Homework 4

Theory Part

Q1 Consider a layer in CNN that takes in a single channel input of 64 × 64, and has 96 filters. In each of the following cases, compute the number of parameters that are learned in this layer. We assume that bias is present for each weight.

[1] A convolution layer with filters of same size as the input.

$$Param = (ksize^2 + 1)*channel$$

 $Param = (64^2 + 1)*96$
 $Param = 393312$

Out[1]: 393312

[2] A convolution layer with 8 × 8 filters with stride of 4

$$Param = (ksize)^2 * channel + bias$$
 $Param = (8^2 + 1) * 96$ $Param = 6240$

Out[2]: 6240

[3]. A convolution layer with 1 × 1 filter and a stride of 1

$$egin{aligned} Param &= (ksize)^2*channel + bias \ Param &= (1^2 + 1)*96 \ Param &= 192 \end{aligned}$$

Q2 Suppose you would have a neuron which has an RBF kernel as activation function (remember the evil wolf? Drop your linear style of thoughts. Circumferential thoughts can be nice too.)

$$y = exp(-(x_1^2 + x_2^2)) + b$$

with parameter b. What would be the shapes realized by the set of points $\{(x1,x2):y((x1,x2))=0\}$ as a function of b ? Explain in at most 2 sentences and/or a little math.

$$egin{aligned} 0 &= exp(-(x_1^2 + x_2^2)) + b \ -b &= exp(-(x_1^2 + x_2^2)) \ -ln(-b) &= x_1^2 + x_2^2 \end{aligned}$$

Therefore, it is a circle centered around the origin with radius $\sqrt{-ln(-b)}$. Obviously this is only valid when -1 < b < 0.

Supposed now we add weight,

$$y = exp(-(w_1x_1^2 + w_2x_2^2)) + b$$

what shapes can we realize now? Explain in at most 5 sentences and/or a little math. You can make references to publicly available in the internet materials to explain.

$$-ln(-b) = w_1x_1^2 + w_2x_2^2 \ -ln(-b) = rac{x_1^2}{w_1^{-1}} + rac{x_2^2}{w_2^{-1}} \ 1 = rac{x_1^2}{-ln(-b)\cdot w_1^{-1}} + rac{x_2^2}{-ln(-b)\cdot w_2^{-1}} \ 1 = \left(rac{x_1}{\sqrt{-ln(-b)\cdot w_1^{-1}}}
ight)^2 + \left(rac{x_2}{\sqrt{-ln(-b)\cdot w_2^{-1}}}
ight)^2$$

hence it is an ellipse, centered around the origin with radius $\sqrt{-ln(-b)\cdot w_1^{-1}}$ along the x_1 axis and radius $\sqrt{-ln(-b)\cdot w_2^{-1}}$ along the x_2 axis.

Q3 Suppose you have five linear neurons neurons n1, . . . , n5, realizing above decision boundaries as shown in Figure 1. That is: for every decision boundary we have outputs are = 0.5 in the zones marked with red plusses, and = 0.2 in the zones marked with the blue minuses.

igure1

As you know, each neuron is realized by:

$$n_i = 0.3 H(w_1^{(i)} x_1 + w_2^{(i)} x_2 + b^{(i)}) + 0.2, \quad H(z) \in 0, 1$$

where H is the threshold activation function. You want to predict positive values in a shape marked in green in Figure 1. You want to achieve this prediction by combining these neurons using a threshold neuron H:

$$y = H(\sum_i v_i^* n_i + b^*)$$

[1] _what do you have to do with the weights of n_5 so that you can move the decision boundary of n_5 so that you can realize the shape in green shown above (in the sense of having positive values inside and negative values outside.)? Give a qualitative description. Note: Give a qualitative description in 3 sentences at most. Note that there is an x- and an y-axis, which helps you to express vectors qualitatively._

The position of the decision boundary of n_5 depends on its weight and biases. Particularly, the ratio between w_1 and w_2 determines the slant of the boundary, while the ratio between the b and w_2 determines its offset from origin. As the desired position is a shift upwards (given that the boundary continues infinitely), we want to decrease b so that the boundaries shift upwards.

