

Introduction to Digital Systems

Part III (Sequential Components)

2020/2021

Sequential Logic Fundamentals and Basic Circuits

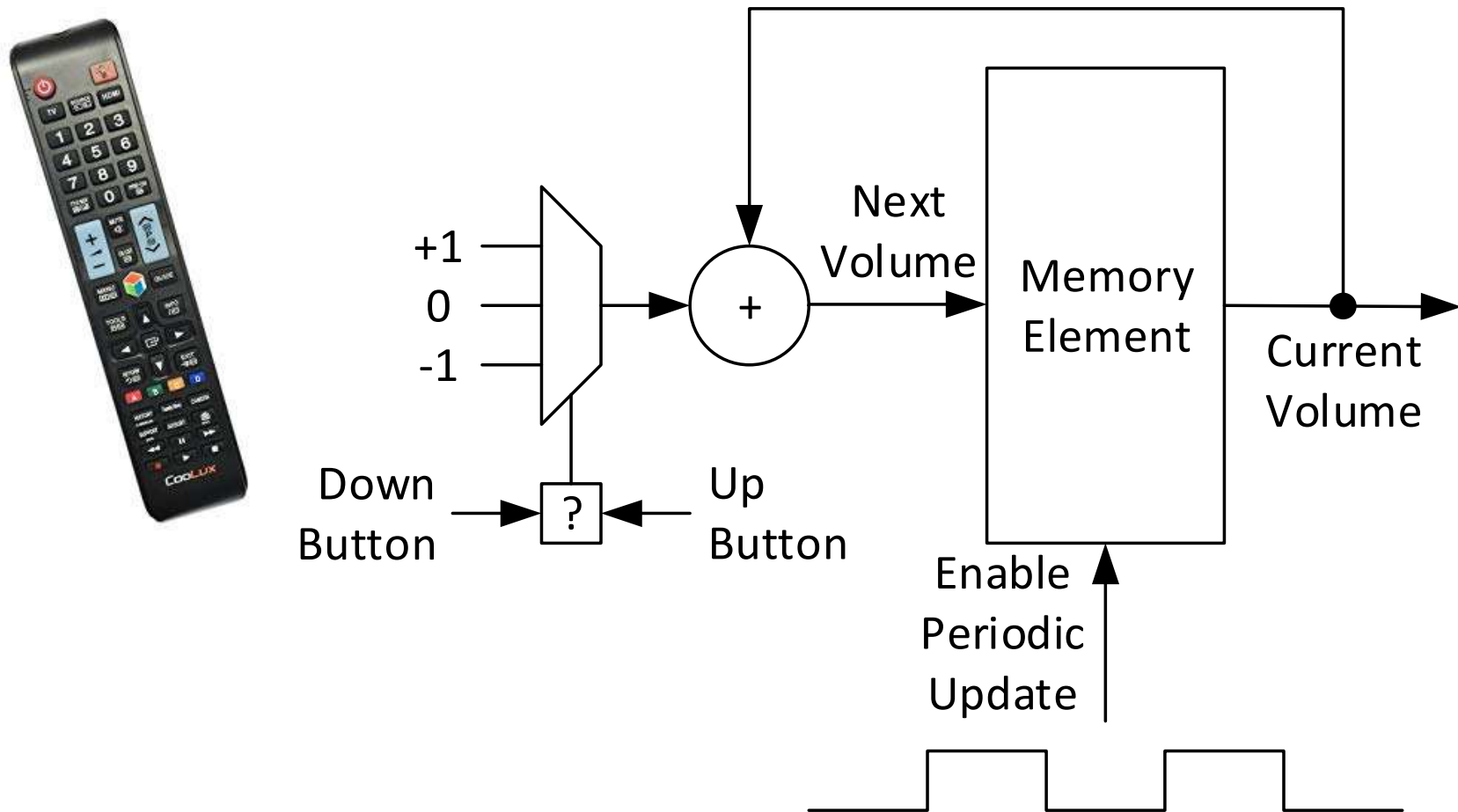
Arnaldo Oliveira, Augusto Silva, Iouliia Skliarova

Lecture Contents

- Sequential logic circuits fundamentals
 - Motivation and concepts
- Sequential logic basic circuits (memory elements built with ordinary gates and feedback loops)
 - S-R Latch
 - D Latch
 - D Flip-flop

Figures and most content extracted from: John F. Wakerly, “Digital Design – Principles and Practices”, 4 ed., Pearson – Prentice Hall, 2006 (chapter 7). Reading chapter 7 (4th ed.) or chapter 10 (5th ed.) is highly recommended.

Sequential Circuit Example

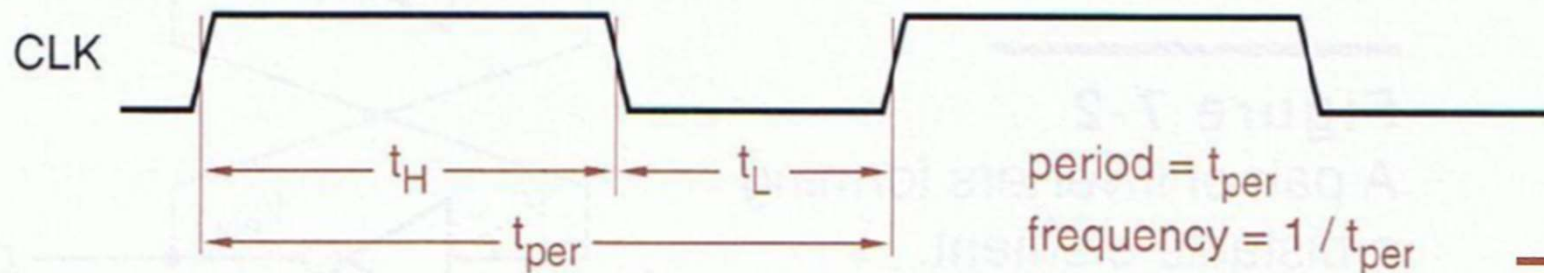
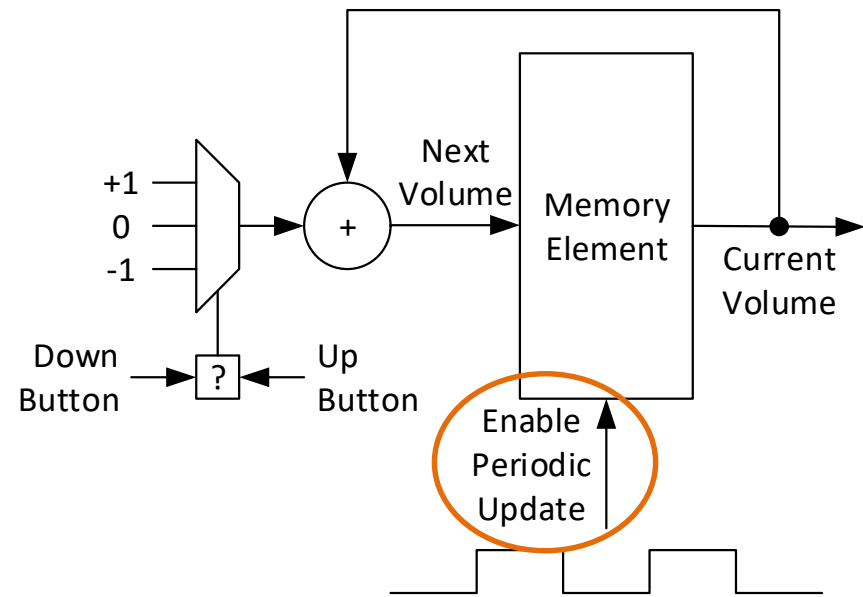


Introduction

- **Combinatorial** logic circuit
 - Is one whose outputs depend only on its current inputs
- **Sequential** logic circuit
 - Is one whose outputs depend not only on its current inputs, but also on the past sequence of inputs, possibly far back in time
- **State** of a sequential circuit
 - Is a collection of state variables whose values at any one time contain all the information about the past, necessary to account for the circuit's future behavior
- N-bit state variable: 2^N maximum number of states

Clock Signals

- State changes of most sequential circuits occur at times specified by a free-running clock signal
- Active high / active low clock signals



$$\begin{aligned}\text{period} &= t_{per} \\ \text{frequency} &= 1 / t_{per} \\ \text{duty cycle} &= t_H / t_{per}\end{aligned}$$

Figure 7-1
Clock signals:

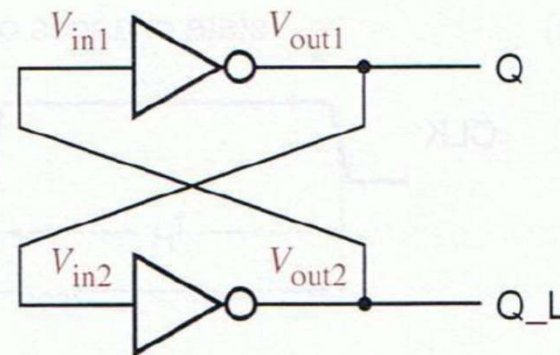


Bistable Element (Basic Structure)

- No inputs and therefore no way of controlling or changing its state (random set at power up)
- Only illustrative but serves the basis for more complex and useful memory elements

Figure 7-2

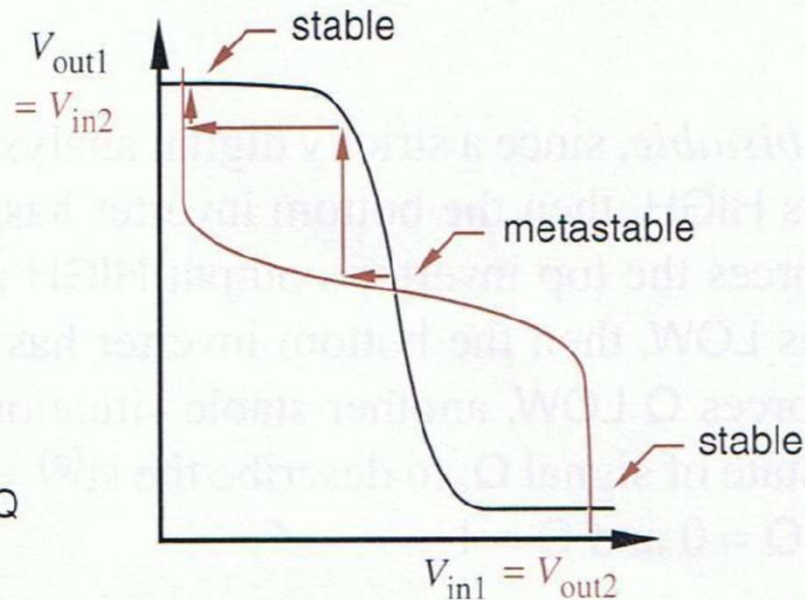
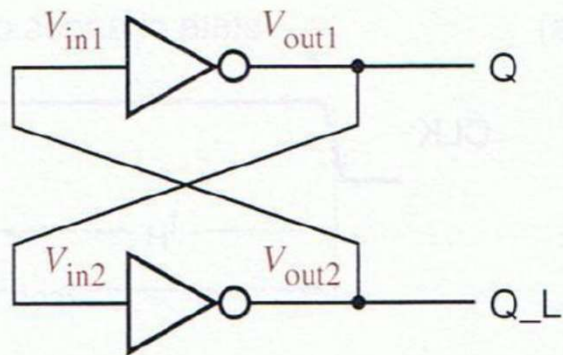
A pair of inverters forming a bistable element.



