

A Bayesian Reanalysis of Studies in Violent Media Research

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We thank Andrew Przybylski and Dirk Mügge for providing critiques of an early version of this manuscript.

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Abstract

Although many studies have reported statistically significant effects of violent video games on aggressive outcomes, the purported causal association remains controversial. This controversy stems in part from questions of experimental control. In typical experimental research, aggressive outcomes are measured after participants are randomly assigned to play a violent or nonviolent game, and differences between game groups are thought to represent the causal effect of violent video games. Proponents of violent-media effects argue that the violent and nonviolent games are matched on all dimensions besides violence, and so observed effects are due to violent content alone. Meanwhile, skeptics argue that the games are not well matched in most experiments, but that when they are, there is no effect of violence. Both sides in this argument require statistical evidence for the null hypothesis: proponents need to argue that confounding differences between games are zero, whereas skeptics need to argue that the effects of violent content are zero. However, this evidence cannot be provided by the traditional use of null-hypothesis significance testing. To evaluate these claims, we apply a more appropriate Bayesian analysis to measure evidence for or against the null hypothesis. We conclude that small-sample pilot tests cannot rule out substantial confounds. Furthermore, we find that studies that claim to find an absence of violent video game effects vary substantially in the strength of evidence, with some even finding some evidence of an effect. We recommend the use of Bayesian analyses, larger sample sizes, and the creation of custom-designed games for experimental research.

A Bayesian Reanalysis of Studies in Violent Media Research

Despite more than two decades of research, the scientific literature on whether violent video games cause aggressive outcomes remains divided and contentious. To date, this relationship has been examined in hundreds of individual studies and in aggregate by several different meta-analyses. Even the meta-analyses are divided and contentious—some argue that there is a meaningfully large effect (Anderson et al., 2010; Greitemeyer & Mügge, 2014) and others argue there is no meaningful effect (e.g., Ferguson & Kilburn, 2009; Sherry, 2001). Note here that both positions, that video game violence increases aggression and that video game violence has no effect on aggression, are theoretically important and *a priori* plausible. They both deserve serious and fair consideration.

A typical experiment in this literature tests for an effect of violence on aggressive outcomes by randomly assigning participants to play a violent or nonviolent video game. After gameplay, an aggressive outcome such as hostile affect, aggressive-word accessibility, or aggressive behavior is collected. The outcome is compared across groups to estimate an effect size and determine statistical significance. In theory, then, assessing the effect of violent video-game content should be straightforward, and there is little reason to expect such controversy.

One reason for the difficulty revolves around experimental control. Commercially-available violent and nonviolent video games are not typically designed to be exactly like one another except for violent content. Although the experimenter has experimental control over the video game a participant plays, the experimenter does not have experimental control over the content of the video game. This lack of control generates the possibility that the violent and nonviolent games differ in dimensions besides violent content. Such differences may constitute confounds which are responsible for observed post-play differences in aggressive outcomes. For example, if the violent game is also more arousing and more frustrating than the nonviolent game, these differences may cause increases in aggressive outcomes, even if violent content does not. Thus, violent

media experiments often begin with an attempt to demonstrate that the violent and nonviolent games are as similar as possible on all other dimensions so as to minimize the possibility of confounds and support the argument that the observed differences, if any, are due to violent content alone.

Some researchers have argued that the violent-video game effect is not due to violent content but to these other confounding factors. For example, Adachi and Willoughby (2011) argue that it is competition rather than violence that causes increases in aggressive behavior, and that matching game stimuli on competitive content eliminates the purported effect of violence. Elson, Bruer, Van Looy, Kneer, and Quandt (2013) argue that changes in aggressive behavior are caused by differences in pace of action rather than violent content. Przybylski, Deci, Rigby, and Ryan (2014) find that competence-impeding games can influence aggressive outcomes, but do not detect effects of violent content. Although these authors do not argue any inference regarding the effects of violent content, one might interpret these results as indicating an absence of an effect. Each of these arguments favors the position that under certain circumstances there is no effect of video game violence on aggression.

Statistical Arguments for the Null Hypothesis

Both proponents and skeptics of violent-game effects make arguments for the truth of the null hypothesis. Proponents argue for the null hypothesis when comparing two video games and arguing that they do not differ in potential confounds. Such a comparison is considered a success if the two games differ significantly in violent content but do not differ significantly in confounds. The nonsignificant test result is considered evidence for the truth of the null hypothesis. On the other hand, skeptics report conducting their own experiments and finding nonsignificant results of violent games on aggressive outcomes. Skeptics consider these statistics as providing evidence for the null hypothesis of no effect.

However, it can be difficult to use statistics to argue for the truth of the null

hypothesis. Null-hypothesis significance testing (NHST), the nearly ubiquitous approach for inference in psychological research, may not be used to state evidence for the null hypothesis that the true effect size is zero. In NHST, the probability of the data are evaluated given the assumption that there is no true effect. If the probability of the data or more extreme data is less than 1-in-20 ($p < .05$), the data are said to be sufficiently unusual given the null hypothesis of no effect, and the null hypothesis is rejected in favor of an alternative hypothesis of some effect.

NHST can be used to reject the null hypothesis in favor of an alternative hypothesis to infer evidence for an effect. It cannot, however, be used to reject the alternative hypothesis in favor of the null hypothesis. A p -value greater than .05 may reflect a true effect size of zero, but it also may reflect insufficient power to detect a true nonzero effect. Therefore, it is unknown whether the previously discussed null findings reflect evidence for the null hypothesis or a lack of power. Researchers need a method for stating positive evidence for the null rather than a lack of evidence for an effect.

In the present manuscript, we examine the strength of evidence for video game effects vs. a fairly-treated no-video-game-effect null. To do so, we present methods for Bayesian inference that allow researchers to state positive evidence for either hypothesis as determined by the data. In so doing, we will make frequent reference to effect sizes. Although effect sizes in this literature are often described in terms of the Pearson correlation ρ , we will typically convert such effect sizes to their equivalent values in terms of the standardized mean difference δ for the sake of simplicity and consistency.

First, we present these Bayesian methods and explain how they can be used not only to find evidence for effects of experimental factors, but also evidence for invariance (i.e., the null hypothesis) in outcomes with respect to experimental factors. Following this, we assess whether violent and nonviolent game stimuli appear to be well-matched by reanalyzing several exemplars of pilot studies in violent video game research for which necessary statistics were available. We then examine the strength of evidence for the lack

of an effect in those studies reporting no significant effect of violent content. Finally, results are summarized and used to inform practical suggestions offered for stronger, more informative research. The present manuscript is not intended as a systematic review, but the inferential problems we describe are found frequently throughout the literature.

Bayesian Inference

At the heart of being able to state evidence for an effect or for an invariance is Bayesian model comparison. Bayesian model comparison has a long history in statistics and even in psychology. Perhaps the first to suggest the methods we cover was Laplace (1829, republished in 1986), and seminal development occurred through World War II and was presented most comprehensively by Jeffreys (1961). Edwards, Lindman, and Savage (1963) were perhaps the first psychologists to recommend the approach and did so with uncommon gusto in their landmark *Psychological Review* article. The method has gained increasing popularity in statistics and psychology in recent years (Berger & Delampady, 1987; Gallistel, 2009; Raftery, 1995; Rouder, Speckman, Sun, Morey, & Iverson, 2009; Wagenmakers, 2007) and is rapidly becoming widespread, especially in cognitive domains. The main hurdle to adoption has often been the difficulty of computation and the unavailability of software (Gallistel, 2009), but these hurdles have been largely removed with Morey and Rouder’s (2014) BayesFactor library for the **R** statistics language and with the freeware statistics program JASP (<http://jasp-stats.com>).

In Bayesian analysis probabilities are used to confer a degree of belief on events, parameters, and even theoretically important positions. Analysts start with stated beliefs and then update those beliefs rationally and optimally using Bayes’ rule. For updating beliefs about positions, we use the following form of Bayes’ rule:

$$\frac{Pr(H_0|\text{Data})}{Pr(H_1|\text{Data})} = \frac{Pr(\text{Data}|H_0)}{Pr(\text{Data}|H_1)} \times \frac{Pr(H_0)}{Pr(H_1)} \quad (1)$$

It is best to start with the term on the far right, $Pr(H_0)/Pr(H_1)$ which is called the *prior*

odds. This term describes the researcher's beliefs about the plausibility of the positions before collecting the data. The term on the left, $Pr(H_0|Data)/Pr(H_1|Data)$, called the *posterior odds*, describes the researcher's beliefs after collecting the data. The key question is how did the data affect the beliefs, or, restated, what is the strength of evidence from the data. This evidence is described by the middle term, $Pr(Data|H_0)/Pr(Data|H_1)$, which is also called the *Bayes factor*. We will denote the Bayes factor with B , and subscript it to indicate which hypothesis is in the numerator and denominator:

$$B_{01} = \frac{Pr(Data|H_0)}{Pr(Data|H_1)} \text{ and } B_{10} = \frac{Pr(Data|H_1)}{Pr(Data|H_0)}.$$

Bayes factor values range from 0 to ∞ and describe how much more probable the data are under one position than another. For example, $B_{01} = 10$ means that the data are ten times more probable than under the null than under the alternative, while $B_{01} = 0.1$ means that the data are ten times more probable under the alternative than under the null. Infinite support for the null and alternative are obtained when $B_{01} = \infty$ and $B_{01} = 0$, respectively. A Bayes factor of $B_{01} = B_{10} = 1$ expresses equivalency; the data do not discriminate at all among the positions.