[2] _after moving the decision boundary of n5 appropriately, the green shape looks a bit like an logical AND-combination of the +-zones for every neuron. How to choose the weights v_i^* and the bias b^* in $y = H(\sum_i v_i^* n_i + b^*)$ so that you can realize the green shape (in the sense of having positive values inside and negative values outside that shape)? Note: n_i gives out values either 0.5 or 0.2_

Lets say that function H has a threshold h=0, such that

$$H(z) = 1[z > h] = 1[z > 0]$$

If we were to take green area as $\{+1\}$, for the threshold neuron to fire +1, we will need all neurons n_i to fire 0.5,

$$egin{aligned} 1 &= H(\sum_i 0.5 v_i^* + b^*) \ &= 1[(\sum_i 0.5 v_i^* + b^*) > 0] \ &(\sum_i 0.5 v_i^* + b^*) > 0 \quad -- \quad (1) \end{aligned}$$

If we were to take non-green area as $\{-1\}$, for the threshold neuron to fire -1, we will need at least one neuron n_j to fire 0.2,

$$egin{aligned} 0 &= H(\sum_{i=1} v_i^* n_i + v_j^* n_j + b^*) \ 0 &= H(\sum_{i=1} 0.5 v_i^* + 0.2 v_j^* + b^*) \ 0 &= 1[\sum_{i=1} 0.5 v_i^* + 0.2 v_j^* + b^* > 0] \ \sum_{i=1} 0.5 v_i^* + 0.2 v_j^* + b^* <= 0 \quad -- \quad (2) \end{aligned}$$

For simplicity, we set $v_i^* = 1$ for all i. Finding b,

$$0.5 \cdot 5 + b^* > 0 \quad -- \quad (1)$$
 $2.5 + b^* > 0$ $b^* > -2.5$ $0.5 \cdot 4 + 0.2 + b^* <= 0 \quad -- \quad (2)$ $2.2 + b^* <= 0$ $b^* <= -2.2$ $therefore \quad -2.5 < b <= -2.2$

we can pick any b within this range, e.g. b=-2.4 with our $v_i^st=1$, such that

$$H(\sum_i 0.5 - 2.4) = H(2.5 - 2.4) \quad \textit{for all } n_i = 0.5$$

$$= H(0.1) = 1[0.1 > 0] = 1 \quad \textit{(green)}$$

$$H(\sum_{i-1} 0.5 + 0.2 - 2.4) = H(2.2 - 2.4) \quad \textit{for four } n_i = 0.5 \textit{ and one } n_j = 0.2$$

$$= H(-0.2) = 1[-0.2 > 0] = 0 \quad \textit{(outside)}$$

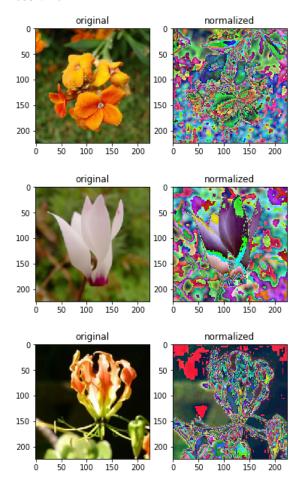
Coding - Part 1

For this section, there is a script called hw4_code.py that will hold some definitions e.g. the FlowerDataset class and train_model function.

Below we will do some sanity check on the dataset.

```
In [7]: from hw4_code import *
        import matplotlib.pyplot as plt
        %matplotlib inline
        from torchvision import transforms
        # testing dataset
        flower_dataset = FlowerDataset('..\\datasets\\flowersstuff\\102flowers\\flowers_data', mode='train')
        flower_dataset_val = FlowerDataset('...\\datasets\\flowersstuff\\102flowers\\flowers_data', mode='val')
        for i in range(3):
            flower1 = flower_dataset[i]
            print('label:',flower1['label'])
            image = transforms.ToPILImage()(flower1['image'])
            invTrans = transforms.Compose([ transforms.Normalize(mean = [ 0., 0., 0. ],
                                                                  std = [1/0.229, 1/0.224, 1/0.225]),
                                             transforms.Normalize(mean = [ -0.485, -0.456, -0.406 ],
                                                                  std = [ 1., 1., 1. ]),
                                            transforms.ToPILImage(),
            clear_image = invTrans(flower1['image'])
            plt.figure()
            plt.subplot(121)
            plt.imshow(clear_image)
            plt.title('original')
            plt.subplot(122)
            plt.imshow(image)
            plt.title('normalized')
```

label: 45
label: 87
label: 20



```
In [8]: # Getting pretrained resnet
from torchvision import models

def get_pretrained_resnet(use_gpu=True):
    model = models.resnet18(pretrained=True)
    if use_gpu:
        model = model.cuda(0)
        return model

resnetmodel = get_pretrained_resnet()
resnet_dict = resnetmodel.state_dict()
```

