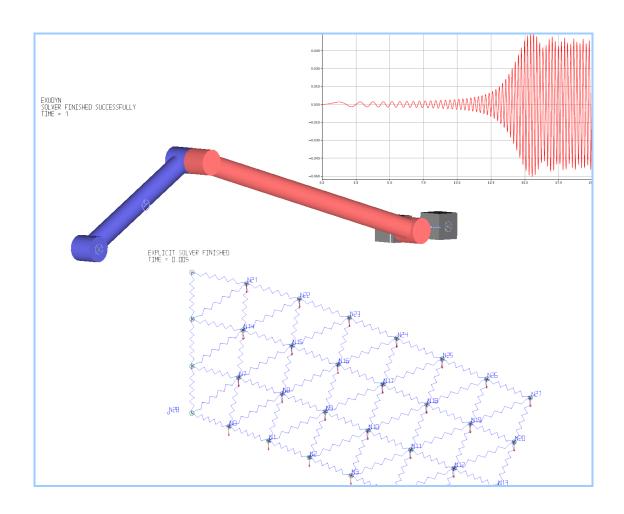
## Flexible Multibody Dynamics Systems with Python and C++

# **EXUDYN**

(flexible multibody dynamics)

## User documentation



EXUDYN version = 0.1.272

University of Innsbruck, Department of Mechatronics, January 31, 2020,

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# **Contents**

1	Get	Getting Started			
	1.1	Gettir	ng started	1	
		1.1.1	What is EXUDYN?	1	
		1.1.2	Who is developing EXUDYN?	2	
		1.1.3	How to link EXUDYN with Python (recommended for beginners)?	2	
		1.1.4	How to install EXUDYN and using the C++ code (advanced)?	3	
		1.1.5	Goals of EXUDYN	3	
		1.1.6	Run a simple example in Spyder	3	
	1.2	FAQ -	- Frequently asked questions	5	
2	Ove	erview (	on EXUDYN	7	
	2.1	Modu	ıle structure	7	
		2.1.1	Overview of modules	7	
		2.1.2	Conventions: items, indices, coordinates	8	
	2.2	Items	: Nodes, Objects, Loads, Markers, Sensors,	10	
		2.2.1	Nodes	10	
		2.2.2	Objects	10	
		2.2.3	Markers	11	
		2.2.4	Loads	11	
		2.2.5	Sensors	11	
		2.2.6	Reference coordinates and displacements	12	
	2.3	Exudy	yn Basics	12	
		2.3.1	Interaction with the EXUDYN module	12	
		2.3.2	Simulation settings	12	
		2.3.3	Visualization settings	13	
		2.3.4	Solver	14	
		2.3.5	Generating output and results	14	
		2.3.6	Graphics pipeline	17	
		2.3.7	Generating animations	19	
	2.4	C++ (	Code	20	
		2.4.1	Focus of the C++ code	20	
		242	C++ Code structure	21	

		2.4.3	C++ Code: Modules	21				
		2.4.4	Code style and conventions	22				
		2.4.5	Notation conventions	23				
		2.4.6	No-abbreviations-rule	23				
	2.5	Chang	ges	24				
3	Tuto	orial		27				
4	Pyth	Python-C++ command interface						
	4.1	1 EXUDYN						
	4.2	Syster	mContainer	35				
	4.3	MainSystem						
		4.3.1	MainSystem: Node	37				
		4.3.2	MainSystem: Object	38				
		4.3.3	MainSystem: Marker	40				
		4.3.4	MainSystem: Load	41				
		4.3.5	MainSystem: Sensor	41				
	4.4	Syster	mData	42				
		4.4.1	SystemData: Access coordinates	43				
		4.4.2	SystemData: Get object local-to-global (LTG) coordinate mappings	45				
	4.5	Type definitions						
		4.5.1	OutputVariableType	46				
		4.5.2	ConfigurationType	47				
		4.5.3	LinearSolverType	47				
5	Objects, nodes, markers, loads and sensors reference manual 49							
	5.1	List of	f Items	49				
	5.2	Nodes	s	50				
		5.2.1	NodePoint	50				
		5.2.2	NodePoint2D	51				
		5.2.3	NodeRigidBodyEP	52				
		5.2.4	NodeRigidBody2D	53				
		5.2.5	NodePoint2DSlope1	54				
		5.2.6	NodeGenericODE2	55				
		5.2.7	NodeGenericData	56				
		5.2.8	NodePointGround	57				
	5.3	Objects						
		5.3.1	ObjectMassPoint	58				
		5.3.2	ObjectMassPoint2D	58				
		5.3.3	ObjectRigidBody	59				
		5.3.4	ObjectRigidBody2D	60				
		535	Object ANCFC able 2D	61				

		5.3.6	ObjectALEANCFCable2D			
		5.3.7	ObjectGround			
		5.3.8	ObjectConnectorSpringDamper			
		5.3.9	ObjectConnectorCartesianSpringDamper			
		5.3.10	ObjectConnectorCoordinateSpringDamper			
		5.3.11	ObjectConnectorDistance			
		5.3.12	ObjectConnectorCoordinate			
		5.3.13	ObjectContactCoordinate			
		5.3.14	ObjectContactCircleCable2D			
		5.3.15	ObjectContactFrictionCircleCable2D			
		5.3.16	ObjectJointSliding2D			
		5.3.17	ObjectJointALEMoving2D			
		5.3.18	ObjectJointRevolute2D			
		5.3.19	ObjectJointPrismatic2D			
	5.4	Marke	rs			
		5.4.1	MarkerBodyMass			
		5.4.2	MarkerBodyPosition			
		5.4.3	MarkerBodyRigid			
		5.4.4	MarkerNodePosition			
		5.4.5	MarkerNodeRigid			
		5.4.6	MarkerNodeCoordinate			
		5.4.7	MarkerBodyCable2DShape			
		5.4.8	MarkerBodyCable2DCoordinates			
	5.5	Loads				
		5.5.1	LoadForceVector			
		5.5.2	LoadTorqueVector			
		5.5.3	LoadMassProportional			
		5.5.4	LoadCoordinate			
	5.6	Sensor	rs			
		5.6.1	SensorNode			
	5.7	Graph	icsData			
6	6 EXUDYN Settings					
-	6.1		Settings 87 Ation settings			
	0.1	6.1.1	SolutionSettings			
		6.1.2	NumericalDifferentiationSettings			
		6.1.3	NewtonSettings			
		6.1.4	Generalized Alpha Settings			
		6.1.5	TimeIntegrationSettings			
		6.1.6	StaticSolverSettings			
		6.1.7	SimulationSettings			
	6.2		ization settings			

10 License						
9	Refe	erences		119		
	8.4	Newm	nark method	117		
	8.3	•	sentation of coordinates and equations of motion	116		
	8.2		it trapezoidal rule solver	116		
	8.1	-	an computation			
8	Solv			115		
		·	ard niput			
	7.1 7.2		ard input			
,	7.1	-		113		
7	3D (	Graphic	es Visualization	113		
		6.3.7	$Main Solver Implicit Second Order \ \dots $	109		
		6.3.6	MainSolverStatic	106		
		6.3.5	SolverOutputData	105		
		6.3.4	SolverConvergenceData	104		
		6.3.3	SolverIterationData	104		
		6.3.2	SolverLocalData	103		
		6.3.1	CSolverTimer	102		
	6.3		substructures	102		
			VisualizationSettings	101		
			VSettingsSensors	101		
		6.2.11	VSettingsLoads	100		
		6.2.10	VSettingsMarkers	100		
		6.2.9	VSettingsConnectors	99		
		6.2.8	VSettingsBodies	99		
		6.2.7	VSettingsBeams	99		
		6.2.6	VSettingsNodes	98		
		6.2.5	VSettingsExportImages	98		
		6.2.4	VSettingsContour	97		
		6.2.3	VSettingsOpenGL	96		
		6.2.2	VSettingsWindow	95		
		6.2.1	VSettingsGeneral	94		

## Chapter 1

# **Getting Started**

The documentation for EXUDYN is split into this introductory section, including a quick start up, code structure and important hints, as well as a couple of sections containing references to the available Python interfaces to interact with EXUDYN and finally some information on theory (e.g., 'Solver').

EXUDYN is hosted on GitHub:

• web: https://github.com/jgerstmayr/EXUDYN/wiki

For any comments, requests, issues, bug reports, send an email to:

• email: reply.exudyn@gmail.com

Thanks for your contribution!

## 1.1 Getting started

This section will show:

- 1. What is EXUDYN?
- 2. Who is developing EXUDYN?
- 3. How to install EXUDYN
- 4. How to link EXUDYN and Python
- 5. Goals of EXUDYN
- 6. Run a simple example in Spyder
- 7. FAQ Frequently asked questions

#### 1.1.1 What is EXUDYN?

EXUDYN is a C++ based Python library for efficient simulation of flexible multibody dynamics systems. It is designed to easily set up complex multibody models, consisting of rigid and flexible bodies with joints, loads and other components.

The formulation is mostly based on redundant coordinates. This means that computational objects (rigid bodies, flexible bodies, ...) are added as independent bodies to the system. Hereafter,

connectors (e.g., springs or constraints) are used to interconnect the bodies. The connectors are using Markers on the bodies as interfaces, in order to transfer forces and displacements. For details on the interaction of nodes, objects, markers and loads see Section 2.2.

#### 1.1.2 Who is developing EXUDYN?

EXUDYN is currently (1-2020) developed at the University of Innsbruck. In the first phase most of the core code has been (and still is) written by Johannes Gerstmayr, implementing ideas of earlier developments of HOTINT. 15 years of development led to a lot of lessions learned.

Some specific codes regarding pybind interface and parallelization have been written by Stefan Holzinger, who also supports the upload to GitLab. Important discussions with researchers from the community where important for the design and development of EXUDYN, where we like to mention Joachim Schöberl from TU-Vienna who influenced the design of the code. During a Comet-K2 cooperation project, several discussions with the TMECH/LCM group in Linz influenced the code development.

The cooperation and funding within the EU H2020-MSCA-ITN project 'Joint Training on Numerical Modelling of Highly Flexible Structures for Industrial Applications' will support the further development of the code.

## 1.1.3 How to link EXUDYN with Python (recommended for beginners)?

In order to run EXUDYN, you need an appropriate Python installation. We recommend to use

- Anaconda, 32bit, Python 3.6.5
- Spyder 3.2.8 (Python 3.6.5 32 bits)

If you plan to use 64bit and newer Python versions, we recommend to use VS2019 to compile your code, which offers Python 3.7 compatibility. However, you should know that Python versions and the version of the module must be identical (e.g., Python 3.6 32 **both** in the exudyn module and in Spyder).

The simplest way to start is, to copy the files (and possibly further files that are needed)

- exudynUtilities.py
- itemInterface.py
- exudyn.pyd

to your working directory and directly import the modules as described in tutorials and examples. The second way (**recommended**) is to use Python's sys module to link to your WorkingRelease directory, for example:

```
import sys
sys.path.append('C:\\DATA\\cpp\\EXUDYN_git\\main\\bin\\WorkingRelease')
```

In the future, there will also be a possibility to install the module using pip commands – we are happy, if somebody could do this!

## 1.1.4 How to install EXUDYN and using the C++ code (advanced)?

EXUDYN is still under intensive development of core modules. There are several ways to using the code, but you **cannot** install EXUDYN as compared to other executable programs and apps.

In order to make full usage of the C++ code and extending it, you can use:

- Windows / Microsoft Visual Studio 17 and above:
  - get the files from git
  - put them into a local directory (recommended: C:/DATA/cpp/EXUDYN\_git)
  - start main\_sln.sln with Visual Studio
  - compile the code and run main/pythonDev/pytest.py example code
  - adapt pytest.py for your applications
  - extend the C++ source code
  - link it to your own code
  - NOTE: on some systems, you might need to replace '/' with '\'
- Linux, etc.: not fully supported yet; however, all external libraries are Linux-compatible and thus should run with minimum adaptation efforts.

#### 1.1.5 Goals of EXUDYN

After the first development phase (planned in Q4/2021), it will

- be a small multibody library, which can be easily linked to other projects,
- allow to efficiently simulate small scale systems (compute 100000s time steps per second for systems with  $n_{DOF} < 10$ ),
- allow to efficiently simulate medium scaled systems for problems with  $n_{DOF} < 1\,000\,000$  (planned: Q4 2020),
- use multi-threaded parallel computing techniques (planned: Q4 2020),
- be accessible safe and at a wide range via the Python interface,
- allow to add user defined objects in C++,
- allow to add user defined objects in Python (planned: 2021),
- allow to add user defined solvers in Python (finished: Q1 2020).

### 1.1.6 Run a simple example in Spyder

After performing the steps of the previous section, this section shows a simplistic model which helps you to check if EXUDYN runs on your computer.

In order to start, run the python interpreter Spyder. For the following example, either

#### Listing 1.1: My first example

```
from itemInterface import *
                                #conversion of data to exudyn dictionaries
import exudyn as exu
                               #C++ EXUDYN library
SC = exu.SystemContainer()
                                 #container of systems
mbs = SC.AddSystem()
                                #add a new system to work with
nMP = mbs.AddNode(NodePoint2D(referenceCoordinates=[0,0]))
mbs.AddObject(ObjectMassPoint2D(physicsMass=10, nodeNumber=nMP ))
mMP = mbs.AddMarker(MarkerNodePosition(nodeNumber = nMP))
mbs.AddLoad(Force(markerNumber = mMP, loadVector=[0.001,0,0]))
mbs.Assemble()
                                #assemble system and solve
simulationSettings = exu.SimulationSettings()
SC. TimeIntegrationSolve (mbs, 'GeneralizedAlpha', simulationSettings)
```

- open Spyder and copy the example provided in Listing 1.1 into a new file, or
- open myFirstExample.py from your WorkingRelease directory

Hereafter, press the play button or F5 in Spyder.

If successful, the IPython Console of Spyder will print something like:

If you check your current directory (where myFirstExample.py lies), you will find a new file coordinatesSolution.txt, which contains the results of your computation (with default values for time integration). The beginning and end of the file should look like:

```
0.05,1.25e-07,0,5e-06,0,0.0001,0
...

0.96,4.608e-05,0,9.6e-05,0,0.0001,0
0.97,4.7045e-05,0,9.7e-05,0,0.0001,0
0.98,4.802e-05,0,9.8e-05,0,0.0001,0
0.99,4.9005e-05,0,9.9e-05,0,0.0001,0
1,5e-05,0,0.0001,0,0.0001,0
#simulation finished=2019-11-14,20:35:12
#Solver Info: errorOccurred=0,converged=1,solutionDiverged=0,total time steps=100,total
Newton iterations=100,total Newton jacobians=100
```

Within this file, the first column shows the simulation time and the following columns provide solution of coordinates, their derivatives and Lagrange multipliers on system level. As expected, the x-coordinate of the point mass has constant acceleration a = f/m = 0.001/10 = 0.0001, the velocity grows up to 0.0001 after 1 second and the point mass moves 0.00005 along the x-axis.

## 1.2 FAQ – Frequently asked questions

- 1. Where do I find the '.exe' file?
  - → EXUDYN is only available via the python interface as exudyn.pyd library, which is located in folder: main/bin/WorkingRelease. This means that you need to run python (best: Spyder) and import the EXUDYN module.
- 2. Why does type auto completion does not work for mbs (Main system)?
  - → most python environments only have information up to the first sub-structure, e.g., SC=exu. SystemContai provides full access to SC in the type completion, but mbs=SC.AddSystem() is at the second sub-structure of the module and is not accessible.
    WORKAROUND: type mbs=MainSystem() before the mbs=SC.AddSystem() command and the interpreter will know what type mbs is. This also works for settings, e.g., simulation settings 'Newton'.
- 3. What is the difference between MarkerBodyPosition and MarkerBodyRigid?
  - → Position markers (and nodes) do not have information on the orientation (rotation). For that reason, there is a difference between position based and rigid-body based markers. In case of a rigid body attached to ground with a SpringDamper, you can use both, MarkerBodyPosition or MarkerBodyRigid, markers. For a prismatic joint, you will need a MarkerBodyRigid.
- 4. Why can't I get the focus of the simulation window on startup (render window hidden)?
  - → Starting EXUDYN out of Spyder might not bring the simulation window to front, because of specific settings in Spyder(version 3.2.8), e.g., Tools→Preferences→Editor→Advanced settings: uncheck 'Maintain focus in the Editor after running cells or selections'; Alternatively, set

SC.visualizationSettings.window.alwaysOnTop=True **before** starting the renderer with exu.StartRenderer()

5. When importing EXUDYN in python (windows) I get the error (or similar):

```
Traceback (most recent call last):
   File "C:\DATA\cpp\EXUDYN_git\main\pythonDev\pytest.py", line 18, in <module>
    import exudyn as exu
ImportError: DLL load failed: %1 is no valid Win32 application.
```

→ probably this is a 32/64bit problem. Your Python installation and EXUDYN need to be **BOTH** either 64bit OR 32bit (Check in your python help; exudyn in WorkingRelease64 is the 64bit version, in WorkingRelease it is the 32bit version) and the Python installation and EXUDYN need to have **BOTH** the same version and 1st subversion number (e.g., 3.6.5 should be compatible with 3.6.2).

## **Chapter 2**

## **Overview on EXUDYN**

#### 2.1 Module structure

This section will show:

- Overview of modules
- Conventions: dimension of nodes, objects and vectors
- Coordinates: reference coordinates and displacements
- Nodes, Objects, Markers and Loads

#### 2.1.1 Overview of modules

Currently, the module structure is simple:

- Python parts:
  - itemInterface: contains the interface, which transfers python classes (e.g., of a NodePoint)
     to dictionaries that can be understood by the C++ module
  - exudynUtilities: constains helper classes in Python, which allows simpler working with EXUDYN
- C++ parts, see Figs. 2.1 and 2.2:
  - exudyn<sup>1</sup>: on this level, there are just very few functions: SystemContainer(), StartRenderer(),
     StopRenderer()
  - SystemContainer: contains the systems (most important), solvers (static, dynamics, ...), visualization settings
  - mbs: system created with mbs = SC.AddSystem(), this structure contains everything that defines a solvable multibody system; a large set of nodes, objects, markers, loads can added to the system, see Section 5;

<sup>&</sup>lt;sup>1</sup>note that there is a second module, called exudynFast, which does deactivates all range-, index- or memory allocation checks at the gain of higher speed (probably 30 percent in regular cases). To check which version you have, just type exu.\_\_doc\_\_ and you will see a note on 'exudynFast' in the exudynFast module.

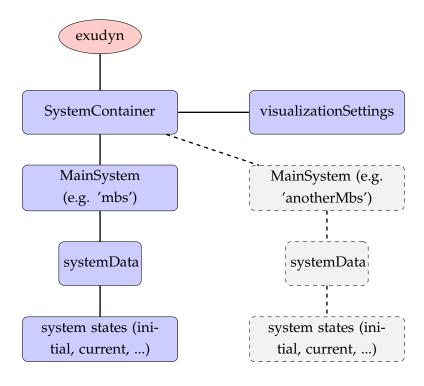


Figure 2.1: Overview of exudyn module.

 mbs.systemData: contains the initial, current, visualization, ... states of the system and holds the items, see Fig. 2.2

#### 2.1.2 Conventions: items, indices, coordinates

In this documentation, we will use the term **item** to identify nodes, objects, markers and loads:

$$item \in \{node, object, marker, load\}$$
 (2.1)

#### Indices: arrays and vector starting with 0:

As known from Python, all **indices** of arrays, vectors, etc. are starting with 0. This means that the first component of the vector v=[1,2,3] is accessed with v[0] in Python (and also in the C++ part of EXUDYN). The range is usually defined as range(0,3), in which '3' marks the index after the last valid component of an array or vector.

## Dimensionality of objects and vectors:

As a convention, quantities in EXUDYN are 3D, such as nodes, objects, markers, loads, measured quantities, etc. For that reason, we denote planar nodes, objects, etc. with the suffix '2D', but 3D objects do not get this suffix.

Output and input to objects, markers, loads, etc. is usually given by 3D vectors (or matrices), such as (local) position, force, torque, rotation, etc. However, initial and reference values for nodes depend on their dimensionality. As an example, consider a NodePoint2D:

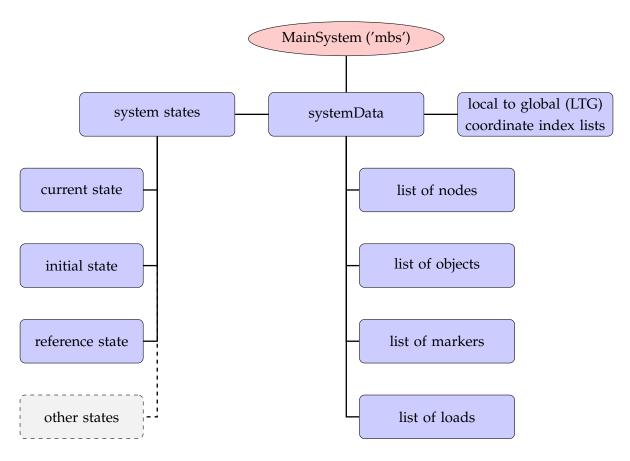


Figure 2.2: Overview of systemData, which connects items and states. Note that access to items is provided via functions in system.

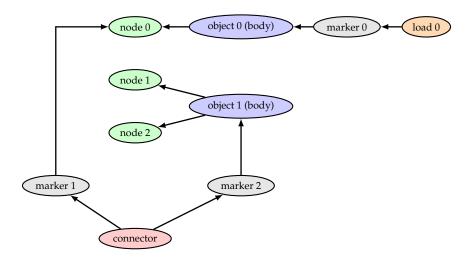


Figure 2.3: Typical interaction of items in a multibody system. Note that both, bodies and connectors/constraints are (computational) objects. The arrows indicate, that, e.g., object 1 has node 1 and node 2 (indices) and that marker 0 is attached to object 0, while load 0 uses marker 0 to apply the load. Sensors could additionally be attached to certain items.

- referenceCoordinates is a 2D vector (but could be any dimension in general nodes)
- measuring the current position of NodePoint2D gives a 3D vector
- when attaching a MarkerNodePosition and a LoadForceVector, the force will be still a 3D vector

Furthermore, the local position in 2D objects is provided by a 3D vector. Usually, the dimensionality is given in the reference manual. User errors in the dimensionality will be usually detected either by the python interface (i.e., at the time the item is created) or by the system-preprocessor

## 2.2 Items: Nodes, Objects, Loads, Markers, Sensors, ...

In this section, the most important part of EXUDYN are provided. An overview of the interaction of the items is given in Fig. 2.3

#### 2.2.1 **Nodes**

Nodes provide the coordinates (and the degrees of freedom) to the system. They have no mass, stiffness or whatsoever assigned. Without nodes, the system has no unknown coordinates. Adding a node provides (for the system unknown) coordinates. In addition we also need equations for every nodal coordinate – otherwise the system cannot be computed (NOTE: this is currently not checked by the preprocessor).

#### 2.2.2 Objects

Objects are 'computational objects' and they provide equations to your system. Objects additionally often provide derivatives and have measurable quantities (e.g. displacement) and they provide access, which can be used to apply, e.g., forces.

Objects can be a:

- general object (e.g. a controller, user defined object, ...; no example yet)
- body: has a mass or mass distribution; markers can be placed on bodies; loads can be applied; constraints can be attached via markers; bodies can be:
  - ground object: has no nodes
  - simple body: has one node (e.g. mass point, rigid body)
  - finite element and more complicated body (e.g. FFRF-object): has more than one node
- connector: uses markers to connect nodes and/or bodies; adds additional terms to system equations either based on stiffness/damping or with constraints (and Lagrange multipliers). Possible connectors:
  - algebraic constraint (e.g. constrain two coordinates:  $q_1 = q_2$ )
  - classical joint
  - spring-damper or penalty constraint

#### 2.2.3 Markers

Markers are interfaces between objects/nodes and constraints/loads. A constraint (which is also an object) or load cannot act directly on a node or object without a marker. As a benefit, the constraint or load does not need to know whether it is applied, e.g., to a node or to a local position of a body.

Typical situations are:

- Node Marker Load
- Node Marker Constraint (object)
- Body(object) Marker Load
- Body1 Marker1 Joint(object) Marker2 Body2

#### **2.2.4** Loads

Loads are used to apply forces and torques to the system. The load values are static values. However, you can use Python functionality to modify loads either by linearly increasing them during static computation or by using the 'preStepPyExecute' structure in order to modify loads in every integration step depending on time or on measured quantities (thus, creating a controller).

#### 2.2.5 Sensors

Sensors are only used to measure output variables (values) in order to simpler generate the requested output quantities. They have a very weak influence on the system, because they are only evaluated after certain solver steps as requested by the user.

### 2.2.6 Reference coordinates and displacements

Nodes usually have separated reference and initial quantities. Here, referenceCoordinates are the coordinates for which the system is defined upon creation. Reference coordinates are needed, e.g., for definition of joints and for the reference configuration of finite elements. In many cases it marks the undeformed configuration (e.g., with finite elements), but not, e.g., for ObjectConnectorSpringDamper, which has its own reference length.

Initial displacement (or rotation) values are provided separately, in order to start a system from a configuration different from the reference configuration. As an example, the initial configuration of a NodePoint is given by referenceCoordinates + initialDisplacements, while the initial state of a dynamic system additionally needs initialVelocities.

## 2.3 Exudyn Basics

This section will show:

- Interaction with the EXUDYN module
- Simulation settings
- Visualization settings
- Generating output and results
- Graphics pipeline
- Generating animations

#### 2.3.1 Interaction with the EXUDYN module

It is important that the EXUDYN module is basically a state machine, where you create items on the C++ side using the Python interface. This helps you to easily set up models using many other Python modules (numpy, sympy, matplotlib, ...) while the computation will be performed in the end on the C++ side in a very efficient manner.

#### Where do objects live?

Whenever a system container is created with SC = exu.SystemContainer(), the structure SC lives in C++ and will be modified via the python interface. Usually, the system container will hold at least one system, usually called mbs. Commands such as mbs.AddNode(...) add objects to the system mbs. The system will be prepared for simulation by mbs.Assemble() and can be solved (e.g., using SC.TimeIntegrationSolve(...)) and evaluated hereafter using the results files. Using mbs.Reset() will clear the system and allows to set up a new system. Items can be modified (ModifyObject(...)) after first initialization, even during simulation.

#### 2.3.2 Simulation settings

The simulation settings consists of a couple of substructures, e.g., for solutionSettings, staticSolver, timeIntegration as well as a couple of general options – for details see Sections 6.1.1 - 6.1.7.

Simulation settings are needed for every solver. They contain solver-specific parameters (e.g., the way how load steps are applied), information on how solution files are written, and very specific control parameters, e.g., for the Newton solver.