Bistable Element (Analog Analysis)

Figure 7-3

Transfer functions for inverters in a bistable feedback loop.



Transfer function:

$$V_{out1} = T(V_{in1})$$

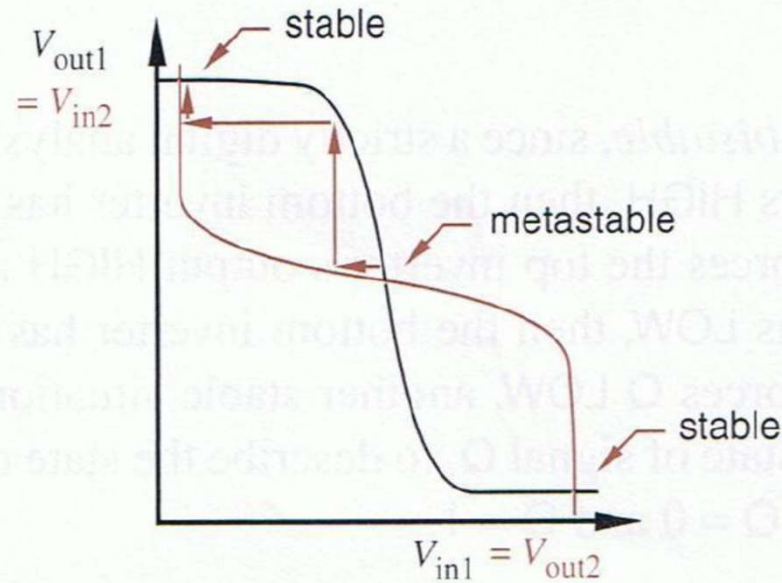
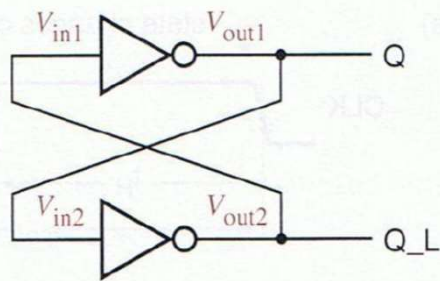
$$V_{out2} = T(V_{in2})$$

$$\begin{aligned} V_{in1} &= V_{out2} \\ &= T(V_{in2}) \\ &= T(V_{out1}) \\ &= T(T(V_{in1})) \end{aligned}$$

3 equilibrium points: 2 stable and 1 metastable

Metastability

Figure 7-3
Transfer functions for inverters in a bistable feedback loop.



Transfer function:

$$V_{out1} = T(V_{in1})$$

$$V_{out2} = T(V_{in2})$$

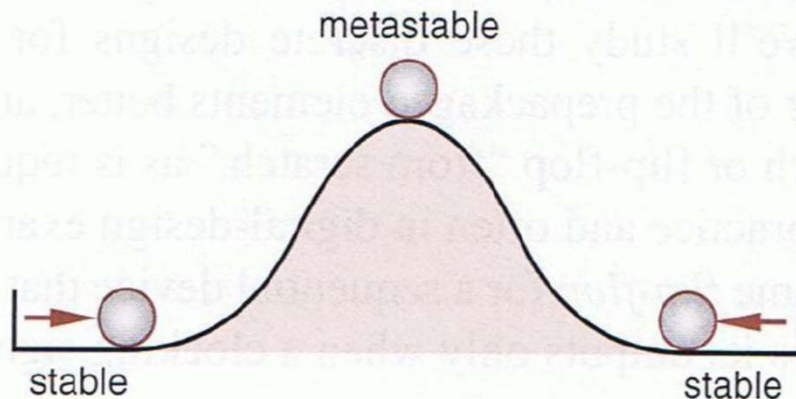


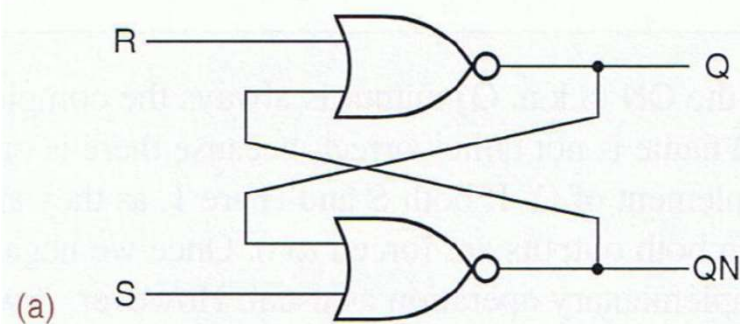
Figure 7-4
Ball and hill analogy for metastable behavior.

Effects of noise and circuit impairments on metastability



S-R Latch

(Structure and Function Table)



(b)

S	R	Q	QN
0	0	last Q	last QN
0	1	0	1
1	0	1	0
1	1	0	0

Figure 7-5
S-R latch: (a) circuit design using NOR gates; (b) function table.

S-R Latch

(Operation/Timing Diagrams)

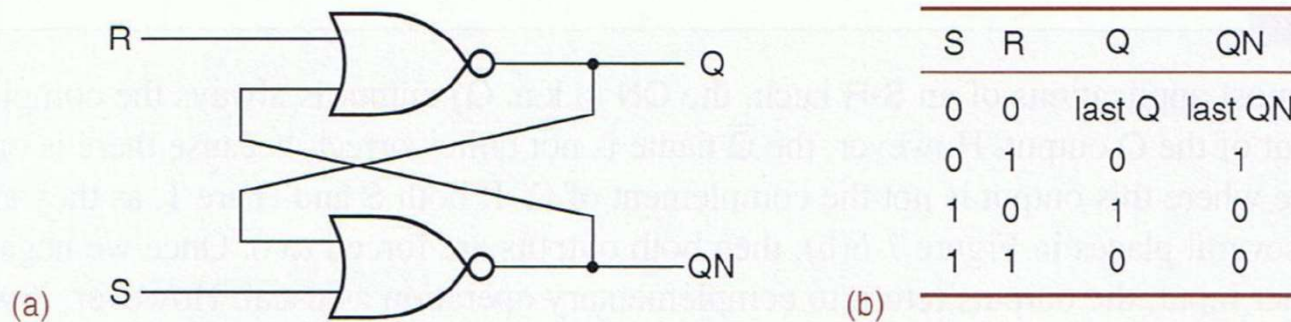
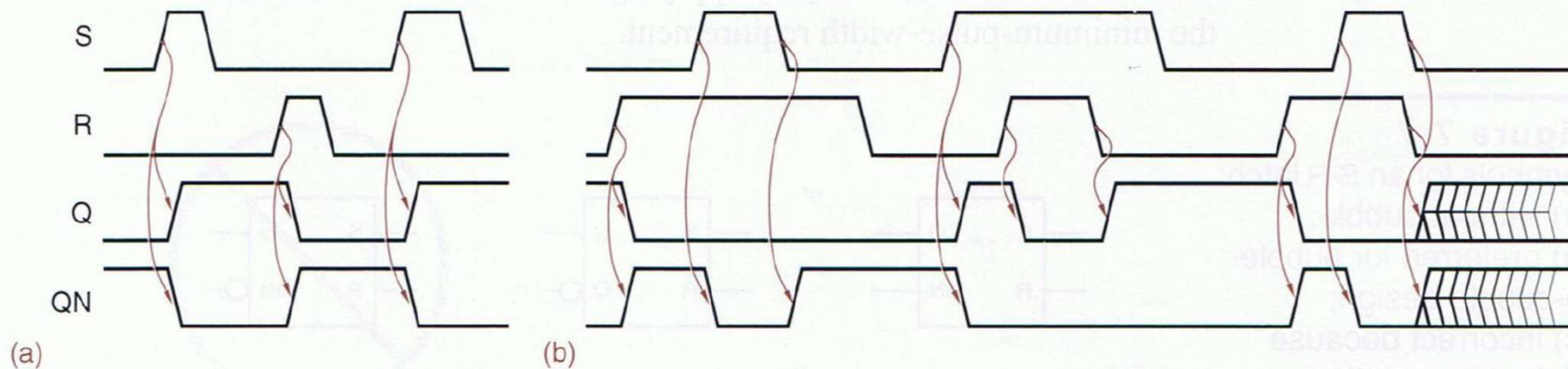
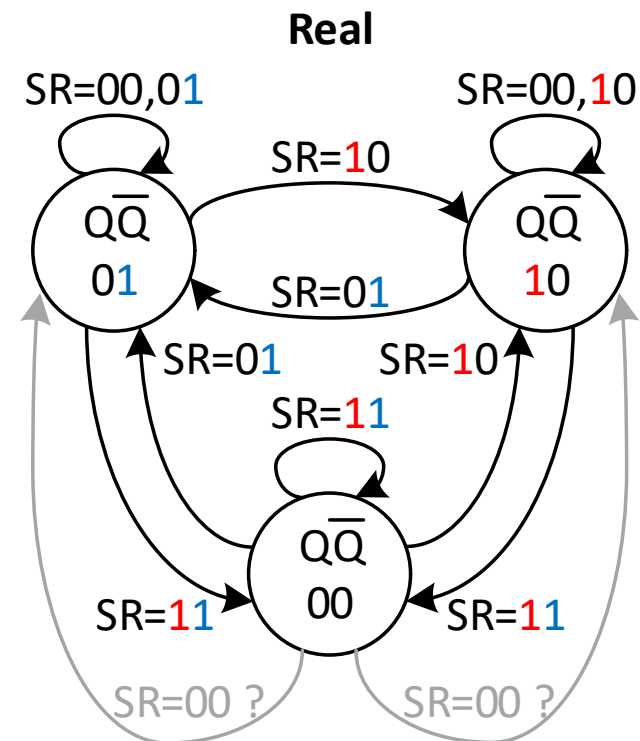
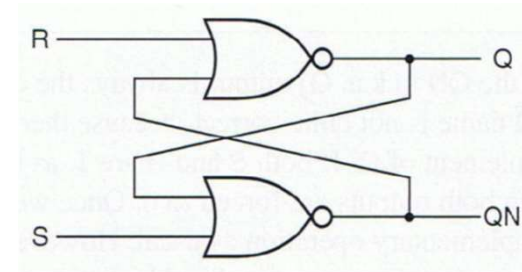
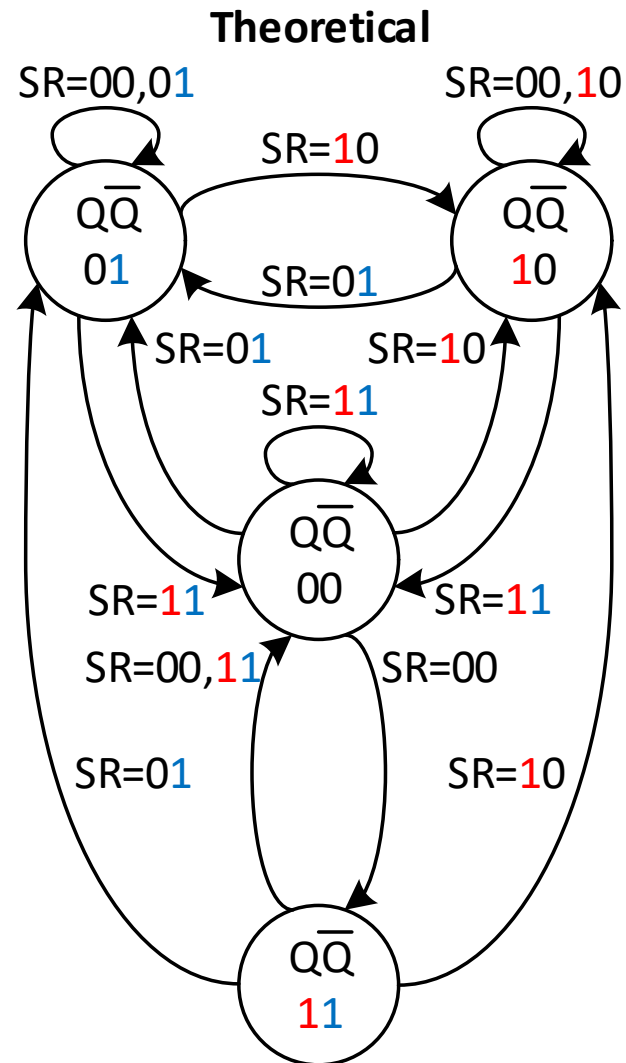


