0} - \mathbf{UF}_t(t, l_{\text{off}}) = 0 \tag{5.61}$$

Note that the index 2 equations are used, if the solver uses index 2 formulation OR if the flag parameters.velocityLevel = True (or both). The user functions include dependency on time t, but this time dependency is not respected in the computation of initial accelerations. Therefore, it is recommended that UF and UF $_t$  does not include initial accelerations.

If activeConnector = False, the (index 1) algebraic equation reads for ALL cases:

$$\mathbf{c}(\lambda_0) = \lambda_0 = 0 \tag{5.62}$$

#### **Example** for ObjectConnectorCoordinate:

### 5.3.17 ObjectContactCoordinate

A penalty-based contact condition for one coordinate; the contact gap g is defined as g = marker.value[1] - marker.value[0] - offset; the contact force  $f_c$  is zero for gap > 0 and otherwise computed from  $f_c = g * contactStiffness+\dot{g}*contactDamping$ ; during Newton iterations, the contact force is actived only, if dataCoordinate[0] <= 0; dataCoordinate is set equal to gap in nonlinear iterations, but not modified in Newton iterations.

### Additional information for ObjectContactCoordinate:

- The Object has the following types = Connector
- Requested marker type = Coordinate
- Requested node type = GenericData

### The item **ObjectContactCoordinate** with type = 'ContactCoordinate' has the following parameters:

Name	type	size	default value	description
name	String		"	connector's unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	markers define contact gap
			INT]	
nodeNumber	Index		MAXINT	node number of a NodeGenericData for 1
				dataCoordinate (used for active set strategy
				==> holds the gap of the last discontinuous
				iteration)
contactStiffness	UReal		0.	contact (penalty) stiffness [SI:N/m]; acts
				only upon penetration
contactDamping	UReal		0.	contact damping [SI:N/(m s)]; acts only
				upon penetration
offset	UReal		0.	offset [SI:m] of contact
activeConnector	bool		True	flag, which determines, if the connector
				is active; used to deactivate (temorarily) a
				connector or constraint
visualization	VObjectContactC	Coordinat	e	parameters for visualization of item

### The item VObjectContactCoordinate has the following parameters:

Name	type	size	default value	description
show	Bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = diameter of spring; size == -
				1.f means that default connector size is used
color	Float4		[-1.,-1.,-1.]	RGBA connector color; if R==-1, use default
				color

### 5.3.18 ObjectContactCircleCable2D

A very specialized penalty-based contact condition between a 2D circle (=marker0, any Position-marker) on a body and an ANCFCable2DShape (=marker1, Marker: BodyCable2DShape), in xy-plane; a node NodeGenericData is required with the number of cordinates according to the number of contact segments; the contact gap g is integrated (piecewise linear) along the cable and circle; the contact force  $f_c$  is zero for gap > 0 and otherwise computed from  $f_c = g * contactStiffness + <math>\dot{g} * contactDamping$ ; during Newton iterations, the contact force is actived only, if dataCoordinate[0] <= 0; dataCoordinate is set equal to gap in nonlinear iterations, but not modified in Newton iterations.

### Additional information for ObjectContactCircleCable2D:

- The Object has the following types = Connector
- Requested marker type = \_None
- Requested node type = GenericData

The item **ObjectContactCircleCable2D** with type = 'ContactCircleCable2D' has the following parameters:

Name	type	size	default value	description
name	String		"	connector's unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX- INT ]	markers define contact gap
nodeNumber	Index		MAXINT	node number of a NodeGenericData for nSegments dataCoordinates (used for ac- tive set strategy ==> hold the gap of the last discontinuous iteration and the friction state)
numberOfContactSegments	Index		3	number of linear contact segments to determine contact; each segment is a line and is associated to a data (history) variable; must be same as in according marker
contactStiffness	UReal		0.	contact (penalty) stiffness [SI:N/m/(contact segment)]; the stiffness is per length of the beam axis; specific contact forces (per length) $f_N$ act in contact normal direction only upon penetration
contactDamping	UReal		0.	contact damping [SI:N/(m s)/(contact segment)]; the damping is per length of the beam axis; acts in contact normal direction only upon penetration
circleRadius	UReal		0.	radius [SI:m] of contact circle
offset	UReal		0.	offset [SI:m] of contact, e.g. to include thickness of cable element
activeConnector	bool		True	flag, which determines, if the connector is active; used to deactivate (temorarily) a connector or constraint
visualization	VObjectContact	CircleCab	e2D	parameters for visualization of item

The item VObjectContactCircleCable2D has the following parameters:

Name	type	size	default value	description
show	Bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = diameter of spring; size == -
				1.f means that default connector size is used
color	Float4		[-1.,-1.,-1.]	RGBA connector color; if R==-1, use default
				color

### 5.3.19 ObjectContactFrictionCircleCable2D

A very specialized penalty-based contact/friction condition between a 2D circle in the local x/y plane (=marker0, a Rigid-Body Marker) on a body and an ANCFCable2DShape (=marker1, Marker: BodyCable2DShape), in xy-plane; a node NodeGenericData is required with  $3\times$ (number of contact segments) – containing per segment: [contact gap, stick/slip (stick=1), last friction position]; the contact gap g is integrated (piecewise linear) along the cable and circle; the contact force  $f_c$  is zero for gap > 0 and otherwise computed from  $f_c = g * contactStiffness + <math>\dot{g} * contactDamping$ ; during Newton iterations, the contact force is actived only, if dataCoordinate[0] <= 0; dataCoordinate is set equal to gap in nonlinear iterations, but not modified in Newton iterations.

### Additional information for ObjectContactFrictionCircleCable2D:

- The Object has the following types = Connector
- Requested marker type = \_None
- Requested node type = GenericData

The item **ObjectContactFrictionCircleCable2D** with type = 'ContactFrictionCircleCable2D' has the following parameters:

Name	type	size	default value	description
name	String		"	connector's unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX- INT ]	markers define contact gap
nodeNumber	Index		MAXINT	node number of a NodeGenericData with 3 × nSegments dataCoordinates (used for active set strategy ==> hold the gap of the last discontinuous iteration and the friction state)
numberOfContactSegments	Index		3	number of linear contact segments to determine contact; each segment is a line and is associated to a data (history) variable; must be same as in according marker
contactStiffness	UReal		0.	contact (penalty) stiffness [SI:N/m/(contact segment)]; the stiffness is per length of the beam axis; specific contact forces (per length) $f_N$ act in contact normal direction only upon penetration
contactDamping	UReal		0.	contact damping [SI:N/(m s)/(contact segment)]; the damping is per length of the beam axis; acts in contact normal direction only upon penetration
frictionVelocityPenalty	UReal		0.	velocity dependent penalty coefficient for friction [SI:N/(m s)/(contact segment)]; the coefficient causes tangential (contact) forces against relative tangential velocities in the contact area

frictionStiffness	UReal	0.	CURRENTLY NOT IMPLEMENTED: dis-
			placement dependent penalty/stiffness co-
			efficient for friction [SI:N/m/(contact seg-
			ment)]; the coefficient causes tangential
			(contact) forces against relative tangential
			displacements in the contact area
frictionCoefficient	UReal	0.	friction coefficient $\mu$ [SI: 1]; tangential spe-
			cific friction forces (per length) $f_T$ must ful-
			fill the condition $f_T \leq \mu f_N$
circleRadius	UReal	0.	radius [SI:m] of contact circle
offset	UReal	0.	offset [SI:m] of contact, e.g. to include thick-
			ness of cable element
activeConnector	bool	True	flag, which determines, if the connector
			is active; used to deactivate (temorarily) a
			connector or constraint
visualization	VObjectContactFricti	onCircleCable2D	parameters for visualization of item

# $The\ item\ VObject Contact Friction Circle Cable 2D\ has\ the\ following\ parameters:$

Name	type	size	default value	description
show	Bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = diameter of spring; size == -
				1.f means that default connector size is used
color	Float4		[-1.,-1.,-1.]	RGBA connector color; if R==-1, use default
				color

# 5.3.20 ObjectJointGeneric

A generic joint in 3D; constrains components of the absolute position and rotations of two points given by PointMarkers or RigidMarkers; an additional local rotation can be used to define three rotation axes and/or sliding axes

### Additional information for ObjectJointGeneric:

- The Object has the following types = Connector, Constraint
- Requested marker type = Position + Orientation
- **Short name** for Python = **GenericJoint**

The item **ObjectJointGeneric** with type = 'JointGeneric' has the following parameters:

Name	type	size	default value	description
name	String		"	constraints's unique name
markerNumbers	ArrayIndex	2	[ MAXINT, MAX-INT ]	list of markers used in connector
constrainedAxes	ArrayIndex	6	[1,1,1,1,1,1]	flag, which determines which translation $(0,1,2)$ and rotation $(3,4,5)$ axes are constrained; for $j_i$ , two values are possible: 0=free axis, 1=constrained axis
rotationMarker0	Matrix3D		[[1,0,0], [0,1,0], [0,0,1]]	local rotation matrix for marker <i>m</i> 0; translation and rotation axes for marker <i>m</i> 0 are defined in the local body coordinate system and additionally transformed by rotation-Marker0
rotationMarker1	Matrix3D		[[1,0,0], [0,1,0], [0,0,1]]	local rotation matrix for marker <i>m</i> 1; translation and rotation axes for marker <i>m</i> 1 are defined in the local body coordinate system and additionally transformed by rotation-Marker1
activeConnector	bool		True	flag, which determines, if the connector is active; used to deactivate (temorarily) a connector or constraint
offsetUserFunctionParameters	Vector6D		[0.,0.,0.,0.,0.]	vector of 6 parameters for joint's offsetUser- Function
offsetUserFunction	PyFunctionVector6	DScala	rVector6D 0	A python function which defines the time-dependent (fixed) offset of translation (indices 0,1,2) and rotation (indices 3,4,5) joint coordinates with parameters (t, offsetUserFunctionParameters); the offset represents the current value of the object; it is highly RECOMMENDED to use sufficiently smooth functions, having consistent initial offsets with initial configuration of bodies, zero or compatible initial offset-velocity, and no accelerations; Example for python function: def f(t, offsetUserFunctionParameters): return [offsetUserFunctionParameters[0]*(1-np.cos(t*10*2*np.pi)), 0,0,0,0,0]

offsetUserFunction_t	PyFunctionVector6l	DScala	rVector6D	(NOT IMPLEMENTED YET)time deriva-
			0	tive of offsetUserFunction using the
				same parameters; needed for 'veloc-
				ityLevel=True', or for index2 time integra-
				tion and for computation of initial acceler-
				ations in SecondOrderImplicit integrators
visualization	VObjectJointGeneri	С		parameters for visualization of item

# The item VObjectJointGeneric has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
axesRadius	float		0.1	radius of joint axes to draw
axesLength	float		0.4	length of joint axes to draw
color	Float4		[-1.,-1.,-1.]	RGBA connector color; if R==-1, use default
				color

# Detailed information on ObjectJointGeneric:

input parameter	symbol	description see tables above
markerNumbers	$[m0, m1]^{T}$	
constrainedAxes	$\mathbf{j} = [j_0, \ldots, j_5]$	
rotationMarker0	$^{m0,J0}\mathbf{A}$	
rotationMarker1	$^{m1,J1}\mathbf{A}$	
offsetUserFunctionParameters	Ppar	
offsetUserFunction	$UF(t, \mathbf{p}_{par})$	
offsetUserFunction_t	$UF_t(t, \mathbf{p}_{par})$	

# The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Position	$^{0}$ <b>p</b> $_{m0}$	current global position of position marker
		m0
Velocity	$^{0}\mathbf{v}_{m0}$	current global velocity of position marker
		<i>m</i> 0
DisplacementLocal	$^{J0}\Delta\mathbf{p}$	relative displacement in local joint0 coor-
		dinates; uses local J0 coordinates even for
		spherical joint configuration
VelocityLocal	$^{J0}\Delta {f v}$	relative translational velocity in local joint0
		coordinates
Rotation	$^{J0}\boldsymbol{\theta} = [\theta_0, \theta_1, \theta_2]^{\mathrm{T}}$	relative rotation parameters (Tait Bryan
		Rxyz); if all axes are fixed, this output rep-
		resents the rotational drift; for a revolute
		joint, it contains the rotation of this axis

AngularVelocityLocal	$^{J0}\Delta\omega$	relative angular velocity in local joint0 co-
		ordinates; if all axes are fixed, this output
		represents the angular velocity constraint
		error; for a revolute joint, it contains the
		angular velocity of this axis
ForceLocal	<sup>J0</sup> f	joint force in local J0 coordinates
TorqueLocal	<sup>J0</sup> <b>m</b>	joint torque in local J0 coordinates; depend-
		ing on joint configuration, the result may
		not be the according torque vector

# **Description of Item:**

# **Definition of quantities:**

intermediate variables	symbol	description
marker m0 position	<sup>0</sup> <b>p</b> <sub>m0</sub>	current global position which is provided
		by marker m0
marker m0 orientation	$^{0,m0}\mathbf{A}$	current rotation matrix provided by marker
		m0
joint J0 orientation	$^{0,J0}\mathbf{A} = ^{0,m0}\mathbf{A}^{m0,J0}\mathbf{A}$	joint J0 rotation matrix
joint J0 orientation vectors	$^{0,J0}\mathbf{A} = [\mathbf{v}_{x0},  \mathbf{v}_{y0},  \mathbf{v}_{z0}]^{\mathrm{T}}$	orientation vectors used for definition of
		constraint equations
marker m1 position	${}^{0}\mathbf{p}_{m1}$ ${}^{0,m1}\mathbf{A}$	accordingly
marker m1 orientation	$^{0,m1}\mathbf{A}$	current rotation matrix provided by marker
		m1
joint J1 orientation	$^{0,J1}\mathbf{A} = ^{0,m1}\mathbf{A}^{m1,J1}\mathbf{A}$	joint J1 rotation matrix
joint J1 orientation vectors	$^{0,J1}\mathbf{A} = [\mathbf{v}_{x1}, \mathbf{v}_{y1}, \mathbf{v}_{z1}]^{\mathrm{T}}$	orientation vectors used for definition of
		constraint equations
marker m0 velocity	$^{0}\mathbf{v}_{m0}$	current global velocity which is provided
		by marker m0
marker m1 velocity	$^{0}\mathbf{v}_{m1}$	accordingly
marker m0 velocity	$^{b}\omega_{m0}$	current local angular velocity vector pro-
		vided by marker m0
marker m1 velocity	$^{b}\omega_{m1}$	current local angular velocity vector pro-
		vided by marker m1
Displacement	${}^{0}\Delta\mathbf{p} = {}^{0}\mathbf{p}_{m1} - {}^{0}\mathbf{p}_{m0}$	used, if all translational axes are con-
		strained
Velocity	${}^{0}\Delta\mathbf{v} = {}^{0}\mathbf{v}_{m1} - {}^{0}\mathbf{v}_{m0}$	used, if all translational axes are con-
		strained (velocity level)
DisplacementLocal	$^{J0}\Delta\mathbf{p}$	
VelocityLocal	$^{J0}\Delta {f v}$	$(^{0,m0}\mathbf{A}^{m0,J0}\mathbf{A})^{\mathrm{T}}{}^{0}\Delta\mathbf{v}$ note that this is the
,		global relative velocity projected into the
		local J0 coordinate system
AngularVelocityLocal	$^{J0}\Delta\omega$	$({}^{0,m0}\mathbf{A} {}^{m0,0}\mathbf{A})^{\mathrm{T}}({}^{0,m1}\mathbf{A} {}^{m1}\omega - {}^{0,m0}\mathbf{A} {}^{m0}\omega)$
algebraic variables	$\mathbf{z} = [\lambda_0, \ldots, \lambda_5]^{\mathrm{T}}$	vector of algebraic variables (Lagrange
0	, , , , , , , ,	multipliers) according to the algebraic
		equations

# Connector equations for translational part (activeConnector = True):

If  $[j_0, \ldots, j_2] = [1, 1, 1]^T$ , meaning that all translational coordinates are fixed, the translational index 3 constraints

read ( $UF_{0,1,2}(t, \mathbf{p}_{par})$ ) is the translational part of the user function UF),

$${}^{0}\mathbf{p}_{m1} - {}^{0}\mathbf{p}_{m0} - UF_{0,1,2}(t, \mathbf{p}_{par}) = \mathbf{0}$$
 (5.63)

and the translational index 2 constraints read

$${}^{0}\mathbf{v}_{m1} - {}^{0}\mathbf{v}_{m0} - UF_{t:0,1,2}(t, \mathbf{p}_{nar}) = \mathbf{0}$$
(5.64)

If  $[j_0, ..., j_2] \neq [1,1,1]^T$ , meaning that at least one translational coordinate is free, the translational index 3 constraints read for every component  $k \in [0,1,2]$  of the vector  ${}^{J0}\Delta \mathbf{p}$ 

$$^{J0}\Delta p_k - UF_k(t, \mathbf{p}_{par}) = 0 \text{ if } j_k = 1 \text{ and}$$
 (5.65)

$$\lambda_k = 0 \quad \text{if} \quad j_k = 0 \tag{5.66}$$

(5.67)

and the translational index 2 constraints read for every component  $k \in [0, 1, 2]$  of the vector  ${}^{J0}\Delta \mathbf{v}$ 

$$^{J0}\Delta v_k - UF_{t;k}(t, \mathbf{p}_{par}) = 0 \text{ if } j_k = 1 \text{ and}$$
 (5.68)

$$\lambda_k = 0 \quad \text{if} \quad j_k = 0 \tag{5.69}$$

(5.70)

#### Connector equations for rotational part (activeConnector = True):

The following equations are exemplarily for certain constrained rotation axes configurations, which shall represent all other possibilities. Equations are only given for the index 3 case; the index 2 case can be derived from these equations easily (see C++ code...). In case of user functions, the additional rotation matrix  $^{J0,J0U}$ **A** ( $UF_{3,4,5}(t, \mathbf{p}_{par})$ ), in which the three components of  $UF_{3,4,5}$  are interpreted as Tait-Bryan angles that are added to the joint frame.