With learning rate 0.1,

Studio 1 - French O	
[train] - Epoch 0 >> Epoch loss 1.84182 accuracy 0.034	in 442.9377s
<pre>[train] - Epoch 1</pre>	in 448.1263s
<pre>[train] - Epoch 2</pre>	in 434.1745s
[train] - Epoch 3 >> Epoch loss 0.63054 accuracy 0.498	in 434.5283s
[train] - Epoch 4	
>> Epoch loss 0.48427 accuracy 0.627 [val] - Epoch 0	in 435.3186s
>> Epoch loss 0.50609 accuracy 0.561 [val] - Epoch 1	in 28.6890s
>> Epoch loss 0.50609 accuracy 0.561 [val] - Epoch 2	in 29.2429s
>> Epoch loss 0.50609 accuracy 0.561 [val] - Epoch 3	in 28.0560s
>> Epoch loss 0.50609 accuracy 0.561	in 27.9266s
<pre>[val] - Epoch 4</pre>	in 28.2003s
With learning rate 1,	
<pre>[train] - Epoch 0</pre>	in 435.5767s
[train] - Epoch 1 >> Epoch loss 0.06936 accuracy 0.977	in 438.4414s
[train] - Epoch 2	
>> Epoch loss 0.02621 accuracy 0.999 [train] - Epoch 3	in 434.8344s
>> Epoch loss 0.01594 accuracy 1.000 [train] - Epoch 4	in 432.8960s
>> Epoch loss 0.01160 accuracy 1.000 [val] - Epoch 0	in 435.0222s
>> Epoch loss 0.11504 accuracy 0.879 [val] - Epoch 1	in 27.7213s
>> Epoch loss 0.11504 accuracy 0.879	in 27.9815s
<pre>[val] - Epoch 2</pre>	in 27.9220s
<pre>[val] - Epoch 3</pre>	in 27.9824s
<pre>[val] - Epoch 4</pre>	in 28.0526s
With learning rate 10,	
[train] - Epoch 0	÷= 425 1002-
<pre>>> Epoch loss 0.14960 accuracy 0.876 [train] - Epoch 1</pre>	in 435.1083s
>> Epoch loss 0.28600 accuracy 0.707 [train] - Epoch 2	in 435.4502s
>> Epoch loss 0.04029 accuracy 0.961 [train] - Epoch 3	in 438.7462s
>> Epoch loss 0.00938 accuracy 0.994 [train] - Epoch 4	in 440.7829s
>> Epoch loss 0.00379 accuracy 0.998	in 437.6852s
[val] - Epoch 0 >> Epoch loss 0.04910 accuracy 0.945	in 27.5148s
<pre>[val] - Epoch 1</pre>	in 27.5783s
<pre>[val] - Epoch 2</pre>	in 27.5548s
<pre>[val] - Epoch 3</pre>	in 27.5676s
[val] - Epoch 4 >> Epoch loss 0.04910 accuracy 0.945	in 27.4915s
// Lpocii 1033 0.04310 accuracy 0.343	111 2/.43135

```
In [11]: # now lets do the same thing, but train with an empty resnet
         def get_empty_resnet(use_gpu=True):
             model = models.resnet18(pretrained=False)
             if use gpu:
                 model = model.cuda(0)
             return model
         emptymodel = get_pretrained_resnet()
         empty_dict = resnetmodel.state_dict()
In [13]: # training with various learn rate
         for lr in [0.1, 1, 10]:
             print("\n\n\) learning rate {},\n".format(lr))
             learnrate = lr
             optimizer = optim.SGD(emptymodel.parameters(), lr=learnrate, momentum=0.9)
             trainedmodel = train_model(flower_dataset, emptymodel, optimizer,
                                        epoch=5, mode='train', use_gpu=True, print_every=1)
             trainedmodel = train_model(flower_dataset_val, trainedmodel, optimizer,