Figure 7-5
S-R latch: (a) circuit design using NOR gates; (b) function table.

Figure 7-6 Typical operation of an S-R latch: (a) “normal” inputs; (b) S and R asserted simultaneously.

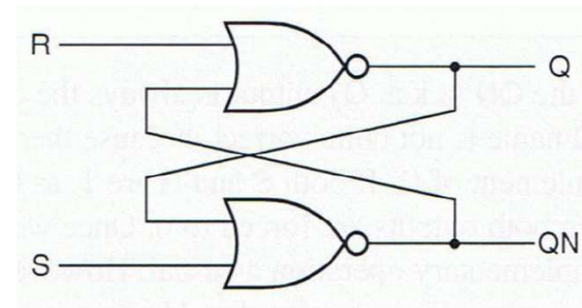
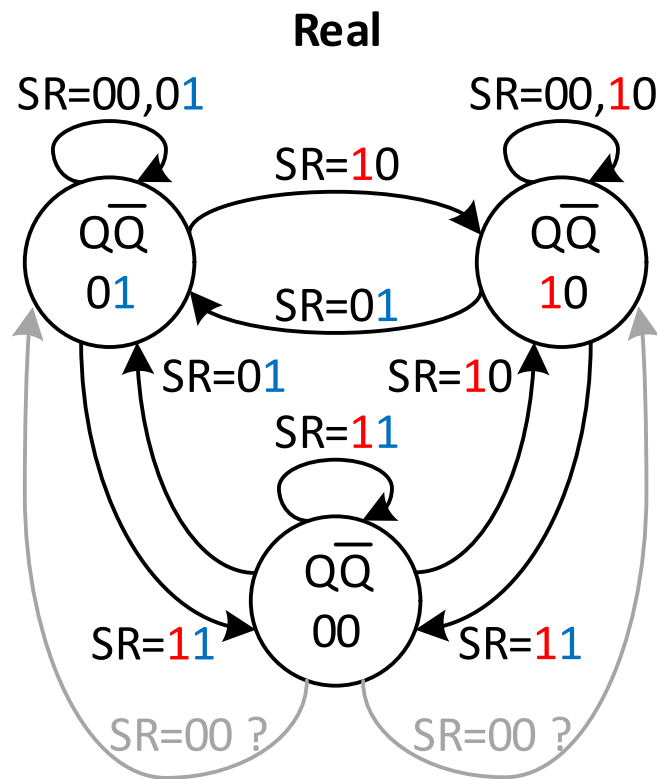


S-R Latch (State Diagram)



S-R Latch

(Characteristic Equation)



SR	00	01	11	10
Q				
0	0	0	X	1
1	1	0	X	1

$$Q^+ = S + \bar{Q}.R$$



S-R Latch (Symbol)

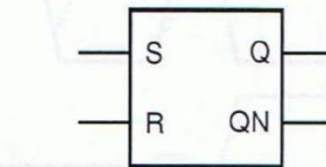
Figure 7-7

Symbols for an S-R latch:

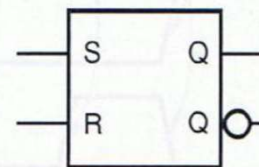
(a) without bubble;

(b) preferred for bubble-to-bubble design;

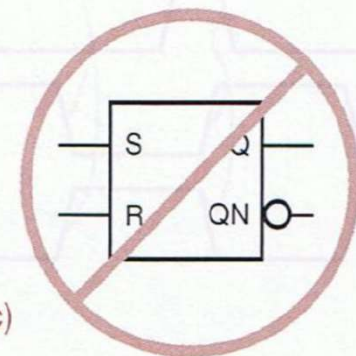
(c) incorrect because of double negation.



(a)

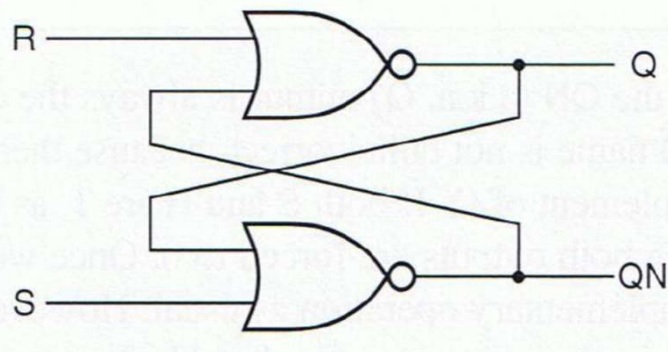


(b)



(c)

S-R Latch (Timing Parameters)



- t_{pLH} – propagation time LOW-to-HIGH
- t_{pHL} – propagation time HIGH-to-LOW
- $T_{pw(min)}$ – minimum pulse width

Non-determinism/metastability due to violation of $T_{pw(min)}$

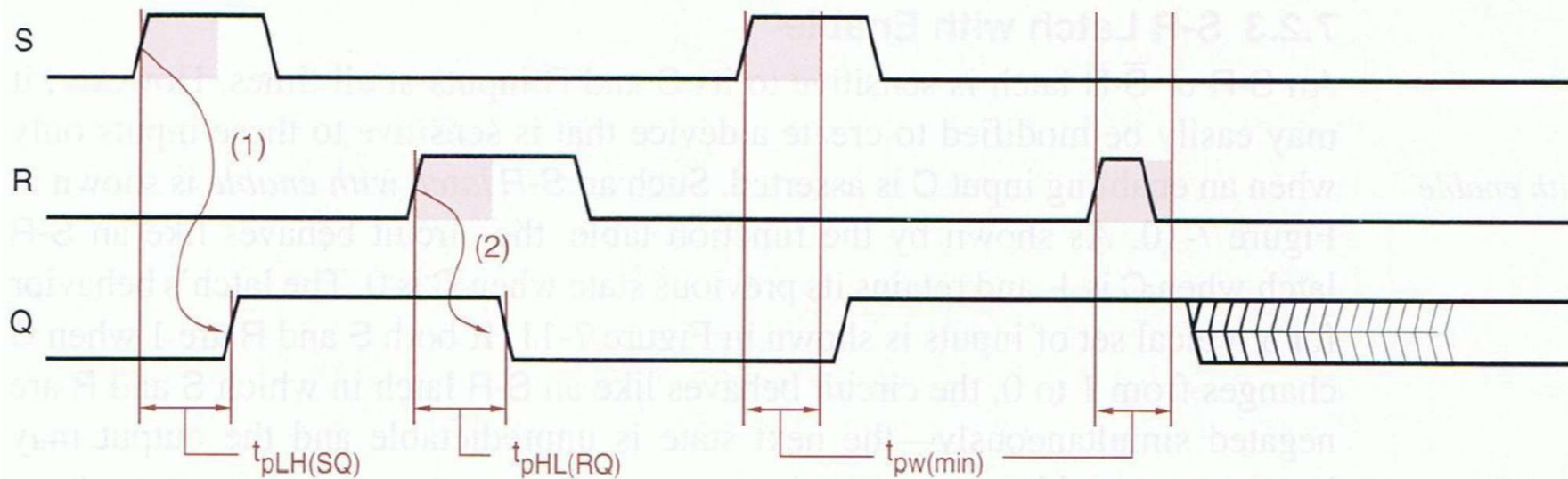
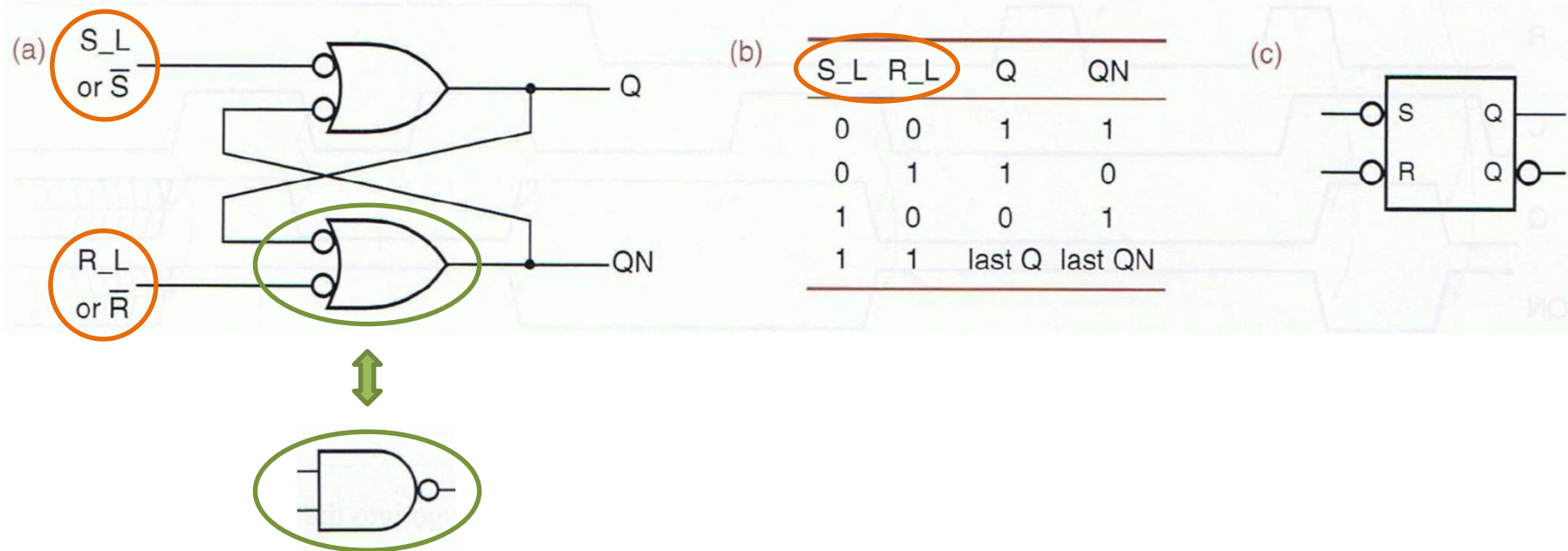


Figure 7-8 Timing parameters for an S-R latch.

