

1.

$$\frac{\sin 30^\circ + \cos 60^\circ}{\tan 45^\circ} = \frac{\frac{1}{2} + \frac{1}{2}}{1} = \frac{1}{1} = 1$$

2.

$$\frac{(\sin 45^\circ)^{-1} + \tan 60^\circ}{\cos 30^\circ} = \frac{\left(\frac{\sqrt{2}}{2}\right)^{-1} + \sqrt{3}}{\frac{\sqrt{3}}{2}} = \frac{\frac{1}{\frac{\sqrt{2}}{2}} + \sqrt{3}}{\frac{\sqrt{3}}{2}} = \frac{\frac{2}{\sqrt{2}} + \sqrt{3}}{\frac{\sqrt{3}}{2}} = \frac{\frac{2}{\sqrt{2}} + \frac{\sqrt{3}}{1}}{\frac{\sqrt{3}}{2}} = \frac{\frac{2 + \sqrt{6}}{\sqrt{2}}}{\frac{\sqrt{3}}{2}} = \frac{2 + \sqrt{6}}{\sqrt{2}} \times \frac{\sqrt{6}}{\sqrt{6}} = \frac{4 + 2\sqrt{6}}{\sqrt{6}} = \frac{4\sqrt{6} + 2 \times 6}{6} = \frac{4\sqrt{6} + 12}{6} = \frac{2\sqrt{6} + 6}{3}$$

3.

$$2 \tan 60^\circ \times \tan 30^\circ = (2) \times (\sqrt{3}) \times \left(\frac{\sqrt{3}}{3}\right) = \left(\frac{2}{1}\right) \times \left(\frac{\sqrt{3}}{1}\right) \times \left(\frac{\sqrt{3}}{3}\right) = \frac{2\sqrt{9}}{3} = \frac{2 \times 3}{3} = \frac{6}{3} = 2$$

4.

$$\sqrt{2} \cos 60^\circ \times \cot 45^\circ = (\sqrt{2}) \times \left(\frac{1}{2}\right) \times (1) = \frac{\sqrt{2}}{1} \times \frac{1}{2} \times \frac{1}{1} = \frac{\sqrt{2}}{2}$$

5.

$$\frac{3 \tan 30^\circ}{\sec 60^\circ} = \frac{(3) \times \left(\frac{\sqrt{3}}{3}\right)}{\frac{\sqrt{3}}{2}} = \frac{3 \times \frac{\sqrt{3}}{3}}{\frac{\sqrt{3}}{2}} = \frac{\frac{3\sqrt{3}}{3}}{\frac{\sqrt{3}}{2}} = \frac{6\sqrt{3}}{3\sqrt{3}} = 2$$

6.

$$5 \sin 30^\circ - 3\sqrt{2} \sin 45^\circ + \frac{1}{4} \tan 45^\circ = \left(\frac{5}{1}\right) \times \left(\frac{1}{2}\right) - \left(\frac{3\sqrt{2}}{1}\right) \times \left(\frac{\sqrt{2}}{2}\right) + \left(\frac{1}{4}\right) \times \left(\frac{1}{1}\right) = \frac{5}{2} - \frac{3\sqrt{4}}{2} + \frac{1}{4} = \frac{5}{2} - \frac{3 \times 2}{2} + \frac{1}{4} = \frac{5}{2} - \frac{6}{2} + \frac{1}{4} = \frac{10 - 12 + 1}{4} = -\frac{1}{4}$$

7.

$$(\cos 30^\circ - \cos 45^\circ)(\cos 30^\circ + \cos 45^\circ) = \left(\frac{\sqrt{3}}{2} - \frac{\sqrt{2}}{2}\right) \left(\frac{\sqrt{3}}{2} + \frac{\sqrt{2}}{2}\right) = \frac{\sqrt{9}}{4} + \frac{\sqrt{6}}{4} - \frac{\sqrt{6}}{4} - \frac{\sqrt{4}}{4} = \frac{3}{4} - \frac{2}{4} = \frac{1}{4}$$

8.

$$\frac{\cos 45^\circ + \sin 45^\circ}{\csc 45^\circ} = \frac{\frac{\sqrt{2}}{2} + \frac{\sqrt{2}}{2}}{\frac{\sqrt{2}}{1}} = \frac{\frac{2\sqrt{2}}{2}}{\frac{\sqrt{2}}{1}} = \frac{2\sqrt{2}}{2\sqrt{2}} = 1$$

9.