One of the key properties of Bayes factors is that they describe changes in beliefs rather than beliefs themselves. Consequently, two researchers may not agree about the plausibility of positions *a priori*, and, in this case, they will not agree about the posterior plausibility. Nonetheless, they may agree about the Bayes factors, the evidence from data. Therefore, the Bayes factor is not dependent on these prior odds and serves as evidence regardless of beliefs about the initial plausibility of positions. Because Bayes factors describe evidence or change in belief rather than belief itself, it is considered an ideal statistic for scientific communication (Jeffreys, 1961). This property contrasts favorably with NHST, which is about making decisions with long-term error rates controlled rather than about expressing evidence from data.

The remaining task is defining the probability of data under a hypothesis. We describe the simple case where the data are normally distributed and the question is whether the true effect size is zero or nonzero. Let δ and $\hat{\delta}$ describe the true effect size and the observed effect size, respectively. There are two probabilities that need to be computed, $Pr(\text{Data}|H_0)$ and $Pr(\text{Data}|H_1)$. The former is straightforward. For this simple case, $Pr(\text{Data}|H_0)$ is $Pr(\hat{\delta} \mid \delta = 0)$, which is obtained from the t distribution. Figure 1A shows the hypothesis that $\delta = 0$ as an arrow at zero. Figure 1B shows the probability density under this hypothesis for all values of $\hat{\delta}$ for a sample size of 40 observations divided evenly across two cells. The case for the alternative is more complicated. If the alternative is a single point, say $\delta = 0.43$ (here chosen as an example because $\delta = 0.43$ is the effect size of violent games on aggressive behaviors as described by Anderson et al., 2010), then it is relatively straightforward to compute the probability $Pr(\hat{\delta} \mid \delta = 0.43)$, which is obtained from a noncentral t distribution. This alternative too is represented as an arrow in Figure 1A, and the probability density under this alternative is also shown in Figure 1B. The Bayes factor is simply the ratio of the probabilities. So, for example, if the observed effect size is 0.1, as shown by the circles in Figure 1B, then the probability density for H_0 is 0.38, the probability density for H_1 is 0.23, and the Bayes factor B_{01} , their ratio, is 1.6.

The specification of a point alternative, though often done in power analyses, strikes us as too constrained. In Bayesian analysis, the analyst can consider a range of alternatives. Figure 1C shows the point null and a distributed alternative. Under this alternative, smaller effects are more weighted than larger ones, and positive effects are as weighted as negative ones. The shown alternative is the default one recommended by Rouder and Morey and colleagues (Morey & Rouder, 2011; Rouder & Morey, 2012; Rouder, Morey, Speckman, & Province, 2012; Rouder et al., 2009) as being broadly appropriate for research in psychological sciences. This alternative takes the form of a Cauchy distribution, a fat-tailed distribution defined by a scale parameter that specifies the 50% probability interval. The distribution $\delta \sim \text{Cauchy}(0.4)$, then, describes the effect size

as having 50% probability of being between -0.4 and $+0.4$. The appropriateness of this prior is supported by work by Jeffreys (1961), Liang, Paulo, Molina, Clyde, and Berger (2008), and Zellner and Siow (1980). The probability density under this alternative for all values of $\hat{\delta}$ is shown in Figure 1D, and the density is more diffuse than that for the null. As before, Bayes factor values are computed as the ratio of these probability densities. As an example again, if the observed effect size is 0.1, as shown by the circles in Figure 1D, then the probability density for H_0 is again 0.38, the probability density of this H_1 is 0.14, and the Bayes factor B_{01} , their ratio, is 2.7.

In the above examples, the obtained Bayes factors are fairly small. There is not much evidence to be gleaned from forty observations between two cells. However, with a larger sample, say two hundred observations between two cells, the probability density function for each hypothesis becomes sharper. Differences between the hypotheses are exaggerated, and stronger Bayes factors may be obtained. Figure 1E shows the previous case of two point hypotheses of $H_0 : \delta = 0$ and $H_1 : \delta = 0.43$, an observed effect size of 0.1, and two hundred observations. The Bayes factor is now $B_{01} = 12$. The larger sample has afforded better resolution for discriminating between the two hypotheses. Figure 1F shows the point null and distributed alternative scenario, again with the larger sample size of two hundred observations. The Bayes factor here is $B_{01} = 4.3$.

The relationships between observed effect size, sample size, and Bayes factor are further plotted in Figure 2. Figure 2A shows Bayes factor values for the null vs. the point-alternative hypothesis. Figure 2B shows Bayes factor values for the null vs. the default alternative as a function of observed effect size. A small sample of $n = 40$ is plotted as the solid line, while a larger sample of $n = 200$ is plotted as the dashed line. As can be seen, small observed effect sizes correspond to evidence for the null while larger values correspond to increased evidence for the alternative. When sample sizes are large, the hypotheses are easier to discriminate, and Bayes factors more readily diverge from 1.

Although these examples involve the comparison of two hypotheses, it is also possible

to specify and compare several hypotheses. For example, one might compare a null hypothesis, one alternative hypothesis, and another alternative hypothesis. In the Bayesian perspective, each hypothesis is a statement of belief, and the evidence for or against any statement can be judged and weighed relative to any other statement.

This multiple-hypothesis approach can be useful when two competing hypotheses would predict effects of different magnitudes or directions. For example, an observed negative effect might constitute strong evidence for a hypothesis of negative effect relative to a hypothesis of positive effect and modest evidence for a hypothesis of negative effect relative to a hypothesis of no effect. The comparison of multiple hypotheses is also helpful when assessing the results of a replication. One alternative hypothesis can describe the anticipated effect in broad terms such as “some effect in either direction with modest size,” while another alternative hypothesis can describe the anticipated effect specifically as it was obtained in previous research, say “a positive effect of $\hat{\delta} = 0.43, [0.03, 0.83]$ ” (see Boekel et al., 2014, for an example). One might further wish to compare whether an experiment’s results best support the null hypothesis, a meta-analytic estimate, or a bias-adjusted meta-analytic estimate. For an accessible introduction to specifying alternative hypotheses and appropriate software tools for hypothesis comparison, we suggest the interested reader consult recent work by Dienes (2011, 2014) and by Rouder and Morey (2012) and Rouder et al. (2012). Additionally, the freeware software program JASP (<https://jasp-stats.org>) provides Bayes factors for *t*-tests and ANOVA in a point-and-click SPSS-like environment and may be useful for users not yet comfortable with **R**.

Sample Size and the Strength of Evidence

A common problem in violent-games research, as in most psychological research, concerns statistical power. Many studies arguing the absence of effects (both between stimuli in pilot testing and between conditions in aggressive outcomes) are based on relatively small sample sizes. For example, the typical pilot test features about 20 subjects

for within-subjects testing (e.g., Arriaga, Esteves, Carneiro, & Monteiro, 2008) or about 12-15 per cell for between-subjects testing (e.g., Anderson et al., 2004; Valadez & Ferguson, 2012). In such small samples, only very large effects like $|\delta| = 1.0$ or $|\rho| = .55$ could be tested with 80% power. It is not unusual when such a pilot test ends in failure to detect significant differences between stimuli, and it remains unknown whether this failure reflects a true null or a lack of power.

Statistical power is also a concern in research argued to demonstrate that violent games do not influence aggressive outcomes. In this literature, some studies are well-powered but others are not. If one assumes that the true effect size of violent content on aggressive affect, cognition, and behavior are as reported in Anderson et al. (2010)'s meta-analysis, then one needs sample sizes of $n = 69$, $n = 127$, and $n = 136$, respectively, to test them with 80% one-tailed power. Some studies meet or exceed these recommended sample sizes, while others fall short to various degrees. Whatever the size of the study, one needs a method to appraise the strength of evidence.

Using NHST to claim an invariance creates a perverse incentive to underpower studies—the smaller the sample size, the more likely a failure-to-reject result. An underpowered study will almost always indicate that two games have no significant differences or that an effect of violent games could not be detected. In some cases, statistical power can be further reduced by the application of harsh multiple comparison corrections. NHST in this context implicitly and subtly rewards researchers for collecting insufficient data by yielding the desired research conclusion.