S-R Latch (with NAND Gates)

Figure 7-9 $\bar{S}\text{-}\bar{R}$ latch: (a) circuit design using NAND gates; (b) function table; (c) logic symbol.



S-R Latch with Enable (C)

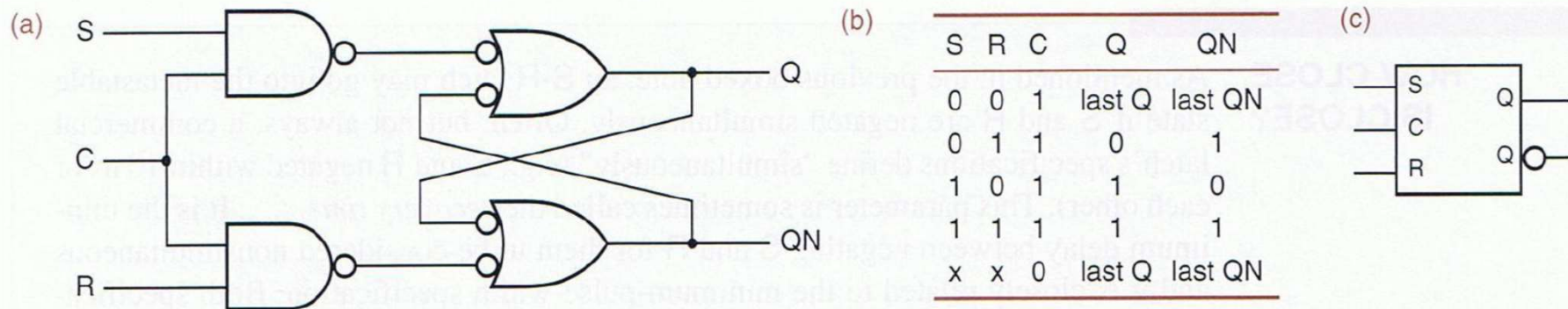


Figure 7-10 S-R latch with enable: (a) circuit using NAND gates; (b) function table; (c) logic symbol.

S-R Latch with Enable (Operation)

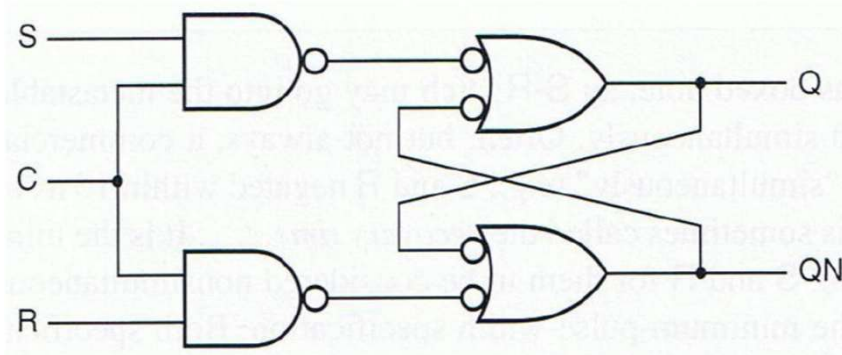
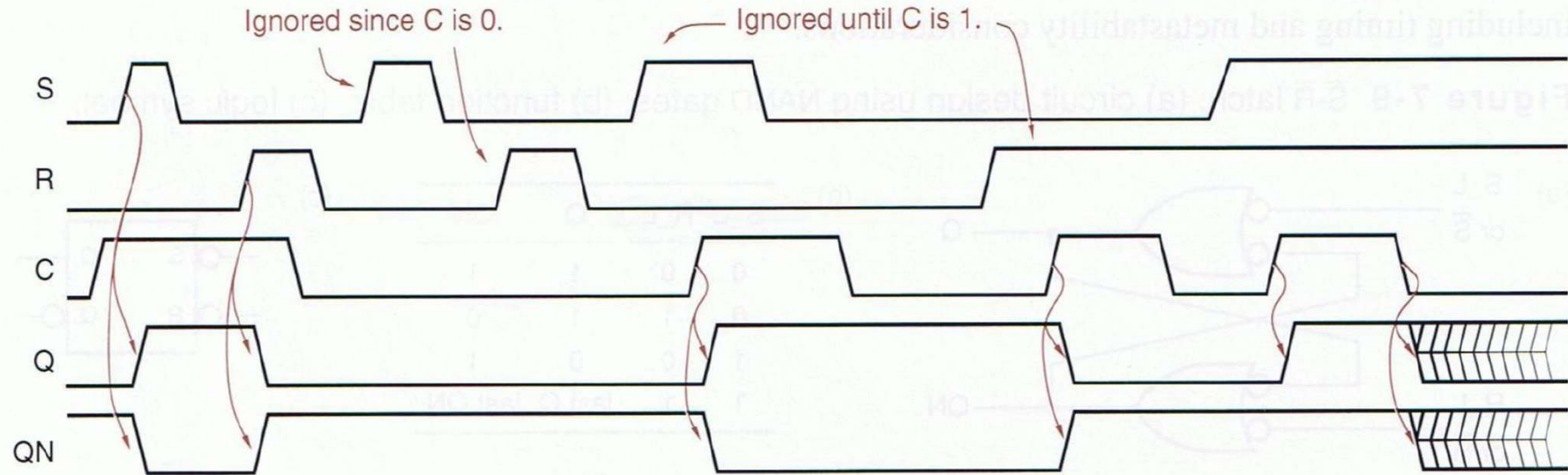


Figure 7-11 Typical operation of an S-R latch with enable.



D Latch (Structure and Operation)

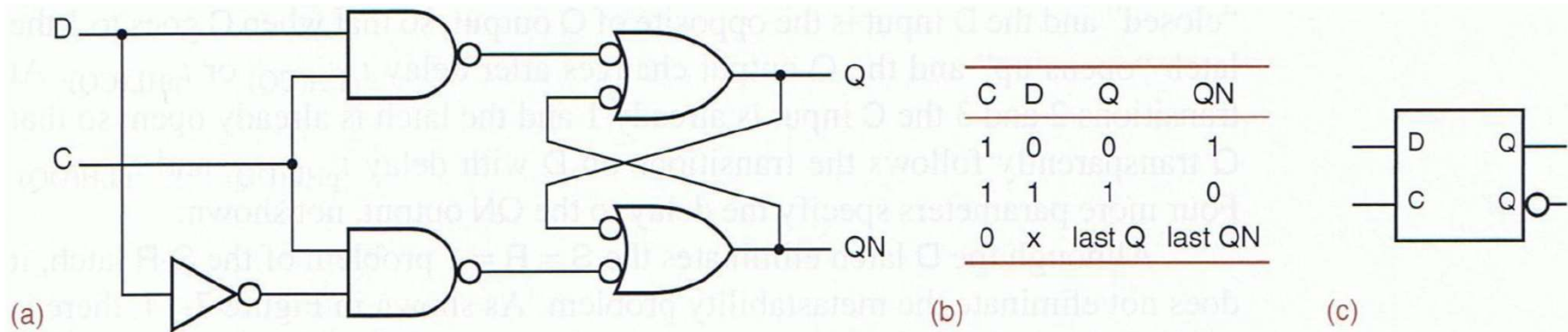


Figure 7-12 D latch: (a) circuit design using NAND gates; (b) function table; (c) logic symbol.

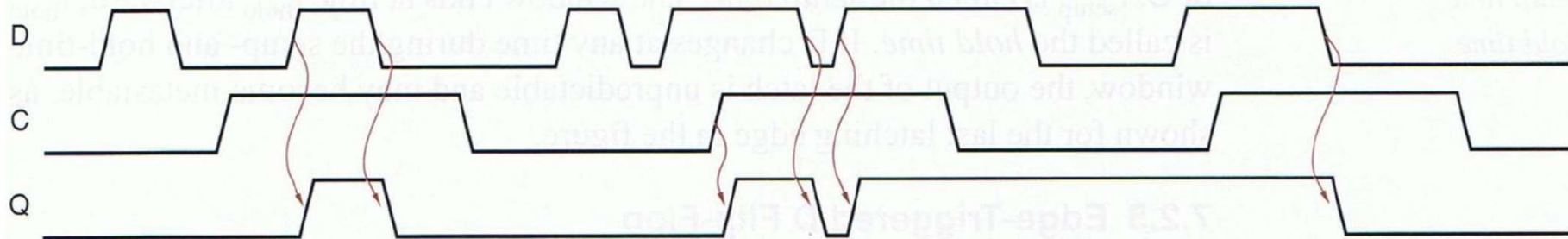
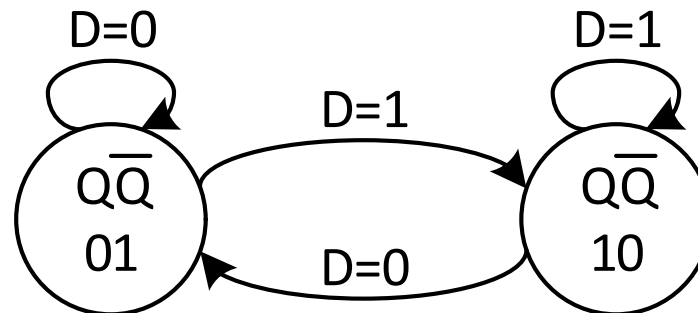
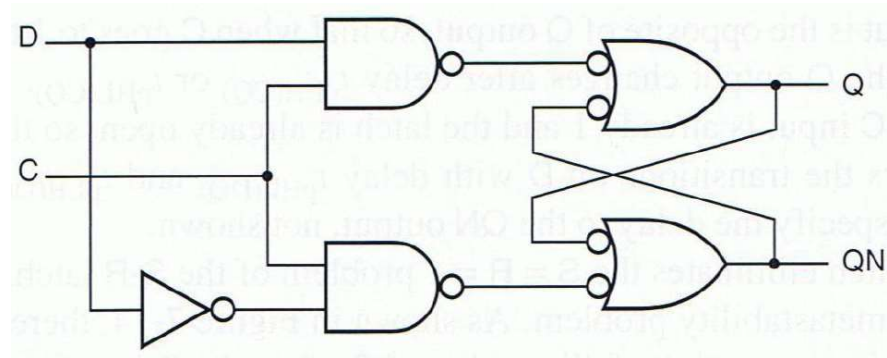


Figure 7-13 Functional behavior of a D latch for various inputs.