The simulation settings structure is created with

```
simulationSettings = exu.SimulationSettings()
```

Hereafter, values of the structure can be modified, e.g.,

```
#10 seconds of simulation time:
simulationSettings.timeIntegration.endTime = 10
    #1000 steps for time integration:
simulationSettings.timeIntegration.numberOfSteps = 1000
    #assigns a new tolerance for Newton's method:
simulationSettings.timeIntegration.newton.relativeTolerance = 1e-9
    #write some output while the solver is active (SLOWER):
simulationSettings.timeIntegration.verboseMode = 2
    #write solution every 0.1 seconds:
simulationSettings.solutionSettings.solutionWritePeriod = 0.1
    #use sparse matrix storage and solver (package Eigen):
    simulationSettings.linearSolverType = exu.LinearSolverType.EigenSparse
```

### 2.3.3 Visualization settings

Visualization settings are used for user interaction with the model. E.g., the nodes, markers, loads, etc., can be visualized for every model. There are default values, e.g., for the size of nodes, which may be inappropriate for your model. Therefore, you can adjust those parameters. In some cases, huge models require simpler graphics representation, in order not to slow down performance – e.g., the number of faces to represent a cylinder should be small if there are 10000s of cylinders drawn. Even computation performance can be slowed down, if visualization takes lots of CPU power. However, visualization is performed in a separate thread, which usually does not influence the computation exhaustively. Details on visualization settings and its substructures are provided in Sections 6.2.1 – 6.2.13.

The visualization settings structure can be accessed in the system container SC (access per reference, no copying!), accessing every value or structure directly, e.g.,

```
SC.visualizationSettings.nodes.defaultSize = 0.001 #draw nodes very small
#change openGL parameters; current values can be obtained from SC.GetRenderState()
#change zoom factor:
SC.visualizationSettings.openGL.initialZoom = 0.2
#set the center point of the scene (can be attached to moving object):
SC.visualizationSettings.openGL.initialCenterPoint = [0.192, -0.0039, -0.075]
```



Figure 2.4: Basic solver flow chart for SolveSystem(). This flow chart is the same for static solver and for time integration.

```
#turn of auto-fit:
SC.visualizationSettings.general.autoFitScene = False

#change smoothness of a cylinder:
SC.visualizationSettings.general.cylinderTiling = 100

#make round objects flat:
SC.visualizationSettings.openGL.shadeModelSmooth = False

#turn on coloured plot, using y-component of displacements:
SC.visualizationSettings.contour.outputVariable = exu.OutputVariableType.
    Displacement
SC.visualizationSettings.contour.outputVariableComponent = 1 #0=x, 1=y, 2=z
```

#### 2.3.4 Solver

Both in the static as well as in the dynamic case, the solver runs in a loop to solve a nonlinear system of (differential and/or algebraic) equations over a given time or load interval. For the time integration (dynamic solver), Fig. 2.4 shows the basic loops for the solution process. The inner loops are shown in Fig. 2.6 and Fig. 2.7. The static solver behaves very similar, while no velocities or accelerations need to be solved and time is replaced by load steps.

Settings for the solver substructures, like timer, output, iterations, etc. are described in Sections 6.3.1 - 6.3.5. The description of interfaces for solvers starts in Section 6.3.6.

#### 2.3.5 Generating output and results

The solvers provide a number of options in solutionSettings to generate a solution file. As a default, exporting solution to the solution file is activated with a writing period of 0.01 seconds.

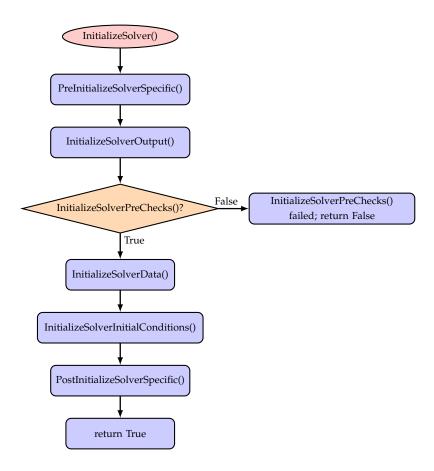


Figure 2.5: Basic solver flow chart for function InitializeSolver().

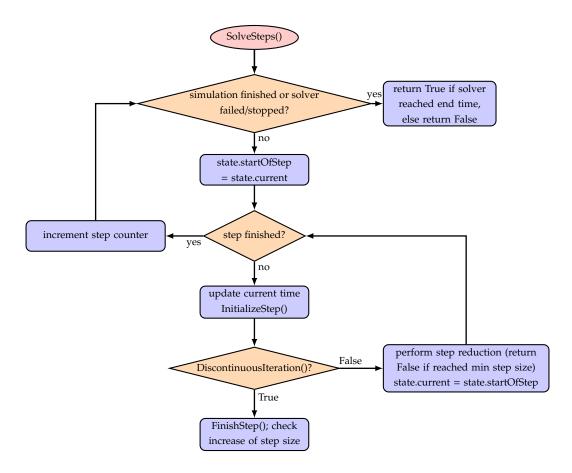


Figure 2.6: Solver flow chart for SolveSteps(), which is the inner loop of the solver.

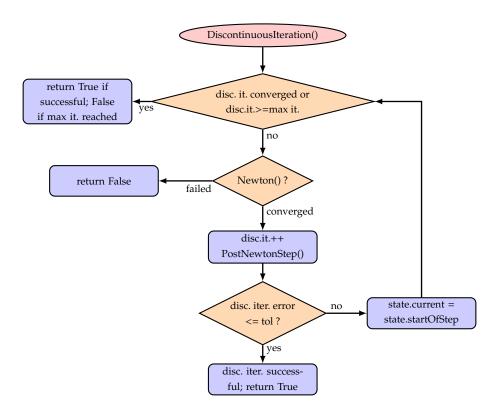


Figure 2.7: Solver flow chart for DiscontinuousIteration(), which is run for every solved step inside the static/dynamic solvers. If the DiscontinuousIteration() returns False, SolveSteps() will try to reduce the step size.

#### Typical output settings are:

```
#create a new simulationSettings structure:
simulationSettings = exu.SimulationSettings()

#activate writing to solution file:
simulationSettings.solutionSettings.writeSolutionToFile = True
#write results every 1ms:
simulationSettings.solutionSettings.solutionWritePeriod = 0.001

#assign new filename to solution file
simulationSettings.solutionSettings.coordinatesSolutionFileName= "myOutput.txt"

#do not export certain coordinates:
simulationSettings.solutionSettings.exportDataCoordinates = False
```

## 2.3.6 Graphics pipeline

The user cannot interact with the visualization part for now. There are basically two loops during simulation, which feed the graphics pipeline. The solver runs a loop:

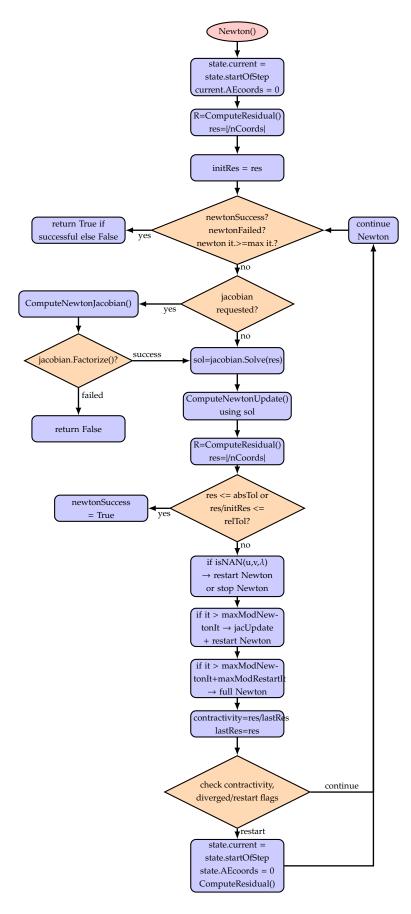


Figure 2.8: Solver flow chart for Newton(), which is run inside the DiscontinuousIteration(). The shown case is valid for newtonResidualMode = 0.

- compute new step
- finish computation step; results are in current state
- copy current state to visualization state (thread safe)
- signal graphics pipeline that new visualization data is available

The openGL graphics thread runs the following loop:

- render openGL scene with a given graphicsData structure (containing lines, faces, text, ...)
- go idle for some milliseconds
- check if openGL rendering needs an update (e.g. due to user interaction)
  - → if update is needed, the visualization of all items is updated stored in a graphicsData structure)
- check if new visualization data is available and the time since last update is larger than a presribed value, the graphicsData structure is updated with the new visualization state

#### 2.3.7 Generating animations

In many dynamics simulations, it is very helpful to create animations in order to better understand the motion of bodies. Specifically, the animation can be used to visualize the model much slower or faster than the model is computed.

Animations are created based on a series of images (frames, snapshots) taken during simulation. It is important, that the current view is used to record these images – this means that the view should not be changed during the recording of images. To turn on recording of images during solving, set the following flag to a positive value

• simulationSettings.solutionSettings.recordImagesInterval = 0.01

which means, that after every 0.01 seconds of simulation time, an image of the current view is taken and stored in the directory and filename (without filename ending) specified by

• SC.visulizationSettings.exportImages.saveImageFileName = 'myFolder/frame'

By default, a consecutive numbering is generated for the image, e.g., 'frame0000.tga, frame0001.tga,...'. Note that '.tga' files contain raw image data and therefore can become very large.

To create animation files, an external tool FFMPEG is used to efficiently convert a series of images into an animation. In windows, simple DOS batch files can do the job to convert frames given in the local directory to animations, e.g.:

```
echo off

REM 2019-12-23, Johannes Gerstmayr

REM helper file for EXUDYN to convert all frame00000.tga, frame000001.tga, ... files to a video

REM for higher quality use crf option (standard: -crf 23, range: 0-51, lower crf value means higher quality)

IF EXIST animation.mp4 (
```

```
echo "animation.mp4 already exists! rename the file"

) ELSE (

"C:\Program Files (x86)\FFMPEG\bin\ffmpeg.exe" -r 25 -start_number 0 -i frame%%05d.

tga -c:v libx264 -vf "fps=25,format=yuv420p" animation.mp4

)
```

After the video has been created, you should delete the single images:

```
REM 2019-12-23, Johannes Gerstmayr

REM helper file for EXUDYN

REM delete all .tga images of current directory

del *.tga
```

#### 2.4 C++ Code

This section covers some information on the C++ code. For more information see the Open source code and use doxygen.

Exudyn was developed for the efficient simulation of flexible multi-body systems. Exudyn was designed for rapid implementation and testing of new formulations and algorithms in multibody systems, whereby these algorithms can be easily implemented in efficient C++ code. The code is applied to industry-related research projects and applications.

#### 2.4.1 Focus of the C++ code

#### Four principles:

- 1. developer-friendly
- 2. error minimization
- 3. efficiency
- 4. user-friendliness

The focus is therefore on:

- A developer-friendly basic structure regarding the C++ class library and the possibility to add new components.
- The basic libraries are slim, but extensively tested; only the necessary components are available
- Complete unit tests are added to new program parts during development; for more complex processes, tests are available in Python
- In order to implement the sometimes difficult formulations and algorithms without errors, error avoidance is always prioritized.

- To generate efficient code, classes for parallelization (vectorization and multithreading) are provided. We live the principle that parallelization takes place on multi-core processors with a central main memory, and thus an increase in efficiency through parallelization is only possible with small systems, as long as the program runs largely in the cache of the processor cores. Vectorization is tailored to SIMD commands as they have Intel processors, but could also be extended to GPGPUs in the future.
- The user interface (Python) provides a 1:1 image of the system and the processes running in it, which can be controlled with the extensive possibilities of Python.

#### 2.4.2 C++ Code structure

The functionality of the code is based on systems (MainSystem/CSystem) representing the multibody system or similar physical systems to be simulated. Parts of the core structure of Exudyn are:

- CSystem / MainSystem: a multibody system which consists of nodes, objects, markers, loads, etc.
- SystemContainer: holds a set of systems; connects to visualization (container)
- node: used to hold coordinates (unknowns)
- (computational) object: leads to equations, using nodes
- marker: defines a consistent interface to objects (bodies) and nodes; write access ('AccessFunction')
   provides jacobian and read access ('OutputVariable')
- load: acts on an object or node via a marker
- computational objects: efficient objects for computation = bodies, connectors, connectors, loads, nodes, ...
- visualization objects: interface between computational objects and 3D graphics
- main (manager) objects: do all tasks (e.g. interface to visualization objects, GUI, python, ...) which are not needed during computation
- static solver, kinematic solver, time integration
- python interface via pybind11; items are accessed with a dictionary interface; system structures and settings read/written by direct access to the structure (e.g. SimulationSettings, Visualization-Settings)
- interfaces to linear solvers; future: optimizer, eigenvalue solver, ... (mostly external or in python)

#### 2.4.3 C++ Code: Modules

The following internal modules are used, which are represented by directories in main/src:

- Autogenerated: item (nodes, objects, markers and loads) classes split into main (management, python connection), visualization and computation
- Graphics: a general data structure for 2D and 3D graphical objects and a tiny openGL visualization; linkage to GLFW

- Linalg: Linear algebra with vectors and matrices; separate classes for small vectors (SlimVector), large vectors (Vector and ResizableVector), vectors without copying data (LinkedDataVector), and vectors with constant size (ConstVector)
- Main: mainly contains SystemContainer, System and ObjectFactory
- Objects: contains the implementation part of the autogenerated items
- Pymodules: manually created libraries for linkage to python via pybind; remaining linking to python is located in autogenerated folder
- pythonGenerator: contains python files for automatic generation of C++ interfaces and python interfaces of items;
- Solver: contains all solvers for solving a CSystem
- System: contains core item files (e.g., MainNode, CNode, MainObject, CObject, ...)
- Tests: files for testing of internal linalg (vector/matrix), data structure libraries (array, etc.) and functions
- Utilities: array structures for administrative/managing tasks (indices of objects ... bodies, forces, connectors, ...); basic classes with templates and definitions

The following main external libraries are linked to Exudyn:

- LEST: for testing of internal functions (e.g. linalg)
- GLFW: 3D graphics with openGL; cross-platform capabilities
- Eigen: linear algebra for large matrices, linear solvers, sparse matrices and link to special solvers
- pybind11: linking of C++ to python

#### 2.4.4 Code style and conventions

This section provides general coding rules and conventions, partly applicable to the C++ and python parts of the code. Many rules follow common conventions (e.g., google code style, but not always – see notation):

- write simple code (no complicated structures or uncommon coding)
- write readable code (e.g., variables and functions with names that represent the content or functionality; AVOID abbreviations)
- put a header in every file, according to Doxygen format
- put a comment to every (global) function, member function, data member, template parameter
- ALWAYS USE curly brackets for single statements in 'if', 'for', etc.; example: if (i < n) i += 1;
- use Doxygen-style comments (use '//!' Qt style and '@ date' with '@' instead of 'for commands)
- use Doxygen (with preceeding '@') 'test' for tests, 'todo' for todos and 'bug' for bugs
- USE 4-spaces-tab
- use C++11 standards when appropriate, but not exhaustively
- ONE class ONE file rule (except for some collectors of single implementation functions)
- add complete unit test to every function (every file has link to LEST library)

- avoid large classes (>30 member functions; > 15 data members)
- split up god classes (>60 member functions)
- mark changed code with your name and date
- REPLACE tabs by spaces: Extras->Options->C/C++->Tabstopps: tab stopp size = 4 (=standard)
   KEEP SPACES=YES

#### 2.4.5 Notation conventions

The following notation conventions are applied (**no exceptions!**):

- use lowerCamelCase for names of variables (including class member variables), consts, c-define variables, ...; EXCEPTION: for algorithms following formulas, e.g.,  $f = M * q_t t + K * q$ , GBar, ...
- use UpperCamelCase for functions, classes, structs, ...
- Special cases for CamelCase: write 'ODEsystem', BUT: 'ODE1Equations'
- '[...]Init' ... in arguments, for initialization of variables; e.g. 'valueInit' for initialization of member variable 'value'
- use American English troughout: Visualization, etc.
- for (abbreviations) in captial letters, e.g. ODE, use a lower case letter afterwards:
- do not use consecutive capitalized words, e.g. DO NOT WRITE 'ODEAE'
- for functions use ODEComputeCoords(), for variables avoid 'ODE' at beginning: use nODE or write odeCoords
- do not use '\_' within variable or function names; exception: derivatives, release\_assert
- use name which exactly describes the function/variable: 'numberOfItems' instead of 'size' or 'l'
- examples for variable names: secondOrderSize, massMatrix, mThetaTheta
- examples for function/class names: SecondOrderSize, EvaluateMassMatrix, Position(const Vector3D& localPosition)
- use the Get/Set...() convention if data is retrieved from a class (Get) or something is set in a class (Set): Use const. T& Get () /T& Get if direct access to variables is needed: Use Get/Set for pybind11
- (Set); Use const T& Get()/T& Get if direct access to variables is needed; Use Get/Set for pybind11
   example Get/Set: Real\* GetDataPointer(), Vector::SetAll(Real), GetTransposed(), SetRotationalParameters
- use 'Real' instead of double or float: for compatibility, also for AVX with SP/DP
- use 'Index' for array/vector size and index instead of size\_t or int
- item: object, node, marker, load: anything handled within the computational/visualization systems

#### 2.4.6 No-abbreviations-rule

SetColor(...), ...

The code uses a **minimum set of abbreviations**; however, the following abbreviation rules are used throughout: In general: DO NOT ABBREVIATE function, class or variable names: GetDataPointer() instead of GetPtr(); exception: cnt, i, j, k, x or v in cases where it is really clear (5-line member functions).

Exceptions to the NO-ABBREVIATIONS-RULE:

- ODE ... ordinary differential equations;
- ODE2 ... marks parts related to second order differential equations (SOS2, EvalF2 in HOTINT)
- ODE1 ... marks parts related to first order differential equations (ES, EvalF in HOTINT)
- AE ... algebraic equations (IS, EvalG in HOTINT); write 'AEcoordinates' for 'algebraicEquation-sCoordinates'
- 'C[...]' ... Computational, e.g. for ComputationalNode ==> use 'CNode'
- min, max ... minimum and maximum
- write time derivatives with underscore: \_t, \_tt; example: Position\_t, Position\_tt, ...
- write space-wise derivatives ith underscore: \_x, \_xx, \_y, ...
- if a scalar, write coordinate derivative with underscore: \_q, \_v (derivative w.r.t. velocity coordinates)
- for components, elements or entries of vectors, arrays, matrices: use 'item' throughout
- '[...]Init' ... in arguments, for initialization of variables; e.g. 'valueInit' for initialization of member variable 'value'

## 2.5 Changes

The following list covers changes in the python interface and functionality:

#### • Version 0.1.260 → Version 0.1.263

Changes in the python interface:

- mbs.systemData.GetCurrentTime() → mbs.systemData.GetTime()
- mbs.systemData.GetVisualizationTime()  $\rightarrow$  mbs.systemData.GetTime(configurationType=exu.ConfigurationType=ex

#### • Version 0.1.244 → Version 0.1.245

Changes in the implementation / solver (LEADS TO DIFFERENT RESULTS):

 Solvers updated: static solver and time integration have been updated; old solvers are still available with the 'OldSolver' extension

Changes in the python interface (new functions / interface to call the old solvers):

- SC.SolveStaticOldSolver(...)
- SC.TimeIntegrationSolve(mbs, 'GeneralizedAlphaOldSolver', simulationSettings)

### • Version 0.1.243 → Version 0.1.244

Changes in the python interface:

- simulationSettings.staticSolver.pauseAfterEachStep
  - → simulationSettings.pauseAfterEachStep (merged with timeIntegration.pauseAfterEachStep

#### • Version 0.1.238 → Version 0.1.240

Changes in the implementation / solver (LEADS TO DIFFERENT RESULTS):

- generalizedAlpha: corrected initialization of algorithmic acceleration for discontinuous iteration
- time integration: corrected time t for evaluation of RHS from beginning to end of time step (improves accuracy for time-dependent loads significantly)

## Changes in the python interface:

- simulationSettings.timeIntegration.pauseAfterEachStep
  - → simulationSettings.pauseAfterEachStep
- ADDED: simulationSettings.timeIntegration.verboseModeFile
- ADDED: simulationSettings.staticSolver.verboseModeFile

## **Chapter 3**

## **Tutorial**

This section will show:

- A basic tutorial for a 1D mass and spring-damper with initial displacements, shortest possible model with practically no special settings
- A more advanced 2D rigid-body model (coming soon)
- Links to examples section

The python source code of this section can be found in the file:

```
main/pythonDev/Examples/springDamperTutorial.py
```

This tutorial will set up a mass point and a spring damper, dynamically compute the solution and evaluate the reference solution.

To start up, we set the system path to the directory of the library (needs to be adjusted!):

```
import sys
sys.path.append('C:\\DATA\\cpp\\EXUDYN_git\\main\\bin\\WorkingRelease') #for Spider
```

We import the exudyn library and the interface for all nodes, objects, markers and loads:

```
import exudyn as exu
from itemInterface import *
import numpy as np
```

Next, we need a SystemContainer, which contains all computable systems and add a new system. Per default, you always should name your system 'mbs' (multibody system), in order to copy/paste code parts from other examples, tutorials and other projects:

```
SC = exu.SystemContainer()
mbs = SC.AddSystem()
```

In order to check, which version you are using, you can printout the current EXUDYN version. This version is in line with the issue tracker and marks the number of open/closed issues added to EXUDYN:

```
print('EXUDYN version='+exu.__version__)
```

Using the powerful Python language, we can define some variables for our problem, which will also be used for the analytical solution:

```
L=0.5 #reference position of mass

mass = 1.6 #mass in kg

spring = 4000 #stiffness of spring—damper in N/m

damper = 8 #damping constant in N/(m/s)

f =80 #force on mass
```

For the simple spring-mass-damper system, we need initial displacements and velocities:

```
u0=-0.08  #initial displacement
v0=1  #initial velocity
x0=f/spring  #static displacement
print('resonance frequency = '+str(np.sqrt(spring/mass)))
print('static displacement = '+str(x0))
```

We first need to add nodes, which provide the coordinates (and the degrees of freedom) to the system. The following line adds a 3D node for 3D mass point<sup>1</sup>:

Here, Point (=NodePoint) is a Python class, which takes a number of arguments defined in the reference manual. The arguments here are referenceCoordinates, which are the coordinates for which the system is defined. The initial configuration is given by referenceCoordinates + initialDisplacements, while the initial state additionally gets initialVelocities.

While Point adds 3 unknown coordinates to the system, which need to be solved, we also can add ground nodes, which can be used similar to nodes, but they do not have unknown coordinates – and therefore also have no initial displacements or velocities. The advantage of ground nodes (and ground bodies) is that no constraints are needed to fix these nodes. Such a ground node is added via:

```
nGround=mbs.AddNode(NodePointGround(referenceCoordinates = [0,0,0]))
```

In the next step, we add an object<sup>2</sup>, which provides equations for coordinates. The MassPoint needs at least a mass (kg) and a node number to which the mass point is attached. Additionally, graphical objects could be attached:

```
massPoint = mbs.AddObject(MassPoint(physicsMass = mass, nodeNumber = n1))
```

<sup>&</sup>lt;sup>1</sup>Note: Point is an abbreviation for NodePoint, defined in itemInterface.py.

<sup>&</sup>lt;sup>2</sup>For the moment, we just need to know that objects either depend on one or more nodes, which are usually bodies and finite elements, or they can be connectors, which connect (the coordinates of) objects via markers, see Section 2.1.

In order to apply constraints and loads, we need markers. These markers are used as local positions (and frames), where we can attach a constraint lateron. In this example, we work on the coordinate level, both for forces as well as for constraints. Markers are attached to the according ground and regular node number, additionally using a coordinate number (0 ... first coordinate):

This means that loads can be applied to the first coordinate of node n1 via marker with number nodeMarker.

Now we add a spring-damper to the markers with numbers groundMarker and the nodeMarker, providing stiffness and damping parameters:

Finally, a load is added to marker nodeMarker, with a scalar load with value f:

As our system is fully set, we can print the overall information and assemble the system to make it ready for simulation:

```
print(mbs)
mbs.Assemble()
```

We will use time integration and therefore define a number of steps (fixed step size; must be provided) and the total time span for the simulation:

```
steps = 1000 #number of steps to show solution
tEnd = 1 #end time of simulation
```

All settings for simulation, see according reference section, can be provided in a structure given from exu.SimulationSettings(). Note that this structure will contain all default values, and only non-default values need to be provided:

```
simulationSettings = exu.SimulationSettings()
simulationSettings.solutionSettings.solutionWritePeriod = 1e-2 #output interval
simulationSettings.timeIntegration.numberOfSteps = steps
simulationSettings.timeIntegration.endTime = tEnd
```

We are using a generalized alpha solver, where numerical damping is needed for index 3 constraints. As we have only spring-dampers, we can set the spectral radius to 1, meaning no numerical damping:

```
simulationSettings.timeIntegration.generalizedAlpha.spectralRadius = 1
```

In order to visualize the results online, a renderer can be started. As our computation will be very fast, it is a good idea to wait for the user to press SPACE, before starting the simulation (uncomment second line):

As the simulation is still very fast, we will not see the motion of our node. Using e.g. steps=10000000 in the lines above allows you online visualize the resulting oscillations.

Finally, we start the solver, by telling which system to be solved, solver type and the simulation settings:

```
SC. TimeIntegrationSolve(mbs, 'GeneralizedAlpha', simulationSettings)
```

After simulation, our renderer needs to be stopped (otherwise it would stay in background and prohibit further simulations). Sometimes you would like to wait until closing the render window, using WaitForRenderEngineStopFlag():

There are several ways to evaluate results, see the reference pages. In the following we take the final value of node n1 and read its 3D position vector:

```
#evaluate final (=current) output values
u = mbs.GetNodeOutput(n1, exu.OutputVariableType.Position)
print('displacement=',u)
```

The following code generates a reference (exact) solution for our example:

```
import matplotlib.pyplot as plt
import matplotlib.ticker as ticker

omega0 = np.sqrt(spring/mass) #eigen frequency of undamped system

dRel = damper/(2*np.sqrt(spring*mass)) #dimensionless damping

omega = omega0*np.sqrt(1-dRel**2) #eigen freq of damped system

C1 = u0-x0 #static solution needs to be considered!

C2 = (v0+omega0*dRel*C1) / omega #C1, C2 are coeffs for solution

refSol = np.zeros((steps+1,2))

for i in range(0,steps+1):
    t = tEnd*i/steps
    refSol[i,0] = t

    refSol[i,1] = np.exp(-omega0*dRel*t)*(C1*np.cos(omega*t)+C2*np.sin(omega*t))+x0
```

```
plt.plot(refSol[:,0], refSol[:,1], 'r-') #exact solution
```

Now we can load our results from the default solution file coordinatesSolution.txt, which is in the same directory as your python tutorial file. For convenient reading the file containing commented lines, we use a numpy feature and finally plot the displacement of coordinate 0 or our mass point<sup>3</sup>:

```
data = np.loadtxt('coordinatesSolution.txt', comments='#', delimiter=',')
plt.plot(data[:,0], data[:,1], 'b-') #numerical solution
```

In order to get a nice plot within Spyder, the following options can be used<sup>4</sup>:

```
ax=plt.gca() # get current axes
ax.grid(True, 'major', 'both')
ax.xaxis.set_major_locator(ticker.MaxNLocator(10))
ax.yaxis.set_major_locator(ticker.MaxNLocator(10))
plt.tight_layout()
plt.show()
```

Further examples can be found in your copy of exudyn:

main/pythonDev/Examples

<sup>&</sup>lt;sup>3</sup>data[:,0] contains the simulation time, data[:,1] contains displacement of (global) coordinate 0, data[:,2] contains displacement of (global) coordinate 1, ...)

<sup>&</sup>lt;sup>4</sup>note, in some environments you need finally the command plt.show()

## Chapter 4

## Python-C++ command interface

This section lists the basic interface functions which can be used to set up a EXUDYN model in Python.

