

$$M = \begin{pmatrix} 0 & 1 & 2 & -2 \\ 1 & 0 & 1 & 1 \\ 1 & -1 & -1 & 3 \end{pmatrix} \quad \begin{pmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 2 & -2 \\ 1 & -1 & -1 & 3 \end{pmatrix} \quad \begin{pmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 2 & -2 \\ 0 & -1 & -2 & 2 \end{pmatrix} \quad \begin{pmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 2 & -2 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

$$P_{12}$$

$$L_3 \rightarrow L_3 - L_1$$

$$L_3 \rightarrow L_3 + L_2$$

$$E_{32}(1) \cdot E_{31}(-1) \cdot P_{12} \cdot M = U$$

$$P_{12} \cdot M = E_{31}(1) \cdot E_{32}(-1) \cdot U$$

$$P_{12} = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix} \quad E_{31}(1) = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{pmatrix} \quad E_{32}(-1) = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & -1 & 1 \end{pmatrix} \quad U = \begin{pmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 2 & -2 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$