                                        epoch=1, mode='val', use_gpu=True, print_every=1)
         With learning rate 0.1,
         [train] - Epoch 0..
                                                                         in 442.9514s
               >> Epoch loss 0.82801 accuracy 0.366
         [train] - Epoch 1..
                                                                         in 445.8555s
               >> Epoch loss 0.61871 accuracy 0.508
         [train] - Epoch 2..
               >> Epoch loss 0.47620 accuracy 0.635
                                                                         in 433.9480s
         [train] - Epoch 3..
               >> Epoch loss 0.37526 accuracy 0.734
                                                                         in 435.6844s
         [train] - Epoch 4..
                                                                         in 436.9786s
               >> Epoch loss 0.30134 accuracy 0.807
         [val] - Epoch 0..
               >> Epoch loss 0.37327 accuracy 0.649
                                                                         in 28.3487s
         With learning rate 1,
         [train] - Epoch 0..
               >> Epoch loss 0.23467 accuracy 0.837
                                                                         in 437.0729s
         [train] - Epoch 1..
               >> Epoch loss 0.05134 accuracy 0.989
                                                                         in 435.1459s
         [train] - Epoch 2..
               >> Epoch loss 0.02194 accuracy 1.000
                                                                         in 437.3835s
         [train] - Epoch 3..
               >> Epoch loss 0.01423 accuracy 1.000
                                                                         in 433.7015s
         [train] - Epoch 4..
               >> Epoch loss 0.01061 accuracy 1.000
                                                                         in 433.5076s
         [val] - Epoch 0..
               >> Epoch loss 0.12527 accuracy 0.875
                                                                         in 27.4427s
         With learning rate 10,
         [train] - Epoch 0..
               >> Epoch loss 0.08040 accuracy 0.939
                                                                         in 435.1173s
         [train] - Epoch 1..
               >> Epoch loss 0.35823 accuracy 0.642
                                                                         in 438.3859s
         [train] - Epoch 2..
               >> Epoch loss 0.05526 accuracy 0.942
                                                                         in 435.5303s
         [train] - Epoch 3...
```