By comparison, Bayes factors are quite good at indicating when the collected data are not sufficient. If the sample size is too small, then the Bayes factors will hover around the value 1, representing no change in beliefs. Bayes factors only become substantially larger or smaller when the sample size becomes large. Analysis by Bayes factors therefore sets up the correct incentives, as researchers must have sufficiently large samples to obtain compelling Bayes factor values. This is vastly preferable to an NHST approach in which the desired

$p > .05$ can almost always be obtained by collection of small, uninformative samples.

But how large must a Bayes factor be to become compelling? Recall that posterior beliefs are the product of prior beliefs and the Bayes factor. There can be no objective threshold that separates “sufficient evidence” from “insufficient evidence”, as prior beliefs are inherently subjective. Thus, to the question “How much evidence do I need?” the answer is simply “Enough to convince your reviewers, readers, critics, and yourself.” If the obtained Bayes factor is not sufficiently large, more data can be collected. Although such optional or conditional stopping is a serious and dangerous form of research flexibility in NHST (Simmons, Nelson, & Simonsohn, 2011), it is not a problem for Bayes factor (Dienes, 2011; Rouder, 2014). Thus, data could be freely collected until the obtained Bayes factor is satisfyingly convincing (e.g., Matzke et al., 2015).

Arguing the Null in Pilot Testing of Matched Stimuli

To address the problems of poor power and the improper application of NHST, we apply the Bayesian approach described above to interpreting the results of several stimulus-matching pilot tests for which necessary statistics were available. As described previously, experiments of violent game effects on aggressive outcomes use pilot testing to check for confounding differences between the violent and nonviolent game stimuli. To make a causal statement that the observed effects are specifically due to violence, it is useful to first make sure that the two games are alike in all dimensions save violence, thereby indicating an absence of confounds.

In the research literature on violent games, proponents have suggested that this process of matching demonstrates that the effects of violent video games are specifically due to violent content and not other confounds (Anderson et al., 2004). At the same time, skeptics have suggested that matching games on certain dimensions eliminates the effect of violent games (Adachi & Willoughby, 2011). However, interpretation of these pilot tests has been improper and incoherent. For example, pilot tests in this research domain have

sometimes estimated the differences between stimuli as being large, but because the results were not statistically significant, the null hypothesis was considered confirmed. In one particularly remarkable case, post-hoc Bonferroni correction for multiple comparisons was applied to control the Type I error rate across comparisons on 14 dimensions, lowering the critical value of p to .0036 (Arriaga et al., 2008). Differences as large as $\hat{\rho} = .53$ were observed but escaped consideration due to the small sample size and harsh multiple comparison correction. To their credit, the authors acknowledge that the pilot sample was small, but still do not entertain the possibility that the pilot test provided evidence of differences; instead, they conclude that the pilot test indicates that the games are relatively well-matched.

We reevaluate some exemplar pilot tests by applying Bayesian model comparison, proposing two hypotheses for pilot testing. The first is a null hypothesis of no difference in potential confounds, $H_0 : \delta = 0$, and the alternative hypothesis is a hypothesis of a moderate difference, $H_A : \delta \sim \text{Cauchy}(0.5)$.¹ This choice of scale in the alternative hypothesis is subjective but appropriate. Effects of violent games are expected to be small (e.g., $\rho = .21$, or about $\delta = 0.43$), so confounds should be examined on a similarly small scale.

We use the `ttestBF` function in the `BayesFactor` package (Morey & Rouder, 2014) to calculate paired-sample or two-sample Bayesian t -tests with scale on effect size set to 0.5. (For a comparison against a null interval over $[-0.1, 0.1]$, consult the supplementary materials.) By entering the sample size and the obtained t -value of each test, we obtain a Bayes factor describing the strength of evidence for or against the null relative to this alternative hypothesis.

¹If it is unreasonable to expect that the stimuli are perfectly matched, a null hypothesis of minimal difference can be used instead to treat very small differences as practically equivalent to zero (e.g., $H_0 : \delta \sim \text{Uniform}(-.1, .1)$, see the `nullInterval` argument for the `ttestBF` function in the `BayesFactor` **R** package).

Reanalysis of Select Pilot Tests in Violent Media Research

We re-examined pilot data from Arriaga et al. (2008) and present the results in Table 1. The pilot test, with its sample of $n = 20$ (within subjects), has not provided strong evidence of matching between stimuli on all dimensions. Bayes factors reveal that there is evidence that some dimensions do not differ, but evidence that other dimensions do. After the pilot test, the readers and researchers are roughly three times more confident the games do not differ in involvement, presence, boredom, satisfaction, identification, or excitement. However, they should also be twice as concerned that the games differ in feelings of competence, and nearly four times as concerned that they differ in difficulty. Tests of whether the games differed in discomfort, realism, pleasure, action, or disorientation were largely uninformative. These conclusions are very different from those of the original authors, who interpret the nonsignificant results of the pilot test as indicating that the games are equivalent on all measures, or at worst, that the results might be merely inconclusive. Given that the two tested video games, *Unreal Tournament* (a first-person shooter game) and *Motocross Madness* (a racing game), come from very different game genres with very different rules of play, one might have some prior belief that the games are not well matched. It is possible, then, that the primary results from this study, in which the violent game was associated with greater aggressive behavior and hostility, are not caused by violent content specifically, but may be caused instead by differences in experienced competence or the difficulty of gameplay.²

Another classic pilot test in this literature is found in Anderson et al. (2004, study 1), in which 120 subjects each played one of 10 games (i.e, $n = 12$ per cell). The games *Glider Pro* and *Marathon 2* were selected as a matched pair differing in violent content but not in other dimensions. Our reanalysis is summarized in Table 1. Evidence for the null hypothesis is slight, and reanalysis indicates that the games instead may differ in amount

²It is necessary in conventional analyses to account for the effects of multiple comparisons on desired long-run error rates. Bayesians, in contrast, are interested in the quantification of evidence, not the control of such error rates, so there is no need for such corrections (Dienes, 2011; Royall, 1997).

of action.³ Further data collection would be necessary to arrive at certainty about the equivalence or difference of these two games on these dimensions.

Mistaken inferences regarding the results of pilot testing are also found among skeptics of violent media effects. We re-evaluate the pilot test from Valadez and Ferguson (2012). This study used a three-level one-way ANOVA design to compare a violent game condition to two non-violent game control conditions. In the violent game condition, participants played a segment from the later stages of the open-world shooter game *Red Dead Redemption*. In one control condition, participants played a segment from the beginning of *Red Dead Redemption*, argued to contain little or no violence because of the early stage of the game, and in the other control condition, participants played the soccer game *FIFA*, a nonviolent game. A small sample was collected (cell $ns = 15, 10$, and 15 , respectively, between-subjects), to rate each game on difficulty, competitiveness, and pace of action. Differences in difficulty and competitiveness were reported as not significant, $F(2, 40) = 2.36, p > .05$ and $F(2, 40) = 3.09, p > .05$, respectively, while differences in pace of action were significant $F(2, 40) = 4.27, p = .02$. This last variable was explored through Bonferroni post-hoc analysis, and it was decided that the two control conditions differed from each other but not from the active condition.

To determine the strength of evidence for or against invariance in the Valadez and Ferguson data set, we computed all pairwise t -values and corresponding Bayes factors. The results are reported in Table 2. Contrary to the authors' conclusions, the results of the pilot test indicate that the games are not well matched. In particular, Bayes factors indicate evidence that the two *Red Dead Redemption* conditions differ in competitiveness and the two control conditions differ in all dimensions. Most other comparisons are largely uninformative, as might be expected of the small sample size. Given our prior beliefs that the early stages of a game are often rather easier than the later stages, that *Red Dead*

³We computed slightly different t -values than the original authors from the reported summary statistics. We used the reported MSE which is an averaged variance which may not well reflect individual-cell variabilities. These differences are of minimal concern—given the small sample size per cell, the Bayes factor values are necessarily close to 1.0.

Redemption and *FIFA* are very different genres of game, and given that the evidence indicates differences between the conditions, we are again not convinced that the stimuli are well-matched. Rather than demonstrate that the stimuli are matched, the pilot test has instead indicated that the games are probably quite different.