To import the module, just include the EXUDYN module in Python (for compatibility with examples and other users, we recommend to use the 'exu' abbreviation throughout)<sup>1</sup>:

```
import exudyn as exu
```

The exudyn module will usually hold one SystemContainer, which is a class that is initialized by assigning a system container to a variable, usually denoted as 'SC':

```
SC = exu.SystemContainer()
```

Furthermore, there are a couple of commands available directly in the EXUDYN module, given in the following subsections. Regarding the **(basic) module access**, functions are related to the 'exudyn = exu' module, see these examples:

```
import exudyn as exu

SC = exu.SystemContainer()
exu.InfoStat()
exu.Go()
nInvalid = exu.InvalidIndex()
```

Understanding the usage of functions for python object 'SystemContainer' provided by EXUDYN, the following examples might help:

```
import exudyn as exu

SC = exu.SystemContainer()

mbs = SC.AddSystem()

nSys = SC.NumberOfSystems()

print(nSys)

SC.Reset()
```

<sup>&</sup>lt;sup>1</sup>note that there is a second module, called exudynFast, which does deactivates all range-, index- or memory allocation checks at the gain of higher speed (probably 30 percent in regular cases). To check which version you have, just type exu.\_\_doc\_\_ and you will see a note on 'exudynFast' in the exudynFast module.

Understanding the usage of functions for the 'MainSystem' provided by SystemContainer, the following examples might help:

```
import exudyn as exu

SC = exu.SystemContainer()

mbs = SC.AddSystem()

mbs.Reset()

mbs.WaitForUserToContinue()
```

#### 4.1 EXUDYN

These are the access functions to the EXUDYN module.

function/structure name	description
Go()	Creates a SystemContainer SC and a main system mbs
InfoStat()	Print some global (debug) information: linear algebra,
	memory allocation, threads, computational efficiency, etc.
StartRenderer()	Start OpenGL rendering engine (in separate thread)
StopRenderer()	Stop OpenGL rendering engine
SetOutputPrecision(numberOfDigits)	Set the precision (integer) for floating point numbers writ-
	ten to console (reset when simulation is started!)
InvalidIndex()	This function provides the invalid index, which depends
	on the kind of 32-bit, 64-bit signed or unsigned integer;
	e.g. node index or item index in list
SetWriteToConsole(flag)	set flag to write (true) or not write to console; default =
	true
SetWriteToFile(filename, flagWriteToFile = true, flagAp-	set flag to write (true) or not write to console; default
pend = false)	value of flagWriteToFile = false; flagAppend appends
	output to file, if set true; in order to finalize the file, write
	exu.SetWriteToFile(", False) to close the output file
	EXAMPLE:
	exu.SetWriteToConsole(False) #no output to console
	exu.SetWriteToFile(filename='testOutput.log', flag-
	WriteToFile=True, flagAppend=False)
	exu.Print('print this to file')
	exu.SetWriteToFile(", False) #terminate writing to file
	which closes the file
Set Print Delay Milli Seconds (delay Milli Seconds)	add some delay (in milliSeconds) to printing to console,
	in order to let Spyder process the output; default = 0
Print(pyObject)	this print command allows printing via exudyn, which
	allows to redirect all output to file; can print strings as
	well as printable python objects

## 4.2 SystemContainer

The SystemContainer is the top level of structures in EXUDYN. The container holds all systems, solvers and all other data structures for computation. Currently, only one container shall be used. In future, multiple containers might be usable at the same time.

Example:

import exudyn as exu
SC = exu.SystemContainer()
mbs = SC.AddSystem()

function/structure name	description
AddSystem()	add a new computational system
Reset()	delete all systems and reset SystemContainer (including
	graphics)
NumberOfSystems()	obtain number of systems available in system container
GetSystem(systemNumber)	obtain systems with index from system container
WaitForRenderEngineStopFlag()	Wait for user to stop render engine (Press 'Q' or Escape-
	key)
RenderEngineZoomAll()	Send zoom all signal, which will perform zoom all at next
	redraw request
GetRenderState()	Get dictionary with current render state (openGL zoom,
	modelview, etc.)
	EXAMPLE:
	SC = exu.SystemContainer()
	d = SC.GetRenderState()
	print(d['zoom'])
RedrawAndSaveImage()	Redraw openGL scene and save image (command waits
	until process is finished)
TimeIntegrationSolve(mainSystem, solverName, simula-	Call time integration solver for given system with
tionSettings)	solverName ('RungeKutta1'explicit solver, 'General-
	izedAlpha'implicit solver); use simulationSettings to
	individually configure the solver
	EXAMPLE:
	simSettings = exu.SimulationSettings()
	simSettings.timeIntegration.numberOfSteps = 1000
	simSettings.timeIntegration.endTime = 2
	simSettings.timeIntegration.verboseMode = 1
	SC. Time Integration Solve (mbs, 'Generalized Alpha', sim Setting and the solution of the so
StaticSolve(mainSystem, simulationSettings)	Call solver to compute a static solution of the system, con-
	sidering acceleration and velocity coordinates to be zero
	(initial velocities may be considered by certain objects)
	EXAMPLE:
	simSettings = exu.SimulationSettings()
	simSettings.staticSolver.newton.relativeTolerance = 1e-6
	SC.StaticSolve(mbs, simSettings)

visualizationSettings	this structure is read/writeable and contains visualization
	settings, which are immediately applied to the rendering
	window.
	EXAMPLE:
	SC = exu.SystemContainer()
	SC.visualizationSettings.autoFitScene=False

### 4.3 MainSystem

This is the structure which defines a (multibody) system. In C++, there is a MainSystem (links to python) and a System (computational part). For that reason, the name is MainSystem on the python side, but it is often just called 'system'. It can be created, visualized and computed. Use the following functions for system manipulation.

#### Usage:

```
import exudyn as exu
SC = exu.SystemContainer()
mbs = SC.AddSystem()
```

function/structure name	description
Assemble()	assemble items (nodes, bodies, markers, loads,);
	Calls CheckSystemIntegrity(), AssembleCoordinates(),
	AssembleLTGLists(), and AssembleInitializeSystemCoor-
	dinates()
AssembleCoordinates()	assemble coordinates: assign computational coordinates
	to nodes and constraints (algebraic variables)
AssembleLTGLists()	build local-to-global (ltg) coordinate lists for objects (used
	to build global ODE2RHS, MassMatrix, etc. vectors and
	matrices)
AssembleInitializeSystemCoordinates()	initialize all system-wide coordinates based on initial val-
	ues given in nodes
Reset()	reset all lists of items (nodes, bodies, markers, loads,)
	and temporary vectors; deallocate memory
WaitForUserToContinue()	interrupt further computation until user input -> 'pause'
	function
SendRedrawSignal()	this function is used to send a signal to the renderer that
	the scene shall be redrawn because the visualization state
	has been updated
GetRenderEngineStopFlag()	get the current stop simulation flag; true=user wants to
	stop simulation
SetRenderEngineStopFlag()	set the current stop simulation flag; set to false, in order to
	continue a previously user-interrupted simulation

repr()	return the representation of the system, which can be, e.g.,
()	,
	printed
	EXAMPLE:
	print(mbs)
systemIsConsistent	this flag is used by solvers to decide, whether the system
	is in a solvable state; this flag is set to false as long as
	Assemble() has not been called; any modification to the
	system, such as Add(), Modify(), etc. will set the flag
	to false again; this flag can be modified (set to true), if
	a change of e.g. an object (change of stiffness) or load
	(change of force) keeps the system consistent, but would
	normally lead to systemIsConsistent=False
solverSignalJacobianUpdate	this flag is used by solvers to decide, whether the jaco-
	bian should be updated; at beginning of simulation and
	after jacobian computation, this flag is set automatically to
	False; use this flag to indicate system changes, e.g. during
	time integration
systemData	Access to SystemData structure; enables access to number
	of nodes, objects, and to (current, initial, reference,)
	state variables (ODE2, AE, Data,)

#### 4.3.1 MainSystem: Node

This section provides functions for adding, reading and modifying nodes. Nodes are used to define coordinates (unknowns to the static system and degrees of freedom if constraints are not present). Nodes can provide various types of coordinates for second/first order differential equations (ODE2/ODE1), algebraic equations (AE) and for data (history) variables – which are not providing unknowns in the nonlinear solver but will be solved in an additional nonlinear iteration for e.g. contact, friction or plasticity.

function/structure name	description
AddNode(itemDict)	add a node with nodeDefinition in dictionary format; re-
	turns (global) node number of newly added node
	EXAMPLE:
	nodeDict = {'nodeType': 'Point',
	'referenceCoordinates': [1.0, 0.0, 0.0],
	'initialDisplacements': [0.0, 2.0, 0.0],
	'name': 'example node'}
	mbs.AddNode(nodeDict)
AddNode(pyObject)	add a node with nodeDefinition from Python node class;
	returns (global) node number of newly added node
	EXAMPLE:
	item = Rigid2D( referenceCoordinates= [1,0.5,0], initialVe-
	locities= [10,0,0])
	mbs.AddNode(item)

GetNodeNumber(nodeName)	get node's number by name (string)
	EXAMPLE:
	n = mbs.GetNodeNumber('example node')
GetNode(nodeNumber)	get node's dictionary by index
	EXAMPLE:
	nodeDict = mbs.GetNode(0)
ModifyNode(nodeNumber, nodeDict)	modify node's dictionary by index
	EXAMPLE:
	mbs.ModifyNode(nodeNumber, nodeDict)
GetNodeDefaults(typeName)	get node's default values for a certain nodeType as (dic-
	tionary)
	EXAMPLE:
	nodeType = 'Point'
	nodeDict = mbs.GetNodeDefaults(nodeType)
CallNodeFunction(nodeNumber, functionName, args =	call specific node function
dict())	
GetNodeOutput(nodeNumber, variableType, configura-	get the ouput of the node specified with the OutputVari-
tion = ConfigurationType.Current)	ableType; default configuration = 'current'; output may
	be scalar or array (e.g. displacement vector)
	EXAMPLE:
	mbs.GetNodeOutput(nodeNumber=0, variable-
	Type='exu.OutputVariable.Displacement')
GetNodeODE2Index(nodeNumber)	get index in the global ODE2 coordinate vector for the first
	node coordinate of the specified node
	EXAMPLE:
	mbs.GetNodeODE2Index(nodeNumber=0)
GetNodeParameter(nodeNumber, parameterName)	get nodes's parameter from nodeNumber and parame-
	terName; parameter names can be found for the specific
	items in the reference manual
SetNodeParameter(nodeNumber, parameterName,	set parameter 'parameterName' of node with nodeNum-
value)	ber to value; parameter names can be found for the specific
	items in the reference manual

#### 4.3.2 MainSystem: Object

This section provides functions for adding, reading and modifying objects, which can be bodies (mass point, rigid body, finite element, ...), connectors (spring-damper or joint) or general objects. Objects provided terms to the residual of equations resulting from every coordinate given by the nodes. Single-noded objects (e.g. mass point) provides exactly residual terms for its nodal coordinates. Connectors constrain or penalize two markers, which can be, e.g., position, rigid or coordinate markers. Thus, the dependence of objects is either on the coordinates of the marker-objects/nodes or on nodes which the objects possess themselves.

function/structure name	description

AddObject(itemDict)	add a object with objectDefinition in dictionary format; returns (global) object number of newly added object <b>EXAMPLE</b> : objectDict = {'objectType': 'MassPoint', 'physicsMass': 10, 'nodeNumber': 0,
	'name': 'example object'} mbs.AddObject(objectDict)
AddObject(pyObject)	add a object with objectDefinition from Python object class; returns (global) object number of newly added object  EXAMPLE:  item = MassPoint(name='heavy object', nodeNumber=0, physicsMass=100)  mbs.AddObject(item)
GetObjectNumber(objectName)	get object's number by name (string)  EXAMPLE:  n = mbs.GetObjectNumber('heavy object')
GetObject(objectNumber)	get object's dictionary by index  EXAMPLE: objectDict = mbs.GetObject(0)
ModifyObject(objectNumber, objectDict)	modify object's dictionary by index  EXAMPLE:  mbs.ModifyObject(objectNumber, objectDict)
GetObjectDefaults(typeName)	get object's default values for a certain objectType as (dictionary)  EXAMPLE: objectType = 'MassPoint' objectDict = mbs.GetObjectDefaults(objectType)
CallObjectFunction(objectNumber, functionName, args = dict())	call specific object function
GetObjectOutput(objectNumber, variableType)	get object's output variable from objectNumber and OutputVariableType
GetObjectOutputBody(objectNumber, variableType, localPosition, configuration)	get body's output variable from objectNumber and OutputVariableType  EXAMPLE:  u = mbs.GetObjectOutputBody(objectNumber = 1, variableType = exu.OutputVariableType.Position, localPosition=[1,0,0], configuration = exu.ConfigurationType.Initial)
GetObjectParameter(objectNumber, parameterName)	get objects's parameter from objectNumber and parameterName; parameter names can be found for the specific items in the reference manual
SetObjectParameter(objectNumber, parameterName, value)	set parameter 'parameterName' of object with objectNumber to value; parameter names can be found for the specific items in the reference manual

#### 4.3.3 MainSystem: Marker

This section provides functions for adding, reading and modifying markers. Markers define how to measure primal kinematical quantities on objects or nodes (e.g., position, orientation or coordinates themselves), and how to act on the quantities which are dual to the kinematical quantities (e.g., force, torque and generalized forces). Markers provide unique interfaces for loads, sensors and constraints in order to address these quantities independently of the structure of the object or node (e.g., rigid or flexible body).

function/structure name	description
AddMarker(itemDict)	add a marker with markerDefinition in dictionary format;
	returns (global) marker number of newly added marker
	EXAMPLE:
	markerDict = {'markerType': 'NodePosition',
	'nodeNumber': 0,
	'name': 'position0'}
	mbs.AddMarker(markerDict)
AddMarker(pyObject)	add a marker with markerDefinition from Python marker
	class; returns (global) marker number of newly added
	marker
	EXAMPLE:
	item = MarkerNodePosition(name='my
	marker',nodeNumber=1)
	mbs.AddMarker(item)
GetMarkerNumber(markerName)	get marker's number by name (string)
	EXAMPLE:
	n = mbs.GetMarkerNumber('my marker')
GetMarker(markerNumber)	get marker's dictionary by index
	EXAMPLE:
	markerDict = mbs.GetMarker(0)
ModifyMarker(markerNumber, markerDict)	modify marker's dictionary by index
	EXAMPLE:
	mbs.ModifyMarker(markerNumber, markerDict)
GetMarkerDefaults(typeName)	get marker's default values for a certain markerType as
	(dictionary)
	EXAMPLE:
	markerType = 'NodePosition'
	markerDict = mbs.GetMarkerDefaults(markerType)
GetMarkerParameter(markerNumber, parameterName)	get markers's parameter from markerNumber and param-
	eterName; parameter names can be found for the specific
	items in the reference manual
SetMarkerParameter(markerNumber, parameterName,	set parameter 'parameterName' of marker with marker-
value)	Number to value; parameter names can be found for the
	specific items in the reference manual

#### 4.3.4 MainSystem: Load

This section provides functions for adding, reading and modifying operating loads. Loads are used to act on the quantities which are dual to the primal kinematic quantities, such as displacement and rotation. Loads represent, e.g., forces, torques or generalized forces.

function/structure name	description	
AddLoad(itemDict)	add a load with loadDefinition in dictionary format; re-	
	turns (global) load number of newly added load	
	EXAMPLE:	
	loadDict = {'loadType': 'ForceVector',	
	'markerNumber': 0,	
	'loadVector': [1.0, 0.0, 0.0],	
	'name': 'heavy load'}	
	mbs.AddLoad(loadDict)	
AddLoad(pyObject)	add a load with loadDefinition from Python load class;	
	returns (global) load number of newly added load	
	EXAMPLE:	
	item = mbs.AddLoad(LoadForceVector(loadVector=[1,0,0],n	narkerNumbe
	load'))	
	mbs.AddLoad(item)	
GetLoadNumber(loadName)	get load's number by name (string)	
	EXAMPLE:	
	n = mbs.GetLoadNumber('heavy load')	
GetLoad(loadNumber)	get load's dictionary by index	
	EXAMPLE:	
	loadDict = mbs.GetLoad(0)	
ModifyLoad(loadNumber, loadDict)	modify load's dictionary by index	
	EXAMPLE:	
	mbs.ModifyLoad(loadNumber, loadDict)	
GetLoadDefaults(typeName)	get load's default values for a certain loadType as (dictio-	
	nary)	
	EXAMPLE:	
	loadType = 'ForceVector'	
	loadDict = mbs.GetLoadDefaults(loadType)	
GetLoadParameter(loadNumber, parameterName)	get loads's parameter from loadNumber and parameter-	
	Name; parameter names can be found for the specific	
	items in the reference manual	
Set Load Parameter (load Number, parameter Name, value)	set parameter 'parameterName' of load with loadNumber	
	to value; parameter names can be found for the specific	
	items in the reference manual	

#### 4.3.5 MainSystem: Sensor

This section provides functions for adding, reading and modifying operating sensors. Sensors are used to measure information in nodes, objects, markers, and loads for output in a file.

function/structure name	description
AddSensor(itemDict)	add a sensor with sensor definition in dictionary format;
	returns (global) sensor number of newly added sensor
	EXAMPLE:
	sensorDict = {'sensorType': 'Node',
	'nodeNumber': 0,
	'fileName': 'sensor.txt',
	'name': 'test sensor'}
	mbs.AddSensor(sensorDict)
AddSensor(pyObject)	add a sensor with sensor definition from Python sensor
	class; returns (global) sensor number of newly added
	sensor
	EXAMPLE:
	item = mbs.AddSensor(SensorNode(sensorType=exu.SensorType.Node
	sensor'))
	mbs.AddSensor(item)
GetSensorNumber(sensorName)	get sensor's number by name (string)
	EXAMPLE:
	n = mbs.GetSensorNumber('test sensor')
GetSensor(sensorNumber)	get sensor's dictionary by index
	EXAMPLE:
	sensorDict = mbs.GetSensor(0)
ModifySensor(sensorNumber, sensorDict)	modify sensor's dictionary by index
	EXAMPLE:
	mbs.ModifySensor(sensorNumber, sensorDict)
GetSensorDefaults(typeName)	get sensor's default values for a certain sensorType as
	(dictionary)
	EXAMPLE:
	sensorType = 'Node'
	sensorDict = mbs.GetSensorDefaults(sensorType)
GetSensorParameter(sensorNumber, parameterName)	get sensors's parameter from sensorNumber and param-
	eterName; parameter names can be found for the specific
	items in the reference manual
SetSensorParameter(sensorNumber, parameterName,	set parameter 'parameterName' of sensor with sensor-
value)	Number to value; parameter names can be found for the
	specific items in the reference manual

#### 4.4 SystemData

This is the data structure of a system which contains Objects (bodies/constraints/...), Nodes, Markers and Loads. The SystemData structure allows advanced access to this data, which HAS TO BE USED WITH CARE, as unexpected results and system crash might happen.

#### Usage:

```
#obtain current ODE2 system vector (e.g. after static simulation finished):
```

u = mbs.systemData.GetODE2Coordinates()

#set initial ODE2 vector for next simulation:

mbs.systemData.SetODE2Coordinates(coordinates=u,configurationType=exu.ConfigurationType.Initial)

function/structure name	description
NumberOfLoads()	return number of loads in system
	EXAMPLE:
	print(mbs.systemData.NumberOfLoads())
NumberOfMarkers()	return number of markers in system
	EXAMPLE:
	print(mbs.systemData.NumberOfMarkers())
NumberOfNodes()	return number of nodes in system
	EXAMPLE:
	print(mbs.systemData.NumberOfNodes())
NumberOfObjects()	return number of objects in system
	EXAMPLE:
	print(mbs.systemData.NumberOfObjects())
GetTime(configurationType =	88
exu.ConfigurationType.Current)	EXAMPLE:
	mbs.systemData.GetTime(exu.ConfigurationType.Initial)
SetTime(newTime, configurationType =	or con-Summer and control and the control and
exu.ConfigurationType.Current)	care, e.g. in user-defined solvers.
	EXAMPLE:
	mbs.systemData.SetTime(10.,
	exu.ConfigurationType.Initial)
GetCurrentTime()	DEPRICATED; get current (simulation) time; time is up-
	dated in time integration solvers and in static solver;
	use this function e.g. during simulation to define time-
	dependent loads
	EXAMPLE:
	mbs.systemData.GetCurrentTime()
SetVisualizationTime()	DEPRICATED; set time for render window (visualization)
	EXAMPLE:
	mbs.systemData.SetVisualizationTime(1.3)
Info()	print detailed system information for every item; for short
	information use print(mbs)
	EXAMPLE:
	mbs.systemData.Info()

#### 4.4.1 SystemData: Access coordinates

This section provides access functions to global coordinate vectors. Assigning invalid values or using wrong vector size might lead to system crash and unexpected results.

function/structure name	description
GetODE2Coordinates(configuration =	get ODE2 system coordinates (displacements) for given
exu.ConfigurationType.Current)	configuration (default: exu.Configuration.Current)
	EXAMPLE:
	uCurrent = mbs.systemData.GetODE2Coordinates()

CatODE2Casudinates(assudinates		ant ODE2 metale condinates (displacements) for since
SetODE2Coordinates(coordinates, configuration	=	set ODE2 system coordinates (displacements) for given
exu.ConfigurationType.Current)		configuration (default: exu.Configuration.Current); in-
		valid vector size may lead to system crash!
		EXAMPLE:
		mbs.systemData.SetODE2Coordinates(uCurrent)
GetODE2Coordinates_t(configuration	=	get ODE2 system coordinates (velocities) for given config-
exu.ConfigurationType.Current)		uration (default: exu.Configuration.Current)
		EXAMPLE:
		vCurrent = mbs.systemData.GetODE2Coordinates_t()
SetODE2Coordinates_t(coordinates, configuration	=	set ODE2 system coordinates (velocities) for given con-
exu.ConfigurationType.Current)		figuration (default: exu.Configuration.Current); invalid
		vector size may lead to system crash!
		EXAMPLE:
		mbs.systemData.SetODE2Coordinates_t(vCurrent)
GetODE1Coordinates(configuration	=	get ODE1 system coordinates (displacements) for given
exu.ConfigurationType.Current)		configuration (default: exu.Configuration.Current)
		EXAMPLE:
		qCurrent = mbs.systemData.GetODE1Coordinates()
SetODE1Coordinates(coordinates, configuration	=	set ODE1 system coordinates (displacements) for given
exu.ConfigurationType.Current)		configuration (default: exu.Configuration.Current); in-
		valid vector size may lead to system crash!
		EXAMPLE:
		mbs.systemData.SetODE1Coordinates(qCurrent)
GetAECoordinates(configuration	=	get algebraic equations (AE) system coordinates for given
exu.ConfigurationType.Current)		configuration (default: exu.Configuration.Current)
		EXAMPLE:
		lambdaCurrent = mbs.systemData.GetAECoordinates()
SetAECoordinates(coordinates, configuration	=	set algebraic equations (AE) system coordinates for given
exu.ConfigurationType.Current)		configuration (default: exu.Configuration.Current); in-
		valid vector size may lead to system crash!
		EXAMPLE:
		mbs.systemData.SetAECoordinates(lambdaCurrent)
GetDataCoordinates(configuration	=	get system data coordinates for given configuration (de-
exu.ConfigurationType.Current)		fault: exu.Configuration.Current)
,		EXAMPLE:
		dataCurrent = mbs.systemData.GetDataCoordinates()
SetDataCoordinates(coordinates, configuration	=	set system data coordinates for given configuration (de-
exu.ConfigurationType.Current)		fault: exu.Configuration.Current); invalid vector size may
0 71		lead to system crash!
		EXAMPLE:
		mbs.systemData.SetDataCoordinates(dataCurrent)
GetSystemState(configuration	=	get system state for given configuration (default:
exu.ConfigurationType.Current)		exu.Configuration.Current); state vectors do not include
John Gardiner, Percurrent,		the non-state derivatives ODE1_t and ODE2_tt and the
		time; function is copying data - not highly efficient; format
		of pyList: [ODE2Coords, ODE2Coords_t, ODE1Coords,
		AEcoords, dataCoords]  EXAMPLE:
		sysStateList = mbs.systemData.GetSystemState()

SetSystemState(systemStateList,	configuration	=	set system data coordinates for given configuration (de-
exu.ConfigurationType.Current)			fault: exu.Configuration.Current); invalid list of vectors
			/ vector size may lead to system crash; write access to
			state vectors (but not the non-state derivatives ODE1_t
			and ODE2_tt and the time); function is copying data
			- not highly efficient; format of pyList: [ODE2Coords,
			ODE2Coords_t, ODE1Coords, AEcoords, dataCoords]
			EXAMPLE:
			mbs.systemData.SetDataCoordinates(sysStateList, con-
			figurationType = exu.ConfigurationType.Initial)

#### 4.4.2 SystemData: Get object local-to-global (LTG) coordinate mappings

This section provides access functions the LTG-lists for every object (body, constraint, ...) in the system.

function/structure name	description
GetObjectLTGODE2(objectNumber)	get local-to-global coordinate mapping (list of global coor-
	dinate indices) for ODE2 coordinates; only available after
	Assemble()
	EXAMPLE:
	ltgObject4 = mbs.systemData.GetObjectLTGODE2(4)
GetObjectLTGODE1(objectNumber)	get local-to-global coordinate mapping (list of global coor-
	dinate indices) for ODE1 coordinates; only available after
	Assemble()
	EXAMPLE:
	ltgObject4 = mbs.systemData.GetObjectLTGODE1(4)
GetObjectLTGAE(objectNumber)	get local-to-global coordinate mapping (list of global coor-
	dinate indices) for algebraic equations (AE) coordinates;
	only available after Assemble()
	EXAMPLE:
	ltgObject4 = mbs.systemData.GetObjectLTGODE2(4)
GetObjectLTGData(objectNumber)	get local-to-global coordinate mapping (list of global co-
	ordinate indices) for data coordinates; only available after
	Assemble()
	EXAMPLE:
	ltgObject4 = mbs.systemData.GetObjectLTGData(4)

## 4.5 Type definitions

This section defines a couple of structures, which are used to select, e.g., a configuration type or a variable type. In the background, these types are integer numbers, but for safety, the types should be used as type variables. Conversion to integer is possible:

x = int(exu.OutputVariableType.Displacement)

and also conversion from integer:

#### 4.5.1 OutputVariableType

This section shows the OutputVariableType structure, which is used for selecting output values, e.g. for GetObjectOutput(...) or for selecting variables for contour plot.

