

Computer Vision

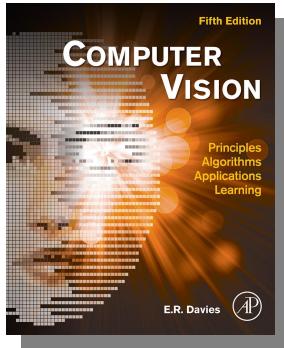
Corner detection

Prof. Dr. Gustavo T Laureano

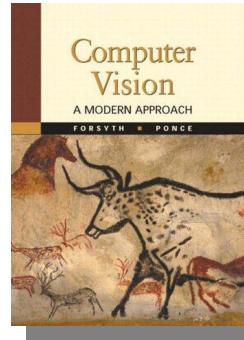


Course References

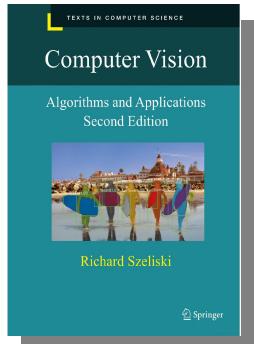
Many of the words of this course are taken from the books:



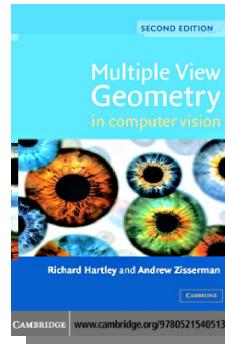
Computer & Machine Vision – Theory, Algorithms, Practicalities.
Fourth Edition, 2018. Elsevier Inc.
E. Roy Davies



Computer Vision – A modern Approach.
2003. Prentice Hall.
David Forsyth and Jean Ponce



Computer Vision – Algorithm and Applications.
2021. Springer.
Richard Szeliski



Multiple View Geometry.
Second Edition, 2012.
Cambridge.
Richard Hartley & Andrew Zisserman



Objectives

Corner detection

Harris/Plessey

Shi-Tomasi

Susan

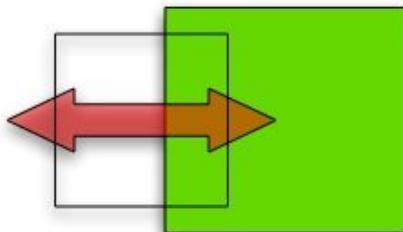
FAST

Blob Detection

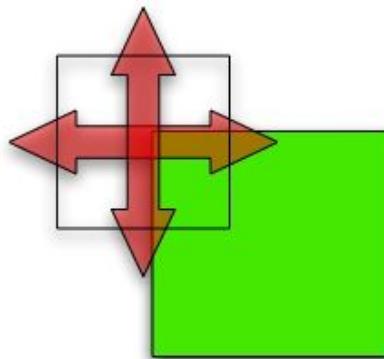


Low Level Features (Corners)

What is a corner?



Edge



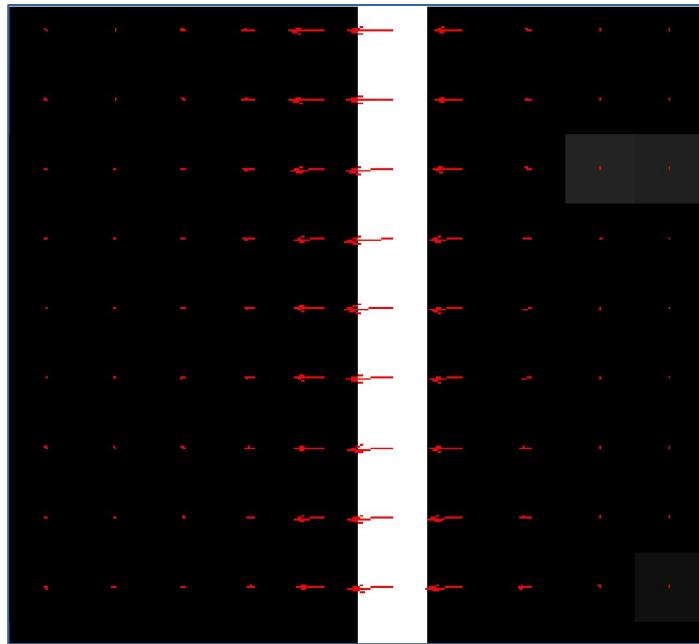
Corner



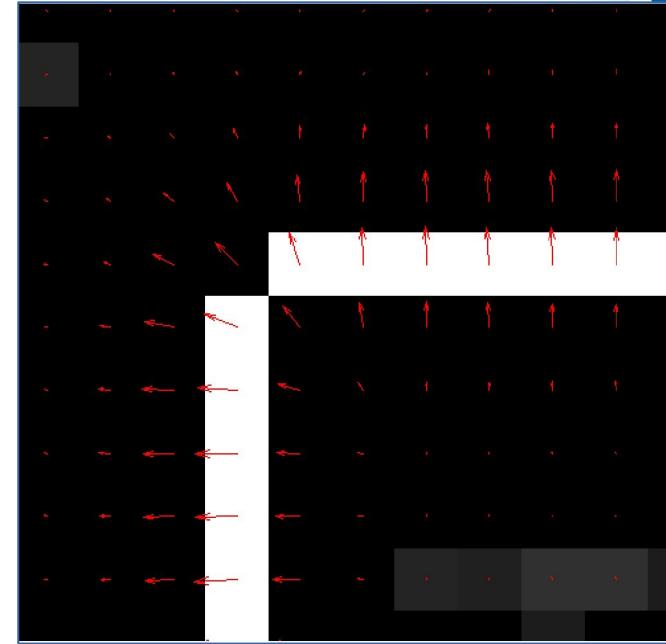
Low Level Features (Corners)

What is a corner?

Gradients:



Edge



Corner



Low Level Features (Corners)

Moravec Operator:

- Transformation described by Hans P. Moravec (1977) to identify interest points:
- Points with great intensity variation in your neighborhood
- Principle:

- Verifies intensity variation of shifted regions around central point

X-direction			
A1	A2 B1	A3 B2	B3
A4	A5 B4	A6 B5	B6
A7	A8 B7	A9 B8	B9

Y-direction			
B1	B2	B3	
A1 B4	A2 B5	A3 B6	
A4 B7	A5 B8	A6 B9	
A7	A8	A9	

H-direction			
	B1	B2	B3
A1	A2 B4	A3 B5	B6
A4	A5 B7	A6 B8	B9
A7	A8	A9	

Low Level Features (Corners)



- Moravec Operator:

X-direction

A1	A2 B1	A3 B2	B3
A4	A5 B4	A6 B5	B6
A7	A8 B7	A9 B8	B9

Horizontal Moravec Intensity Variation:

$$V_x = \sum_{i=1}^9 (A_i - B_i)^2 = \sum_{i=1}^9 (B_i - A_i)^2 \approx \sum_{i=1}^9 \left(\frac{\partial I_i}{\partial x} \right)^2$$

where: $\frac{\partial I_i}{\partial x} \equiv I_i \otimes (-1, 0, 1) \approx B_i - A_i$

H-direction

	B1	B2	B3
A1	A2 B4	A3 B5	B6
A4	A5 B7	A6 B8	B9
A7	A8	A9	

Diagonal Moravec Intensity Variation:

$$V_h = \sum_{i=1}^9 (A_i - B_i)^2 = \sum_{i=1}^9 (B_i - A_i)^2 \approx \sum_{i=1}^9 \left(\frac{\partial I_i}{\partial h} \right)^2$$

where: $\frac{\partial I_i}{\partial h} \equiv I_i \otimes \begin{bmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ -1 & 0 & 0 \end{bmatrix} \approx B_i - A_i$

B1	B2	B3
A1 B4	A2 B5	A3 B6
A4 B7	A5 B8	A6 B9
A7	A8	A9

Vertical Moravec Intensity Variation:

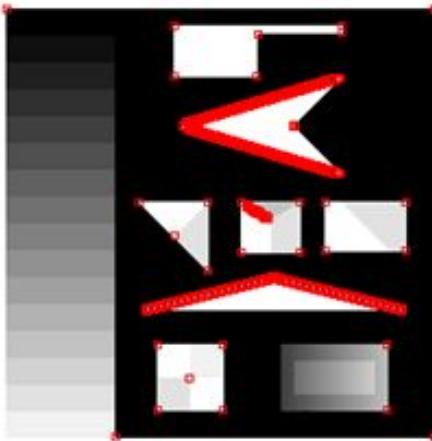
$$V_y = \sum_{i=1}^9 (A_i - B_i)^2 = \sum_{i=1}^9 (B_i - A_i)^2 \approx \sum_{i=1}^9 \left(\frac{\partial I_i}{\partial y} \right)^2$$

where: $\frac{\partial I_i}{\partial y} \equiv I_i \otimes (-1, 0, 1)^T \approx B_i - A_i$



Low Level Features (Corners)

- Moravec Operator:
 - Rotation sensitive



Original Image

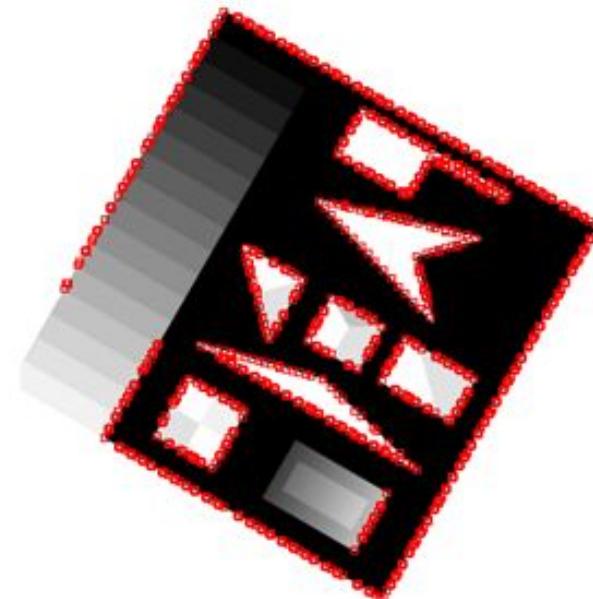


Image Rotated 30°

Low Level Features (Corners)

- Harris and Plessey Operator
 - Described **Chris Harris e Mike Stephens** in 1988.
 - Based on Moravec Operator.
 - Less sensitive to rotation.

Chris Harris and Mike Stephens
(1988).

A combined corner and edge detector.
Plessey Research Roke Manor.

$$I(x + \Delta_x, y + \Delta_y) = I(x, y) + \overbrace{\frac{\partial I(x, y)}{\partial x}}^{G_x} \cdot \Delta_x + \overbrace{\frac{\partial I(x, y)}{\partial y}}^{G_y} \cdot \Delta_y + HOT(x, y)$$

A COMBINED CORNER AND EDGE DETECTOR

Chris Harris & Mike Stephens
Plessey Research Roke Manor, United Kingdom.
© The Plessey Company plc, 1988

Combinance of corner and edge detection is prime requirement for 3D interpretation of image sequences using feature tracking. This paper describes a combined corner and edge detector which is able to detect both corner and edge features simultaneously. The combined detector is based on the Moravec operator and it is shown to perform well given consistency of selected inputs.

INTRODUCTION

The problem we are addressing is Alvey Project M0119 in the area of 3D interpretation of image sequences using feature tracking. The problem is to estimate the position and orientation of a camera moving in a 3D world, in which the viewed scenes will consist of man-made objects. In order to solve this problem it is necessary to obtain an understanding of several aspects, comprising motion analysis, scene analysis and feature extraction. The first two aspects have been addressed by the two frames from a sequence illustrated in Figure 1. The third aspect, feature extraction, is the subject of this paper. A computer vision system based upon motion analysis and scene analysis must be able to extract features from the images. These features must be stable enough to be tracked over time and also be able to withstand changes in the environment. The detection of the 3D analogues of these features can be considered.

To enable explicit tracking of image features to be performed, the features must be extracted in such a way that they are continuous like corners, or edge pixels (edges). For this reason, the combined corner and edge detector is proposed. It is hoped that this combined detector will provide the means, especially for small targets,

THE EDGE TRACKING PROBLEM

Matching between two images is a pixel-by-pixel basis works for static scenes, because of the known eye-ball camera position. However, because of the unknown eye-ball camera position, when the camera moves in a 3D world, the feature positions will change. To track features in a 3D world, it is necessary to estimate by solving for the motion beforehand, but we can estimate motion by tracking features in a 2D world. This is done by using the combined corner and edge detector, followed by KLT Filtering. This approach is instructive, especially when the features are edges. The KLT Filtering is used to estimate the motion of the features in the image sequence, and tracking these segments as the features.

Now, the necessary images we shall be considering are pairs of images from a sequence. We shall be using the combined corner and edge detector to extract features from each image fragment, and using these as our feature features will be extracted from the other image fragment. The images will be expected to change differently on each image of the sequence. As a result, the estimated motion of the features will be different, and the KLT Filtering will provide the motion, especially for small targets.



Figure 1. Pair of images from an outdoor sequence.

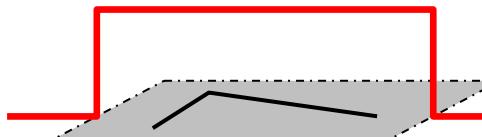
Low Level Features (Corners)

- Harris and Plessey Operator

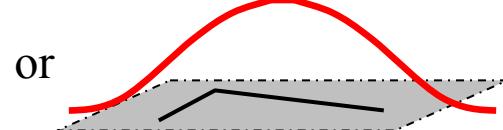
- Described **Chris Harris e Mike Stephens** in 1988.
- Based on Moravec Operator.
- Less sensitive to rotation.

$$c(x, y, \Delta x, \Delta y) = \sum_{(x,y) \in W} w(x, y) \cdot \left(\underbrace{I(x + \Delta x, y + \Delta y)}_{\text{Shifted Image}} - \underbrace{I(x, y)}_{\text{Original Image}} \right)^2$$

Window function $w(x, y) =$



1 in window, 0 outside



Gaussian

Chris Harris and Mike Stephens
(1988).

A combined corner and edge detector.
Plessey Research Roke Manor.

A COMBINED CORNER AND EDGE DETECTOR

Chris Harris & Mike Stephens
Plessey Research Roke Manor, United Kingdom.
© The Plessey Company plc, 1988

Corner detection, orientation and segmentation. However, the lack of connectivity of feature points is a major limitation of this approach. The combined corner and edge detector overcomes this by combining corner and edge detection, and it is shown to perform with good consistency on several images.