Adachi and Willoughby (2011) report two pilot studies intended to demonstrate that the games used (*Conan*, an action-adventure combat game, and *Fuel*, a racing game) were matched on certain game dimensions but differed in violent content. In the first pilot, $n = 14$ participants played each of two games (within-subjects). This pilot provided slight evidence that the two games did not differ in competition, difficulty, or pace of action, B s = 2.61, 2.48, and 2.22 in favor of the null, respectively. The subsequent Study 1 provided little further evidence that the games did not differ, B s = 2.43, 1.06, and 1.05 in favor of the null relative to the alternative, respectively. Again, considering that the two games came from very different genres (action-adventure, racing), this may not be sufficient to convince everyone that the games are identical in all ways besides violent content. Still, at least the pilot test did not provide evidence that the games instead differed. Note also that neither this study nor Valadez and Ferguson (2012) tested games for equivalence in frustration or feelings of competence, so it is possible that other confounds exist but were not tested.⁴

Figure 3 shows the relationships between sample size, p -value, and evidence for the null in between-subject and within-subject study designs. Supposing one desires at least 3-to-1 evidence in favor of the null, a between-subjects design needs at least 66 subjects and a within-subjects design needs at least 17 subjects. These numbers are based on the optimistic assumption that the observed difference is exactly zero (e.g. $p = 1.0$). In practice, nonzero differences are likely to be observed and will provide less support for the

⁴Again, if it seems too conservative to expect that stimuli are exactly matched, and minor differences are acceptable, the null hypothesis could instead be specified as the interval $\delta \sim \text{Uniform}[-0.1, 0.1]$. In that case, the Bayes factors change little, and are as follows. In the pilot test, B_{01} s = 3.37, 3.11, and 2.68 in favor of the null for competition, difficulty, or pace of action, respectively. In the first study, B s = 3.04, 1.07, and 1.06 in favor of the null, respectively.

null and may even favor the alternative hypothesis. Thus, although the above studies were picked as examples, they may be representative of the literature.

To the best of our knowledge, the largest pilot test not finding significant confounds is reported by Anderson and Carnagey (2009), who conducted $n = 32$ subjects in a 2 (Violence: violent, nonviolent; within) \times 2 (Sport: Football, Baseball; between) mixed-design ANOVA. Other similarly-sized pilot studies typically find significant confounds, which are then later applied as covariates in analysis (e.g., Anderson & Dill, 2000; Gitter, Ewell, Guadagno, Stillman, & Baumeister, 2013). In general, we have found few pilot studies that collected more than 20 subjects in a within-subjects design or more than 40 subjects in a between-subjects design. Thus, while the examples provided above do not constitute a systematic review, we expect that these criticisms apply to a majority of studies in the literature.

Studies Without Pilot Tests

Not all studies conduct pilot tests to attempt to demonstrate the equivalence of game stimuli. In such cases, there is no evidence one way or the other and no change in beliefs. The researcher, reader, and reviewers have only their prior beliefs concerning the equivalence or inequivalence of stimuli. Scientific skepticism may require that researchers consider stimuli unmatched until evidence indicates otherwise. Examples of experiments not reporting pilot tests for equivalence include Bartholow and Anderson (2002), Bartholow, Sestir, and Davis (2005), and Hasan, Bègue, and Bushman (2012).

Summary

Because NHST cannot provide evidence in favor of the null hypothesis, it is inappropriate to argue that two experimental stimuli are matched on the basis of a non-significant test result. Non-significant test results can almost always be obtained, even if the null hypothesis is false, through collection of an arbitrarily small sample size and application of harsh multiple-comparison corrections. Although it is indeed a good idea to

match stimuli, pilot tests from this literature often provide little evidence that stimuli are matched, and in fact, often indicate that the two stimuli involve some confounds. That said, although the past evidence for matching is not compelling, future research studies may be able to use larger pilot studies to provide better evidence of matching.

As an alternative to NHST, we advocate the use of Bayesian statistics. Bayes factor evidence may favor the null hypothesis of no difference, may favor an alternative hypothesis of a confounding difference, or may favor neither, indicating an absence of evidence for either hypothesis.

We note that another approach used in this literature is to not equate stimuli at all, but rather to collect measurements of potential confounds and apply them as covariates to attempt to adjust the groups to equality (e.g., Bushman & Anderson, 2002, 2009; Carnagey, Anderson, & Bushman, 2007; Sestir & Bartholow, 2010). Although this practice is sometimes recommended as “destructive testing” (Anderson & Anderson, 1996; Prot & Anderson, 2013), the appropriateness of this practice is controversial and rests upon several delicate statistical assumptions. A full exploration of this problem is beyond the scope of the present manuscript, but the interested reader may find a number of arguments against attempting to equate unequal groups through ANCOVA (e.g., Miller & Chapman, 2001). Thus, much as in the insufficient pretesting examples above, one cannot be certain that this approach completely eliminates the effect of confounds on the dependent variable.

Setting aside the issue of matched stimuli, it would still be interesting to assess the degree of evidence for the null hypothesis in those studies reporting no significant effects of video game violence. These reported studies vary substantially in their sample sizes and estimated effect sizes and so vary too in their evidence for or against the null. We reanalyze these findings in the next section.

Bayesian Reanalysis of Nonsignificant Results

Some researchers have argued that there is no effect of violent game contents when the video games are well matched on confounding dimensions. Research exploring these confounds has found significant effects of the confound but nonsignificant effects of violent content. Such research suggests that previous studies have overestimated the effect of violent media by mistaking the effects of confounding game features for the effect of violence. If true, this would indicate that effect size estimates from previous meta-analyses (e.g., $r = .21$ or $d = 0.43$, Anderson et al., 2010) are overstated.

Yet, there seem to be inferential difficulties in the claim that there are no effects. At one extreme, consider the results of Elson et al. (2013) in which one of the reported outcomes has a p -value of .073, which barely misses the conventional .05 criterion. Not only is this p -value small, the observed effect size of $\hat{\delta} = .41$ is about the same size as the meta-analytic value of $\hat{\delta} = .43$ reported by Anderson et al. (2010). This may seem to be more a confirmation of the effect than a refutation.

Bayesian Model Comparison and Hypothesis Specification

To assess the strength of evidence for or against the null hypothesis, we re-evaluate these null findings through Bayesian model comparison. Unlike in pilot testing, where we had only vague hypotheses about effects, violent-game-effects research can build on previous work to describe more specific hypotheses. We therefore compare four hypotheses: a null hypothesis, a vague alternative hypothesis, a less vague alternative hypothesis, and a highly specific alternative hypothesis. As before, the null hypothesis describes the true effect size as exactly zero: $H_0 : \delta = 0$. The three alternative hypotheses are more involved and are described next.

The vague alternative hypothesis is that the true effect is probably small-to-medium in magnitude, but we know little about the direction of effect or which magnitudes are particularly likely. We will refer to this minimally-informative alternate hypothesis as H_{A1} ,

the first alternative hypothesis, and model it with a minimally-informative prior known as the Jeffreys-Zellner-Siow or JZS prior (see Jeffreys, 1961; Liang et al., 2008; Rouder et al., 2009; Zellner & Siow, 1980). H_{A1} is specified as $\delta \sim \text{Cauchy}(0.4)$. By evaluating the probability of this hypothesis relative to the null hypothesis, we create Bayes factor B_{01} , the probability ratio of H_0 as compared to H_{A1} . We calculate B_{01} by using the BayesFactor package for **R** (Morey & Rouder, 2014).

A second, more specific alternative hypothesis is that the true effect is small-to-medium in magnitude but strictly positive. We model this with a *folded* Cauchy distribution, restricting the probability to only positive values. This one-tailed hypothesis H_{A2} is specified as $\delta \sim \text{Cauchy}^+(0.4)$. Comparing the probabilities of H_0 and H_{A2} yields B_{02} , the evidence for the null relative to this one-tailed alternative. We calculate B_{02} with the metaBF function for **R** provided by Rouder and Morey (2011).

The more precise alternative hypothesis is that the true effect is equal to that estimated by previous meta-analysis, e.g. $\delta = .43[.35, .52]$ (Anderson et al., 2010). We use the meta-analytic effect size estimate and standard error to derive our third and most specific alternative hypothesis, $H_{A3} : \delta \sim \text{Normal}(.43, .04)$, where .43 and .04 are the mean and standard deviation of the effect size. By again comparing the probability of the data given H_0 against the probability given H_{A3} , we create Bayes factor B_{03} . B_{03} gives the measure of evidence for the null hypothesis relative to the meta-analytic expectation of the effect size. (Note that the mean and standard deviation used in H_{A3} will vary depending on the particular outcome tested: aggressive cognition, aggressive behavior, and aggressive affect each have slightly different meta-analytic effect size estimates. The above example references the effect of violent game content on aggressive behavior.) We calculate B_{03} using **R** code provided by Christie, Baguley, and Kaye found on Dienes' website (http://www.lifesci.sussex.ac.uk/home/Zoltan_Dienes/inference/bayesFactorCalc2.R).

With these Bayes factors, researchers can assess the relative evidence for all three alternative hypotheses relative to the null hypothesis. The nonspecific alternative

hypothesis H_{A1} could be supported by effect sizes of various magnitudes and either sign, and $B_{01} < 1$ indicates support for this broad hypothesis relative to the null. H_{A2} describes an hypothesized increase of modest magnitude, and B_{02} summarizes the strength of evidence for the null relative to this increase. Finally, H_{A3} precisely describes the meta-analytic estimate. $B_{03} > 1$ indicates evidence for the null relative to the meta-analytic expectation, while $B_{03} < 1$ indicates evidence consistent with the meta-analytic estimate.