in 436.0038s

in 436.5753s

in 27.9151s

>> Epoch loss 0.01359 accuracy 0.988

>> Epoch loss 0.00421 accuracy 0.998

>> Epoch loss 0.05358 accuracy 0.944

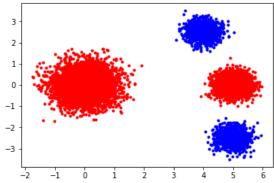
[train] - Epoch 4..

[val] - Epoch 0..

```
In [16]: # now lets do the same thing, but train with an unfrozen resnet
         import torch.nn as nn
         def get_unfrozen_resnet(numcl, use_gpu=True):
             model = models.resnet18(pretrained=False)
             num_ftrs = model.fc.in_features
             model.fc = nn.Linear(num_ftrs, numcl)
             if use_gpu:
                 model = model.cuda(0)
             return model
         unfrozenmodel = get_pretrained_resnet()
         unfrozen_dict = resnetmodel.state_dict()
In [17]: # training with various learn rate
         for lr in [0.1, 1, 10]:
             print("\n\nWith learning rate {},\n".format(lr))
             learnrate = lr
             optimizer = optim.SGD(unfrozenmodel.parameters(), lr=learnrate, momentum=0.9)
             trainedmodel = train_model(flower_dataset, unfrozenmodel, optimizer,
                                        epoch=5, mode='train', use_gpu=True, print_every=1)
             trainedmodel = train_model(flower_dataset_val, trainedmodel, optimizer,
                                        epoch=1, mode='val', use_gpu=True, print_every=1)
         With learning rate 0.1,
         [train] - Epoch 0..
               >> Epoch loss 1.84156 accuracy 0.033
                                                                        in 436.6851s
         [train] - Epoch 1..
                                                                         in 438.1763s
               >> Epoch loss 1.19135 accuracy 0.194
         [train] - Epoch 2..
               >> Epoch loss 0.84679 accuracy 0.352
                                                                         in 439.2018s
         [train] - Epoch 3..
               >> Epoch loss 0.63122 accuracy 0.499
                                                                         in 439.1671s
         [train] - Epoch 4..
               >> Epoch loss 0.48525 accuracy 0.624
                                                                         in 438.4431s
         [val] - Epoch 0..
                                                                         in 28.5880s
               >> Epoch loss 0.50701 accuracy 0.557
         With learning rate 1,
         [train] - Epoch 0..
               >> Epoch loss 0.32747 accuracy 0.740
                                                                         in 438.2457s
         [train] - Epoch 1..
                                                                         in 437.4092s
               >> Epoch loss 0.06945 accuracy 0.977
         [train] - Epoch 2..
               >> Epoch loss 0.02642 accuracy 0.999
                                                                         in 435.1354s
         [train] - Epoch 3..
               >> Epoch loss 0.01607 accuracy 1.000
                                                                         in 436.9965s
         [train] - Epoch 4..
               >> Epoch loss 0.01164 accuracy 1.000
                                                                         in 437.0905s
         [val] - Epoch 0..
               >> Epoch loss 0.11233 accuracy 0.877
                                                                         in 27.9271s
         With learning rate 10,
         [train] - Epoch 0..
               >> Epoch loss 0.21452 accuracy 0.814
                                                                         in 437.2194s
         [train] - Epoch 1..
               >> Epoch loss 0.25315 accuracy 0.732
                                                                         in 436.8206s
         [train] - Epoch 2..
                                                                         in 436.9103s
               >> Epoch loss 0.03555 accuracy 0.967
         [train] - Epoch 3..
               >> Epoch loss 0.00800 accuracy 0.996
                                                                         in 435.5079s
         [train] - Epoch 4..
               >> Epoch loss 0.00257 accuracy 0.999
                                                                         in 435.8060s
         [val] - Epoch 0..
                                                                         in 28.1246s
               >> Epoch loss 0.05316 accuracy 0.948
```

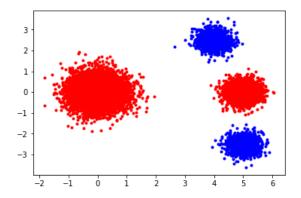
Coding Part 2

```
from hw4 code2 import *
In [101]:
         import numpy as np
         def plot_dataset(data, label):
             true_mask = label.reshape((-1)).astype(bool)
             false_mask = (1-label).reshape((-1)).astype(bool)
             data_true = np.transpose(data[true_mask])
             data_false = np.transpose(data[false_mask])
             plt.figure()
             plt.plot(data_true[0], data_true[1], '.b')
             plt.plot(data_false[0], data_false[1], '.r')
In [102]:
         print("from samplestr.txt:")
         data_tr, label_tr = from_text('samplestr.txt')
         plot_dataset(data_tr, label_tr)
         from samplestr.txt:
         samples with positive class: 2000
         samples with negative class: 8000
           3
           2
```



```
In [103]: print("from sampleste.txt:")
          data_te, label_te = from_text('sampleste.txt')
          plot_dataset(data_te, label_te)
```