INTRODUCTION

The problem we are addressing is Alvey Project M0119 in the field of mobile robot navigation. The task is to build an autonomous 3D world, in which the viewed scenes will be interpreted and used to build up a 3D model of the environment. This model will be used to predict the effects of the robot's actions, to obtain an understanding of natural scenes, compute the best path through them, and to control the robot's motion. The problem is compounded by the fact that the scenes are unstructured, and the robot must move in an unpredictable environment, as shown by the two frames from a sequence illustrated in Figure 1.

The problem of tracking moving objects in such scenes can be solved using a computer vision system based upon motion analysis. The basic idea is to compare successive frames of the scene, and to track the features in the scene. The first step in this process is to extract features, and the second step is to track the features as they move.

To produce feature maps for each frame, we shall be considering two types of features. The first type of feature is the corner or junction point, and the second type is the edge point. The corner detector is a combined corner and edge detector, and the edge detector is a Kirsch Filter. This approach is instructive in that it shows how the two types of features can be combined. The edge detector also provides a useful way of segmenting the image into regions, and tracking these segments as the features move.

Now, the necessary images we shall be considering are pairs of frames from a sequence, and the features we shall be extracting are the features in one frame, and the features in the next frame, and using these to find feature matches will be the problem of feature matching.

It is this problem that we shall be addressing in this paper, and the results presented here are expected to differ significantly from those of previous work.

For example, the combined corner and edge detector provides a measure of the orientation of the features, and this measure can be used to provide the motion, especially with no images.



Figure 1. Pair of images from a radar sequence.

Low Level Features (Corners)



- Harris and Plessey Operator

- Described **Chris Harris e Mike Stephens** in 1988.
- Based on Moravec Operator.
- Less sensitive to rotation.

$$c(x, y, \Delta x, \Delta y) = \sum_{(x,y) \in W} w(x, y) \cdot \left(\underbrace{I(x + \Delta x, y + \Delta y)}_{\text{Shifted Image}} - \underbrace{I(x, y)}_{\text{Original Image}} \right)^2$$

- The shift function can be approximated by Taylor expansion.

$$\begin{aligned} I(x + \Delta x, y + \Delta y) &= I(x, y) + \overbrace{\frac{\partial I(x, y)}{\partial x}}^{G_x} \cdot \Delta x + \overbrace{\frac{\partial I(x, y)}{\partial y}}^{G_y} \cdot \Delta y + \overbrace{H.O.T.}^{\text{High order terms}} \\ &\approx I(x, y) + [G_x \quad G_y] \cdot \begin{bmatrix} \Delta x \\ \Delta y \end{bmatrix} \end{aligned}$$

Chris Harris and Mike Stephens
(1988).
A combined corner and edge detector.
Plessey Research Roke Manor.





Low Level Features (Corners)

- Harris and Plessey Operator

- Given: $c(x, y, \Delta x, \Delta y) = \sum_{(x,y) \in W} w(x, y) \cdot \left(\overbrace{I(x + \Delta x, y + \Delta y)}^{\text{Shifted Image}} - \overbrace{I(x, y)}^{\text{Original Image}} \right)^2$
- $I(x + \Delta x, y + \Delta y) \approx I(x, y) + [G_x \quad G_y] \cdot \begin{bmatrix} \Delta x \\ \Delta y \end{bmatrix}$
- Simplifying the equations, we have:

$$c(x, y, \Delta x, \Delta y) \approx \sum_{(x,y) \in W} w(x, y) \cdot \left(I(x, y) + [G_x \quad G_y] \cdot \begin{bmatrix} \Delta x \\ \Delta y \end{bmatrix} - I(x, y) \right)^2$$

$$c(x, y, \Delta x, \Delta y) \approx [\Delta x \quad \Delta y] \cdot \left(\sum_{(x,y) \in W} w(x, y) \cdot \begin{bmatrix} G_x^2 & G_x G_y \\ G_y G_x & G_y^2 \end{bmatrix} \right) \cdot \begin{bmatrix} \Delta x \\ \Delta y \end{bmatrix}$$

Low Level Features (Corners)

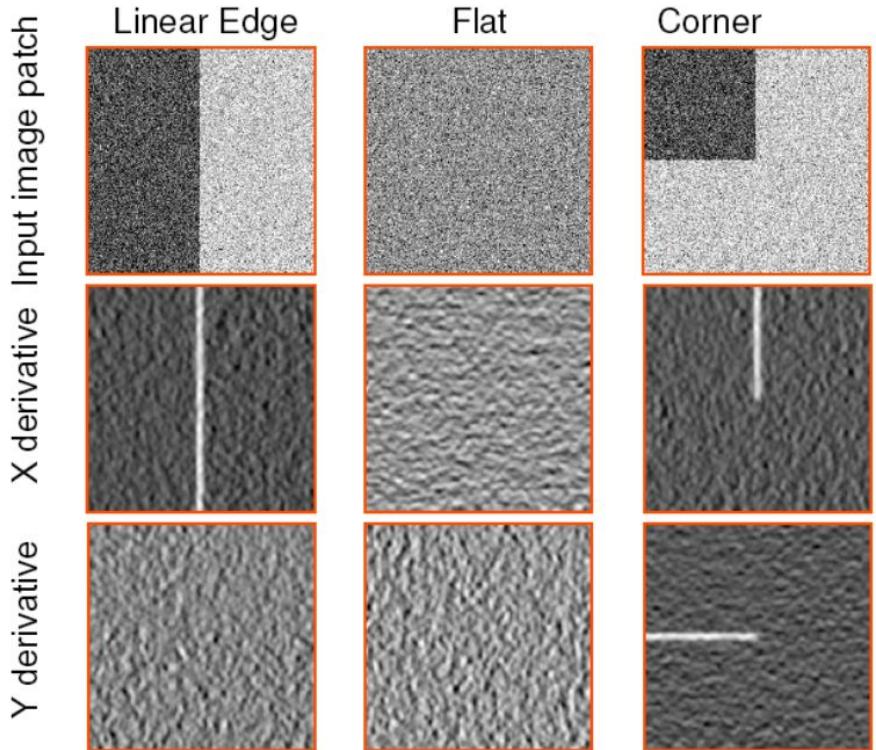


- Harris and Plessey Operator
 - Given:
 -
 -
 -
 -
 -
 -
 -
 - Simplifying the equations, we have:



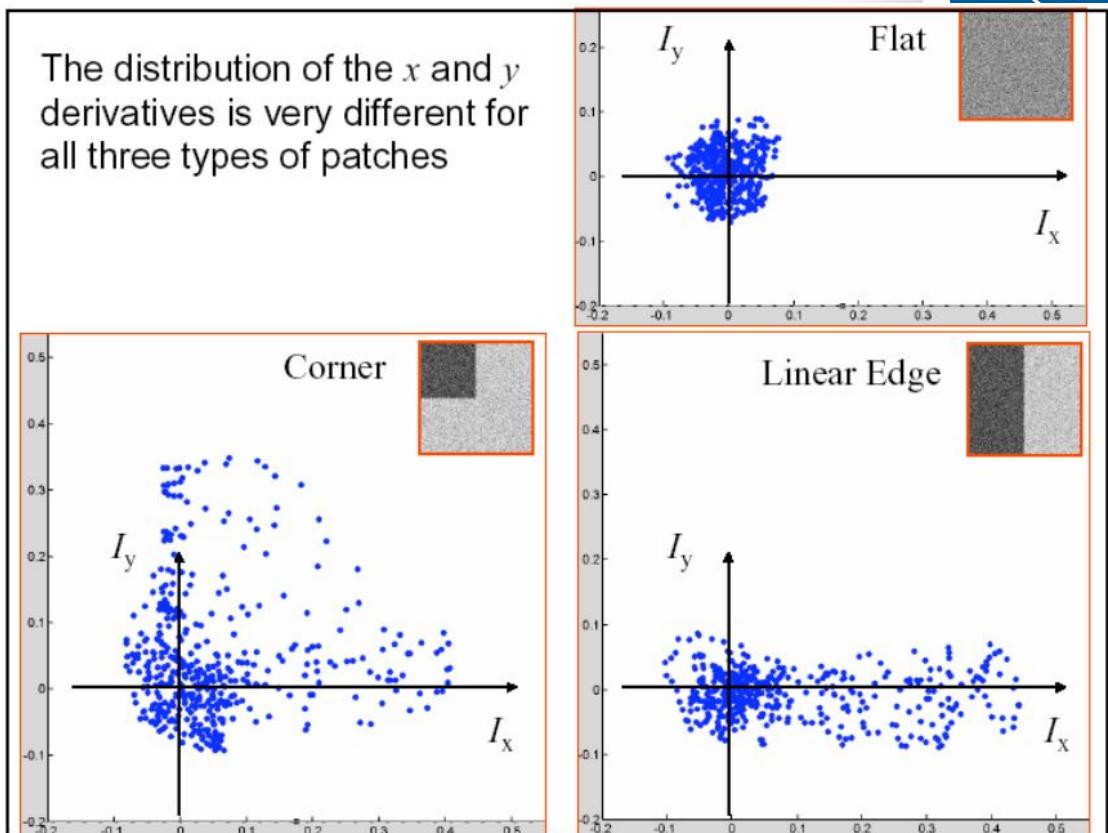
Low Level Features (Corners)

- Harris and Plessey Operator
 - Image gradients



Low Level Features (Corners)

- Harris and Plessey Operator
 - Image gradients
 - Plotting derivatives

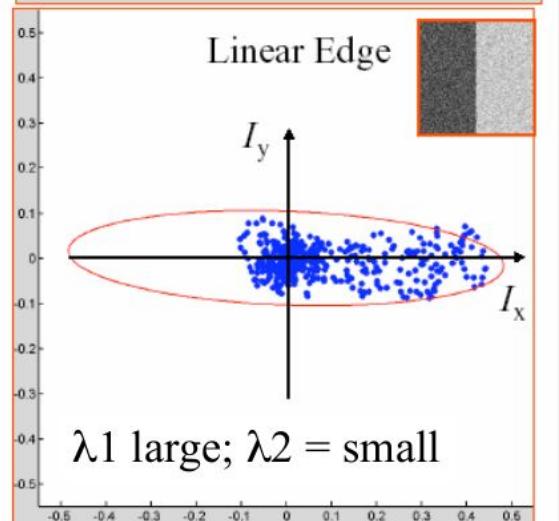
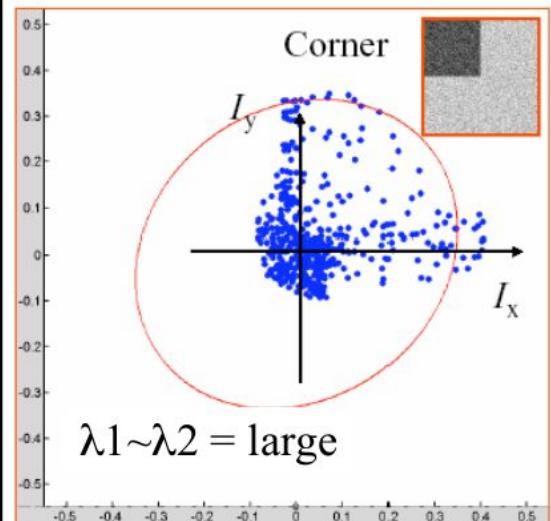
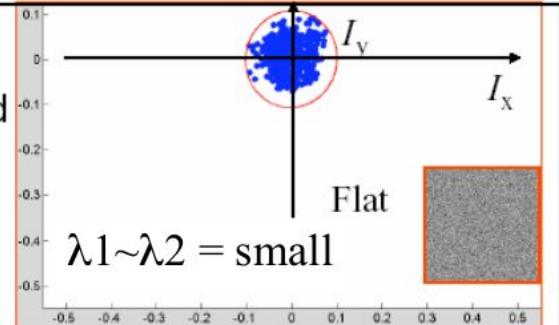


Low Level Features (Corners)



- Harris and Plessey Operator
 - Image gradients
 - Plotting derivatives
 - Fitting ellipses

The distribution of x and y derivatives can be characterized by the shape and size of the principal component ellipse

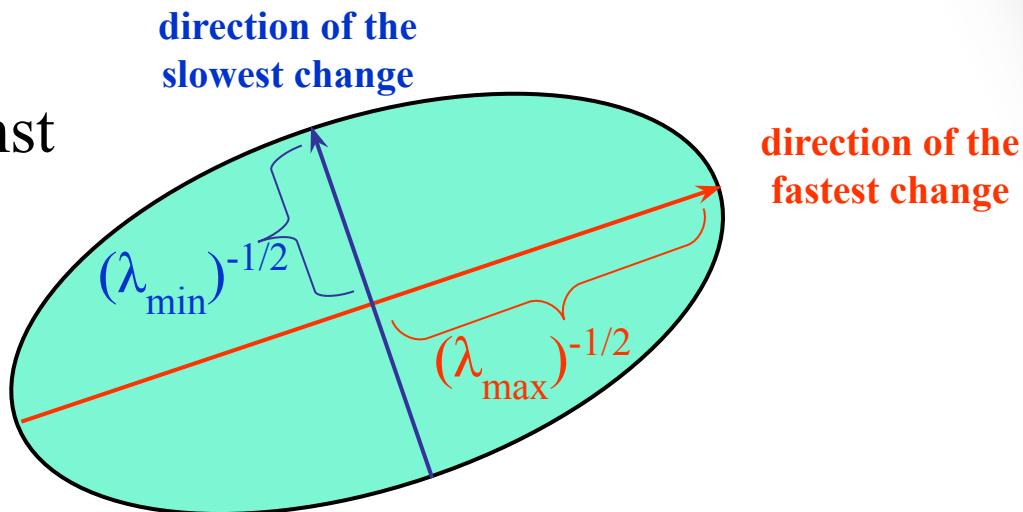




Low Level Features (Corners)

- Harris and Plessey Operator
 - Image gradients
 - Plotting derivatives
 - Fitting ellipses

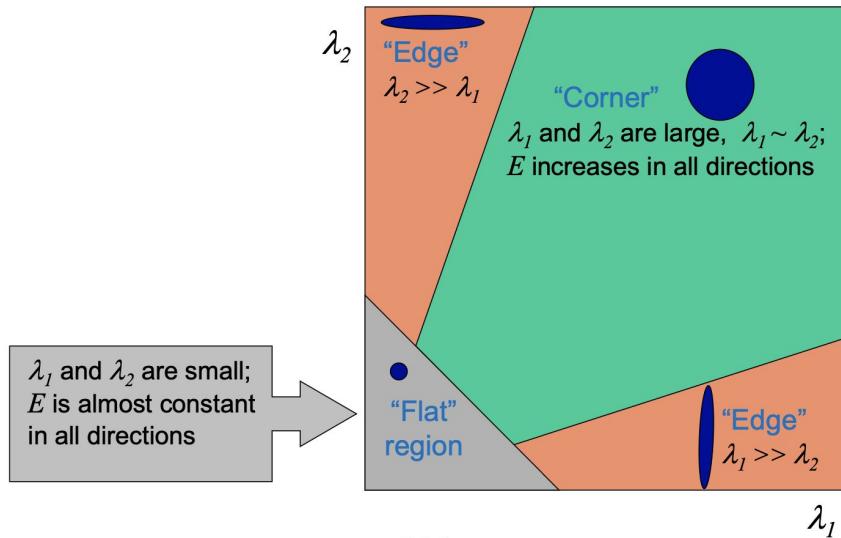
Ellipse $E(u, v) = \text{const}$





Low Level Features (Corners)

- Harris and Plessey Operator
 - The eigenvalues determine the elongation of covariance ellipse.
 - The eigenvectors determine the slope of covariance ellipse.
 - k is empirically defined in interval: $0.04 \leq k \leq 0.06$



Harris detector: Steps



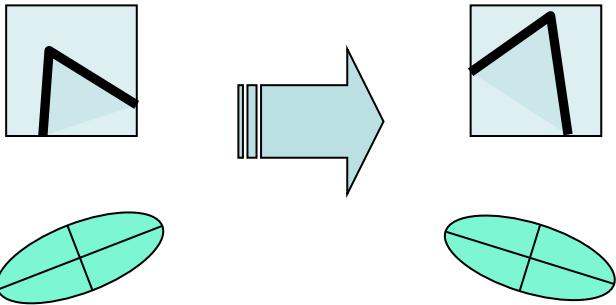
1. Compute Gaussian derivatives at each pixel
2. Compute second moment matrix H in a Gaussian window around each pixel
3. Compute corner response function R
4. Threshold R
5. Find local maxima of response function
(nonmaximum suppression)

C.Harris and M.Stephens. "[A Combined Corner and Edge Detector.](#)"
Proceedings of the 4th Alvey Vision Conference: pages 147—151, 1988.

