

UNIVERSITÉ DE GENÈVE

DATA SCIENCE

TP 1: Linear Algebra

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September 28, 2021



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DE GENÈVE**

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1 - Matrix

.1

When the number of equations, here 3, is strictly larger than the number of variables, here 2, the equations system has no solution.

.2

2 - The importance of the mathematical concept behind a code

.1

`def project_on_first(u, v)` receives two column vectors as an argument, and it projects v onto u , the projected vector is usually called v' . Visually, it means that v' and u are collinear. This also means that: $\exists \alpha$ tq. $v' * \alpha = u$.

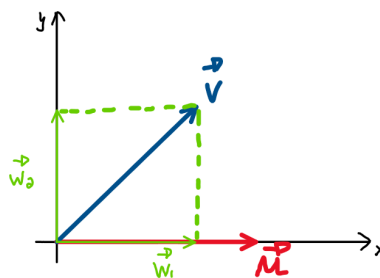


Figure 1: Projection of \vec{v} onto $\vec{u} = \vec{w}_1$

.2

`zip()` function takes as argument two python lists of same size. It then merges one value from the first list, with another value from the second list (same index), creating a list of tuples.

Let's see an example:

$$x = \text{zip}([1,2], [3,4]) \rightarrow x = [(1,3),(2,4)]$$

This means that the three last lines of code perform a simple dot operation between the two vectors given as argument to `zip()`.

$$\text{It can be rewritten as: } r = \text{np.dot}(u, v)$$

.3

Step 1: find the vector \vec{w}_2 orthogonal to \vec{u}

If we look at Figure 1, we can see that \vec{w}_1 is collinear to \vec{u} , and that \vec{w}_2 is orthogonal to \vec{u} . Moreover, $\vec{v} = \vec{w}_1 + \vec{w}_2$, which means we can easily compute \vec{w}_2 if we have already computed \vec{w}_1 .

$$\vec{w}_2 = \vec{v} - \vec{w}_1$$

Step 2: Make it so the orthogonal vector \vec{w}_2 has the same norm as vector \vec{u}

We must first compute $\|\vec{u}\|$ as well as $\|\vec{w}_2\|$.

By multiplying \vec{w}_2 by a given real value α we can find a new vector \vec{w}_2' that is collinear to \vec{w}_2 , but of different norm.

$$\alpha = \|\vec{u}\| / \|\vec{w}_2\|$$

`def orthogonal_norm_on_first(u, v)` is the function inside `some_script.py` that does this computation.

3 - Computing Eigenvalues, Eigenvectors, and Determinants

.1

.2

.3

4 - Computing Projection Onto a Line

.1

.2