$$\frac{\cos 30^\circ}{\sin 60^\circ + \cos 45^\circ} = \frac{\frac{\sqrt{3}}{2}}{\frac{\sqrt{3}}{2} + \frac{\sqrt{2}}{2}} = \frac{\frac{\sqrt{3}}{2}}{\frac{2\sqrt{3} + 2\sqrt{2}}{4}} = \frac{4\sqrt{3}}{4\sqrt{3} + 4\sqrt{2}} = \left(\frac{\sqrt{3}}{\sqrt{3} + \sqrt{2}}\right) \left(\frac{\sqrt{3} - \sqrt{2}}{\sqrt{3} - \sqrt{2}}\right) = \frac{\sqrt{9} - \sqrt{6}}{\sqrt{9} - \sqrt{4}} = \frac{3 - \sqrt{6}}{3 - 2} = 3 - \sqrt{6}$$

10.

$$\frac{2 \sin 60^\circ}{\cot 30^\circ - 4 \sin 45^\circ} = \frac{\left(\frac{2}{1}\right) \left(\frac{\sqrt{3}}{2}\right)}{\left(\frac{\sqrt{3}}{1}\right) - \left(\frac{4}{1}\right) \left(\frac{\sqrt{2}}{2}\right)} = \frac{\frac{2\sqrt{3}}{2}}{\left(\frac{\sqrt{3}}{1}\right) - \left(\frac{4\sqrt{2}}{2}\right)} = \frac{\frac{2\sqrt{3}}{2}}{\frac{2\sqrt{3} - 4\sqrt{2}}{2}} = \left(\frac{2\sqrt{3}}{2\sqrt{3} - 4\sqrt{2}}\right) \left(\frac{\sqrt{3} + \sqrt{2}}{\sqrt{3} + \sqrt{2}}\right) = \frac{2\sqrt{9} + 2\sqrt{6}}{2 \times 3 - 4 \times 2} = \frac{2 \times 3 + 2\sqrt{6}}{6 - 8} = \frac{6 + 2\sqrt{6}}{-2} = \frac{3 + \sqrt{6}}{-1} = -3 - \sqrt{6}$$

1.

$$\sin 30^\circ \times \cos 60^\circ + \cos 30^\circ \times \sin 60^\circ = \left(\frac{1}{2}\right) \times \left(\frac{1}{2}\right) + \left(\frac{\sqrt{3}}{2}\right) \times \left(\frac{\sqrt{3}}{2}\right) = \frac{1}{4} + \frac{\sqrt{9}}{4} = \frac{1}{4} + \frac{3}{4} = \frac{4}{4} = 1$$

2.

$$\cos 30^\circ \times \cos 60^\circ - \operatorname{sen} 30^\circ \times \operatorname{sen} 60^\circ = \left(\frac{\sqrt{3}}{2}\right) \times \left(\frac{1}{2}\right) - \left(\frac{1}{2}\right) \times \left(\frac{\sqrt{3}}{2}\right) = \frac{\sqrt{3}}{4} - \frac{\sqrt{3}}{4} = 0$$

3.

$$\frac{\tan 60^\circ - \tan 30^\circ}{1 + \tan 60^\circ \times \tan 30^\circ} = \frac{\frac{\sqrt{3}}{1} - \frac{\sqrt{3}}{3}}{1 + \left(\frac{\sqrt{3}}{1}\right)\left(\frac{\sqrt{3}}{3}\right)} = \frac{\frac{3\sqrt{3} - \sqrt{3}}{3}}{\frac{1}{1} + \frac{\sqrt{9}}{3}} = \frac{\frac{2\sqrt{3}}{3}}{\frac{3+3}{3}} = \frac{2\sqrt{3}}{6} = \frac{\sqrt{3}}{3}$$

4.

$$\frac{1}{\operatorname{sen}^2 30^\circ} + \frac{1}{\cos^2 60^\circ} = \frac{1}{\left(\frac{1}{2}\right)^2} + \frac{1}{\left(\frac{1}{2}\right)^2} = \frac{1}{\frac{1}{4}} + \frac{1}{\frac{1}{4}} = 4 + 4 = 8$$

5.

$$\frac{\cos 30^\circ}{\tan 45^\circ} + \frac{\operatorname{sen} 30^\circ}{\cos 60^\circ} = \frac{\frac{\sqrt{3}}{2}}{\frac{1}{1}} + \frac{\frac{1}{2}}{\frac{1}{2}} = \frac{\sqrt{3}}{2} + \frac{2}{2} = \frac{2\sqrt{3} + 4}{4} = \frac{\sqrt{3} + 2}{2}$$