If **3 rotation axes are constrained**,  $[j_3, \ldots, j_5] = [1, 1, 1]^T$ , the index 3 constraint equations read

$$\mathbf{v}_{0}^{\mathsf{T}}\mathbf{v}_{\nu 1} = 0 \tag{5.71}$$

$$\mathbf{v}_{z0}^{\mathsf{T}}\mathbf{v}_{x1} = 0 \tag{5.72}$$

$$\mathbf{v}_{v0}^{\mathrm{T}}\mathbf{v}_{v1} = 0 \tag{5.73}$$

If **2 rotation axes are constrained**, e.g.,  $[j_3, ..., j_5] = [0, 1, 1]^T$ , the index 3 constraint equations read

$$\lambda_3 = 0 \tag{5.74}$$

$$\mathbf{v}_{v0}^{\mathsf{T}}\mathbf{v}_{v1} = 0 \tag{5.75}$$

$$\mathbf{v}_{x0}^{\mathrm{T}}\mathbf{v}_{z1} = 0 \tag{5.76}$$

If **1 rotation axis is constrained**, e.g.,  $[j_3, \ldots, j_5] = [1, 0, 0]^T$ , the index 3 constraint equations read

$$\mathbf{v}_{u0}^{\mathrm{T}}\mathbf{v}_{z1} = 0 \tag{5.77}$$

$$\lambda_4 = 0 \tag{5.78}$$

$$\lambda_5 = 0 \tag{5.79}$$

if activeConnector = False,

$$\mathbf{z} = \mathbf{0} \tag{5.80}$$

### 5.3.21 ObjectJointSpherical

A spherical joint, which constrains the relative translation between two position based markers.

### Additional information for ObjectJointSpherical:

- The Object has the following types = Connector, Constraint
- Requested marker type = Position
- **Short name** for Python = **SphericalJoint**

### The item **ObjectJointSpherical** with type = 'JointSpherical' has the following parameters:

Name	type	size	default value	description
name	String		"	constraints's unique name
markerNumbers	ArrayIndex	2	[ MAXINT, MAX-	list of markers used in connector
			INT ]	
constrainedAxes	ArrayIndex	3	[1,1,1]	flag, which determines which translation
				(0,1,2) and rotation (3,4,5) axes are con-
				strained; for $j_i$ , two values are possible:
				0=free axis, 1=constrained axis
activeConnector	bool		True	flag, which determines, if the connector
				is active; used to deactivate (temorarily) a
				connector or constraint
visualization	VObjectJointSpheri	cal		parameters for visualization of item

### The item VObjectJointSpherical has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
jointRadius	float		0.1	radius of joint to draw
color	Float4		[-1.,-1.,-1.]	RGBA connector color; if R==-1, use default
				color

### Detailed information on ObjectJointSpherical:

input parameter	symbol	description see tables above
markerNumbers	$[m0, m1]^{\mathrm{T}}$	
constrainedAxes	$\mathbf{j} = [j_0, \ldots, j_2]$	

### The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Position	<sup>0</sup> <b>p</b> <sub>m0</sub>	current global position of position marker
		<i>m</i> 0
Velocity	$^{0}\mathbf{v}_{m0}$	current global velocity of position marker
		<i>m</i> 0
Displacement	${}^{0}\Delta\mathbf{p} = {}^{0}\mathbf{p}_{m1} - {}^{0}\mathbf{p}_{m0}$	constraint drift or relative motion, if not all
		axes fixed
Force	<sup>0</sup> <b>f</b>	joint force in global coordinates

### **Description of Item:**

### Definition of quantities:

intermediate variables	symbol	description
marker m0 position	<sup>0</sup> <b>p</b> <sub>m0</sub>	current global position which is provided
		by marker m0
marker m1 position	$^{0}\mathbf{p}_{\ m1}$	current global position which is provided
		by marker m1
marker m0 velocity	$^{0}\mathbf{v}_{m0}$	current global velocity which is provided
		by marker m0
marker m1 velocity	$^{0}\mathbf{v}_{m1}$	current global velocity which is provided
		by marker m1
relative velocity	${}^{0}\Delta\mathbf{v} = {}^{0}\mathbf{v}_{m1} - {}^{0}\mathbf{v}_{m0}$	constraint velocity error, or relative velocity
		if not all axes fixed
algebraic variables	$\mathbf{z} = [\lambda_0, \ldots, \lambda_2]^{\mathrm{T}}$	vector of algebraic variables (Lagrange
		multipliers) according to the algebraic
		equations

#### Connector equations (activeConnector = True):

If  $[j_0, ..., j_2] = [1, 1, 1]^T$ , meaning that all translational coordinates are fixed, the translational index 3 constraints read

$${}^{0}\mathbf{p}_{m1} - {}^{0}\mathbf{p}_{m0} = \mathbf{0} \tag{5.81}$$

and the translational index 2 constraints read

$${}^{0}\mathbf{v}_{m1} - {}^{0}\mathbf{v}_{m0} = \mathbf{0} \tag{5.82}$$

If  $[j_0, ..., j_2] \neq [1, 1, 1]^T$ , meaning that at least one translational coordinate is free, the translational index 3 constraints read for every component  $k \in [0, 1, 2]$  of the vector  ${}^0\Delta \mathbf{p}$ 

$${}^{0}\Delta p_{k} = 0 \text{ if } j_{k} = 1 \text{ and}$$
 (5.83)

$$\lambda_k = 0 \quad \text{if} \quad j_k = 0 \tag{5.84}$$

(5.85)

and the translational index 2 constraints read for every component  $k \in [0, 1, 2]$  of the vector  ${}^{0}\Delta \mathbf{v}$ 

$${}^{0}\Delta v_{k} = 0 \quad \text{if} \quad j_{k} = 1 \quad \text{and}$$
 (5.86)

$$\lambda_k = 0 \quad \text{if} \quad j_k = 0 \tag{5.87}$$

(5.88)

if activeConnector = False,

$$\mathbf{z} = \mathbf{0} \tag{5.89}$$

# 5.3.22 ObjectJointRevolute2D

 $A \ revolute \ joint \ in \ 2D; constrains \ the \ absolute \ 2D \ position \ of \ two \ points \ given \ by \ PointMarkers \ or \ RigidMarkers$ 

### Additional information for ObjectJointRevolute2D:

- The Object has the following types = Connector, Constraint
- Requested marker type = Position
- **Short name** for Python = **RevoluteJoint2D**

The item **ObjectJointRevolute2D** with type = 'JointRevolute2D' has the following parameters:

Name	type	size	default value	description
name	String		"	constraints's unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	list of markers used in connector
			INT]	
activeConnector	bool		True	flag, which determines, if the connector
				is active; used to deactivate (temorarily) a
				connector or constraint
visualization	VObjectJointRevolu	ıte2D		parameters for visualization of item

The item VObjectJointRevolute2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = radius of revolute joint; size
				== -1.f means that default connector size is
				used
color	Float4		[-1.,-1.,-1.]	RGBA connector color; if R==-1, use default
				color

### 5.3.23 ObjectJointPrismatic2D

A prismatic joint in 2D; allows the relative motion of two bodies, using two RigidMarkers; the vector  $\mathbf{t}_0$  = axisMarker0 is given in local coordinates of the first marker's (body) frame and defines the prismatic axis; the vector  $\mathbf{n}_1$  = normalMarker1 is given in the second marker's (body) frame and is the normal vector to the prismatic axis; using the global position vector  $\mathbf{p}_0$  and rotation matrix  $\mathbf{A}_0$  of marker0 and the global position vector  $\mathbf{p}_1$  rotation matrix  $\mathbf{A}_1$  of marker1, the equations for the prismatic joint follow as

$$(\mathbf{p}_1 - \mathbf{p}_0)^T \cdot \mathbf{A}_1 \cdot \mathbf{n}_1 = 0 \tag{5.90}$$

$$(\mathbf{A}_0 \cdot \mathbf{t}_0)^T \cdot \mathbf{A}_1 \cdot \mathbf{n}_1 = 0 \tag{5.91}$$

The lagrange multipliers follow for these two equations  $[\lambda_0, \lambda_1]$ , in which  $\lambda_0$  is the transverse force and  $\lambda_1$  is the torque in the joint.

### Additional information for ObjectJointPrismatic2D:

- The Object has the following types = Connector, Constraint
- Requested marker type = Position + Orientation
- **Short name** for Python = **PrismaticJoint2D**

The item ObjectJointPrismatic2D with type = 'JointPrismatic2D' has the following parameters:

Name	type	size	default value	description
name	String		"	constraints's unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	list of markers used in connector
			INT]	
axisMarker0	Vector3D		[1.,0.,0.]	direction of prismatic axis, given as a 3D
				vector in Marker0 frame
normalMarker1	Vector3D		[0.,1.,0.]	direction of normal to prismatic axis, given
				as a 3D vector in Marker1 frame
constrainRotation	bool		True	flag, which determines, if the connector also
				constrains the relative rotation of the two
				objects; if set to false, the constraint will
				keep an algebraic equation set equal zero
activeConnector	bool		True	flag, which determines, if the connector
				is active; used to deactivate (temorarily) a
				connector or constraint
visualization	VObjectJointPrism	atic2D		parameters for visualization of item

The item VObjectJointPrismatic2D has the following parameters:

, ,		01		
Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization and false if it is not shown
drawSize	float		-1.	drawing size = radius of revolute joint; size == -1.f means that default connector size is used
color	Float4		[-1.,-1.,-1.]	RGBA connector color; if R==-1, use default color

### 5.3.24 ObjectJointSliding2D

A specialized sliding joint (without rotation) in 2D between a Cable2D (marker1) and a position-based marker (marker0); the data coordinate x[0] provides the current index in slidingMarkerNumbers, and x[1] the local position in the cable element at the beginning of the timestep.

### Additional information for ObjectJointSliding2D:

- The Object has the following types = Connector, Constraint
- Requested marker type = \_None
- Requested node type = GenericData
- **Short name** for Python = **SlidingJoint2D**

The item **ObjectJointSliding2D** with type = 'JointSliding2D' has the following parameters:

Name	type	size	default value	description
name	String		"	constraints's unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-INT ]	marker m0: position-marker of mass point or rigid body; marker m1: updated marker to Cable2D element, where the sliding joint currently is attached to; must be initialized with an appropriate (global) marker number according to the starting position of the sliding object; this marker changes
slidingMarkerNumbers	ArrayIndex			with time (PostNewtonStep)  these markers are used to update marker m1, if the sliding position exceeds the current cable's range; the markers must be sorted such that marker $m_{si}$ at x=cable(i).length is equal to marker(i+1) at x=0 of cable(i+1)
slidingMarkerOffsets	Vector			this list contains the offsets of every sliding object (given by slidingMarker-Numbers) w.r.t. to the initial position (0): marker m0: offset=0, marker m1: offset=Length(cable0), marker m2: offset=Length(cable0)+Length(cable1),
nodeNumber	Index		MAXINT	node number of a NodeGenericData for 1 dataCoordinate showing the according marker number which is currently active and the start-of-step (global) sliding posi- tion
classicalFormulation	bool		True	uses a formulation with 3 equations, including the force in sliding direction to be zero; forces in global coordinates, only index 3; alternatively: use local formulation, which only needs two equations and can be used with index 2 formulation
activeConnector	bool		True	flag, which determines, if the connector is active; used to deactivate (temorarily) a connector or constraint
visualization	VObjectJointSlid	ling2D		parameters for visualization of item

# The item VObjectJointSliding2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = radius of revolute joint; size
				== -1.f means that default connector size is
				used
color	Float4		[-1.,-1.,-1.]	RGBA connector color; if R==-1, use default
				color

# Detailed information on ObjectJointSliding2D:

input parameter	symbol	description see tables above
markerNumbers	$[m0, m1]^{\mathrm{T}}$	
slidingMarkerNumbers	$[m_{s0},\ldots,m_{sn}]^{\mathrm{T}}$	
slidingMarkerOffsets	$[d_{s0},\ldots,d_{sn}]$	
nodeNumber	$n_{GD}$	

# The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Position		position vector of joint given by marker0
Velocity		velocity vector of joint given by marker0
SlidingCoordinate		global sliding coordinate along all ele-
		ments; the maximum sliding coordinate is
		equivalent to the reference lengths of all
		sliding elements
Force		joint force vector (3D)

### **Description of Item:**

### **Definition of quantities:**

intermediate variables	symbol	description
data node	$\mathbf{x} = [x_{data0}, x_{data1}]^{\mathrm{T}}$	coordinates of node with node number $n_{GD}$
data coordinate 0	$x_{data0}$	the current index in slidingMarkerNum-
		bers
data coordinate 1	$x_{data1}$	the global sliding coordinate (ranging from
		0 to the total length of all sliding elements)
		at <b>start-of-step</b> - beginning of the timestep
marker m0 position	$^{0}$ <b>p</b> $_{m0}$	current global position which is provided
		by marker m0
marker m0 velocity	$^{0}\mathbf{v}_{m0}$	current global velocity which is provided
		by marker m0
cable coordinates	<b>q</b> ANCF,m1	current coordiantes of the ANCF cable el-
		ement with the current marker <i>m</i> 1 is refer-
		ring to
sliding position	$^{0}\mathbf{r}_{ANCF} = \mathbf{S}(s_{el})\mathbf{q}_{ANCF,m1}$	current global position at the ANCF cable
		element, evaluated at local sliding position
		$s_{el}$

sliding position slope	${}^{0}\mathbf{r}'_{ANCF} = \mathbf{S}'(s_{el})\mathbf{q}_{ANCF,m1} = [r'_{0}, r'_{1}]^{\mathrm{T}}$	current global slope vector of the ANCF ca-
		ble element, evaluated at local sliding posi-
		tion $s_{el}$
sliding velocity	${}^{0}\mathbf{v}_{ANCF} = \mathbf{S}(s_{el})\dot{\mathbf{q}}_{ANCF,m1}$	current global velocity at the ANCF cable
		element, evaluated at local sliding position
		$s_{el}$ ( $s_{el}$ not differentiated!!!)
sliding velocity slope	${}^{0}\mathbf{v}'_{ANCF} = \mathbf{S}'(s_{el})\dot{\mathbf{q}}_{ANCF,m1}$	current global slope velocity vector of the
		ANCF cable element, evaluated at local
		sliding position $s_{el}$
sliding normal vector	$^{0}\mathbf{n}=[-r_{1}^{\prime},r_{0}^{\prime}]$	2D normal vector computed from slope $\mathbf{r}' =$
		<sup>0</sup> r' <sub>ANCF</sub>
sliding normal velocity vector	${}^{0}\dot{\mathbf{n}} = [-\dot{r}'_{1},  \dot{r}'_{0}]$	time derivative of 2D normal vector com-
		puted from slope velocity $\dot{\mathbf{r}}' = {}^{0}\dot{\mathbf{r}}'_{ANCF}$
algebraic coordinates	$\mathbf{z} = [\lambda_0,  \lambda_1,  s]^{\mathrm{T}}$	algebraic coordinates composed of La-
		grange multipliers $\lambda_0$ and $\lambda_1$ (in local cable
		coordinates: $\lambda_0$ is in axis direction) and the
		current sliding coordinate s, which is local
		in the current cable element.
local sliding coordinate	s	local incremental sliding coordinate s: the
		(algebraic) sliding coordinate relative to the
		<b>start-of-step value</b> . Thus, <i>s</i> only contains
		small local increments.

output variables	symbol	formula
Position	<sup>0</sup> <b>p</b> <sub>m0</sub>	current global position of position marker
		m0
Velocity	<sup>0</sup> <b>v</b> <sub>m0</sub>	current global velocity of position marker
		m0
SlidingCoordinate	$s_g = s + x_{data1}$	current value of the global sliding coordi-
		nate
Force	f	see below

Assume we have given the sliding coordinate s (e.g., as a guess of the Newton method or beginning of the time step). The element sliding coordinate (in the local coordinates of the current sliding element) is computed as

$$s_{el} = s + x_{data1} - d_{m1} = s_g - d_{m1}. (5.92)$$

The vector (=difference; error) between the marker m0 and the marker m1 (= $\mathbf{r}_{ANCF}$ ) positions reads

$${}^{0}\Delta \mathbf{p} = {}^{0}\mathbf{r}_{ANCF} - {}^{0}\mathbf{p}_{m0} \tag{5.93}$$

