

BST 140.651 Final Exam

Notes:

- You may use your one 8.5 by 11 formula sheet.
- Please use only the basic mathematical functions on your calculator.
- Show your work on all questions. Simple “yes” or “no” answers will be graded as if blank.
- Please be neat and write legibly. Use the back of the pages if necessary.
- There are three pages containing 8 questions.
- Good luck!

signature and **printed name**

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4. Let X be binomial with success probability p_1 and n_1 trials and Y be an independent binomial with success probability p_2 and n_2 trials. Let $\hat{p}_1 = X/n_1$ and $\hat{p}_2 = Y/n_2$ be the associated sample proportions. What would be an estimate for the standard error for $\hat{p}_1 - \hat{p}_2$? To have consistent notation with the next problem, label this value $\hat{SE}_{\hat{p}_1 - \hat{p}_2}$.

5. Consider the previous problem. Suppose that it is known that

$$Z = \frac{\hat{p}_1 - \hat{p}_2 - (p_1 - p_2)}{\hat{SE}_{\hat{p}_1 - \hat{p}_2}}$$

is standard normally distributed for large n_1 and n_2 . Use this fact to derive a 95% confidence interval for $p_1 - p_2$. (Do not just give an answer, show some steps.)

6. You are in desperate need to simulate standard normal random variables yet do not have a computer available. You do, however, have ten standard six sided dice. Knowing that the mean of a single die roll is 3.5 and the standard deviation is 1.71, describe how you could use the dice to approximately simulate standard normal random variables. (Be precise.)

7. Calculate *and interpret* a 95% confidence interval for the change in BMI for the treated group; assume normality.
8. Does the change in BMI over the two year period appear to differ between the treated and placebo groups? Create the relevant 95% confidence interval *and interpret*. Assume normality and a common variance.