Low Level Features (Corners)



- Harris and Plessey Operator



- Ellipse rotates but its shape (i.e. eigenvalues) remains the same

Corner response R is invariant to image rotation

Low Level Features (Corners)

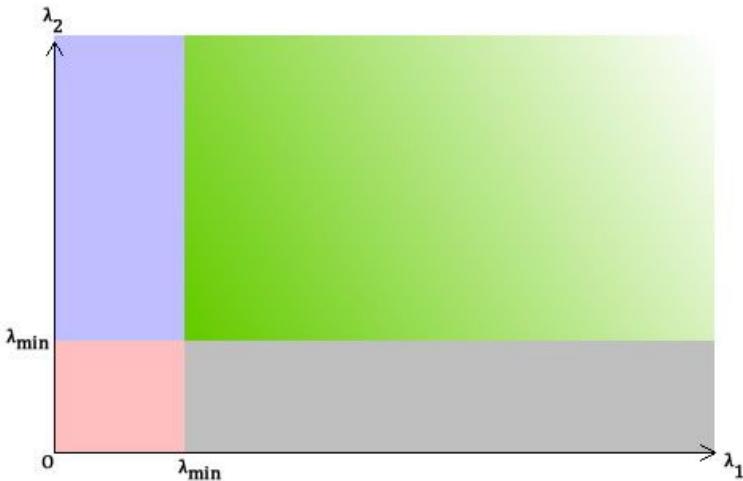


- Harris and Plessey Operator

**Demonstration
(MATLAB)**

Low Level Features (Corners)

- Shi-Tomasi Operator
 - They propose an alternative computation of corner response
 - $$R(x, y) = \min(\lambda_1, \lambda_2)$$
 - The eigenvalues have to be greater than λ_{min}



IEEE Conference on Computer Vision and Pattern Recognition (CVPR'94) Seattle, June 1994

Good Features to Track

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Bad Features to Track

Bad features can become occluded, and trackers often blindly drift away from their original target when this occurs. No feature-based vision system can hope to work well if these issues have been settled.

In this paper we propose to increase the stability of image features during tracking by using an optimal feature selection criterion that quantifies the change of appearance of a feature between the first and the current frame. This criterion is based on the ratio of the feature's rms residue between the first and the current frame, and when dissimilarity grows too large the feature is discarded. The authors believe that they have made two main contributions to this problem. First, we provide experimental evidence that pure trend-following methods for feature selection, such as the mean-squared-dissimilarity method, are inadequate. Second, we propose a more principled way of determining affine changes by a Newton-Raphson style minimization procedure, in the style of what Lipshitz and Kornai [1] and Szelc and Deriche [2] did. In addition, we propose a more principled way to select features than the more traditional "interest" or "blob" detection methods. We show that good features with good texture properties can be defined by optimizing the tracker's accuracy. In other words, the same set of features can be selected for tracking the world, making it that feature selection is not even harmful to most structure-from-motion algorithms. Furthermore,

This research was supported by the National Science Foundation under contract NAG-1-10734.

Jianbo Shi and Carlo Tomasi (1994). *Good Features To Track*. Computer Vision and Pattern Recognition (CVPR'94)

Low Level Features (Corners)



- OpenCV function: goodFeaturesToTrack()

- void goodFeaturesToTrack(
 - InputArray image,
 - OutputArray corners,
 - int maxCorners = 100,
 - double qualityLevel = 0.01,
 - double minDistance = 10,
 - InputArray mask=noArray(),
 - int blockSize=3,
 - bool useHarrisDetector = false,
 - double k=0.04)

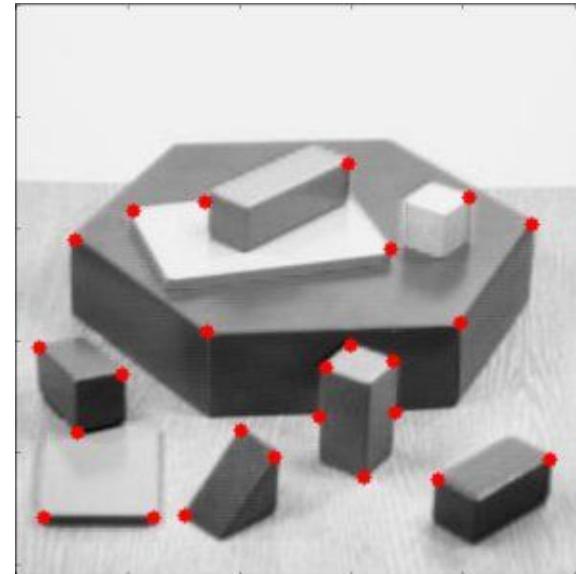




Low Level Features (Corners)

- OpenCV function: goodFeaturesToTrack()

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 - double minDistance = 10,
 - InputArray mask=noArray(),
 - int blockSize=3,
 - bool useHarrisDetector = false,
 - double k=0.04)



Low Level Features (Corners)

- Others corner detectors
- Smallest Univalve Segment Assimilating Nucleus (SUSAN)
 - Edge detector
 - Corner detector
 - Noise filter

Technical Report TR95SMS1c

(Shorter versions have now been published in IJCV [66] and ICPR96 [64],
and the relevant patent is [60]. To reference this research, cite [66])

SUSAN – A New Approach to Low Level Image Processing

Technical Report TR95SMS1c
(Shorter version have now been published in IJCV [66] and ICPR96 [64],
and the relevant patent is [60]. To reference this research, cite [66])

1995

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[www.fmrib.ox.ac.uk/~stree](http://fmrib.ox.ac.uk/~stree)

J.M. Brady
Department of Engineering Science, Oxford University, Oxford, UK

Abstract

This paper describes a new approach to low level image processing, in particular, edge and corner detection and structure preserving noise reduction.
The basic idea is to associate a feature with a local image region which is of similar brightness to that pixel; each pixel has associated with it a local image region which is of similar brightness to that pixel. This association is based on the minimization of the difference between the local image regions, and the noise reduction method uses this to detect structures in the image. The resulting edge and corner detection methods are robust and fast.
The new feature-detector and the new noise-reduction method are described, along with their results.

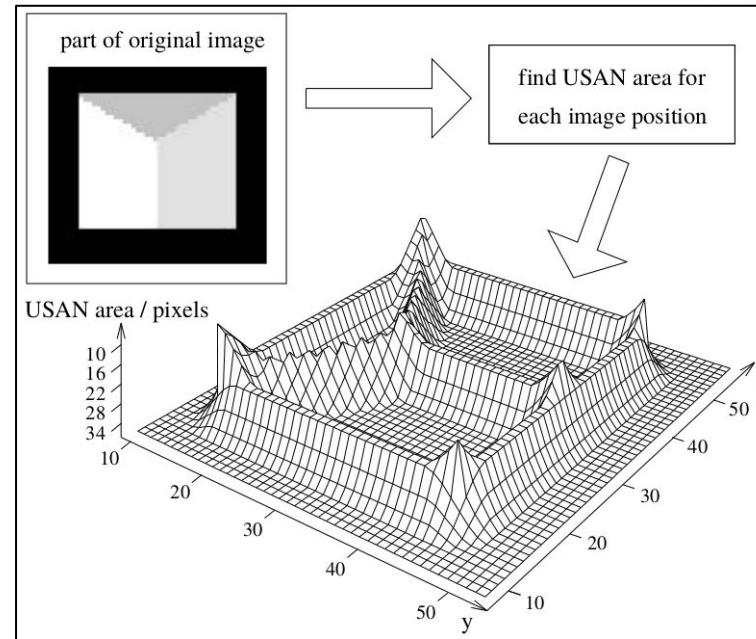
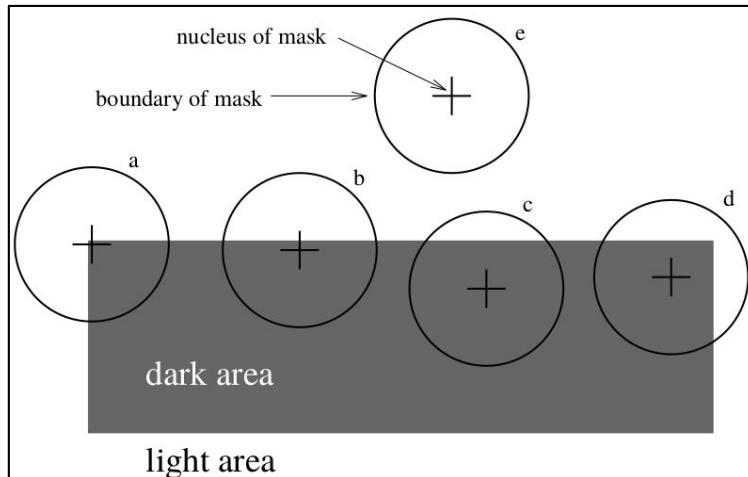
Keywords: edge detection, feature detection, minima/area, noise reduction, smoothing.

S. M. Smith and J. M. Brady (1995)
SUSAN - A new Approach to Low Level Image Processing
Technical Report Oxford University

Low Level Features (Corners)



- Others corner detectors
- Smallest Univalue Segment Assimilating Nucleus (SUSAN)



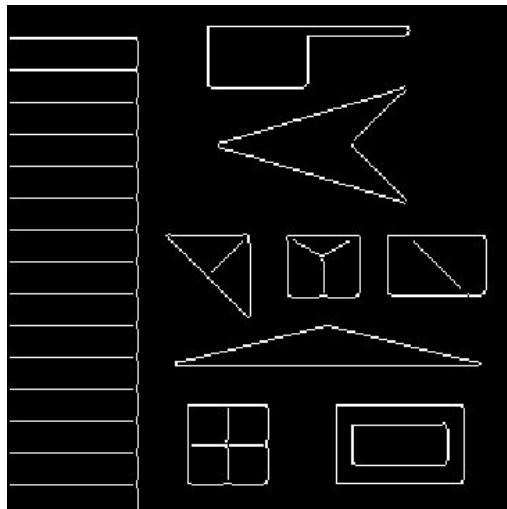
Low Level Features (Corners)



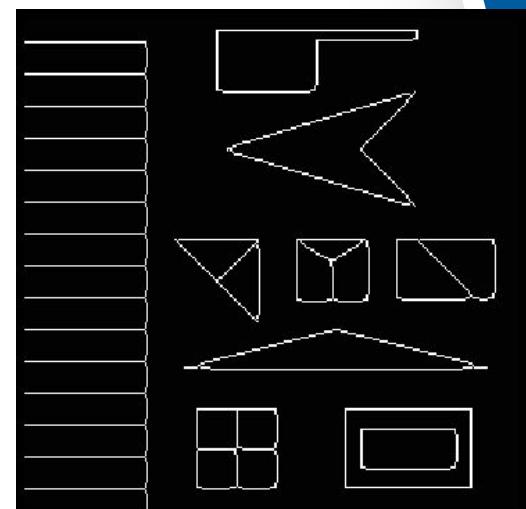
- Others corner detectors
- Smallest Univalue Segment Assimilating Nucleus (SUSAN)



Test
Image



Canny edge
detector

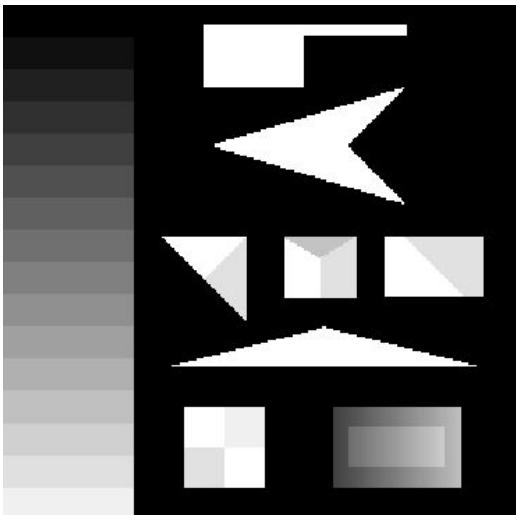


SUSAN edge
detector

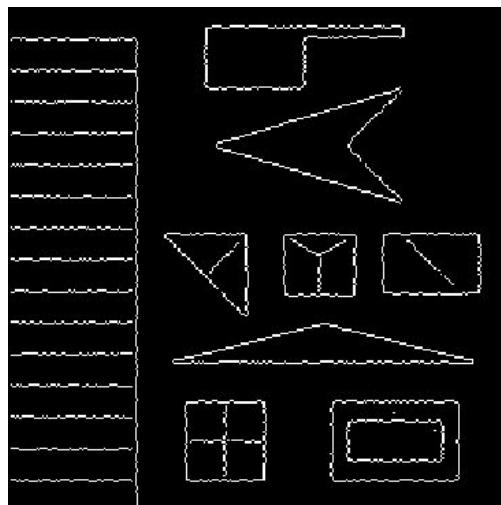
Low Level Features (Corners)