Available output variables and the interpreation of the output variable can be found at the object definitions. The Output VariableType does not provide information about the size of the output variable, which can be either scalar or a list (vector). For vector output quantities, the contour plot option offers an additional parameter for selection of the Component of the OutputVariableType.

function/structure name	description
None	no value; used, e.g., to select no output variable in contour
	plot
Distance	e.g., measure distance in spring damper connector
Position	measure 3D position, e.g., of node or body
Displacement	measure displacement; usually difference between current
	position and reference position
Velocity	measure (translational) velocity of node or object
Acceleration	measure (translational) acceleration of node or object
RotationMatrix	measure rotation matrix of rigid body node or object
AngularVelocity	measure angular velocity of node or object
AngularAcceleration	measure angular acceleration of node or object
Rotation	measure, e.g., scalar rotation of 2D body or rotation within
	a joint
Coordinates	measure the coordinates of a node or object; coordinates
	usually just contain displacements, but not the position
	values
Coordinates_t	measure the time derivative of coordinates (= velocity co-
	ordinates) of a node or object
SlidingCoordinate	measure sliding coordinate in sliding joint
Director1	measure a director (e.g. of a rigid body frame), or a slope
	vector in local 1 or x-direction
Director2	measure a director (e.g. of a rigid body frame), or a slope
	vector in local 2 or y-direction
Director3	measure a director (e.g. of a rigid body frame), or a slope
	vector in local 3 or z-direction
Force	measure force, e.g., in joint or beam (resultant force)
Torque	measure torque, e.g., in joint or beam (resultant couple/-
	moment)
Strain	measure strain, e.g., axial strain in beam
Stress	measure stress, e.g., axial stress in beam
Curvature	measure curvature; may be scalar or vectorial: twist and
	curvature
EndOfEnumList	this marks the end of the list, usually not important to the
	user

#### 4.5.2 ConfigurationType

This section shows the ConfigurationType structure, which is used for selecting a configuration for reading or writing information to the module. Specifically, the ConfigurationType.Current configuration is usually used at the end of a solution process, to obtain result values, or the ConfigurationType.Initial is used to set initial values for a solution process.

function/structure name	description
None	no configuration; usually not valid, but may be used, e.g.,
	if no configurationType is required
Initial	initial configuration prior to static or dynamic solver;
	is computed during mbs.Assemble() or AssembleInitial-
	izeSystemCoordinates()
Current	current configuration during and at the end of the com-
	putation of a step (static or dynamic)
Reference	configuration used to define deformable bodies (reference
	configuration for finite elements) or joints (configuration
	for which some joints are defined)
StartOfStep	during computation, this refers to the solution at the start
	of the step = end of last step, to which the solver falls back
	if convergence fails
Visualization	this is a state completely de-coupled from computation,
	used for visualization
EndOfEnumList	this marks the end of the list, usually not important to the
	user

#### 4.5.3 LinearSolverType

This section shows the LinearSolverType structure, which is used for selecting output values, e.g. for GetObjectOutput(...) or for selecting variables for contour plot.

function/structure name	description
None	no value; used, e.g., if no solver is selected
EXUdense	use dense matrices and according solvers for densly popu-
	lated matrices (usually the CPU time grows cubically with
	the number of unknowns)
EigenSparse	use sparse matrices and according solvers; additional
	overhead for very small systems; specifically, memory al-
	location is performed during a factorization process

## **Chapter 5**

# Objects, nodes, markers, loads and sensors reference manual

This section includes the reference manual for all objects (bodies/constraints), nodes, markers, loads and sensors.

#### 5.1 List of Items

The following items are available in EXUDYN:

- NodePoint
- NodePoint2D
- NodeRigidBodyEP
- NodeRigidBody2D
- NodePoint2DSlope1
- NodeGenericODE2
- NodeGenericData
- NodePointGround
- ObjectMassPoint
- ObjectMassPoint2D
- ObjectRigidBody
- ObjectRigidBody2D
- ObjectANCFCable2D
- ObjectALEANCFCable2D
- ObjectGround
- ObjectConnectorSpringDamper
- ObjectConnectorCartesianSpringDamper
- ObjectConnectorCoordinateSpringDamper

- ObjectConnectorDistance
- ObjectConnectorCoordinate
- ObjectContactCoordinate
- ObjectContactCircleCable2D
- ObjectContactFrictionCircleCable2D
- ObjectJointSliding2D
- ObjectJointALEMoving2D
- ObjectJointRevolute2D
- ObjectJointPrismatic2D
- MarkerBodyMass
- MarkerBodyPosition
- MarkerBodyRigid
- MarkerNodePosition
- MarkerNodeRigid
- MarkerNodeCoordinate
- MarkerBodyCable2DShape
- MarkerBodyCable2DCoordinates
- LoadForceVector
- LoadTorqueVector
- LoadMassProportional
- LoadCoordinate
- SensorNode

#### 5.2 Nodes

#### 5.2.1 NodePoint

A 3D point node for point masses or solid finite elements which has 3 displacement degrees of freedom for second order differential equations.

Short name for Python: Point

Output variables (chose type, e.g., OutputVariableType.Position):

- Position: global 3D position vector of node (=displacement+reference position)
- **Displacement**: global 3D displacement vector of node
- Velocity: global 3D velocity vector of node
- Coordinates: coordinates vector of node
- Coordinates\_t: velocity coordinates vector of node

The item NodePoint has the following parameters:

Name	type	size	default value	description
type = 'Point'	·	<u> </u>		item typename for initialization
name	String		"	node"s unique name
referenceCoordinates	Vector3D	3	[0.,0.,0.]	reference coordinates of node ==> e.g. ref.
				coordinates for finite elements; global posi-
				tion of node without displacement
initialDisplacements	Vector3D	3	[0.,0.,0.]	initial displacement coordinate
initialVelocities	Vector3D	3	[0.,0.,0.]	initial velocity coordinate
visualization	VNodePoint			parameters for visualization of item

The item VNodePoint has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size (diameter, dimensions of un-
				derlying cube, etc.) for item; size == -1.f
				means that default size is used
color	Float4	4	[-1.,-1.,-1.]	Default RGBA color for nodes; 4th value
				is alpha-transparency; R=-1.f means, that
				default color is used

#### 5.2.2 NodePoint2D

A 2D point node for point masses or solid finite elements which has 2 displacement degrees of freedom for second order differential equations.

**Short name** for Python: **Point2D** 

**Output variables** (chose type, e.g., OutputVariableType.Position):

- Position: global 3D position vector of node (=displacement+reference position)
- Displacement: global 3D displacement vector of node
- Velocity: global 3D velocity vector of node
- Coordinates: coordinates vector of node
- Coordinates\_t: velocity coordinates vector of node

The item NodePoint2D has the following parameters:

Name	type	size	default value	description
type = 'Point2D'				item typename for initialization
name	String		"	node"s unique name
referenceCoordinates	Vector2D	2	[0.,0.]	reference coordinates of node ==> e.g. ref.
				coordinates for finite elements; global posi-
				tion of node without displacement

initialDisplacements	Vector2D	2	[0.,0.]	initial displacement coordinate
initialVelocities	Vector2D	2	[0.,0.]	initial velocity coordinate
visualization	VNodePoint2D			parameters for visualization of item

The item VNodePoint2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size (diameter, dimensions of un-
				derlying cube, etc.) for item; size == -1.f
				means that default size is used
color	Float4	4	[-1.,-1.,-1.]	Default RGBA color for nodes; 4th value
				is alpha-transparency; R=-1.f means, that
				default color is used

#### 5.2.3 NodeRigidBodyEP

A 3D rigid body node based on Euler parameters for rigid bodies or beams; the node has 3 displacement coordinates (displacements of center of mass - COM: ux,uy,uz) and four rotation coordinates (Euler parameters = quaternions); all coordinates lead to second order differential equations; additionally there is one constraint equation for quaternions; The rotation matrix **A**, transforming local (body-fixed) 3D positions  $\mathbf{p}_{loc} = [p_{loc}^x \ p_{loc}^y \ p_{loc}^z]^T$  to global 3D positions  $\mathbf{p}_{glob} = [p_{glob}^x \ p_{glob}^y \ p_{glob}^z]^T$ ,

$$\mathbf{p}_{oloh} = \mathbf{A}\mathbf{p}_{loc},\tag{5.1}$$

is defined according to the book of Shabana, same with the transformation matrix G between time derivatives of Euler parameters and angular velocities.

Short name for Python: Rigid3DEP

Output variables (chose type, e.g., Output Variable Type. Position):

- Position: global 3D position vector of node (=displacement+reference position)
- Displacement: global 3D displacement vector of node
- Velocity: global 3D velocity vector of node
- AngularVelocity: global 3D velocity vector of node
- Coordinates: coordinates vector of node
- Coordinates\_t: velocity coordinates vector of node

The item NodeRigidBodyEP has the following parameters:

Name	type	size	default value	description
type = 'RigidBodyEP'				item typename for initialization

name	String		"	node"s unique name
referenceCoordinates	Vector7D	3	[0.,0.,0., 0.,0.,0.,0.]	reference coordinates (x-pos,y-pos,z-pos
				and 4 Euler parameters) of node ==> e.g.
				ref. coordinates for finite elements or refer-
				ence position of rigid body (e.g. for defini-
				tion of joints)
initialDisplacements	Vector7D	3	[0.,0.,0., 0.,0.,0.,0.]	initial displacement coordinates: ux,uy,uz
				and 4 Euler parameters relative to reference
				coordinates
initialVelocities	Vector7D	3	[0.,0.,0., 0.,0.,0.,0.]	initial velocity coordinate: time derivatives
				of ux,uy,uz and 4 Euler parameters
visualization	VNodeRigidBodyE	P		parameters for visualization of item

The item VNodeRigidBodyEP has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size (diameter, dimensions of un-
				derlying cube, etc.) for item; size == -1.f
				means that default size is used
color	Float4	4	[-1.,-1.,-1.]	Default RGBA color for nodes; 4th value
				is alpha-transparency; R=-1.f means, that
				default color is used

#### 5.2.4 NodeRigidBody2D

A 2D rigid body node for rigid bodies or beams; the node has 2 displacement degrees of freedom (displacement of center of mass - COM: ux,uy) and one rotation coordinate (rotation around z-axis: uphi); all coordinates lead to second order differential equations; The rotation matrix  $\mathbf{A}$ , transforming local (body-fixed) 3D positions  $\mathbf{p}_{loc} = [p_{loc}^x \ p_{loc}^y \ p_{loc}^y]^T$  to global 3D positions  $\mathbf{p}_{glob} = [p_{glob}^x \ p_{glob}^y]^T$ ,

$$\mathbf{p}_{glob} = \mathbf{A}\mathbf{p}_{loc},\tag{5.2}$$

is defined as

$$\mathbf{A} = \begin{bmatrix} \cos(\varphi) & -\sin(\varphi) \\ \sin(\varphi) & \cos(\varphi) \end{bmatrix}. \tag{5.3}$$

Short name for Python: Rigid2D

Output variables (chose type, e.g., OutputVariableType.Position):

- Position: global 3D position vector of node (=displacement+reference position)
- Displacement: global 3D displacement vector of node
- Velocity: global 3D velocity vector of node

- Coordinates: coordinates vector of node
- Coordinates\_t: velocity coordinates vector of node

The item NodeRigidBody2D has the following parameters:

Name	type	size	default value	description
type = 'RigidBody2D'	·			item typename for initialization
name	String		"	node"s unique name
referenceCoordinates	Vector3D	3	[0.,0.,0.]	reference coordinates (x-pos,y-pos and ro-
				tation phi) of node ==> e.g. ref. coordi-
				nates for finite elements; global position of
				node without displacement
initialDisplacements	Vector3D	3	[0.,0.,0.]	initial displacement coordinates: ux, uy
				and uphi
initialVelocities	Vector3D	3	[0.,0.,0.]	initial velocity coordinate: vx, vy, omega
visualization	VNodeRigidBody2	:D		parameters for visualization of item

The item VNodeRigidBody2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size (diameter, dimensions of un-
				derlying cube, etc.) for item; size == -1.f
				means that default size is used
color	Float4	4	[-1.,-1.,-1.]	Default RGBA color for nodes; 4th value
				is alpha-transparency; R=-1.f means, that
				default color is used

#### 5.2.5 NodePoint2DSlope1

A 2D point/slope vector node for planar Bernoulli-Euler ANCF (absolute nodal coordinate formulation) beam elements; the node has 4 displacement degrees of freedom (2 for displacement of point node and 2 for the slope vector 'slopex'); all coordinates lead to second order differential equations; the slope vector defines the directional derivative w.r.t the local axial (x) coordinate, denoted as ()'; in straight configuration aligned at the global x-axis, the slope vector reads  $\mathbf{r}' = [r'_x \ r'_y]^T = [1 \ 0]^T$ .

Short name for Python: Point2DS1

Output variables (chose type, e.g., OutputVariableType.Position):

- Position: global 3D position vector of node (=displacement+reference position)
- Displacement: global 3D displacement vector of node
- Velocity: global 3D velocity vector of node
- Coordinates: coordinates vector of node (2 displacement coordinates + 2 slope vector coordinates)

• **Coordinates\_t**: velocity coordinates vector of node (derivative of the 2 displacement coordinates + 2 slope vector coordinates)

The item NodePoint2DSlope1 has the following parameters:

Name	type	size	default value	description
type = 'Point2DSlope1'		item typename for initialization		
name	String		"	node"s unique name
referenceCoordinates	Vector4D	4	[0.,0.,1.,0.]	reference coordinates (x-pos,y-pos; x-slopex, y-slopex) of node; global position of node without displacement
initialDisplacements	Vector4D	4	[0.,0.,0.]	initial displacement coordinates: ux, uy and x/y "displacements" of slopex
initialVelocities	Vector4D	4	[0.,0.,0.]	initial velocity coordinates
visualization	VNodePoint2D	Slope1		parameters for visualization of item

The item VNodePoint2DSlope1 has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size (diameter, dimensions of un-
				derlying cube, etc.) for item; size == -1.f
				means that default size is used
color	Float4	4	[-1.,-1.,-1.]	Default RGBA color for nodes; 4th value
				is alpha-transparency; R=-1.f means, that
				default color is used

#### 5.2.6 NodeGenericODE2

A node containing a number of ODE2 variables; use e.g. for scalar dynamic equations (Mass1D) or for the ALECable element.

**Output variables** (chose type, e.g., OutputVariableType.Position):

- Coordinates: coordinates vector of node
- Coordinates\_t: velocity coordinates vector of node

The item NodeGenericODE2 has the following parameters:

Name	type	size	default value	description
type = 'GenericODE2'				item typename for initialization
name	String		"	node"s unique name
referenceCoordinates	Vector			generic reference coordinates of node; must be consistent with numberO- fODE2Coordinates

initialCoordinates	Vector		[]	initial displacement coordinates;
				must be consistent with numberO-
				fODE2Coordinates
initialCoordinates_t	Vector		[]	initial velocity coordinates; must be consis-
				tent with numberOfODE2Coordinates
numberOfODE2Coordinates	Index		0	number of generic ODE2 coordinates
visualization	VNodeGenericODE2	2		parameters for visualization of item

The item VNodeGenericODE2 has the following parameters:

Name	type	size	default value	description
show	bool		False	set true, if item is shown in visualization
				and false if it is not shown

#### 5.2.7 NodeGenericData

A node containing a number of data (history) variables; use e.g. for contact (active set), friction or plasticity (history variable).

Output variables (chose type, e.g., OutputVariableType.Position):

• Coordinates: data coordinates (history variables) vector of node

The item NodeGenericData has the following parameters:

Name	type	size	default value	description
type = 'GenericData'	·			item typename for initialization
name	String		"	node"s unique name
initialCoordinates	Vector		[]	initial data coordinates
numberOfDataCoordinates	Index		0	number of generic data coordinates (history
				variables)
visualization	VNodeGenericData	1		parameters for visualization of item

The item VNodeGenericData has the following parameters:

Name	type	size	default value	description
show	bool		False	set true, if item is shown in visualization
				and false if it is not shown

#### 5.2.8 NodePointGround

A 3D point node fixed to ground. The node can be used as NodePoint, but does not lead to equations. Applied or reaction forces do not have any effect.

Short name for Python: PointGround

**Output variables** (chose type, e.g., OutputVariableType.Position):

• **Position**: global 3D position vector of node (=reference position)

• **Displacement**: zero 3D vector

• Velocity: zero 3D vector

Coordinates: vector of length zeroCoordinates\_t: vector of length zero

The item NodePointGround has the following parameters:

Name	type	size	default value	description
type = 'PointGround'			item typename for initialization	
name	String		"	node"s unique name
referenceCoordinates	Vector3D	3	[0.,0.,0.]	reference coordinates of node ==> e.g. ref.
				coordinates for finite elements; global posi-
				tion of node without displacement
visualization	VNodePointGround	d		parameters for visualization of item

The item VNodePointGround has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size (diameter, dimensions of un-
				derlying cube, etc.) for item; size == -1.f
				means that default size is used
color	Float4	4	[-1.,-1.,-1.]	Default RGBA color for nodes; 4th value
				is alpha-transparency; R=-1.f means, that
				default color is used

#### 5.3 Objects

#### 5.3.1 ObjectMassPoint

A 3D mass point which is attached to a position-based node. Equations of motion with the displacements  $[u_x \ u_y \ u_z]^T$ , the mass m and the residual of all forces  $[R_x \ R_y \ R_z]^T$  are given as

$$\begin{bmatrix} m \cdot \ddot{u}_x \\ m \cdot \ddot{u}_y \\ m \cdot \ddot{u}_z \end{bmatrix} = \begin{bmatrix} R_x \\ R_y \\ R_z \end{bmatrix}. \tag{5.4}$$

Short name for Python: MassPoint

Output variables (chose type, e.g., Output Variable Type. Position):

• Position: global position vector of translated local position

• Displacement: global displacement vector of center point

• Velocity: global velocity vector of center point

The item ObjectMassPoint has the following parameters:

Name	type	size	default value	description
type = 'MassPoint'			item typename for initialization	
name	String		"	objects"s unique name
physicsMass	UReal		0.	mass [SI:kg] of mass point
nodeNumber	Index		MAXINT	node number for mass point
visualization	VObjectMassPoint			parameters for visualization of item

The item VObjectMassPoint has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
graphicsData	BodyGraphicsData			Structure contains data for body visualiza-
				tion; data is defined in special list / dictio-
				nary structure

#### 5.3.2 ObjectMassPoint2D

A 2D mass point which is attached to a position-based 2D node. Equations of motion with the displacements  $[u_x \ u_y]^T$ , the mass m and the residual of all forces  $[R_x \ R_y]^T$  are given as

$$\begin{bmatrix} m \cdot \dot{u}_x \\ m \cdot \dot{u}_y \end{bmatrix} = \begin{bmatrix} R_x \\ R_y \end{bmatrix}. \tag{5.5}$$

Short name for Python: MassPoint2D

Output variables (chose type, e.g., OutputVariableType.Position):

• Position: global position vector of translated local position

• Displacement: global displacement vector of center point

• Velocity: global velocity vector of center point

The item ObjectMassPoint2D has the following parameters:

Name	type	size	default value	description
type = 'MassPoint2D'			item typename for initialization	
name	String		"	objects"s unique name
physicsMass	UReal		0.	mass [SI:kg] of mass point
nodeNumber	Index		MAXINT	node number for mass point
visualization	VObjectMassPoint2l	D		parameters for visualization of item

The item VObjectMassPoint2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
graphicsData	BodyGraphicsData			Structure contains data for body visualiza-
				tion; data is defined in special list / dictio-
				nary structure

#### 5.3.3 ObjectRigidBody

A 3D rigid body which is attached to a 3D rigid body node. Equations of motion with the displacements  $[u_x \ u_y \ u_z]^T$  of the center of mass and the rotation parameters (Euler parameters) **q**, the mass m, inertia  $\mathbf{J} = [J_{xx}, J_{xy}, J_{xz}; J_{yx}, J_{yy}, J_{yz}; J_{zx}, J_{zy}, J_{zz}]$  and the residual of all forces and moments  $[R_x \ R_y \ R_z \ R_{q0} \ R_{q1} \ R_{q2} \ R_{q3}]^T$  are given as ...

Short name for Python: RigidBody

Output variables (chose type, e.g., OutputVariableType.Position):

- Position: global position vector of rotated and translated local position
- Displacement: global displacement vector of local position
- Velocity: global velocity vector of local position
- Angular Velocity: angular velocity of body
- RotationMatrix: rotation matrix in vector form (stored in row-major order)

The item ObjectRigidBody has the following parameters:

Name	type	size defau	tion

type = 'RigidBody'			item typename for initialization
name	String	"	objects"s unique name
physicsMass	UReal	0.	mass [SI:kg] of mass point
physicsInertia	Vector6D	[0.,0.,0., 0.,0.,0.]	inertia components [SI:kgm <sup>2</sup> ]:
			$[J_{xx}, J_{yy}, J_{zz}, J_{yz}, J_{xz}, J_{xy}]$ of rigid body w.r.t.
			center of mass
nodeNumber	Index	MAXINT	node number for rigid body node
visualization	VObjectRigidBody		parameters for visualization of item

The item VObjectRigidBody has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
graphicsData	BodyGraphicsData			Structure contains data for body visualiza-
				tion; data is defined in special list / dictio-
				nary structure

#### 5.3.4 ObjectRigidBody2D

A 2D rigid body which is attached to a rigid body 2D node. Equations of motion with the displacements  $[u_x \ u_y]^T$  of the center of mass and the rotation  $\varphi$  (positive rotation around z-axis), the mass m, inertia around z-axis J and the residual of all forces and moments  $[R_x \ R_y \ R_{\varphi}]^T$  are given as

$$\begin{bmatrix} m \cdot \ddot{u}_x \\ m \cdot \ddot{u}_y \\ J\varphi \end{bmatrix} = \begin{bmatrix} R_x \\ R_y \\ R_\varphi \end{bmatrix}. \tag{5.6}$$

Short name for Python: RigidBody2D

Output variables (chose type, e.g., OutputVariableType.Position):

- Position: global position vector of rotated and translated local position
- Displacement: global displacement vector of local position
- Velocity: global velocity vector of local position
- Rotation: scalar rotation angle of body
- Angular Velocity: angular velocity of body
- RotationMatrix: rotation matrix in vector form (stored in row-major order)

The item ObjectRigidBody2D has the following parameters:

Name	type	size	default value	description
type = 'RigidBody2D'				item typename for initialization

name	String	"	objects"s unique name
physicsMass	UReal	0.	mass [SI:kg] of mass point
physicsInertia	UReal	0.	inertia [SI:kgm²] of rigid body w.r.t. center
			of mass
nodeNumber	Index	MAXINT	node number for 2D rigid body node
visualization	VObjectRigidBody2D		parameters for visualization of item

The item VObjectRigidBody2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
graphicsData	BodyGraphicsData			Structure contains data for body visualiza-
				tion; data is defined in special list / dictio-
				nary structure

#### 5.3.5 ObjectANCFCable2D

A 2D cable finite element using 2 nodes of type NodePoint2DSlope1; the element has 8 coordinates and uses cubic polynomials for position interpolation; the Bernoulli-Euler beam is capable of large deformation as it employs the material measure of curvature for the bending.

Short name for Python: Cable2D

Output variables (chose type, e.g., OutputVariableType.Position):

- Position: global position vector of local axis (1) and cross section (2) position
- Displacement: global displacement vector of local axis (1) and cross section (2) position
- Velocity: global velocity vector of local axis (1) and cross section (2) position
- **Director1**: (axial) slope vector of local axis position
- Strain: axial strain (scalar)
- Curvature: axial strain (scalar)
- Force: (local) section normal force (scalar)
- Torque: (local) bending moment (scalar)

The item ObjectANCFCable2D has the following parameters:

Name	type	size	default value	description
type = 'ANCFCable2D'				item typename for initialization
name	String		"	objects"s unique name
physicsLength	UReal		0.	reference length $L$ [SI:m] of beam; such that
				the total volume (e.g. for volume load)
				gives $\rho AL$

physicsMassPerLength	UReal	0.	mass ρA [SI:kg/m²] of beam
physicsBendingStiffness	UReal	0.	bending stiffness EI [SI:Nm <sup>2</sup> ] of beam; the
			bending moment is $m = EI(\kappa - \kappa_0)$ , in which
			$\kappa$ is the material measure of curvature
physicsAxialStiffness	UReal	0.	axial stiffness EA [SI:N] of beam; the axial
			force is $f_{ax} = EA(\varepsilon - \varepsilon_0)$ , in which $\varepsilon =  \mathbf{r}'  - 1$
			is the axial strain
physicsBendingDamping	UReal	0.	bending damping $d_{EI}$ [SI:Nm <sup>2</sup> /s] of beam;
			the additional virtual work due to damping
			is $\delta W_{\dot{\kappa}} = \int_0^L \dot{\kappa} \delta \kappa dx$
physicsAxialDamping	UReal	0.	axial stiffness $d_{EA}$ [SI:N/s] of beam; the ad-
			ditional virtual work due to damping is
			$\delta W_{\dot{\varepsilon}} = \int_0^L \dot{\varepsilon} \delta \varepsilon dx$
physicsReferenceAxialStrain	UReal	0.	reference axial strain of beam (pre-
			deformation) $\varepsilon_0$ [SI:1] of beam; without ex-
			ternal loading the beam will statically keep
			the reference axial strain value
physicsReferenceCurvature	UReal	0.	reference curvature of beam (pre-
			deformation) $\kappa_0$ [SI:1/m] of beam; without
			external loading the beam will statically
			keep the reference curvature value
nodeNumbers	Index2	[MAXINT, MAX-	two node numbers ANCF cable element
		INT]	
useReducedOrderIntegration	Bool	False	false: use Gauss order 9 integration for vir-
			tual work of axial forces, order 5 for virtual
			work of bending moments; true: use Gauss
			order 7 integration for virtual work of axial
			forces, order 3 for virtual work of bending
			moments
visualization	VObjectANCFCable2D	)	parameters for visualization of item

The item VObjectANCFCable2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawHeight	float		0.	if beam is drawn with rectangular shape,
				this is the drawing height
color	Float4		[-1.,-1.,-1.]	RGBA color of the object; if R==-1, use de-
				fault color

#### 5.3.6 ObjectALEANCFCable2D

A 2D cable finite element using 2 nodes of type NodePoint2DSlope1 and a axially moving coordinate of type NodeGenericODE2; the element has 8+1 coordinates and uses cubic polynomials for position interpolation; the element in addition to ANCFCable2D adds an Eulerian axial velocity by the GenericODE2 coordinate

Short name for Python: ALECable2D

**Output variables** (chose type, e.g., OutputVariableType.Position):

• Position: global position vector of local axis (1) and cross section (2) position

• Displacement: global displacement vector of local axis (1) and cross section (2) position

• Velocity: global velocity vector of local axis (1) and cross section (2) position

• Director1: (axial) slope vector of local axis position

• **Strain**: axial strain (scalar)

• Curvature: axial strain (scalar)

• Force: (local) section normal force (scalar)

• Torque: (local) bending moment (scalar)

The item ObjectALEANCFCable2D has the following parameters:

Name	type	size	default value	description
type = 'ALEANCFCable2D'	'	<u>'</u>		item typename for initialization
name	String		"	objects"s unique name
physicsLength	UReal		0.	reference length L [SI:m] of beam; such that
				the total volume (e.g. for volume load)
				gives $\rho AL$
physicsMassPerLength	UReal		0.	mass $\rho A$ [SI:kg/m <sup>2</sup> ] of beam
physicsMovingMassFactor	UReal		1.	this factor denotes the amount of $\rho A$
				which is moving; physicsMovingMassFac-
				tor=1 means, that all mass is moving;
				physicsMovingMassFactor=0 means, that
				no mass is moving; factor can be used to
				simulate e.g. pipe conveying fluid, in which
				$\rho A$ is the mass of the pipe+fluid, while
				<i>physicsMovingMassFactor</i> $\cdot \rho A$ is the mass
				per unit length of the fluid
physicsBendingStiffness	UReal		0.	bending stiffness EI [SI:Nm <sup>2</sup> ] of beam; the
				bending moment is $m = EI(\kappa - \kappa_0)$ , in which
				$\kappa$ is the material measure of curvature
physicsAxialStiffness	UReal		0.	axial stiffness EA [SI:N] of beam; the axial
				force is $f_{ax} = EA(\varepsilon - \varepsilon_0)$ , in which $\varepsilon =  \mathbf{r}'  - 1$
				is the axial strain
physicsBendingDamping	UReal		0.	bending damping $d_{EI}$ [SI:Nm <sup>2</sup> /s] of beam;
				the additional virtual work due to damping
				is $\delta W_{\dot{\kappa}} = \int_0^L \dot{\kappa} \delta \kappa dx$
physicsAxialDamping	UReal		0.	axial stiffness $d_{EA}$ [SI:N/s] of beam; the ad-
				ditional virtual work due to damping is
				$\delta W_{\dot{\varepsilon}} = \int_0^L \dot{\varepsilon} \delta \varepsilon dx$
physicsReferenceAxialStrain	UReal		0.	reference axial strain of beam (pre-
				deformation) $\varepsilon_0$ [SI:1] of beam; without ex-
				ternal loading the beam will statically keep
				the reference axial strain value

physicsReferenceCurvature	UReal	0.	reference curvature of beam (pre-
			deformation) $\kappa_0$ [SI:1/m] of beam; without
			external loading the beam will statically
			keep the reference curvature value
physicsUseCouplingTerms	bool	True	true: correct case, where all coupling terms
			due to moving mass are respected; false:
			only include constant mass for ALE node
			coordinate, but deactivate other coupling
			terms (behaves like ANCFCable2D then)
nodeNumbers	Index3	[MAXINT, MAX-	two node numbers ANCF cable element,
		INT, MAXINT]	third node=ALE GenericODE2 node
useReducedOrderIntegration	Bool	False	false: use Gauss order 9 integration for vir-
			tual work of axial forces, order 5 for virtual
			work of bending moments; true: use Gauss
			order 7 integration for virtual work of axial
			forces, order 3 for virtual work of bending
			moments
visualization	VObjectALEANCF	Cable2D	parameters for visualization of item

The item VObjectALEANCFCable2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawHeight	float		0.	if beam is drawn with rectangular shape,
				this is the drawing height
color	Float4		[-1.,-1.,-1.]	RGBA color of the object; if R==-1, use de-
				fault color

#### 5.3.7 ObjectGround

A ground object behaving like a rigid body, but having no degrees of freedom; used to attach body-connectors without an action.