The vector (=difference; error) between the marker m0 and the marker m1 velocities reads

$${}^{0}\Delta \mathbf{v} = {}^{0}\dot{\mathbf{r}}_{ANCF} - {}^{0}\mathbf{v}_{m0} \tag{5.94}$$

**Algebraic constraint equations (classicalFormulation=True)**: The 2D sliding joint is implemented having 3 equations, using the special algebraic coordinates **z**. The algebraic equations read

$$^{0}\Delta p = 0$$
, ... 2 index 3 equations, ensuring the sliding body to stay at the cable (5.95)

$$[\lambda_0, \lambda_1] \cdot {}^0\mathbf{r}'_{ANCF} = 0$$
, ... 1 index 1 equation, ensuring the force in sliding direction = 0 (5.96)

(5.97)

No index 2 case exists, because no time derivative exists for  $s_{el}$ . The jacobian matrices for algebraic and ODE2 coordinates read

$$J_{AE} = \begin{bmatrix} 0 & 0 & r'_0 \\ 0 & 0 & r'_1 \\ r'_0 & r'_1 & r''_0 \lambda_0 + r''_1 \lambda_1 \end{bmatrix}$$
 (5.98)

$$J_{ODE2} = \begin{bmatrix} -J_{pos,m0} & \mathbf{S}(s_{el}) \\ \mathbf{0}^{\mathrm{T}} & [\lambda_0, \lambda_1] \cdot \mathbf{S}'(s_{el}) \end{bmatrix}$$
(5.99)

if activeConnector = False, the algebraic equations are changed to:

$$\lambda_0 = 0, \tag{5.100}$$

$$\lambda_1 = 0, \tag{5.101}$$

$$s = 0 ag{5.102}$$

**Algebraic constraint equations (classicalFormulation=False)**: The 2D sliding joint is implemented having 3 equations (first equation is dummy and could be eliminated), using the special algebraic coordinates **z**. The algebraic equations read

 $\lambda_0 = 0$ , ... this equation is not necessary, but can be used for switching to other mod (5.103)  $^0\Delta \mathbf{p}^{\mathrm{T}} {}^0\mathbf{n} = 0$ , ... equation ensures that sliding body stays at cable centerline; index3 equati (5.104)  $^0\Delta \mathbf{p}^{\mathrm{T}} {}^0\mathbf{r}'_{ANCF} = 0$ . ... resolves the sliding coordinate s; index1 equation! (5.105)

In the index 2 case, the second equation reads

$${}^{0}\Delta\mathbf{v}^{\mathsf{T}}\,{}^{0}\mathbf{n}\,+{}^{0}\Delta\mathbf{p}^{\mathsf{T}}\,{}^{0}\dot{\mathbf{n}}\,=0\tag{5.106}$$

if activeConnector = False, the algebraic equations are changed to:

$$\lambda_0 = 0, \tag{5.107}$$

$$\lambda_1 = 0, \tag{5.108}$$

$$s = 0 ag{5.109}$$

**Post Newton Step**: After the Newton solver has converged, a PostNewtonStep is performed for the element, which updates the marker *m*1 index if necessary.

$$s_{el} < 0 \rightarrow x_{data0} = 1$$
  
 $s_{el} > L \rightarrow x_{data0} + 1$  (5.110)

Furthermore, it is checked, if  $x_{data0}$  becomes smaller than zero, which raises a warning and keeps  $x_{data0} = 0$ . The same results if  $x_{data0} \ge sn$ , then  $x_{data0} = sn$ . Finally, the data coordinate is updated in order to provide the starting value for the next step,

$$\chi_{data1} += s. \tag{5.111}$$

Examples: see TestModels!

### 5.3.25 ObjectJointALEMoving2D

A specialized axially moving joint (without rotation) in 2D between a ALE Cable2D (marker1) and a position-based marker (marker0); ALE=Arbitrary Lagrangian Eulerian; the data coordinate x[0] provides the current index in slidingMarkerNumbers, and the ODE2 coordinate q[0] provides the (given) moving coordinate in the cable element.

### Additional information for ObjectJointALEMoving2D:

- The Object has the following types = Connector, Constraint
- Requested marker type = \_None
- Requested node type: read detailed information of item
- **Short name** for Python = **ALEMovingJoint2D**

The item **ObjectJointALEMoving2D** with type = 'JointALEMoving2D' has the following parameters:

Name	type	size	default value	description
name	String		"	constraints's unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	marker m0: position-marker of mass point
			INT]	or rigid body; marker m1: updated marker
				to ANCF Cable2D element, where the slid-
				ing joint currently is attached to; must
				be initialized with an appropriate (global)
				marker number according to the starting
				position of the sliding object; this marker
				changes with time (PostNewtonStep)
slidingMarkerNumbers	ArrayIndex			a list of sn (global) marker numbers which
				are are used to update marker1
slidingMarkerOffsets	Vector			this list contains the offsets of ev-
				ery sliding object (given by sliding-
				MarkerNumbers) w.r.t. to the ini-
				tial position (0): marker0: offset=0,
				marker1: offset=Length(cable0), marker2:
				offset=Length(cable0)+Length(cable1),
slidingOffset	Real		0.	sliding offset list [SI:m]: a list of sn scalar
				offsets, which represent the (reference arc)
				length of all previous sliding cable elements
nodeNumbers	ArrayIndex		[ MAXINT, MAX-	node number of NodeGenericData (GD)
			INT]	with one data coordinate and of Node-
				GenericODE2 (ALE) with one ODE2 coor-
				dinate
usePenaltyFormulation	bool		False	flag, which determines, if the connector
				is formulated with penalty, but still using
				algebraic equations (IsPenaltyConnector()
				still false)
penaltyStiffness	Real		0.	penalty stiffness [SI:N/m] used if usePenal-
				tyFormulation=True
activeConnector	bool		True	flag, which determines, if the connector
				is active; used to deactivate (temorarily) a
				connector or constraint
visualization	VObjectJointALEM	1oving2	D	parameters for visualization of item

# The item VObjectJointALEMoving2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = radius of revolute joint; size
				== -1.f means that default connector size is
				used
color	Float4		[-1.,-1.,-1.]	RGBA connector color; if R==-1, use default
				color

# $Detailed\ information\ on\ Object Joint ALE Moving 2D:$

input parameter	symbol	description see tables above
markerNumbers	$[m0, m1]^{T}$	
slidingMarkerNumbers	$[m_{s0},\ldots,m_{sn}]^{\mathrm{T}}$	
slidingMarkerOffsets	$[d_{s0},\ldots,d_{sn}]$	
slidingOffset	$S_{off}$	
nodeNumbers	$[n_{GD}, n_{ALE}]$	
penaltyStiffness	k	

### The following output parameters are available as OutputVariableType in sensors and other functions:

output parameter	symbol	description
Position	<sup>0</sup> <b>p</b> <sub>m0</sub>	current global position of position marker
		<i>m</i> 0
Velocity	<sup>0</sup> <b>v</b> <sub>m0</sub>	current global velocity of position marker
		m0
SlidingCoordinate	$s_g = q_{ALE} + s_{off}$	current value of the global sliding ALE co-
		ordinate, including offset; note that refer-
		ence coordinate of $q_{ALE}$ is ignored!
Coordinates	$[x_{data0}, q_{ALE}]^{\mathrm{T}}$	provides two values: [0] = current sliding
		marker index, [1] = ALE sliding coordinate
Coordinates_t	$[\dot{q}_{ALE}]^{\mathrm{T}}$	provides ALE sliding velocity
Force	f	joint force vector (3D)

# **Description of Item:**

intermediate variables	symbol	description
generic data node	$\mathbf{x} = [x_{data0}]^{\mathrm{T}}$	coordinates of node with node number $n_{GD}$
generic ODE2 node	$\mathbf{q} = [q_0]^{\mathrm{T}}$	coordinates of node with node number
		$n_{ALE}$ , which is shared with all ALE-ANCF
		and ALE sliding joint objects
data coordinate	$x_{data0}$	the current index in slidingMarkerNum-
		bers
ALE coordinate	$q_{ALE} = q_0$	current ALE coordinate (in fact this is the
		Eulerian coordinate in the ALE formula-
		tion); note that reference coordinate of $q_{ALE}$
		is ignored!

marker m0 position	<sup>0</sup> <b>p</b> m0	current global position which is provided
		by marker m0
marker m0 velocity	<sup>0</sup> <b>v</b> <sub>m0</sub>	current global velocity which is provided
		by marker m0
cable coordinates	<b>q</b> <sub>ANCF,m1</sub>	current coordiantes of the ANCF cable el-
		ement with the current marker m1 is refer-
		ring to
sliding position	${}^{0}\mathbf{r}_{ANCF} = \mathbf{S}(s_{el})\mathbf{q}_{ANCF,m1}$	current global position at the ANCF cable
		element, evaluated at local sliding position
		$S_{el}$
sliding position slope	$^{0}\mathbf{r}_{ANCF}^{\prime}=\mathbf{S}^{\prime}(s_{el})\mathbf{q}_{ANCF,m1}$	current global slope vector of the ANCF ca-
		ble element, evaluated at local sliding posi-
		$tion s_{el}$
sliding velocity	${}^{0}\mathbf{v}_{ANCF} = \mathbf{S}(s_{el})\dot{\mathbf{q}}_{ANCF,m1} + \dot{q}_{ALE}{}^{0}\mathbf{r}'_{ANCF}$	current global velocity at the ANCF cable
		element, evaluated at local sliding position
		$s_{el}$ , including convective term
sliding normal vector	$^{0}\mathbf{n}=\left[ -r_{1}^{\prime},r_{0}^{\prime}\right]$	2D normal vector computed from slope $\mathbf{r}' =$
		<sup>0</sup> <b>r</b> ' <sub>ANCF</sub>
algebraic variables	$\mathbf{z} = [\lambda_0,  \lambda_1]^{\mathrm{T}}$	algebraic variables (Lagrange multipliers)
		according to the algebraic equations

The element sliding coordinate (in the local coordinates of the current sliding element) is computed from the ALE coordinate

$$s_{el} = q_{ALE} + s_{off} - d_{m1} = s_g - d_{m1}. (5.112)$$

The vector (=difference; error) between the marker m0 and the marker m1 (= $\mathbf{r}_{ANCF}$ ) positions reads

$${}^{0}\Delta \mathbf{p} = {}^{0}\mathbf{r}_{ANCF} - {}^{0}\mathbf{p}_{m0} \tag{5.113}$$

The vector (=difference; error) between the marker *m*0 and the marker *m*1 velocities reads

$${}^{0}\Delta\mathbf{v} = {}^{0}\mathbf{v}_{ANCF} - {}^{0}\mathbf{v}_{m0} \tag{5.114}$$

**Algebraic constraint equations**: The 2D sliding joint is implemented having 2 equations, using the Lagrange multipliers **z**. The algebraic (index 3) equations read

$$^{0}\Delta\mathbf{p} = 0 \tag{5.115}$$

Note that the Lagrange multipliers  $[\lambda_0, \lambda_1]^T$  are the global forces in the joint. In the index 2 case the algebraic equations read

$$^{0}\Delta\mathbf{v}=0\tag{5.116}$$

If usePenalty = True, the algebraic equations are changed to:

$${}^{0}\Delta\mathbf{p} - \frac{1}{k}\mathbf{z} = 0. \tag{5.117}$$

If activeConnector = False, the algebraic equations are changed to:

$$\lambda_0 = 0, \tag{5.118}$$

$$\lambda_1 = 0. ag{5.119}$$

**Post Newton Step**: After the Newton solver has converged, a PostNewtonStep is performed for the element, which updates the marker *m*1 index if necessary.

$$s_{el} < 0 \rightarrow x_{data0} = 1$$
  
 $s_{el} > L \rightarrow x_{data0} + 1$  (5.120)

Furthermore, it is checked, if  $x_{data0}$  becomes smaller than zero, which raises a warning and keeps  $x_{data0} = 0$ . The same results if  $x_{data0} \ge sn$ , then  $x_{data0} = sn$ . Finally, the data coordinate is updated in order to provide the starting value for the next step,

$$x_{data1} += s. (5.121)$$

Examples: see TestModels!

# 5.4 Markers

### 5.4.1 MarkerBodyMass

A marker attached to the body mass; use this marker to apply a body-load (e.g. gravitational force).

### Additional information for MarkerBodyMass:

• The Marker has the following types = Object, Body, BodyMass

The item **MarkerBodyMass** with type = 'BodyMass' has the following parameters:

Name	type	size	default value	description
name	String		"	marker's unique name
bodyNumber	Index		MAXINT	body number to which marker is attached
				to
visualization	VMarkerBodyMass			parameters for visualization of item

The item VMarkerBodyMass has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

# 5.4.2 MarkerBodyPosition

A position body-marker attached to local position (x,y,z) of the body.

### Additional information for MarkerBodyPosition:

• The Marker has the following types = Object, Body, Position

The item **MarkerBodyPosition** with type = 'BodyPosition' has the following parameters:

Name	type	size	default value	description
name	String		"	marker's unique name
bodyNumber	Index		MAXINT	body number to which marker is attached
				to
localPosition	Vector3D	3	[0.,0.,0.]	local body position of marker; e.g. local
				(body-fixed) position where force is applied
				to
visualization	VMarkerBodyPosit	ion		parameters for visualization of item

The item VMarkerBodyPosition has the following parameters:

Name	;	type	size	default value	description
show		bool		True	set true, if item is shown in visualization
					and false if it is not shown

# 5.4.3 MarkerBodyRigid

A rigid-body (position+orientation) body-marker attached to local position (x,y,z) of the body.

# Additional information for MarkerBodyRigid:

• The Marker has the following types = Object, Body, Position, Orientation

The item **MarkerBodyRigid** with type = 'BodyRigid' has the following parameters:

Name	type	size	default value	description
name	String		"	marker's unique name
bodyNumber	Index		MAXINT	body number to which marker is attached
				to
localPosition	Vector3D	3	[0.,0.,0.]	local body position of marker; e.g. local
				(body-fixed) position where force is applied
				to
visualization	VMarkerBodyRigid	l		parameters for visualization of item

The item VMarkerBodyRigid has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

#### 5.4.4 MarkerNodePosition

A node-Marker attached to a position-based node.

#### Additional information for MarkerNodePosition:

• The Marker has the following types = Node, Position

The item **MarkerNodePosition** with type = 'NodePosition' has the following parameters:

Name	type	size	default value	description
name	String		"	marker's unique name
nodeNumber	Index		MAXINT	node number to which marker is attached
				to
visualization	VMarkerNodePosit	ion		parameters for visualization of item

The item VMarkerNodePosition has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

## 5.4.5 MarkerNodeRigid

A rigid-body (position+orientation) node-marker attached to a rigid-body node.

## Additional information for MarkerNodeRigid:

• The Marker has the following types = Node, Position, Orientation

The item **MarkerNodeRigid** with type = 'NodeRigid' has the following parameters:

Name	type	size	default value	description
name	String		"	marker's unique name
nodeNumber	Index		MAXINT	node number to which marker is attached
				to
visualization	VMarkerNodeRigio	ı		parameters for visualization of item

The item VMarkerNodeRigid has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

#### 5.4.6 MarkerNodeCoordinate

A node-Marker attached to a ODE2 coordinate of a node; for other coordinates (ODE1,...) other markers need to be defined.

#### Additional information for MarkerNodeCoordinate:

• The Marker has the following types = Node, Coordinate

The item **MarkerNodeCoordinate** with type = 'NodeCoordinate' has the following parameters:

Name	type	size	default value	description
name	String		"	marker's unique name
nodeNumber	Index		MAXINT	node number to which marker is attached
				to
coordinate	Index		MAXINT	coordinate of node to which marker is at-
				tached to
visualization	VMarkerNode(	Coordinate		parameters for visualization of item

The item VMarkerNodeCoordinate has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

#### 5.4.7 MarkerSuperElementPosition

A position marker attached to a SuperElement, such as ObjectFFRF, ObjectGenericODE2 and ObjectFFRFreducedOrder (for which it is inefficient!!!). The marker acts on the mesh nodes, not on the underlying nodes of the object. For a list of n mesh node numbers, referencing to mesh node points  ${}^b\mathbf{p}_i$  and weights  $w_i$ , the body-fixed marker position  ${}^b\mathbf{p}_m$  results in  ${}^b\mathbf{p}_m = \sum_{i=0}^{n-1} w_i \cdot {}^b\mathbf{p}_i$ . EXAMPLE for single node marker on body 4, mesh node 10: MarkerSuperElementPosition(bodyNumber=4, meshNodeNumber=[10], weightingFactors=[1])

#### Additional information for MarkerSuperElementPosition:

• The Marker has the following types = Object, Body, Position

The item **MarkerSuperElementPosition** with type = 'SuperElementPosition' has the following parameters:

Name	type	size	default value	description
name	String		"	marker's unique name
bodyNumber	Index		MAXINT	body number to which marker is attached
				to
meshNodeNumbers	ArrayIndex		[]	mesh node numbers of superelement which
				are used to compute the body-fixed marker
				position; the related nodes must provide
				3D position information, such as Node-
				Point, NodePoint2D, NodeRigidBody[]; in
				order to retrieve the global node number,
				the generic body needs to convert local into
				global node numbers
weightingFactors	Vector		[]	weighting factors per node to compute the
				final local position
visualization	VMarkerSuperElen	nentPo	sition	parameters for visualization of item

The item VMarkerSuperElementPosition has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
showMarkerNodes	bool		True	set true, if all nodes are shown (similar to
				marker, but with less intensity)

## 5.4.8 MarkerBodyCable2DShape

A special Marker attached to a 2D ANCF beam finite element with cubic interpolation and 8 coordinates.

