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71.71 (I)

a	b	c	$a \wedge b$	$b \vee c$	$a \wedge (b \vee c)$
T	T	T	T	T	T
T	T	F	T	T	T
T	F	F	F	F	F
F	F	F	F	F	F
F	F	T	F	T	F
F	T	T	F	T	F
F	T	F	F	T	F
T	F	T	T	T	T

(II)

a	b	c	\wedge	\vee	\wedge	$(a \wedge b) \vee (a \wedge c)$
T	T	T	T	T	T	T
T	T	F	T	T	F	T
T	F	F	F	F	F	F
F	F	F	F	F	F	F
F	F	T	F	F	F	F
F	T	T	F	F	F	F
F	T	F	F	F	F	F
T	F	T	F	T	T	T

(I) = (II)



1.2 ①

2

a	b	c	v	Λ	$a \vee (b \wedge c)$
T	T	T	T	T	T
T	T	F	T	F	T
T	F	F	T	F	T
F	F	F	F	F	F
F	F	T	F	F	F
F	T	T	T	T	T
T	F	T	T	F	T
F	T	F	F	F	F

②

a	b	c	v	Λ	Λ	$(a \vee b) \wedge (a \wedge c)$
T	T	T	T	T	T	T
T	T	F	T	T	T	T
T	F	F	T	T	T	T
F	F	F	F	F	F	F
F	F	T	F	F	T	F
F	T	T	T	T	T	T
F	T	F	T	F	F	F
T	F	T	T	T	T	T

①-② ✓

1.3

a	$a \vee a$
T	T
F	F

✓

1.4

a	$a \wedge a$
T	T
F	F

✓

Equivalences

$$\begin{aligned} 1) (a \vee b) \wedge c &\stackrel{?}{=} \neg(\neg(\neg a \wedge \neg c) \supset \neg c) \\ &\stackrel{?}{=} \neg(\neg\neg(a \vee b) \supset \neg c) \quad (2) \\ &\stackrel{?}{=} \neg((a \vee b) \supset \neg c) \quad (3) \\ &\stackrel{?}{=} \neg(\neg(a \vee b) \vee \neg c) \quad (4) \\ &\stackrel{?}{=} \neg\neg(a \vee b) \wedge \neg\neg c \quad (5) \\ &\stackrel{?}{=} (a \vee b) \wedge c \end{aligned}$$

✓

$$2) a \vee b \vee a \supset c$$

$$\begin{aligned} &\stackrel{?}{=} \neg(\neg b \wedge \neg a) \supset c \\ &\stackrel{?}{=} \neg\neg(b \vee a) \supset c \quad (2) \\ &\stackrel{?}{=} b \vee a \supset c \quad (3) \end{aligned}$$

2.5) ①

a	b	c	$\neg a$	$\neg b$	$(a \vee b) \wedge c$
T	T	T	F	F	T
T	T	F	F	F	F
T	F	F	F	T	F
F	F	F	T	T	F
F	F	T	T	F	F
F	T	T	T	F	T
T	F	T	F	T	T
F	T	F	T	F	F

②

a	b	c	$\neg a$	$\neg b$	$\neg c$	$\neg(\neg a \wedge \neg b) \supset \neg c$
T	T	T	F	F	F	T
T	T	F	F	F	T	F
T	F	F	F	T	T	F
F	F	F	T	T	T	F
F	F	T	T	F	T	F
F	T	T	T	F	F	T
F	T	F	T	T	F	F
T	F	T	F	T	F	T

① \equiv ②

$$2.3) a \vee (b \wedge a) \supset (c \wedge d) \vdash (c \supset d) \supset (\neg a \wedge \neg b) \vee \neg a$$

$$\rightarrow 4$$

$$(\neg c \vee \neg d) \supset (\neg a \wedge \neg b) \vee \neg a$$

$$\downarrow 4$$

$$\neg(\neg c \vee \neg d) \vee (\neg a \wedge \neg b) \vee \neg a$$

$$\downarrow 5$$

$$(\neg a \wedge \neg b) \vee \neg a \vee \neg(\neg c \vee \neg d)$$

$$\downarrow 2$$

$$(\neg a \wedge \neg b) \vee \neg a \vee \neg \neg c \wedge \neg \neg d$$

$$\downarrow 3$$

$$(\neg a \wedge \neg b) \vee \neg a \vee c \wedge d$$

$$\downarrow 3$$

$$\neg(\neg(\neg a \wedge \neg b) \vee \neg a) \vee c \wedge d$$

$$\downarrow 2$$

$$\neg(\neg(\neg a \wedge \neg b) \wedge \neg \neg a) \vee c \wedge d$$

$$\downarrow 3$$

$$\neg(\neg(\neg a \wedge \neg b) \wedge a) \vee c \wedge d$$

$$\downarrow 7$$

$$\neg(\neg \neg a \vee \neg \neg b \wedge a) \vee c \wedge d$$

$$\downarrow 3$$

$$\neg(a \vee b \wedge a) \vee c \wedge d$$

$$\downarrow 4$$

$$(a \vee b \wedge a) \supset (c \wedge d)$$

$$\downarrow 6$$

$$a \vee (a \wedge b) \supset c \wedge d$$