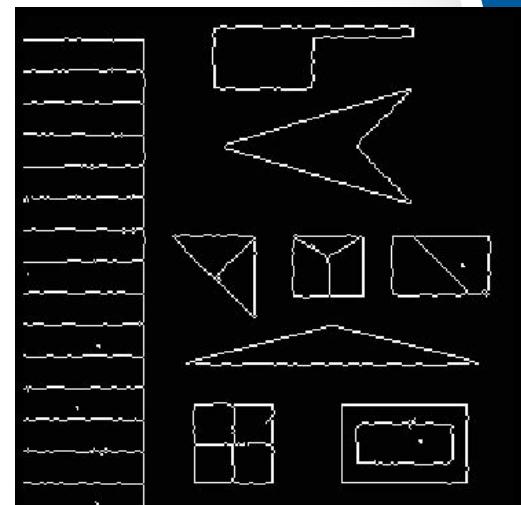
- Others corner detectors
- Smallest Univalue Segment Assimilating Nucleus (SUSAN)



Test
Image



Canny edge
detector
AWGN (5db)

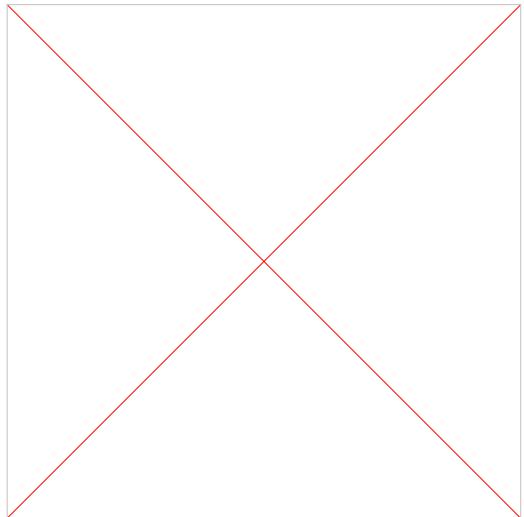


SUSAN edge
detector
AWGN (5db)

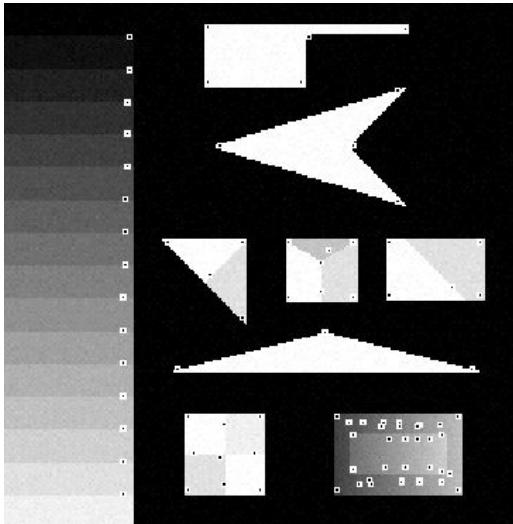
Low Level Features (Corners)



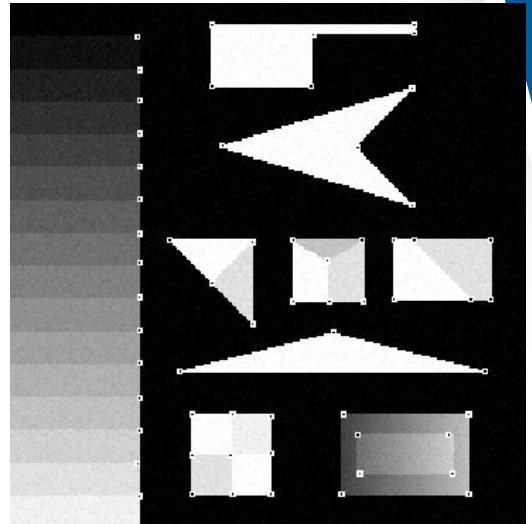
- Others corner detectors
- Smallest Univalue Segment Assimilating Nucleus (SUSAN)



Test
Image



Harris-Plessey corner
detector
AWGN (5db)



SUSAN corner
detector
AWGN (5db)



Low Level Features (Corners)

- Others corner detectors
- FASTER and better: A machine learning approach to corner detection
- (FAST Corner Detector)

Faster and better: a machine learning approach to corner detection
Edward Rosten, Reid Porter, and Tom Drummond

Abstract. The computational efficiency of a corner detector has been the subject of much work over the last 20 years. This paper presents a new approach to corner detection which is significantly faster than previous methods. It is based on the observation that corners can be detected by analysing the local image statistics around a point. This is done using a sliding window approach, and the resulting features are then used in a support vector machine classifier to predict if a corner is present or not. The proposed algorithm is able to detect corners at a rate of approximately 20 frames per second. We also show that despite being principally aimed at real-time corner detection, our algorithm is able to achieve significantly superior results to existing corner detectors. Finally, the computation time required to process an image is proportional to the number of corners detected, making the algorithm suitable for real-time corner detection.

Index Terms—corner detection, feature extraction, tracking

CORNER detection is used in a wide variety of vision tasks such as tracking, localisation, SLAM and registration. In fact it is so important that there is even a journal dedicated to it [1].

Not only has the development of a large number of corner detection algorithms been an active field of research,

but the field has also been the subject of much debate.

The reason for this is that while the basic idea is simple,

the details of how to implement it are not.

In this paper we propose a new corner detection algorithm which is both very fast and very accurate.

We also show that it is able to detect corners at a rate of

approximately 20 frames per second.

Finally, we show that the proposed algorithm is able to

achieve significantly better results than previous corner

detectors.

The remainder of this paper is organised as follows.

Section 2 gives some background information on

corners and corner detection.

Section 3 describes the proposed algorithm.

Section 4 shows experimental results.

Section 5 concludes the paper.

I. INTRODUCTION

Corner detection is one of the first steps in many vision tasks such as tracking, localisation, SLAM and registration.

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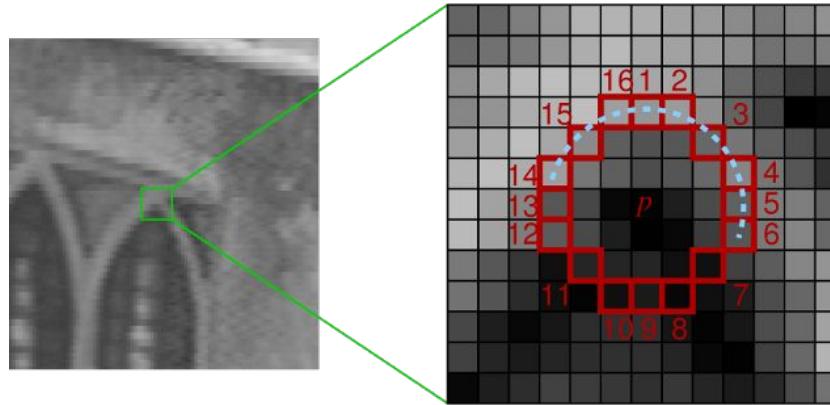
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Section 4 shows experimental results.

Section 5 concludes the paper.



Eduard Rosten and Tom Drummond (2010)

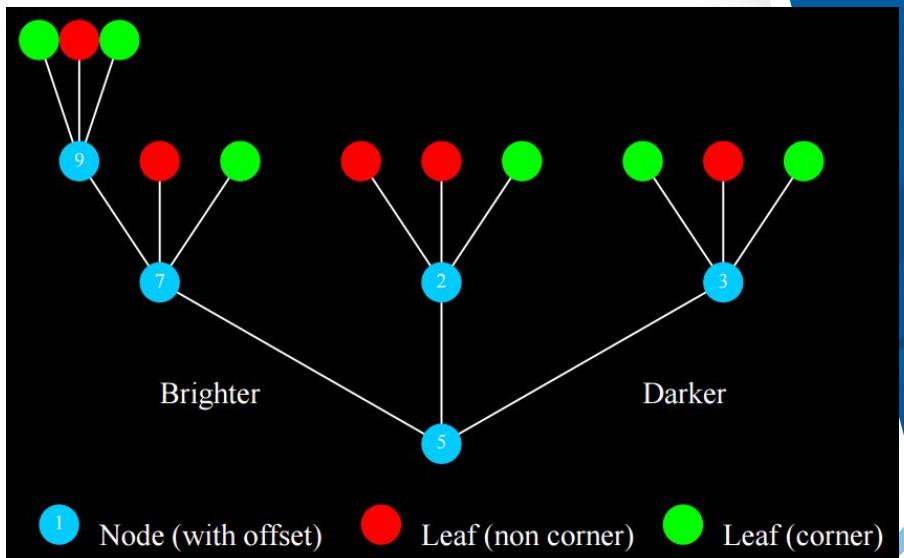
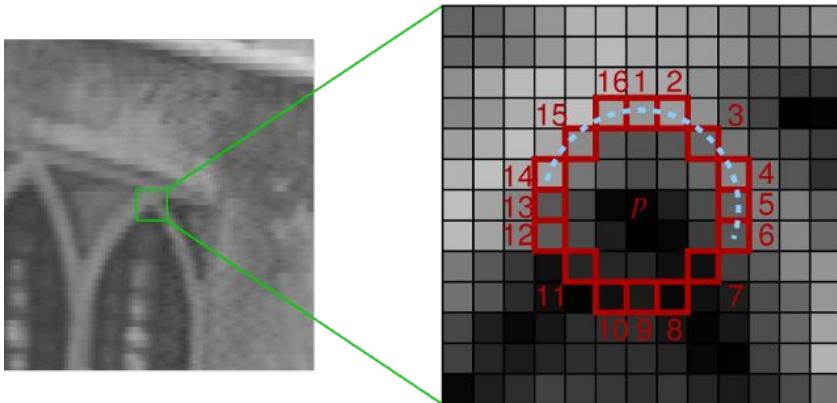
FASTER and better: A machine learning approach to corner detection

IEEE Trans. Pattern Analysis and Machine Intelligence

Low Level Features (Corners)



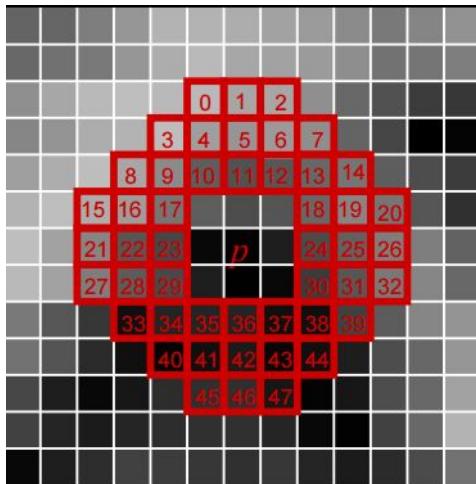
- Others corner detectors
- FASTER and better: A machine learning approach to corner detection
- (FAST Corner Detector)



Low Level Features (Corners)



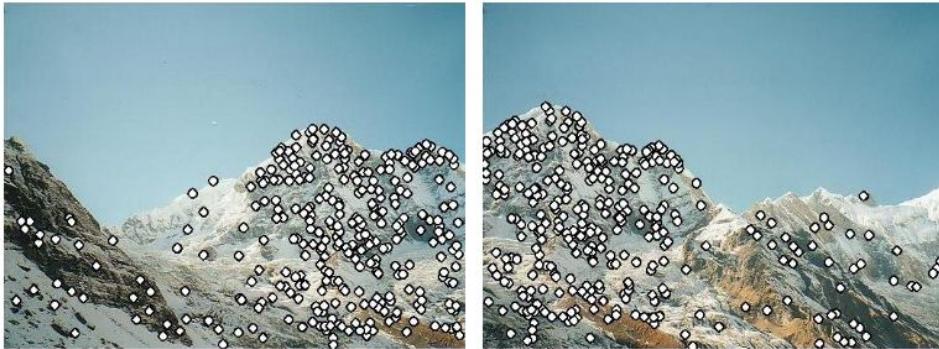
- Others corner detectors
- FASTER and better: A machine learning approach to corner detection
- (FAST-ER: Enhanced Repeatability)



Detector	Opteron 2.6GHz		Pentium III 850MHz	
	ms	%	ms	%
Fast $n = 9$ (non-max suppression)	1.33	6.65	5.29	26.5
Fast $n = 9$ (raw)	1.08	5.40	4.34	21.7
Fast $n = 12$ (non-max suppression)	1.34	6.70	4.60	23.0
Fast $n = 12$ (raw)	1.17	5.85	4.31	21.5
Original FAST $n = 12$ (non-max suppression)	1.59	7.95	9.60	48.0
Original FAST $n = 12$ (raw)	1.49	7.45	9.25	48.5
Harris	24.0	120	166	830
DoG	60.1	301	345	1280
SUSAN	7.58	37.9	27.5	137.5

Table 1. Timing results for a selection of feature detectors run on fields (768×288) of a PAL video sequence in milliseconds, and as a percentage of the processing budget per frame. Note that since PAL and NTSC, DV and 30Hz VGA (common for webcams) have approximately the same pixel rate, the percentages are widely applicable. Approximately 500 features per field are detected.

Characteristics of good features



- **Repeatability**
 - The same feature can be found in several images despite geometric and photometric transformations
- **Saliency**
 - Each feature has a distinctive description
- **Compactness and efficiency**
 - Many fewer features than image pixels
- **Locality**
 - A feature occupies a relatively small area of the image; robust to clutter and occlusion

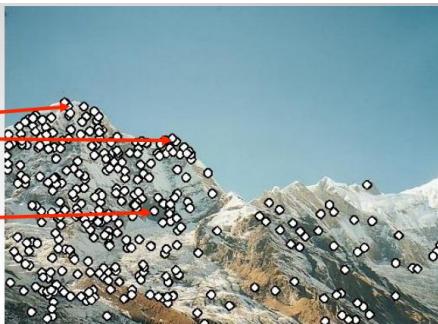
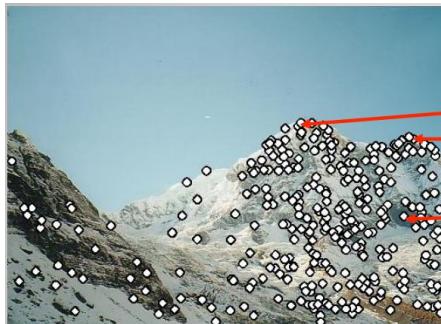
Why to use corners or features of images?





Why to use corners or features of images?

- **Example of motivation:**
 - Image registration





Why to use corners or features of images?