6.

$$\begin{aligned} \frac{1}{\cos 30^\circ} \times \frac{1}{\tan 60^\circ} - \frac{1}{\operatorname{sen} 45^\circ} &= \frac{\frac{1}{\frac{1}{\sqrt{3}}}}{\frac{2}{2}} \times \frac{1}{\frac{1}{\sqrt{3}}} - \frac{\frac{1}{\frac{1}{\sqrt{2}}}}{\frac{2}{2}} = \frac{2}{\sqrt{3}} \times \frac{1}{\sqrt{3}} - \frac{2}{\sqrt{2}} = \frac{2}{\sqrt{9}} - \frac{2}{\sqrt{2}} = \frac{2}{3} - \frac{2}{\sqrt{2}} = \frac{2\sqrt{2} - 6}{3\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} = \frac{2\sqrt{4} - 6\sqrt{2}}{3\sqrt{4}} = \frac{2 \times 2 - 6\sqrt{2}}{3 \times 2} \\ &= \frac{4 - 6\sqrt{2}}{6} = \frac{2 - 3\sqrt{2}}{3} \end{aligned}$$

7.

$$\frac{\operatorname{sen} 60^\circ - \cos^2 45^\circ}{\cos 60^\circ} = \frac{\frac{\sqrt{3}}{2} - \left(\frac{\sqrt{2}}{2}\right)^2}{\frac{1}{2}} = \frac{\frac{\sqrt{3}}{2} - \frac{2}{4}}{\frac{1}{2}} = \frac{\frac{4\sqrt{3} - 4}{8}}{\frac{1}{2}} = \frac{8\sqrt{3} - 8}{8} = \sqrt{3} - 1$$

8.

$$\operatorname{sen} 30^\circ \times \cos 45^\circ - \tan 60^\circ = \left(\frac{1}{2}\right) \times \left(\frac{\sqrt{2}}{2}\right) - \frac{\sqrt{3}}{1} = \frac{\sqrt{2}}{4} - \frac{\sqrt{3}}{1} = \frac{\sqrt{2} - 4\sqrt{3}}{4}$$

9.

$$\begin{aligned} (\operatorname{sen} 45^\circ)^{-1} \times \operatorname{sen} 60^\circ - (\cot 30^\circ)^{-1} &= \left(\frac{\sqrt{2}}{2}\right)^{-1} \times \frac{\sqrt{3}}{2} - (\sqrt{3})^{-1} = \frac{1}{\frac{\sqrt{2}}{2}} \times \frac{\sqrt{3}}{2} - \frac{1}{\sqrt{3}} = \frac{\frac{1}{1}}{\frac{\sqrt{2}}{2}} \times \frac{\sqrt{3}}{2} - \frac{1}{\sqrt{3}} = \frac{2}{\sqrt{2}} \times \frac{\sqrt{3}}{2} - \frac{1}{\sqrt{3}} = \frac{2\sqrt{3}}{2\sqrt{2}} - \frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{\sqrt{2}} - \frac{1}{\sqrt{3}} \\ &= \frac{\sqrt{9} - \sqrt{2}}{\sqrt{6}} = \frac{3 - \sqrt{2}}{\sqrt{6}} \times \frac{\sqrt{6}}{\sqrt{6}} = \frac{3\sqrt{6} - \sqrt{12}}{\sqrt{36}} = \frac{3\sqrt{6} - 2\sqrt{3}}{6} \end{aligned}$$

10.

$$\begin{aligned} 2(\operatorname{sen} 30^\circ - \operatorname{sen} 45^\circ)^2 - 1 &= 2\left(\frac{1}{2} + \frac{\sqrt{2}}{2}\right)^2 - 1 = 2\left(\frac{1}{4} + \frac{\sqrt{2}}{2} + \frac{2}{4}\right) - 1 = 2\left(\frac{3}{4} + \frac{\sqrt{2}}{2}\right) - 1 = \frac{2}{1} \times \left(\frac{3}{4} + \frac{\sqrt{2}}{2}\right) - 1 = \frac{6}{4} + \frac{2\sqrt{2}}{2} - 1 = \frac{3}{2} + \frac{\sqrt{2}}{1} - \frac{1}{1} \\ &= \frac{3 + 2\sqrt{2} - 2}{2} = \frac{1 + 2\sqrt{2}}{2} \end{aligned}$$

3

1.

