

UNIVERSITÉ DE GENÈVE

METAHEURISTICS FOR OPTIMIZATION

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## TP 0: Stochastic processes

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## Simulation of a balanced dice

### Intro

During this exercise we will be simulating rolls of a  $N$ -face balanced dice. This means that the dice has  $N$  possible outcomes at each throw, all faces are equally likely with a probability of  $1/N$ .

For each roll we need to do the following three tasks:

- (1) compute a new random value  $r \in [0, 1)$ , done with `random()` function from `random` package
- (2) compute  $i = N * r$
- (3) compute  $\lfloor i \rfloor$ , done with `floor()` function from `math` package

After doing the three tasks, we get a value, that is the simulated roll.

The following graphic represents this phenomenon for  $N = 6, 15$

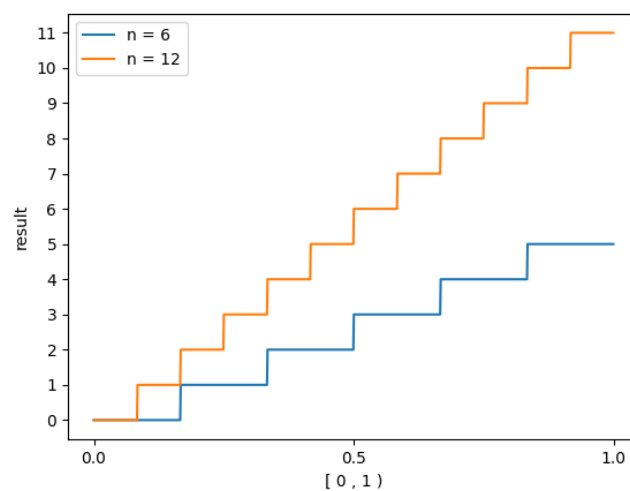


Figure 1: Values for  $N = \{6, 12\}$

In the image above we see this kind of step function, this is due to the fact that we use the function `.floor()`. The function that does this computation can be found in the `functions.py` file, and its signature is the following:

`balancedDice(N)`, where  $N$  corresponds to the number of faces in the balanced dice.

To check if the function works well we simply use it a large amount of times, or  $n$  times, if all faces are represented the same amount of times we know it is a good simulation. Obviously we need  $n$  to be large enough.

### Results

For our results we will run the script with  $N = 6$ , and  $n = \{100, 1000, 10000\}$ .

To 'read' the results, we will be computing the frequency of each face. Let's say the face represented by the value 1 was seen 20 times out of 100 rolls, then its frequency is  $20/100 = 0.2$ .

Face	1	2	3	4	5	6
Frequency: 100 rolls	0.18	0.21	0.15	0.18	0.15	0.13
Frequency: 1000 rolls	0.184	0.17	0.148	0.165	0.167	0.166
Frequency: 10000 rolls	0.1742	0.167	0.1671	0.1663	0.1641	0.1613

## Discrete Case