- **Example of motivation:**

- Automate object tracking
- Motion estimation
- Optical flow

H. Badino and T. Kanade:

"A Head-Wearable Short-Baseline Stereo System for the Simultaneous Estimation of Structure and Motion".
IAPR Conference on Machine Vision Applications (MVA), Nara, Japan, June 2011.

Why to use corners or features of images?



- **Example of motivation:**

- 3D Reconstruction
- Augmented Reality

Richard Newcombe, Steven Lovegrove and Andrew Davison
DTAM: Dense Tracking and Mapping in Real-Time"
ICCV 2011.



Why to use corners or features of images?

- **List of motivations:**

- Image registration
- Automate object tracking
- Point matching for computing disparity
- Stereo calibration
 - Estimation of fundamental matrix
- Motion based segmentation
- Recognition
- 3D object reconstruction
- Robot navigation
- Image retrieval and indexing

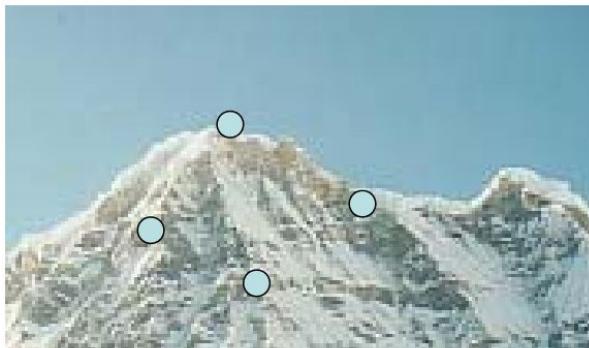


Main Concepts



- **Goal 1: interest operator repeatability**

- We want to detect, at least some of, the same points in the images.
- Yet we have to be able to run the detection procedure independently per image.
- Ideal interest point operators must be invariant to:
 - Noise
 - Illumination
 - Translation
 - Rotation
 - Scale



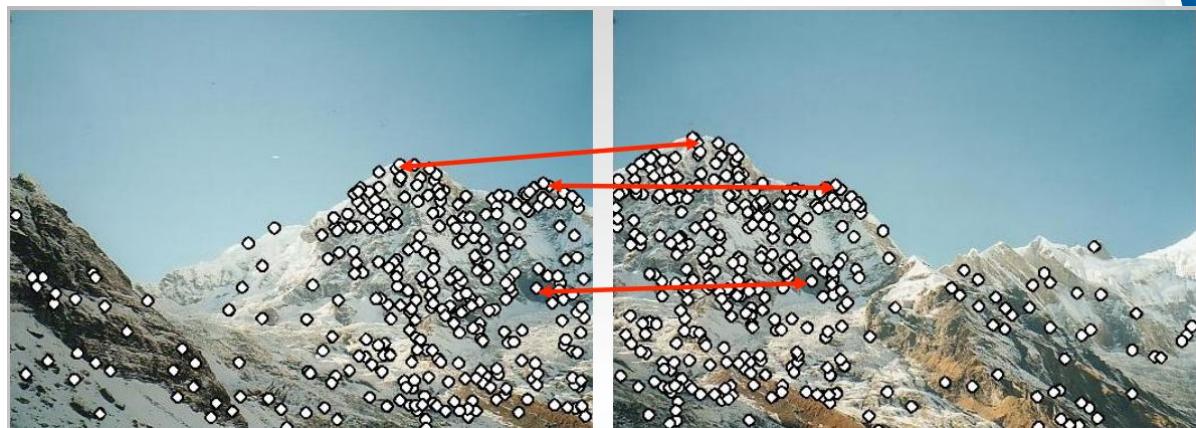
No chance to find true matches!



Main Concepts

- **Goal 2: descriptor distinctiveness**

- We want to be able to reliably determine which point goes with which (Matches).
- Must provide some invariance to geometric and photometric differences between the two views.
- Ideal descriptors must be robust to:
 - Noise
 - Illumination
 - Translation
 - Rotation
 - Scale
 - Perspective
 - Partial occlusion

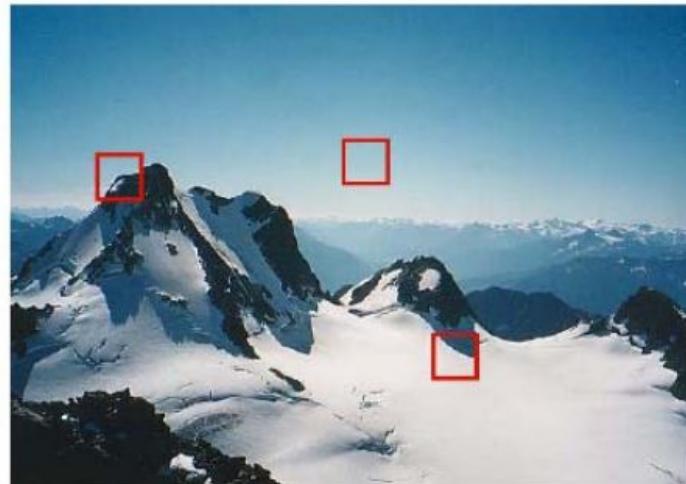
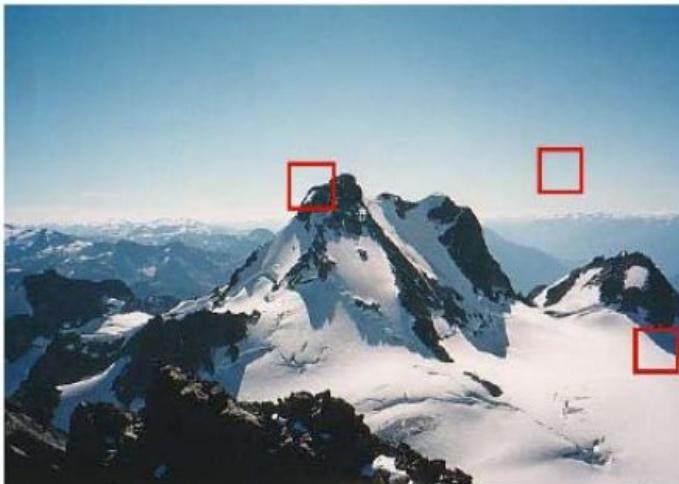


Main Concepts



- **Goal 2: descriptor distinctiveness**

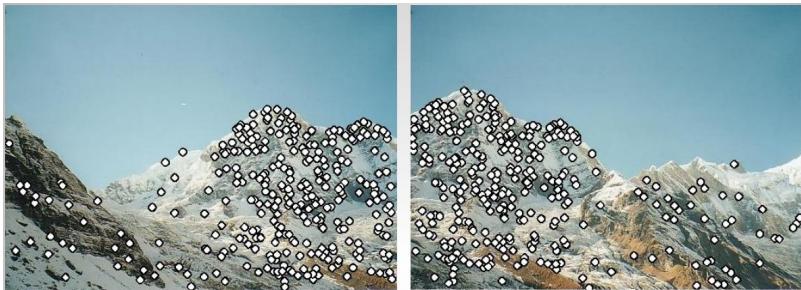
- Some patches can be matched with high accuracy than others.



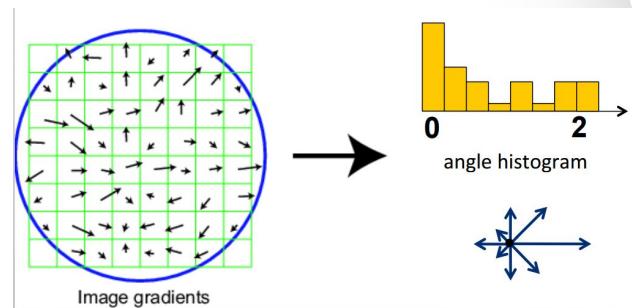


How to use interest points?

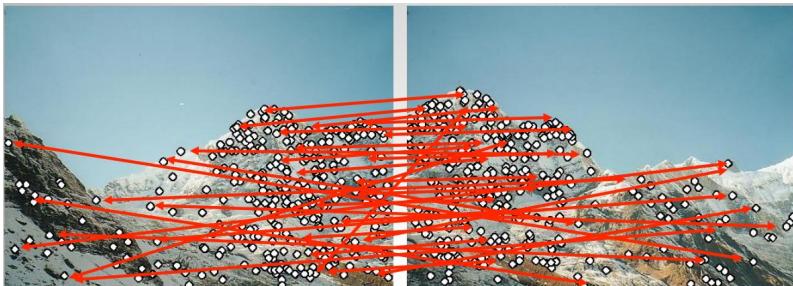
1) Detection



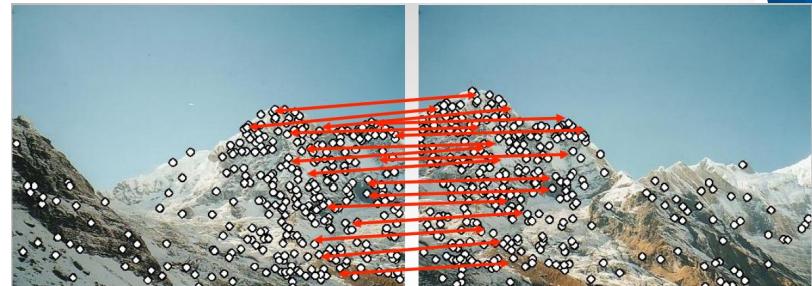
2) Description



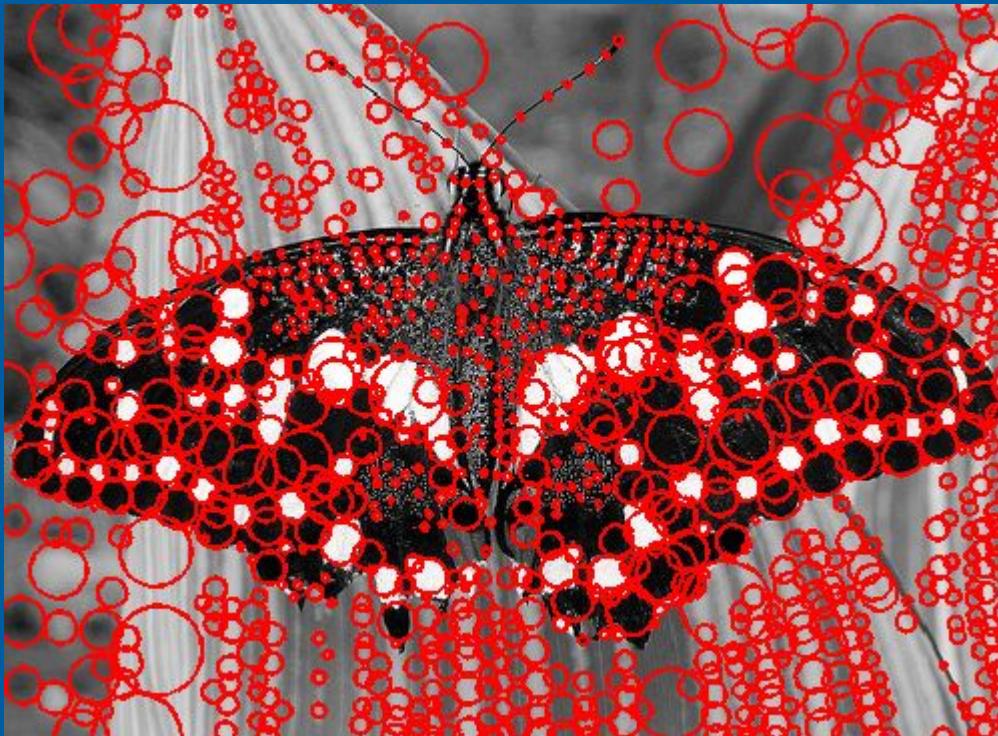
3) Matching



4) Filtering



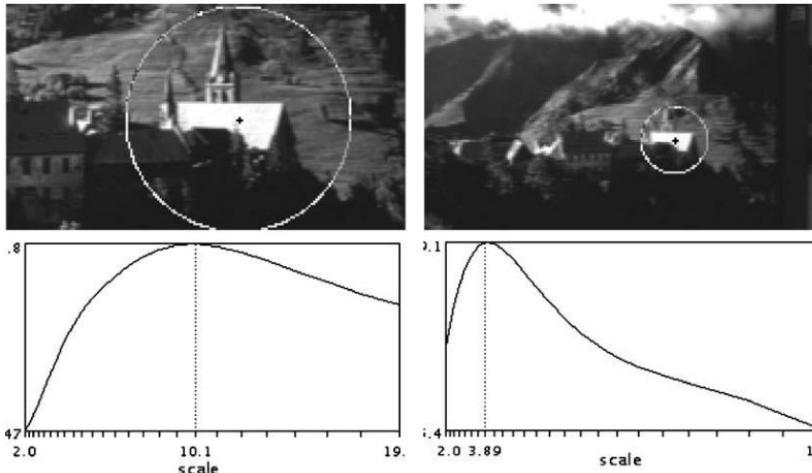
Blob Detection





Blob detection with scale selection

- Goal: independently detect corresponding regions in scaled versions of the same image
- Need *scale selection* mechanism for finding characteristic region size that is *covariant* with the image transformation

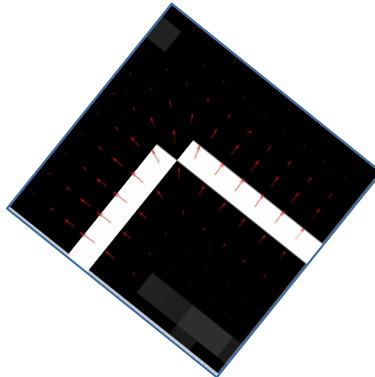
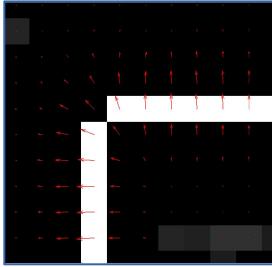




Recap Harris

Harris & Stephens (1988)

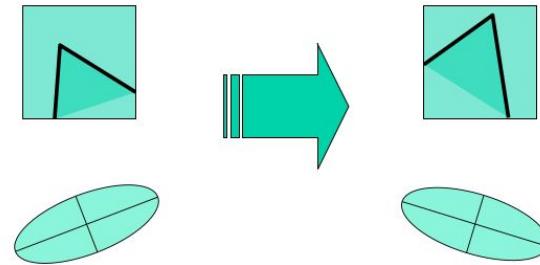
$$\det(C) - \kappa \text{trace}^2(C)$$





Recap Harris

Properties: Rotational Invariance



Ellipse rotates but its shape
(eigenvalues) remains the same

Corner response is **invariant** to image rotation

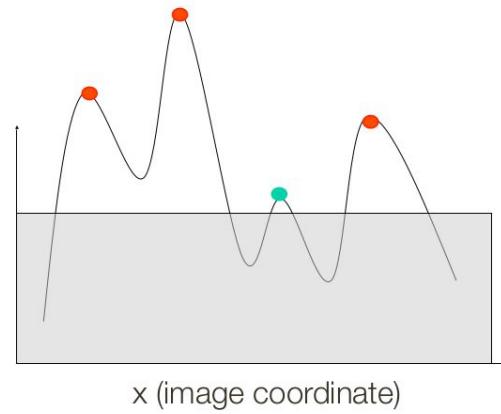
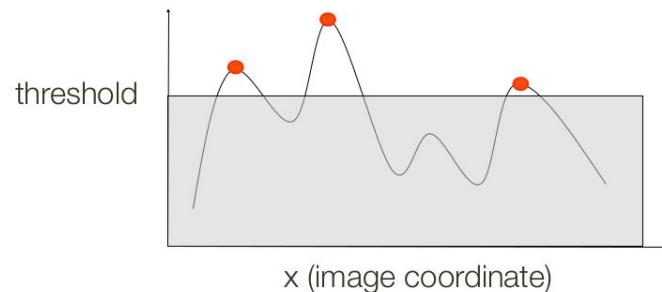


Recap Harris

Properties: (partial) Invariance to Intensity Shifts and Scaling

Only derivatives are used -> Invariance to intensity shifts

Intensity scale could effect performance

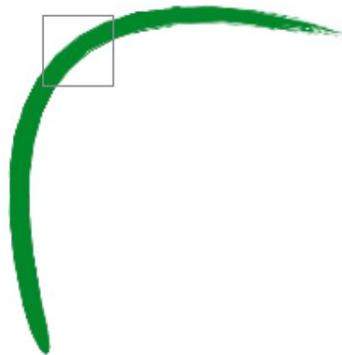




Recap Harris

Properties: NOT Invariant to Scale Changes

edge!