$$\frac{\tan^2 30^\circ + \operatorname{sen}^2 30^\circ}{(\operatorname{sen} 45^\circ)^{-2} \div (\operatorname{sen} 30^\circ)^{-2}} = \frac{\left(\frac{\sqrt{3}}{3}\right)^2 + \left(\frac{1}{2}\right)^2}{\frac{\frac{1}{\left(\frac{\sqrt{2}}{2}\right)^2} \div \frac{1}{\left(\frac{1}{2}\right)^2}}{\frac{\frac{3}{9} + \frac{1}{4}}{\frac{\frac{1}{2} \div \frac{1}{4}}{\frac{12+9}{36}} = \frac{21}{36} = \frac{21}{36} = \frac{84}{72} = \frac{7}{6}}}$$

2.

$$\begin{aligned} \frac{\operatorname{sen} 60^\circ \times (\cos 45^\circ)^{-1} - \tan 30^\circ}{\tan 45^\circ} &= \frac{\frac{\sqrt{3}}{2} \times \frac{1}{\frac{\sqrt{2}}{2}} - \frac{\sqrt{3}}{3}}{1} = \frac{\frac{\sqrt{3}}{2} \times \frac{2}{\sqrt{2}} - \frac{\sqrt{3}}{3}}{1} = \frac{2\sqrt{3}}{2\sqrt{2}} - \frac{\sqrt{3}}{3} = \frac{\sqrt{3}}{\sqrt{2}} - \frac{\sqrt{3}}{3} = \frac{3\sqrt{3} - \sqrt{6}}{3\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} = \frac{3\sqrt{6} - \sqrt{12}}{3\sqrt{4}} = \frac{3\sqrt{6} - 2\sqrt{3}}{3 \times 2} \\ &= \frac{3\sqrt{6} - 2\sqrt{3}}{6} \end{aligned}$$

3.

$$2 \operatorname{sen} 30^\circ - \cos 30^\circ \times (\cos 45^\circ)^{-1} = \left(\frac{2}{1}\right) \times \left(\frac{1}{2}\right) - \frac{\sqrt{3}}{2} \times \frac{1}{\frac{\sqrt{2}}{2}} = \frac{2}{2} - \frac{\sqrt{3}}{2} \times \frac{2}{\sqrt{2}} = \frac{1}{1} - \frac{2\sqrt{3}}{2\sqrt{2}} = \frac{1}{1} - \frac{\sqrt{3}}{\sqrt{2}} = \frac{\sqrt{2} - \sqrt{3}}{\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sqrt{4} - \sqrt{6}}{\sqrt{4}} = \frac{2 - \sqrt{6}}{2}$$

4.

$$\begin{aligned} \tan 60^\circ - (\operatorname{sen} 60^\circ \times \cos 45^\circ)^{-1} &= \frac{\sqrt{3}}{1} - \left(\frac{\sqrt{3}}{2} \times \frac{\sqrt{2}}{2}\right)^{-1} = \frac{\sqrt{3}}{1} - \left(\frac{\sqrt{6}}{4}\right)^{-1} = \frac{\sqrt{3}}{1} - \frac{1}{\frac{\sqrt{6}}{4}} = \frac{\sqrt{3}}{1} - \frac{4}{\sqrt{6}} = \frac{\sqrt{3}}{1} - \frac{4}{\sqrt{6}} = \frac{\sqrt{18} - 4}{\sqrt{6}} = \frac{3\sqrt{2} - 4}{\sqrt{6}} \times \frac{\sqrt{6}}{\sqrt{6}} \\ &= \frac{3\sqrt{12} - 4\sqrt{6}}{\sqrt{36}} = \frac{3 \times 2\sqrt{3} - 4\sqrt{6}}{6} = \frac{6\sqrt{3} - 4\sqrt{6}}{6} = \frac{3\sqrt{3} - 2\sqrt{6}}{3} \end{aligned}$$

5.

$$\frac{\sec^3 45^\circ - \cot^2 30^\circ}{(\cot 60^\circ)^{-2}} = \frac{(\sqrt{2})^3 - (\sqrt{3})^2}{\left(\frac{\sqrt{3}}{3}\right)^2} = \frac{\sqrt{8} - 3}{\frac{1}{\frac{3}{9}}} = \frac{2\sqrt{2} - 3}{\frac{9}{3}} = \frac{2\sqrt{2} - 3}{3}$$

6.