D Latch

(State Diagram and Characteristic Equation)

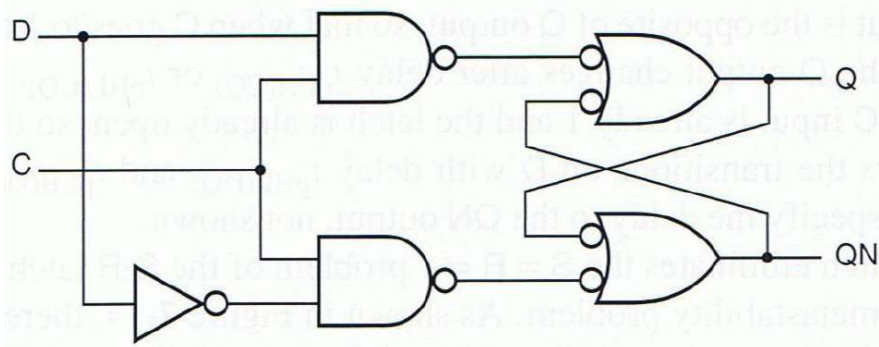


D	0	1
Q		
0	0	1
1	0	1

$$Q^+ = D$$



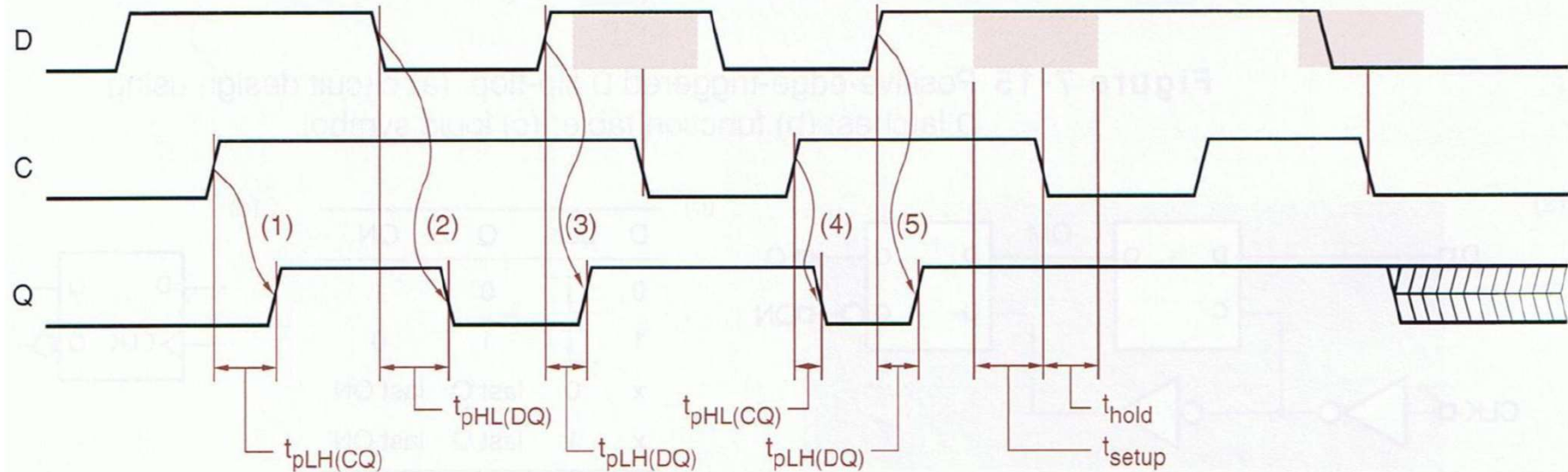
D Latch (Timing Parameters)



- t_{pLH} – propagation time LOW-to-HIGH
- t_{pHL} – propagation time HIGH-to-LOW
- t_{setup} – setup time
- t_{hold} – hold time

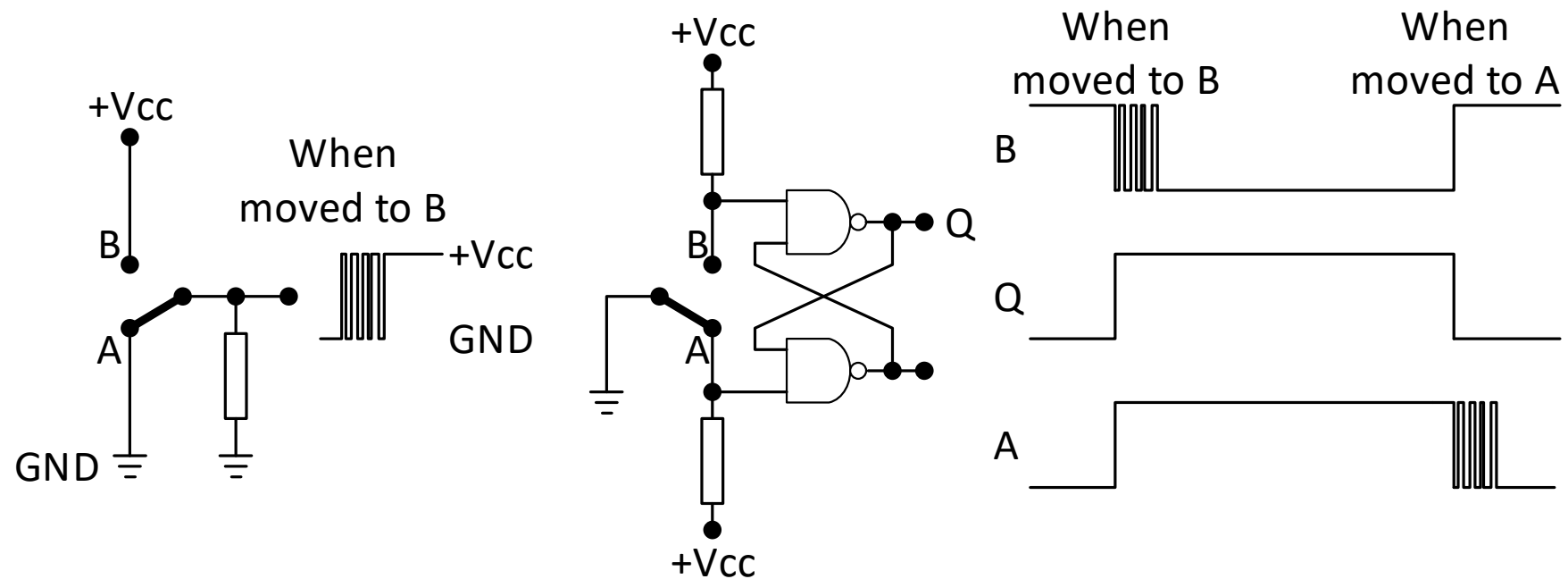
Non-determinism/metastability due to violation of t_{setup} and/or t_{hold}

Figure 7-14 Timing parameters for a D latch.