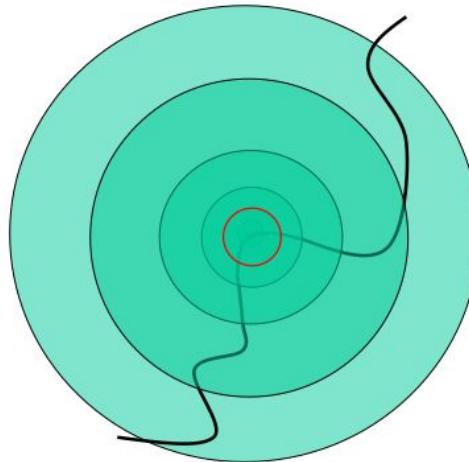
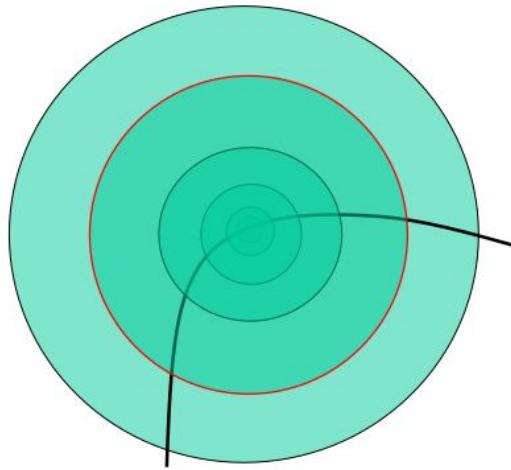
corner!





How to deal with scale?

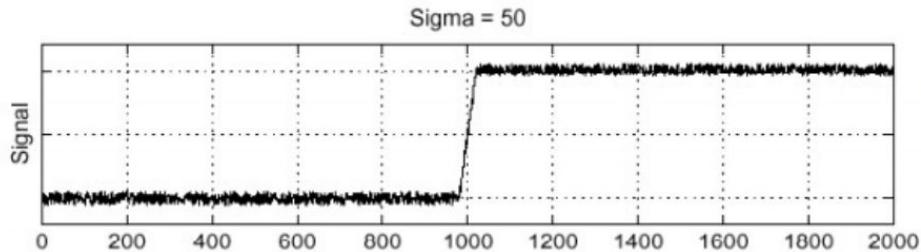
Find local maxima in both, **position** and **scale**.





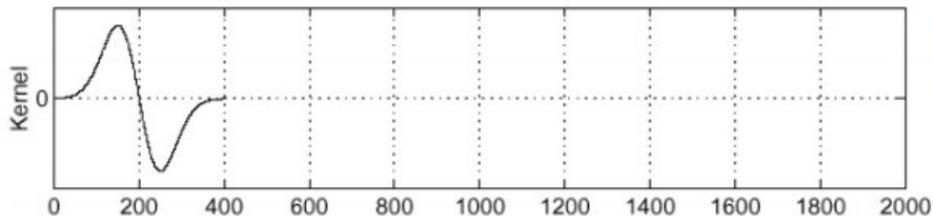
How to deal with scale?

f



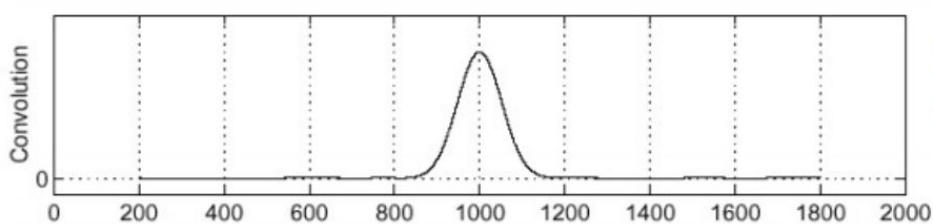
Edge

$\frac{d}{dx} g$



Derivative
of Gaussian

$f * \frac{d}{dx} g$

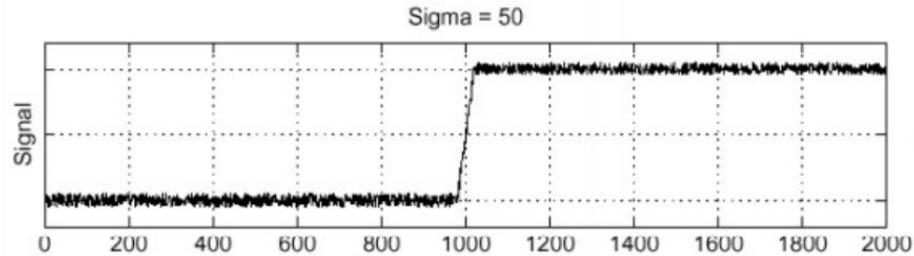


Edge = maximum
of derivative

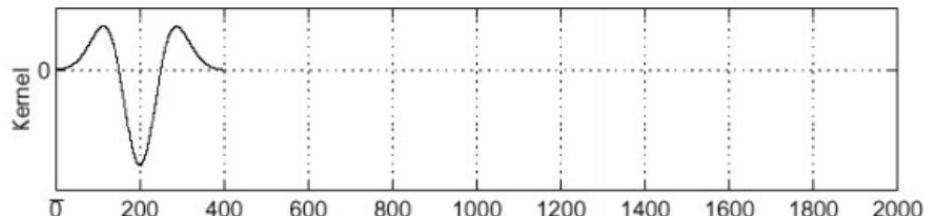


How to deal with scale?

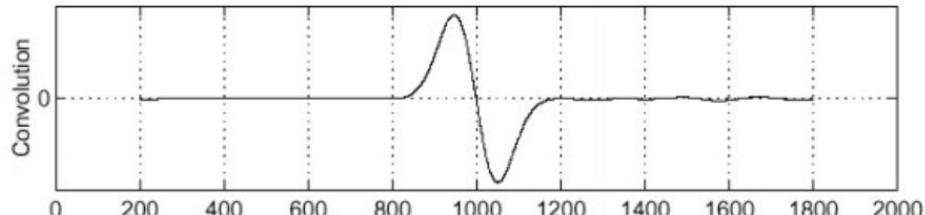
f



$\frac{d^2}{dx^2} g$



$f * \frac{d^2}{dx^2} g$



Edge

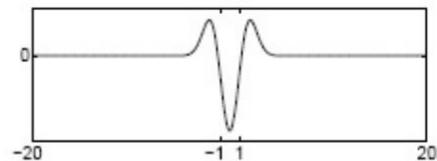
Second derivative
of Gaussian
(Laplacian)

Edge = zero crossing
of second derivative

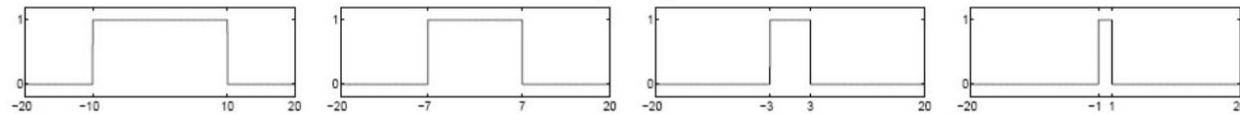


How to deal with scale?

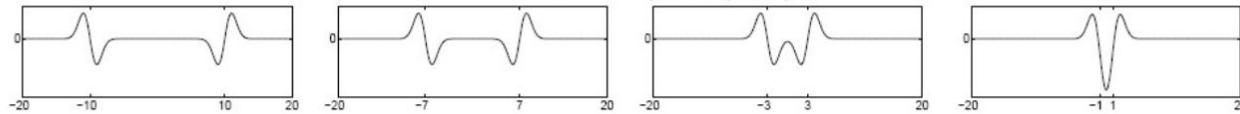
Laplacian filter



Original signal



Convolved with Laplacian ($\sigma = 1$)

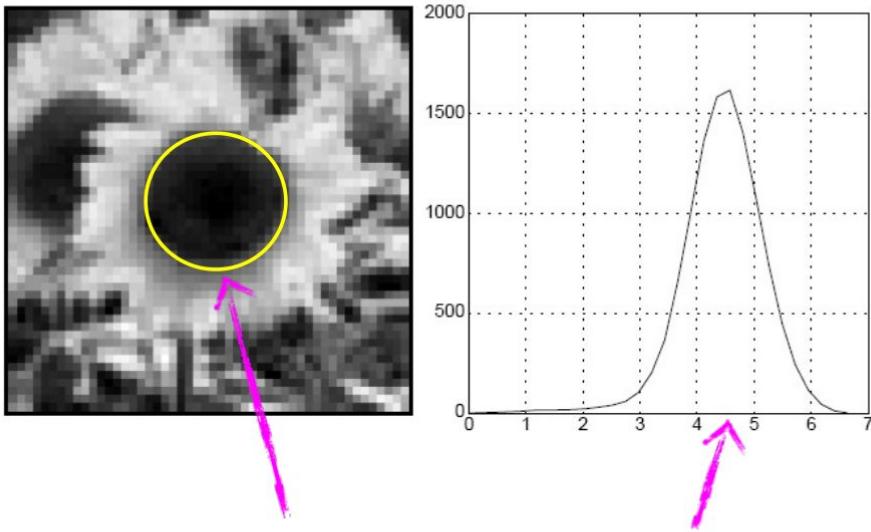


Highest response when the signal has the same **characteristic scale** as the filter





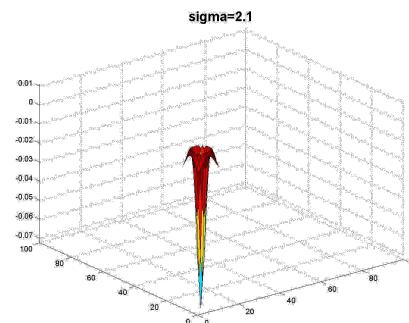
characteristic scale - the scale that produces peak filter response



characteristic scale

we need to search over characteristic scales

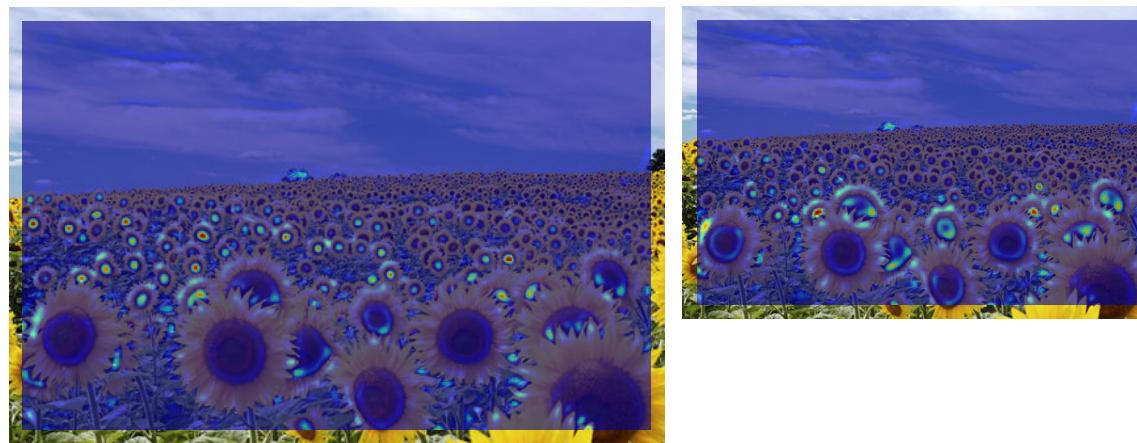
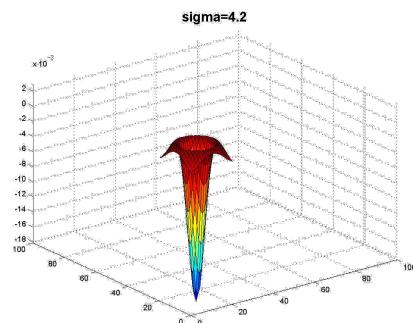
Applying Laplacian Filter at Different Scales



jet color scale
blue: low, red: high

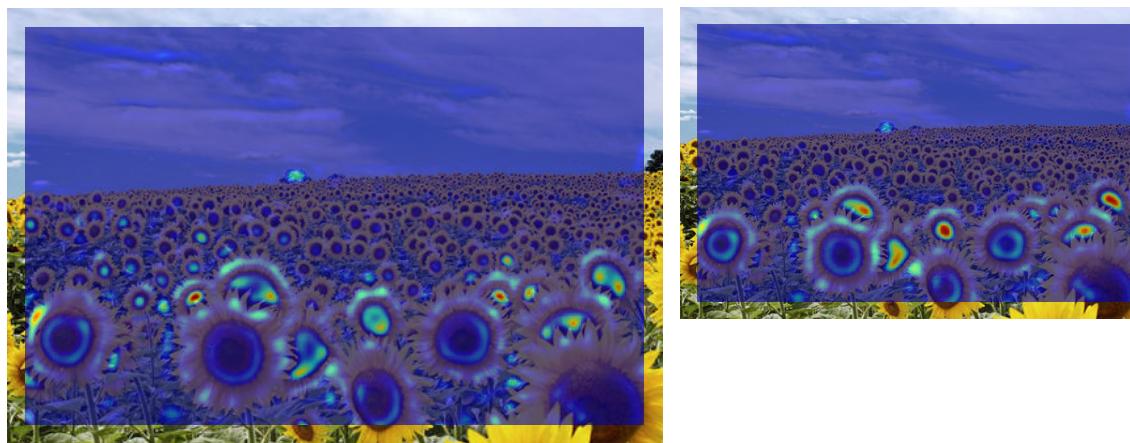
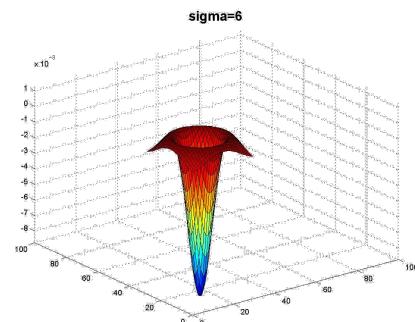
Slide Credit: Ioannis (Yannis) Gkioulekas (CMU)