Reanalysis of Null Findings in VVG Research

We apply this approach to the current literature of studies interpreted as finding evidence of no effect of violent video games on aggressive behavior. Each study has a confidence interval that overlaps with $\delta = 0$ which caused researchers to retain and argue for the null hypothesis. Our analysis quantifies the strength of evidence for the null, if any.

As always, analysis involves an amount of subjectivity. In performing these analyses, our goal was to assess the evidence for or against a difference between participants who played a nonviolent game and participants who played a violent game. Some studies had unusual experimental or control conditions that required subjective but judicious treatment. In Ferguson et al. (2008), half of participants were allowed to choose their own game condition (violent or nonviolent), rather than being randomly assigned to play a violent or nonviolent game. We do not think this self-assignment condition supplies an appropriate test of the hypothesis. We exclude those participants from this analysis, as the absence of random assignment implies a loss of experimental control. In Ferguson and Rueda (2010), some subjects were not assigned to play any video game, but were instead made to wait in a room for 45 minutes due to a purported computer error. This control condition does not seem relevant to our hypothesis; therefore, we compare only those subjects who were randomly assigned to play a violent or nonviolent video game.

Findings are summarized in Table 3. We find that, among these null results, the strength of evidence for the null varies substantially. In studies with small sample sizes

(Ferguson et al., 2008, Study 1; Adachi & Willoughby, 2011, Study 1 and 2), evidence for the null in each experiment is slight. In contrast, studies with larger sample sizes (Ivory & Kalyanaraman, 2007, aggressive cognition; Przybylski et al., 2014, Study 1, 2, and 5; Tear & Nielsen, 2014), provide stronger evidence for the null. Finally, in cases where effect sizes were close to $\hat{\delta} = 0.43$ but the confidence interval failed to exclude zero, we do not interpret the study as disproving H_{A3} in favor of H_0 . Bayes factors recognize that $\hat{\delta} = 0.41$ much more closely resembles $\delta = 0.43$ than it does $\delta = 0$. Thus, re-examination of the reported effect of violent game content in Elson et al. (2013) indicates one agnostic result (effects on mean noise duration) and one moderately informative replication (effects on mean noise intensity). The non-significant result has been misinterpreted as support for the null when instead support has been found for the alternative.

A similar phenomenon is observed in Valadez and Ferguson (2012). In this study, participants' hostile feelings were measured before and after playing one of three games: a late-game section of *Red Dead Redemption* (the active condition), an early-game section of *Red Dead Redemption* (one control condition), and *FIFA* (a second control condition). The condition in which the participants played the beginning section of *Red Dead Redemption* was considered a nonviolent control condition, as was *FIFA*. Thus, the latter section of *Red Dead Redemption* was compared to the other two conditions, and with a time (pre-, post) \times game (active, controls 1 & 2) test statistic of $F(1, 94) = 3.11, p = .09, \hat{\delta} = 0.35$, the authors argued positive evidence for the null hypothesis. On the contrary, compared to the meta-analytic estimate of the effects of violent games on aggressive affect ($\hat{\delta} = 0.61, [0.52, 0.72]$, Anderson et al., 2010), the data slightly support the alternative hypothesis, not the null, at 1-to-1.9 odds.

The interpretation of this study's results are complicated by the overall decline in post-play aggressive affect. It is possible that this phenomenon supports hypothesized effects of violent games in that all gameplay decreases aggressive affect but violent game content increases aggressive affect relative to nonviolent game content. The sum of these

two effects may provide a net decrease in aggressive affect. This would indicate that violent game content increases aggressive affect relative to the absence of violent game content, but that use of violent games nonetheless decrease aggressive affect relative to not having played a violent game. (However, remember also that the conditions do not appear to be well-matched, and so this phenomenon could still be due to the same confounds that may cause the effect observed in other research.) We excuse ourselves from interpretation of this difference. Our point is merely that there is some evidence that the two conditions differ, contrary to the argument of the authors. Future research could explore the possibility of decreased aggressive affect in both violent and nonviolent video game use through application of repeated measures designs to determine whether purported increases caused by violent games instead reflect smaller decreases. However, one should be aware that repeated measurement of aggressive outcomes immediately before and after violent gameplay may alert participants to the research hypotheses and make it difficult to collect valid data.

In summary, while all nonsignificant findings receive the same uninformative “failure-to-reject” decision in NHST, a Bayesian analysis provides a more nuanced perspective by providing a quantification of continuous amounts of evidence for or against the null relative to selected alternatives. Attention to the strength of evidence will help researchers to determine whether they have evidence of no effect, evidence of an effect, or inconclusive evidence. This evidence tells researchers whether a research finding has been replicated, an effect has been disconfirmed, or a boundary of the phenomenon has been reached.

Bayes Factor Is Still Influenced by Researcher Flexibility

We describe above how Elson et al. (2013) seem to have found evidence for the theorized effect despite their original argument for the null. In our correspondence with these authors, they asked that we consider their criticism that the Competitive Reaction

Time Task measure of aggression used in this and other studies can be quantified flexibly, potentially allowing researchers to selectively report the quantification with the biggest effect size or the smallest p -value (Elson, Mohseni, Breuer, Scharkow, & Quandt, 2014). In this literature, they argue, this particular measure is quantified in many different ways across studies, suggesting that researchers may attempt several different quantifications until one yields statistical significance. Bayesian model comparison is not immune to these problems, as Bayes factors are still a function of the data and thus still sensitive to flexibility in quantification or censorship in report.

To support their argument, Elson et al. (2014) demonstrated that the same experiment can yield substantially various effect sizes and p -values depending on which quantification strategy is used. In the same way, the obtained B_{03} varies substantially depending on the quantification: if mean intensity is used, B_{03} favors the alternative, 1-to-5, but if mean duration is used, B_{03} favors neither hypothesis, 1-to-1. We examine these fluctuations in Bayes factor across quantification strategy in Table 4. As Elson et al. (2014) had noticed, various quantification strategies yielded effect sizes ranging from $\omega = -.32$ (count of low-volume trials, here reported as negative, as it is in the direction opposite to that hypothesized) to $\omega = .00$ (first-trial volume) to $\omega = .39$ (count of high-volume trials). Similarly, B_{03} ranges from 1400-to-1 (count of low-volume trials) to 3.5-to-1 (first-trial volume) to 1-to-280 (count of high-volume trials). To minimize potential flexibility in quantification, we suggest that researchers preregister their primary study outcomes, share the raw task data, and provide evidence of the validity of particular quantifications, when possible.

Summary

Although many of the studies analyzed were claimed by $p > .05$ to support a null violent-content video-game effect, the evidence varied considerably. Some studies provided strong evidence for the null, others provided only slight evidence for the null, and still

others actually provided some evidence for the hypothesized phenomenon. As in the pilot testing example above, failure to reject the null does not necessarily constitute evidence in favor of the null and may instead represent insufficient sample size. Even when sample sizes are sufficient, a principled quantification is needed to express the strength of evidence for or against the null relative to a reasonable and meaningful alternative hypothesis. This principled quantification may be accomplished by the application of Bayesian model comparison techniques presented by Rouder and Morey (2012), Rouder et al. (2012), and Dienes (2011, 2014).

Reanalysis indicates that some null findings have substantial evidence, while others have less. Results from Przybylski et al. (2014) provide a sizable Bayes factor value for B_{03} , indicating that the effect of violent games on aggressive affect is more likely to be zero than it is to be that estimated in previous meta-analysis so long as experimental control is maintained over feelings of competence. On the other hand, Bayes factor values of B_{03} from Adachi and Willoughby (2011) are modest. A larger experiment might be necessary to more firmly establish that aggressive behavior is influenced by competitive rather than violent game content. Attention to the strength of evidence may aid in theory development, indicating where evidence of boundary conditions is strong and where evidence is less certain.

Finally, Bayesian analysis is not a panacea for all difficulties in analysis and reporting. It is a function of the data and cannot address concerns about selective reporting. When data are selectively reported according to the hypothesis they support, Bayes factor will be biased. It is thereby important that all studies be reported. We further urge researchers to pre-register their hypotheses and analytic strategies, including their method of CRTT quantification. We further urge researchers to attempt a thorough and systematic validation of the CRTT in an attempt to choose a limited number of methods which clearly measure a limited number of constructs. Like any other statistical analysis, Bayesian model comparison is still subject to the problem of “garbage in, garbage out.”

Discussion

Making principled and coherent arguments for the null hypothesis is a crucial part of the scientific process. In violent media research, the null hypothesis is of critical importance in matching stimulus materials in pilot testing and in demonstrating the boundary conditions or absence of an effect of violent media. Despite this importance, traditional statistical practices cannot be used to support the null, at least not in a principled fashion. As an alternative, we suggest Bayesian model comparison, which allows for fair and principled tests between the null hypothesis and reasonable alternative hypotheses.