## Additional information for MarkerBodyCable2DShape:

• The Marker has the following types = Object, Body, Coordinate

The item **MarkerBodyCable2DShape** with type = 'BodyCable2DShape' has the following parameters:

Name	type	size	default value	description
name	String		"	marker's unique name
bodyNumber	Index		MAXINT	body number to which marker is attached
				to
numberOfSegments	Index		3	number of number of segments; each seg-
				ment is a line and is associated to a data
				(history) variable; must be same as in ac-
				cording contact element
visualization	VMarkerBody	Cable2DSha	ape	parameters for visualization of item

The item VMarkerBodyCable2DShape has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

## 5.4.9 MarkerBodyCable2DCoordinates

A special Marker attached to the coordinates of a 2D ANCF beam finite element with cubic interpolation.

#### Additional information for MarkerBodyCable2DCoordinates:

• The Marker has the following types = Object, Body, Coordinate

The item **MarkerBodyCable2DCoordinates** with type = 'BodyCable2DCoordinates' has the following parameters:

Name	type	size	default value	description
name	String		"	marker's unique name
bodyNumber	Index		MAXINT	body number to which marker is attached
				to
visualization	VMarkerBodyC	Cable2DCo	ordinates	parameters for visualization of item

 $The\ item\ VMarkerBody Cable 2D Coordinates\ has\ the\ following\ parameters:$ 

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

## 5.5 Loads

#### 5.5.1 LoadForceVector

Load with (3D) force vector; attached to position-based marker.

#### Additional information for LoadForceVector:

- Requested marker type = Position
- **Short name** for Python = **Force**

The item **LoadForceVector** with type = 'ForceVector' has the following parameters:

Name	type	size	default value	description
name	String		"	load's unique name
markerNumber	Index		MAXINT	marker's number to which load is applied
loadVector	Vector3D		[0.,0.,0.]	vector-valued load [SI:N]
bodyFixed	Bool		False	if bodyFixed is true, the load is defined in
				body-fixed (local) coordinates, leading to a
				follower force; if false: global coordinates
				are used
loadVectorUserFunction	PyFunctionVector3	DScala	rVector3D	A python function which defines the time-
			0	dependent load with parameters (Real
				t, Vector3D load); the load represents
				the current value of the load; WARN-
				ING: this factor does not work in com-
				bination with static computation (load-
				Factor); Example for python function:
				def f(t, loadVector): return [loadVec-
				tor[0]*np.sin(t*10*2*3.1415),0,0]
visualization	VLoadForceVector			parameters for visualization of item

The item VLoadForceVector has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

## 5.5.2 LoadTorqueVector

Load with (3D) torque vector; attached to rigidbody-based marker.

#### Additional information for LoadTorqueVector:

- Requested marker type = Orientation
- **Short name** for Python = **Torque**

The item **LoadTorqueVector** with type = 'TorqueVector' has the following parameters:

Name	type	size	default value	description
name	String		"	load's unique name
markerNumber	Index		MAXINT	marker's number to which load is applied
loadVector	Vector3D		[0.,0.,0.]	vector-valued load [SI:N]
bodyFixed	Bool		False	if bodyFixed is true, the load is defined in
				body-fixed (local) coordinates, leading to a
				follower torque; if false: global coordinates
				are used
loadVectorUserFunction	PyFunctionVector3	DScala	rVector3D	A python function which defines the time-
			0	dependent load with parameters (Real
				t, Vector3D load); the load represents
				the current value of the load; WARN-
				ING: this factor does not work in com-
				bination with static computation (load-
				Factor); Example for python function:
				def f(t, loadVector): return [loadVec-
				tor[0]*np.sin(t*10*2*3.1415),0,0]
visualization	VLoadTorqueVecto	r		parameters for visualization of item

#### The item VLoadTorqueVector has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

## 5.5.3 LoadMassProportional

Load attached to BodyMass-based marker, applying a 3D vector load (e.g. the vector [0,-g,0] is used to apply gravitational loading of size g in negative y-direction).

#### $Additional\ information\ for\ LoadMass Proportional:$

- Requested marker type = Body + BodyMass
- **Short name** for Python = **Gravity**

The item **LoadMassProportional** with type = 'MassProportional' has the following parameters:

Name	type	size	default value	description
name	String		"	load's unique name
markerNumber	Index		MAXINT	marker's number to which load is applied
loadVector	Vector3D		[0.,0.,0.]	vector-valued load [SI:N/kg = m/s <sup>2</sup> ]
loadVectorUserFunction	PyFunctionVector3	DScala	rVector3D	A python function which defines the time-
			0	dependent load with parameters (Real
				t, Vector3D load); the load represents
				the current value of the load; WARN-
				ING: this factor does not work in com-
				bination with static computation (load-
				Factor); Example for python function:
				def f(t, loadVector): return [loadVec-
				tor[0]*np.sin(t*10*2*3.1415),0,0]
visualization	VLoadMassPropor	tional		parameters for visualization of item

The item VLoadMassProportional has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

#### 5.5.4 LoadCoordinate

Load with scalar value, which is attached to a coordinate-based marker; the load can be used e.g. to apply a force to a single axis of a body, a nodal coordinate of a finite element or a torque to the rotatory DOF of a rigid body.

#### Additional information for LoadCoordinate:

• Requested marker type = Coordinate

The item **LoadCoordinate** with type = 'Coordinate' has the following parameters:

Name	type	size	default value	description
name	String		"	load's unique name
markerNumber	Index		MAXINT	marker's number to which load is applied
load	Real		0.	scalar load [SI:N]
loadUserFunction	PyFunctionScalar2		0	A python function which defines the time-
				dependent load with parameters (Real t,
				Real load); the load represents the cur-
				rent value of the load; WARNING: this
				factor does not work in combination with
				static computation (loadFactor); Example
				for python function: def f(t, load): return
				load*np.sin(t*10*2*3.1415)
visualization	VLoadCoordinate			parameters for visualization of item

The item VLoadCoordinate has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

#### 5.6 Sensors

#### 5.6.1 SensorNode

A sensor attached to a node. The sensor measures OutputVariables and outputs values into a file, showing per line [time, sensorValue[0], sensorValue[1], ...]. A user function can be attached to modify sensor values accordingly.

The item **SensorNode** with type = 'Node' has the following parameters:

Name	type	size	default value	description
name	String		"	marker's unique name
nodeNumber	Index		MAXINT	node number to which sensor is attached to
writeToFile	bool		True	true: write sensor output to file
fileName	String		"	directory and file name for sensor file out- put; default: empty string generates sensor + sensorNumber + outputVariableType
outputVariableType	OutputVariableTyp	e	OutputVariableTy	/pe:OthpmatVariableType for sensor
visualization	VSensorNode			parameters for visualization of item

The item VSensorNode has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

## 5.6.2 SensorObject

A sensor attached to any object except bodies (connectors, constraint, spring-damper, etc). As a difference to other SensorBody, the connector sensor measures quantities without a local position. The sensor measures OutputVariable and outputs values into a file, showing per line [time, sensorValue[0], sensorValue[1], ...]. A user function can be attached to postprocess sensor values accordingly.

The item **SensorObject** with type = 'Object' has the following parameters:

Name	type	size	default value	description
name	String		"	marker's unique name
objectNumber	Index		MAXINT	object (e.g. connector) number to which sensor is attached to
writeToFile	bool		True	true: write sensor output to file
fileName	String		"	directory and file name for sensor file out- put; default: empty string generates sensor + sensorNumber + outputVariableType
outputVariableType	OutputVariableType		OutputVariableTyp	e:QixlipmatVariableType for sensor
visualization	VSensorObject			parameters for visualization of item

The item VSensorObject has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown; sensors can be
				shown at the position assiciated with the
				object - note that in some cases, there might
				be no such position (e.g. data object)!

## 5.6.3 SensorBody

A sensor attached to a body-object with local position. As a difference to other ObjectSensors, the body sensor has a local position at which the sensor is attached to. The sensor measures OutputVariableBody and outputs values into a file, showing per line [time, sensorValue[0], sensorValue[1], ...]. A user function can be attached to postprocess sensor values accordingly.

The item **SensorBody** with type = 'Body' has the following parameters:

Name	type	size	default value	description
name	String		"	marker's unique name
bodyNumber	Index		MAXINT	body (=object) number to which sensor is
				attached to
localPosition	Vector3D	3	[0.,0.,0.]	local (body-fixed) body position of sensor
writeToFile	bool		True	true: write sensor output to file
fileName	String		"	directory and file name for sensor file out-
				put; default: empty string generates sensor
				+ sensorNumber + outputVariableType
outputVariableType	OutputVariableTyp	e	OutputVariableTy <sub>1</sub>	pe:QtxtpmatVariableType for sensor
visualization	VSensorBody			parameters for visualization of item

The item VSensorBody has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

## 5.6.4 SensorSuperElement

A sensor attached to a SuperElement-object with mesh node number. As a difference to other ObjectSensors, the SuperElement sensor has a mesh node number at which the sensor is attached to. The sensor measures OutputVariableSuperElement and outputs values into a file, showing per line [time, sensorValue[0], sensorValue[1], ...]. A user function can be attached to postprocess sensor values accordingly.

The item **SensorSuperElement** with type = 'SuperElement' has the following parameters:

Name	type s	ize default value	description
name	String	"	marker's unique name
bodyNumber	Index	MAXINT	body (=object) number to which sensor is
			attached to
meshNodeNumber	Index	-1	mesh node number, which is a local node
			number with in the object (starting with 0);
			the node number may represent a real Node
			in mbs, or may be virtual and reconstructed
			from the object coordinates such as in Ob-
			jectFFRFreducedOrder
writeToFile	bool	True	true: write sensor output to file
fileName	String	"	directory and file name for sensor file out-
			put; default: empty string generates sensor
			+ sensorNumber + outputVariableType
outputVariableType	OutputVariableType	OutputVariable <sup>7</sup>	Гуре: <b>Qixtpma</b> tVariableТуре for sensor
visualization	VSensorSuperElemen	t	parameters for visualization of item

The item VSensorSuperElement has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

#### 5.6.5 SensorLoad

A sensor attached to a load. The sensor measures the load values and outputs values into a file, showing per line [time, sensorValue[0], sensorValue[1], ...].

The item **SensorLoad** with type = 'Load' has the following parameters:

Name	type	size	default value	description
name	String		"	marker's unique name
loadNumber	Index		MAXINT	load number to which sensor is attached to
writeToFile	bool		True	true: write sensor output to file
fileName	String		"	directory and file name for sensor file out-
				put; default: empty string generates sensor
				+ sensorNumber + outputVariableType
visualization	VSensorLoad			parameters for visualization of item

The item VSensorLoad has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown; CURRENTLY
				NOT AVAILABLE

# 5.7 GraphicsData

Some items may include a 'graphicsData' structure. GraphicsData contains a list of graphicsData items, i.e. graphicsData = [graphicsItem1, graphicsItem2, ...]. Every single graphicsItem may be defined as one of the following structures using a specific 'type':

Name	type	default value	description
type = 'Line':			draws a polygonal line between all specified points
color	list	[0,0,0,1]	list of 4 floats to define RGB-color and transparency
data	list	mandatory	list of float triples of x,y,z coordinates of the line
			floats to define RGB-color and transparency; Exam-
			ple: data=[0,0,0, 1,0,0, 1,1,0, 0,1,0, 0,0,0] draws a
			rectangle with side length 1
type = 'Circle':			draws a circle with center point, normal (defines plane of
color	list	[0,0,0,1]	circle) and radius list of 4 floats to define RGB-color and transparency
radius	float	mandatory	radius
position	list	mandatory	list of float triples of x,y,z coordinates of center point
1			of the circle
normal	list	[0,0,1]	list of float triples of x,y,z coordinates of normal to the
			plane of the circle; the default value gives a circle in
			the $(x, y)$ -plane
type = 'Text':			places the given text at position
color	list	[0,0,0,1]	list of 4 floats to define RGB-color and transparency
text	string	mandatory	text to be displayed
position	list	mandatory	list of float triples of [x,y,z] coordinates of the left upper
			position of the text; e.g. position=[20,10,0]
type = 'TriangleLis	st':		draws a flat triangle mesh for given points and connectivity
points	list	mandatory	list [x0,y0,z0, x1,y1,z1,] containing $n \times 3$ floats
			(grouped x0,y0,z0, x1,y1,z1,) to define x,y,z coor-
			dinates of points, <i>n</i> being the number of points (=ver-
			tices)
colors	list	empty	list [R0,G0,B0,A0, R1,G2,B1,A1,] containing $n \times 4$
			floats to define RGB-color and transparency A, where $n$
			must be according to number of points; if field 'colors'
			does not exist, default colors will be used
normals	list	empty	list $[n0x,n0y,n0z,]$ containing $n \times 3$ floats to define
			normal direction of triangles per point, where $n$ must
			be according to number of points; if field 'normals'
			does not exist, default normals [0,0,0] will be used
triangles	list	mandatory	list [T0point0, T0point1, T0point2,] containing
			$n_{trig} \times 3$ floats to define point indices of each vertex of
			the triangles (=connectivity); point indices start with
			index 0; the maximum index must be $\leq$ points.size()

Examples of GraphicsData can be found in the Python examples and in exudynUtilities.py.

# **Chapter 6**

# **EXUDYN Settings**

This section includes the reference manual for settings which are available in the python interface, e.g. simulation settings, visualization settings, and others.

## 6.1 Simulation settings

This section includes hierarchical structures for simulation settings, e.g., time integration, static solver, Newton iteration and solution file export.

## 6.1.1 SolutionSettings

General settings for exporting the solution (results) of a simulation. SolutionSettings has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
writeSolutionToFile	bool		True	flag (true/false), which determines if
				(global) solution vector is written to file
appendToFile	bool		False	flag (true/false); if true, solution and solver-
				Information is appended to existing file
				(otherwise created)
writeFileHeader	bool		True	flag (true/false); if true, file header is writ-
				ten (turn off, e.g. for multiple runs of time
				integration)
writeFileFooter	bool		True	flag (true/false); if true, information at end
				of simulation is written: convergence, total
				solution time, statistics
solutionWritePeriod	UReal		0.01	time span (period), determines how often
				the solution is written during a simulation
sensorsAppendToFile	bool		False	flag (true/false); if true, sensor output is ap-
				pended to existing file (otherwise created)
sensorsWriteFileHeader	bool		True	flag (true/false); if true, file header is written
				for sensor output (turn off, e.g. for multiple
				runs of time integration)

sensorsWritePeriod	UReal	0.01	time span (period), determines how often
			the sensor output is written during a simulation
exportVelocities	bool	True	solution is written as displacements, velocities[, accelerations] [,algebraicCoordinates] [,DataCoordinates]
exportAccelerations	bool	True	solution is written as displacements, [velocities,] accelerations [,algebraicCoordinates] [,DataCoordinates]
exportAlgebraicCoordinates	bool	True	solution is written as displacements, [velocities,] [accelerations,], algebraicCoordinates (=Lagrange multipliers) [,DataCoordinates]
exportDataCoordinates	bool	True	solution is written as displacements, [velocities,] [accelerations,] [,algebraicCoordinates (=Lagrange multipliers)] ,DataCoordinates
coordinatesSolutionFileName	FileName	'coordinatesSolution.tx	t' filename and (relative) path of solution file containing all coordinates versus time
solverInformationFileName	FileName	'solverInformation.txt'	filename and (relative) path of text file showing detailed information dur- ing solving; detail level according to yourSolver.verboseModeFile; if solution- Settings.appendToFile is true, the informa- tion is appended in every solution step
solutionInformation	String	"	special information added to header of solution file (e.g. parameters and settings, modes,)
outputPrecision	Index	10	precision for floating point numbers written to solution and sensor files
recordImagesInterval	Real	-1.	record frames (images) during solving: amount of time to wait until next image (frame) is recorded; set recordImages = - 1. if no images shall be recorded; set, e.g., recordImages = 0.01 to record an image every 10 milliseconds (requires that the time steps / load steps are sufficiently small!); for file names, etc., see VisualizationSettings.exportImages