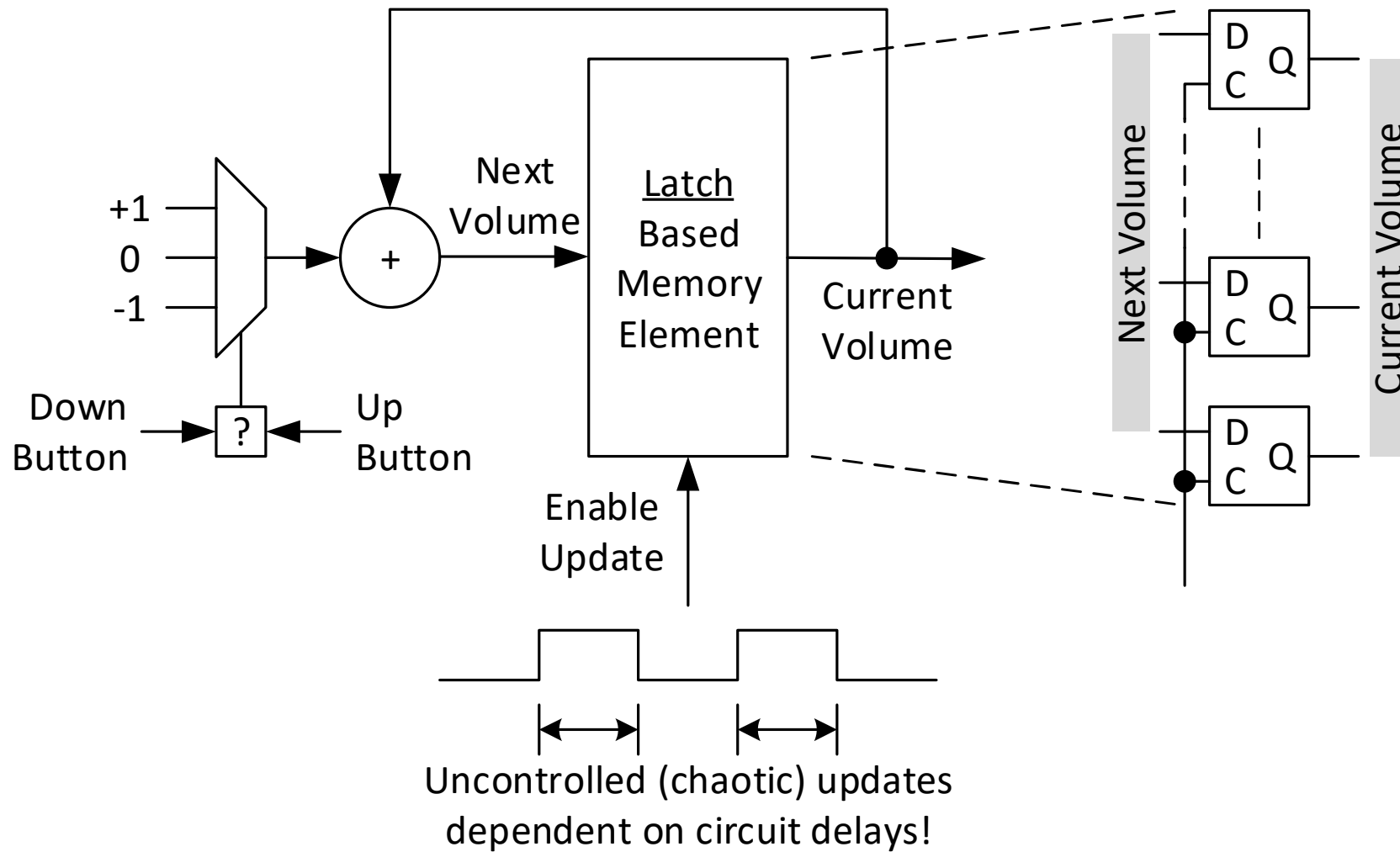


Application Example of an S-R Latch

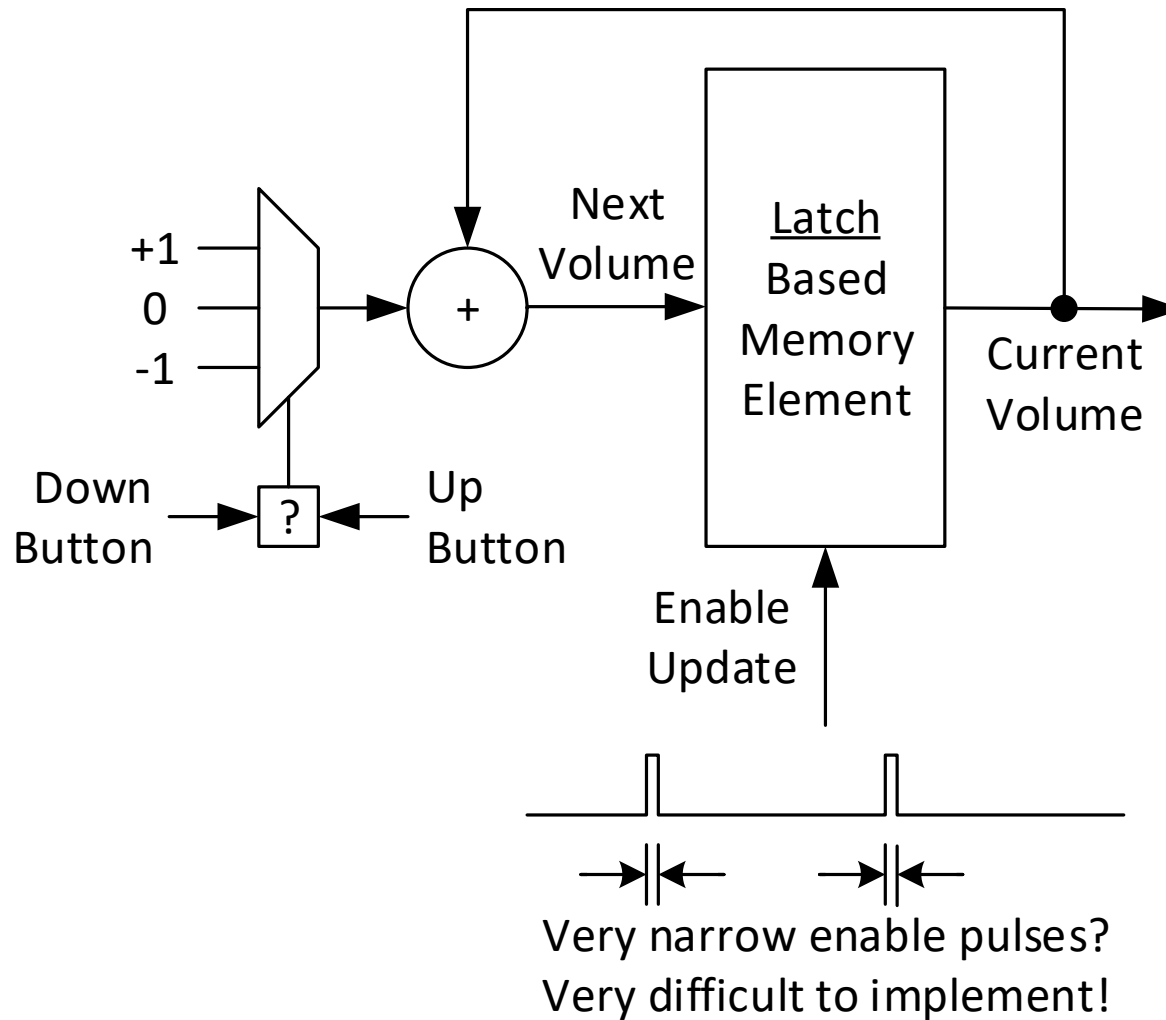
Debounce mechanical switches



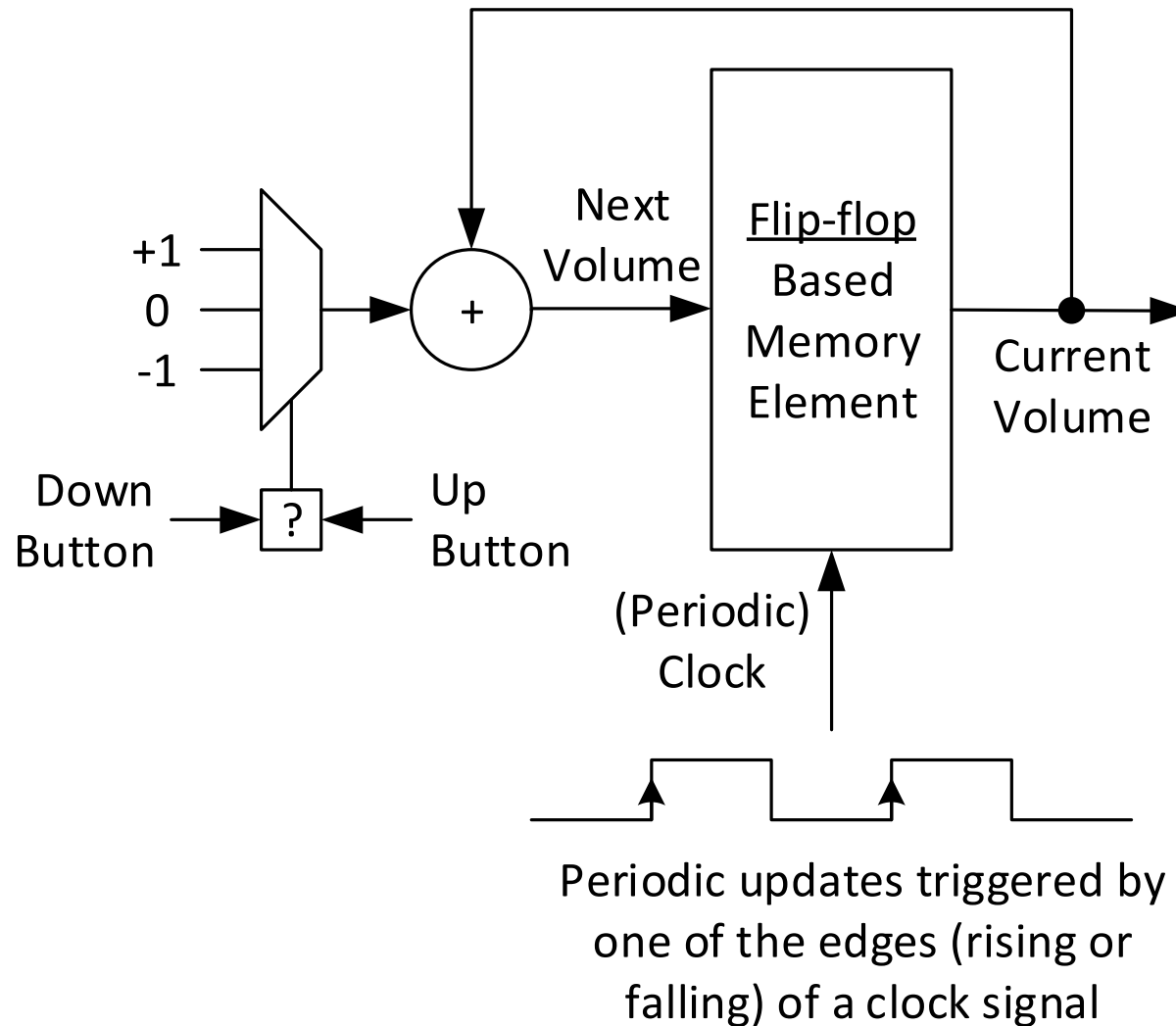
Latch Limitations/Issues



Possible Solution? Unfeasible!



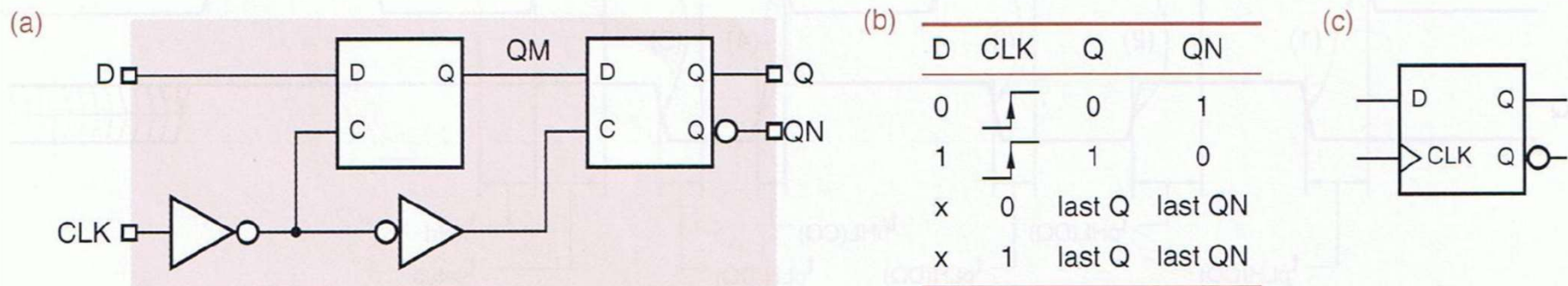
A Feasible Solution



Positive-edge-triggered D Flip-flop

Latches are not used frequently standalone but are a fundamental building block for flip-flops

Figure 7-15 Positive-edge-triggered D flip-flop: (a) circuit design using D latches; (b) function table; (c) logic symbol.



Clock Signals (revisited)

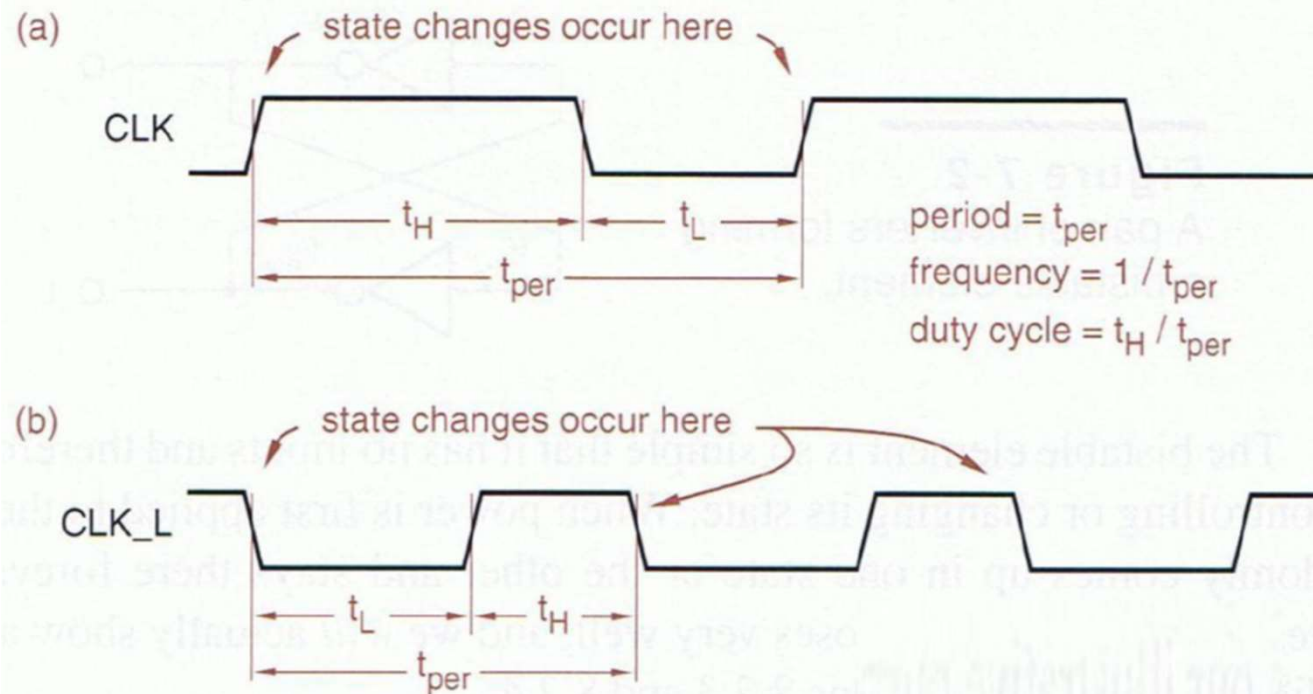


Figure 7-1
Clock signals:
(a) active high;
(b) active low.

