

# Option price with different volatility models

xiaoli\_209255438

5 Dec 2022

.pull-left[ ### Volatility models - **Standard deviation**]

.pull-right[ ### Option pricing models - **Simple Black-Scholes**

$$Call = Se^{-qt}N(d_1) - Ke^{-rt}N(d_2)$$

$$Put = Ke^{-rt}N(-d_2) - Se^{-qt}N(-d_1)$$

$$d_{1,2} = \frac{\log(\frac{S}{K}) + (r - q \pm \frac{\sigma^2}{2})t}{\sigma\sqrt{t}}$$

] — #Results

3month-call option on Apple Inc. with following parameter. - K = 120, S = 148.11R = 0.0421, T = 0.25, Q = 0.0061, Actual call price = 31.35

##		BSM_SD	BSM_EWMA	BSM_GARCH	BSM_SV	Actual
## 1	In-the-Money	26.74217757	27.1084363	26.91855601	30.34989122	31.35
## 2	Out-of--Money	0	1.129831294	0.6713966474	2.089795823	2.19

Conclude: - The results of standard deviation, EWMA, GARCH seems to be inaccurate. The most possible reason is that the calculation formula is based on European style, while the option provided by APPLE Inc.(AAPL) is American type. The actual trading option price must be higher than or equal to the results computed by Black-Scholes equation.

- Since the stochastic volatility models are calibrated to satisfy the implied volatility from the real market, the model capture the forward looking factors in the market. As a consequence, The Heston Model offers more precise prediction in option pricing.