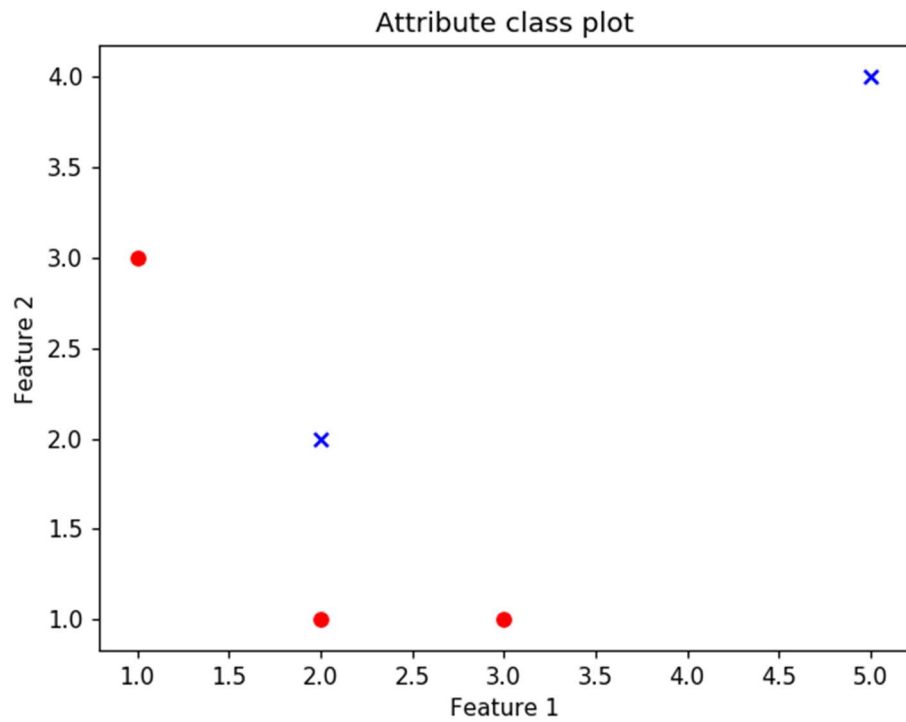


TPC4

1.

a)



Given that the red circles are $a=0$ and blue crosses $a=1$, we can verify that this data is not linearly separable, because it is not possible to “draw” a line that separates the data by feature.

b) Using the following gradient formula as role model:

$$\frac{\partial \log L(\mathcal{D})}{\partial \beta_0} = \sum_{n=1}^N (\pi(1 | x_n) - a_n)$$

$$\frac{\partial \log L(\mathcal{D})}{\partial \beta_1} = \sum_{n=1}^N x_n (\pi(1 | x_n) - a_n)$$

For the first weight $\beta_0 = 0$, we calculate the first gradient which gave a value of 0.5 and its corresponding new weight (using gradient descent): -0.5. We used the top formula from above, because this weight doesn't depend on any attribute.

For the second and third weight, $\beta_1=0$, $\beta_2=0$, we also calculate the gradient which gives a value of -0.5 each and its corresponding new weights (using gradient descent) 0.5 each. We used the bottom formula from above, because this weight depends on its attributes.

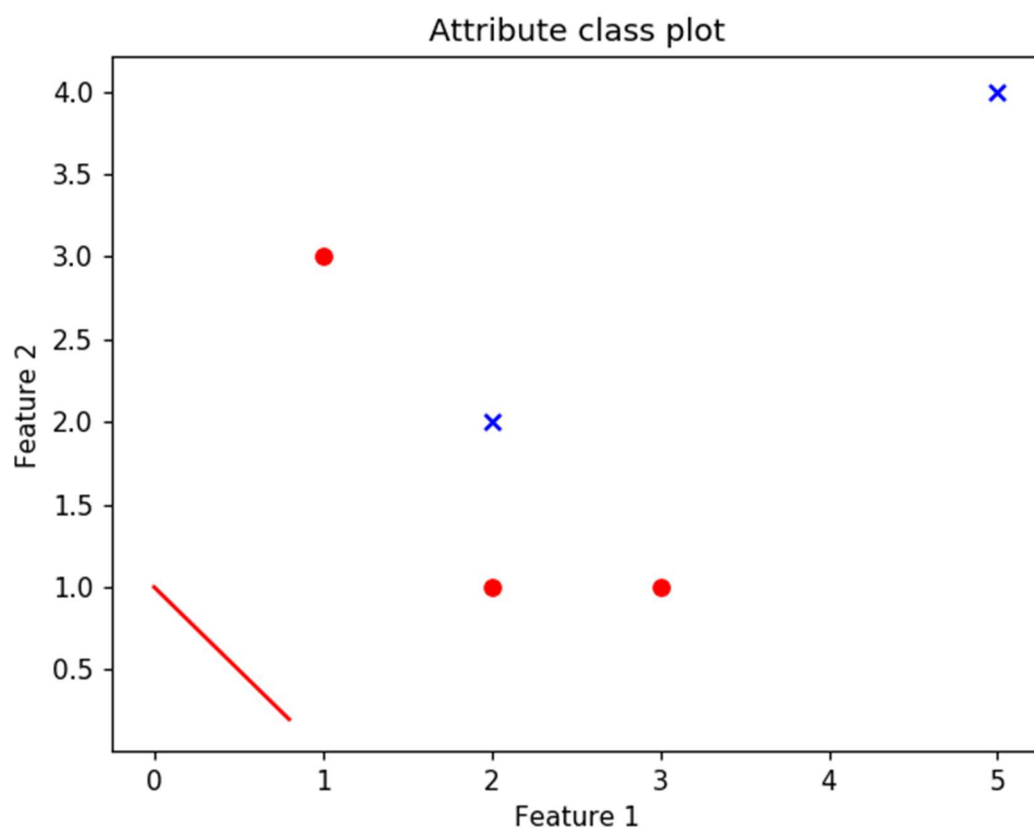
Giving the following recalculated weights:

$\beta_0 = -0.5$

$\beta_1 = 0.5$

$\beta_2 = 0.5$

c)



We can verify, that it does not properly classify the data.

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