## 6.1.2 Numerical Differentiation Settings

Settings for numerical differentiation of a function (needed for computation of numerical jacobian e.g. in implizit integration); HOTINT1: relativeEpsilon \* Maximum(minimumCoordinateSize, fabs(x(i))). NumericalDifferentiationSettings has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
relativeEpsilon	UReal		1e-7	relative differentiation parameter ep-
				silon; the numerical differentiation
				parameter $\varepsilon$ follows from the for-
				mula ( $\varepsilon = \varepsilon_{\text{relative}} * max(q_{min},  q_i  +$
				$[q_i^{Ref}]$ ), with $\varepsilon_{ m relative}$ =relativeEpsilon,
				$q_{min}$ =minimumCoordinateSize, $q_i$ is the
				current coordinate which is differentiated,
				and $qRef_i$ is the reference coordinate of the
				current coordinate
minimumCoordinateSize	UReal		1e-2	minimum size of coordinates in relative dif-
				ferentiation parameter
doSystemWideDifferentiation	bool		False	true: system wide differentiation (e.g. all
				ODE2 equations w.r.t. all ODE2 coordi-
				nates); false: only local (object) differenti-
				ation
addReferenceCoordinatesToEps	silon		False	true: for the size estimation of the differen-
	bool			tiation parameter, the reference coordinate
				$q_i^{Ref}$ is added to ODE2 coordinates -> see;
				false: only the current coordinate is used
				for size estimation of the differentiation pa-
				rameter

# 6.1.3 NewtonSettings

Settings for Newton method used in static or dynamic simulation. NewtonSettings has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
numericalDifferentiation	NumericalDifferent	iatioı	Settings	numerical differentiation parameters for
				numerical jacobian (e.g. Newton in static
				solver or implicit time integration)
useNumericalDifferentiation	bool		False	flag (true/false); false = perform direct com-
				putation of jacobian, true = use numerical
				differentiation for jacobian
useNewtonSolver	bool		True	flag (true/false); false = linear computation,
				true = use Newton solver for nonlinear so-
				lution
relativeTolerance	UReal		1e-8	relative tolerance of residual for Newton
				(general goal of Newton is to decrease the
				residual by this factor)
absoluteTolerance	UReal		1e-10	absolute tolerance of residual for New-
				ton (needed e.g. if residual is ful-
				filled right at beginning); condition:
				sqrt(q*q)/numberOfCoordinates <= abso-
				luteTolerance

weightTolerancePerCoordinate	bool	False	flag (true/false); false = compute error as L2-
weight folerancer erecordinate	5001	Taise	Norm of residual; true = compute error as
			(L2-Norm of residual) / (sqrt(number of co-
			_
			ordinates)), which can help to use common
2 11 26 1			tolerance independent of system size
newtonResidualMode	Index	0	0 use residual for computation of error
			(standard); 1 use change of solution in-
			crement for error (set relTol and absTol to
			same values!) ==> may be advantageous if
			residual is zero, e.g., in kinematic analysis;
			TAKE CARE with this flag
adaptInitialResidual	bool	True	flag (true/false); false = standard; true: if
			initialResidual is very small (or zero), it
			may increas dramatically in first step; to
			achieve relativeTolerance, the initialResid-
			ual will by updated by a higher residual
			within the first Newton iteration
1:C INI C C C C	TID 1	0.5	
modifiedNewtonContractivity	UReal	0.5	maximum contractivity (=reduction of er-
			ror in every Newton iteration) accepted by
			modified Newton; if contractivity is greater,
			a Jacobian update is computed
useModifiedNewton	bool	False	true: compute Jacobian only at first step; no
			Jacobian updates per step; false: Jacobian
			computed in every step
modifiedNewtonJacUpdatePers	Step	False	true: compute Jacobian at every time step,
_	bool		but not in every iteration (except for bad
			convergence ==> switch to full Newton)
maxIterations	Index	25	maximum number of iterations (including
			modified + restart Newton steps); after that
			iterations, the static/dynamic solver stops
			with error
maxModifiedNewtonIterations	Index	8	maximum number of iterations for modi-
maxivioumed New torriterations	niuex	0	
			fied Newton (without Jacobian update); af-
			ter that number of iterations, the modified
			Newton method gets a jacobian update and
			is further iterated
maxModifiedNewtonRestartIte	rations	7	maximum number of iterations for modi-
	Index		fied Newton after aJacobian update; after
			that number of iterations, the full Newton
			method is started for this step
maximumSolutionNorm	UReal	1e38	this is the maximum allowed value
			for solutionU.L2NormSquared() which
			is the square of the square norm
			(value= $u_1^2+u_2^2+$ ), and solutionV/A; if the
			norm of solution vectors are larger, Newton
			method is stopped; the default value is cho-
			sen such that it would still work for single
			precision numbers (float)
mayDiagontinuousIteesties	Indov		
maxDiscontinuousIterations	Index	5	maximum number of discontinuous (post
Ì			Newton) iterations

ignoreMaxDiscontinuousIterati	ons	True	continue solver if maximum number of
	bool		discontinuous (post Newton) iterations is
			reached (ignore tolerance)
discontinuousIterationToleranc	e	1	absolute tolerance for discontinuous (post
	UReal		Newton) iterations; the errors represent ab-
			solute residuals and can be quite high
stepInformation	Index	2	0 only current step time, 1 show time
			to go, 2 show newton iterations (Nit)
			per step, 3 show discontinuous iterations
			(Dit) and newton jacobians (jac) per step

## 6.1.4 GeneralizedAlphaSettings

Settings for generalized-alpha, implicit trapezoidal or Newmark time integration methods. GeneralizedAlphaSettings has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
newmarkBeta	UReal		0.25	value beta for Newmark method; default
				value beta = $\frac{1}{4}$ corresponds to (undamped)
				trapezoidal rule
newmarkGamma	UReal		0.5	value gamma for Newmark method; de-
				fault value gamma = $\frac{1}{2}$ corresponds to (un-
				damped) trapezoidal rule
useIndex2Constraints	bool		False	set useIndex2Constraints = true in order to
				use index2 (velocity level constraints) for-
				mulation
useNewmark	bool		False	if true, use Newmark method with beta and
				gamma instead of generalized-Alpha
spectralRadius	UReal		0.9	spectral radius for Generalized-alpha
				solver; set this value to 1 for no damping
				or to 0 < spectralRadius < 1 for damping
				of high-frequency dynamics; for position-
				level constraints (index 3), spectralRadius
				must be < 1
computeInitialAccelerations	bool		True	true: compute initial accelerations from
				system EOM in acceleration form; NOTE
				that initial accelerations that are following
				from user functions in constraints are not
				considered for now! false: use zero acceler-
				ations

## 6.1.5 TimeIntegrationSettings

General parameters used in time integration; specific parameters are provided in the according solver settings, e.g. for generalizedAlpha.

TimeIntegrationSettings has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
newton	NewtonSettings			parameters for Newton method; used for
				implicit time integration methods only
startTime	UReal		0	start time of time integration (usually set to
				zero)
endTime	UReal		1	end time of time integration
numberOfSteps	UInt		100	number of steps in time integration;
				stepsize is computed from (endTime-
				startTime)/numberOfSteps
adaptiveStep	bool		True	true: use step reduction if step fails; false:
				constant step size
minimumStepSize	UReal		1e-8	lower limit of time step size, before integra-
				tor stops
verboseMode	Index		0	0 no output, 1 show short step infor-
				mation every 2 seconds (error), 2 show
				every step information, 3 show also solu-
				tion vector, 4 show also mass matrix and
				jacobian (implicit methods), 5 show also
				Jacobian inverse (implicit methods)
verboseModeFile	Index		0	same behaviour as verboseMode, but out-
				puts all solver information to file
generalizedAlpha	GeneralizedAlphaS	etting	gs	parameters for generalized-alpha, implicit
				trapezoidal rule or Newmark (options only
				apply for these methods)
preStepPyExecute	String		"	Python code to be executed prior to every
				step and after last step, e.g. for postprocess-
				ing

## 6.1.6 StaticSolverSettings

Settings for static solver linear or nonlinear (Newton). StaticSolverSettings has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
newton	NewtonSettings			parameters for Newton method (e.g. in
				static solver or time integration)
numberOfLoadSteps	Index		1	number of load steps; if numberOfLoad-
				Steps=1, no load steps are used and full
				forces are applied at once
loadStepDuration	UReal		1	quasi-time for all load steps (added to cur-
				rent time in load steps)

log dCtomCtomt	LIDaal	0	a guasi time which can be used for
loadStepStart	UReal	0	a quasi time, which can be used for
			the output (first column) as well as
			for time-dependent forces; quasi-
			time is increased in every step i by
			loadStepDuration/numberOfLoad-
			Steps; loadStepTime = loadStepStart +
			i*loadStepDuration/numberOfLoadSteps,
			but loadStepStart untouched ==> incre-
			ment by user
loadStepGeometric	bool	False	if loadStepGeometric=false, the load steps
The state of the s			are incremental (arithmetic series, e.g.
			0.1,0.2,0.3,); if true, the load steps are
			increased in a geometric series, e.g. for
			n = 8 numberOfLoadSteps and $d =$
			1000 loadStepGeometricRange, it follows:
			$1000^{1/8}/1000 = 0.00237, 1000^{2/8}/1000 =$
			$0.00562$ , $1000^{3/8}/1000 = 0.0133$ ,,
			$1000^{7/8}/1000 = 0.422, 1000^{8/8}/1000 = 1$
loadStepGeometricRange	UReal	1000	if loadStepGeometric=true, the load steps
1			are increased in a geometric series, see load-
			StepGeometric
useLoadFactor	bool	True	true: compute a load factor $\in [0,1]$ from
useLoadi actor	5001	liue	
			static step time; all loads are scaled by the
			load factor; false: loads are always scaled
			with 1 – use this option if time dependent
			loads use a userFunction
stabilizerODE2term	UReal	0	add mass-proportional stabilizer term in
			ODE2 part of jacobian for stabilization
			(scaled ), e.g. of badly conditioned prob-
			lems; the diagnoal terms are scaled with
			$stabilizer = (1 - loadStepFactor^2)$ , and go
			to zero at the end of all load steps:
			loadStepFactor = 1 -> stabilizer = 0
1CCt	1 1	T	
adaptiveStep	bool	True	true: use step reduction if step fails; false:
			fixed step size
minimumStepSize	UReal	1e-8	lower limit of step size, before nonlinear
			solver stops
verboseMode	Index	1	0 no output, 1 show errors and load
			steps, 2 show short Newton step infor-
			mation (error), 3 show also solution vec-
			tor, 4 show also jacobian, 5 show also
			Jacobian inverse
verboseModeFile	Index	0	same behaviour as verboseMode, but out-
verbosemoderile	niuex		
C. P.F.	0	"	puts all solver information to file
preStepPyExecute	String		Python code to be executed prior to every
			load step and after last step, e.g. for post-
		1 1	processing

## 6.1.7 SimulationSettings

General Settings for simulation; according settings for solution and solvers are given in subitems of this structure.

SimulationSettings has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
timeIntegration	TimeIntegrationSet	tings		time integration parameters
solutionSettings	SolutionSettings			settings for solution files
staticSolver	StaticSolverSettings	•		static solver parameters
linearSolverType	LinearSolverType		LinearSolverType::EXU	dense
				selection of numerical linear solver:
				exu.LinearSolverType.EXUdense
				(dense matrix inverse),
				exu.LinearSolverType.EigenSparse (sparse
				matrix LU-factorization), (enumeration
				type)
cleanUpMemory	bool		False	true: solvers will free memory at exit (rec-
				ommended for large systems); false: keep
				allocated memory for repeated computa-
				tions to increase performance
displayStatistics	bool		False	display general computation information at
				end of time step (steps, iterations, function
				calls, step rejections,
displayComputationTime	bool		False	display computation time statistics at end
				of solving
pauseAfterEachStep	bool		False	pause after every time step or static load
				step(user press SPACE)
outputPrecision	Index		6	precision for floating point numbers written
				to console; e.g. values written by solver
numberOfThreads	Index		1	number of threads used for parallel com-
				putation (1 == scalar processing); not yet
				implemented (status: Nov 2019)

# 6.2 Visualization settings

This section includes hierarchical structures for visualization settings, e.g., drawing of nodes, bodies, connectors, loads and markers and furthermore openGL, window and save image options.

## 6.2.1 VSettingsGeneral

General settings for visualization.

VSettingsGeneral has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	

graphicsUpdateInterval	float		0.1	interval of graphics update during simula-
				tion in seconds; $0.1 = 10$ frames per second;
				low numbers might slow down computa-
				tion speed
autoFitScene	bool		True	automatically fit scene within first second
				after StartRenderer()
textSize	float		12.	general text size if not overwritten
minSceneSize	float		0.1	minimum scene size for initial scene size
				and for autoFitScene, to avoid division by
				zero; SET GREATER THAN ZERO
backgroundColor	Float4	4	[1.,1.,1.,1.]	
				red, green, blue and alpha values for back-
				ground of render window (white=[1,1,1,1];
				black = [0,0,0,1])
coordinateSystemSize	float		0.4	size of coordinate system relative to screen
drawCoordinateSystem	bool		True	false = no coordinate system shown
showComputationInfo	bool		True	false = no info about computation (current
				time, solver, etc.) shown
pointSize	float		0.01	global point size (absolute)
circleTiling	Index		16	global number of segments for circles; if
				smaller than 2, 2 segments are used (flat)
cylinderTiling	Index		16	global number of segments for cylinders; if
				smaller than 2, 2 segments are used (flat)
sphereTiling	Index		6	global number of segments for spheres; if
				smaller than 2, 2 segments are used (flat)
axesTiling	Index		12	global number of segments for drawing
				axes cylinders and cones (reduce this num-
				ber, e.g. to 4, if many axes are drawn)

# 6.2.2 VSettingsWindow

Window and interaction settings for visualization; handle changes with care, as they might lead to unexpected results or crashes.

VSettingsWindow has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
renderWindowSize	Index2	2	[1024,768]	initial size of OpenGL render window in
				pixel
startupTimeout	Index		5000	OpenGL render window startup timeout in
				ms (change might be necessary if CPU is
				very slow)
alwaysOnTop	bool		False	true: OpenGL render window will be al-
				ways on top of all other windows
maximize	bool		False	true: OpenGL render window will be max-
				imized at startup

showWindow	bool	True	true: OpenGL render window is shown on
			startup; false: window will be iconified at
			startup (e.g. if you are starting multiple
			computations automatically)
keypressRotationStep	float	5.	rotation increment per keypress in degree
			(full rotation = 360 degree)
mouseMoveRotationFactor	float	1.	rotation increment per 1 pixel mouse move-
			ment in degree
keypressTranslationStep	float	0.1	translation increment per keypress relative
			to window size
zoomStepFactor	float	1.15	change of zoom per keypress (keypad +/-)
			or mouse wheel increment

# 6.2.3 VSettingsOpenGL

OpenGL settings for 2D and 2D rendering. VSettingsOpenGL has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
initialCenterPoint	Float3	3	[0.,0.,0.]	
				centerpoint of scene (3D) at renderer
				startup; overwritten if autoFitScene = True
initialZoom	float		1.	initial zoom of scene; overwritten/ignored
				if autoFitScene = True
initialMaxSceneSize	float		1.	initial maximum scene size (auto: diago-
				nal of cube with maximum scene coordi-
				nates); used for 'zoom all' functionality and
				for visibility of objects; overwritten if aut-
				oFitScene = True
initialModelRotation	StdArray33F	3x3	[Matrix3DF[3,3,1.,0.,0.,	
			0.,1.,0., 0.,0.,1.]]	initial model rotation matrix for OpenGl;
				in python use e.g.: initialModelRota-
				tion=[[1,0,0],[0,1,0],[0,0,1]]
multiSampling	Index	1	1	multi sampling turned off (<=1) or turned
				on to given values (2, 4, 8 or 16); increases
				the graphics buffers and might crash due
				to graphics card memory limitations; only
				works if supported by hardware; if it does
				not work, try to change 3D graphics hard-
				ware settings!
lineWidth	float	1	1.	width of lines used for representation of
				lines, circles, points, etc.
lineSmooth	bool	1	True	draw lines smooth
textLineWidth	float	1	1.	width of lines used for representation of text
textLineSmooth	bool	1	False	draw lines for representation of text smooth

showFaces	bool	1	True	show faces of triangles, etc.; using the options showFaces=false and show- FaceEdges=true gives are wire frame rep- resentation
showFaceEdges	bool	1	False	show edges of faces; using the options showFaces=false and show-FaceEdges=true gives are wire frame representation
shadeModelSmooth	bool	1	True	true: turn on smoothing for shaders, which uses vertex normals to smooth surfaces
materialSpecular	Float4	4	[1.,1.,1.,1.]	4f specular color of material
materialShininess	float	1	60.	shininess of material
enableLight0	bool	1	True	turn on/off light0
light0position	Float4	ig  4	[1.,1.,-10.,0.]	4f position vector of GL light0; 4th value should be 0, otherwise the vector obtains a special interpretation, see opengl manuals
light0ambient	float	1	0.25	ambient value of GL light0
light0diffuse	float	1	0.4	diffuse value of GL light0
light0specular	float	1	0.4	specular value of GL light0
enableLight1	bool	1	True	turn on/off light1
light1position	Float4	4	[0.,3.,2.,0.]	4f position vector of GL light1; 4th value should be 0, otherwise the vector obtains a special interpretation, see opengl manuals
light1ambient	float	1	0.25	ambient value of GL light1
light1diffuse	float	1	0.4	diffuse value of GL light1
light1specular	float	1	0.	specular value of GL light1
drawFaceNormals	bool	1	False	draws triangle normals, e.g. at center of triangles; used for debugging of faces
drawVertexNormals	bool	1	False	draws vertex normals; used for debugging
drawNormalsLength	float	1	0.1	length of normals; used for debugging

## 6.2.4 VSettingsContour

Settings for contour plots; use these options to visualize field data, such as displacements, stresses, strains, etc. for bodies, nodes and finite elements.