**Output variables** (chose type, e.g., OutputVariableType.Position):

- Position: global position vector of rotated and translated local position
- Displacement: global displacement vector of local position
- Velocity: global velocity vector of local position
- Angular Velocity: angular velocity of body
- RotationMatrix: rotation matrix in vector form (stored in row-major order)

The item ObjectGround has the following parameters:

Name	type	size	default value	description
type = 'Ground'				item typename for initialization
name	String		"	objects"s unique name
referencePosition	Vector3D	3	[0.,0.,0.]	reference position for ground object; local
				position is added on top of reference posi-
				tion for a ground object
visualization	VObjectGround			parameters for visualization of item

The item VObjectGround has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
color	Float4		[-1.,-1.,-1.]	RGB node color; if R==-1, use default color
graphicsData	BodyGraphicsData			Structure contains data for body visualiza-
				tion; data is defined in special list / dictio-
				nary structure

#### 5.3.8 ObjectConnectorSpringDamper

An simple spring-damper element with additional force; connects to position-based markers.

**Short name** for Python: **SpringDamper Requested marker type** = Marker::Position

The item ObjectConnectorSpringDamper has the following parameters:

Name	type	size	default value	description
type = 'ConnectorSpringD	Damper'	item typename for initialization		
name	String		"	connector"s unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	list of markers used in connector
			INT]	
referenceLength	UReal		0.	reference length [SI:m] of spring
stiffness	UReal		0.	stiffness [SI:N/m] of spring; acts against
				(length-initialLength)
damping	UReal		0.	damping [SI:N/(m s)] of damper; acts
				against d/dt(length)
force	UReal		0.	added constant force [SI:N] of spring; scalar
				force; f=1 is equivalent to reducing initial-
				Length by 1/stiffness; $f > 0$ : tension; $f < 0$ :
				compression
activeConnector	bool		True	flag, which determines, if the connector
				is active; used to deactivate (temorarily) a
				connector or constraint

springForceUserFunction	PyFunctionScalar5		0	A python function which defines the spring
				force with parameters (deltaL, deltaL_t,
				Real stiffness, Real damping, Real spring-
				Force); the parameters are provided to the
				function using the current values of the
				SpringDamper object; The python function
				will only be evaluated, if activeConnector is
				true, otherwise the SpringDamper is inac-
				tive; Example for python function: def f(u,
				$v, k, d, F0$ ): return $k^*u + d^*v + F0$
visualization	VObjectConnectorS	pringD	amper	parameters for visualization of item

The item VObjectConnectorSpringDamper has the following parameters:

Name	type	size	default value	description
show	Bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = diameter of spring; size == -
				1.f means that default connector size is used
color	Float4		[-1.,-1.,-1.]	RGB connector color; if R==-1, use default
				color

#### $5.3.9 \quad Object Connector Cartesian Spring Damper$

An 3D spring-damper element acting accordingly in three directions (x,y,z); connects to position-based markers; represents a penalty-based spherical joint; the resulting force in the spring-damper reads (m0 = marker[0]) and m1 = marker[1]):

$$force_x = (m1.position_x - m0.position_x - offset_x) \cdot stiffness_x + (m1.velocity_x - m0.velocity_x) \cdot damping_x, etc.$$
 (5.7)

Short name for Python: CartesianSpringDamper

**Requested marker type** = Marker::Position

The item ObjectConnectorCartesianSpringDamper has the following parameters:

Name	type	size	default value	description
type = 'ConnectorCartesianSpringDamper'				item typename for initialization
name	String		"	connector"s unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	list of markers used in connector
			INT]	
stiffness	Vector3D		[0.,0.,0.]	stiffness [SI:N/m] of springs; act against rel-
				ative displacements in x, y, and z-direction
damping	Vector3D		[0.,0.,0.]	damping [SI:N/(m s)] of dampers; act
				against relative velocities in x, y, and z-
				direction

offset	Vector3D		[0.,0.,0.]	offset between two springs
activeConnector	bool		True	flag, which determines, if the connector
				is active; used to deactivate (temorarily) a
				connector or constraint
visualization	VObjectConnectorO	Cartesi	anSpringDamper	parameters for visualization of item

The item VObjectConnectorCartesianSpringDamper has the following parameters:

Name	type	size	default value	description
show	Bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = diameter of spring; size == -
				1.f means that default connector size is used
color	Float4		[-1.,-1.,-1.]	RGB connector color; if R==-1, use default
				color

### 5.3.10 ObjectConnectorCoordinateSpringDamper

A 1D (scalar) spring-damper element acting on single ODE2 coordinates; connects to coordinate-based markers; NOTE that the coordinate markers only measure the coordinate (=displacement), but the reference position is not included as compared to position-based markers!; the spring-damper can also act on rotational coordinates; the resulting force in the spring-damper reads (m0 = marker[0] and m1 = marker[1]):

$$f = (m1.coordinate - m0.coordinate - offset) \cdot stiffness + (m1.coordinate_t - m0.coordinate_t) \cdot damping$$
 (5.8)

If dry (Coulomb) friction is non-zero, an additional term

$$sign(m1.coordinate_t - m0.coordinate_t) \cdot dryFriction$$
 (5.9)

is added to the force f.

**Short name** for Python: **CoordinateSpringDamper Requested marker type** = Marker::Coordinate

The item ObjectConnectorCoordinateSpringDamper has the following parameters:

Name	type	size	default value	description
type = 'ConnectorCoordin	ateSpringDamper'			item typename for initialization
name	String		"	connector"s unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	list of markers used in connector
			INT]	
stiffness	Real		0.	stiffness [SI:N/m] of spring; acts against rel-
				ative value of coordinates
damping	Real		0.	damping [SI:N/(m s)] of damper; acts
				against relative velocity of coordinates
offset	Real		0.	offset between two coordinates (reference
				length of springs), see equation

dryFriction	Real	0.	dry friction coefficient against relative ve-
			locity
dryFrictionProportionalZone	Real	0.	limit velocity [m/s] up to which the friction
			is proportional to velocity (for regulariza-
			tion / avoid numerical oscillations)
activeConnector	bool	True	flag, which determines, if the connector
			is active; used to deactivate (temorarily) a
			connector or constraint
springForceUserFunction	PyFunctionScalar7	0	A python function which defines the spring
			force with parameters (deltaL, deltaL $_t$ , Real
			stiffness, Real damping, Real offset, Real
			dryFriction, Real dryFrictionProportional-
			Zone); the parameters are provided to
			the function using the current values of
			the SpringDamper object; note that $u =$
			(m1.coordinate – m0.coordinate), not includ-
			ing the offset; The python function will only
			be evaluated, if activeConnector is true, oth-
			erwise the SpringDamper is inactive; Ex-
			ample for python function: def f(u, v, k, d,
			offset, mu, muProp): return $k*u + d*v + F0$
visualization	VObjectConnectorCo	ordinateSpringDamper	parameters for visualization of item

 $The\ item\ VObject Connector Coordinate Spring Damper\ has\ the\ following\ parameters:$ 

Name	type	size	default value	description
show	Bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = diameter of spring; size == -
				1.f means that default connector size is used
color	Float4		[-1.,-1.,-1.]	RGB connector color; if R==-1, use default
				color

## 5.3.11 ObjectConnectorDistance

Connector which enforces constant or prescribed distance between two bodies/nodes.

**Short name** for Python: **DistanceConstraint Requested marker type** = Marker::Position

The item ObjectConnectorDistance has the following parameters:

Name	type	size	default value	description
type = 'ConnectorDistance'				item typename for initialization
name	String		"	constraints"s unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	list of markers used in connector
			INT]	

distance	UReal		0.	prescribed distance [SI:m] of the used mark-
				ers
activeConnector	bool		True	flag, which determines, if the connector
				is active; used to deactivate (temorarily) a
				connector or constraint
visualization	VObjectConnectorI	Distano	e	parameters for visualization of item

The item VObjectConnectorDistance has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = link size; size == -1.f means
				that default connector size is used
color	Float4		[-1.,-1.,-1.]	RGB connector color; if R==-1, use default
				color

### 5.3.12 ObjectConnectorCoordinate

A coordinate constraint which constrains two (scalar) coordinates of Marker[Node|Body]Coordinates attached to nodes or bodies. The constraint must fulfill the condition:

$$factorValue1 * marker[1].value - marker[0].value - offset = 0$$
 (5.10)

**Short name** for Python: **CoordinateConstraint Requested marker type** = Marker::Coordinate

The item ObjectConnectorCoordinate has the following parameters:

Name	type	size	default value	description
type = 'ConnectorCoordinate	e'	1		item typename for initialization
name	String		"	constraints"s unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	list of markers used in connector
			INT]	
offset	UReal		0.	An offset between the two values
factorValue1	UReal		1.	An additional factor multiplied with value1
				used in algebraic equation
velocityLevel	bool		False	If true: connector constrains velocities (only
				works for ODE2 coordinates!); offset is used
				between velocities
activeConnector	bool		True	flag, which determines, if the connector
				is active; used to deactivate (temorarily) a
				connector or constraint
visualization	VObjectConnecto	orCoordi	nate	parameters for visualization of item

The item VObjectConnectorCoordinate has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = link size; size == -1.f means
				that default connector size is used
color	Float4		[-1.,-1.,-1.]	RGB connector color; if R==-1, use default
				color

### 5.3.13 ObjectContactCoordinate

A penalty-based contact condition for one coordinate; the contact gap g is defined as g = marker.value[1] - marker.value[0] - offset; the contact force  $f_c$  is zero for gap > 0 and otherwise computed from  $f_c = g * contactStiffness+\dot{g}*contactDamping$ ; during Newton iterations, the contact force is actived only, if dataCoordinate[0] <= 0; dataCoordinate is set equal to gap in nonlinear iterations, but not modified in Newton iterations.

**Requested marker type** = Marker::Coordinate

The item ObjectContactCoordinate has the following parameters:

Name	type	size	default value	description
type = 'ContactCoordinate'	item typename for initialization			
name	String		"	connector"s unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	markers define contact gap
			INT]	
nodeNumber	Index		MAXINT	node number of a NodeGenericData for 1
				dataCoordinate (used for active set strategy
				==> holds the gap of the last discontinuous
				iteration)
contactStiffness	UReal		0.	contact (penalty) stiffness [SI:N/m]; acts
				only upon penetration
contactDamping	UReal		0.	contact damping [SI:N/(m s)]; acts only
				upon penetration
offset	UReal		0.	offset [SI:m] of contact
activeConnector	bool		True	flag, which determines, if the connector
				is active; used to deactivate (temorarily) a
				connector or constraint
visualization	VObjectContactCo	ordinat	e	parameters for visualization of item

The item VObjectContactCoordinate has the following parameters:

Name	type	size	default value	description
show	Bool		True	set true, if item is shown in visualization
				and false if it is not shown

drawSize	float		-1.	drawing size = diameter of spring; size == -	
		1.f means that default connector size is u		1.f means that default connector size is used	
color	Float4		[-1.,-1.,-1.]	RGB connector color; if R==-1, use default	
				color	

### 5.3.14 ObjectContactCircleCable2D

A very specialized penalty-based contact condition between a 2D circle (=marker0, any Position-marker) on a body and an ANCFCable2DShape (=marker1, Marker: BodyCable2DShape), in xy-plane; a node NodeGenericData is required with the number of cordinates according to the number of contact segments; the contact gap g is integrated (piecewise linear) along the cable and circle; the contact force  $f_c$  is zero for gap > 0 and otherwise computed from  $f_c = g * contactStiffness + <math>\dot{g} * contactDamping$ ; during Newton iterations, the contact force is actived only, if dataCoordinate[0] <= 0; dataCoordinate is set equal to gap in nonlinear iterations, but not modified in Newton iterations.

### **Requested marker type** = Marker::None

The item ObjectContactCircleCable2D has the following parameters:

Name	type	size	default value	description
type = 'ContactCircleCable2D'				item typename for initialization
name	String		"	connector"s unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	markers define contact gap
			INT]	
nodeNumber	Index		MAXINT	node number of a NodeGenericData for
				nSegments dataCoordinates (used for ac-
				tive set strategy ==> hold the gap of the
				last discontinuous iteration and the friction
				state)
numberOfContactSegments	Index		3	number of linear contact segments to deter-
				mine contact; each segment is a line and is
				associated to a data (history) variable; must
				be same as in according marker
contactStiffness	UReal		0.	contact (penalty) stiffness [SI:N/m/(contact
				segment)]; the stiffness is per length of
				the beam axis; specific contact forces (per
				length) $f_N$ act in contact normal direction
				only upon penetration
contactDamping	UReal		0.	contact damping [SI:N/(m s)/(contact seg-
				ment)]; the damping is per length of the
				beam axis; acts in contact normal direction
				only upon penetration
circleRadius	UReal		0.	radius [SI:m] of contact circle
offset	UReal		0.	offset [SI:m] of contact, e.g. to include thick-
				ness of cable element
activeConnector	bool		True	flag, which determines, if the connector
				is active; used to deactivate (temorarily) a
				connector or constraint
visualization	VObjectContactC	ircleCab	e2D	parameters for visualization of item

The item VObjectContactCircleCable2D has the following parameters:

Name	type	size	default value	description
show	Bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = diameter of spring; size == -
				1.f means that default connector size is used
color	Float4		[-1.,-1.,-1.]	RGB connector color; if R==-1, use default
				color

### 5.3.15 ObjectContactFrictionCircleCable2D

A very specialized penalty-based contact/friction condition between a 2D circle (=marker0, any Position-marker) on a body and an ANCFCable2DShape (=marker1, Marker: BodyCable2DShape), in xy-plane; a node NodeGenericData is required with  $3\times$ (number of contact segments) – containing per segment: [contact gap, stick/slip (stick=1), last friction position]; the contact gap g is integrated (piecewise linear) along the cable and circle; the contact force  $f_c$  is zero for gap > 0 and otherwise computed from  $f_c = g * contactStiffness + g * contactDamping$ ; during Newton iterations, the contact force is actived only, if dataCoordinate[0] <= 0; dataCoordinate is set equal to gap in nonlinear iterations, but not modified in Newton iterations.

### **Requested marker type** = Marker::None

The item ObjectContactFrictionCircleCable2D has the following parameters:

Name	type	size	default value	description	
type = 'ContactFrictionCircleCa	type = 'ContactFrictionCircleCable2D'				
name	String		"	connector"s unique name	
markerNumbers	ArrayIndex		[ MAXINT, MAX- INT ]	markers define contact gap	
nodeNumber	Index		MAXINT	node number of a NodeGenericData with 3 × nSegments dataCoordinates (used for active set strategy ==> hold the gap of the last discontinuous iteration and the friction state)	
numberOfContactSegments	Index		3	number of linear contact segments to determine contact; each segment is a line and is associated to a data (history) variable; must be same as in according marker	
contactStiffness	UReal		0.	contact (penalty) stiffness [SI:N/m/(contact segment)]; the stiffness is per length of the beam axis; specific contact forces (per length) $f_N$ act in contact normal direction only upon penetration	
contactDamping	UReal		0.	contact damping [SI:N/(m s)/(contact segment)]; the damping is per length of the beam axis; acts in contact normal direction only upon penetration	

frictionVelocityPenalty	UReal	0.	velocity dependent penalty coefficient for
			friction [SI:N/(m s)/(contact segment)]; the
			coefficient causes tangential (contact) forces
			against relative tangential velocities in the
			contact area
frictionStiffness	UReal	0.	CURRENTLY NOT IMPLEMENTED: dis-
			placement dependent penalty/stiffness co-
			efficient for friction [SI:N/m/(contact seg-
			ment)]; the coefficient causes tangential
			(contact) forces against relative tangential
			displacements in the contact area
frictionCoefficient	UReal	0.	friction coefficient $\mu$ [SI: 1]; tangential spe-
			cific friction forces (per length) $f_T$ must ful-
			fill the condition $f_T \leq \mu f_N$
circleRadius	UReal	0.	radius [SI:m] of contact circle
offset	UReal	0.	offset [SI:m] of contact, e.g. to include thick-
			ness of cable element
activeConnector	bool	True	flag, which determines, if the connector
			is active; used to deactivate (temorarily) a
			connector or constraint
visualization	VObjectContactFrict	tionCircleCable2D	parameters for visualization of item

The item VObjectContactFrictionCircleCable2D has the following parameters:

Name	type	size	default value	description
show	Bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = diameter of spring; size == -
				1.f means that default connector size is used
color	Float4		[-1.,-1.,-1.]	RGB connector color; if R==-1, use default
				color

### 5.3.16 ObjectJointSliding2D

A specialized sliding joint (without rotation) in 2D between a Cable2D (marker1) and a position-based marker (marker0); the data coordinates provide [0] the current index in slidingMarkerNumbers, and [1] the local position in the cable element at the beginning of the timestep; the algebraic variables are

$$\mathbf{q}_{AE} = \begin{bmatrix} \lambda_x & \lambda_y & s \end{bmatrix}^T \tag{5.11}$$

in which  $\lambda_x$  and  $\lambda_y$  are the Lagrange multipliers for the position of the sliding joint and s is the (algebraic) sliding coordinate relative to the value at the beginning at the solution step; the data coordinates are

$$\mathbf{q}_{Data} = [i_{marker} \ s_0]^T \tag{5.12}$$

in which  $i_{marker}$  is the current local index to the slidingMarkerNumber list and  $s_0$  is the sliding coordinate (which is the total sliding length along all cable elements in the cableMarkerNumber list) at the beginning of

the solution step.

Short name for Python: SlidingJoint2D

Output variables (chose type, e.g., OutputVariableType.Position):

- Position: position vector of joint given by marker0
- Velocity: velocity vector of joint given by marker0
- **SlidingCoordinate**: global sliding coordinate along all elements; the maximum sliding coordinate is equivalent to the reference lengths of all sliding elements
- Force: joint force vector (3D)

### **Requested marker type** = Marker::None

The item ObjectJointSliding2D has the following parameters:

Name	type	size	default value	description
type = 'JointSliding2D'				item typename for initialization
name	String		"	constraints"s unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	marker0: position-marker of mass point or
			INT]	rigid body; marker1: updated marker to
				Cable2D element, where the sliding joint
				currently is attached to; must be initial-
				ized with an appropriate (global) marker
				number according to the starting position
				of the sliding object; this marker changes
				with time (PostNewtonStep)
slidingMarkerNumbers	ArrayIndex		[]	these markers are used to update marker1,
				if the sliding position exceeds the current
				cable"s range; the markers must be sorted
				such that marker(i) at x=cable.length is
				equal to marker(i+1) at x=0
slidingMarkerOffsets	Vector			this list contains the offsets of ev-
				ery sliding object (given by sliding-
				MarkerNumbers) w.r.t. to the ini-
				tial position (0): marker0: offset=0,
				marker1: offset=Length(cable0), marker2:
				offset=Length(cable1)+Length(cable1),
nodeNumber	Index		MAXINT	node number of a NodeGenericData for
				1 dataCoordinate showing the according
				marker number which is currently active
				and the initial (global) sliding position
activeConnector	bool		True	flag, which determines, if the connector
				is active; used to deactivate (temorarily) a
				connector or constraint
visualization	VObjectJointSliding2	2D		parameters for visualization of item

The item VObjectJointSliding2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = radius of revolute joint; size
				== -1.f means that default connector size is
				used
color	Float4		[-1.,-1.,-1.]	RGB connector color; if R==-1, use default
				color

### 5.3.17 ObjectJointALEMoving2D

A specialized axially moving joint (without rotation) in 2D between a ALE Cable2D (marker1) and a position-based marker (marker0); the data coordinate [0] provides the current index in slidingMarkerNumbers, and the ODE2 coordinate [0] provides the (given) moving coordinate in the cable element; the algebraic variables are

$$\mathbf{q}_{AE} = [\lambda_x \ \lambda_y]^T \tag{5.13}$$

, in which  $\lambda_x$  and  $\lambda_y$  are the Lagrange multipliers for the position constraint of the moving joint; the data coordinate is

$$\mathbf{q}_{Data} = [i_{marker}]^T \tag{5.14}$$

in which  $i_{marker}$  is the current local index to the slidingMarkerNumber list.

Short name for Python: ALEMovingJoint2D

Output variables (chose type, e.g., OutputVariableType.Position):

- Position: position vector of joint given by marker0
- Velocity: velocity vector of joint given by marker0
- SlidingCoordinate: global sliding coordinate along all elements + slidingOffset
- Coordinates: provides two values: [0] = current sliding marker index, [1] = ALE sliding coordinate
- Coordinates\_t: provides one value: [0] ALE sliding velocity
- Force: joint force vector (3D)

**Requested marker type** = Marker::None

The item ObjectJointALEMoving2D has the following parameters:

Name	type	size	default value	description
type = 'JointALEMoving2D'				item typename for initialization
name	String		"	constraints"s unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	marker0: position-marker of mass point or
			INT]	rigid body; marker1: updated marker to
				Cable2D element, where the sliding joint
				currently is attached to; must be initial-
				ized with an appropriate (global) marker
				number according to the starting position
				of the sliding object; this marker changes
				with time (PostNewtonStep)

slidingMarkerNumbers	ArrayIndex	[]	these markers are used to update marker1,
			if the sliding position exceeds the current
			cable"s range; the markers must be sorted
			such that marker(i) at x=cable.length is
			equal to marker(i+1) at x=0
slidingMarkerOffsets	Vector	[]	this list contains the offsets of ev-
			ery sliding object (given by sliding-
			MarkerNumbers) w.r.t. to the ini-
			tial position (0): marker0: offset=0,
			marker1: offset=Length(cable0), marker2:
			offset=Length(cable0)+Length(cable1),
slidingOffset	Real	0.	offset [SI:m] used set the sliding position
			relative to the chosen Eulerian (NodeGener-
			icODE2) coordinate; the following rela-
			tion is used: slidingPosition = posALE +
			slidingOffset
nodeNumbers	ArrayIndex	[ MAXINT, MAX-	node numbers of: [0] NodeGenericData for
		INT ]	1 dataCoordinate showing the according
			marker number which is currently active;
			[1] of the GenericNodeODE2 of the ALE
			sliding coordinate
activeConnector	bool	True	flag, which determines, if the connector
			is active; used to deactivate (temorarily) a
			connector or constraint
visualization	VObjectJointALEMo	oving2D	parameters for visualization of item

The item VObjectJointALEMoving2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = radius of revolute joint; size
				== -1.f means that default connector size is
				used
color	Float4		[-1.,-1.,-1.]	RGB connector color; if R==-1, use default
				color

## 5.3.18 ObjectJointRevolute2D

A revolute joint in 2D; constrains the absolute 2D position of two points given by PointMarkers or RigidMarkers

**Short name** for Python: **RevoluteJoint2D Requested marker type** = Marker::Position

The item ObjectJointRevolute2D has the following parameters:

Name type	size default value descrip	otion
-----------	----------------------------	-------

type = 'JointRevolute2D'				item typename for initialization
name	String		"	constraints"s unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	list of markers used in connector
			INT]	
activeConnector	bool		True	flag, which determines, if the connector
				is active; used to deactivate (temorarily) a
				connector or constraint
visualization	VObjectJointRevolu	ıte2D		parameters for visualization of item

The item VObjectJointRevolute2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = radius of revolute joint; size
				== -1.f means that default connector size is
				used
color	Float4		[-1.,-1.,-1.]	RGB connector color; if R==-1, use default
				color

### 5.3.19 ObjectJointPrismatic2D

A prismatic joint in 2D; allows the relative motion of two bodies, using two RigidMarkers; the vector  $\mathbf{t}_0$  = axisMarker0 is given in local coordinates of the first marker's (body) frame and defines the prismatic axis; the vector  $\mathbf{n}_1$  = normalMarker1 is given in the second marker's (body) frame and is the normal vector to the prismatic axis; using the global position vector  $\mathbf{p}_0$  and rotation matrix  $\mathbf{A}_0$  of marker0 and the global position vector  $\mathbf{p}_1$  rotation matrix  $\mathbf{A}_1$  of marker1, the equations for the prismatic joint follow as

$$(\mathbf{p}_1 - \mathbf{p}_0)^T \cdot \mathbf{A}_1 \cdot \mathbf{n}_1 = 0 \tag{5.15}$$

$$(\mathbf{A}_0 \cdot \mathbf{t}_0)^T \cdot \mathbf{A}_1 \cdot \mathbf{n}_1 = 0 \tag{5.16}$$

The lagrange multipliers follow for these two equations  $[\lambda_0, \lambda_1]$ , in which  $\lambda_0$  is the transverse force and  $\lambda_1$  is the torque in the joint.