$$\frac{2 \operatorname{sen} 30^\circ \times \cos 30^\circ}{\csc 60^\circ + \sec 30^\circ} = \frac{\left(\frac{2}{1}\right) \times \left(\frac{1}{2}\right) \times \left(\frac{\sqrt{3}}{2}\right)}{\frac{2\sqrt{3}}{3} + \frac{2\sqrt{3}}{3}} = \frac{\frac{2\sqrt{3}}{4}}{\frac{6\sqrt{3} + 6\sqrt{3}}{9}} = \frac{18\sqrt{3}}{24\sqrt{3} + 24\sqrt{3}} = \frac{18\sqrt{3}}{48\sqrt{3}} = \frac{18}{48} = \frac{3}{8}$$

7.

$$\frac{\operatorname{sen}^2 30^\circ + \cos^2 30^\circ + 1}{\sec 45^\circ \times \tan 30^\circ} = \frac{\left(\frac{1}{2}\right)^2 + \left(\frac{\sqrt{3}}{2}\right)^2 + 1}{\left(\frac{\sqrt{2}}{1}\right) \times \left(\frac{\sqrt{3}}{3}\right)} = \frac{\frac{1}{4} + \frac{3}{4} + 1}{\frac{\sqrt{6}}{3}} = \frac{\frac{4}{4} + 1}{\frac{\sqrt{6}}{3}} = \frac{1 + 1}{\frac{\sqrt{6}}{3}} = \frac{2}{\frac{\sqrt{6}}{3}} = \frac{2}{\frac{\sqrt{6}}{3}} = \frac{6}{\sqrt{6}} \times \frac{\sqrt{6}}{\sqrt{6}} = \frac{6\sqrt{6}}{\sqrt{36}} = \frac{6\sqrt{6}}{6} = \sqrt{6}$$

8.

$$\begin{aligned} \frac{\sqrt{3} \operatorname{sen} 45^\circ + \sqrt{2} \cos 30^\circ}{\tan 60^\circ} &= \frac{\left(\frac{\sqrt{3}}{1}\right) \left(\frac{\sqrt{2}}{2}\right) + \left(\frac{\sqrt{2}}{1}\right) \left(\frac{\sqrt{3}}{2}\right)}{\frac{\sqrt{3}}{1}} = \frac{\frac{\sqrt{6}}{2} + \frac{\sqrt{6}}{2}}{\frac{\sqrt{3}}{1}} = \frac{\frac{2\sqrt{6} + 2\sqrt{6}}{4}}{\frac{\sqrt{3}}{1}} = \frac{2\sqrt{6} + 2\sqrt{6}}{4\sqrt{3}} = \frac{4\sqrt{6}}{4\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = \frac{4\sqrt{18}}{4\sqrt{9}} = \frac{4 \times 3\sqrt{2}}{4 \times 3} = \frac{12\sqrt{2}}{12} \\ &= \sqrt{2} \end{aligned}$$

9.

$$\frac{\tan 60^\circ - \tan 30^\circ}{\tan 60^\circ \times \tan 30^\circ} = \frac{\frac{\sqrt{3}}{1} - \frac{\sqrt{3}}{3}}{\left(\frac{\sqrt{3}}{1}\right) \times \left(\frac{\sqrt{3}}{3}\right)} = \frac{\frac{3\sqrt{3} - \sqrt{3}}{3}}{\frac{\sqrt{9}}{3}} = \frac{\frac{3\sqrt{3} - \sqrt{3}}{3}}{\frac{3}{3}} = \frac{9\sqrt{3} - 3\sqrt{3}}{9} = \frac{3\sqrt{3} - \sqrt{3}}{3} = \frac{2\sqrt{3}}{3}$$

10.

$$\begin{aligned} \frac{\cot^3 45^\circ + \sec^2 30^\circ \times \csc^2 60^\circ}{(\cot 60^\circ)^{-1}} &= \frac{(1)^3 + \left(\frac{2\sqrt{3}}{3}\right)^2 \times \left(\frac{2\sqrt{3}}{3}\right)^2}{\frac{1}{\frac{\sqrt{3}}{3}}} = \frac{1 + \frac{4 \times 3}{9} \times \frac{4 \times 3}{9}}{\frac{1}{\frac{\sqrt{3}}{3}}} = \frac{1 + \frac{12}{9} \times \frac{12}{9}}{\frac{3}{\sqrt{3}}} = \frac{1 + \frac{4}{3} \times \frac{4}{3}}{\frac{3}{\sqrt{3}}} = \frac{1 + \frac{16}{9}}{\frac{3}{\sqrt{3}}} = \frac{\frac{9 + 16}{9}}{\frac{3}{\sqrt{3}}} = \frac{\frac{25}{9}}{\frac{3}{\sqrt{3}}} \\ &= \frac{25\sqrt{3}}{27} \end{aligned}$$