Applying Laplacian Filter at Different Scales



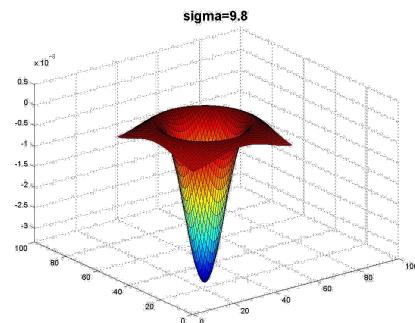
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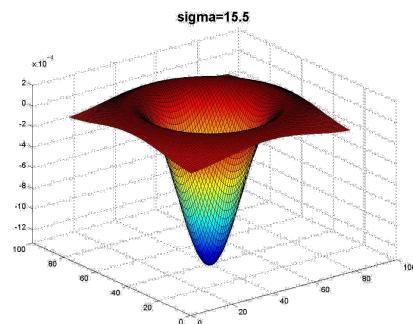
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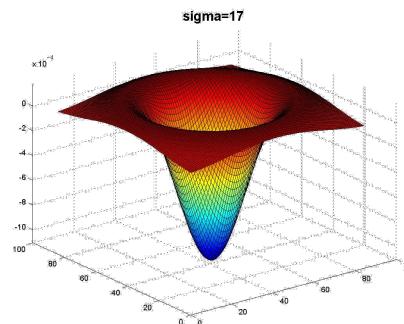
Slide Credit: Ioannis (Yannis) Gkioulekas (CMU)

Applying Laplacian Filter at Different Scales



Slide Credit: Ioannis (Yannis) Gkioulekas (CMU)

Applying Laplacian Filter at Different Scales



Slide Credit: Ioannis (Yannis) Gkioulekas (CMU)

Applying Laplacian Filter at Different Scales

Full size

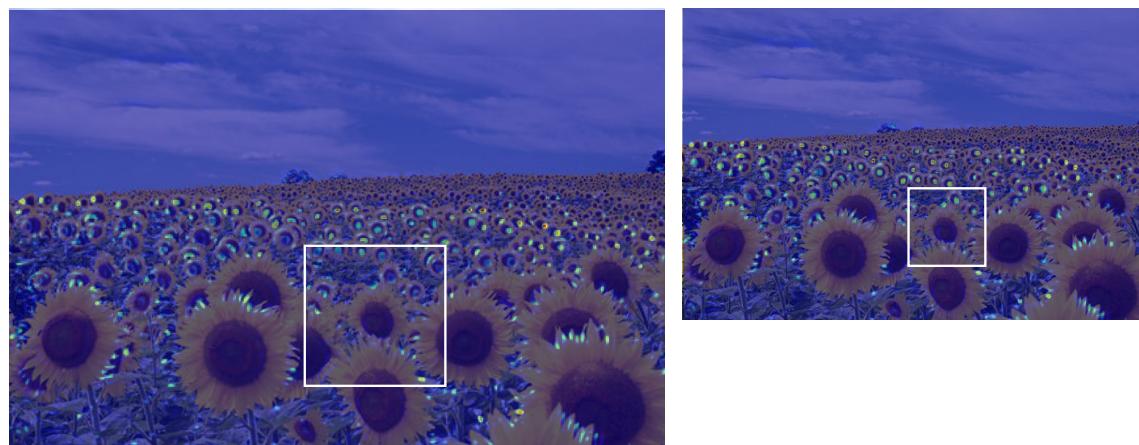
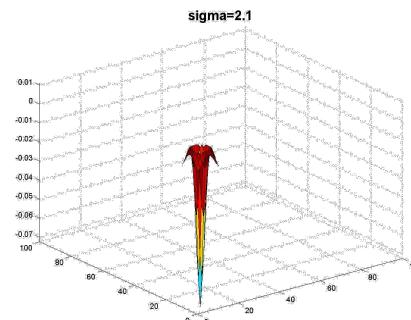


3/4 size



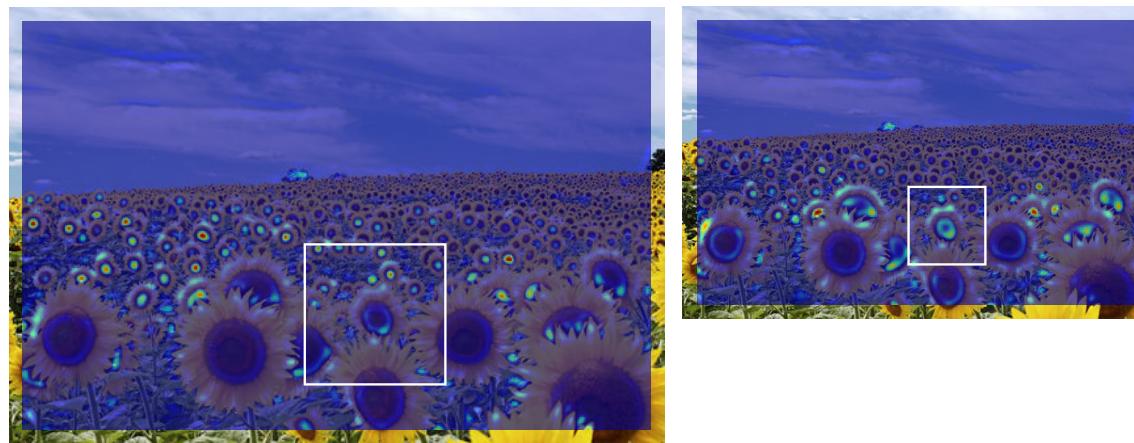
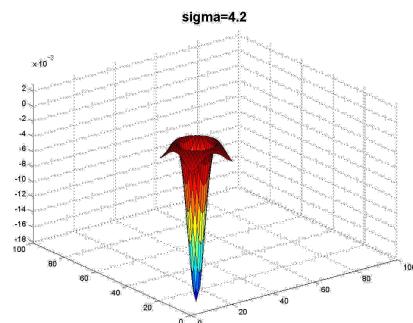
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Applying Laplacian Filter at Different Scales



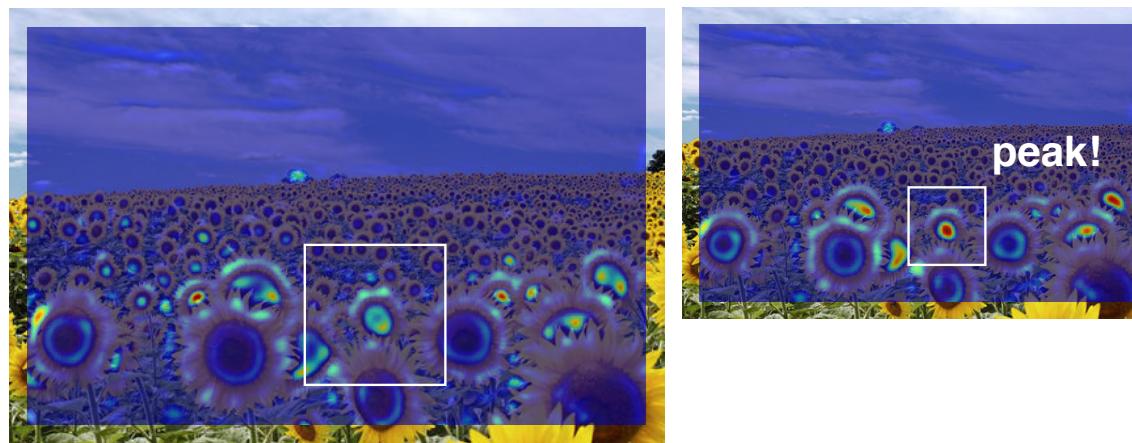
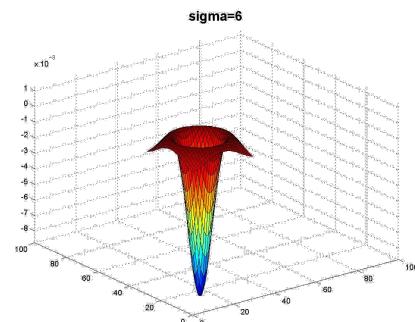
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Applying Laplacian Filter at Different Scales



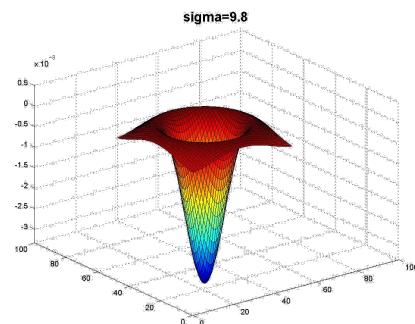
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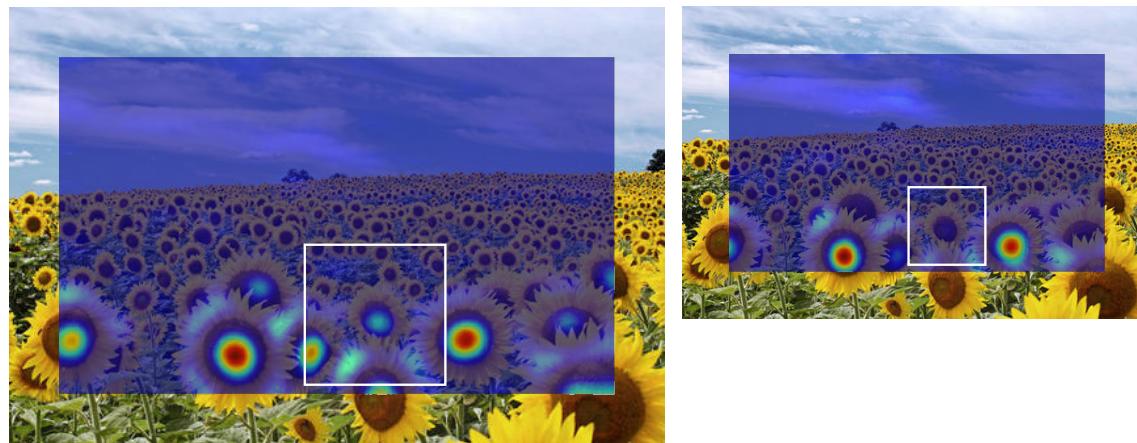
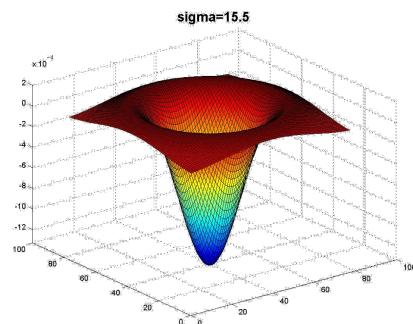
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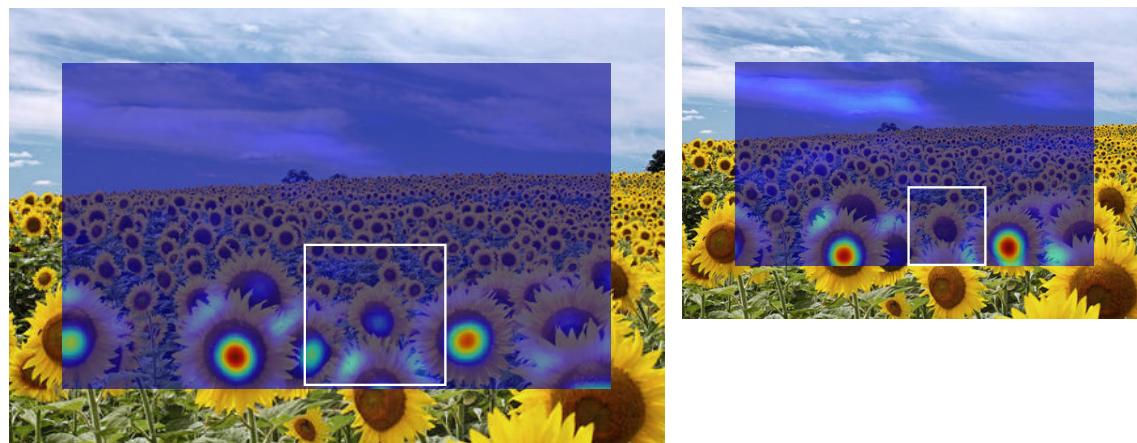
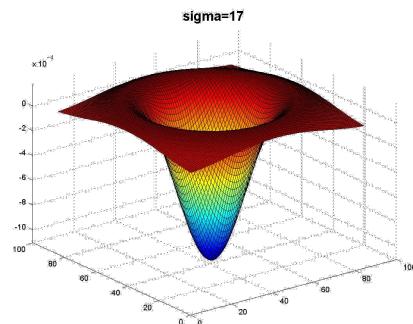
Slide Credit: Ioannis (Yannis) Gkioulekas (CMU)

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Applying Laplacian Filter at Different Scales

