

# Secure Compilation

## Lecture 2

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## 1 Introduction

### 1.1 Source Language

#### 1.1.1 Types

We just have integers and functions in source language.

$$\sigma ::= \text{int} \mid \sigma_1 \rightarrow \sigma_2 ::=$$

#### 1.1.2 Terms

### 1.2 Target Language

## 2 Preservation Proof

**Theorem 2.1** (Type Preservation). *If  $\Gamma \vdash e_S : \sigma$  and  $\Gamma \vdash e_S : \alpha \rightsquigarrow e_T$  then  $\Gamma_S^+ \vdash e_T : \sigma^+$*

For correctness, we want to show  $e_S \approx e_T$ . This is not contextual equivalence because source language and target language are two different languages. There are many ways to prove compiler correction. We want to say that when:

$$e_S \approx e_T \text{ then } \sigma \approx \sigma^+$$

$$\begin{aligned} V \llbracket \sigma \rrbracket &= \{ (V_S, V_T) \mid j \cdot \vdash V_S : \sigma \wedge \cdot ; \cdot \vdash V_T : \sigma^+ \dots \} \\ V \llbracket \text{ints} \rrbracket &= \{ (n_S, n_T) \} \\ V \llbracket \sigma_1 \rightarrow \sigma_2 \rrbracket &= \{ (\lambda x : \sigma_1 \cdot e_S \text{ pack } (\tau_{env}, \langle \lambda (Z : \tau, x_T : \sigma_1^+) \cdot e_T, V_{env} \rangle)) \\ &\quad j \forall (v_S, v_T) \mathcal{E} V \llbracket \sigma_1 \rrbracket \cdot (e_S[v_s / x_s], e_T[v_{env} / z, v_T / x_T]) \in \mathcal{E} \llbracket \sigma_2 \rrbracket \} \end{aligned}$$

### **3 Logical Relations**

In logical relations we map related input to related outputs. Same source value and target value are related.