

HW10 Report

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Environment

Visual studio code, Windows 10

Language

c++11

Compile & Execute

1. In terminal, type in `cd /[file's name]` to change direction to file directory.
2. After successful compilation, type in `./hw10 ./[test input file's name]` command.
3. The answer will be output on the screen.

Description

Error query table

▼ First, I calculate error value for different combination of red intensities in terms of different k. In order to find the closet pixels for each red intensity combination, I use a for loop to test every pixel from 0 to 255.

```
//find the closet pixels for each red intensity combination.
for(int l = 0; l < 256; l++){
    for(int i = 1; i <= d; i++){
        long long int ans = 0;
        for(int j = i; j <= d; j++){
            ans += (r[j]-l) * (r[j]-l) * p[j]; //sum of squared errors
            f[i][j] = min(f[i][j], ans); //Error value query set for each combination of reds.
        }
    }
}
```

DP

$$error(i, j) = \min(error(i, j), error(l, j - 1) + f(l + 1, i))$$

$i \in [1, d], j \in [1, k], \text{ and } l \in [1, i]$
 f is error query table

```
dp[0][0] = 0;

//assign error value for each blank

for(*int* i = 1; i <= d; i++){
    for(*int* j = 1; j <= k; j++){
        for(*int* l = 0; l < i; l++){
            dp[i][j] = min(dp[i][j], dp[l][j-1] + f[l+1][i]);
        }
    }
}
```

Complexity

$$O(d^2 * k)$$

▼ In the preprocessed error query table, the complexity is $O(256 * d * d)$. In the main part of DP, the complexity is $O(d * k * d)$. Hence, the total complexity is $O(d^2 * k)$.

Reference

2017年world final Problem F Posterize (DP)