Our re-analysis found that research in this area would benefit from larger samples and more finely-graded interpretations of results. Inspection of a selection of pilot studies found that many pilot studies provided little evidence of matching, and in some cases even provided evidence of confounding differences between game stimuli. These results indicate that pilot tests often fail in their intended purpose and that violent and nonviolent game stimuli used in research may not be well-matched. To address this problem, we suggest the collection of larger samples and the application of Bayesian analysis. Larger samples would provide stronger evidence, and Bayesian analysis would provide more nuanced, less dichotomous results.

In similar fashion, main study results argued to show no effect of violent game content were found to vary substantially in the strength of evidence for the null. In two cases, a p -value very close to the critical threshold was presented as a disconfirmatory finding (Elson et al., 2013; Valadez & Ferguson, 2012); re-evaluation of these reports indicate instead some evidence of a difference between groups. We applaud and encourage research efforts in this area which strive to test the boundaries and causal substrates of the effects (if any) of violent games on aggressive thoughts, feelings, and behavior. However, such research efforts will likely require larger sample sizes to provide sufficiently compelling evidence.

Other Approaches To Support The Null

We note that Bayesian analysis is not the only way to provide evidence for the null hypothesis relative to some alternative. One option is to perform a significance test against a second null hypothesis of some effect. For example, when failing to detect an anticipated effect, one could test against the expected effect size θ_0 with the secondary null hypothesis $H_{02} : \delta = \theta_0$, where θ_0 is a previously-reported effect size or an effect size necessary for some level of statistical power. If the study retains H_0 while rejecting H_{02} , it could be argued that the study data are sufficiently unlikely given that the true effect size is θ_0 (e.g., Simonsohn, Simmons, & Nelson, 2014). For example, if a study estimates the effect of violent games on aggressive behavior as $\hat{\delta} = 0.06, [-0.25, 0.37]$, one might say that the result is improbable ($p < .05$) if the true effect size were $\delta = 0.43$.

However, this approach yields dichotomous inferences, and so cannot discriminate between no evidence, a little evidence, and a lot of evidence. The problems of dichotomous test results are particularly salient when one considers how slight changes in p -value lead to opposite conclusions, such as how the null is rejected at $p = .049$ but the null is retained at $p = .051$. NHST also cannot handle small amounts of evidence well. Given slight evidence, either the null is retained and the slight evidence is mislabeled as no evidence at all, or the null is rejected and the effect size is grossly misestimated. Finally, this approach only accepts a single point value θ_0 as the hypothesis. This is too constraining; there are often a range of values that are probable given a hypothesis.

Among the studies that we reanalyzed, many had CIs that included the meta-analytic estimate (Table 3). Application of this significance test, then, would report that these studies were simply uninformative. Our Bayesian analysis indicates instead that there is some evidence, even if it is not strong enough to be “statistically significant.”

A second alternative is to quantify the effect size and its confidence interval (ESCI). This approach has the advantage relative to NHST of being continuous in quantification. However, ESCI provides neither quantifiable nor inferentially consistent statistics (see

Morey, Rouder, Verhagen, & Wagenmakers, 2014), and when making inferences using ESCI, researchers seem to mentally convert them to NHST anyway (Hoekstra, Morey, Rouder, & Wagenmakers, 2014). Although it is true that values near the ends of the confidence interval are less likely, one cannot know exactly how much less likely they are. Similarly, a wide CI indicates that more samples would be necessary to provide a more precise estimate of the effect size, but there is no way of knowing at what point the CI is sufficiently precise for inference. ESCI is a useful descriptive tool but does not permit inferences about the strength of evidence.

Practical Recommendations

We offer two other practical recommendations to improve pilot-testing and primary tests of hypotheses in this literature. First, we note that it may not be feasible to pilot test and match game stimuli to necessary precision. Because the hypothesis-relevant effects of violent game content are hypothesized to be small, hypothesis-irrelevant confounds must be controlled for on a similarly small scale. Because an alternative hypothesis of such small scale closely resembles the null, large amounts of data are likely to be necessary to disentangle the two. Worse, collection of a large sample does not guarantee that the Bayes factor indeed will favor the null. One could potentially invest many subjects in such a test only to find that the games are not well matched.

As an alternative to pilot testing commercially-available games for equivalence, we instead favor the approach of software modification. In this approach, researchers take an existing game and modify it with software tools so that the core game is the same, but the construct of interest varies across conditions (see Elson & Quandt, 2014). It is not unlike adjusting the parameters of a computer task's script to observe the parameters' effects on participants' behavior. The unmodified portions of the game's code are kept identical between versions. Because games developed in this way are more obviously matched, it requires less pilot evidence to conclude that they are indeed matched, and if such evidence

is sought, it is more likely to be obtained. One such manipulation, which involves identical game files which vary in violent content and in the difficulty of gameplay, has been made publicly available for use on OSF (Hilgard, 2014). However, such homemade game modifications may have their limits. It will be infeasible to make professional-quality game modifications with graphics, gameplay, and acting on par with some modern popular video games. Although research suggests that graphical fidelity is not an important moderator of game effects (Barlett, Rodeheffer, Baldassaro, Hinkin, & Harris, 2008; Ivory & Kalyanaraman, 2007), it is possible that such homemade games do not capture the full real-world phenomenon of video gaming.

As a second practical recommendation, we ask that researchers collect larger samples in their experiments. Effects in this research domain are hypothesized to be small. Thus, large samples will be necessary to discriminate effectively between the null and alternative hypotheses. To collect larger pilot samples, pilot tests might be conducted as an appendix to another experiment. However, primary study outcomes will remain time-consuming to detect. It is possible that some effects are too small to be feasibly studied in single-institution experiments. Multi-site investigations could help to increase sample sizes. *Antagonistic* multi-site collaborations could be especially productive and may alleviate concerns of differences in bias or competence across research teams. In other research areas, some researchers are already conducting such preregistered antagonistic collaborations, agreeing to collect data until a sufficiently large Bayes factor is obtained in support of one hypothesis over the other (e.g., Matzke et al., 2015). Because the conditions of such experiments are agreed to in advance by both skeptics and proponents, these provide a fair and informative test of a hypothesis.

Better Research through Bayes

We close with an optimistic thought about how Bayesian analysis might further shape the scientific process. It is well understood that, historically, papers finding

significant ($p < .05$) effects are more likely to be published than are papers without significant effects (Atkinson, Furlong, & Wampold, 1982; Cooper, DeNeve, & Charlton, 1997; McDaniel, Rothstein, & Whetzel, 2006). This process is thought to contribute to publication bias, in that only research obtaining $p < .05$ gets published, and questionable research practices, in that researchers muss with their results until the necessary $p < .05$ threshold is reached. Both of these processes will lead to overestimated effect sizes and the propagation of Type I errors. With Bayes factors, there is no such dichotomization or sufficient threshold; instead, evidence is collected and its strength reported. Acceptance of evidence as a continuous quantity may, we hope, reduce journals' and researchers' preference for results that just pass an arbitrary threshold that unjustly separates "sufficient evidence" from "insufficient evidence." By assessing the finely-quantified weight of evidence for each argument from each experiment, we can reach a greater understanding of what is certain, what is uncertain, where evidence is truly contradictory, and where we are arguing over sampling error.

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Table 1

Bayesian results of pilot tests of stimulus equivalence

	t	p	$\hat{\delta}$	B_{01}
Arriaga et al., 2008				
Difficulty	2.63	.017	1.25	1-to-3.6
Competence	2.27	.035	1.06	1-to-2.1
Discomfort	1.67	.110	0.80	1.1-to-1
Realism	1.56	.135	0.75	1.3-to-1
Frustration	1.32	.201	0.63	1.6-to-1
Pleasure	1.29	.214	0.61	1.7-to-1
Action	1.24	.229	0.58	1.8-to-1
Disorientation	1.14	.267	0.54	1.9-to-1
Excitement	0.89	.385	0.43	2.4-to-1
Identification	0.86	.398	0.41	2.4-to-1
Satisfaction	0.83	.419	0.39	2.5-to-1
Boredom	0.79	.437	0.37	2.5-to-1
Presence	0.53	.601	0.24	2.9-to-1
Involvement	0.48	.634	0.22	2.9-to-1
Anderson et al., 2004				
Action	2.35	.028	1.01	1-to-2.4
Difficulty	1.00	.327	0.43	1.6-to-1
Frustration	-0.79	.436	-0.34	1.8-to-1
Enjoyment	-0.40	.693	-0.16	2.0-to-1
Violence	5.48	< .001	2.34	1-to-720

Pilot test results from Arriaga et al. (2008) and Anderson et al. (2004). Pilot data is largely agnostic between the null and alternative, and in fact sometimes indicates equally strong evidence of certain confounds. *Note:* B_{01} ranges from 1-to- ∞ (perfect evidence for alternative) to ∞ -to-1 (perfect evidence for null). $H_0 : \delta = 0$; $H_1 : \delta \sim \text{Cauchy}(0.5)$. All Bayes factors rounded to two significant digits.