from sampleste.txt: samples with positive class: 2000 samples with negative class: 8000



```
In [104]:
         Creating a new Neural Network
         from torch import nn
         import torch.nn.functional as F
         class OurNet(nn.Module):
            def __init__(self):
               super(OurNet, self).__init__()
               self.fc = nn.Linear(2, 1)
            def forward(self, x):
               x = F.relu(self.fc(x))
               \textbf{return} \ x
         our_net = OurNet()
         print(our_net)
         OurNet(
          (fc): Linear(in_features=2, out_features=1, bias=True)
In [105]: # testing the Dataset subclass from hw4_code2
         train_set = ImbaDataset('.', mode='train')
         print('train:',train_set[2])
         test_set = ImbaDataset('.', mode='test')
         print('test:', test_set[2])
```

```
In [106]: # simple training
          import torch
          from torch.utils.data import DataLoader
          import torch.optim as optim
          from torch.autograd import Variable
          from torch.utils.data.sampler import WeightedRandomSampler
          our_net = OurNet().double()
          optimizer = optim.SGD(our_net.parameters(), lr=0.1)
          criterion = nn.BCEWithLogitsLoss()
          def train_ournet(dataset, model, optimizer, criterion, batch_sampler=None,
                           mode='train', balanced_acc=True):
              print_truecount = False#True
              if batch_sampler:
                  loader = DataLoader(dataset, batch_sampler=batch_sampler)
              else:
                  loader = DataLoader(dataset, batch_size=128)
              running_loss = 0
              running_corrects = 0
              total_data = 0
              # for balanced sampling
              true_pos = 0
              true_neg = 0
              total_positive = 0
              total_negative = 0
              if mode == 'train':
                  model.train()
              else:
                  model.eval()
              for inputdata in loader:
                  data = Variable(inputdata['data'])
                  labels = Variable(inputdata['label']).view(-1,1)
                  if print_truecount:
                       print('First batch true count:', labels.sum().item(), 'out of', len(labels),
                              '({}%)".format(labels.sum().item() * 100 / len(labels)))
                       print truecount = False
                  outputs = model.forward(data)
                  predictions = (outputs > 0)
                  # balanced stuff
                  true_pos += (predictions.double() * labels.double()).sum().item()
                  true_neg += ((1-predictions).double() * (1-labels).double()).sum().item()
                  total_positive += labels.sum().item()
                  total_negative += (1-labels).sum().item()
                  loss = criterion(outputs, labels)
                  if mode == 'train':
                      loss.backward()
                       optimizer.step()
                  # balanced stuff
                    total_data += (labels * (positive_weight-1) + 1).sum().item()
                  total data += len(labels)
                  corrects = (predictions.double().cpu() == labels.cpu()).double()
                    weights = (positive_weight - 1) * labels.cpu() + 1
                  running_corrects += (corrects).sum().item()
                  running_loss += loss.item()
                print("total data:", total_data)
              running_corrects /= (total_data)#float(128*100)
              if mode == 'train':
                  print("Trained with accuracy {} and loss {}".format(running_corrects, running_loss))
              elif mode == 'test':
                  print("Tested with accuracy {} and loss {}".format(running_corrects, running_loss))
              if balanced_acc:
                  true_pos_rate = true_pos/total_positive
                  true_neg_rate = true_neg/(total_negative)
                  b_acc = (true_pos_rate + true_neg_rate) / 2
```

```
True Positive Rate:", true_pos_rate)
True Negative Rate:", true_neg_rate)
                   print("
                   print("
                             Balanced Accuracy:", b_acc)
                   print('----')
               return model
In [107]: our_net = OurNet().double()
           our_net_trained = train_ournet(train_set, our_net, optimizer, criterion)
           our_net_trained = train_ournet(train_set, our_net_trained, optimizer, criterion, mode='test')
           our_net_trained = train_ournet(test_set, our_net_trained, optimizer, criterion, mode='test')
           print(our_net_trained.state_dict())
           Trained with accuracy 0.6371 and loss 65.16015314912875
              True Positive Rate: 1.0
              True Negative Rate: 0.546375
              Balanced Accuracy: 0.7731875
           Tested with accuracy 0.6371 and loss 65.16015314912875
              True Positive Rate: 1.0
              True Negative Rate: 0.546375
              Balanced Accuracy: 0.7731875
           Tested with accuracy 0.6395 and loss 65.14335670596058
              True Positive Rate: 1.0
              True Negative Rate: 0.549375
              Balanced Accuracy: 0.7746875
           OrderedDict([('fc.weight', tensor([[ 0.2524, 0.1391]], dtype=torch.float64)), ('fc.bias', tensor([-0.1658],
           dtype=torch.float64))])
In [108]: | w = our_net_trained.state_dict()['fc.weight']
           b = our_net_trained.state_dict()['fc.bias']
           w1 = w[0,0].item()
           w2 = w[0,1].item()
           b1 = b[0].item()
           m = -w1/w2
           c = -b/w2
           line_x = [ i/100 \text{ for i in } range(-300, 700)]
           line_y = [ m*i + c for i in line_x]
           plot_dataset(data_tr, label_tr)
           plt.plot(line_x, line_y, '.c')
           samples with positive class: 2000
           samples with negative class: 8000
Out[108]: [<matplotlib.lines.Line2D at 0x203efea45c0>]
              7.5
              5.0
              2.5
              0.0
             -2.5
             -5.0
```

To achieve 50-50 on minibatches, we need a Sampler subclass.