VSettingsContour has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
outputVariableComponent	Index	1	0	select the component of the chosen output
				variable; e.g., for displacements, 3 compo-
				nents are available: $0 == x$ , $1 == y$ , $2 == z$
				component; if this component is not avail-
				able by certain objects or nodes, no value is
				drawn

outputVariable	OutputVariableTyp	e	OutputVariableType::_	None
				selected contour plot output variable type;
				select OutputVariableTypeNone to deac-
				tivate contour plotting.
minValue	float	1	0	minimum value for contour plot; set man-
				ually, if automaticRange == False
maxValue	float	1	1	maximum value for contour plot; set man-
				ually, if automaticRange == False
automaticRange	bool		True	if true, the contour plot value range is cho-
				sen automatically to the maximum range
showColorBar	bool		True	show the colour bar with minimum and
				maximum values for the contour plot
colorBarTiling	Index	1	12	number of tiles (segements) shown in the
				colorbar for the contour plot

## 6.2.5 VSettingsExportImages

Functionality to export images to files (.tga format) which can be used to create animations; to activate image recording during the solution process, set SolutionSettings.recordImagesInterval accordingly. VSettingsExportImages has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
saveImageTimeOut	Index		5000	timeout for safing a frame as image to disk;
				this is the amount of time waited for re-
				drawing; increase for very complex scenes
saveImageFileName	FileName		'images/frame'	filename (without extension!) and (rel-
				ative) path for image file(s) with con-
				secutive numbering (e.g., frame0000.tga,
				frame0001.tga,); folders must already ex-
				ist!
saveImageFileCounter	Index		0	current value of the counter which is used
				to consecutively save frames (images) with
				consecutive numbers
saveImageSingleFile	bool		False	true: only save single files with given file-
				name, not adding numbering; false: add
				numbering to files, see saveImageFileName

## 6.2.6 VSettingsNodes

Visualization settings for nodes.

VSettingsNodes has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	

show	bool		True	flag to decide, whether the nodes are shown
showNumbers	bool		False	flag to decide, whether the node number is
				shown
drawNodesAsPoint	bool		True	simplified/faster drawing of nodes; uses
				general->pointSize as drawing size; if
				drawNodesAsPoint==True, the basis of the
				node will be drawn with lines
showBasis	bool		False	show basis (three axes) of coordinate sys-
				tem in 3D nodes
basisSize	float		0.2	size of basis for nodes
tiling	Index		4	tiling for node if drawn as sphere; used to
				lower the amount of triangles to draw each
				node; if drawn as circle, this value is multi-
				plied with 4
defaultSize	float		-1.	global node size; if -1.f, node size is relative
				to openGL.initialMaxSceneSize
defaultColor	Float4	4	[0.2,0.2,1.,1.]	
				default cRGB olor for nodes; 4th value is
				alpha-transparency
showNodalSlopes	Index		False	draw nodal slope vectors, e.g. in ANCF
				beam finite elements

# 6.2.7 VSettingsBeams

Visualization settings for beam finite elements.

VSettingsBeams has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
axialTiling	Index		8	number of segments to discretise the beams
				axis

# 6.2.8 VSettingsBodies

Visualization settings for bodies.

VSettingsBodies has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
show	bool		True	flag to decide, whether the bodies are
				shown
showNumbers	bool		False	flag to decide, whether the body(=object)
				number is shown
defaultSize	Float3	3	[1.,1.,1.]	
				global body size of xyz-cube

defaultColor	Float4	4	[0.3,0.3,1.,1.]	
				default cRGB olor for bodies; 4th value is
deformationScaleFactor	float		1	global deformation scale factor; also applies
				to nodes, if drawn; used for scaled drawing
				of (linear) finite elements, beams, etc.
beams	VSettingsBeams			visualization settings for beams (e.g. AN-
				CFCable or other beam elements)

## 6.2.9 VSettingsConnectors

Visualization settings for connectors.

VSettingsConnectors has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
show	bool		True	flag to decide, whether the connectors are
				shown
showNumbers	bool		False	flag to decide, whether the connec-
				tor(=object) number is shown
defaultSize	float		0.1	global connector size; if -1.f, connector size
				is relative to maxSceneSize
showJointAxes	bool		False	flag to decide, whether contact joint axes of
				3D joints are shown
jointAxesLength	float		0.2	global joint axes length
jointAxesRadius	float		0.02	global joint axes radius
showContact	bool		False	flag to decide, whether contact points, lines,
				etc. are shown
springNumberOfWindings	Index		8	number of windings for springs drawn as
				helical spring
contactPointsDefaultSize	float		0.02	global contact points size; if -1.f, connector
				size is relative to maxSceneSize
defaultColor	Float4	4	[0.2,0.2,1.,1.]	
				default cRGB olor for connectors; 4th value
				is alpha-transparency

# 6.2.10 VSettingsMarkers

Visualization settings for markers.

VSettingsMarkers has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
show	bool		True	flag to decide, whether the markers are
				shown

showNumbers	bool		False	flag to decide, whether the marker numbers
				are shown
drawSimplified	bool		True	draw markers with simplified symbols
defaultSize	float		-1.	global marker size; if -1.f, marker size is
				relative to maxSceneSize
defaultColor	Float4	4	[0.1,0.5,0.1,1.]	
				default cRGB olor for markers; 4th value is
				alpha-transparency

# 6.2.11 VSettingsLoads

Visualization settings for loads.

VSettingsLoads has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
show	bool		True	flag to decide, whether the loads are shown
showNumbers	bool		False	flag to decide, whether the load numbers
				are shown
defaultSize	float		0.2	global load size; if -1.f, load size is relative
				to maxSceneSize
defaultRadius	float		0.005	global radius of load axis if drawn in 3D
fixedLoadSize	bool		True	if true, the load is drawn with a fixed vec-
				tor length in direction of the load vector,
				independently of the load size
drawSimplified	bool		True	draw markers with simplified symbols
loadSizeFactor	float		0.1	if fixedLoadSize=false, then this scaling fac-
				tor is used to draw the load vector
defaultColor	Float4	4	[0.7,0.1,0.1,1.]	
				default cRGB olor for loads; 4th value is
				alpha-transparency

# 6.2.12 VSettingsSensors

Visualization settings for sensors.

VSettingsSensors has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
show	bool		True	flag to decide, whether the sensors are
				shown
showNumbers	bool		False	flag to decide, whether the sensor numbers
				are shown
drawSimplified	bool		True	draw sensors with simplified symbols

169

defaultSize	float		-1.	global sensor size; if -1.f, sensor size is rela-
				tive to maxSceneSize
defaultColor	Float4	4	[0.6,0.6,0.1,1.]	
				default cRGB olor for sensors; 4th value is
				alpha-transparency

#### 6.2.13 VisualizationSettings

Settings for visualization.

VisualizationSettings has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
general	VSettingsGeneral			general visualization settings
window	VSettingsWindow			visualization window and interaction set-
				tings
openGL	VSettingsOpenGL			OpenGL rendering settings
contour	VSettingsContour			contour plot visualization settings
exportImages	VSettingsExportIma	ages		settings for exporting (saving) images to
				files in order to create animations
nodes	VSettingsNodes			node visualization settings
bodies	VSettingsBodies			body visualization settings
connectors	VSettingsConnector	rs		connector visualization settings
markers	VSettingsMarkers			marker visualization settings
loads	VSettingsLoads			load visualization settings
sensors	VSettingsSensors			sensor visualization settings

#### 6.3 Solver substructures

This section includes structures contained in the solver, which can be accessed via the python interface during solution or for building a customized solver in python.

#### 6.3.1 CSolverTimer

Structure for timing in solver. Each Real variable is used to measure the CPU time which certain parts of the solver need. This structure is only active if the code is not compiled with the \_\_FAST\_EXUDYN\_LINALG option and if displayComputationTime is set True. Timings will only be filled, if useTimer is True. CSolverTimer has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
useTimer	bool		True	flag to decide, whether the timer is used
				(true) or not

total	Real	0.	total time measured between start and end
			of computation (static/dynamics)
factorization	Real	0.	solve or inverse
newtonIncrement	Real	0.	Jac <sup>-1</sup> * RHS; backsubstitution
integrationFormula	Real	0.	time spent for evaluation of integration for-
			mulas
ODE2RHS	Real	0.	time for residual evaluation of ODE2 right-
			hand-side
AERHS	Real	0.	time for residual evaluation of algebraic
			equations right-hand-side
totalJacobian	Real	0.	time for all jacobian computations
jacobianODE2	Real	0.	jacobian w.r.t. coordinates of ODE2 equa-
			tions (not counted in sum)
jacobianODE2_t	Real	0.	jacobian w.r.t. coordinates_t of ODE2 equa-
			tions (not counted in sum)
jacobianAE	Real	0.	jacobian of algebraic equations (not
			counted in sum)
massMatrix	Real	0.	mass matrix computation
reactionForces	Real	0.	CqT * lambda
postNewton	Real	0.	post newton step
writeSolution	Real	0.	time for writing solution
overhead	Real	0.	overhead, such as initialization, copying
			and some matrix-vector multiplication
python	Real	0.	time spent for python functions
visualization	Real	0.	time spent for visualization in computation
			thread
Reset()	void	useSolverTimer	reset solver timings to initial state by as-
			signing default values; useSolverTimer sets
			the useTimer flag
Sum()	Real		compute sum of all timers (except for those
			counted multiple, e.g., jacobians
StartTimer()	void	value	start timer function for a given variable;
			subtracts current CPU time from value
StopTimer()	void	value	stop timer function for a given variable;
			adds current CPU time to value
ToString()	String		converts the current timings to a string

## 6.3.2 SolverLocalData

Solver local data structure for solution vectors, system matrices and temporary vectors and data structures. SolverLocalData has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
nODE2	Index		0	number of second order ordinary diff. eq.
				coordinates
nODE1	Index		0	number of first order ordinary diff. eq. co-
				ordinates

nAE	Index	0	number of algebraic coordinates
nData	Index	0	number of data coordinates
nSys	Index	0	number of system (unknown) coordinates
			= nODE2+nODE1+nAE
startAE	Index	0	start of algebraic coordinates, but set to zero
			if nAE==0
systemResidual	ResizableVector		system residual vector (vectors will be
			linked to this vector!)
newtonSolution	ResizableVector		Newton decrement (computed from resid-
			ual and jacobian)
tempODE2	ResizableVector		temporary vector for ODE2 quantities; use
			in initial accelerations and during Newton
temp2ODE2	ResizableVector		second temporary vector for ODE2 quanti-
			ties; use in static computation
tempODE2F0	ResizableVector		temporary vector for ODE2 Jacobian
tempODE2F1	ResizableVector		temporary vector for ODE2 Jacobian
startOfStepStateAAlgorithmic	ResizableVector		additional term needed for generalized al-
			pha (startOfStep state)
aAlgorithmic	ResizableVector		additional term needed for generalized al-
			pha (current state)
CleanUpMemory()	void		if desired, temporary data is cleaned up to
			safe memory
SetLinearSolverType()	void	linearSolverType	set linear solver type and matrix version:
			links system matrices to according dense/s-
			parse versions
GetLinearSolverType()	LinearSolverType		return current linear solver type (dense/s-
			parse)

## 6.3.3 SolverIterationData

Solver internal structure for counters, steps, step size, time, etc.; solution vectors, residuals, etc. are Solver-LocalData. The given default values are overwritten by the simulationSettings when initializing the solver. SolverIterationData has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
maxStepSize	Real		0.	constant or maximum stepSize
minStepSize	Real		0.	minimum stepSize for static/dynamic
				solver; only used, if adaptive step is acti-
				vated
currentStepSize	Real		0.	stepSize of current step
numberOfSteps	Index		0	number of time steps (if fixed size); n
currentStepIndex	Index		0	current step index; i
adaptiveStep	bool		True	if true, the step size may be adaptively con-
				trolled

currentTime	Real	0.	holds the current simulation time, copy
			of state.current.time; interval is [start-
			Time,tEnd]; in static solver, duration is
			loadStepDuration
startTime	Real	0.	time at beginning of time integration
endTime	Real	0.	end time of static/dynamic solver
discontinuousIteration	Index	0	number of current discontinuous iteration
newtonSteps	Index	0	number of current newton steps
newtonStepsCount	Index	0	count total Newton steps
newtonJacobiCount	Index	0	count total Newton jacobian computations
rejectedModifiedNewtonSteps	Index	0	count the number of rejected modified
			Newton steps (switch to full Newton)
discontinuousIterationsCount	Index	0	count total number of discontinuous itera-
			tions (min. 1 per step)
ToString()	String		convert iteration statistics to string; used for
			displayStatistics option

# 6.3.4 SolverConvergenceData

Solver internal structure for convergence information: residua, iteration loop errors and error flags. For detailed behavior of these flags, visit the source code!.

SolverConvergenceData has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
stepReductionFailed	bool		False	true, if iterations over time/static steps
				failed (finally, cannot be recovered)
discontinuousIterationsFailed			False	true, if discontinuous iterations failed (may
	bool			be recovered if adaptive step is active)
linearSolverFailed	bool		False	true, if linear solver failed to factorize
newtonConverged	bool		False	true, if Newton has (finally) converged
newtonSolutionDiverged	bool		False	true, if Newton diverged (may be recov-
				ered)
jacobianUpdateRequested	bool		True	true, if a jacobian update is requested in
				modified Newton (determined in previous
				step)
massMatrixNotInvertible	bool		True	true, if mass matrix is not invertable during
				initialization or solution (explicit solver)
discontinuousIterationError	Real		0.	error of discontinuous iterations (contact,
				friction,) outside of Newton iteration
residual	Real		0.	current Newton residual
lastResidual	Real		0.	last Newton residual to determine contrac-
				tivity
contractivity	Real		0.	Newton contractivity = geometric decay of
				error in every step
errorCoordinateFactor	Real		1.	factor may include the number of system
				coordinates to reduce the residual

InitializeData()	void	initialize SolverConvergenceData by as-
		signing default values

### 6.3.5 SolverOutputData

Solver internal structure for output modes, output timers and counters. SolverOutputData has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
finishedSuccessfully	bool		False	flag is false until solver finshed successfully
				(can be used as external trigger)
verboseMode	Index		0	this is a copy of the solvers verboseMode
				used for console output
verboseModeFile	Index		0	this is a copy of the solvers verboseMode-
				File used for file
writeToSolutionFile	bool		False	if false, no solution file is generated and no
				file is written
writeToSolverFile	bool		False	if false, no solver output file is generated
				and no file is written
sensorValuesTemp	ResizableVector			temporary vector for per sensor values
				(overwritten for every sensor; usually con-
				tains last sensor)
lastSolutionWritten	Real		0.	simulation time when last solution has been
				written
lastSensorsWritten	Real		0.	simulation time when last sensors have
				been written
lastImageRecorded	Real		0.	simulation time when last image has been
				recorded
cpuStartTime	Real		0.	CPU start time of computation (starts
				counting at computation of initial condi-
				tions)
cpuLastTimePrinted	Real		0.	CPU time when output has been printed
				last time
InitializeData()	void			initialize SolverOutputData by assigning
				default values

### 6.3.6 MainSolverStatic

PyBind interface (trampoline) class for static solver. With this interface, the static solver and its substructures can be accessed via python. NOTE that except from SolveSystem(...), these functions are only intended for experienced users and they need to be handled with care, as unexpected crashes may happen if used inappropriate. Furthermore, the functions have a lot of overhead (performance much lower than internal solver) due to python interfaces, and should thus be used for small systems. To access the solver in python, write:

## solver = MainSolverStatic()

and hereafter you can access all data and functions via 'solver'. MainSolverStatic has the following items:

Name	type/function re- turn type	size	default value / func- tion args	description
timer	CSolverTimer		U	timer which measures the CPU time of solver sub functions
it	SolverIterationData			all information about iterations (steps, discontinuous iteration, newton,)
conv	SolverConvergence	Data		all information about tolerances, errors and residua
output	SolverOutputData			output modes and timers for exporting solver information and solution
newton	NewtonSettings			copy of newton settings from timeint or staticSolver
loadStepGeometricFactor	Real			multiplicative load step factor; this factor is computed from loadStepGeometric parameters in SolveSystem()
CheckInitialized()	bool		mainSystem	check if MainSolver and MainSystem are correctly initialized ==> otherwise raise SysError
ComputeLoadFactor()	Real		simulationSettings	for static solver, this is a factor in interval [0,1]; MUST be overwritten
GetSolverName()	std::string			get solver name - needed for output file header and visualization window
IsStaticSolver()	bool			return true, if static solver; needs to be over- written in derived class
GetSimulationEndTime()	Real		simulationSettings	compute simulation end time (depends on static or time integration solver)
ReduceStepSize()	bool		mainSystem, simula- tionSettings, severity	reduce step size (1normal, 2severe prob- lems); return true, if reduction was success- ful
IncreaseStepSize()	void		mainSystem, simula- tionSettings	increase step size if convergence is good
InitializeSolver()	bool		mainSystem, simula- tionSettings	initialize solverSpecific,data,it,conv; set/compute initial conditions (solver- specific!); initialize output files
PreInitializeSolverSpecific()	void		mainSystem, simula- tionSettings	pre-initialize for solver specific tasks; called at beginning of InitializeSolver, right after Solver data reset
InitializeSolverOutput()	void		mainSystem, simula- tionSettings	initialize output files; called from Initialize- Solver()
InitializeSolverPreChecks()	bool		mainSystem, simula- tionSettings	check if system is solvable; initialize dense/sparse computation modes
InitializeSolverData()	void		mainSystem, simula- tionSettings	initialize all data,it,conv; called from InitializeSolver()
InitializeSolverInitialCondition	s() void		mainSystem, simula- tionSettings	set/compute initial conditions (solver-specific!); called from InitializeSolver()