Table 2

Results of pilot test from Valadez and Ferguson (2012).

	Difficulty		Pace		Competitiveness	
	t	B_{01}	t	B_{01}	t	B_{01}
Active vs. Control1	1.64	1-to-1.1	1.25	1.3-to-1	2.54	1-to-3.16
Active vs. Control2	-1.47	1.1-to-1	-2.00	1-to-1.6	0.05	2.1-to-1
Control1 vs. Control2	-3.35	1-to-12	-3.39	1-to-13	-2.54	1-to-3.2

Pilot testing often suggests that the conditions are different, not equivalent, on ratings. Evidence of invariance, when found, is very small. *Note:* B_{01} ranges from 1-to- ∞ (perfect evidence for alternative) to ∞ -to-1 (perfect evidence for null). $H_0 : \delta = 0$; $H_1 : \delta \sim \text{Cauchy}(0.5)$. All Bayes factors rounded to two significant digits.

Table 3

Bayesian re-analysis of claimed null results.

	$\hat{\delta}$	95% CI	n	B_{01}	B_{02}	B_{03}
Aggressive Affect						
Anderson et al., 2010, Meta-analysis	0.61	[0.52, 0.72]	2513	-	-	-
Valadez & Ferguson, 2012	0.35	[-0.07, 0.78]	100	1-to-1.12	1-to-1.46	1-to-2.0
Przybylski et al., 2014, S1	0.01	[-0.39, 0.41]	99	3.0-to-1	5.1-to-1	62-to-1
Przybylski et al., 2014, S2	-0.16	[-0.56, 0.23]	101	2.3-to-1	9.0-to-1	680-to-1
Przybylski et al., 2014, S5	0.06	[-0.32, 0.44]	109	3.0-to-1	4.2-to-1	41-to-1
Ivory & Kalyanaraman, 2007	0.36	[-0.00, 0.72]	120	1-to-1.4	1-to-1.9	1-to-2.7
Aggressive Behavior						
Anderson et al., 2010, Meta-analysis	0.43	[0.35, 0.52]	1454	-	-	-
Elson et al., 2014, Noise Intensity	0.40	[-0.04, 0.84]	84	1-to-1.2	1-to-1.7	1-to-4.8
Elson et al., 2014, Noise Duration	0.22	[-0.22, 0.65]	84	2.0-to-1	2.0-to-1	1-to-1
Ferguson et al. 2008, Study 1	-0.21	[-0.78, 0.36]	50	2.0-to-1	6.2-to-1	8.3-to-1
Ferguson & Rueda, 2010	0.06	[-0.42, 0.55]	77	2.5-to-1	3.8-to-1	2.9-to-1
Adachi & Willoughby, 2011, S1	0.00	[-0.62, 0.62]	42	2.2-to-1	3.6-to-1	2.5-to-1
Adachi & Willoughby, 2011, S2	0.09	[-0.42, 0.61]	60	2.4-to-1	3.2-to-1	2.1-to-1
Tear & Nielsen, 2014	0.03	[-0.35, 0.41]	120	3.0-to-1	5.1-to-1	7.4-to-1
Aggressive Cognition						
Anderson et al., 2010, Meta-analysis	0.45	[0.37, 0.52]	2887	-	-	-
Ivory & Kalyanaraman, 2007	0.08	[-0.29, 0.44]	120	3.0-to-1	4.1-to-1	5.4-to-1

Some studies present only modest evidence against the effect, and several indicate evidence for the effect despite nonsignificant p -values. *Note:* B_{01} = evidence for $H_0 : \delta = 0$ compared to $H_{A1} : \delta \sim \text{Cauchy}(0.4)$. B_{02} = evidence for $H_0 : \delta = 0$ compared to $H_{A2} : \delta \sim \text{Cauchy}^+(0.4)$. B_{03} = evidence for $H_0 : \delta = 0$ compared to $H_{A3} : \delta \sim \text{Normal}(\mu, \sigma)$, with μ and σ taken from Anderson et al. (2010). Bayes factors range from 1-to- ∞ (perfect evidence for alternative) to ∞ -to-1 (perfect evidence for null). All Bayes factors rounded to two significant digits. Valadez and Ferguson (2012) effect size is the 2 (Game: *Red Dead Redemption*, *FIFA*) \times 2 (Time: pre-, post-) interaction effect. Ferguson et al. (2008) effect size is of those 50 subjects who were randomly assigned to play a violent or nonviolent game. Ferguson and Rueda (2010) effect size is the complex contrast between those participants who played a violent game vs. those who played a nonviolent game. Tear and Nielsen (2014) effect size is the complex contrast between those participants who played a violent game vs. those who played a nonviolent game.

Table 4

Flexible analysis influences Bayes factors, too.

Quantification	$\hat{\delta}$	B_{01}	B_{02}	B_{03}
Mean volume	0.41	1-to-1.2	1-to-1.7	1-to-4.8
Mean volume after wins	0.26	1.6-to-1	1.5-to-1	1-to-1.6
Mean volume after losses	0.45	1-to-1.7	1-to-2.5	1-to-7.2
Mean duration	0.22	2.0-to-1	2.0-to-1	1-to-1
Mean duration after wins	0.10	2.6-to-1	3.4-to-1	2.7-to-1
Mean duration after losses	0.28	1.5-to-1	1.3-to-1	1-to-1.9
Mean volume \times duration	0.37	1.0-to-1	1-to-1.3	1-to-3.7
Mean volume \times sqrt(duration)	0.37	1.0-to-1	1-to-1.3	1-to-3.6
Mean volume \times ln(duration)	0.32	1.3-to-1	1-to-1	1-to-2.5
Count high volume settings	0.87	1-to-140	1-to-340	1-to-280
Count high duration settings	0.10	2.6-to-1	3.5-to-1	2.8-to-1
First-trial volume	0.06	2.7-to-1	3.9-to-1	3.5-to-1
First-trial duration	0.02	2.8-to-1	4.5-to-1	4.9-to-1
Count low volume settings	-0.72	1-to-19	1-to-39	1400-to-1

Bayes factors for each effect size as calculated by Elson et al. (2014, study 2, table 2). As pointed out by these authors, the various approaches to quantifying the results of the Competitive Reaction Time Task measure of aggression can lead to very different research conclusions. Bayes factors are not immune to problems of flexible analysis and reporting. *Note:* B_{01} = evidence for $H_0 : \delta = 0$ compared to $H_{A1} : \delta \sim \text{Cauchy}(0.4)$. B_{02} = evidence for $H_0 : \delta = 0$ compared to $H_{A2} : \delta \sim \text{Cauchy}^+(0.4)$. B_{03} = evidence for $H_0 : \delta = 0$ compared to $H_{A3} : \delta \sim \text{Normal}(\mu, \sigma)$, with μ and σ taken from Anderson et al. (2010). Bayes factors range from 1-to- ∞ (perfect evidence for alternative) to ∞ -to-1 (perfect evidence for null). All Bayes factors rounded to two significant digits.