Full size



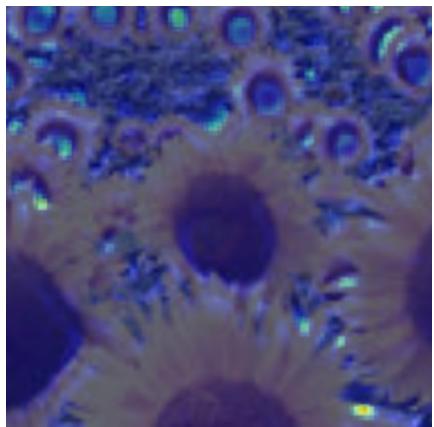
3/4 size



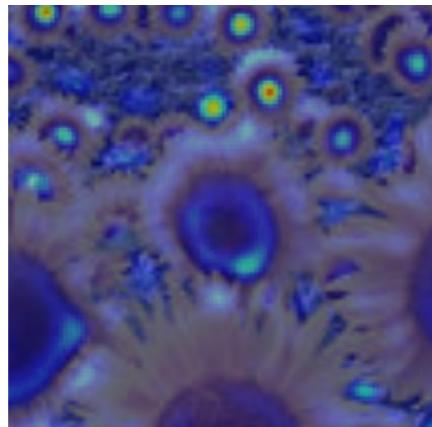
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Applying Laplacian Filter at Different Scales

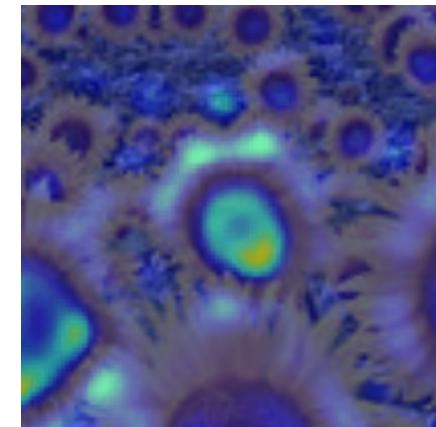
2.1



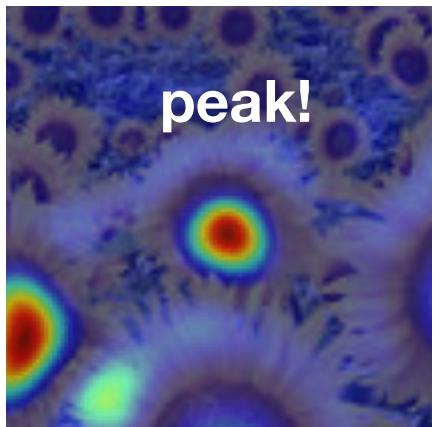
4.2



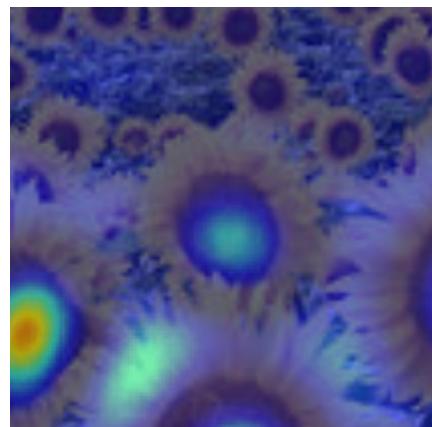
6.0



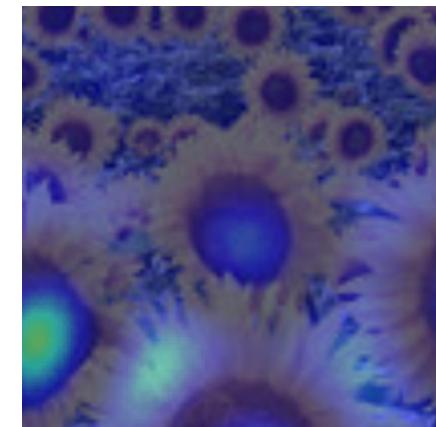
9.8



15.5

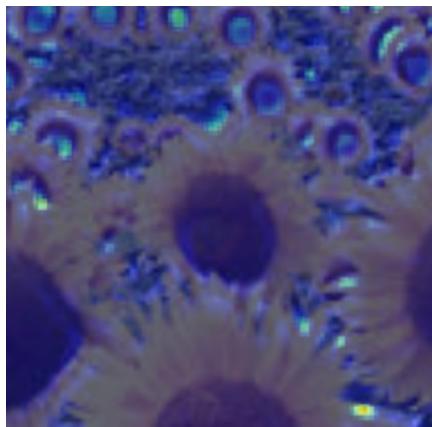


17.0

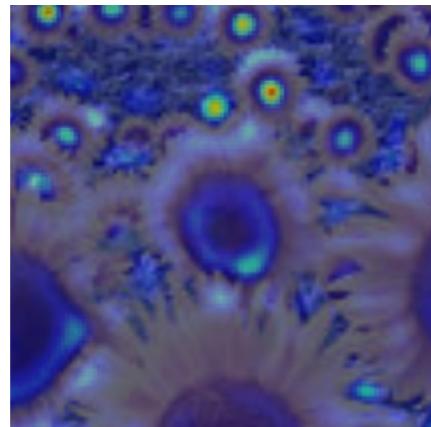


Applying Laplacian Filter at Different Scales

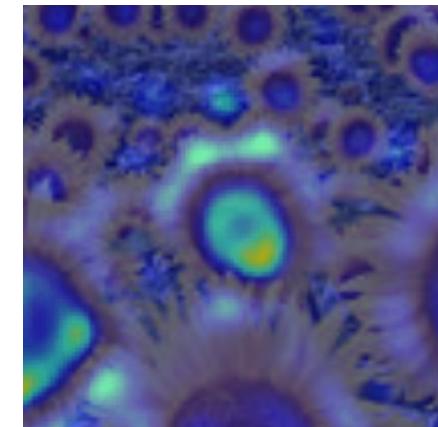
2.1



4.2

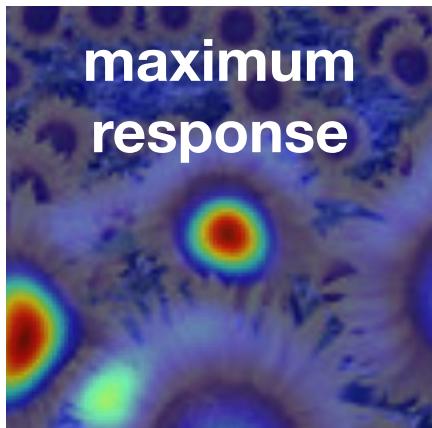


6.0

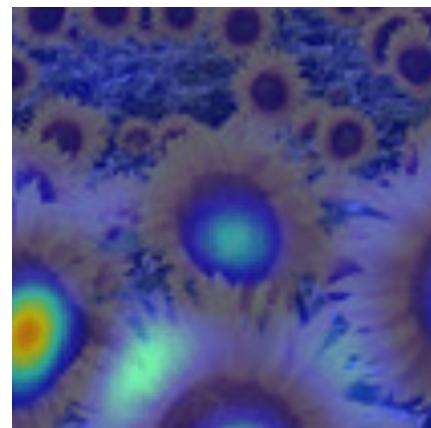


9.8

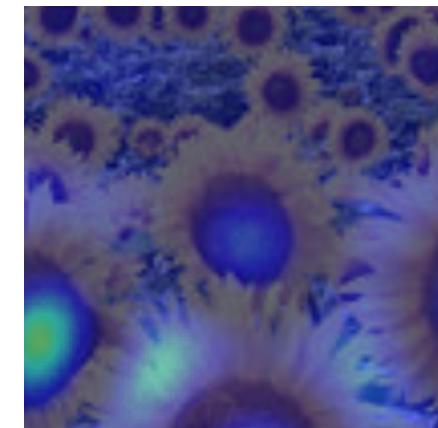
**maximum
response**



15.5

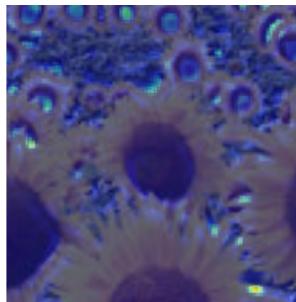


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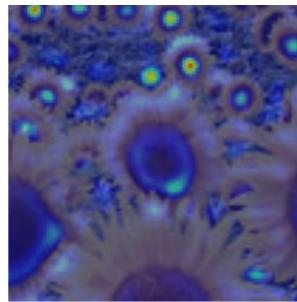


Optimal Scale

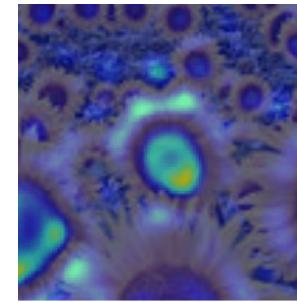
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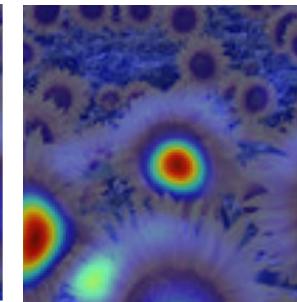
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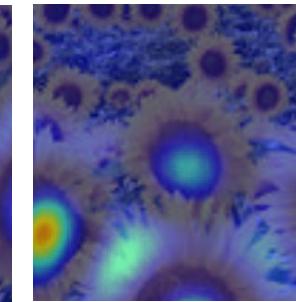
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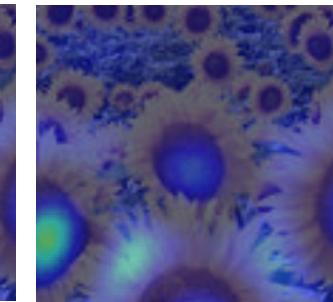
9.8



15.5

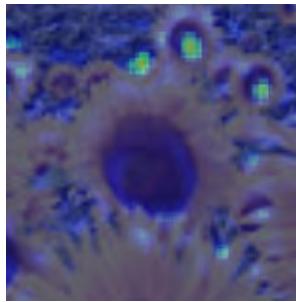


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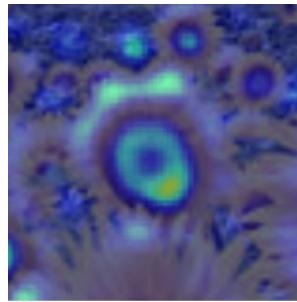


Full size image

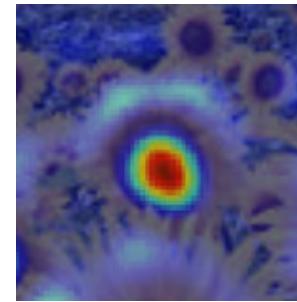
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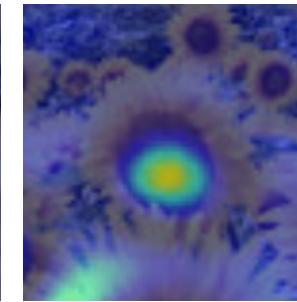
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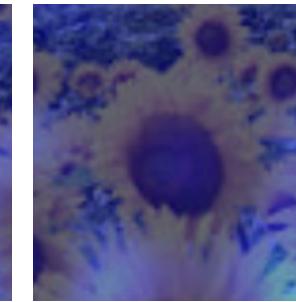
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9.8



15.5

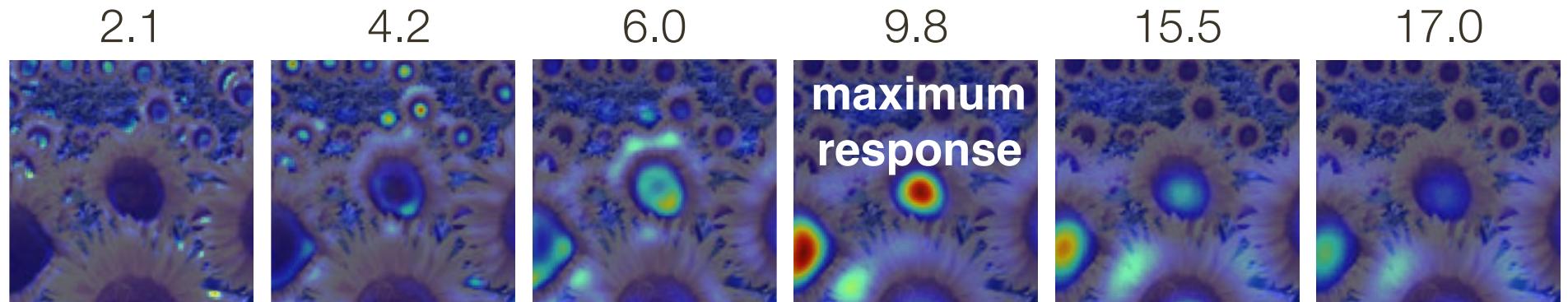


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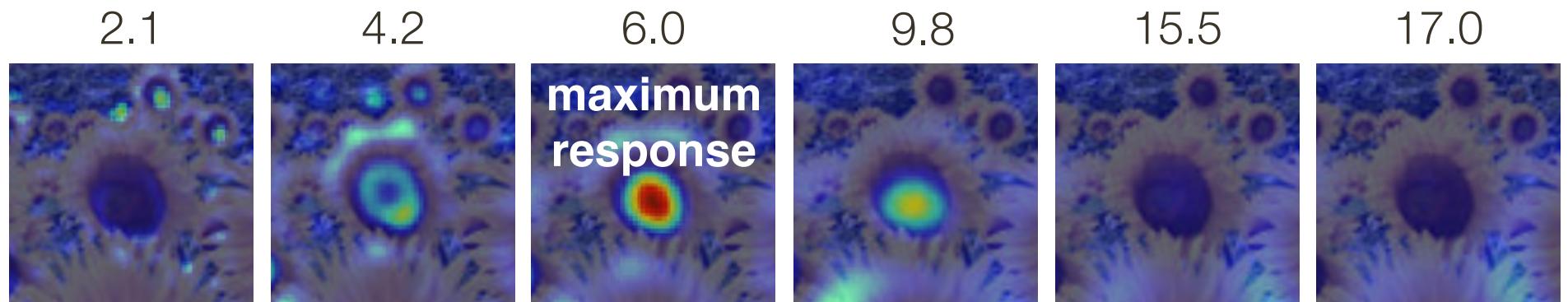


3/4 size image

Optimal Scale



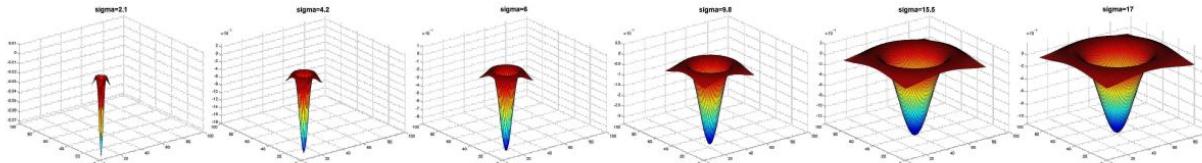
Full size image



3/4 size image



Applying **Laplacian** Filter at Different **Scales**



Full size



3/4 size