PostInitializeSolverSpecific()	void	mainSystem, simula- tionSettings	post-initialize for solver specific tasks; called at the end of InitializeSolver
ColveCrystom( )	bool	mainSystem, simula-	
SolveSystem()	DOOI	tionSettings	solve System: InitializeSolver, SolveSteps, FinalizeSolver
FinalizeSolver()	void	mainSystem, simula-	write concluding information (timer statis-
		tionSettings	tics, messages) and close files
SolveSteps()	bool	mainSystem, simula-	main solver part: calls multiple Initial-
		tionSettings	izeStep()/ DiscontinuousIteration()/ Fin-
			ishStep(); do step reduction if necessary;
			return true if success, false else
UpdateCurrentTime()	void	mainSystem, simula-	update currentTime (and load factor);
		tionSettings	MUST be overwritten in special solver class
InitializeStep()	void	mainSystem, simula-	initialize static step / time step; python-
_		tionSettings	functions; do some outputs, checks, etc.
FinishStep()	void	mainSystem, simula-	finish static step / time step; write output of
•		tionSettings	results to file
DiscontinuousIteration()	bool	mainSystem, simula-	perform discontinuousIteration for static
` ,		tionSettings	step / time step; CALLS ComputeNewton-
			Residual
Newton()	bool	mainSystem, simula-	perform Newton method for given solver
,		tionSettings	method
ComputeNewtonResidual()	void	mainSystem, simula-	compute residual for Newton method (e.g.
1		tionSettings	static or time step); store result in system-
			Residual
ComputeNewtonUpdate()	void	mainSystem, simula-	compute update for currentState from new-
1 1 1		tionSettings	tonSolution (decrement from residual and
			jacobian)
ComputeNewtonJacobian()	void	mainSystem, simula-	compute jacobian for newton method of
1		tionSettings	given solver method; store result in system-
			Jacobian
WriteSolutionFileHeader()	void	mainSystem, simula-	write unique file header, depending on stat-
,		tionSettings	ic/ dynamic simulation
WriteCoordinatesToFile()	void	mainSystem, simula-	write unique coordinates solution file
, ,		tionSettings	
IsVerboseCheck()	bool	level	return true, if file or console output is at or
,			above the given level
VerboseWrite()	void	level, str	write to console and/or file in case of level
GetODE2size()	Index		number of ODE2 equations in solver
GetODE1size()	Index		number of ODE1 equations in solver (not
			yet implemented)
GetAEsize()	Index		number of algebraic equations in solver
GetDataSize()	Index		number of data (history) variables in solver
GetSystemJacobian()	NumpyMatrix		get locally stored / last computed system
cetty oterrique obtain()	1 tamp j triadity		jacobian of solver
GetSystemMassMatrix()	NumpyMatrix		get locally stored / last computed mass ma-
See y Sterring and Strating	1 tampy water		trix of solver
GetSystemResidual()	NumpyVector		get locally stored / last computed system

GetNewtonSolution()	NumpyVector		get locally stored / last computed solution
			(=increment) of Newton
SetSystemJacobian()	void	systemJacobian	set locally stored system jacobian of solver;
			must have size nODE2+nODE1+nAE
SetSystemMassMatrix()	void	systemMassMatrix	set locally stored mass matrix of solver;
			must have size nODE2+nODE1+nAE
SetSystemResidual()	void	systemResidual	set locally stored system residual; must
			have size nODE2+nODE1+nAE
ComputeMassMatrix()	void	mainSystem, scalar-	compute systemMassMatrix (multiplied
		Factor=1.	with factor) in cSolver and return mass ma-
			trix
ComputeJacobianODE2RHS()	void	mainSystem, scalar-	set systemJacobian to zero and add jaco-
		Factor=1.	bian (multiplied with factor) of ODE2RHS
			to systemJacobian in cSolver
ComputeJacobianODE2RHS_t(	)	mainSystem, scalar-	add jacobian of ODE2RHS_t (multiplied
	void	Factor=1.	with factor) to systemJacobian in cSolver
ComputeJacobianAE()	void	mainSystem, scalar-	add jacobian of algebraic equations (mul-
		Factor_ODE2=1.,	tiplied with factor) to systemJacobian in
		scalarFac-	cSolver; the scalarFactors are scaling the
		tor_ODE2_t=1.,	derivatives w.r.t. ODE2 coordinates and
		velocityLevel=false	w.r.t. ODE2_t (velocity) coordinates; if ve-
			locityLevel == true, the constraints are eval-
			uated at velocity level
ComputeODE2RHS()	void	mainSystem	compute the RHS of ODE2 equations in sys-
			temResidual in range(0,nODE2)
ComputeAlgebraicEquations(	)	mainSystem, veloc-	compute the algebraic equations in sys-
	void	ityLevel=false	temResidual in range(nODE2+nODE1,
			nODE2+nODE1+nAE)

### 6.3.7 MainSolverImplicitSecondOrder

PyBind interface (trampoline) class for dynamic implicit solver. Note that this solver includes the classical Newmark method (set useNewmark True; with option of index 2 reduction) as well as the generalized-alpha method. With the interface, the dynamic implicit solver and its substructures can be accessed via python. NOTE that except from SolveSystem(...), these functions are only intended for experienced users and they need to be handled with care, as unexpected crashes may happen if used inappropriate. Furthermore, the functions have a lot of overhead (performance much lower than internal solver) due to python interfaces, and should thus be used for small systems. To access the solver in python, write

solver = MainSolverImplicitSecondOrder()

and hereafter you can access all data and functions via 'solver'. In this solver, user functions are possible to extend the solver at certain parts, while keeping the overal C++ performance.

MainSolverImplicitSecondOrder has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	

timer	CSolverTimer				timer which measures the CPU time of
tiller	Coorver Time				solver sub functions
it	SolverIterationData				all information about iterations (steps, dis-
	SorvernerationBata				continuous iteration, newton,)
conv	SolverConvergence	Data			all information about tolerances, errors and
Conv	Borverconvergence	Data			residua
output	SolverOutputData				output modes and timers for exporting
σιιριι	SolverOutputData				solver information and solution
newton	NewtonSettings				copy of newton settings from timeint or
newton	Newtonsettings				staticSolver
newmarkBeta	Real				
newmarkbeta	Real				copy of parameter in timeIntegration.generalizedAlpha
newmarkGamma	Real				
newmarkGamma	Real				copy of parameter in timeIntegra-
.1.114	D 1				tion.generalizedAlpha
alphaM	Real				copy of parameter in timeIntegra-
1.1. E	D 1				tion.generalizedAlpha
alphaF	Real				copy of parameter in timeIntegra-
15. 1					tion.generalizedAlpha
spectralRadius	Real				copy of parameter in timeIntegra-
					tion.generalizedAlpha
factJacAlgorithmic	Real				locally computed parameter from general-
					izedAlpha parameters
CheckInitialized()	bool		mainSystem		check if MainSolver and MainSystem are
					correctly initialized ==> otherwise raise Sy-
					sError
ComputeLoadFactor()	Real		simulationSett	ings	for static solver, this is a factor in interval
					[0,1]; MUST be overwritten
GetAAlgorithmic()	NumpyVector				get locally stored / last computed algorith-
					mic accelerations
GetStartOfStepStateAAlgorithm	nic()				get locally stored / last computed algorith-
	NumpyVector				mic accelerations at start of step
SetUserFunctionUpdateCurren	tTime()		mainSystem,	user-	set user function
	void		Function		
Set User Function Initialize Step (.	)		mainSystem,	user-	set user function
	void		Function		
SetUserFunctionFinishStep()			mainSystem,	user-	set user function
	void		Function		
SetUserFunctionDiscontinuous	Iteration()		mainSystem,	user-	set user function
	void		Function		
SetUserFunctionNewton()	void		mainSystem,	user-	set user function
			Function		
SetUserFunctionComputeNewt	onUpdate()		mainSystem,	user-	set user function
1	void		Function		
SetUserFunctionComputeNewt	onResidual()		mainSystem,	user-	set user function
r	void		Function		
SetUserFunctionComputeNewt			mainSystem,	user-	set user function
	void		Function		
GetSolverName()	std::string				get solver name - needed for output file
coloried which					header and visualization window
					ricader and visuanzadon window

IsStaticSolver()	bool		return true, if static solver; needs to be over- written in derived class
GetSimulationEndTime()	Real	simulationSettings	compute simulation end time (depends on static or time integration solver)
ReduceStepSize()	bool	mainSystem, simula-	reduce step size (1normal, 2severe prob-
reducestepsize()	5001	tionSettings, severity	lems); return true, if reduction was success-
		tionSettings, severity	ful
IncreaseStepSize()	void	mainSystem, simula-	increase step size if convergence is good
increasestepsize()	Void		increase step size ii convergence is good
Televity (Colored )	1 1	tionSettings	initialize solverSpecific,data,it,cony;
InitializeSolver()	bool	mainSystem, simula-	1 , , , ,
		tionSettings	set/compute initial conditions (solver-
			specific!); initialize output files
PreInitializeSolverSpecific()		mainSystem, simula-	pre-initialize for solver specific tasks; called
	void	tionSettings	at beginning of InitializeSolver, right after
			Solver data reset
InitializeSolverOutput()	void	mainSystem, simula-	initialize output files; called from Initialize-
		tionSettings	Solver()
InitializeSolverPreChecks()		mainSystem, simula-	check if system is solvable; initialize
	bool	tionSettings	dense/sparse computation modes
InitializeSolverData()	void	mainSystem, simula-	initialize all data, it, conv; called from Initial-
		tionSettings	izeSolver()
InitializeSolverInitialCondition	s()	mainSystem, simula-	set/compute initial conditions (solver-
	void	tionSettings	specific!); called from InitializeSolver()
PostInitializeSolverSpecific()		mainSystem, simula-	post-initialize for solver specific tasks;
1	void	tionSettings	called at the end of InitializeSolver
SolveSystem()	bool	mainSystem, simula-	solve System: InitializeSolver, SolveSteps,
, , ,		tionSettings	FinalizeSolver
FinalizeSolver()	void	mainSystem, simula-	write concluding information (timer statis-
,		tionSettings	tics, messages) and close files
SolveSteps()	bool	mainSystem, simula-	main solver part: calls multiple Initial-
correcteps()	2001	tionSettings	izeStep()/ DiscontinuousIteration()/ Fin-
		l deficettings	ishStep(); do step reduction if necessary;
			return true if success, false else
UpdateCurrentTime()	void	mainSystem, simula-	update currentTime (and load factor);
opuate current rime ()	Void	tionSettings	MUST be overwritten in special solver class
InitializeStep()	void	mainSystem, simula-	initialize static step / time step; python-
minanzestep()	Void		
Einigh Cton( )	: 1	tionSettings	functions; do some outputs, checks, etc.
FinishStep()	void	mainSystem, simula-	finish static step / time step; write output of
D: (: 1: (: ( )	1 1	tionSettings	results to file
DiscontinuousIteration()	bool	mainSystem, simula-	perform discontinuousIteration for static
		tionSettings	step / time step; CALLS ComputeNewton-
			Residual
Newton()	bool	mainSystem, simula-	perform Newton method for given solver
		tionSettings	method
ComputeNewtonResidual()	void	mainSystem, simula-	compute residual for Newton method (e.g.
		tionSettings	static or time step); store result in system-
			Residual
ComputeNewtonUpdate()	void	mainSystem, simula-	compute update for currentState from new-
		tionSettings	tonSolution (decrement from residual and
	1		jacobian)

ComputeNewtonJacobian()	void	mainSystem, simula-	compute jacobian for newton method of
1		tionSettings	given solver method; store result in system-
			Jacobian
WriteSolutionFileHeader()	void	mainSystem, simula-	write unique file header, depending on stat-
		tionSettings	ic/ dynamic simulation
WriteCoordinatesToFile()	void	mainSystem, simula-	write unique coordinates solution file
		tionSettings	
IsVerboseCheck()	bool	level	return true, if file or console output is at or
			above the given level
VerboseWrite()	void	level, str	write to console and/or file in case of level
GetODE2size()	Index		number of ODE2 equations in solver
GetODE1size()	Index		number of ODE1 equations in solver (not
			yet implemented)
GetAEsize()	Index		number of algebraic equations in solver
GetDataSize()	Index		number of data (history) variables in solver
GetSystemJacobian()	NumpyMatrix		get locally stored / last computed system
			jacobian of solver
GetSystemMassMatrix()	NumpyMatrix		get locally stored / last computed mass ma-
			trix of solver
GetSystemResidual()	NumpyVector		get locally stored / last computed system
			residual
GetNewtonSolution()	NumpyVector		get locally stored / last computed solution
			(=increment) of Newton
SetSystemJacobian()	void	systemJacobian	set locally stored system jacobian of solver;
			must have size nODE2+nODE1+nAE
SetSystemMassMatrix()	void	systemMassMatrix	set locally stored mass matrix of solver;
C (C ( P : 1 1/ )	• 1	, D : 1 1	must have size nODE2+nODE1+nAE
SetSystemResidual()	void	systemResidual	set locally stored system residual; must
Comments Mana Matrice( )	: 1	iCt	have size nODE2+nODE1+nAE
ComputeMassMatrix()	void	mainSystem, scalar- Factor=1.	compute systemMassMatrix (multiplied
		ractor=1.	with factor) in cSolver and return mass matrix
ComputeJacobianODE2RHS()	woid	mainSystem, scalar-	set systemJacobian to zero and add jaco-
Compute Jacobian ODE 2Ki 15()	Void	Factor=1.	bian (multiplied with factor) of ODE2RHS
		ractor-1.	to systemJacobian in cSolver
ComputeJacobianODE2RHS_t(.	)	mainSystem, scalar-	add jacobian of ODE2RHS_t (multiplied
compared and a second	void	Factor=1.	with factor) to systemJacobian in cSolver
ComputeJacobianAE()	void	mainSystem, scalar-	add jacobian of algebraic equations (mul-
Comparejacozana iz()	Voice	Factor_ODE2=1.,	tiplied with factor) to systemJacobian in
		scalarFac-	cSolver; the scalarFactors are scaling the
		tor_ODE2_t=1.,	derivatives w.r.t. ODE2 coordinates and
		velocityLevel=false	w.r.t. ODE2_t (velocity) coordinates; if ve-
			locityLevel == true, the constraints are eval-
			uated at velocity level
ComputeODE2RHS()	void	mainSystem	compute the RHS of ODE2 equations in sys-
. ' '			temResidual in range(0,nODE2)
ComputeAlgebraicEquations(	)	mainSystem, veloc-	compute the algebraic equations in sys-
1 0 1 (	void	ityLevel=false	temResidual in range(nODE2+nODE1,
			nODE2+nODE1+nAE)

# Chapter 7

# 3D Graphics Visualization

The 3D graphics visualization window is kept simple, but useful to see the animated results of the multibody system.

## 7.1 Mouse input

The following table includes the mouse functions.

Button	action	remarks
left mouse button	move model	keep left mouse button pressed to move the model in the
		current x/y plane
right mouse button	rotate model	keep right mouse button pressed to rotate model around
		current current $X_1/X_2$ axes
mouse wheel	zoom	use mouse wheel to zoom (on touch screens 'pinch-to-
		zoom' might work as well)

## 7.2 Keyboard input

The following table includes the keyboard shortcuts available in the window.