Positive-edge-triggered D Flip-flop (Functional Behavior / Operation)

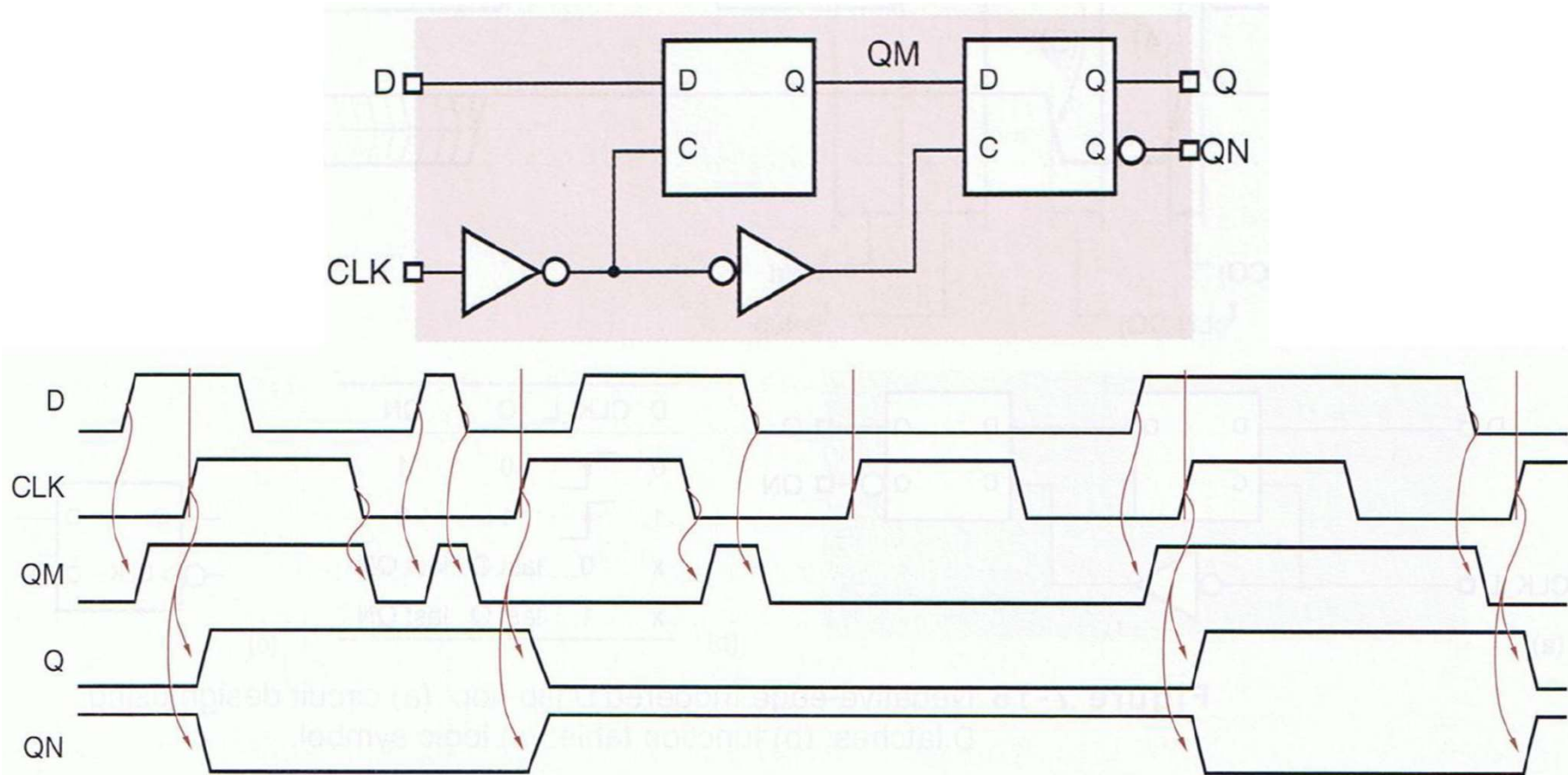
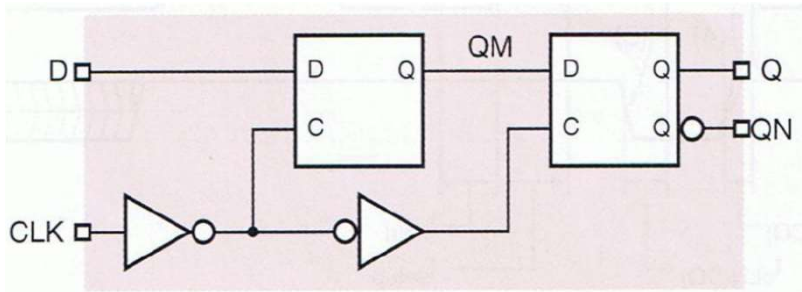


Figure 7-16 Functional behavior of a positive-edge-triggered D flip-flop.

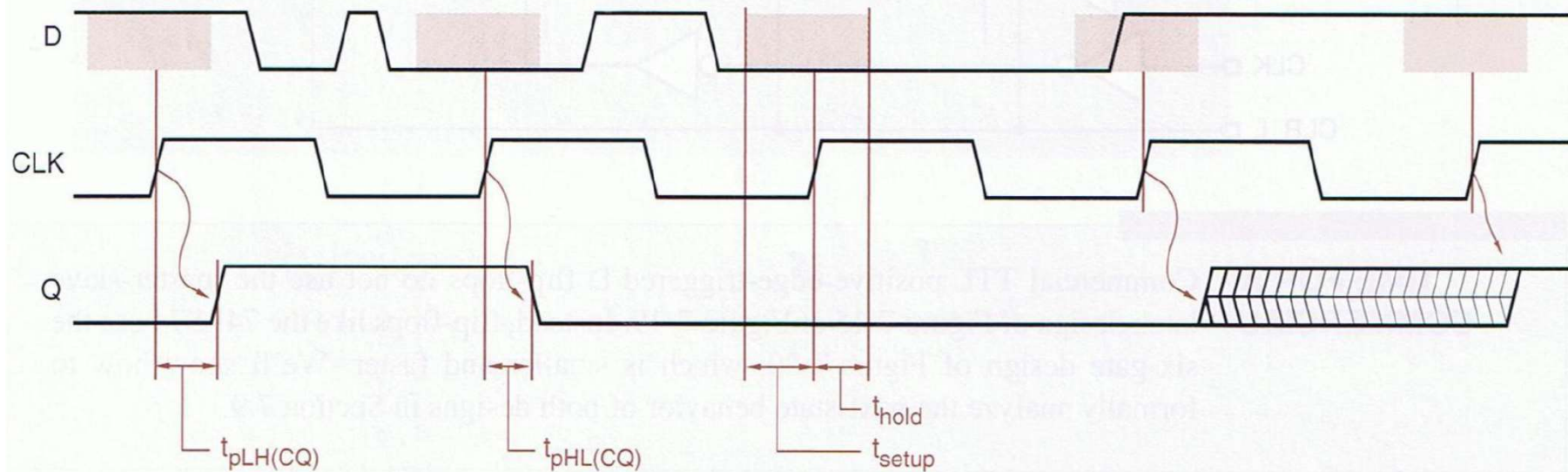
Positive-edge-triggered D Flip-flop (Timing Behavior)



- t_{pLH} – propagation time LOW-to-HIGH
- t_{pHL} – propagation time HIGH-to-LOW
- t_{setup} – setup time
- t_{hold} – hold time

Non-determinism/metastability due to violation of t_{setup} and/or t_{hold}

Figure 7-17 Timing behavior of a positive-edge-triggered D flip-flop.



Negative-edge-triggered D Flip-flop

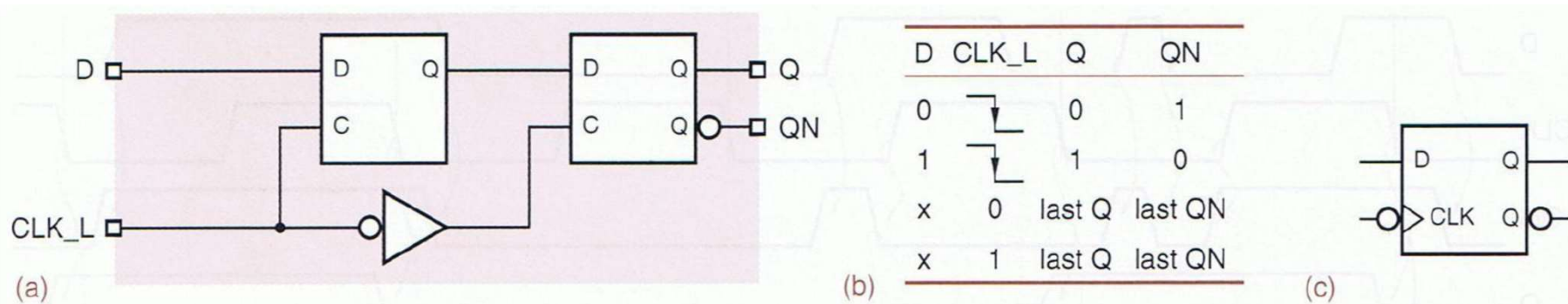
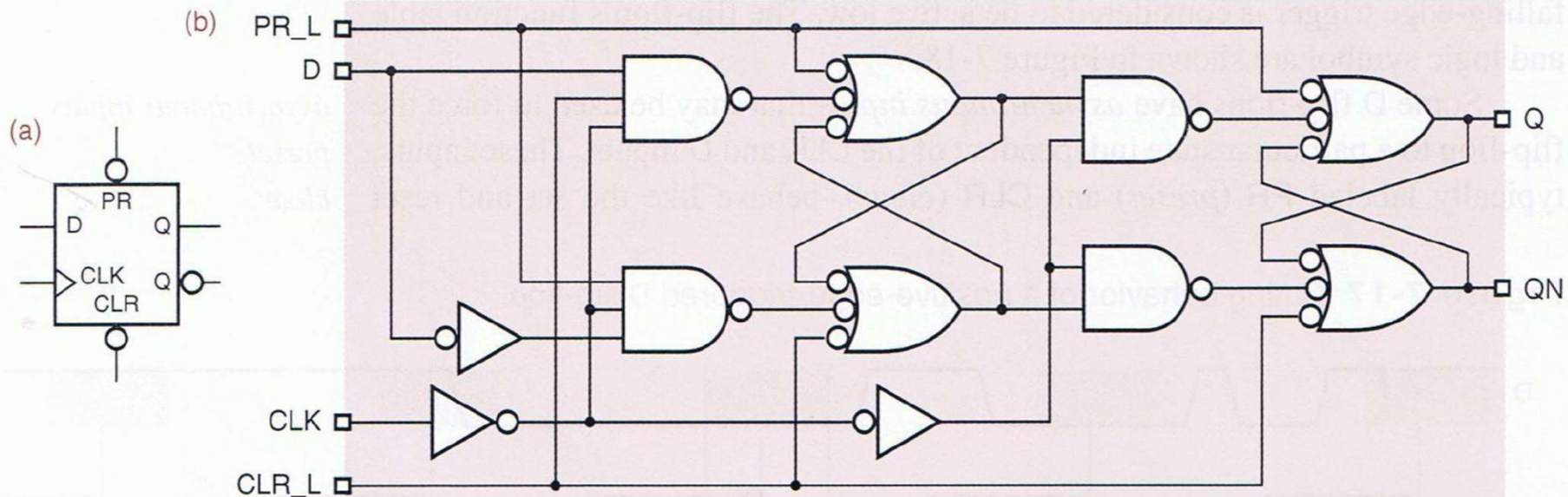