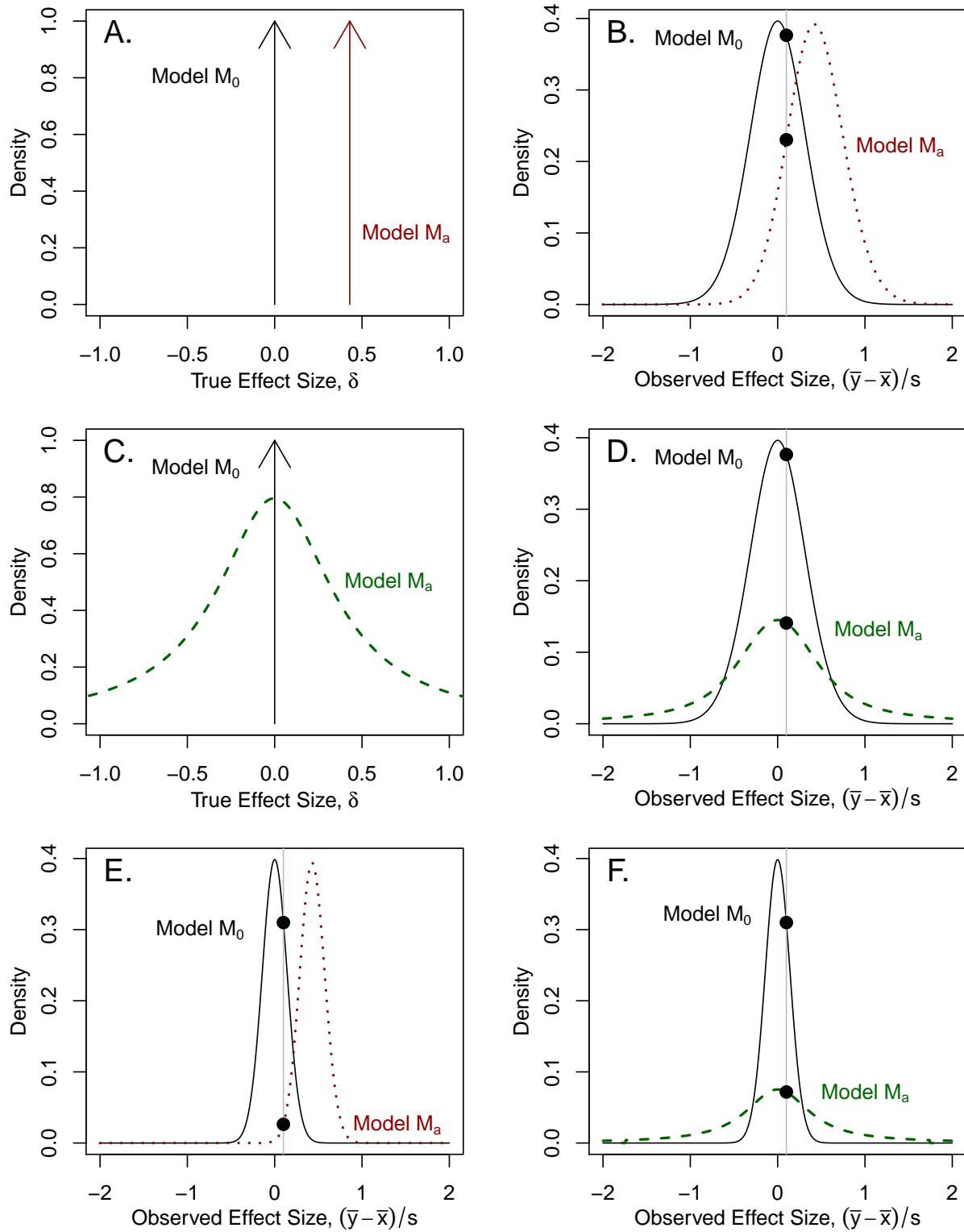


Figure 1. Bayesian model comparison. Panel A shows two point hypotheses $H_0 : \delta = 0$ and $H_1 : \delta = 0.43$. Panel B shows the probability of an observed effect size given these hypotheses and a sample of 40 observations between two cells. For an observed effect size $\hat{\delta} = 0.1$, indicated by the vertical grey line, the Bayes factor B_{01} is the ratio of the probabilities, $0.38/0.23 = 1.6$. Panel C shows a null hypothesis and a distributed alternative hypothesis $H_1 : \delta \sim \text{Cauchy}(0.4)$. Panel D shows the probabilities of the observed effect size given these hypotheses and a sample of 40 observations between two cells. Panels E and F recreate Panels C and D, respectively, with a larger sample of two hundred observations.

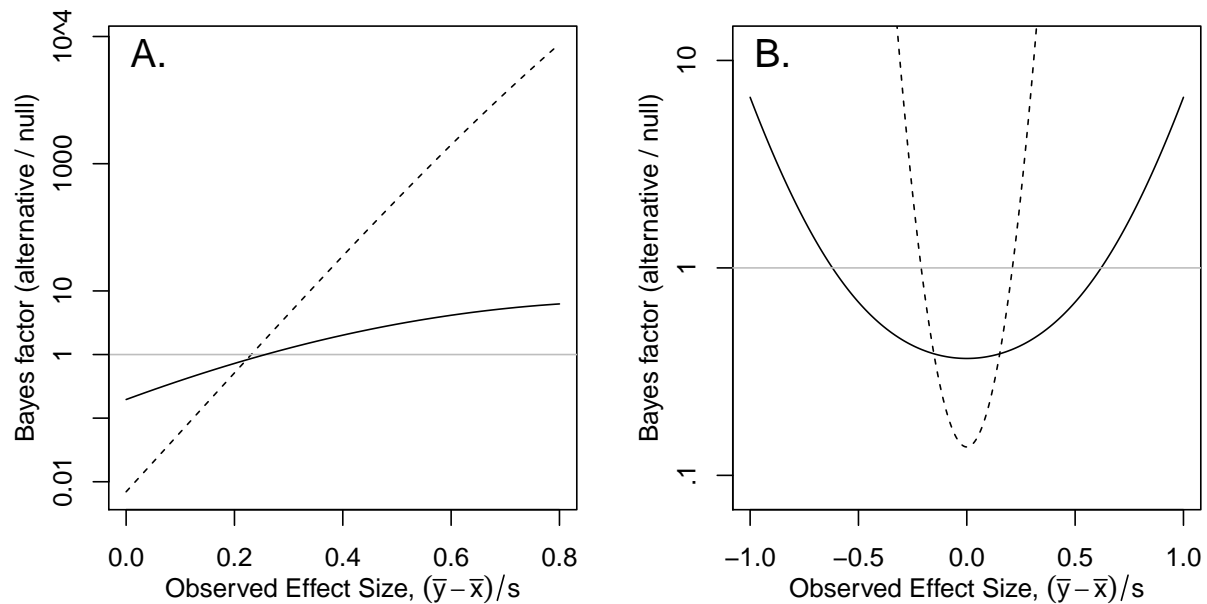


Figure 2. Bayes factors by effect size and sample size. Panel A shows the Bayes factor for the point-alternative hypothesis $H_1: \delta = 0.43$. Panel B shows the Bayes factor for the distributed alternative hypothesis $H_1: \delta \sim \text{Cauchy}(0.5)$. Solid lines indicate Bayes factors for a small sample of forty observations while dashed lines represent Bayes factors for a larger sample of four hundred observations.

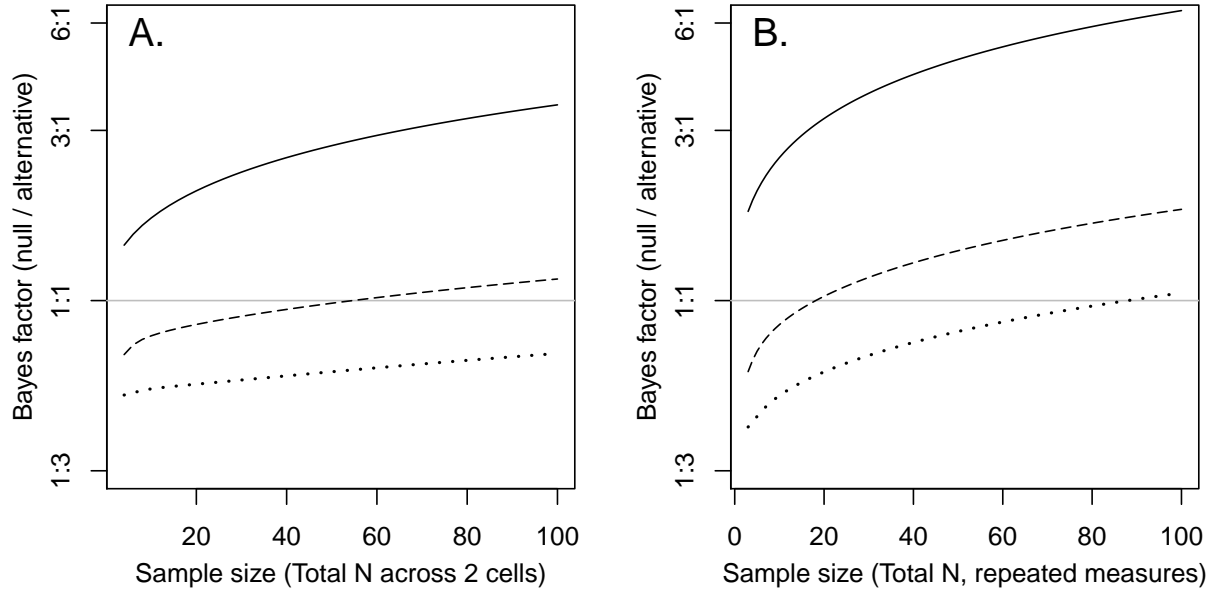


Figure 3. Bayes factors by study design and sample size in comparison of $H_0 : \delta = 0$ and $H_1 : \delta \sim \text{Cauchy}(0.5)$. Panel A shows the Bayes factor from an independent groups pilot test. Panel B shows the Bayes factor from a repeated-measures pilot test. Solid lines indicate the largest possible Bayes factor, which is obtained at $p = 1.0$. Dashed lines represent the Bayes factor for $p = .10$, and dotted lines represent the Bayes factor for the $p = .05$ threshold. Bayes factors above the grey axis indicate increasing evidence for the null. Even in the best possible result, larger samples are necessary to provide even 3:1 evidence in favor of the null, and small samples just missing statistical significance may represent slight evidence for the alternative over the null.