Key(s)	action	remarks
1,2,3,4 or 5	visualization update speed	the entered digit controls the visualization update, which
		can be changed from 1=1 update per 20ms to 5=1 update
		per 100s
'.' or KEYPAD '+'	zoom in	zoom one step into scene (additionally press CTRL to per-
		form small zoom step)
',' or KEYPAD '-'	zoom out	zoom one step out of scene (additionally press CTRL to
		perform small zoom step)
0 or KEYPAD '0'	reset rotation	set rotation such that the scene is oriented in the x/y plane
A	zoom all	set zoom such that the whole scene is visible
CURSOR UP, DOWN,	move scene	use coursor keys to move the scene up, down, left, and
		right

С	show/hide connectors	pressing this key switches the visibility of connectors
CTRL+C	show/hide connector num-	pressing this key switches the visibility of connector num-
	bers	bers
В	show/hide bodies	pressing this key switches the visibility of bodies
CTRL+B	show/hide body numbers	pressing this key switches the visibility of body numbers
L	show/hide loads	pressing this key switches the visibility of loads
CTRL+L	show/hide load numbers	pressing this key switches the visibility of load numbers
M	show/hide markers	pressing this key switches the visibility of markers
CTRL+M	show/hide marker numbers	pressing this key switches the visibility of marker numbers
N	show/hide nodes	pressing this key switches the visibility of nodes
CTRL+N	show/hide node numbers	pressing this key switches the visibility of node numbers
S	show/hide sensors	pressing this key switches the visibility of sensors
CTRL+S	show/hide sensor numbers	pressing this key switches the visibility of sensor numbers
Q	stop simulation	simulation is stopped and cannot be recovered
X	execute command	open dialog to enter a python command (in global python
		scope)
V	visualization settings	open dialog to modify visualization settings
ESCAPE	close render window	stops the simulation and closes the render window
SPACE	continue simulation	if simulation is paused, it can be continued by pressing
		space; use SHIFT+SPACE to continuously activate 'con-
		tinue simulation'

# **Chapter 8**

# Solver

## 8.1 Jacobian computation

The computation of the global jacobian matrix is time consuming for the static solver or implicit time integration. The equations are split into  $2^{nd}$  order differential equations,  $1^{st}$  order differential equations and algebraic equationsparts. From this structure, in the general non-symmetric case,  $3 \times 3$  submatrices result for the jacobian. Every submatrix of the jacobian has a certain meaning and needs to be computed individually. Specifically, in implicit time integration the  $2^{nd}$  order differential equations× $2^{nd}$  order differential equationsterm includes the (tangent) stiffness matrix and the mass matrix.

For efficient computation purpose, the elements provide a list of flags, which determine the dependencies as well as available (analytical) functions to compute the local (object) jacobian:

- ODE2\_ODE2 . . . derivative of ODE2 equations with respect to ODE2 variables
- ODE2\_ODE2\_t ... derivative of ODE2 equations with respect to ODE2\_t (velocity) variables
- ODE1\_ODE1 ... derivative of ODE1 equations with respect to ODE1 variables (NOT YET AVAILABLE)
- AE\_ODE2 ... derivative of AE (algebraic) equations with respect to ODE2 variables
- AE\_ODE2\_t ... derivative of AE (algebraic) equations with respect to ODE2\_t (velocity) variables (NOT YET AVAILABLE)
- AE\_ODE1 . . . derivative of AE (algebraic) equations with respect to ODE1 variables (NOT YET AVAILABLE)
- AE\_AE ... derivative of AE (algebraic) equations with respect to AE variables

If one of these flags is set (binary; e.g.ODE2\_ODE2 + ODE2\_ODE2\_t), then the according local jacobian is computed and assembled into the global jacobian in the static or implicit dynamic solver.

Jacobians can also be supplied in analytical (function) form, which is indicated by an additional flag with the same name but an additional term '\_function', e.g. 'ODE2\_ODE2\_function' indicates that the derivative of ODE2 equations with respect to its ODE2 coordinates is provided in an analytical form (this is the tangent stiffness matrix).

Two **object** functions are used to compute the local jacobians:

- ComputeJacobianODE2\_ODE2(Matrix& jacobian, Matrix& jacobian\_ODE2\_t): computes the ODE2\_ODE2 and ODE2\_ODE2\_t jacobians
- ComputeJacobianAE(Matrix& jacobian, Matrix& jacobian\_AE): computes the AE\_ODE2 and AE\_AE jacobians of the object ITSELF

Two connector functions are used to compute the local jacobians, using MarkerData:

- ComputeJacobianODE2\_ODE2(Matrix& jacobian, Matrix& jacobian\_ODE2\_t, const MarkerDataStructure& markerData): computes the ODE2\_ODE2 and ODE2\_ODE2\_t jacobians of the connector; e.g. for spring-damper
- ComputeJacobianAE(Matrix& jacobian, Matrix& jacobian\_AE, const MarkerDataStructure& marker-Data): computes the AE\_ODE2 and AE\_AE jacobians of the connector; e.g. for coordinate constraint

The system jacobian has the structure (2= ODE2, 1= ODE1,  $\lambda$  = AE;  $\bar{\mathbf{f}}_2$  = according system residual including dynamic (mass matrix) terms in time integration;  $\mathbf{g}_{\lambda}$  = algebraic equations):

$$\begin{bmatrix} \frac{\partial \bar{\mathbf{f}}_2}{\partial \mathbf{q}_2} & 0 & \left(\frac{\partial \mathbf{g}_{\lambda}}{\partial \mathbf{q}_2}\right)^T \\ 0 & \frac{\partial \mathbf{f}_1}{\partial \mathbf{q}_1} & \left(\frac{\partial \mathbf{g}_{\lambda}}{\partial \mathbf{q}_1}\right)^T \\ \frac{\partial \mathbf{g}_{\lambda}}{\partial \mathbf{q}_2} & \frac{\partial \mathbf{g}_{\lambda}}{\partial \mathbf{q}_1} & \frac{\partial \mathbf{g}_{\lambda}}{\partial \mathbf{q}_{\lambda}} \end{bmatrix}$$
(8.1)

Two system jacobian functions are currently available:

- JacobianODE2RHS(temp, newton, factorODE2, factorODE2\_t, jacobian\_ODE2\_t): compute analytical/numerical differentiation of ODE2RHS w.r.t. ODE2 and ODE2\_t coordinates; if analytical/functional version of jacobian is available and Newton flag 'useNumericalDifferentiation'=false, then the according jacobian is computed by its according function; results are 2 jacobians; the factors 'factor\_ODE2' and 'factor\_ODE2\_t' are used to scale the two jacobians; if a factor is zero, the according jacobian is not computed.
- JacobianAE(temp, newton, jacobian, factorODE2, velocityLevel, fillIntoSystemMatrix): compute constraint jacobian of AE with respect to ODE2 ('fillIntoSystemMatrix'=true: also w.r.t. [ODE1] and AE) coordinates  $\rightarrow$  direct computation given by access functions; 'factorODE2' is used to scale the ODE2-part of the jacobian (to avoid postmultiplication); velocityLevel = true: velocityLevel constraints are used, if available; 'fillIntoSystemMatrix'=true: fill in both  $\frac{\partial \tilde{f}_{\lambda}}{\partial q_2}$ ,  $\frac{\partial \tilde{f}_{\lambda}}{\partial q_2}$  AND  $\frac{\partial \tilde{f}_{\lambda}}{\partial q_2}$  at according locations into system matrix; 'fillIntoSystemMatrix'=false: (this is a temporary/WORKAROUND function):

The system jacobian functions compute the local jacobians either by means of a provided function or numerically, using the 'NumericalDifferentiation' settings of 'Newton'.

## 8.2 Implicit trapezoidal rule solver

This solver represents a class of solvers, which are based on the implicit trapezoidal rule. This integration includes the start value and the end value of a time step for the interpolation, thus being a trapezoidal integration rule. In some specializations, e.g. the Newmark method, the interpolation might only depend on the start value or the end value.

Most important representations of this rule:

- Trapezoidal rule (= Newmark with  $\beta = \frac{1}{4}$  and  $\gamma = \frac{1}{2}$ )
- Newmark method
- Generalized- $\alpha$  method (= generalized Newmark method with additional parameters

## 8.3 Representation of coordinates and equations of motion

Nomenclature:

- '2' ... second order equations (usually of a mechanical system)
- '1' ... first order equations (e.g. of a controller, fluid, etc.)
- $'\lambda'$  ... algebraic equations (usually of joints)
- M ... mass matrix
- q<sub>2</sub> ... 'displacement' coordinates of ODE2 equations
- $\dot{q}_2 \dots$  'velocity' coordinates of ODE2 equations
- $\bullet~\ddot{q}_2\dots$  'acceleration' coordinates of ODE2 equations
- **q**<sub>1</sub> ... coordinates of ODE1 equations
- **q**<sub>1</sub> ... 'velocity' coordinates of ODE1 equations
- $\mathbf{q}_{\lambda}$  ... Lagrange multipliers
- f<sub>2</sub> ... right-hand-side of ODE2 equations (except for action of joint reaction forces)
- f<sub>1</sub> ... right-hand-side of ODE1 equations
- g ... algebraic equations
- K ... (tangent) stiffness matrix
- D ... damping/gyroscopic matrix
- *h* . . . step size of time integration method

The equations of motion in EXUDYN are represented as

$$\mathbf{M}\ddot{\mathbf{q}}_{2} + \frac{\partial \mathbf{g}}{\partial \mathbf{q}_{2}^{T}} \mathbf{q}_{\lambda} = \mathbf{f}_{2}(\mathbf{q}_{2}, \dot{\mathbf{q}}_{2}, t)$$
 (8.2)

$$\dot{\mathbf{q}}_1 + \frac{\partial \mathbf{g}}{\partial \mathbf{q}_1^{\mathrm{T}}} \mathbf{q}_{\lambda} = \mathbf{f}_1(\mathbf{q}_1, t) \tag{8.3}$$

$$\mathbf{g}(\mathbf{q}_2, \dot{\mathbf{q}}_2, \mathbf{q}_1, \mathbf{q}_{\lambda}, t) = 0 \tag{8.4}$$

Note that the term  $\frac{\partial \mathbf{g}}{\partial q_1} \mathbf{q}_{\lambda}$  is not yet implemented, such that algebraic equations may not yet depend on 1<sup>st</sup> order differential equations coordinates.

It is important to note, that for linear mechanical systems,  $f_2$  becomes

$$\mathbf{f}_{2}^{lin} = \mathbf{f}^{a} - \mathbf{K}\mathbf{q}_{2} - \mathbf{D}\dot{\mathbf{q}}_{1} \tag{8.5}$$

in which  $f^a$  represents applied forces and K and D become part of the system Jacobian for time integration.

#### 8.4 Newmark method

The Newmark method obtains two parameters  $\beta$  and  $\gamma$ . The main ideas are

- Interpolate the displacements and the velocities linearly using the accelerations of the beginning of the time step (subindex '0') and the end of the time step (subindex 'T').
- Solve the system equations at the end of the time step for the unknown accelerations as well as for 1<sup>st</sup> order differential equations and algebraic equations coordinates.

We abbreviate the unknown accelerations by  $\ddot{\mathbf{q}} = \mathbf{a}$  and the unknown velocities  $\dot{\mathbf{q}} = \mathbf{v}$ . Thus, the equations at the end of the time step read (bring all terms to LHS):

$$\mathbf{f}_{2}^{\text{Newmark}} = \mathbf{M} \mathbf{a}_{2}^{T} + \frac{\partial \mathbf{g}}{\partial \mathbf{q}_{2}^{T}} \mathbf{q}_{\lambda}^{T} - \mathbf{f}_{2}(\mathbf{q}_{2}^{T}, \dot{\mathbf{q}}_{2}^{T}, t) = 0$$
(8.6)

$$\mathbf{f}_{1}^{\text{Newmark}} = \mathbf{v}_{1}^{T} + \frac{\partial \mathbf{g}}{\partial \mathbf{q}_{1}^{T}} \mathbf{q}_{\lambda}^{T} - \mathbf{f}_{1}(\mathbf{q}_{1}^{T}, t) = 0$$
(8.7)

$$\mathbf{f}_{\lambda}^{\text{Newmark}} = \mathbf{g}(\mathbf{q}_{2}^{T}, \dot{\mathbf{q}}_{2}^{T}, \mathbf{q}_{1}^{T}, \mathbf{q}_{\lambda}^{T}, t) = 0$$
(8.8)

Within Eq. (8.6), the 2<sup>nd</sup> order differential equations displacements and velocities and for 1<sup>st</sup> order differential equations coordinates are given by

$$\mathbf{q}_{2}^{T} = \mathbf{q}_{2}^{0} + h\dot{\mathbf{q}}_{2}^{0} + h^{2}(\frac{1}{2} - \beta)\mathbf{a}_{2}^{0} + h^{2}\beta\mathbf{a}_{2}^{T}$$

$$\dot{\mathbf{q}}_{2}^{T} = \dot{\mathbf{q}}_{2}^{0} + h(1 - \gamma)\mathbf{a}_{2}^{0} + h\gamma\mathbf{a}_{2}^{T}$$

$$\mathbf{q}_{1}^{T} = \mathbf{q}_{1}^{0} + h(1 - \gamma)\mathbf{v}_{1}^{0} + h\gamma\mathbf{v}_{1}^{T}$$
(8.9)

The unknowns for the Newton method are

$$\mathbf{q}^{\text{Newton}} = \begin{bmatrix} \mathbf{a}_2^T \\ \mathbf{v}_1^T \\ \mathbf{q}_{\Lambda}^T \end{bmatrix}$$
 (8.10)

For the Newton method, we need to compute an update for the unknowns Eq. (8.10), using the known residual  $\mathbf{r}_{i-1}$  and the inverse of the Jacobian  $\mathbf{J}_{i-1}$  of step i-1,

$$\mathbf{q}_{i}^{\text{Newton}} = \mathbf{q}_{i-1}^{\text{Newton}} - \mathbf{J}^{-1} \left( \mathbf{q}_{i-1}^{\text{Newton}} \right) \mathbf{r} \left( \mathbf{q}_{i-1}^{\text{Newton}} \right)$$
(8.11)

The Jacobian has the following  $3 \times 3$  structure,

$$\mathbf{J} = \begin{bmatrix} \mathbf{J}_{22} & \mathbf{J}_{21} & \mathbf{J}_{2\lambda} \\ \mathbf{J}_{12} & \mathbf{J}_{11} & \mathbf{J}_{1\lambda} \\ \mathbf{J}_{\lambda 2} & \mathbf{J}_{\lambda 1} & \mathbf{J}_{\lambda \lambda} \end{bmatrix}$$
(8.12)

Note that currently, all terms related to '1' are not implemented. The other terms are only evaluated in the specific jacobian computation, if according flags are set in GetAvailableJacobian(). Otherwise, the constraint needs to be implemented as object which can employ all kinds of coordinates, which do not depend on coordinates of markers.

The available Jacobians need to be rewritten in terms of the Newton unknowns (8.10), and thus read

$$J_{22} = \frac{\partial \mathbf{f}_{2}^{\text{Newmark}}}{\partial \mathbf{a}_{2}^{\text{T}}} = \frac{\partial \mathbf{f}_{2}^{\text{Newmark}}}{\partial \mathbf{q}_{2}^{\text{T}}} \frac{\mathbf{q}_{2}}{\mathbf{a}_{2}^{\text{T}}} + \frac{\partial \mathbf{f}_{2}^{\text{Newmark}}}{\partial \dot{\mathbf{q}}_{2}^{\text{T}}} \frac{\dot{\mathbf{q}}_{2}}{\mathbf{a}_{2}^{\text{T}}} = h^{2}\beta \mathbf{K} + h\gamma \mathbf{D}$$

$$J_{2\lambda} = \frac{\partial \mathbf{f}_{2}^{\text{Newmark}}}{\partial \mathbf{q}_{\lambda}^{\text{T}}} = \frac{\partial \mathbf{g}}{\partial \mathbf{q}_{2}^{\text{T}}}$$

$$J_{\lambda 2} = \frac{\partial \mathbf{f}_{\lambda}^{\text{Newmark}}}{\partial \mathbf{a}_{2}^{\text{T}}} = \frac{\partial \mathbf{g}}{\partial \mathbf{a}_{2}^{\text{T}}} = \frac{\partial \mathbf{g}}{\partial \mathbf{q}_{2}^{\text{T}}} \frac{\mathbf{q}_{2}}{\mathbf{q}_{2}^{\text{T}}} + \frac{\partial \mathbf{g}}{\partial \dot{\mathbf{q}}_{2}^{\text{T}}} \frac{\dot{\mathbf{q}}_{2}}{\mathbf{a}_{2}^{\text{T}}} = h^{2}\beta \frac{\partial \mathbf{g}}{\partial \mathbf{q}_{2}^{\text{T}}} + h\gamma \frac{\partial \mathbf{g}}{\partial \dot{\mathbf{q}}_{2}^{\text{T}}}$$

$$J_{\lambda \lambda} = \frac{\partial \mathbf{f}_{\lambda}^{\text{Newmark}}}{\partial \mathbf{q}_{\lambda}^{\text{T}}} = \frac{\partial \mathbf{g}}{\partial \mathbf{q}_{\lambda}^{\text{T}}}$$

$$(8.13)$$

Note that the derivative  $\frac{\mathbf{q}_2}{\mathbf{a}_2^T}$  follows from the Newmark interpolation (8.9) using the relation between  $\mathbf{q}_2^T$  and  $\mathbf{a}_2^T$ . The tangent stiffness matrix  $\mathbf{K}$  must also include derivatives of applied forces  $\mathbf{f}^n$ , which is currently not implemented. Furthermore, the Jacobian is not symmetric, which could be obtained by according scaling.

Once an update  $\mathbf{q}_i^{\text{Newton}}$  has been computed, the interpolation formulas (8.9) need to be evaluated before the next residual and Jacobian can be computed.

# **Chapter 9**

# References

coming soon!

# Chapter 10

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