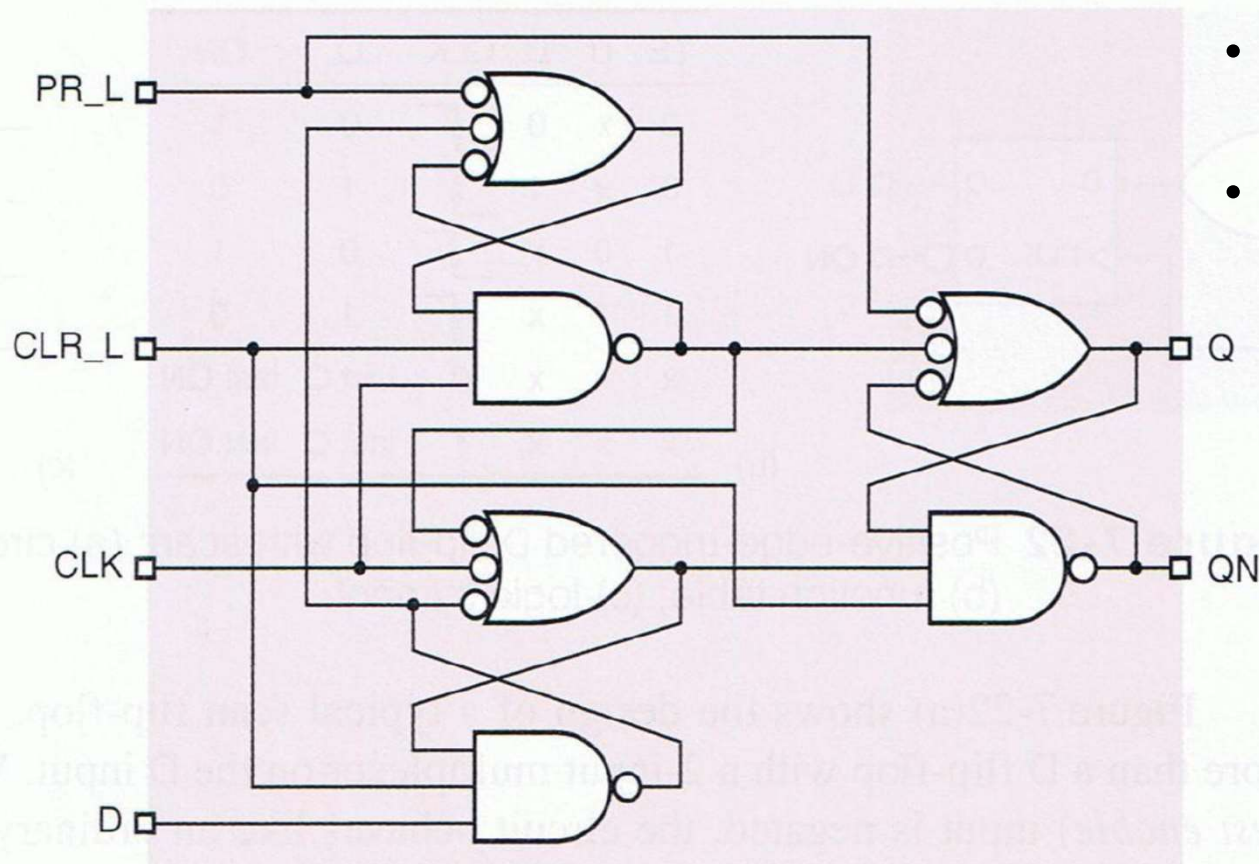
Figure 7-18 Negative-edge triggered D flip-flop: (a) circuit design using D latches; (b) function table; (c) logic symbol.

Positive-edge-triggered D Flip-flop with Preset and Clear

Figure 7-19 Positive-edge-triggered D flip-flop with preset and clear:
(a) logic symbol; (b) circuit design using NAND gates.



Positive-edge-triggered D Flip-flop (7474 Commercial Integrated Circuit)



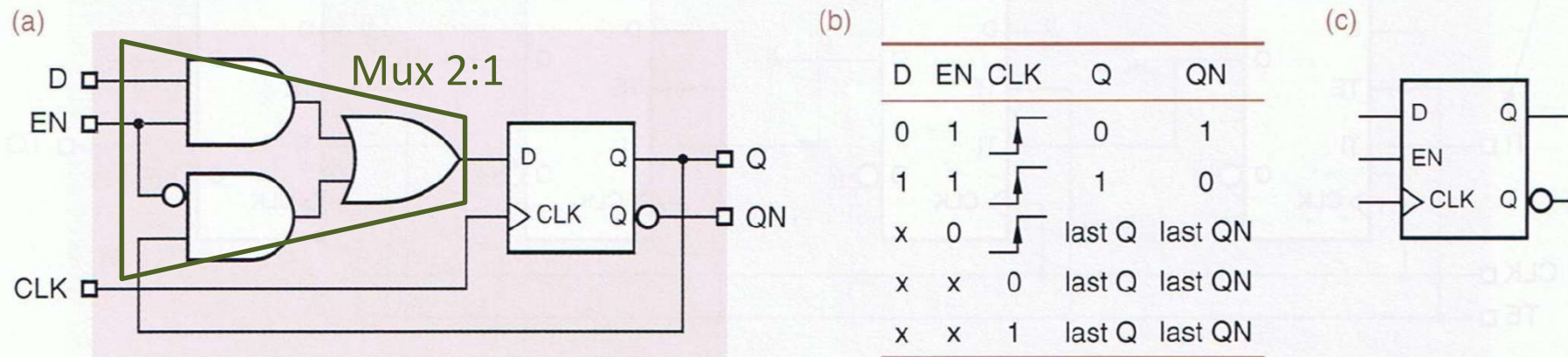
- 6 gates instead of 8 gates + inverters
- To be analyzed later...

Figure 7-20
Commercial circuit for
a positive-edge-
triggered D flip-flop
such as 74LS74.



Positive-edge-triggered D Flip-flop with Enable

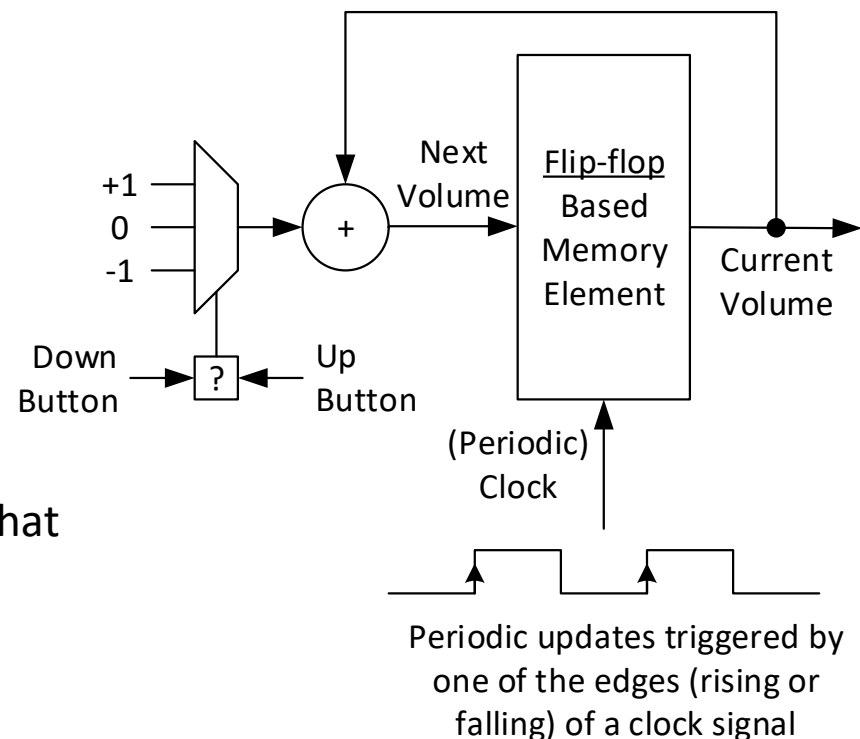
Figure 7-21 Positive-edge-triggered D flip-flop with enable: (a) circuit design; (b) function table; (c) logic symbol.



Exercise

- Design the complete logic diagram of the volume control system based on positive-edge-triggered D Flip-flops with enable (assume 16 levels of volume).
- Component budget

- Flip-flops
- Adder
- Mux 2:1
- Logic gates



- From the usability point of view, what could be the clock frequency?
- How to force a predefined volume level (e.g. half scale) at power up?



Conclusion

- At the end of this lecture and corresponding lab, it is fundamental to know and understand the structure, operation and timing behavior of basic sequential logic circuits (latches and flip-flops)
- Plan for the next lectures
 - Analysis of sequential circuits (Finite State Machines) and timing aspects
 - Synthesis of sequential circuits (Finite State Machines)
 - Standard sequential circuits
 - Registers and shift registers
 - Counters
 - Iterative vs. sequential circuits

Reading chapter 7 (4th ed.) or chapter 10 (5th ed.) of *John F. Wakerly, "Digital Design – Principles and Practices", Pearson – Prentice Hall, is highly recommended.*