-2

-7.5 -10.0 print("

print('

print("

True Positive:", true_pos) True Negative:", true_neg)

```
In [109]: class OurBatchSampler(object):
               Special batch sampler class that ensures a 50-50
               dataset classes.
              def __init__(self, dataset, batch_size, iteration, random=False):
                  self.dataset = dataset
                  self.batch_size = batch_size
                  self.iteration = iteration
                  self.random = random
                  self.idx plus = [idx for idx in range(len(dataset)) if dataset[idx]['label'].item() > 0]
                  self.idx_minus = [idx for idx in range(len(dataset)) if idx not in self.idx_plus]
              def __iter__(self):
                  batch = []
                  for i in range(self.iteration):
                       if self.random:
                           idplus = np.random.choice(self.idx_plus, self.batch_size // 2).tolist()
                           idminus = np.random.choice(self.idx_minus, self.batch_size // 2).tolist()
                       else:
                           idplus = [self.get_positive_det() for i in range(self.batch_size // 2)]
                           idminus = [self.get_negative_det() for i in range(self.batch_size // 2)]
                       batch += idplus + idminus
                       yield batch
                       batch = []
              def get_positive_det(self):
                  idx = self.idx_plus[0]
                  self.idx_plus = self.idx_plus[1:] + [idx]
                  \textbf{return} \text{ idx}
              def get_negative_det(self):
                  idx = self.idx_minus[0]
                  self.idx_minus = self.idx_minus[1:] + [idx]
                  return idx
              def len (self):
                  return self.batch_size * self.iteration
          train_sampler = OurBatchSampler(train_set, 128, 100)
          print('train sampler built')
          test_sampler = OurBatchSampler(test_set, 128, 100)
          print('test sampler built')
```

train sampler built test sampler built

```
In [110]:
          our_net = OurNet().double()
          print('\nWithout 50-50 sampling:')
          our_net_trained = train_ournet(train_set, our_net, optimizer, criterion)
          # print('Train: accuracy')
          # our_net_trained = train_ournet(train_set, our_net_trained, optimizer,
                                            criterion, mode='test')
          print('Test: accuracy')
          our_net_trained = train_ournet(test_set, our_net_trained, optimizer,
                                          criterion, mode='test')
          our_net = OurNet().double()
          print('\n\n\n')
          print('With 50-50 sampling:')
          our_net_trained = train_ournet(train_set, our_net, optimizer, criterion,
                                          batch_sampler=train_sampler)
          # print('Train: accuracy')
          # our_net_trained = train_ournet(train_set, our_net_trained, optimizer,
                                            criterion, mode='test')
          print('Test: accuracy')
          our_net_trained = train_ournet(test_set, our_net_trained, optimizer,
                                          criterion, mode='test')
          # print(our_net_trained.state_dict())
          Without 50-50 sampling:
          Trained with accuracy 0.6981 and loss 55.94245333436154
             True Positive Rate: 0.0
             True Negative Rate: 0.872625
             Balanced Accuracy: 0.4363125
          Test: accuracy
          Tested with accuracy 0.6986 and loss 55.89674747519486
             True Positive Rate: 0.0
             True Negative Rate: 0.87325
             Balanced Accuracy: 0.436625
          With 50-50 sampling:
          Trained with accuracy 0.47140625 and loss 62.13626624408322
             True Positive Rate: 0.46875
             True Negative Rate: 0.4740625
```

Balanced Accuracy: 0.47140625

True Positive Rate: 0.5
True Negative Rate: 0.49425

Tested with accuracy 0.4954 and loss 54.08188945714033

Balanced Accuracy: 0.49712500000000004

Test: accuracy

```
In [111]: w = our_net_trained.state_dict()['fc.weight']
b = our_net_trained.state_dict()['fc.bias']
w1 = w[0,0].item()
w2 = w[0,1].item()
b1 = b[0].item()

m = -w1/w2
c = -b/w2

line_x = [ i/100 for i in range(-300, 700)]
line_y = [ m*i + c for i in line_x]

plot_dataset(data_tr, label_tr)
plt.plot(line_x, line_y, '.c')
```

samples with positive class: 2000
samples with negative class: 8000

Out[111]: [<matplotlib.lines.Line2D at 0x203efe9dc18>]