Short name for Python: PrismaticJoint2D

**Requested marker type** = (Marker::Type)(Marker::Position + Marker::Orientation)

The item ObjectJointPrismatic2D has the following parameters:

Name	type	size	default value	description
type = 'JointPrismatic2D'				item typename for initialization
name	String		"	constraints"s unique name
markerNumbers	ArrayIndex		[ MAXINT, MAX-	list of markers used in connector
			INT]	
axisMarker0	Vector3D		[1.,0.,0.]	direction of prismatic axis, given as a 3D
				vector in Marker0 frame

normalMarker1	Vector3D	[0.,1.,0.]	direction of normal to prismatic axis, given
			as a 3D vector in Marker1 frame
constrainRotation	bool	True	flag, which determines, if the connector also
			constrains the relative rotation of the two
			objects; if set to false, the constraint will
			keep an algebraic equation set equal zero
activeConnector	bool	True	flag, which determines, if the connector
			is active; used to deactivate (temorarily) a
			connector or constraint
visualization	VObjectJointPrisma	tic2D	parameters for visualization of item

The item VObjectJointPrismatic2D has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown
drawSize	float		-1.	drawing size = radius of revolute joint; size
				== -1.f means that default connector size is
				used
color	Float4		[-1.,-1.,-1.]	RGB connector color; if R==-1, use default
				color

## 5.4 Markers

## 5.4.1 MarkerBodyMass

A marker attached to the body mass; use this marker to apply a body-load (e.g. gravitational force). The item MarkerBodyMass has the following parameters:

Name	type	size	default value	description
type = 'BodyMass'				item typename for initialization
name	String		"	marker"s unique name
bodyNumber	Index		MAXINT	body number to which marker is attached
				to
visualization	VMarkerBodyMass			parameters for visualization of item

The item VMarkerBodyMass has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

## 5.4.2 MarkerBodyPosition

A position body-marker attached to local position (x,y,z) of the body. The item MarkerBodyPosition has the following parameters:

Name	type	size	default value	description
type = 'BodyPosition'				item typename for initialization
name	String		"	marker"s unique name
bodyNumber	Index		MAXINT	body number to which marker is attached
				to
localPosition	Vector3D	3	[0.,0.,0.]	local body position of marker; e.g. local
				(body-fixed) position where force is applied
				to
bodyFixed	Bool		False	if bodyFixed is true, the force/sensor is
				using body-fixed coordinates (orientation);
				otherwise, it uses global coordinates
visualization	VMarkerBodyPo	osition		parameters for visualization of item

The item VMarkerBodyPosition has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

## 5.4.3 MarkerBodyRigid

A rigid-body (position+orientation) body-marker attached to local position (x,y,z) of the body. The item MarkerBodyRigid has the following parameters:

Name	type	size	default value	description
type = 'BodyRigid'	<u> </u>			item typename for initialization
name	String		"	marker"s unique name
bodyNumber	Index		MAXINT	body number to which marker is attached
				to
localPosition	Vector3D	3	[0.,0.,0.]	local body position of marker; e.g. local
				(body-fixed) position where force is applied
				to
bodyFixed	Bool		False	if bodyFixed is true, the force/sensor is
				using body-fixed coordinates (orientation);
				otherwise, it uses global coordinates
visualization	VMarkerBodyRigio	1		parameters for visualization of item

The item VMarkerBodyRigid has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

### 5.4.4 MarkerNodePosition

A node-Marker attached to a position-based node.

The item MarkerNodePosition has the following parameters:

Name	type	size	default value	description
type = 'NodePosition'				item typename for initialization
name	String		"	marker"s unique name
nodeNumber	Index		MAXINT	node number to which marker is attached
				to
visualization	VMarkerNodePosit	ion		parameters for visualization of item

The item VMarkerNodePosition has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

## 5.4.5 MarkerNodeRigid

A rigid-body (position+orientation) node-marker attached to a rigid-body node. The item MarkerNodeRigid has the following parameters:

Name	type	size	default value	description
type = 'NodeRigid'				item typename for initialization
name	String		"	marker"s unique name
nodeNumber	Index		MAXINT	node number to which marker is attached
				to
visualization	VMarkerNodeRigio	1		parameters for visualization of item

The item VMarkerNodeRigid has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

### 5.4.6 MarkerNodeCoordinate

A node-Marker attached to a ODE2 coordinate of a node; for other coordinates (ODE1,...) other markers need to be defined.

The item MarkerNodeCoordinate has the following parameters:

Name	type	size	default value	description
type = 'NodeCoordinate'				item typename for initialization
name	String		"	marker"s unique name
nodeNumber	Index		MAXINT	node number to which marker is attached
				to
coordinate	Index		MAXINT	coordinate of node to which marker is at-
				tached to
visualization	VMarkerNodeCoor	dinate		parameters for visualization of item

The item VMarkerNodeCoordinate has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

## 5.4.7 MarkerBodyCable2DShape

A special Marker attached to a 2D ANCF beam finite element with cubic interpolation and 8 coordinates. The item MarkerBodyCable2DShape has the following parameters:

Name	type	size	default value	description
type = 'BodyCable2DShape'				item typename for initialization
name	String		"	marker"s unique name
bodyNumber	Index		MAXINT	body number to which marker is attached
				to
numberOfSegments	Index		3	number of number of segments; each seg-
				ment is a line and is associated to a data
				(history) variable; must be same as in ac-
				cording contact element
visualization	VMarkerBodyCable	2DSh	ipe	parameters for visualization of item

The item VMarkerBodyCable2DShape has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

## 5.4.8 MarkerBodyCable2DCoordinates

A special Marker attached to the coordinates of a 2D ANCF beam finite element with cubic interpolation. The item MarkerBodyCable2DCoordinates has the following parameters:

Name	type	size	default value	description
type = 'BodyCable2DCoordinates'				item typename for initialization
name	String		"	marker"s unique name
bodyNumber	Index		MAXINT	body number to which marker is attached
				to
visualization	VMarkerBodyCable	2DCo	ordinates	parameters for visualization of item

The item VMarkerBodyCable2DCoordinates has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

### 5.5 Loads

### 5.5.1 LoadForceVector

Load with (3D) force vector; attached to position-based marker.

Short name for Python: Force

**Requested marker type** = Marker::Position

The item LoadForceVector has the following parameters:

Name	type	size	default value	description
type = 'ForceVector'	<u> </u>	item typename for initialization		
name	String		"	load"s unique name
markerNumber	Index		MAXINT	marker"s number to which load is applied
loadVector	Vector3D		[0.,0.,0.]	vector-valued load [SI:N]
loadVectorUserFunction	PyFunctionVector3	DScala	rVector3D	A python function which defines the time-
			0	dependent load with parameters (Real
				t, Vector3D load); the load represents
				the current value of the load; WARN-
				ING: this factor does not work in com-
				bination with static computation (load-
				Factor); Example for python function:
				def f(t, loadVector): return [loadVec-
				tor[0]*np.sin(t*10*2*3.1415),0,0]
visualization	VLoadForceVector			parameters for visualization of item

The item VLoadForceVector has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

## 5.5.2 LoadTorqueVector

Load with (3D) torque vector; attached to rigidbody-based marker.

Short name for Python: Torque

**Requested marker type** = Marker::Orientation

The item LoadTorqueVector has the following parameters:

Name	type	size	default value	description
type = 'TorqueVector'		•		item typename for initialization
name	String		"	load"s unique name
markerNumber	Index		MAXINT	marker"s number to which load is applied
loadVector	Vector3D		[0.,0.,0.]	vector-valued load [SI:N]
loadVectorUserFunction	PyFunctionVector3	DScala	rVector3D	A python function which defines the time-
			0	dependent load with parameters (Real
				t, Vector3D load); the load represents
				the current value of the load; WARN-
				ING: this factor does not work in com-
				bination with static computation (load-
				Factor); Example for python function:
				def f(t, loadVector): return [loadVec-
				tor[0]*np.sin(t*10*2*3.1415),0,0]
visualization	VLoadTorqueVecto	r		parameters for visualization of item

The item VLoadTorqueVector has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

### 5.5.3 LoadMassProportional

Load attached to BodyMass-based marker, applying a 3D vector load (e.g. the vector [0,-g,0] is used to apply gravitational loading of size g in negative y-direction).

Short name for Python: Gravity

**Requested marker type** = Marker::BodyMass

The item LoadMassProportional has the following parameters:

Name	type	size	default value	description
type = 'MassProportional'				item typename for initialization
name	String		"	load"s unique name
markerNumber	Index		MAXINT	marker"s number to which load is applied
loadVector	Vector3D		[0.,0.,0.]	vector-valued load [SI:N/kg = m/s <sup>2</sup> ]
loadVectorUserFunction	PyFunctionVector3	DScala	rVector3D	A python function which defines the time-
			0	dependent load with parameters (Real
				t, Vector3D load); the load represents
				the current value of the load; WARN-
				ING: this factor does not work in com-
				bination with static computation (load-
				Factor); Example for python function:
				def f(t, loadVector): return [loadVec-
				tor[0]*np.sin(t*10*2*3.1415),0,0]
visualization	VLoadMassPropor	tional		parameters for visualization of item

The item VLoadMassProportional has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

### 5.5.4 LoadCoordinate

Load with scalar value, which is attached to a coordinate-based marker; the load can be used e.g. to apply a force to a single axis of a body, a nodal coordinate of a finite element or a torque to the rotatory DOF of a rigid body.

**Requested marker type** = Marker::Coordinate

The item LoadCoordinate has the following parameters:

Name	type	size	default value	description
type = 'Coordinate'				item typename for initialization
name	String		"	load"s unique name
markerNumber	Index		MAXINT	marker"s number to which load is applied
load	Real		0.	scalar load [SI:N]
loadUserFunction	PyFunctionScalar2		0	A python function which defines the time-
				dependent load with parameters (Real t,
				Real load); the load represents the cur-
				rent value of the load; WARNING: this
				factor does not work in combination with
				static computation (loadFactor); Example
				for python function: def f(t, load): return
				load*np.sin(t*10*2*3.1415)
visualization	VLoadCoordinate			parameters for visualization of item

The item VLoadCoordinate has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

### 5.6 Sensors

### 5.6.1 SensorNode

A sensor attached to a node. The sensor outputs values into a file, showing time, sensorValue[0], sensorValue[1], ... . A user function can be attached to modify sensor values accordingly.

The item SensorNode has the following parameters:

Name	type	size	default value	description
type = 'Node'			•	item typename for initialization
name	String		"	marker"s unique name
nodeNumber	Index		MAXINT	node number to which sensor is attached to
writeToFile	bool		True	true: write sensor output to file
fileName	String		"	directory and file name for sensor file out- put; default: empty string generates sensor + sensorNumber + outputVariableType
outputVariableType	OutputVariableType	е	OutputVariableTy	rpe:(NutpertVariableType for sensor
visualization	VSensorNode			parameters for visualization of item

The item VSensorNode has the following parameters:

Name	type	size	default value	description
show	bool		True	set true, if item is shown in visualization
				and false if it is not shown

# 5.7 GraphicsData

Some items may include a 'graphicsData' structure. GraphicsData contains a list of graphicsData items, i.e. graphicsData = [graphicsItem1, graphicsItem2, ...]. Every single graphicsItem may be defined as one of the following structures using a specific 'type':

Name	type	default value	description		
type = 'Line':			draws a polygonal line between all specified points		
color	list	[0,0,0,1]	list of 4 floats to define RGB-color and transparency		
data	list	mandatory	list of float triples of x,y,z coordinates of the line		
			floats to define RGB-color and transparency; Exam-		
			ple: data=[0,0,0, 1,0,0, 1,1,0, 0,1,0, 0,0,0] draws a		
			rectangle with side length 1		
type = 'Circle':			draws a circle with center point, normal (defines plane of		
color	list	[0,0,0,1]	circle) and radius list of 4 floats to define RGB-color and transparency		
radius	float	mandatory	radius		
position	list	mandatory	list of float triples of x,y,z coordinates of center point		
1			of the circle		
normal	list	[0,0,1]	list of float triples of x,y,z coordinates of normal to the		
			plane of the circle; the default value gives a circle in		
			the $(x, y)$ -plane		
type = 'Text':			places the given text at position		
color	list	[0,0,0,1]	list of 4 floats to define RGB-color and transparency		
text	string	mandatory	text to be displayed		
position	list	mandatory	list of float triples of [x,y,z] coordinates of the left upper		
			position of the text; e.g. position=[20,10,0]		
type = 'TriangleLis	st':		draws a flat triangle mesh for given points and connectivity		
points	list	mandatory	list [x0,y0,z0, x1,y1,z1,] containing $n \times 3$ floats		
			(grouped x0,y0,z0, x1,y1,z1,) to define x,y,z coor-		
			dinates of points, <i>n</i> being the number of points (=ver-		
			tices)		
colors	list	empty	list [R0,G0,B0,A0, R1,G2,B1,A1,] containing $n \times 4$		
			floats to define RGB-color and transparency A, where $n$		
			must be according to number of points; if field 'colors'		
			does not exist, default colors will be used		
normals	list	empty	list $[n0x,n0y,n0z,]$ containing $n \times 3$ floats to define		
			normal direction of triangles per point, where $n$ must		
			be according to number of points; if field 'normals'		
			does not exist, default normals [0,0,0] will be used		
triangles	list	mandatory	list [T0point0, T0point1, T0point2,] containing		
			$n_{trig} \times 3$ floats to define point indices of each vertex of		
			the triangles (=connectivity); point indices start with		
			index 0; the maximum index must be $\leq$ points.size()		

Examples of GraphicsData can be found in the Python examples and in exudynUtilities.py.

# **Chapter 6**

# **EXUDYN Settings**

This section includes the reference manual for settings which are available in the python interface, e.g. simulation settings, visualization settings, and others.

## 6.1 Simulation settings

This section includes hierarchical structures for simulation settings, e.g., time integration, static solver, Newton iteration and solution file export.

### 6.1.1 SolutionSettings

General settings for exporting the solution (results) of a simulation. SolutionSettings has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
writeSolutionToFile	bool		True	flag (true/false), which determines if
				(global) solution vector is written to file
appendToFile	bool		False	flag (true/false); if true, solution is ap-
				pended to existing file (otherwise created)
writeFileHeader	bool		True	flag (true/false); if true, file header is writ-
				ten (turn off, e.g. for multiple runs of time
				integration)
writeFileFooter	bool		True	flag (true/false); if true, information at end
				of simulation is written: convergence, total
				solution time, statistics
solutionWritePeriod	UReal		0.01	time span (period), determines how often
				the solution is written during a simulation
sensorsAppendToFile	bool		False	flag (true/false); if true, sensor output is ap-
				pended to existing file (otherwise created)
sensorsWriteFileHeader	bool		True	flag (true/false); if true, file header is written
				for sensor output (turn off, e.g. for multiple
				runs of time integration)
sensorsWritePeriod	UReal		0.01	time span (period), determines how often
				the sensor output is written during a simu-
				lation

exportVelocities	bool	True	solution is written as displacements, velocities[, accelerations] [,algebraicCoordinates] [,DataCoordinates]
exportAccelerations	bool	True	solution is written as displacements, [velocities,] accelerations [,algebraicCoordinates] [,DataCoordinates]
exportAlgebraicCoordinates	bool	True	solution is written as displacements, [velocities,] [accelerations,], algebraicCoordinates (=Lagrange multipliers) [,DataCoordinates]
exportDataCoordinates	bool	True	solution is written as displacements, [velocities,] [accelerations,] [,algebraicCoordinates (=Lagrange multipliers)] ,DataCoordinates
coordinatesSolutionFileName	FileName	'coordinatesSolution.tx	t' filename and (relative) path of solution file containing all coordinates versus time
solverInformationFileName	FileName	'solverInormation.txt'	filename and (relative) path of text file showing detailed information during solv- ing; detail level according to your- Solver.verboseModeFile
solutionInformation	String	"	special information added to header of solution file (e.g. parameters and settings, modes,)
outputPrecision	Index	10	precision for floating point numbers written to solution and sensor files
recordImagesInterval	Real	-1.	record frames (images) during solving: amount of time to wait until next image (frame) is recorded; set recordImages = -1. if no images shall be recorded; set, e.g., recordImages = 0.01 to record an image every 10 milliseconds (requires that the time steps / load steps are sufficiently small!); for file names, etc., see VisualizationSettings.exportImages

## 6.1.2 Numerical Differentiation Settings

Settings for numerical differentiation of a function (needed for computation of numerical jacobian e.g. in implizit integration); HOTINT1: relativeEpsilon \* Maximum(minimumCoordinateSize, fabs(x(i))). NumericalDifferentiationSettings has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	

relativeEpsilon	UReal	1e-7	relative differentiation parameter epsilon; the numerical differentiation parameter $\varepsilon$ follows from the formula ( $\varepsilon = \varepsilon_{\text{relative}} * \max(q_{\min},  q_i + [q_i^{Ref}] )$ ), with $\varepsilon_{\text{relative}} = \text{relative} \in \text{Epsilon}$ , $q_{\min} = \min_{i=1}^{n} \min_{j=1}^{n} \min_{i=1}^{n} \min_{j=1}^{n} \sup_{j=1}^{n} \sup_{$
minimumCoordinateSize	UReal	1e-2	minimum size of coordinates in relative dif- ferentiation parameter
doSystemWideDifferentiation	bool	False	true: system wide differentiation (e.g. all ODE2 equations w.r.t. all ODE2 coordinates); false: only local (object) differentiation
addReferenceCoordinatesToEp	silon bool	False	true: for the size estimation of the differentiation parameter, the reference coordinate $q_i^{Ref}$ is added to ODE2 coordinates -> see; false: only the current coordinate is used for size estimation of the differentiation parameter

# 6.1.3 NewtonSettings

Settings for Newton method used in static or dynamic simulation. NewtonSettings has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
numericalDifferentiation	NumericalDifferent	iatioı	Settings	numerical differentiation parameters for
				numerical jacobian (e.g. Newton in static
				solver or implicit time integration)
useNumericalDifferentiation	bool		False	flag (true/false); false = perform direct com-
				putation of jacobian, true = use numerical
				differentiation for jacobian
useNewtonSolver	bool		True	flag (true/false); false = linear computation,
				true = use Newton solver for nonlinear so-
				lution
relativeTolerance	UReal		1e-8	relative tolerance of residual for Newton
				(general goal of Newton is to decrease the
				residual by this factor)
absoluteTolerance	UReal		1e-10	absolute tolerance of residual for New-
				ton (needed e.g. if residual is ful-
				filled right at beginning); condition:
				sqrt(q*q)/numberOfCoordinates <= abso-
				luteTolerance

weightTolerancePerCoordinate	bool	False	flag (true/false); false = compute error as L2-
weight folerancer erecordinate	5001	Taise	Norm of residual; true = compute error as
			(L2-Norm of residual) / (sqrt(number of co-
			_
			ordinates)), which can help to use common
2 11 26 1			tolerance independent of system size
newtonResidualMode	Index	0	0 use residual for computation of error
			(standard); 1 use change of solution in-
			crement for error (set relTol and absTol to
			same values!) ==> may be advantageous if
			residual is zero, e.g., in kinematic analysis;
			TAKE CARE with this flag
adaptInitialResidual	bool	True	flag (true/false); false = standard; true: if
			initialResidual is very small (or zero), it
			may increas dramatically in first step; to
			achieve relativeTolerance, the initialResid-
			ual will by updated by a higher residual
			within the first Newton iteration
1:C INI C C C C	TID 1	0.5	
modifiedNewtonContractivity	UReal	0.5	maximum contractivity (=reduction of er-
			ror in every Newton iteration) accepted by
			modified Newton; if contractivity is greater,
			a Jacobian update is computed
useModifiedNewton	bool	False	true: compute Jacobian only at first step; no
			Jacobian updates per step; false: Jacobian
			computed in every step
modifiedNewtonJacUpdatePers	Step	False	true: compute Jacobian at every time step,
_	bool		but not in every iteration (except for bad
			convergence ==> switch to full Newton)
maxIterations	Index	25	maximum number of iterations (including
			modified + restart Newton steps); after that
			iterations, the static/dynamic solver stops
			with error
maxModifiedNewtonIterations	Index	8	maximum number of iterations for modi-
maxivioumed New torriterations	niuex	0	
			fied Newton (without Jacobian update); af-
			ter that number of iterations, the modified
			Newton method gets a jacobian update and
			is further iterated
maxModifiedNewtonRestartIte	rations	7	maximum number of iterations for modi-
	Index		fied Newton after aJacobian update; after
			that number of iterations, the full Newton
			method is started for this step
maximumSolutionNorm	UReal	1e38	this is the maximum allowed value
			for solutionU.L2NormSquared() which
			is the square of the square norm
			(value= $u_1^2+u_2^2+$ ), and solutionV/A; if the
			norm of solution vectors are larger, Newton
			method is stopped; the default value is cho-
			sen such that it would still work for single
			precision numbers (float)
mayDiagontinuousIteesties	Indov		
maxDiscontinuousIterations	Index	5	maximum number of discontinuous (post
Ì			Newton) iterations

ignoreMaxDiscontinuousIterati	ons	True	continue solver if maximum number of
	bool		discontinuous (post Newton) iterations is
			reached (ignore tolerance)
discontinuousIterationToleranc	e	1	absolute tolerance for discontinuous (post
	UReal		Newton) iterations; the errors represent ab-
			solute residuals and can be quite high
stepInformation	Index	2	0 only current step time, 1 show time
			to go, 2 show newton iterations (Nit)
			per step, 3 show discontinuous iterations
			(Dit) and newton jacobians (jac) per step

### 6.1.4 GeneralizedAlphaSettings

Settings for generalized-alpha, implicit trapezoidal or Newmark time integration methods. GeneralizedAlphaSettings has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
newmarkBeta	UReal		0.25	value beta for Newmark method; default
				value beta = $\frac{1}{4}$ corresponds to (undamped)
				trapezoidal rule
newmarkGamma	UReal		0.5	value gamma for Newmark method; de-
				fault value gamma = $\frac{1}{2}$ corresponds to (un-
				damped) trapezoidal rule
useIndex2Constraints	bool		False	set useIndex2Constraints = true in order to
				use index2 (velocity level constraints) for-
				mulation
useNewmark	bool		False	if true, use Newmark method with beta and
				gamma instead of generalized-Alpha
spectralRadius	UReal		0.9	spectral radius for Generalized-alpha
				solver; set this value to 1 for no damping
				or to 0 < spectralRadius < 1 for damping
				of high-frequency dynamics; for position-
				level constraints (index 3), spectralRadius
				must be < 1
computeInitialAccelerations	bool		True	true: compute initial accelerations from
				system EOM in acceleration form; false: use
				zero accelerations

## 6.1.5 TimeIntegrationSettings

General parameters used in time integration; specific parameters are provided in the according solver settings, e.g. for generalizedAlpha.

TimeIntegrationSettings has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
newton	NewtonSettings			parameters for Newton method; used for
				implicit time integration methods only
startTime	UReal		0	start time of time integration (usually set to
				zero)
endTime	UReal		1	end time of time integration
numberOfSteps	UInt		100	number of steps in time integration;
				stepsize is computed from (endTime-
				startTime)/numberOfSteps
adaptiveStep	bool		True	true: use step reduction if step fails; false:
				constant step size
minimumStepSize	UReal		1e-8	lower limit of time step size, before integra-
				tor stops
verboseMode	Index		0	0 no output, 1 show short step infor-
				mation every 2 seconds (error), 2 show
				every step information, 3 show also solu-
				tion vector, 4 show also mass matrix and
				jacobian (implicit methods), 5 show also
				Jacobian inverse (implicit methods)
verboseModeFile	Index		0	same behaviour as verboseMode, but out-
				puts all solver information to file
generalizedAlpha	GeneralizedAlphaS	ettin	gs	parameters for generalized-alpha, implicit
				trapezoidal rule or Newmark (options only
				apply for these methods)
preStepPyExecute	String		"	Python code to be executed prior to every
				step and after last step, e.g. for postprocess-
				ing

# 6.1.6 StaticSolverSettings

Settings for static solver linear or nonlinear (Newton). StaticSolverSettings has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
newton	NewtonSettings			parameters for Newton method (e.g. in
				static solver or time integration)
numberOfLoadSteps	Index		1	number of load steps; if numberOfLoad-
				Steps=1, no load steps are used and full
				forces are applied at once
loadStepDuration	UReal		1	quasi-time for all load steps (added to cur-
				rent time in load steps)

log dCtomCtomt	LIDaal	0	a guasi time which can be used for
loadStepStart	UReal	0	a quasi time, which can be used for
			the output (first column) as well as
			for time-dependent forces; quasi-
			time is increased in every step i by
			loadStepDuration/numberOfLoad-
			Steps; loadStepTime = loadStepStart +
			i*loadStepDuration/numberOfLoadSteps,
			but loadStepStart untouched ==> incre-
			ment by user
loadStepGeometric	bool	False	if loadStepGeometric=false, the load steps
The state of the s			are incremental (arithmetic series, e.g.
			0.1,0.2,0.3,); if true, the load steps are
			increased in a geometric series, e.g. for
			n = 8 numberOfLoadSteps and $d =$
			1000 loadStepGeometricRange, it follows:
			$1000^{1/8}/1000 = 0.00237, 1000^{2/8}/1000 =$
			$0.00562$ , $1000^{3/8}/1000 = 0.0133$ ,,
			$1000^{7/8}/1000 = 0.422, 1000^{8/8}/1000 = 1$
loadStepGeometricRange	UReal	1000	if loadStepGeometric=true, the load steps
1			are increased in a geometric series, see load-
			StepGeometric
useLoadFactor	bool	True	true: compute a load factor $\in [0,1]$ from
useLoadi actor	5001	liue	
			static step time; all loads are scaled by the
			load factor; false: loads are always scaled
			with 1 – use this option if time dependent
			loads use a userFunction
stabilizerODE2term	UReal	0	add mass-proportional stabilizer term in
			ODE2 part of jacobian for stabilization
			(scaled ), e.g. of badly conditioned prob-
			lems; the diagnoal terms are scaled with
			$stabilizer = (1 - loadStepFactor^2)$ , and go
			to zero at the end of all load steps:
			loadStepFactor = 1 -> stabilizer = 0
1CCt	1 1	T	
adaptiveStep	bool	True	true: use step reduction if step fails; false:
			fixed step size
minimumStepSize	UReal	1e-8	lower limit of step size, before nonlinear
			solver stops
verboseMode	Index	1	0 no output, 1 show errors and load
			steps, 2 show short Newton step infor-
			mation (error), 3 show also solution vec-
			tor, 4 show also jacobian, 5 show also
			Jacobian inverse
verboseModeFile	Index	0	same behaviour as verboseMode, but out-
verbosemoderile	niuex		
C. P.F.	0	"	puts all solver information to file
preStepPyExecute	String		Python code to be executed prior to every
			load step and after last step, e.g. for post-
		1 1	processing

### 6.1.7 SimulationSettings

General Settings for simulation; according settings for solution and solvers are given in subitems of this structure.

SimulationSettings has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
timeIntegration	TimeIntegrationSet	tings		time integration parameters
solutionSettings	SolutionSettings			settings for solution files
staticSolver	StaticSolverSettings	•		static solver parameters
linearSolverType	LinearSolverType		LinearSolverType::EXU	dense
				selection of numerical linear solver:
				exu.LinearSolverType.EXUdense
				(dense matrix inverse),
				exu.LinearSolverType.EigenSparse (sparse
				matrix LU-factorization), (enumeration
				type)
cleanUpMemory	bool		False	true: solvers will free memory at exit (rec-
				ommended for large systems); false: keep
				allocated memory for repeated computa-
				tions to increase performance
displayStatistics	bool		False	display general computation information at
				end of time step (steps, iterations, function
				calls, step rejections,
display Computation Time	bool		False	display computation time statistics at end
				of solving
pauseAfterEachStep	bool		False	pause after every time step or static load
				step(user press SPACE)
outputPrecision	Index		6	precision for floating point numbers written
				to console; e.g. values written by solver
numberOfThreads	Index		1	number of threads used for parallel com-
				putation (1 == scalar processing); not yet
				implemented (status: Nov 2019)

# 6.2 Visualization settings

This section includes hierarchical structures for visualization settings, e.g., drawing of nodes, bodies, connectors, loads and markers and furthermore openGL, window and save image options.

## 6.2.1 VSettingsGeneral

General settings for visualization.

VSettingsGeneral has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	

graphicsUpdateInterval	float		0.1	interval of graphics update during simula-
				tion in seconds; $0.1 = 10$ frames per second;
				low numbers might slow down computa-
				tion speed
autoFitScene	bool		True	automatically fit scene within first second
				after StartRenderer()
textSize	float		12.	general text size if not overwritten
minSceneSize	float		0.1	minimum scene size for initial scene size
				and for autoFitScene, to avoid division by
				zero; SET GREATER THAN ZERO
backgroundColor	Float4	4	[1.,1.,1.,1.]	
				red, green, blue and alpha values for back-
				ground of render window (white=[1,1,1,1];
				black = [0,0,0,1]
coordinateSystemSize	float		0.4	size of coordinate system relative to screen
drawCoordinateSystem	bool		True	false = no coordinate system shown
showComputationInfo	bool		True	false = no info about computation (current
				time, solver, etc.) shown
pointSize	float		0.01	global point size (absolute)
circleTiling	Index		16	global number of segments for circles; if
				smaller than 2, 2 segments are used (flat)
cylinderTiling	Index		16	global number of segments for cylinders; if
				smaller than 2, 2 segments are used (flat)
sphereTiling	Index		8	global number of segments for spheres; if
				smaller than 2, 2 segments are used (flat)

# 6.2.2 VSettingsWindow

Window and interaction settings for visualization; handle changes with care, as they might lead to unexpected results or crashes.

VSettingsWindow has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
renderWindowSize	Index2	2	[1024,768]	initial size of OpenGL render window in
				pixel
startupTimeout	Index		5000	OpenGL render window startup timeout in
				ms (change might be necessary if CPU is
				very slow)
alwaysOnTop	bool		False	true: OpenGL render window will be al-
				ways on top of all other windows
maximize	bool		False	true: OpenGL render window will be max-
				imized at startup
showWindow	bool		True	true: OpenGL render window is shown on
				startup; false: window will be iconified at
				startup (e.g. if you are starting multiple
				computations automatically)

keypressRotationStep	float	5.	rotation increment per keypress in degree
			(full rotation = 360 degree)
mouseMoveRotationFactor	float	1.	rotation increment per 1 pixel mouse move-
			ment in degree
keypressTranslationStep	float	0.1	translation increment per keypress relative
			to window size
zoomStepFactor	float	1.15	change of zoom per keypress (keypad +/-)
			or mouse wheel increment

# 6.2.3 VSettingsOpenGL

OpenGL settings for 2D and 2D rendering. VSettingsOpenGL has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
initialCenterPoint	Float3	3	[0.,0.,0.]	
				centerpoint of scene (3D) at renderer
				startup; overwritten if autoFitScene = True
initialZoom	float		1.	initial zoom of scene; overwritten/ignored
				if autoFitScene = True
initialMaxSceneSize	float		1.	initial maximum scene size (auto: diago-
				nal of cube with maximum scene coordi-
				nates); used for 'zoom all' functionality and
				for visibility of objects; overwritten if aut-
				oFitScene = True
initialModelRotation	StdArray33F	3x3		
			0.,1.,0., 0.,0.,1.]]	initial model rotation matrix for OpenGl;
				in python use e.g.: initialModelRota-
				tion=[[1,0,0],[0,1,0],[0,0,1]]
multiSampling	Index	1	1	multi sampling turned off (<=1) or turned
				on to given values (2, 4, 8 or 16); increases
				the graphics buffers and might crash due
				to graphics card memory limitations; only
				works if supported by hardware; if it does
				not work, try to change 3D graphics hard-
				ware settings!
lineWidth	float	1	1.	width of lines used for representation of
				lines, circles, points, etc.
lineSmooth	bool	1	True	draw lines smooth
textLineWidth	float	1	1.	width of lines used for representation of text
textLineSmooth	bool	1	False	draw lines for representation of text smooth
showFaces	bool	1	True	show faces of triangles, etc.; using
				the options showFaces=false and show-
				FaceEdges=true gives are wire frame rep-
				resentation

showFaceEdges	bool	1	False	show edges of faces; using the options showFaces=false and show-FaceEdges=true gives are wire frame representation
shadeModelSmooth	bool	1	True	true: turn on smoothing for shaders, which
				uses vertex normals to smooth surfaces
materialSpecular	Float4	4	[1.,1.,1.,1.]	
				4f specular color of material
materialShininess	float	1	60.	shininess of material
enableLight0	bool	1	True	turn on/off light0
light0position	Float4	4	[1.,1.,-10.,0.]	
				4f position vector of GL light0; 4th value
				should be 0, otherwise the vector obtains a
				special interpretation, see opengl manuals
light0ambient	float	1	0.25	ambient value of GL light0
light0diffuse	float	1	0.4	diffuse value of GL light0
light0specular	float	1	0.4	specular value of GL light0
enableLight1	bool	1	True	turn on/off light1
light1position	Float4	4	[0.,3.,2.,0.]	
				4f position vector of GL light1; 4th value
				should be 0, otherwise the vector obtains a
				special interpretation, see opengl manuals
light1ambient	float	1	0.25	ambient value of GL light1
light1diffuse	float	1	0.4	diffuse value of GL light1
light1specular	float	1	0.	specular value of GL light1
drawFaceNormals	bool	1	False	draws triangle normals, e.g. at center of
				triangles; used for debugging of faces
drawVertexNormals	bool	1	False	draws vertex normals; used for debugging
drawNormalsLength	float	1	0.1	length of normals; used for debugging

## 6.2.4 VSettingsContour

Settings for contour plots; use these options to visualize field data, such as displacements, stresses, strains, etc. for bodies, nodes and finite elements.

VSettingsContour has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
outputVariableComponent	Index	1	0	select the component of the chosen output
				variable; e.g., for displacements, 3 compo-
				nents are available: $0 == x$ , $1 == y$ , $2 == z$
				component; if this component is not avail-
				able by certain objects or nodes, no value is
				drawn
outputVariable	OutputVariableTyp	e	OutputVariableType::N	lone
				selected contour plot output variable type;
				select OutputVariableType.None to deacti-
				vate contour plotting.

minValue	float	1 (	0	minimum value for contour plot; set man-
				ually, if automaticRange == False
maxValue	float	1	1	maximum value for contour plot; set man-
				ually, if automaticRange == False
automaticRange	bool	-	True	if true, the contour plot value range is cho-
				sen automatically to the maximum range
showColorBar	bool	-	True	show the colour bar with minimum and
				maximum values for the contour plot
colorBarTiling	Index	1 1	12	number of tiles (segements) shown in the
				colorbar for the contour plot

## 6.2.5 VSettingsExportImages

Functionality to export images to files (.tga format) which can be used to create animations; to activate image recording during the solution process, set SolutionSettings.recordImagesInterval accordingly. VSettingsExportImages has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
saveImageTimeOut	Index		5000	timeout for safing a frame as image to disk;
				this is the amount of time waited for re-
				drawing; increase for very complex scenes
saveImageFileName	FileName		'images/rame'	filename (without extension!) and (rel-
				ative) path for image file(s) with con-
				secutive numbering (e.g., frame0000.tga,
				frame0001.tga,); folders must already ex-
				ist!
saveImageFileCounter	Index		0	current value of the counter which is used
				to consecutively save frames (images) with
				consecutive numbers
saveImageSingleFile	bool		False	true: only save single files with given file-
				name, not adding numbering; false: add
				numbering to files, see saveImageFileName

## 6.2.6 VSettingsNodes

Visualization settings for nodes.

VSettingsNodes has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
show	bool		True	flag to decide, whether the nodes are shown
showNumbers	bool		False	flag to decide, whether the node number is
				shown

defaultSize	float	-1.	•	global node size; if -1.f, node size is relative
				to openGL.initialMaxSceneSize
defaultColor	Float4	4 [0.	.2,0.2,1.,1.]	
				default cRGB olor for nodes; 4th value is
				alpha-transparency
showNodalSlopes	Index	Fa	ılse	draw nodal slope vectors, e.g. in ANCF
				beam finite elements

## 6.2.7 VSettingsBeams

Visualization settings for beam finite elements.

 $VS ettings Beams \ has \ the \ following \ items:$ 

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
axialTiling	Index		8	number of segments to discretise the beams
				axis

## 6.2.8 VSettingsBodies

Visualization settings for bodies.

VSettingsBodies has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
show	bool		True	flag to decide, whether the bodies are
				shown
showNumbers	bool		False	flag to decide, whether the body(=object)
				number is shown
defaultSize	Float3	3	[1.,1.,1.]	
				global body size of xyz-cube
defaultColor	Float4	4	[0.2,0.2,1.,1.]	
				default cRGB olor for bodies; 4th value is
beams	VSettingsBeams			visualization settings for beams (e.g. AN-
				CFCable or other beam elements)

## 6.2.9 VSettingsConnectors

Visualization settings for connectors.

VSettingsConnectors has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	

show	bool		True	flag to decide, whether the connectors are shown
showNumbers	bool		False	flag to decide, whether the connector(=object) number is shown
showContact	bool		False	flag to decide, whether contact points, lines, etc. are shown
defaultSize	float		0.1	global connector size; if -1.f, connector size is relative to maxSceneSize
contactPointsDefaultSize	float		0.02	global contact points size; if -1.f, connector size is relative to maxSceneSize
defaultColor	Float4	4	[0.2,0.2,1.,1.]	default cRGB olor for connectors; 4th value is alpha-transparency

# 6.2.10 VSettingsMarkers

Visualization settings for markers.

VSettingsMarkers has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
show	bool		True	flag to decide, whether the markers are
				shown
showNumbers	bool		False	flag to decide, whether the marker numbers
				are shown
defaultSize	float		0.1	global marker size; if -1.f, marker size is
				relative to maxSceneSize
defaultColor	Float4	4	[0.1,0.5,0.1,1.]	
				default cRGB olor for markers; 4th value is
				alpha-transparency

# 6.2.11 VSettingsLoads

Visualization settings for loads.

VSettingsLoads has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
show	bool		True	flag to decide, whether the loads are shown
showNumbers	bool		False	flag to decide, whether the load numbers
				are shown
defaultSize	float		0.2	global load size; if -1.f, node size is relative
				to maxSceneSize

fixedLoadSize	bool	Tru	e	if true, the load is drawn with a fixed vec-
				tor length in direction of the load vector,
				independently of the load size
loadSizeFactor	float	0.1		if fixedLoadSize=false, then this scaling fac-
				tor is used to draw the load vector
defaultColor	Float4	4 [0.7	7,0.1,0.1,1.]	
				default cRGB olor for loads; 4th value is
				alpha-transparency

# 6.2.12 VSettingsSensors

Visualization settings for sensors.

VSettingsSensors has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
show	bool		True	flag to decide, whether the sensors are
				shown
showNumbers	bool		False	flag to decide, whether the sensor numbers
				are shown
defaultSize	float		0.2	global sensor size; if -1.f, node size is rela-
				tive to maxSceneSize
defaultColor	Float4	4	[0.6,0.6,0.1,1.]	
				default cRGB olor for sensors; 4th value is
				alpha-transparency

# 6.2.13 VisualizationSettings

Settings for visualization.

VisualizationSettings has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
general	VSettingsGeneral			general visualization settings
window	VSettingsWindow			visualization window and interaction set-
				tings
openGL	VSettingsOpenGL			OpenGL rendering settings
contour	VSettingsContour			contour plot visualization settings
exportImages	VSettingsExportIma	ages		settings for exporting (saving) images to
				files in order to create animations
nodes	VSettingsNodes			node visualization settings
bodies	VSettingsBodies			body visualization settings
connectors	VSettingsConnector	rs		connector visualization settings
markers	VSettingsMarkers			marker visualization settings
loads	VSettingsLoads			load visualization settings

sensors	VSettingsSensors			sensor visualization settings
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## 6.3 Solver substructures

This section includes structures contained in the solver, which can be accessed via the python interface during solution or for building a customized solver in python.

### 6.3.1 CSolverTimer

Structure for timing in solver. Each Real variable is used to measure the CPU time which certain parts of the solver need. This structure is only active if the code is not compiled with the \_\_FAST\_EXUDYN\_LINALG option and if displayComputationTime is set True. Timings will only be filled, if useTimer is True. CSolverTimer has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
useTimer	bool		True	flag to decide, whether the timer is used (true) or not
total	Real		0.	total time measured between start and end of computation (static/dynamics)
factorization	Real		0.	solve or inverse
newtonIncrement	Real		0.	Jac <sup>-1</sup> * RHS; backsubstitution
integrationFormula	Real		0.	time spent for evaluation of integration formulas
ODE2RHS	Real		0.	time for residual evaluation of ODE2 right- hand-side
AERHS	Real		0.	time for residual evaluation of algebraic equations right-hand-side
totalJacobian	Real		0.	time for all jacobian computations
jacobianODE2	Real		0.	jacobian w.r.t. coordinates of ODE2 equations (not counted in sum)
jacobianODE2_t	Real		0.	jacobian w.r.t. coordinates_t of ODE2 equations (not counted in sum)
jacobianAE	Real		0.	jacobian of algebraic equations (not counted in sum)
massMatrix	Real		0.	mass matrix computation
reactionForces	Real		0.	CqT * lambda
postNewton	Real		0.	post newton step
writeSolution	Real		0.	time for writing solution
overhead	Real		0.	overhead, such as initialization, copying and some matrix-vector multiplication
python	Real		0.	time spent for python functions
visualization	Real		0.	time spent for visualization in computation thread
Reset()	void		useSolverTimer	reset solver timings to initial state by assigning default values; useSolverTimer sets the useTimer flag

Sum()	Real		compute sum of all timers (except for those
			counted multiple, e.g., jacobians
StartTimer()	void	value	start timer function for a given variable;
			subtracts current CPU time from value
StopTimer()	void	value	stop timer function for a given variable;
			adds current CPU time to value
ToString()	String		converts the current timings to a string

### 6.3.2 SolverLocalData

Solver local data structure for solution vectors, system matrices and temporary vectors and data structures. SolverLocalData has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
nODE2	Index		0	number of second order ordinary diff. eq. coordinates
nODE1	Index		0	number of first order ordinary diff. eq. co- ordinates
nAE	Index		0	number of algebraic coordinates
nData	Index		0	number of data coordinates
nSys	Index		0	number of system (unknown) coordinates = nODE2+nODE1+nAE
startAE	Index		0	start of algebraic coordinates, but set to zero if nAE==0
systemResidual	ResizableVector			system residual vector (vectors will be linked to this vector!)
newtonSolution	ResizableVector			Newton decrement (computed from residual and jacobian)
tempODE2	ResizableVector			temporary vector for ODE2 quantities; use in initial accelerations and during Newton
temp2ODE2	ResizableVector			second temporary vector for ODE2 quantities; use in static computation
tempODE2F0	ResizableVector			temporary vector for ODE2 Jacobian
tempODE2F1	ResizableVector			temporary vector for ODE2 Jacobian
start Of Step State A Algorithmic	ResizableVector			additional term needed for generalized alpha (startOfStep state)
aAlgorithmic	ResizableVector			additional term needed for generalized alpha (current state)
CleanUpMemory()	void			if desired, temporary data is cleaned up to safe memory
SetLinearSolverType()	void		linearSolverType	set linear solver type and matrix version: links system matrices to according dense/s- parse versions
GetLinearSolverType()	LinearSolverType			return current linear solver type (dense/s-parse)

#### 6.3.3 SolverIterationData

Solver internal structure for counters, steps, step size, time, etc.; solution vectors, residuals, etc. are Solver-LocalData. The given default values are overwritten by the simulationSettings when initializing the solver. SolverIterationData has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
maxStepSize	Real		0.	constant or maximum stepSize
minStepSize	Real		0.	minimum stepSize for static/dynamic
				solver; only used, if adaptive step is acti-
				vated
currentStepSize	Real		0.	stepSize of current step
numberOfSteps	Index		0	number of time steps (if fixed size); <i>n</i>
currentStepIndex	Index		0	current step index; i
adaptiveStep	bool		True	if true, the step size may be adaptively con-
				trolled
currentTime	Real		0.	holds the current simulation time, copy
				of state.current.time; interval is [start-
				Time,tEnd]; in static solver, duration is
				loadStepDuration
startTime	Real		0.	time at beginning of time integration
endTime	Real		0.	end time of static/dynamic solver
discontinuousIteration	Index		0	number of current discontinuous iteration
newtonSteps	Index		0	number of current newton steps
newtonStepsCount	Index		0	count total Newton steps
newtonJacobiCount	Index		0	count total Newton jacobian computations
rejectedModifiedNewtonSteps	Index		0	count the number of rejected modified
				Newton steps (switch to full Newton)
discontinuousIterationsCount	Index		0	count total number of discontinuous itera-
				tions (min. 1 per step)
ToString()	String			convert iteration statistics to string; used for
				displayStatistics option

### 6.3.4 SolverConvergenceData

Solver internal structure for convergence information: residua, iteration loop errors and error flags. For detailed behavior of these flags, visit the source code!.

SolverConvergenceData has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
stepReductionFailed	bool		False	true, if iterations over time/static steps
				failed (finally, cannot be recovered)
discontinuousIterationsFailed			False	true, if discontinuous iterations failed (may
	bool			be recovered if adaptive step is active)

linearSolverFailed	bool	False	true, if linear solver failed to factorize
newtonConverged	bool	False	true, if Newton has (finally) converged
newtonSolutionDiverged	bool	False	true, if Newton diverged (may be recov-
			ered)
jacobianUpdateRequested	bool	True	true, if a jacobian update is requested in
			modified Newton (determined in previous
			step)
mass Matrix Not Invertible	bool	True	true, if mass matrix is not invertable during
			initialization or solution (explicit solver)
discontinuousIterationError	Real	0.	error of discontinuous iterations (contact,
			friction,) outside of Newton iteration
residual	Real	0.	current Newton residual
lastResidual	Real	0.	last Newton residual to determine contrac-
			tivity
contractivity	Real	0.	Newton contractivity = geometric decay of
			error in every step
errorCoordinateFactor	Real	1.	factor may include the number of system
			coordinates to reduce the residual
InitializeData()	void		initialize SolverConvergenceData by as-
			signing default values

## 6.3.5 SolverOutputData

Solver internal structure for output modes, output timers and counters. SolverOutputData has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
finishedSuccessfully	bool		False	flag is false until solver finshed successfully
				(can be used as external trigger)
verboseMode	Index		0	this is a copy of the solvers verboseMode
				used for console output
verboseModeFile	Index		0	this is a copy of the solvers verboseMode-
				File used for file
writeToSolutionFile	bool		False	if false, no solution file is generated and no
				file is written
writeToSolverFile	bool		False	if false, no solver output file is generated
				and no file is written
sensorValuesTemp	ResizableVector			temporary vector for per sensor values
				(overwritten for every sensor; usually con-
				tains last sensor)
lastSolutionWritten	Real		0.	simulation time when last solution has been
				written
lastSensorsWritten	Real		0.	simulation time when last sensors have
				been written
lastImageRecorded	Real		0.	simulation time when last image has been
				recorded

cpuStartTime	Real	0.	CPU start time of computation (starts
			counting at computation of initial condi-
			tions)
cpuLastTimePrinted	Real	0.	CPU time when output has been printed
			last time
InitializeData()	void		initialize SolverOutputData by assigning
			default values

#### 6.3.6 MainSolverStatic

PyBind interface (trampoline) class for static solver. With this interface, the static solver and its substructures can be accessed via python. NOTE that except from SolveSystem(...), these functions are only intended for experienced users and they need to be handled with care, as unexpected crashes may happen if used inappropriate. Furthermore, the functions have a lot of overhead (performance much lower than internal solver) due to python interfaces, and should thus be used for small systems. To access the solver in python, write:

solver = MainSolverStatic()

and hereafter you can access all data and functions via 'solver'. MainSolverStatic has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
timer	CSolverTimer			timer which measures the CPU time of
				solver sub functions
it	SolverIterationData			all information about iterations (steps, dis-
				continuous iteration, newton,)
conv	SolverConvergence	Data		all information about tolerances, errors and
				residua
output	SolverOutputData			output modes and timers for exporting
				solver information and solution
newton	NewtonSettings			copy of newton settings from timeint or
				staticSolver
load Step Geometric Factor	Real			multiplicative load step factor; this factor is
				computed from loadStepGeometric param-
				eters in SolveSystem()
CheckInitialized()	bool		mainSystem	check if MainSolver and MainSystem are
				correctly initialized ==> otherwise raise Sy-
				sError
ComputeLoadFactor()	Real		simulationSettings	for static solver, this is a factor in interval
				[0,1]; MUST be overwritten
GetSolverName()	std::string			get solver name - needed for output file
				header and visualization window
IsStaticSolver()	bool			return true, if static solver; needs to be over-
				written in derived class
GetSimulationEndTime()	Real		simulationSettings	compute simulation end time (depends on
				static or time integration solver)

ReduceStepSize()	bool	mainSystem, simula-	reduce step size (1normal, 2severe prob-
1		tionSettings, severity	lems); return true, if reduction was success-
			ful
IncreaseStepSize()	void	mainSystem, simula-	increase step size if convergence is good
• ,		tionSettings	
InitializeSolver()	bool	mainSystem, simula-	initialize solverSpecific,data,it,conv;
		tionSettings	set/compute initial conditions (solver-
			specific!); initialize output files
PreInitializeSolverSpecific()		mainSystem, simula-	pre-initialize for solver specific tasks; called
	void	tionSettings	at beginning of InitializeSolver, right after
			Solver data reset
InitializeSolverOutput()	void	mainSystem, simula-	initialize output files; called from Initialize-
		tionSettings	Solver()
InitializeSolverPreChecks()		mainSystem, simula-	check if system is solvable; initialize
	bool	tionSettings	dense/sparse computation modes
InitializeSolverData()	void	mainSystem, simula-	initialize all data, it, conv; called from Initial-
		tionSettings	izeSolver()
InitializeSolverInitialCondition	s()	mainSystem, simula-	set/compute initial conditions (solver-
	void	tionSettings	specific!); called from InitializeSolver()
PostInitializeSolverSpecific()		mainSystem, simula-	post-initialize for solver specific tasks;
•	void	tionSettings	called at the end of InitializeSolver
SolveSystem()	bool	mainSystem, simula-	solve System: InitializeSolver, SolveSteps,
, ,		tionSettings	FinalizeSolver
FinalizeSolver()	void	mainSystem, simula-	write concluding information (timer statis-
		tionSettings	tics, messages) and close files
SolveSteps()	bool	mainSystem, simula-	main solver part: calls multiple Initial-
1 . , ,		tionSettings	izeStep()/ DiscontinuousIteration()/ Fin-
			ishStep(); do step reduction if necessary;
			return true if success, false else
UpdateCurrentTime()	void	mainSystem, simula-	update currentTime (and load factor);
•		tionSettings	MUST be overwritten in special solver class
InitializeStep()	void	mainSystem, simula-	initialize static step / time step; python-
_		tionSettings	functions; do some outputs, checks, etc.
FinishStep()	void	mainSystem, simula-	finish static step / time step; write output of
• • •		tionSettings	results to file
DiscontinuousIteration()	bool	mainSystem, simula-	perform discontinuousIteration for static
		tionSettings	step / time step; CALLS ComputeNewton-
			Residual
Newton()	bool	mainSystem, simula-	perform Newton method for given solver
		tionSettings	method
ComputeNewtonResidual()	void	mainSystem, simula-	compute residual for Newton method (e.g.
		tionSettings	static or time step); store result in system-
			Residual
ComputeNewtonUpdate()	void	mainSystem, simula-	compute update for currentState from new-
•		tionSettings	tonSolution (decrement from residual and
			jacobian)
ComputeNewtonJacobian()	void	mainSystem, simula-	compute jacobian for newton method of
-		tionSettings	given solver method; store result in system-
			Jacobian

WriteSolutionFileHeader()	void	mainSystem, simula- tionSettings	write unique file header, depending on static/ dynamic simulation
WriteCoordinatesToFile()	void	mainSystem, simula- tionSettings	write unique coordinates solution file
IsVerboseCheck()	bool	level	return true, if file or console output is at or above the given level
VerboseWrite()	void	level, str	write to console and/or file in case of level
GetODE2size()	Index		number of ODE2 equations in solver
GetODE1size()	Index		number of ODE1 equations in solver (not yet implemented)
GetAEsize()	Index		number of algebraic equations in solver
GetDataSize()	Index		number of data (history) variables in solver
GetSystemJacobian()	NumpyMatrix		get locally stored / last computed system jacobian of solver
GetSystemMassMatrix()	NumpyMatrix		get locally stored / last computed mass matrix of solver
GetSystemResidual()	NumpyVector		get locally stored / last computed system residual
GetNewtonSolution()	NumpyVector		get locally stored / last computed solution (=increment) of Newton
SetSystemJacobian()	void	systemJacobian	set locally stored system jacobian of solver; must have size nODE2+nODE1+nAE
SetSystemMassMatrix()	void	systemMassMatrix	set locally stored mass matrix of solver; must have size nODE2+nODE1+nAE
SetSystemResidual()	void	systemResidual	set locally stored system residual; must have size nODE2+nODE1+nAE
ComputeMassMatrix()	void	mainSystem, scalar- Factor=1.	compute systemMassMatrix (multiplied with factor) in cSolver and return mass matrix
ComputeJacobianODE2RHS()	void	mainSystem, scalar- Factor=1.	set systemJacobian to zero and add jacobian (multiplied with factor) of ODE2RHS to systemJacobian in cSolver
ComputeJacobianODE2RHS_t(.	) void	mainSystem, scalar- Factor=1.	add jacobian of ODE2RHS_t (multiplied with factor) to systemJacobian in cSolver
ComputeJacobianAE()	void	mainSystem, scalar- Factor_ODE2=1., scalarFac- tor_ODE2_t=1., velocityLevel=false	add jacobian of algebraic equations (multiplied with factor) to systemJacobian in cSolver; the scalarFactors are scaling the derivatives w.r.t. ODE2 coordinates and w.r.t. ODE2_t (velocity) coordinates; if velocityLevel == true, the constraints are evaluated at velocity level
ComputeODE2RHS()	void	mainSystem	compute the RHS of ODE2 equations in systemResidual in range(0,nODE2)
ComputeAlgebraicEquations(	) void	mainSystem, velocityLevel=false	compute the algebraic equations in systemResidual in range(nODE2+nODE1, nODE2+nODE1+nAE)

#### 6.3.7 MainSolverImplicitSecondOrder

PyBind interface (trampoline) class for dynamic implicit solver. Note that this solver includes the classical Newmark method (set useNewmark True; with option of index 2 reduction) as well as the generalized-alpha method. With the interface, the dynamic implicit solver and its substructures can be accessed via python. NOTE that except from SolveSystem(...), these functions are only intended for experienced users and they need to be handled with care, as unexpected crashes may happen if used inappropriate. Furthermore, the functions have a lot of overhead (performance much lower than internal solver) due to python interfaces, and should thus be used for small systems. To access the solver in python, write

solver = MainSolverImplicitSecondOrder()

and hereafter you can access all data and functions via 'solver'. In this solver, user functions are possible to extend the solver at certain parts, while keeping the overal C++ performance. MainSolverImplicitSecondOrder has the following items:

Name	type/function re-	size	default value / func-	description
	turn type		tion args	
timer	CSolverTimer			timer which measures the CPU time of
				solver sub functions
it	SolverIterationData			all information about iterations (steps, dis-
				continuous iteration, newton,)
conv	SolverConvergence	Data		all information about tolerances, errors and
				residua
output	SolverOutputData			output modes and timers for exporting
				solver information and solution
newton	NewtonSettings			copy of newton settings from timeint or
				staticSolver
newmarkBeta	Real			copy of parameter in timeIntegra-
				tion.generalizedAlpha
newmarkGamma	Real			copy of parameter in timeIntegra-
				tion.generalizedAlpha
alphaM	Real			copy of parameter in timeIntegra-
				tion.generalizedAlpha
alphaF	Real			copy of parameter in timeIntegra-
				tion.generalizedAlpha
spectralRadius	Real			copy of parameter in timeIntegra-
				tion.generalizedAlpha
factJacAlgorithmic	Real			locally computed parameter from general-
				izedAlpha parameters
CheckInitialized()	bool		mainSystem	check if MainSolver and MainSystem are
				correctly initialized ==> otherwise raise Sy-
	7. 1			sError
ComputeLoadFactor()	Real		simulationSettings	for static solver, this is a factor in interval
	NY			[0,1]; MUST be overwritten
GetAAlgorithmic()	NumpyVector			get locally stored / last computed algorith-
California (Control A A)				mic accelerations
GetStartOfStepStateAAlgorith				get locally stored / last computed algorith-
	NumpyVector			mic accelerations at start of step
SetUserFunctionUpdateCurren			mainSystem, user-	set user function
	void		Function	

SetUserFunctionInitializeStep(.		mainSystem, user-	set user function
	void	Function	
SetUserFunctionFinishStep()		mainSystem, user-	set user function
	void	Function	
SetUserFunctionDiscontinuous	Iteration()	mainSystem, user-	set user function
	void	Function	
SetUserFunctionNewton()	void	mainSystem, user-	set user function
		Function	
SetUserFunctionComputeNew	tonUpdate()	mainSystem, user-	set user function
	void	Function	
SetUserFunctionComputeNew	onResidual()	mainSystem, user-	set user function
•	void	Function	
SetUserFunctionComputeNew	onIacobian()	mainSystem, user-	set user function
r	void	Function	
GetSolverName()	std::string		get solver name - needed for output file
Getsorverr variety	stastring		header and visualization window
IsStaticSolver()	bool		return true, if static solver; needs to be over-
isstaticsorver()	0001		written in derived class
CatCina Latina FallTima (	Real	at an a 1 of a a C of the and	
GetSimulationEndTime()	Keal	simulationSettings	compute simulation end time (depends on
			static or time integration solver)
ReduceStepSize()	bool	mainSystem, simula-	reduce step size (1normal, 2severe prob-
		tionSettings, severity	lems); return true, if reduction was success-
			ful
IncreaseStepSize()	void	mainSystem, simula-	increase step size if convergence is good
		tionSettings	
InitializeSolver()	bool	mainSystem, simula-	initialize solverSpecific,data,it,conv;
		tionSettings	set/compute initial conditions (solver-
			specific!); initialize output files
PreInitializeSolverSpecific()		mainSystem, simula-	pre-initialize for solver specific tasks; called
	void	tionSettings	at beginning of InitializeSolver, right after
			Solver data reset
InitializeSolverOutput()	void	mainSystem, simula-	initialize output files; called from Initialize-
•		tionSettings	Solver()
InitializeSolverPreChecks()		mainSystem, simula-	check if system is solvable; initialize
,	bool	tionSettings	dense/sparse computation modes
InitializeSolverData()	void	mainSystem, simula-	initialize all data,it,conv; called from Initial-
		tionSettings	izeSolver()
InitializeSolverInitialCondition	s()	mainSystem, simula-	set/compute initial conditions (solver-
	void	tionSettings	specific!); called from InitializeSolver()
PostInitializeSolverSpecific()	Void	mainSystem, simula-	post-initialize for solver specific tasks;
1 ostilitianizesoiverspecific()	void	tionSettings	called at the end of InitializeSolver
SalvaSvetam( )			
SolveSystem()	bool	mainSystem, simula-	solve System: InitializeSolver, SolveSteps,
Fire all and all all and all all and all all all all all all all all all al	: 4	tionSettings	FinalizeSolver
FinalizeSolver()	void	mainSystem, simula-	write concluding information (timer statis-
		tionSettings	tics, messages) and close files
SolveSteps()	bool	mainSystem, simula-	main solver part: calls multiple Initial-
		tionSettings	izeStep()/ DiscontinuousIteration()/ Fin-
			ishStep(); do step reduction if necessary;
			return true if success, false else

UpdateCurrentTime()	void	mainSystem, simula-	update currentTime (and load factor);
		tionSettings	MUST be overwritten in special solver class
InitializeStep()	void	mainSystem, simula- tionSettings	initialize static step / time step; python- functions; do some outputs, checks, etc.
Einigh Ston( )	void	mainSystem, simula-	finish static step / time step; write output of
FinishStep()	Void	tionSettings	results to file
DiscontinuousIteration()	bool	mainSystem, simula-	perform discontinuousIteration for static
		tionSettings	step / time step; CALLS ComputeNewton-
		Ŭ	Residual
Newton()	bool	mainSystem, simula-	perform Newton method for given solver
		tionSettings	method
ComputeNewtonResidual()	void	mainSystem, simula-	compute residual for Newton method (e.g.
•		tionSettings	static or time step); store result in system-
			Residual
ComputeNewtonUpdate()	void	mainSystem, simula-	compute update for currentState from new-
1 , ,		tionSettings	tonSolution (decrement from residual and
		0	jacobian)
ComputeNewtonJacobian()	void	mainSystem, simula-	compute jacobian for newton method of
( )		tionSettings	given solver method; store result in system-
		<i>g</i> -	Jacobian
WriteSolutionFileHeader()	void	mainSystem, simula-	write unique file header, depending on stat-
		tionSettings	ic/ dynamic simulation
WriteCoordinatesToFile()	void	mainSystem, simula-	write unique coordinates solution file
		tionSettings	
IsVerboseCheck()	bool	level	return true, if file or console output is at or
· /			above the given level
VerboseWrite()	void	level, str	write to console and/or file in case of level
GetODE2size()	Index		number of ODE2 equations in solver
GetODE1size()	Index		number of ODE1 equations in solver (not
			yet implemented)
GetAEsize()	Index		number of algebraic equations in solver
GetDataSize()	Index		number of data (history) variables in solver
GetSystemJacobian()	NumpyMatrix		get locally stored / last computed system
			jacobian of solver
GetSystemMassMatrix()	NumpyMatrix		get locally stored / last computed mass ma-
			trix of solver
GetSystemResidual()	NumpyVector		get locally stored / last computed system
			residual
GetNewtonSolution()	NumpyVector		get locally stored / last computed solution
			(=increment) of Newton
SetSystemJacobian()	void	systemJacobian	set locally stored system jacobian of solver;
			must have size nODE2+nODE1+nAE
SetSystemMassMatrix()	void	systemMassMatrix	set locally stored mass matrix of solver;
			must have size nODE2+nODE1+nAE
SetSystemResidual()	void	systemResidual	set locally stored system residual; must
			have size nODE2+nODE1+nAE
ComputeMassMatrix()	void	mainSystem, scalar-	compute systemMassMatrix (multiplied
		Factor=1.	with factor) in cSolver and return mass ma-
			trix

ComputeJacobianODE2RHS()	void	mainSystem, scalar-	set systemJacobian to zero and add jaco-
		Factor=1.	bian (multiplied with factor) of ODE2RHS
			to systemJacobian in cSolver
ComputeJacobianODE2RHS_t(	)	mainSystem, scalar-	add jacobian of ODE2RHS_t (multiplied
	void	Factor=1.	with factor) to systemJacobian in cSolver
ComputeJacobianAE()	void	mainSystem, scalar-	add jacobian of algebraic equations (mul-
		Factor_ODE2=1.,	tiplied with factor) to systemJacobian in
		scalarFac-	cSolver; the scalarFactors are scaling the
		tor_ODE2_t=1.,	derivatives w.r.t. ODE2 coordinates and
		velocityLevel=false	w.r.t. ODE2_t (velocity) coordinates; if ve-
			locityLevel == true, the constraints are eval-
			uated at velocity level
ComputeODE2RHS()	void	mainSystem	compute the RHS of ODE2 equations in sys-
			temResidual in range(0,nODE2)
ComputeAlgebraicEquations(	)	mainSystem, veloc-	compute the algebraic equations in sys-
	void	ityLevel=false	temResidual in range(nODE2+nODE1,
			nODE2+nODE1+nAE)

# Chapter 7

# 3D Graphics Visualization

The 3D graphics visualization window is kept simple, but useful to see the animated results of the multibody system.

### 7.1 Mouse input

The following table includes the mouse functions.

Button	action	remarks
left mouse button	move model	keep left mouse button pressed to move the model in the
		current x/y plane
right mouse button	rotate model	keep right mouse button pressed to rotate model around
		current current $X_1/X_2$ axes
mouse wheel	zoom	use mouse wheel to zoom (on touch screens 'pinch-to-
		zoom' might work as well)

## 7.2 Keyboard input

The following table includes the keyboard shortcuts available in the window.

Key(s)	action	remarks
1,2,3,4 or 5	visualization update speed	the entered digit controls the visualization update, which
		can be changed from 1=1 update per 20ms to 5=1 update
		per 100s
'.' or KEYPAD '+'	zoom in	zoom one step into scene (additionally press CTRL to per-
		form small zoom step)
',' or KEYPAD '-'	zoom out	zoom one step out of scene (additionally press CTRL to
		perform small zoom step)
0 or KEYPAD '0'	reset rotation	set rotation such that the scene is oriented in the x/y plane
A	zoom all	set zoom such that the whole scene is visible
CURSOR UP, DOWN,	move scene	use coursor keys to move the scene up, down, left, and
		right

С	show/hide connectors	pressing this key switches the visibility of connectors
CTRL+C	show/hide connector num-	pressing this key switches the visibility of connector num-
	bers	bers
В	show/hide bodies	pressing this key switches the visibility of bodies
CTRL+B	show/hide body numbers	pressing this key switches the visibility of body numbers
L	show/hide loads	pressing this key switches the visibility of loads
CTRL+L	show/hide load numbers	pressing this key switches the visibility of load numbers
M	show/hide markers	pressing this key switches the visibility of markers
CTRL+M	show/hide marker numbers	pressing this key switches the visibility of marker numbers
N	show/hide nodes	pressing this key switches the visibility of nodes
CTRL+N	show/hide node numbers	pressing this key switches the visibility of node numbers
S	show/hide sensors	pressing this key switches the visibility of sensors
CTRL+S	show/hide sensor numbers	pressing this key switches the visibility of sensor numbers
Q	stop simulation	simulation is stopped and cannot be recovered
X	execute command	open dialog to enter a python command (in global python
		scope)
V	visualization settings	open dialog to modify visualization settings
ESCAPE	close render window	stops the simulation and closes the render window
SPACE	continue simulation	if simulation is paused, it can be continued by pressing
		space; use SHIFT+SPACE to continuously activate 'con-
		tinue simulation'

## **Chapter 8**

## Solver

### 8.1 Jacobian computation

The computation of the global jacobian matrix is time consuming for the static solver or implicit time integration. The equations are split into  $2^{nd}$  order differential equations,  $1^{st}$  order differential equations and algebraic equationsparts. From this structure, in the general non-symmetric case,  $3 \times 3$  submatrices result for the jacobian. Every submatrix of the jacobian has a certain meaning and needs to be computed individually. Specifically, in implicit time integration the  $2^{nd}$  order differential equations× $2^{nd}$  order differential equationsterm includes the (tangent) stiffness matrix and the mass matrix.

For efficient computation purpose, the elements provide a list of flags, which determine the dependencies as well as available (analytical) functions to compute the local (object) jacobian:

- ODE2\_ODE2 . . . derivative of ODE2 equations with respect to ODE2 variables
- ODE2\_ODE2\_t ... derivative of ODE2 equations with respect to ODE2\_t (velocity) variables
- ODE1\_ODE1 ... derivative of ODE1 equations with respect to ODE1 variables (NOT YET AVAILABLE)
- AE\_ODE2 ... derivative of AE (algebraic) equations with respect to ODE2 variables
- AE\_ODE2\_t ... derivative of AE (algebraic) equations with respect to ODE2\_t (velocity) variables (NOT YET AVAILABLE)
- AE\_ODE1 . . . derivative of AE (algebraic) equations with respect to ODE1 variables (NOT YET AVAILABLE)
- AE\_AE ... derivative of AE (algebraic) equations with respect to AE variables

If one of these flags is set (binary; e.g.ODE2\_ODE2 + ODE2\_ODE2\_t), then the according local jacobian is computed and assembled into the global jacobian in the static or implicit dynamic solver.

Jacobians can also be supplied in analytical (function) form, which is indicated by an additional flag with the same name but an additional term '\_function', e.g. 'ODE2\_ODE2\_function' indicates that the derivative of ODE2 equations with respect to its ODE2 coordinates is provided in an analytical form (this is the tangent stiffness matrix).

Two **object** functions are used to compute the local jacobians:

- ComputeJacobianODE2\_ODE2(Matrix& jacobian, Matrix& jacobian\_ODE2\_t): computes the ODE2\_ODE2 and ODE2\_ODE2\_t jacobians
- ComputeJacobianAE(Matrix& jacobian, Matrix& jacobian\_AE): computes the AE\_ODE2 and AE\_AE jacobians of the object ITSELF

Two connector functions are used to compute the local jacobians, using MarkerData:

- ComputeJacobianODE2\_ODE2(Matrix& jacobian, Matrix& jacobian\_ODE2\_t, const MarkerDataStructure& markerData): computes the ODE2\_ODE2 and ODE2\_ODE2\_t jacobians of the connector; e.g. for spring-damper
- ComputeJacobianAE(Matrix& jacobian, Matrix& jacobian\_AE, const MarkerDataStructure& marker-Data): computes the AE\_ODE2 and AE\_AE jacobians of the connector; e.g. for coordinate constraint

The system jacobian has the structure (2= ODE2, 1= ODE1,  $\lambda$  = AE;  $\bar{\mathbf{f}}_2$  = according system residual including dynamic (mass matrix) terms in time integration;  $\mathbf{g}_{\lambda}$  = algebraic equations):

$$\begin{bmatrix} \frac{\partial \bar{\mathbf{f}}_2}{\partial \mathbf{q}_2} & 0 & \left(\frac{\partial \mathbf{g}_{\lambda}}{\partial \mathbf{q}_2}\right)^T \\ 0 & \frac{\partial \mathbf{f}_1}{\partial \mathbf{q}_1} & \left(\frac{\partial \mathbf{g}_{\lambda}}{\partial \mathbf{q}_1}\right)^T \\ \frac{\partial \mathbf{g}_{\lambda}}{\partial \mathbf{q}_2} & \frac{\partial \mathbf{g}_{\lambda}}{\partial \mathbf{q}_1} & \frac{\partial \mathbf{g}_{\lambda}}{\partial \mathbf{q}_{\lambda}} \end{bmatrix}$$
(8.1)

Two system jacobian functions are currently available:

- JacobianODE2RHS(temp, newton, factorODE2, factorODE2\_t, jacobian\_ODE2\_t): compute analytical/numerical differentiation of ODE2RHS w.r.t. ODE2 and ODE2\_t coordinates; if analytical/functional version of jacobian is available and Newton flag 'useNumericalDifferentiation'=false, then the according jacobian is computed by its according function; results are 2 jacobians; the factors 'factor\_ODE2' and 'factor\_ODE2\_t' are used to scale the two jacobians; if a factor is zero, the according jacobian is not computed.
- JacobianAE(temp, newton, jacobian, factorODE2, velocityLevel, fillIntoSystemMatrix): compute constraint jacobian of AE with respect to ODE2 ('fillIntoSystemMatrix'=true: also w.r.t. [ODE1] and AE) coordinates  $\rightarrow$  direct computation given by access functions; 'factorODE2' is used to scale the ODE2-part of the jacobian (to avoid postmultiplication); velocityLevel = true: velocityLevel constraints are used, if available; 'fillIntoSystemMatrix'=true: fill in both  $\frac{\partial \tilde{f}_{\lambda}}{\partial q_2}$ ,  $\frac{\partial \tilde{f}_{\lambda}}{\partial q_2}$  AND  $\frac{\partial \tilde{f}_{\lambda}}{\partial q_3}$  at according locations into system matrix; 'fillIntoSystemMatrix'=false: (this is a temporary/WORKAROUND function):

The system jacobian functions compute the local jacobians either by means of a provided function or numerically, using the 'NumericalDifferentiation' settings of 'Newton'.

## 8.2 Implicit trapezoidal rule solver

This solver represents a class of solvers, which are based on the implicit trapezoidal rule. This integration includes the start value and the end value of a time step for the interpolation, thus being a trapezoidal integration rule. In some specializations, e.g. the Newmark method, the interpolation might only depend on the start value or the end value.

Most important representations of this rule:

- Trapezoidal rule (= Newmark with  $\beta = \frac{1}{4}$  and  $\gamma = \frac{1}{2}$ )
- Newmark method
- Generalized- $\alpha$  method (= generalized Newmark method with additional parameters

## 8.3 Representation of coordinates and equations of motion

Nomenclature:

- '2' ... second order equations (usually of a mechanical system)
- '1' ... first order equations (e.g. of a controller, fluid, etc.)
- $'\lambda'$  ... algebraic equations (usually of joints)
- M ... mass matrix
- q<sub>2</sub> ... 'displacement' coordinates of ODE2 equations
- $\dot{\mathbf{q}}_2 \dots$  'velocity' coordinates of ODE2 equations
- $\ddot{\mathbf{q}}_2$  ... 'acceleration' coordinates of ODE2 equations
- **q**<sub>1</sub> ... coordinates of ODE1 equations
- $\dot{\mathbf{q}}_1 \dots$  'velocity' coordinates of ODE1 equations
- $\mathbf{q}_{\lambda}$  ... Lagrange multipliers
- f<sub>2</sub> ... right-hand-side of ODE2 equations (except for action of joint reaction forces)
- f<sub>1</sub> ... right-hand-side of ODE1 equations
- g ... algebraic equations
- K ... (tangent) stiffness matrix
- D ... damping/gyroscopic matrix
- *h* . . . step size of time integration method

The equations of motion in EXUDYN are represented as

$$\mathbf{M}\ddot{\mathbf{q}}_{2} + \frac{\partial \mathbf{g}}{\partial \mathbf{q}_{2}^{T}} \mathbf{q}_{\lambda} = \mathbf{f}_{2}(\mathbf{q}_{2}, \dot{\mathbf{q}}_{2}, t)$$
 (8.2)

$$\dot{\mathbf{q}}_1 + \frac{\partial \mathbf{g}}{\partial \mathbf{q}_1^{\mathrm{T}}} \mathbf{q}_{\lambda} = \mathbf{f}_1(\mathbf{q}_1, t) \tag{8.3}$$

$$\mathbf{g}(\mathbf{q}_2, \dot{\mathbf{q}}_2, \mathbf{q}_1, \mathbf{q}_{\lambda}, t) = 0 \tag{8.4}$$

Note that the term  $\frac{\partial \mathbf{g}}{\partial q_1} \mathbf{q}_{\lambda}$  is not yet implemented, such that algebraic equations may not yet depend on 1<sup>st</sup> order differential equations coordinates.

It is important to note, that for linear mechanical systems,  $f_2$  becomes

$$\mathbf{f}_{2}^{lin} = \mathbf{f}^{a} - \mathbf{K}\mathbf{q}_{2} - \mathbf{D}\dot{\mathbf{q}}_{1} \tag{8.5}$$

in which  $f^a$  represents applied forces and K and D become part of the system Jacobian for time integration.

#### 8.4 Newmark method

The Newmark method obtains two parameters  $\beta$  and  $\gamma$ . The main ideas are

- Interpolate the displacements and the velocities linearly using the accelerations of the beginning of the time step (subindex '0') and the end of the time step (subindex 'T').
- Solve the system equations at the end of the time step for the unknown accelerations as well as for 1<sup>st</sup> order differential equations and algebraic equations coordinates.

We abbreviate the unknown accelerations by  $\ddot{\mathbf{q}} = \mathbf{a}$  and the unknown velocities  $\dot{\mathbf{q}} = \mathbf{v}$ . Thus, the equations at the end of the time step read (bring all terms to LHS):

$$\mathbf{f}_{2}^{\text{Newmark}} = \mathbf{M} \mathbf{a}_{2}^{T} + \frac{\partial \mathbf{g}}{\partial \mathbf{q}_{2}^{T}} \mathbf{q}_{\lambda}^{T} - \mathbf{f}_{2}(\mathbf{q}_{2}^{T}, \dot{\mathbf{q}}_{2}^{T}, t) = 0$$
(8.6)

$$\mathbf{f}_{1}^{\text{Newmark}} = \mathbf{v}_{1}^{T} + \frac{\partial \mathbf{g}}{\partial \mathbf{q}_{1}^{T}} \mathbf{q}_{\lambda}^{T} - \mathbf{f}_{1}(\mathbf{q}_{1}^{T}, t) = 0$$
(8.7)

$$\mathbf{f}_{\lambda}^{\text{Newmark}} = \mathbf{g}(\mathbf{q}_{2}^{T}, \dot{\mathbf{q}}_{2}^{T}, \mathbf{q}_{1}^{T}, \mathbf{q}_{\lambda}^{T}, t) = 0$$
(8.8)

Within Eq. (8.6), the 2<sup>nd</sup> order differential equations displacements and velocities and for 1<sup>st</sup> order differential equations coordinates are given by

$$\mathbf{q}_{2}^{T} = \mathbf{q}_{2}^{0} + h\dot{\mathbf{q}}_{2}^{0} + h^{2}(\frac{1}{2} - \beta)\mathbf{a}_{2}^{0} + h^{2}\beta\mathbf{a}_{2}^{T}$$

$$\dot{\mathbf{q}}_{2}^{T} = \dot{\mathbf{q}}_{2}^{0} + h(1 - \gamma)\mathbf{a}_{2}^{0} + h\gamma\mathbf{a}_{2}^{T}$$

$$\mathbf{q}_{1}^{T} = \mathbf{q}_{1}^{0} + h(1 - \gamma)\mathbf{v}_{1}^{0} + h\gamma\mathbf{v}_{1}^{T}$$
(8.9)

The unknowns for the Newton method are

$$\mathbf{q}^{\text{Newton}} = \begin{bmatrix} \mathbf{a}_2^T \\ \mathbf{v}_1^T \\ \mathbf{q}_{\Lambda}^T \end{bmatrix}$$
 (8.10)

For the Newton method, we need to compute an update for the unknowns Eq. (8.10), using the known residual  $\mathbf{r}_{i-1}$  and the inverse of the Jacobian  $\mathbf{J}_{i-1}$  of step i-1,

$$\mathbf{q}_{i}^{\text{Newton}} = \mathbf{q}_{i-1}^{\text{Newton}} - \mathbf{J}^{-1} \left( \mathbf{q}_{i-1}^{\text{Newton}} \right) \mathbf{r} \left( \mathbf{q}_{i-1}^{\text{Newton}} \right)$$
(8.11)

The Jacobian has the following  $3 \times 3$  structure,

$$\mathbf{J} = \begin{bmatrix} \mathbf{J}_{22} & \mathbf{J}_{21} & \mathbf{J}_{2\lambda} \\ \mathbf{J}_{12} & \mathbf{J}_{11} & \mathbf{J}_{1\lambda} \\ \mathbf{J}_{\lambda 2} & \mathbf{J}_{\lambda 1} & \mathbf{J}_{\lambda \lambda} \end{bmatrix}$$
(8.12)

Note that currently, all terms related to '1' are not implemented. The other terms are only evaluated in the specific jacobian computation, if according flags are set in GetAvailableJacobian(). Otherwise, the constraint needs to be implemented as object which can employ all kinds of coordinates, which do not depend on coordinates of markers.

The available Jacobians need to be rewritten in terms of the Newton unknowns (8.10), and thus read

$$J_{22} = \frac{\partial \mathbf{f}_{2}^{\text{Newmark}}}{\partial \mathbf{a}_{2}^{\text{T}}} = \frac{\partial \mathbf{f}_{2}^{\text{Newmark}}}{\partial \mathbf{q}_{2}^{\text{T}}} \frac{\mathbf{q}_{2}}{\mathbf{a}_{2}^{\text{T}}} + \frac{\partial \mathbf{f}_{2}^{\text{Newmark}}}{\partial \dot{\mathbf{q}}_{2}^{\text{T}}} \frac{\dot{\mathbf{q}}_{2}}{\mathbf{a}_{2}^{\text{T}}} = h^{2}\beta \mathbf{K} + h\gamma \mathbf{D}$$

$$J_{2\lambda} = \frac{\partial \mathbf{f}_{2}^{\text{Newmark}}}{\partial \mathbf{q}_{\lambda}^{\text{T}}} = \frac{\partial \mathbf{g}}{\partial \mathbf{q}_{2}^{\text{T}}}$$

$$J_{\lambda 2} = \frac{\partial \mathbf{f}_{\lambda}^{\text{Newmark}}}{\partial \mathbf{a}_{2}^{\text{T}}} = \frac{\partial \mathbf{g}}{\partial \mathbf{a}_{2}^{\text{T}}} = \frac{\partial \mathbf{g}}{\partial \mathbf{q}_{2}^{\text{T}}} \frac{\mathbf{q}_{2}}{\mathbf{q}_{2}^{\text{T}}} + \frac{\partial \mathbf{g}}{\partial \dot{\mathbf{q}}_{2}^{\text{T}}} \frac{\dot{\mathbf{q}}_{2}}{\mathbf{a}_{2}^{\text{T}}} = h^{2}\beta \frac{\partial \mathbf{g}}{\partial \mathbf{q}_{2}^{\text{T}}} + h\gamma \frac{\partial \mathbf{g}}{\partial \dot{\mathbf{q}}_{2}^{\text{T}}}$$

$$J_{\lambda \lambda} = \frac{\partial \mathbf{f}_{\lambda}^{\text{Newmark}}}{\partial \mathbf{q}_{\lambda}^{\text{T}}} = \frac{\partial \mathbf{g}}{\partial \mathbf{q}_{\lambda}^{\text{T}}}$$

$$(8.13)$$

Note that the derivative  $\frac{\mathbf{q}_2}{\mathbf{a}_2^T}$  follows from the Newmark interpolation (8.9) using the relation between  $\mathbf{q}_2^T$  and  $\mathbf{a}_2^T$ . The tangent stiffness matrix  $\mathbf{K}$  must also include derivatives of applied forces  $\mathbf{f}^a$ , which is currently not implemented. Furthermore, the Jacobian is not symmetric, which could be obtained by according scaling.

Once an update  $\mathbf{q}_i^{\text{Newton}}$  has been computed, the interpolation formulas (8.9) need to be evaluated before the next residual and Jacobian can be computed.

# **Chapter 9**

# References

coming soon!

## Chapter 10

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